$\frac{\psi(z)}{\Gamma(z)} = -e^{2\gamma z} \prod_{k=0}^{\infty} \left(1 - \frac{z}{x_k}\right) e^{\frac{z}{x_k}}$