

### Question 1 – (20 marks)

1. (1 mark) Machine learning can be split up into two predominant categories of problems. What are they?
2. (1 mark) Suppose you are working on weather prediction and you would like to predict weather it will be raining at 5 p.m. the next day. What category of supervised learning would this belong to?
3. (2 mark) What is Arthur Samuel's definition of Machine Learning?
4. (2 marks) Why is it necessary to normalize the features prior to running gradient descent for regression or classification?
5. (2 marks) Define linear regression and classification for one variable? Explain with examples.
6. (1 mark) What is the purpose of the learning rate? What happens if this value is too small? What happens if this value is too large?
7. (1 marks) What means "Batch gradient" descent? What means "Stochastic gradient" or "on-line" gradient descent?
8. (1 mark) What is the hypothesis  $h_{\theta}(x)$  used in logistic regression?
9. (2 mark) What is the difference between classification and logistic regression?
10. (1 mark) What is the hypothesis/Model in machine learning?
11. (1 mark) Adding new features and finding the optimal parameters using the training set will allow for high accuracy though there is a chance for over fitting. (True or False)?
12. (1 marks) Explain what the problem of over fitting is and explain how you would reduce over fitting in machine learning problems.?
13. (2 marks) What is Tom Mitchell's definition of Machine Learning?
14. (1 mark) What is the problem of overfitting?
15. (1 marks) What is the goal of classification?

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### Question 2 – (10 marks)

Recall Suppose we are given  $m = 5$  training examples:

$$\theta_0 = \theta_1 = 0 \quad \alpha = 1 \quad N = \dots \quad m = 5$$
$$\theta_0 \leftarrow \theta_0 -$$

$x$	$y$
-2	-1
-1	0
1	2
2	3
4	6

#### Parts to solve

1. (6 marks) Given the initial values of  $\theta_0, \theta_1 = 0$  and a learning rate of  $\alpha = 0.1$ , compute  $N = 3$  iterations of gradient descent for finding these parameters for linear regression. Compute both the parameters  $\theta_0, \theta_1$  as well as the cost of iteration.
2. (2 marks) After the third iteration in this question, predict what the outputs would be when  $x = -0.5, 0.5, \text{ and } 1.5$ .



### Question 3 – (25 marks)

Suppose we have the following table that illustrates our training data set concerning thermal resistors where our goal is to create a prediction model where given the current (in milliamps) flowing through the resistor, we want to determine what the voltage (in millivolts) across the resistor would be.

Example	Current $x$ (mA)	Voltage $y$ (mV)
1	1	2.2
2	2.5	3.76
3	4	5.4
4	6	7.9

Because of the highly non-linear relationship between the current and voltage, we will be using new features to allow for higher accuracy. Specifically, we will use two features for our prediction model:  $x_1 = x^2$ ,  $x_2 = \sqrt{x}$ .

#### Parts to solve

1. (2 marks) Using the measurements above, complete the following table in order to create these two features. You may complete the table here or do this in your response booklets:

Example	$x_1$	$x_2$
1		
2		
3		
4		

2. (7 marks) Because of the wide dynamic range, we will need to **feature normalize** the above table before we create our prediction model. Normalize the features above so that they exhibit **zero mean and unit variance**. You can complete the table below here or do this in your response booklets:

Example	$x_1$	$x_2$
1		
2		
3		
4		

3. (12 marks) With the **normalized features**, using a learning rate  $\alpha = 0.75$ , the **regularization parameter**  $\lambda = 0.5$  and with the initial parameters  $\theta_0 = \theta_1 = \theta_2 = 1$ , compute  $N = 1$  iteration and state the parameters  $\theta_0, \theta_1, \theta_2$  as well as the cost  $J(\theta)$ .

4. (4 marks) Using the learned parameters found in the previous step after the first iteration, predict what the output voltage would be if the input current is 2 mA and 3 mA.



**Question 4 – (5 marks)**

Suppose we have the following training example data set. There are three classes in total with two features per training example. A table that shows the features per training example  $x_1, x_2$  and corresponding expected output class  $y$  are shown below:

$x_1$	$x_2$	$y$
-2	3	1
-2	4	1
-1	3	1
3	3	2
4	4	2
4	3	2
-1	-1	3
-2	0	3
-3	-2	3

**(5 marks)** Plot these points in cartesian grid. Which type of classification do you suggest for this question (explain)?