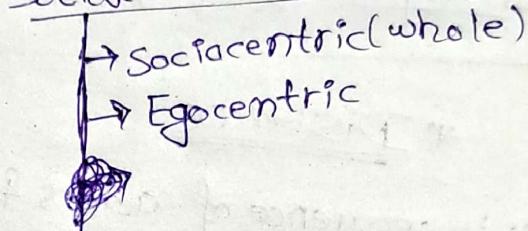


Social Network

- A social network is social structure of people, related to each other through a common relation or interest.
- SNA is study of social networks to understand their structure & behaviour.

People - nodes
relations - edges

Social Network Analysis

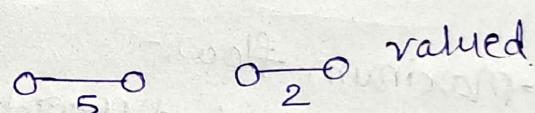
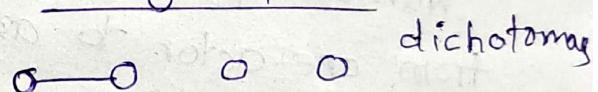


Types of social relations

- friendship
- acquaintance
- kinship
- advice
- hindrance
- sex.

class code :-

Strength of Tie



3 c + fmde

o actor

o o dyad.



triad.

friendship

Kinship

Relations.

o o adjacent node to

o ← o incident node to

o ← o

o → o
o → o

o ← + o

3 isomorphism classes

cont.

- null dyad.
- mutual dyad.
- asymmetric

converse of graph:
Reverse direction of all arcs.

Density :- Number of ties that are present
amount of ties that can be present

out-degree :- sum of connections from an actor to others.

In-degree :- sum of connections to an actor.

* Distance

- walk :- sequence of actors & relations that begins & ends with actors.

- Geodesic distance:- Number of relationships in the shortest possible walk from one actor to another.

- maximum flow:- amount of different actors in neighbourhood of a source that lead to pathways to Target.

• Degree:- sum of connections from or to an actor.

• closeness centrality:-
- Dist. of one actor to all others.

• Between centrality:-
no. that represents how frequently an actor is between other actors geodesic path.

centrality Measures :-

Who is the most prominent?

Who knows the most actors?

* Who controls knowledge flow?

* Who has shortest distance?

closeness

Who has more power?

Between.

Degree



What are LinkedIn connections?

1st - directly connected

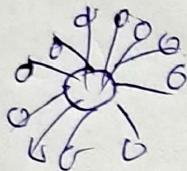
2nd - people connected to 1st degree

3rd - people connected to 2nd degree.

Why 6 degrees of separation?

6 degrees of
Freedom.
separation

Each friend connected to 44 people



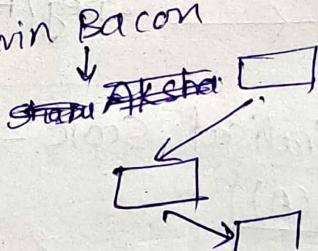
$$(44)^6 \approx 7.26 \text{ Billion people}$$

small world theorem.

You can get job connections easily through random acquaintances than through your close friends! - Veritasium.

strength of weak Tie

The oral of Bacon! \rightarrow Kevin Bacon



Bacon 13.

Erdős Number project

• Adjacency matrix
Lone mode

• Affiliation matrix
Two mode.

Adjacency matrix vs Attribute Matrix

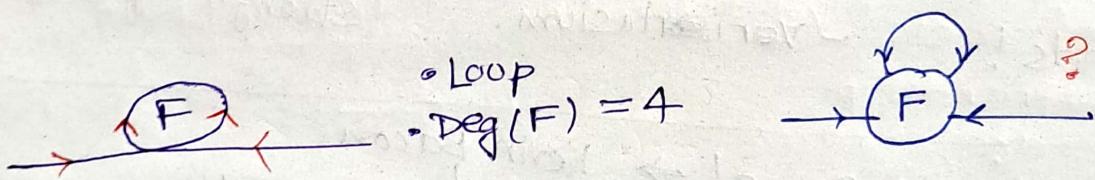
order :- no. of nodes in graph.

cardinality :- no. of edges.
size :- max. no. of edges , ie $\frac{n(n-1)}{2}$ for undirected.
 $n(n-1)$ for directed.

degree centrality

for directed node \rightarrow in-degree
 \rightarrow out-degree.

Average degree $\Rightarrow \frac{\text{Deg}(A) + \text{Deg}(B) + \dots + \text{Deg}(N)}{n}$



Degree centralised score = $\frac{\text{Deg}(A)}{\max(\text{Deg of all other nodes})}$

$$= \frac{\text{Deg}(A)}{n-1}$$

standardised score or normalised form.

closeness centrality:- $\Rightarrow \arg \left(\min \left(\text{dist with all nodes} \right) \right)$

\Rightarrow inverse of sum of distance between a node & other nodes in a network.

closeness score $\Rightarrow \frac{1}{\text{total dist}}$

Standardised score $\Rightarrow \frac{1}{\text{total dist}} \times (n-1)$

most closest node \Rightarrow highest standardised score

Betweenness centrality :-

$$g(v) = \sum_{s \neq v \neq t} \frac{\sigma_{st}(v)}{\sigma_{st}}$$

$$\text{normal}(g(v)) = \frac{g(v) - \min(g)}{\max(g) - \min(g)}$$

which results in $\max \text{normal} \Rightarrow 1$

σ_{st} is total no. of shortest path from $s \rightarrow t$.
 $\sigma_{st}(v)$ is no. of paths passing through v . (v is not s or t).

~~This is not~~

For friendship network, which is most popular person?

Q] For friendship network, which is most popular person?
degree centrality (but there is never fixed answer)

ans:-

Q] Find section in an information flow network that can most efficiently ~~info~~ info flow info?

ans:- closeness centrality.

Q] Which section controls, information flow?

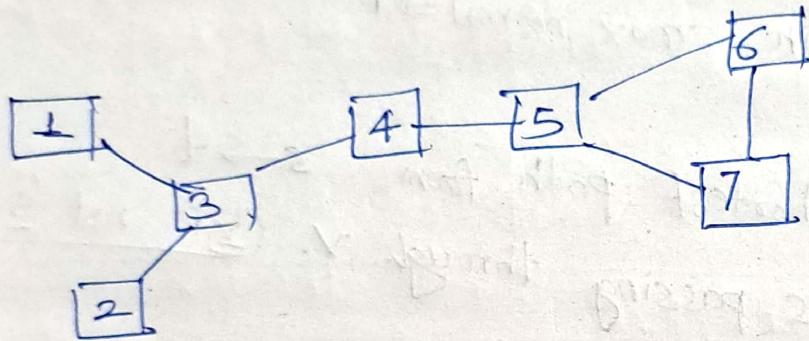
ans:- betweenness centrality

THANK YOU!

- * do all maths yourself.
- * GEPHI network Lab practical.
- * Install NetworkX.
- * Next to Next class :- Quiz.

Data Management :-

- Adjacency Matrix.
 - Asymmetric, binary
 - Asymmetric weighted.
- Affiliation Matrix.



consider only paths involving 4 in them.
As they will have contribution in betweenness.

$$(1-3) \times$$

$$(1-5) \checkmark$$

$$1-3-4-5$$

Node 3

1-2	1
1-4	1
1-5	1
1-6	1
1-7	1

for directed divide by
 $(n-1)(n-2)$

for undirected divide by

$$\frac{(n-1)(n-2)}{2} = \frac{(7-1)(7-2)}{2} = 15$$

2-4	1
2-5	1
2-6	1
2-7	1

9

Hence: - $\frac{9}{15}$ (Here undirected).

Node 5

1-6	1
1-7	1
2-6	1
2-7	1
3-6	1
3-7	1
4-6	1
4-7	1
6-7	0
$\boxed{\frac{8}{15}}$	

node	score
1	0
2	0
3	$\frac{9}{15}$
4	$\frac{9}{15}$
5	$\frac{8}{15}$
6	0
7	0

Another formula

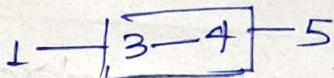
$$\text{between}(S|t) = \frac{\text{no. of paths}}{\text{no. of nodes.}}$$

ex) $(1,5) \Rightarrow \frac{1}{2}$
 between.

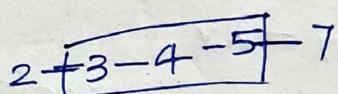
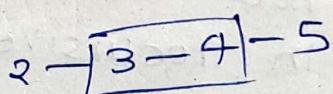
$$(3-5) \Rightarrow \frac{1}{1}$$

$$(2-5) \Rightarrow \frac{1}{2}$$

$$(2-7) \Rightarrow \frac{1}{3}$$



3-4-5.



Graph Measures :-

Eccentricity ($\epsilon(v)$)

$\epsilon(v)$ of vertex 'v' in connected graph G is max. graph distance between 'v' and any other vertex u of G .

$$\epsilon(v) = \max_{u \in V} d(u, v)$$

For disconnected point $\epsilon(v) = \infty$.

• Diameter :- max eccentricity

• Radius :- min eccentricity

• Central Point :- $\epsilon(v) = \text{Radius}$

Eigenvector centrality (You are powerful if friends are powerful)

Influence of node in network:-

Importance of node depends on, importance of its neighbours in recursive manner.

$$Av = \lambda v$$

Select an eigen vector associated with largest eigen value

Eigen Vector

$$A - \lambda I | I | = 0$$

- A is some matrix.
- size of matrix, tells no. of Eigen values

e.g. 3×3 , then 3 eigen values

Greatest Eigen value is Eigenvector centrality

~~compute~~ A is adjacency matrix here.

Katz centrality

- almost same as Eigen vector centrality.
- quality (who) and quantity (how many) matters
- Also considers Attenuation in influence.

Bonacich centrality

Two parametric centrality measure $c(\alpha, \beta)$.

α is normalisation factor

β can be +ve or -ve.

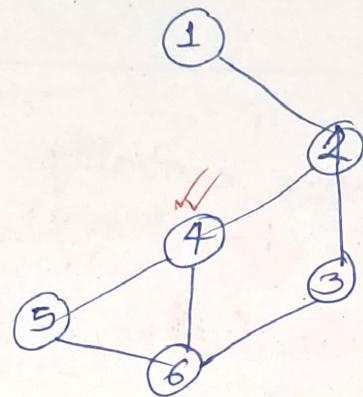
connected to powerful $\xrightarrow{\text{connected to weak node.}}$

Eigen vector centrality works well for strongly connected network.
but not for weakly connected network.

Eigenvector Centrality Example 1 - Exam Question

Solve $A - \lambda I$.

$$v = \begin{bmatrix} 0.31 \\ 0.79 \\ 0.69 \\ 1.00 \\ 0.78 \\ 0.97 \end{bmatrix}$$



$$\lambda = 2, 1, 2.54, 1.5$$

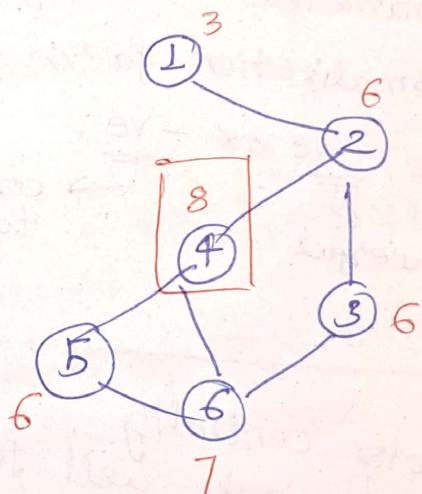
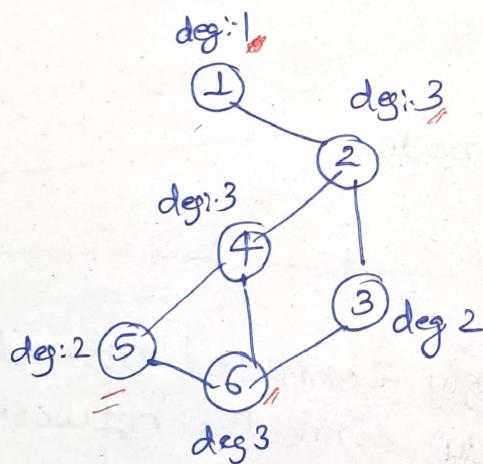
max.

$$Av = 2.54 v$$

choose eigen vector v , with highest eigen value.

(use: Matrixcalc.org
Matrix calculator)

Trick: add degree of your friends.



new power = sum of power of neighbours

Intuitive Approach (Power iteration method)

net power \leftarrow sum of power of neighbours

	0	1	2	3	4	5	6
1	0.31	0.79	0.69	1.00	0.78	0.97	
2	1.00	0.79	0.69	0.32	0.73	0.71	0.90
3	0.79	0.69	0.32	0.73	0.71	1.00	0.90
4	0.69	0.32	0.73	0.71	1.00	0.75	0.90
5	1.00	0.71	1.00	0.75	0.90		
6	0.78	0.90	0.90	0.90	0.90		
						similar as eigen vector	

$$v = \begin{bmatrix} 0.31 \\ 0.79 \\ 0.69 \\ 1.00 \\ 0.78 \\ 0.97 \end{bmatrix}$$

why stop at round 4? (no ~~centered~~ search at Home).
 because at round 5, ~~maybe~~ instead of node 4,
 node 6 will

	5
1	38
2	106
3	85
4	124
5	99
6	128

Stop?

$$X_t = A^T X_{t-1}$$

Stop when new-old < threshold.
 or do this until highest eigen value.

Why iterations?
 because w.r.t time, friends and connections will change

Lets check

	0	1	2	3	4
1	1	0.33	0.375	0.3	0.28
2	1	1	0.75	0.85	0.73
3	1	0.66	0.75	0.65	0.71
4	1	1	1	0.95	1
5	1	0.66	0.75	0.25	0.75
6	1	1	0.875	1	0.90

reaching eigen
value.

stopping criteria

$$1) L_2 \text{ norm } \sqrt{\sum x^2}$$

$$(t_t - t_{t-1}) \leq \delta$$

2) Fluctuation / oscillation.

$$3) |X_t - X_{t-1}| < \delta$$

4) Rayleigh Quotient

H.W

Read Tutorial on PCA by Li Smith.

$$\text{cov}(x, x) = \text{var}(x).$$

$$\text{cov}(x, y) = \text{cov}(y, x)$$

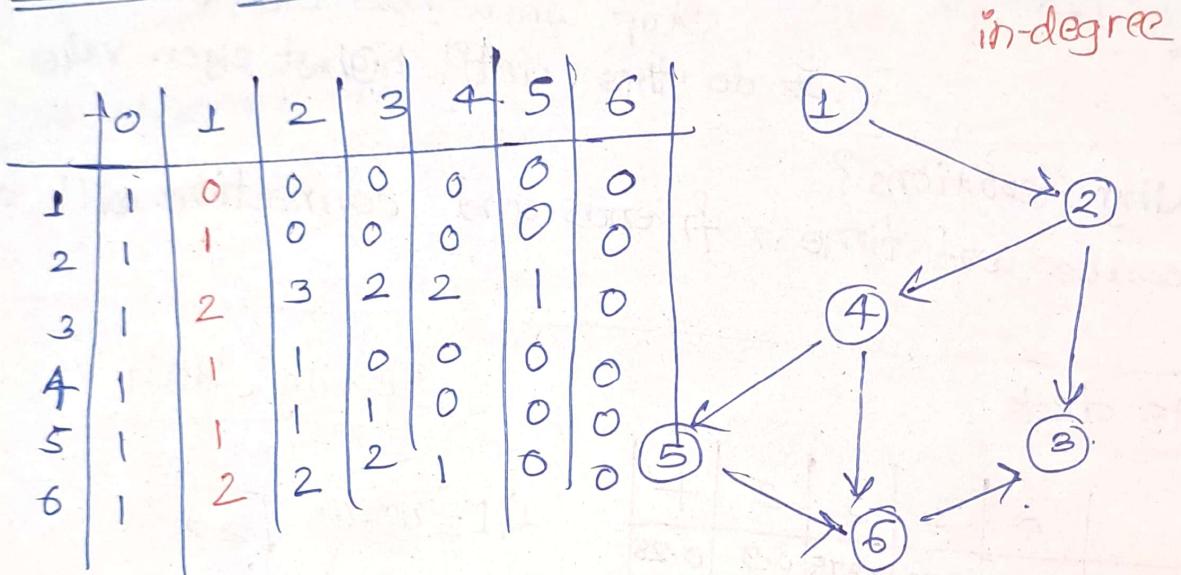
For directed
→ indirected

In links

$$AX_t = X_{t+1}$$

$$A^T X_t = X_{t+1}$$

calculate Eigen vector centrality for directed graph:-



* acyclic digraph.

• all power leaks out.

citation networks are acyclic, so eigen vector centrality is useless.

Adaptation for directed networks:-

$$X = \underbrace{\alpha AX \cdot \mathbf{B}}_{\text{power from neighbours}} + \underbrace{\mathbf{B}^\perp}_{\text{intrinsic power}}$$

power from neighbours

when this converges, we get:-

$$X = \mathbf{B}(1 - \alpha A^T)^{-1} \mathbf{I}_1$$

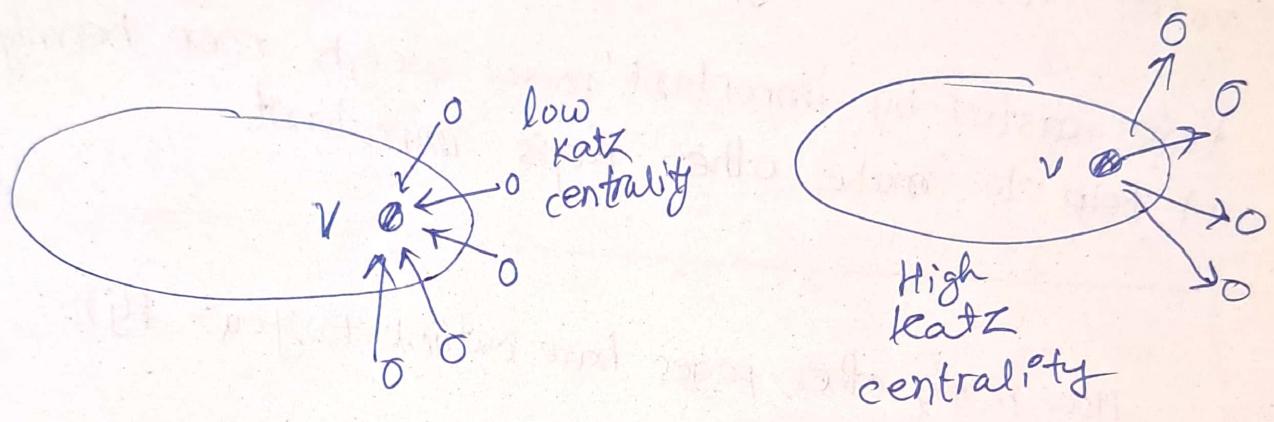
$$X = (1 - \alpha A^T)^{-1} \mathbf{I}_1$$

Ratz centrality
 $\beta = 1$

- If $\alpha=0$, $x=I$, centralities = 1
- As $\alpha \uparrow$, centralities increase
- At $\frac{1}{\lambda_1}$, (λ_1 is largest eigen value) things diverge.

Hence

$$\left[0 \leq \alpha \leq \frac{1}{\lambda_1} \right]$$



PageRank is most powerful measure.

Next class - 1, 2, 3 chapter.

Eigen, Katz, bonachich.

Hard copy Quiz.

Note:- We stop when Eigen vector values converge.

PAGE RANK

For web link analysis models.

PageRank interprets a hyperlink from page x to page y as a vote, by page x , for page y .

However, Page Rank looks at more than sheer number of votes; it also analyses the page that casts the vote.

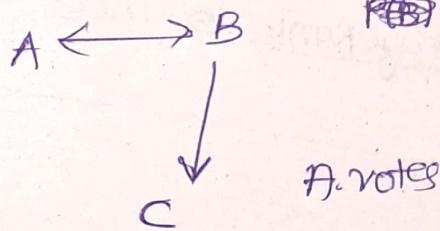
Notes casted by "important" pages weigh more heavily and help to make other pages important.

How many other pages have outlink to you :- $P(j)$

How many votes they give :- O_j

B. votes = 2.

$$P(A) = \frac{P(B)}{2} = 1.5.$$



$$P(B) = \frac{P(A)}{1} = 1.5$$

A. votes = 1

Let's assume $P(B) = 3$.
Then calculate $P(A)$ & $P(C)$.

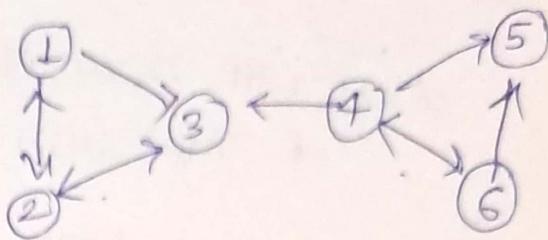
If your network has low rank pages,
Your page Rank will also decrease."

Solving Page Rank

$$P_{i+1} = A^T P_i$$

Stopping criteria $\Rightarrow P_{i+1} - P_i < 0.1$.

$$\bar{A} = \begin{bmatrix} 0 & \frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 \\ \frac{1}{2} & 0 & \frac{1}{2} & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{3} & 0 & \frac{1}{3} & \frac{1}{3} \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} & \frac{1}{2} & 0 \end{bmatrix}$$



Let $P_0 = \begin{pmatrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{pmatrix}$

$$A^T = \begin{bmatrix} 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \\ \frac{1}{2} & 0 & 1 & 0 & 0 & 0 \\ \frac{1}{2} & \frac{1}{2} & 0 & \frac{1}{3} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & \frac{1}{3} & 0 & \frac{1}{2} \\ 0 & 0 & 0 & \frac{1}{3} & 0 & 0 \end{bmatrix}$$

$$P_1 = A^T P_0$$

$$P_2 = A^T P_1$$

\vdots

$$P_g = A^T P_8$$

$$P_8 = \begin{bmatrix} 4.518 \\ 8.898 \\ 6.784 \\ 0.210 \\ 0.315 \\ 0.182 \end{bmatrix} \quad P_g = \begin{bmatrix} 4.501 \\ 9.096 \\ 6.830 \\ 0.173 \\ 0.213 \\ 0.122 \end{bmatrix}$$

$P_g - P_8 < 0.1$, so stop.

$\therefore \text{Rank} :- 2, 3, 1, 5, 4, 6$

Irrespective of P_0 , same Rank will be achieved.

How compare importance of pages.

start with normalisation.
if Total sum = 1

∴ 6 pages, Each Rank is $\frac{1}{6}$.

Total sum = 1.

∴ Updated page rank :-

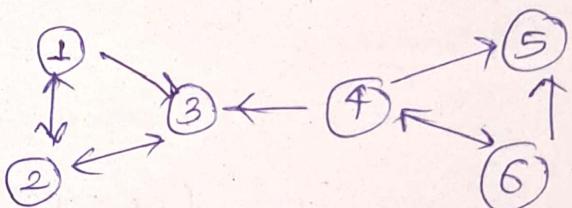
$$p(i) = (1-d) + d \sum_{(j, i \in E)} \frac{p(j)}{o_j}$$

Also $d = 0.8$
is recommended.

$$= (1-d) + d(A^T P)$$

Ex- Let $P_0 = \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{bmatrix}$

$$d = 0.8$$



~~Page 2~~ ~~Iteration 1~~

$$p(1) = (1 - 0.8) + 0.8 \left(\frac{2}{2}\right) = 1$$

$$p(3) = (1 - 0.8) + 0.8 \left(\frac{1}{2} + \frac{3}{2} + \frac{4}{3}\right) = 2.88.$$

$$p(5) = (1 - 0.8) + 0.8 \left(\frac{1}{2} + \frac{3}{2} + \frac{4}{3}\right) = 2.88.$$

Likewise

Ranking : $[5, 2, 3, 4, 1, 6]$
Iteration 1)

Iteration 2) $\rightarrow [2, 3, 1, 5, 4, 6]$.

which is answer.

Next improvement (improved normalisation)

$$P = (1-d) \frac{1}{n} + d \left(\frac{PR(i)}{\alpha(i)} + \frac{PR(j)}{\alpha(j)} + \dots + \frac{PR(n)}{\alpha(n)} \right)$$

cutpoint - delete node to increase components

bridge - delete edge, to increase components

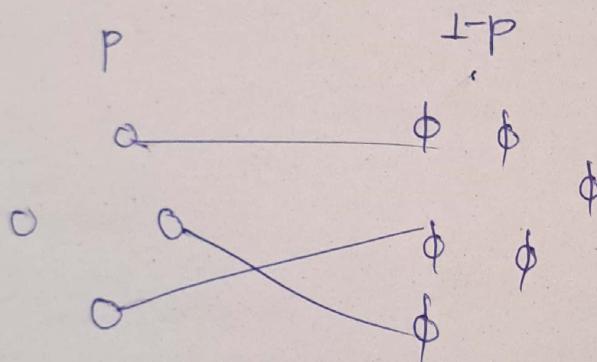
Homophily :- Birds of feather flock together.

Netlogoweb \rightarrow social science \rightarrow segmentation.

consider random network $G(V, E^r)$
where each node is assigned ~~not~~ male: p
female: $1-p$.

Let $G = (V, E)$ be random sample of R with p fraction of male and $1-p$ fraction of female.

- consider any edge $(i, j) \in E^r$ of random network R .



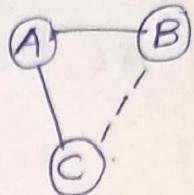
$$E(X^2) - (E(X))^2 = p(1-p) + (1-p)p = 2p(1-p).$$

Computer networks :- Hoax calls, mails (phishing links)

uptill Homophily mid-sem

Social vs selection Influence

- * Triadic closure.
- * Focal closure
- * membership closure



* community Homophily :-

Asian origin vertices:- 5, 7, 8, 10, 11, 12.

Caucasian origin vertices :- 1, 2, 3, 4, 6, 13, 14.

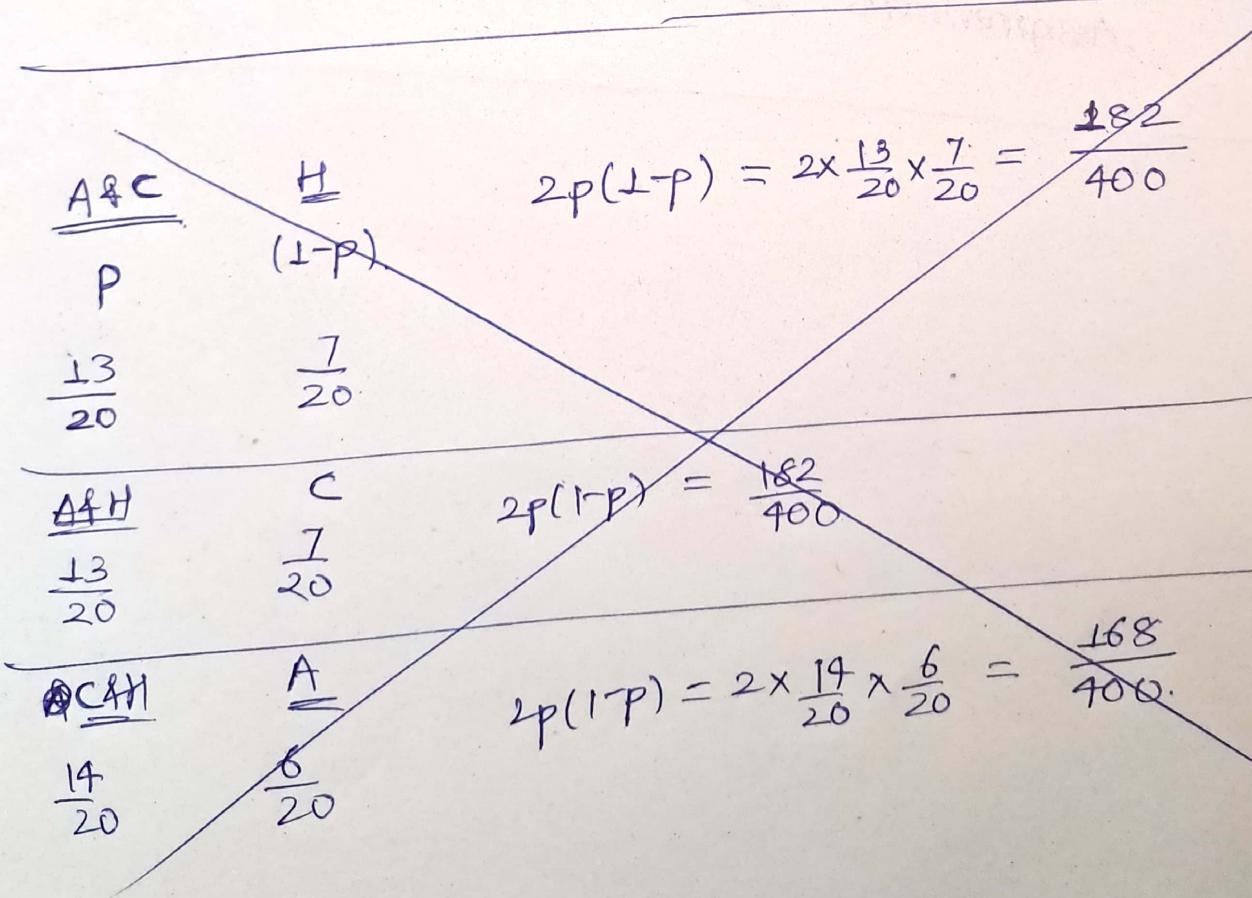
Hispanic origin vertices:- 9, 15, 16, 17, 18, 19, 20.

$$A : \frac{6}{20} = 0.3$$

$$C : \frac{7}{20} = 0.35$$

$$H : \frac{7}{20} = 0.35.$$

$$\# \text{Links} = \frac{\text{sum of degrees}}{2} = 47$$

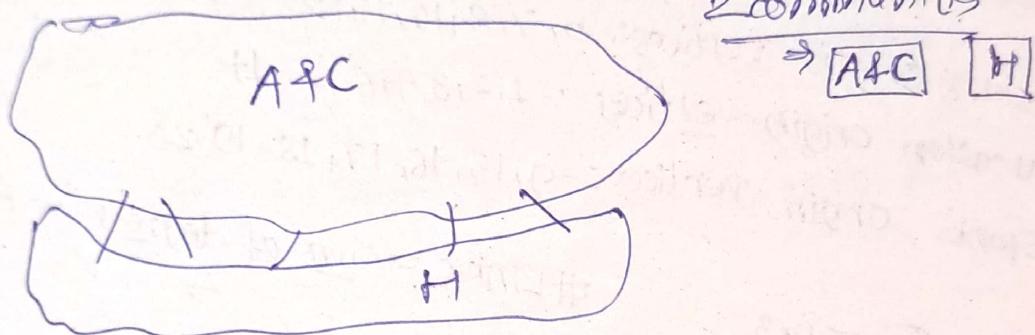


consider any 2 groups.

$$\text{Fraction of A-C Links} = \frac{12}{47} = 0.26$$

$$> 2 * A * C = 2 * 0.3 * 0.5 = [0.21]$$

Fraction Final community detected



Mid-sem exam syllabus over

~~Aze ration~~

Homophily

Assignments :- 35 marks

Evaluating modularity

$A_{ij} \rightarrow$ adjacency matrix

d_i, d_j - degree of i, j

m -edges.

Overall & individual higher modularity \rightarrow Better partition

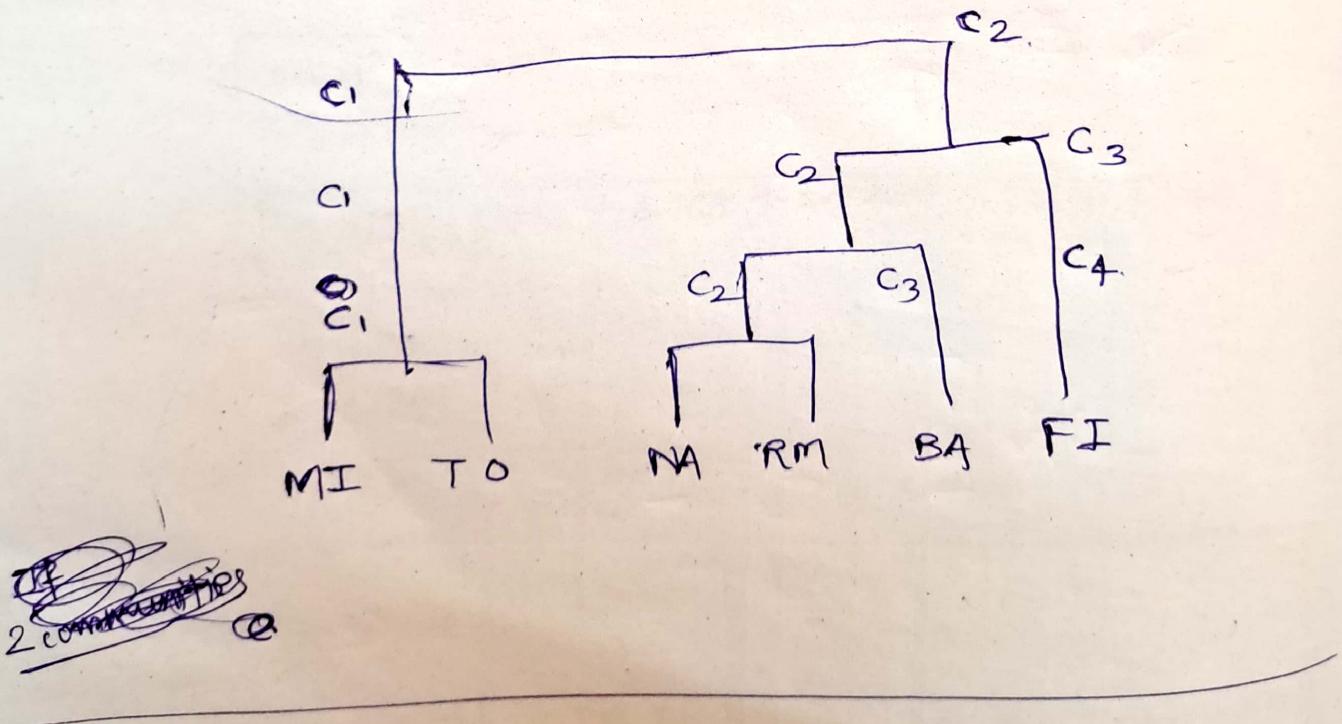
single linkage - minimal

complete linkage - maximal.

MI/TO \rightarrow other

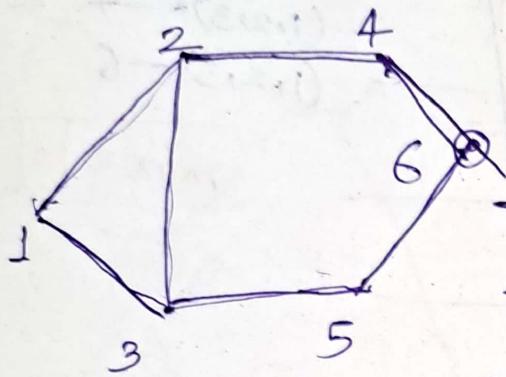
distance calculation \Rightarrow ~~max~~ [MI \rightarrow other, TO \rightarrow other]

[https://matteucci-faculty.polimi.it/clustering/
tutorial_html/hierarchical.html](https://matteucci-faculty.polimi.it/clustering/tutorial_html/hierarchical.html)



Hierarchical Linkage

based on min.dist



	1	2	3	4	5	6
1	0	1	1	2	2	3
2		0	1	1	2	2
3			0	2	1	2
4				0	2	1
5					0	1
6						0

	1,2	3	4	5	6	(52) → 3
1,2	0	1	2	2	3	3-5
3		0	2	1	2	4-6
4			0	2	1	5-6
5				0	1	
6					0	

(52) → 3 $\frac{2}{3}$
3-5 1/2
4-6 1/2
5-6 1/2
1/3 1/2
1/6 1/2
1/3 1/2
1/6 1/2
1/3 1/2
1/6 1/2

	1,2,3	4	5	6
1,2,3	0	2	2	3
4		0	2	1
5			0	1
6				0

	1,2,3	4,6	5	For distance $(1,2,3) - (4,6)$ $(1,2,3) - 4 : 2$ $(1,2,3) - 6 : 3$
1,2,3	0	3	2 (5) /	
4,6	0	2 (3) /	0 (0)	
5	0			max $\Rightarrow [3]$

Tie, here:- choosing pair with minimum total distance :-

pair size

ex) 1,2,3 — 5

$$\begin{array}{r} 1-5 \\ 2-5 \\ 3-5 \\ \hline 5 \end{array} \div (3 \cancel{\times})$$

$$\boxed{5} \cancel{4}$$

$$\frac{5}{3} \checkmark$$

$$1.66$$

pair size $\Rightarrow 3$

4,6 — 5.

$$\begin{array}{r} 4-5 \\ 6-5 \\ \hline 3 \cancel{+} \cancel{2} \end{array}$$

pair size = 2

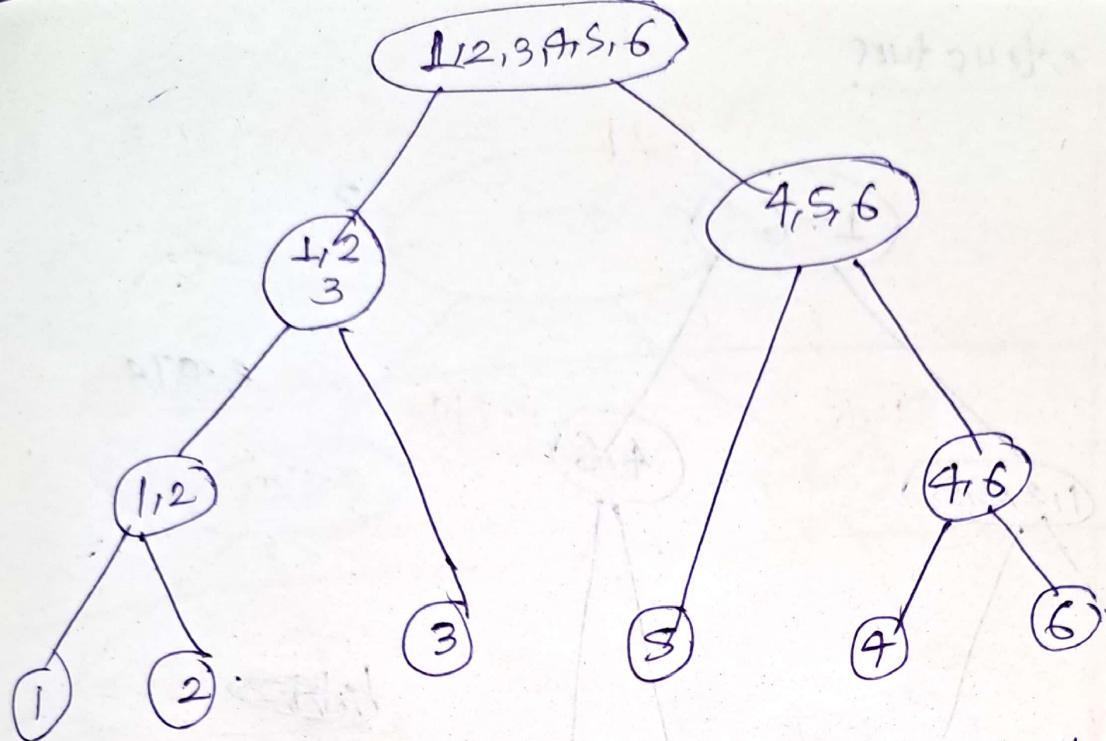
$$\frac{3}{2} \checkmark$$

$$1.5$$

For just dista
 $(1,2) - (4,6)$

Final

	1,2,3	4,6,5	1,2,3 — 4,6 : 3 1,2,3 — 5 : 2
1,2,3	0	3	
4,6,5		0	



complete linkage clustering.

modularity values

$$\text{ex:- } \text{(1,2)} (1,2,3) \rightarrow 1.49$$

How?

take pairs	modularity
1,2	0.57
1,3	0.57
2,3	0.35
	1.49

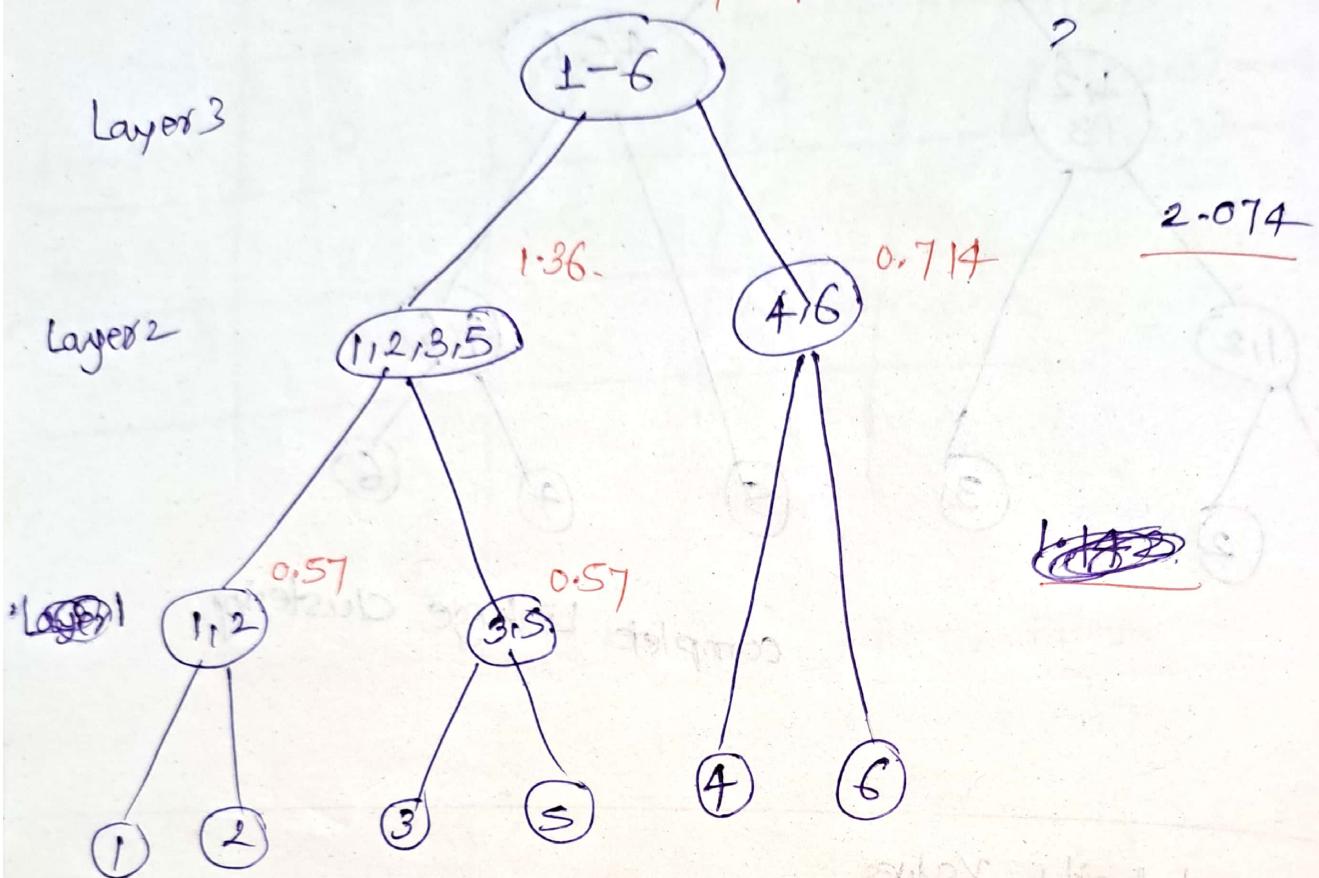
Note:- Hierarchical diagram can be different,
but if done correctly, modularity scores
overall will be same.

Layerwise overall modularity must be more.

another structure

1.21

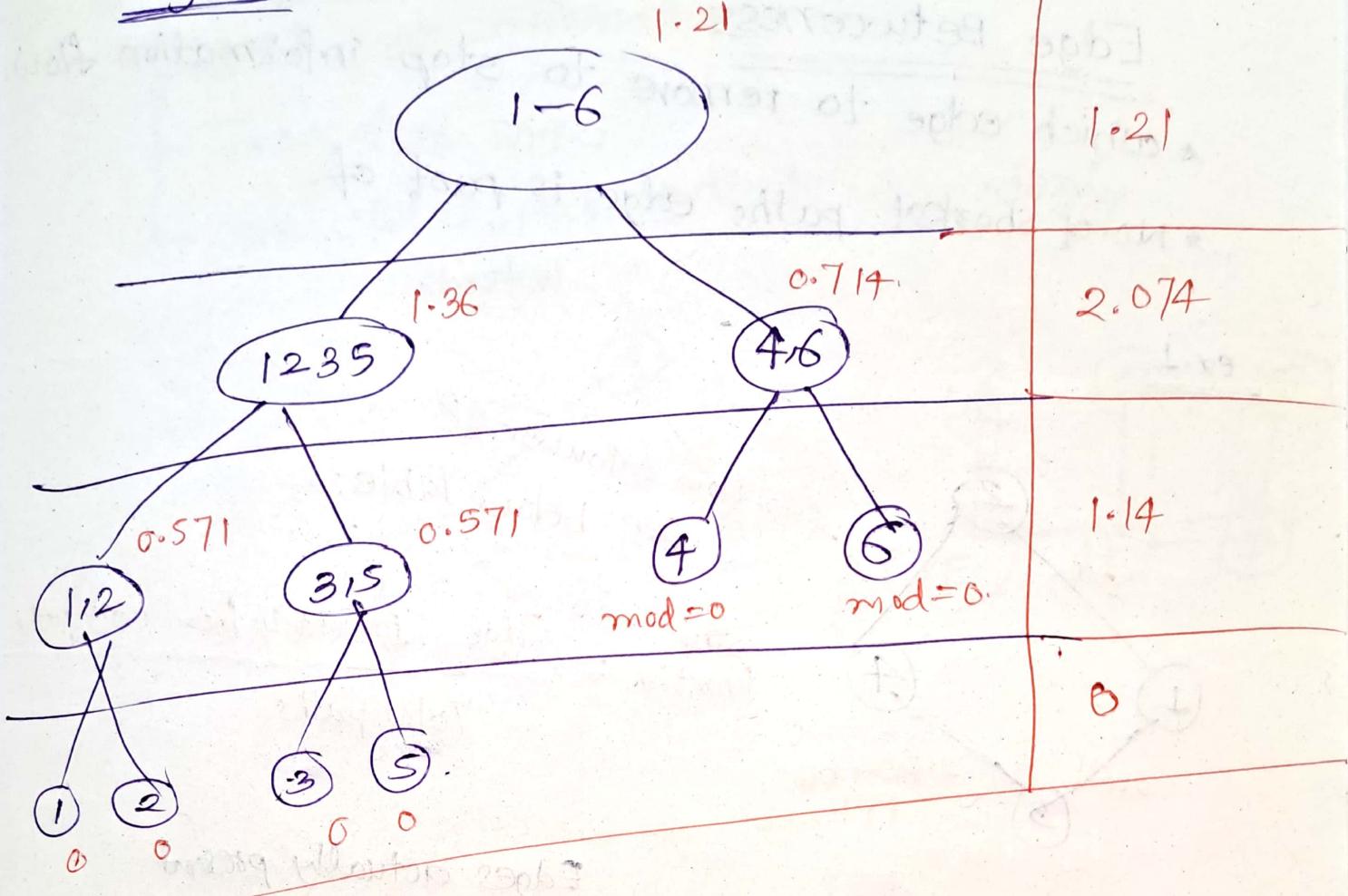
Same



This has less layerwise modularity, so
this is wrong hierarchical structure

complet Linkage clustering need not always
give optimum solution.

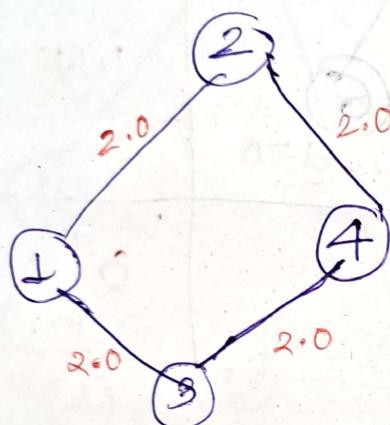
Layers



Edge Betweenness

- * which edge to remove to stop information flow.
- * No. of shortest paths edge is part of.

ex.1



How calculated?
see below Table:-

~~so~~ Fraction = Edge Present in how many path
Total paths.

Edges actually present

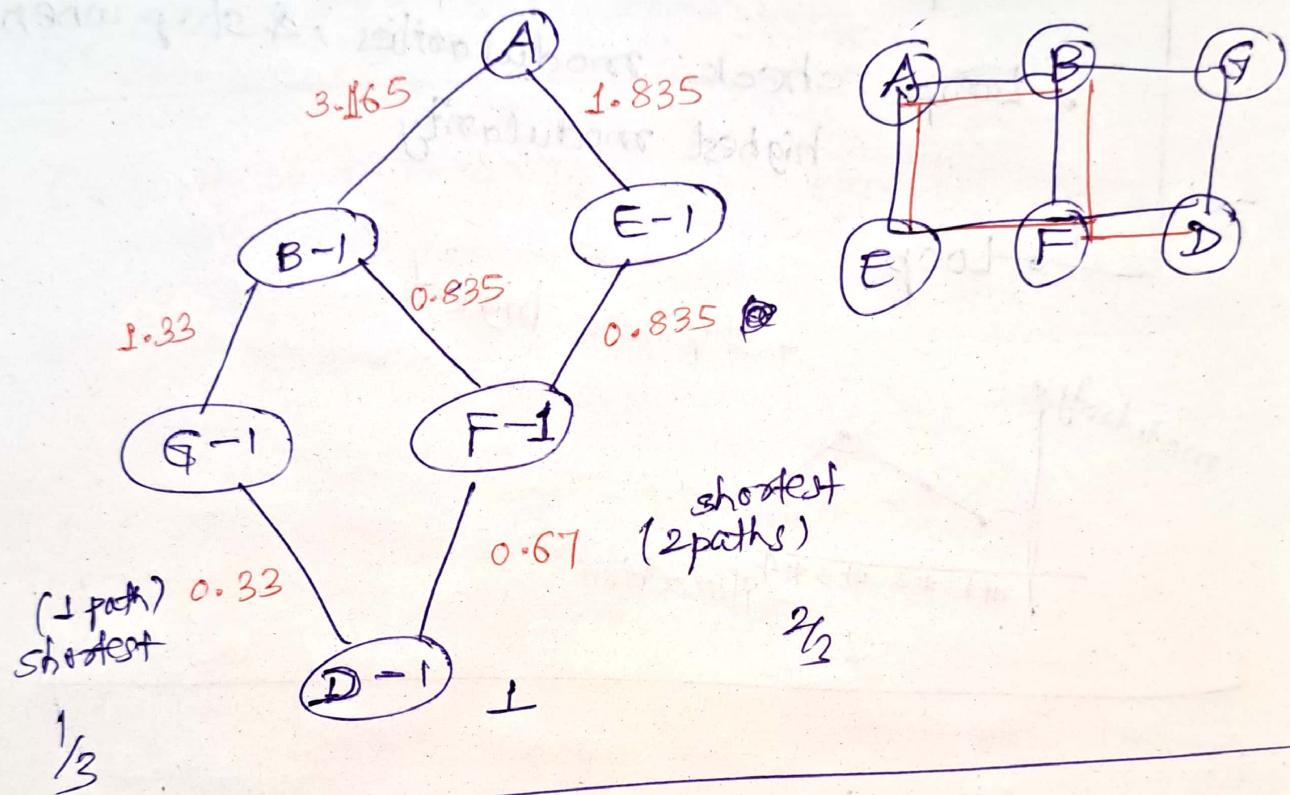
Pairs	Paths	1-2	1-3	2-4	3-4
(1,2)	1-2	1/1			
(1,3)	1-3		1/1		
(1,4)	1-2-4, 1-3-4	1/2	1/2	1/2	1/2
(2,3)	2-1-3, 2-4-3	1/2	1/2	1/2	1/2
(2,4)	2-4			1/1	
(3,4)	3-4				1/1
EdgeBW		2	2	2	2

Info spread

Add your information

Take other info

see total paths & divide accordingly
shortest.



Node betweenness

$$\text{NodeBWC}(i) = \left\{ \sum_{(i,j) \in E} \text{EdgeBWC}(ij) \right\} - \{c_i - 1\}$$

$$\text{NodeBWC}(i) = \frac{\sum_{(i,j) \in E} \text{EdgeBWC}(ij)}{2}$$

c_i :- total nodes

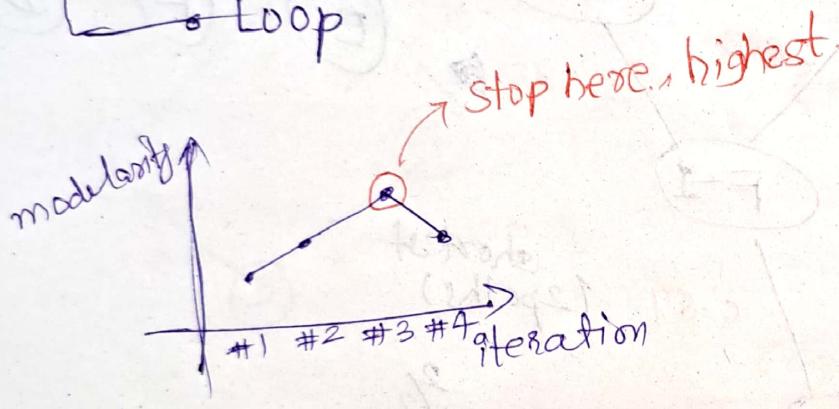
ex

now compare node BWC using Edge Betweeness
and our old formula.

GN algorithm (Girvan Newman)

Find Edge betweeness

- highest value edge break KAD.
 - compute modularity, Take sum.
 - Loop check modularities, & stop when highest modularity
- Loop



Nover score :-

Find neighbours of A & B, excluding A & B.

$$\text{Nover score} = \frac{\text{Intersection}}{\text{Union}}$$

Nover-based GN algorithm :-

- Break edges with least NOVER scores.

Weak Ties / Strong Ties

- * **one step algorithm** finding mates.
- * optimum threshold (helps set Nover score)

Strong Triadic Property:

If A connected strongly to B & C.
Then B & C must atleast be weakly connected.

$$\text{Extent of Homophily} = 1 - \frac{\text{observed}}{\text{expected}}$$

oddities: transitive closure, all pairs, 3D
behaviour of this closure
very oddities in various types of graphs, some
oddities, some off - basic
oddities after it

$$S = (\pi X) \oplus \pi$$

(oddities)

(oddities)

(oddities)

(oddities)

Link Prediction

Information Diffusion and Cascades.

★ Triadic closure will be useful.

Link prediction :- Given a network, predict which edges will be formed in future.

Basic measures :- no. of common neighbours

Jaccard coeff

Resource Allocation Index

Adamic-Adar Index

preferential Attachment score.

Measures requiring community :-

- sundar-rajan - Hoffmann Croft score

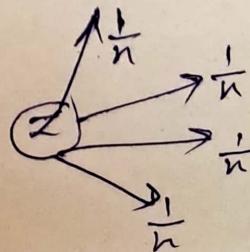
- The ones with most common neighbours i.e. (A,C,2) will connect first
- Then others value will be updated
- Then again connect most common neighbour pair.
- Loop

$$\text{Jacc-coff} = \frac{\# \text{common neighbours}}{\# \text{Total neighbours.}}$$

Resource Allocation.

$$\text{res-alloc}(x,y) = \sum_{u \in \text{common neighbour}} \frac{1}{N(u)}$$

(X) $\xrightarrow{\perp} \textcircled{Z}$ If x has neighbours.



Adamic Adar Index (Exam)*

• similar to res-alloc, but log

$$\text{adamic-adar}(X, Y) = \sum_{u \in \text{common}} \frac{1}{\log(N(u))}$$

Pref Attachment: $|N(X) \cap N(Y)|$ (Exam*)

$$\text{pref}(A, C) = 3 * 3 = 9.$$

product of node's degree

community structure

No. of common neighbours with bonus for
neighbours in same community.

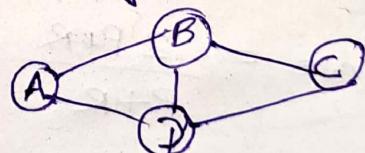
$$|N(X) \cap N(Y)| + \sum_{u \in N(X) \cap N(Y)} f(u)$$

$f(u) = \begin{cases} +, & \text{same community} \\ 0, & \text{different community} \end{cases}$

$$\text{ex: } (A, C) \rightarrow 4$$

$$(E, I) \rightarrow 2$$

$$(A, G) \rightarrow 1.$$



$$(A-C) \Rightarrow B + D + 1 + 1$$

$$\Rightarrow 1 + 1 + 1 + 1$$

$$\boxed{(A-C) \Rightarrow 4}$$

7. Community Resource Allocation

ra-soundarajan-hopcroft $(X, Y) = \sum_{u \in \text{common}} \frac{f(u)}{N(u)}$.

$$(A, C) = \frac{1}{3} + \frac{1}{3} = \boxed{\frac{2}{3}}$$

$$(A, G) = \frac{0}{3} = \boxed{0}$$

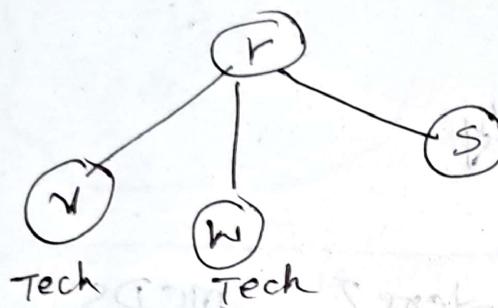
$$\text{critical success Index} = \frac{TP}{TP + FP + FN}$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$\text{Recall} = \frac{TP}{TP + FN}$$

$$\text{F1 score} = \frac{2 P * R}{P + R}$$

Tec 10 :- Information Cascade and Cascading Capacity of a Network :-



r has 3 neighbours

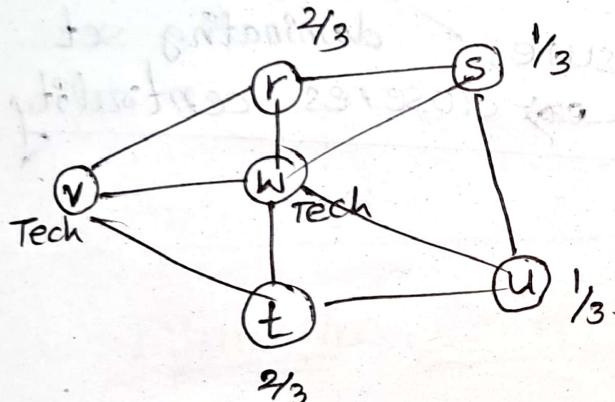
2 adopted technology

$$\frac{2}{3}$$

is adopted

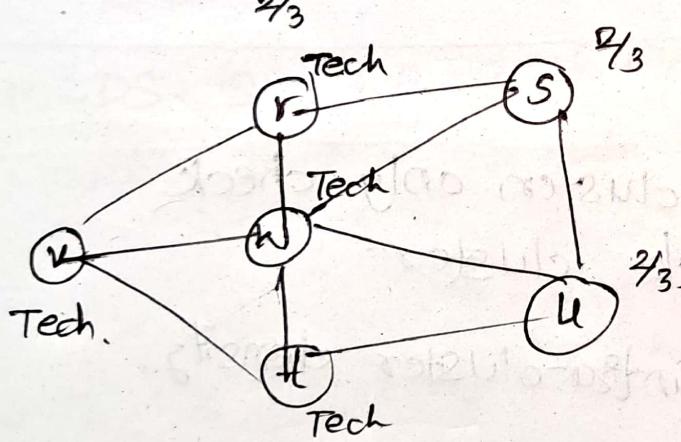
cascading

capacity of r.



Here, q is threshold for evaluate

information passing



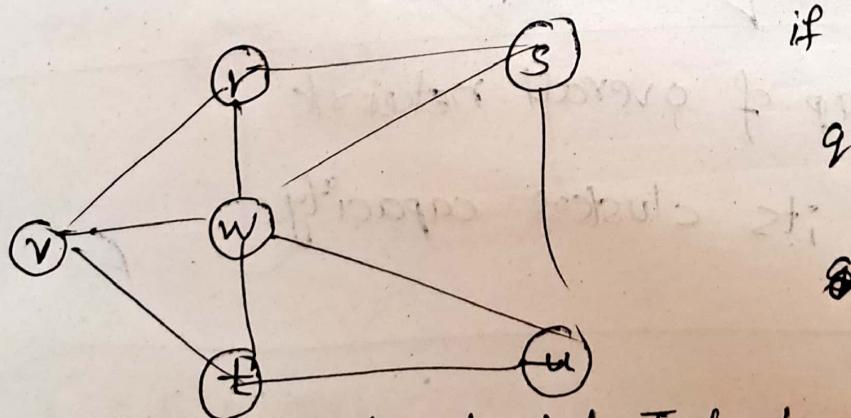
cascading capacity is $\max q$ (threshold)

after which full network cannot adopt technology.

Instead of $q = 0.5$,

if $q \leq \frac{2}{3}$ (max).

$q > \frac{2}{3}$, all cannot adopt tech



all adopted Technology

Q] What proportion of neighbors should adopt a decision before a node starts adopting it?

ans:- 'q' proportion/fraction

q is cascading capacity

? Choice of Initial adopters? MCDS

ans:- use centrality measures. \rightarrow minimum connecting dominating set.

\hookrightarrow closeness centrality

\Rightarrow Inter-cluster density.

* Density of clusters

II.

Inter-

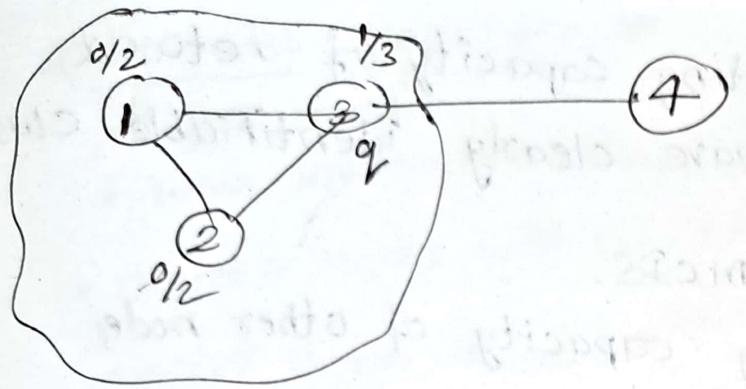
For penetrability of clusters, only check bridge nodes to cluster

Take min. inter-cluster density

then ~~or~~

cascading cap. of overall network

= min. of its clusters capacity



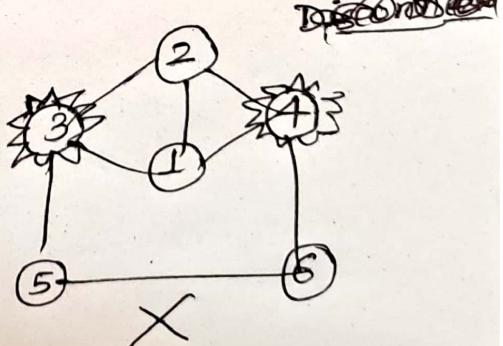
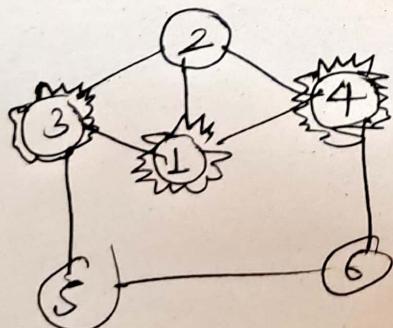
$1 - q$ is less than cluster density
then cluster cannot be penetrated.
i.e. $q \leq 1 - \text{cluster density}$.

Minimum Connected Dominating Set

MCDS is min. set of nodes,
such that → node in MCDS
→ or neighbour of MCDS.
→ must be connected nodes.

* This is NP-complete problem.

ex:-



The MCDS must be connected set

ex:-
 $\{1, 3, 5\}$
 $\{1, 3, 4\}$
 $\{1, 4, 6\}$
 $\{2, 3, 4\}$

How to find cascading capacity of network
that does not have clearly identifiable clusters?

- After coloring MCDS.
- Find cascading capacity of other nodes.
- min capacity of them is cascading capacity

Advantage of MCDS:-

A others will be coloured in 1 tick.

Disadvantage

If we taken less than MCDS set, we need more iterations to color whole network.

★d-mCDS Heuristic★

- degree based.
- when information adopted, set degree = 0.
- degree = nodes with no information.
- color again, those with max. degree
- stop when all get information.

Then find cascading capacity, min. is answer

Almost syllabus over