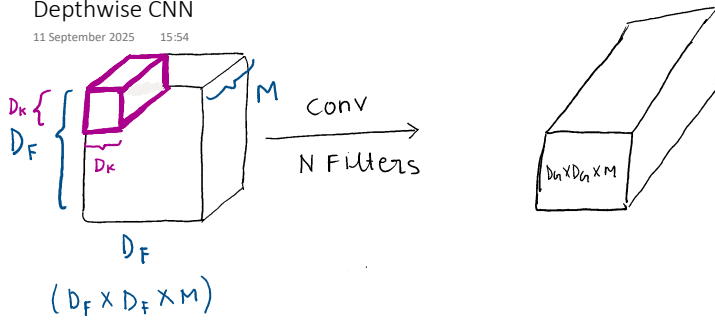


Depthwise CNN

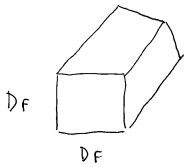
11 September 2025 15:54



Computation of normal convolution

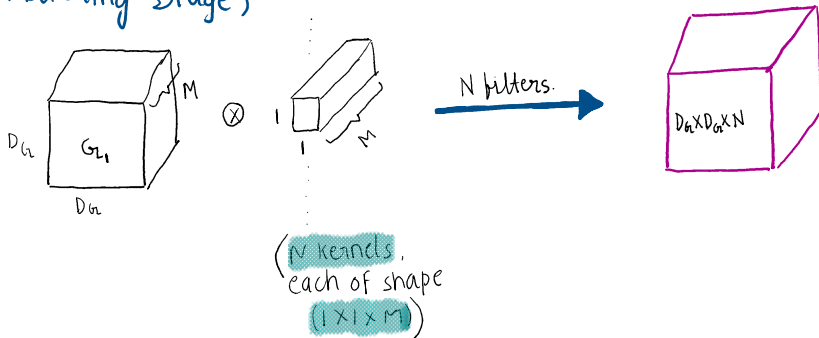
- Mults once = $D_K^2 \times M$
- Mults per Kernel = $D_G^2 \times D_K^2 \times M$
- Mults N Kernels = $N \times D_G^2 \times D_K^2 \times M$

Depthwise Convolution



- We only apply one kernel to a single input channel.
- Hence we require M such kernels over the entire F .
- Each kernel is $D_K \times D_K \times 1$
- Each kernel's output is $D_G \times D_G \times 1$
- Stacking all the kernels (M) we get $D_G \times D_G \times M$

Pointwise Convolution (Filtering stage)



Computation

Depthwise Separable Convolution:

- Mults once = D_K^2
- Mults one channel = $D_G^2 \times D_K^2$
- DC Mults = $M \times D_G^2 \times D_K^2$

Pointwise Convolution:

- Mults once = M
- Mults 1 kernel = $D_G^2 \times M$
- PC Mults = $N \times D_G^2 \times M$

Total = DC Mults + PC Mults

$$= M \times D_G^2 \times D_K^2 + N \times M \times D_G^2$$

$$= M \times D_G^2 (D_K^2 + N)$$

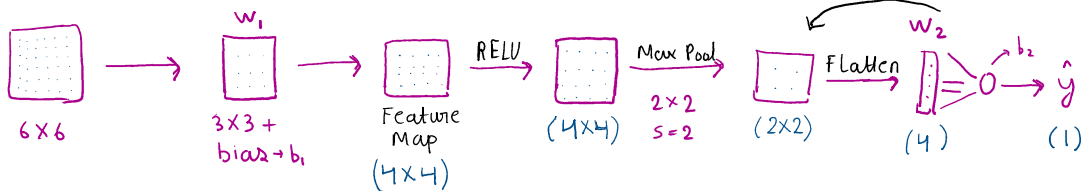
Comparison Standard Vs Depthwise

$$\frac{\text{No. of mults in Depthwise}}{\text{No. of mults in Standard}} = \frac{M \times D_G^2 (D_K^2 + N)}{M \times N \times D_G^2 \times D_K^2}$$

$$= \frac{D_k^2 + N}{(D_k^2 \times N)} = \frac{1}{N} + \frac{1}{D_k^2}$$

1) Group Convolution

- A normal conv would look across all 64 input channels. That's PRICEY
- GroupConv splits 64 channels into groups (paper uses ^{half} the channels as groups \rightarrow 32 groups each size 2).



Trainable Parameters

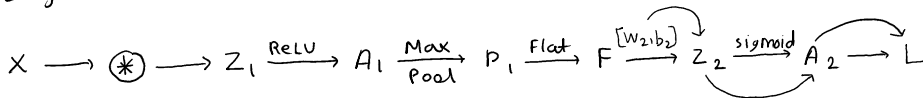
$$w_1 = (3, 3) \quad w_2 = (1, 4)$$

$$b_1 = (1, 1) \quad b_2 = (1, 1)$$

= 15 trainable parameters.

$$L = -y_i \log(\hat{y}_i) - (1 - y_i) \log(1 - \hat{y}_i)$$

Logical Flow



Forward Prop

$$\begin{aligned} Z_1 &= \text{conv}(X, w_1) + b_1 \\ A_1 &= \text{relu}(Z_1) \\ P_1 &= \text{MaxPool}(A_1) \end{aligned} \quad \left| \quad \begin{aligned} F &= \text{flatten}(P_1) \\ Z_2 &= w_2 F + b_2 \\ A_2 &= \sigma(Z_2) \end{aligned} \right.$$

$$\frac{\partial L}{\partial w_2}$$

Gradient Decent on ANN

$$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial A_2} \times \frac{\partial A_2}{\partial Z_2} \times \frac{\partial Z_2}{\partial w_2}$$

Ch-1
Ch-2
Ch-4

The Gaussian Distribution

$$p(x | \mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{\left[-\frac{(x-\mu)^2}{2\sigma^2}\right]}$$

likelihood function

$$p(D | \mu, \sigma^2) = \prod_{n=1}^N p(x_n | \mu, \sigma^2) \quad [D = [x_1, x_2, \dots, x_n]]$$

$$p(D|\mu, \sigma^2) = \prod_{n=1}^N p(x_n | \mu, \sigma^2) \quad [D = x_1, x_2, \dots, x_N]$$

$$\log p(D|\mu, \sigma^2) = \sum_{n=1}^N \log p(x_n | \mu, \sigma^2)$$

$$\log p(D|\mu, \sigma^2) = -\frac{N}{2} \log(2\pi\sigma^2) - \frac{1}{2\sigma^2} \sum_{n=1}^N (x_n - \mu)^2$$

Maximising w.r.t to μ

$$\frac{d}{d\mu} \log p(D|\mu, \sigma^2) = \frac{1}{\sigma^2} \sum_{n=1}^N (x_n - \mu) = 0$$

$$\Rightarrow \mu_{ML} = \frac{1}{N} \sum_{n=1}^N x_n$$

Similarly,

$$\sigma_{ML}^2 = \frac{1}{N} \sum_{n=1}^N (x_n - \mu_{ML})^2$$

Ex-2.1

Given from book:

- True +ve: $\alpha = p(T=1 | C=1) = 0.9$
- False +ve: $\beta = p(T=1 | C=0) = 0.03$
- NEW prior (prevalence): $p(C=1) = \pi = 0.001$
 $\Rightarrow p(C=0) = 1 - \pi = 0.999$

We want to calculate $p(C=1 | T=1)$

Bayes' Theorem:

$$\begin{aligned} p(C=1 | T=1) &= \frac{p(T=1 | C=1) p(C=1)}{p(T=1 | C=1) p(C=1) + p(T=1 | C=0) p(C=0)} \\ &= \frac{\alpha \pi}{\alpha \pi + \beta(1-\pi)} = \frac{0.9 \times 0.001}{0.9 \times 0.001 + 0.003 \times 0.999} \\ &= \frac{0.0009}{0.003087} \approx 0.0292 \end{aligned}$$

Ex-2.4

$$p(x) = 1/(d-c), \quad x \in (c, d)$$

Integrating over x we obtain

$$\int_{-\infty}^{\infty} p(x) dx = \int_c^d \frac{1}{d-c} dx = \frac{d-c}{1} = 1$$

$$\int_{-\infty}^{\infty} p(x) dx = \int_c^d \frac{1}{d-c} dx = \frac{d-c}{d-c} = 1$$

$$E[x] = \int_a^b \frac{1}{b-a} x dx = \left[\frac{x^2}{2(b-a)} \right]_a^b = \frac{b^2 - a^2}{2(b-a)} = \frac{a+b}{2}$$

$$E[x^2] = \int_a^b \frac{1}{b-a} x^2 dx = \left[\frac{x^3}{3(b-a)} \right]_a^b = \frac{b^3 - a^3}{3(b-a)} = \frac{a^2 + ab + b^2}{3}$$

Ex-2.10

For a continuous random variable X

$$E[X] = \int_{-\infty}^{\infty} x p(x) dx$$

$$E[x+z] = \iint (x+z) p(x, z) dx dz$$

$$= \iint (x+z) p(x) p(z) dx dz$$

$$= \int x p(x) dx \underbrace{\int p(z) dz}_{=1} + \underbrace{\int p(x) dx}_{=1} \int z p(z) dz$$

$$= E[x] + E[z]$$