

Ex- 3.1

$$\textcircled{1} \sum_{x \in \{0,1\}} p(x|\mu) = p(x=0|\mu) + p(x=1|\mu) \\ = (1-\mu) + \mu = 1$$

$$\textcircled{2} \sum_{x \in \{0,1\}} x p(x|\mu) = 0 \cdot p(x=0|\mu) + 1 \cdot p(x=1|\mu) = \mu$$

$$\textcircled{3} \sum_{x \in \{0,1\}} (x-\mu)^2 p(x|\mu) = \mu^2 p(x=0|\mu) + (1-\mu)^2 p(x=1|\mu) \\ = \mu^2 (1-\mu) + (1-\mu)^2 \mu \\ = \mu (1-\mu) (\mu + (1-\mu)) \\ = \mu (1-\mu) (\mu + 1 - \mu) \\ = \mu (1-\mu)$$

