

# Building up models

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## Introduction

In this document, we build up models for the NATSAP data, starting from very simple models and gradually getting more and more complex.

## Read in data

Code to read and clean the data.

```
library(lme4)
library(rstan)
library(dplyr)
library(ggplot2)

## Import Data
natsap <- read.csv("NewNATSAP.csv")
dose <- read.csv("NATSAPDoseData.csv")

## Get rid of program with no NatsapID
dose <- dose[!is.na(dose$NatsapId),]

## Select only wanted variables and create diff
natsap_tidy <- natsap %>%
  select(ID = NatsapId,
         sex = GenderNumeric,
         admission_OQ = AdmissionTotalScore,
         discharge_OQ = DischargeTotalScore) %>%
  mutate(diff = admission_OQ - discharge_OQ)

natsap_tidy <- natsap_tidy[complete.cases(natsap_tidy),]

dose_tidy <- dose %>%
  select(rtc_vs_obh = RTCvsOBH,
         ID = NatsapId,
         minutes_ind_therapy = Mode.minutes.of.Individual.Therapy,
         minutes_group_therapy = Mode.minutes.of.Group.Therapy)

## Creates new program IDs incrementing from 1 for loops in Stan
## lookup is the intersection of ID from dose_tidy and natsap_tidy
natsap_tidy_ID <- select(natsap_tidy, ID)
dose_tidy_ID <- select(dose_tidy, ID)
lookup <- semi_join(dose_tidy_ID, natsap_tidy_ID)
lookup <- cbind(lookup, new_ID = 1:length(lookup$ID))

## Selects only the cases in the dataframes that have IDs in Lookup
```

```

## and adds a column including the new indices for the NatsapIds
natsap_tidy <- natsap_tidy %>%
  inner_join(lookup, by = "ID") %>%
  arrange(new_ID)
dose_tidy <- dose_tidy %>%
  inner_join(lookup, by = "ID") %>%
  arrange(new_ID)

## Add sample sizes for each program
n_by_program <- natsap_tidy %>%
  group_by(new_ID) %>%
  summarize(n = n())

dose_tidy <- cbind(dose_tidy, n = n_by_program$n)

## Defines Variables to be passed to Stan
## IPred and GPred have a column of 1's representing the constant term
n_subj <- nrow(natsap_tidy)
n_prog <- nrow(dose_tidy)
sex <- select(natsap_tidy, sex)
ind_pred <- cbind(rep(1, n_subj), sex)
minutes_ind_therapy <- select(dose_tidy, minutes_ind_therapy)
minutes_group_therapy <- select(dose_tidy, minutes_group_therapy)
rtc_vs_obh <- select(dose_tidy, rtc_vs_obh)
group_pred <- cbind(rep(1, n_prog), minutes_ind_therapy, minutes_group_therapy)
diff <- natsap_tidy$diff
ID = select(natsap_tidy, ID)

## Put data in a list for Stan
data_list <- list(n_subj = n_subj,
                  n_prog = n_prog,
                  n_ind_pred = ncol(ind_pred),
                  n_group_pred = ncol(group_pred),
                  diff = diff,
                  ID = ID,
                  ind_pred = ind_pred,
                  group_pred = group_pred)

```

## Simple linear models

We need IDs and sex to be factor variables.

```

natsap_tidy <- natsap_tidy %>%
  mutate(ID = as.factor(ID),
         new_ID = as.factor(new_ID),
         sex = as.factor(sex))

```

Let's look only at diff by sex. This is what Gelman and Hill call "complete pooling".

```

fit_pooled <- lm(diff ~ sex - 1, data = natsap_tidy)
summary(fit_pooled)

```

```
##
## Call:
## lm(formula = diff ~ sex - 1, data = natsap_tidy)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -127.401  -24.164   -2.927   22.599  125.073
##
## Coefficients:
##      Estimate Std. Error t value Pr(>|t|)
## sex0    27.927      1.629   17.14 <2e-16 ***
## sex1    42.401      1.700   24.93 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 34.56 on 861 degrees of freedom
## Multiple R-squared:  0.5154, Adjusted R-squared:  0.5142
## F-statistic: 457.8 on 2 and 861 DF,  p-value: < 2.2e-16
```

Contrast this with no pooling.

```
fit_unpooled <- lm(diff ~ sex + new_ID - 1, data = natsap_tidy)
summary(fit_unpooled)
```

```
##
## Call:
## lm(formula = diff ~ sex + new_ID - 1, data = natsap_tidy)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -128.96  -22.54   -2.00   22.32  132.53
##
## Coefficients:
##      Estimate Std. Error t value Pr(>|t|)
## sex0      39.025      4.649   8.393 < 2e-16 ***
## sex1      48.008      3.005  15.977 < 2e-16 ***
## new_ID2    -3.740      4.990  -0.749 0.453803
## new_ID3   -17.275      5.562  -3.106 0.001961 **
## new_ID4    19.992     19.855   1.007 0.314277
## new_ID5    -4.049      4.233  -0.957 0.339031
## new_ID6   -12.643      6.515  -1.940 0.052659 .
## new_ID7   -20.960      7.161  -2.927 0.003512 **
## new_ID8     5.642     20.170   0.280 0.779754
## new_ID9   -35.341     19.855  -1.780 0.075448 .
## new_ID10  -57.508     24.225  -2.374 0.017823 *
## new_ID11  -11.580      8.026  -1.443 0.149448
## new_ID12  -21.305     13.437  -1.586 0.113197
## new_ID13  -13.358     14.636  -0.913 0.361687
## new_ID14   12.797     11.069   1.156 0.247956
## new_ID15   -5.420      4.977  -1.089 0.276467
## new_ID16  -18.553      4.914  -3.776 0.000171 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 33.99 on 846 degrees of freedom
## Multiple R-squared:  0.5392, Adjusted R-squared:  0.5299
## F-statistic: 58.23 on 17 and 846 DF,  p-value: < 2.2e-16
```

We use `lmer` from the `lme4` package to create a varying intercept model.

```
fit_vint <- lmer(diff ~ sex + (1 | new_ID), data = natsap_tidy)
summary(fit_vint)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: diff ~ sex + (1 | new_ID)
## Data: natsap_tidy
##
## REML criterion at convergence: 8543.9
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.7631 -0.6638 -0.0647  0.6633  3.8548
##
## Random effects:
## Groups Name Variance Std.Dev.
## new_ID (Intercept) 47.93 6.923
## Residual 1160.66 34.068
## Number of obs: 863, groups: new_ID, 16
##
## Fixed effects:
## Estimate Std. Error t value
## (Intercept) 28.908 2.815 10.268
## sex1 10.251 3.147 3.257
##
## Correlation of Fixed Effects:
## (Intr)
## sex1 -0.480
```

```
coef(fit_vint)
```

```
## $new_ID
## (Intercept) sex1
## 1 36.34895 10.25091
## 2 33.87791 10.25091
## 3 22.91950 10.25091
## 4 32.08647 10.25091
## 5 32.95377 10.25091
## 6 27.01840 10.25091
## 7 22.47676 10.25091
## 8 30.64451 10.25091
## 9 25.98757 10.25091
## 10 25.19569 10.25091
## 11 28.13625 10.25091
## 12 26.31753 10.25091
## 13 28.26403 10.25091
```

```
## 14      35.99240 10.25091
## 15      32.62698 10.25091
## 16      21.67361 10.25091
##
## attr(,"class")
## [1] "coef.mer"
```

```
fixef(fit_vint)
```

```
## (Intercept)      sex1
##      28.90752    10.25091
```

```
ranef(fit_vint)
```

```
## $new_ID
##      (Intercept)
## 1      7.4414340
## 2      4.9703946
## 3     -5.9880203
## 4      3.1789487
## 5      4.0462530
## 6     -1.8891183
## 7     -6.4307621
## 8      1.7369903
## 9     -2.9199515
## 10     -3.7118311
## 11     -0.7712724
## 12     -2.5899934
## 13     -0.6434942
## 14      7.0848797
## 15      3.7194570
## 16     -7.2339141
```

## Hierarchical models

Now we add a group-level predictor.

```
## We need to grab the minutes of individual and group therapy for each individual
## as well as the value of rtc_vs_obh
minutes_ind_therapy_full <- minutes_ind_therapy[natsap_tidy$new_ID,]
minutes_group_therapy_full <- minutes_group_therapy[natsap_tidy$new_ID,]
rtc_vs_obh_full <- rtc_vs_obh[natsap_tidy$new_ID,]
```

```
## The model for individual therapy
fit_hier_vint_ind <- lmer(diff ~ sex + minutes_ind_therapy_full + (1 | new_ID),
  data = natsap_tidy)
summary(fit_hier_vint_ind)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: diff ~ sex + minutes_ind_therapy_full + (1 | new_ID)
```

```
## Data: natsap_tidy
##
## REML criterion at convergence: 8543
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.7689 -0.6642 -0.0800  0.6597  3.8790
##
## Random effects:
##   Groups   Name      Variance Std.Dev.
## new_ID    (Intercept)  41.38   6.433
## Residual                1158.80  34.041
## Number of obs: 863, groups: new_ID, 16
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept)      11.4863     9.7812   1.174
## sex1              9.8440     3.1264   3.149
## minutes_ind_therapy_full  0.2101     0.1136   1.849
##
## Correlation of Fixed Effects:
##              (Intr) sex1
## sex1          -0.037
## mnts_nd_th_   -0.961 -0.104
```

```
coef(fit_hier_vint_ind)
```

```
## $new_ID
##      (Intercept)      sex1 minutes_ind_therapy_full
## 1      12.692015  9.84404              0.2100665
## 2      20.321421  9.84404              0.2100665
## 3       4.436198  9.84404              0.2100665
## 4      14.782601  9.84404              0.2100665
## 5      14.548760  9.84404              0.2100665
## 6      12.631598  9.84404              0.2100665
## 7       4.704809  9.84404              0.2100665
## 8      12.257755  9.84404              0.2100665
## 9       8.818625  9.84404              0.2100665
## 10     8.591075  9.84404              0.2100665
## 11    10.039295  9.84404              0.2100665
## 12    10.163037  9.84404              0.2100665
## 13    11.764479  9.84404              0.2100665
## 14    15.708342  9.84404              0.2100665
## 15    13.972065  9.84404              0.2100665
## 16     8.349225  9.84404              0.2100665
##
## attr(,"class")
## [1] "coef.mer"
```

```
fixef(fit_hier_vint_ind)
```

```
##              (Intercept)              sex1 minutes_ind_therapy_full
##              11.4863312              9.8440396              0.2100665
```

```
ranef(fit_hier_vint_ind)
```

```
## $new_ID
##      (Intercept)
## 1      1.2056835
## 2      8.8350894
## 3     -7.0501332
## 4      3.2962695
## 5      3.0624292
## 6      1.1452673
## 7     -6.7815226
## 8      0.7714235
## 9     -2.6677063
## 10    -2.8952561
## 11    -1.4470364
## 12    -1.3232937
## 13     0.2781475
## 14     4.2220106
## 15     2.4857339
## 16    -3.1371062
```

```
## The model for group therapy
fit_hier_vint_group <- lmer(diff ~ sex + minutes_group_therapy_full + (1 | new_ID),
  data = natsap_tidy)
summary(fit_hier_vint_group)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: diff ~ sex + minutes_group_therapy_full + (1 | new_ID)
## Data: natsap_tidy
##
## REML criterion at convergence: 8549.6
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.7945 -0.6550 -0.0777  0.6561  3.8525
##
## Random effects:
## Groups Name Variance Std.Dev.
## new_ID (Intercept) 47.67 6.904
## Residual 1160.05 34.060
## Number of obs: 863, groups: new_ID, 16
##
## Fixed effects:
## Estimate Std. Error t value
## (Intercept) 26.03484 3.66702 7.100
## sex1 9.17485 3.26793 2.808
## minutes_group_therapy_full 0.01301 0.01067 1.219
##
## Correlation of Fixed Effects:
## (Intr) sex1
## sex1 -0.180
## mnts_grp_t_ -0.642 -0.272
```

```
coef(fit_hier_vint_group)
```

```
## $new_ID
##      (Intercept)      sex1 minutes_group_therapy_full
## 1      32.19759 9.174851          0.01300868
## 2      33.65476 9.174851          0.01300868
## 3      19.84313 9.174851          0.01300868
## 4      29.24788 9.174851          0.01300868
## 5      24.52858 9.174851          0.01300868
## 6      25.23230 9.174851          0.01300868
## 7      20.74705 9.174851          0.01300868
## 8      27.82258 9.174851          0.01300868
## 9      23.17545 9.174851          0.01300868
## 10     22.28396 9.174851          0.01300868
## 11     25.95519 9.174851          0.01300868
## 12     23.64197 9.174851          0.01300868
## 13     24.41831 9.174851          0.01300868
## 14     32.10732 9.174851          0.01300868
## 15     31.08569 9.174851          0.01300868
## 16     20.61569 9.174851          0.01300868
##
## attr(,"class")
## [1] "coef.mer"
```

```
fixef(fit_hier_vint_group)
```

```
##              (Intercept)              sex1
##              26.03484110              9.17485096
## minutes_group_therapy_full
##              0.01300868
```

```
ranef(fit_hier_vint_group)
```

```
## $new_ID
##      (Intercept)
## 1      6.16275086
## 2      7.61992062
## 3     -6.19171601
## 4      3.21304313
## 5     -1.50626568
## 6     -0.80254248
## 7     -5.28779125
## 8      1.78773763
## 9     -2.85938662
## 10    -3.75087803
## 11    -0.07964723
## 12    -2.39286836
## 13    -1.61653492
## 14     6.07248049
## 15     5.05085118
## 16    -5.41915332
```



```
## The model for rtc_vs_obh
fit_hier_vint_rtc_vs_obh <-
  lmer(diff ~ sex + rtc_vs_obh_full + (1 | new_ID),
    data = natsap_tidy)
summary(fit_hier_vint_rtc_vs_obh)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: diff ~ sex + rtc_vs_obh_full + (1 | new_ID)
## Data: natsap_tidy
##
## REML criterion at convergence: 8538.4
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.7707 -0.6643 -0.0708  0.6585  3.8636
##
## Random effects:
## Groups Name Variance Std.Dev.
## new_ID (Intercept) 55.09 7.422
## Residual 1160.24 34.062
## Number of obs: 863, groups: new_ID, 16
##
## Fixed effects:
## Estimate Std. Error t value
## (Intercept) 27.371 3.966 6.902
## sex1 9.779 3.219 3.038
## rtc_vs_obh_fullRTC 3.091 5.273 0.586
##
## Correlation of Fixed Effects:
## (Intr) sex1
## sex1 -0.232
## rtc_vs__RTC -0.675 -0.158
```

```
coef(fit_hier_vint_rtc_vs_obh)
```

```
## $new_ID
## (Intercept) sex1 rtc_vs_obh_fullRTC
## 1 34.04058 9.779137 3.090692
## 2 33.88019 9.779137 3.090692
## 3 19.92421 9.779137 3.090692
## 4 30.83223 9.779137 3.090692
## 5 30.57035 9.779137 3.090692
## 6 24.48985 9.779137 3.090692
## 7 21.57263 9.779137 3.090692
## 8 29.14231 9.779137 3.090692
## 9 23.93332 9.779137 3.090692
## 10 23.05755 9.779137 3.090692
## 11 27.41238 9.779137 3.090692
## 12 24.13584 9.779137 3.090692
## 13 26.30809 9.779137 3.090692
## 14 34.64973 9.779137 3.090692
## 15 32.59463 9.779137 3.090692
## 16 21.39657 9.779137 3.090692
```

```
##
## attr("class")
## [1] "coef.mer"
```

```
fixef(fit_hier_vint_rtc_vs_obh)
```

```
##      (Intercept)          sex1 rtc_vs_obh_fullRTC
##      27.371280      9.779137      3.090692
```

```
ranef(fit_hier_vint_rtc_vs_obh)
```

```
## $new_ID
##      (Intercept)
## 1  6.66930227
## 2  6.50890624
## 3 -7.44706594
## 4  3.46095417
## 5  3.19907154
## 6 -2.88142799
## 7 -5.79865148
## 8  1.77102889
## 9 -3.43795740
## 10 -4.31372934
## 11  0.04110205
## 12 -3.23543706
## 13 -1.06319122
## 14  7.27845209
## 15  5.22335270
## 16 -5.97470951
```

Let's try to plot something.

```
## Without having to load the arm package, we can still use the handy
## functions se.fixef and se.ranef
se.fixef <- function (object)
{
  fcoef.name <- names(fixef(object))
  corF <- vcov(object)$factors$correlation
  ses <- corF@sd
  names(ses) <- fcoef.name
  return(ses)
}

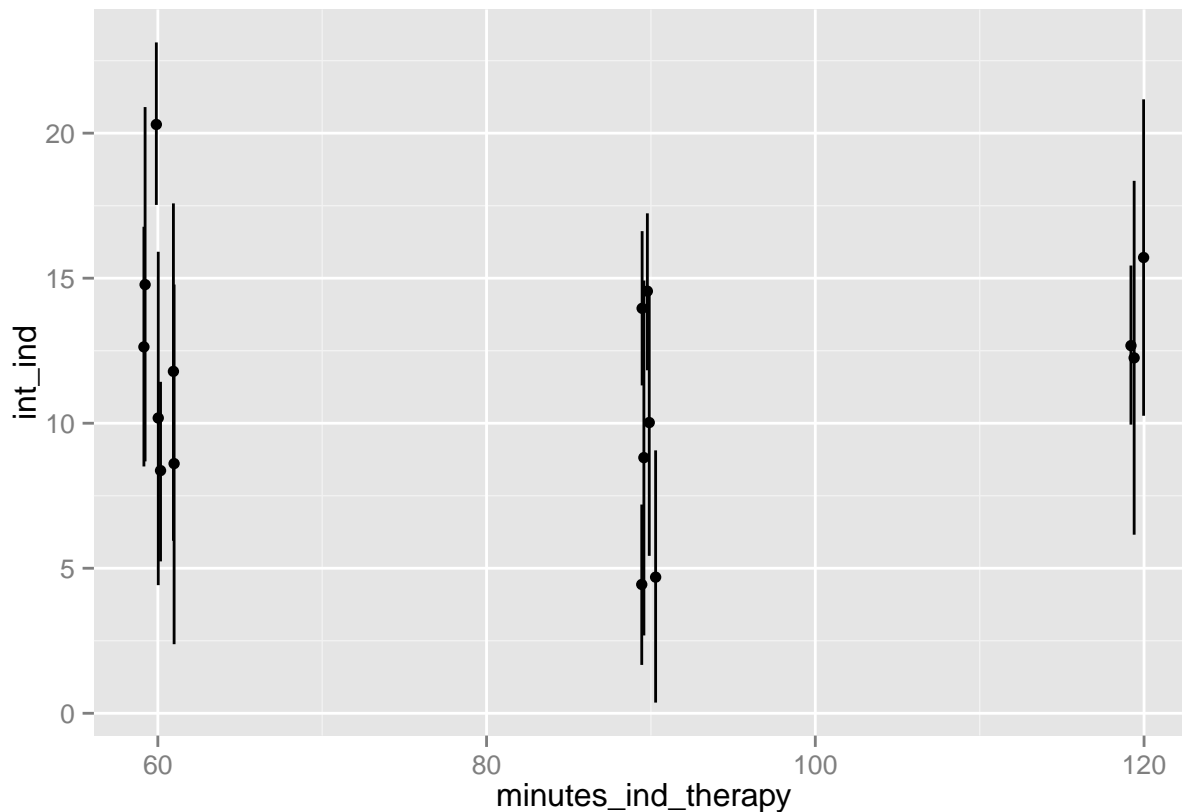
se.ranef <- function (object)
{
  se.bygroup <- ranef(object, condVar = TRUE)
  n.groupings <- length(se.bygroup)
  for (m in 1:n.groupings) {
    vars.m <- attr(se.bygroup[[m]], "postVar")
    K <- dim(vars.m)[1]
    J <- dim(vars.m)[3]
    names.full <- dimnames(se.bygroup[[m]])
```

```

se.bygroup[[m]] <- array(NA, c(J, K))
for (j in 1:J) {
  se.bygroup[[m]][j, ] <- sqrt(diag(as.matrix(vars.m[,
    , j])))
}
dimnames(se.bygroup[[m]]) <- list(names.full[[1]], names.full[[2]])
}
return(se.bygroup)
}

## Extract coefficients for minutes of individual therapy
int_ind <-coef(fit_hier_vint_ind)$new_ID[,1]
se_int_ind <- se.ranef(fit_hier_vint_ind)$new_ID[,1]
int_by_ind <-
  data.frame(dose_tidy$new_ID, minutes_ind_therapy, int_ind, se_int_ind)
limits_ind <- aes(ymax = int_ind + se_int_ind, ymin = int_ind - se_int_ind)
ggplot(int_by_ind, aes(x = minutes_ind_therapy, y = int_ind)) +
  geom_pointrange(limits_ind, position = position_jitter(width = 1))

```

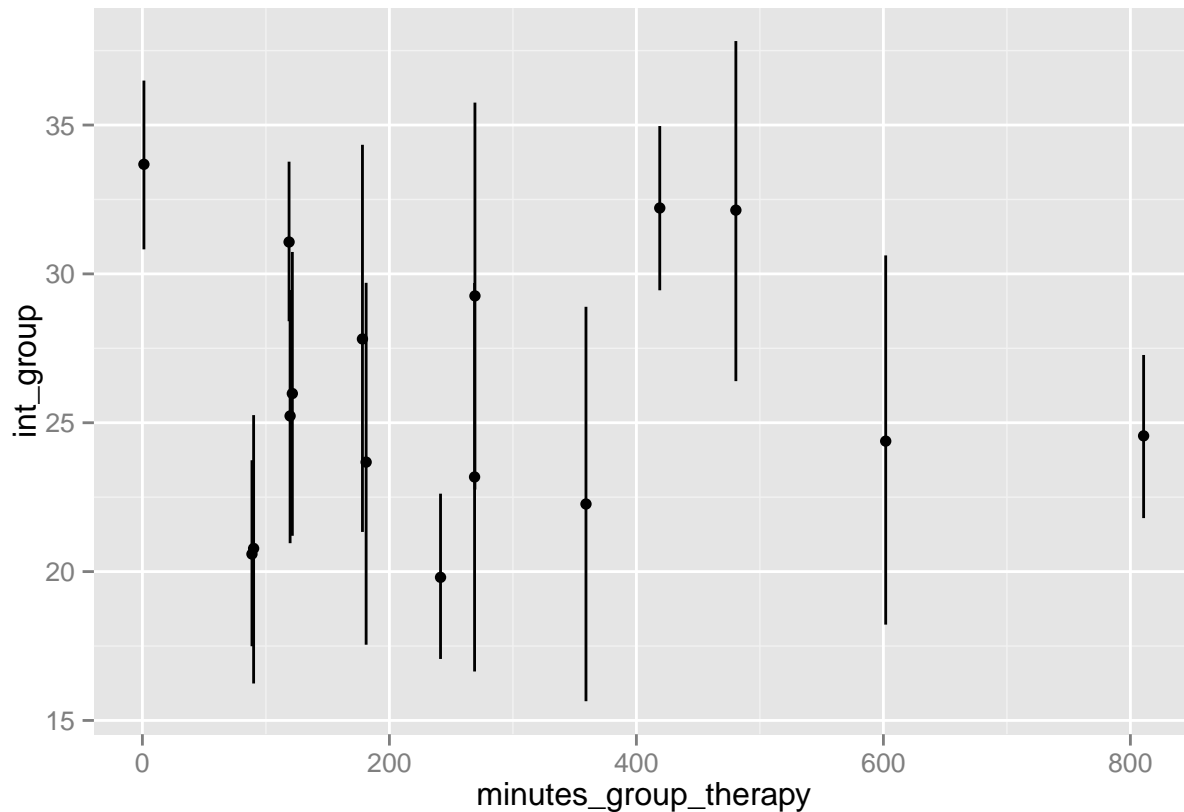


```

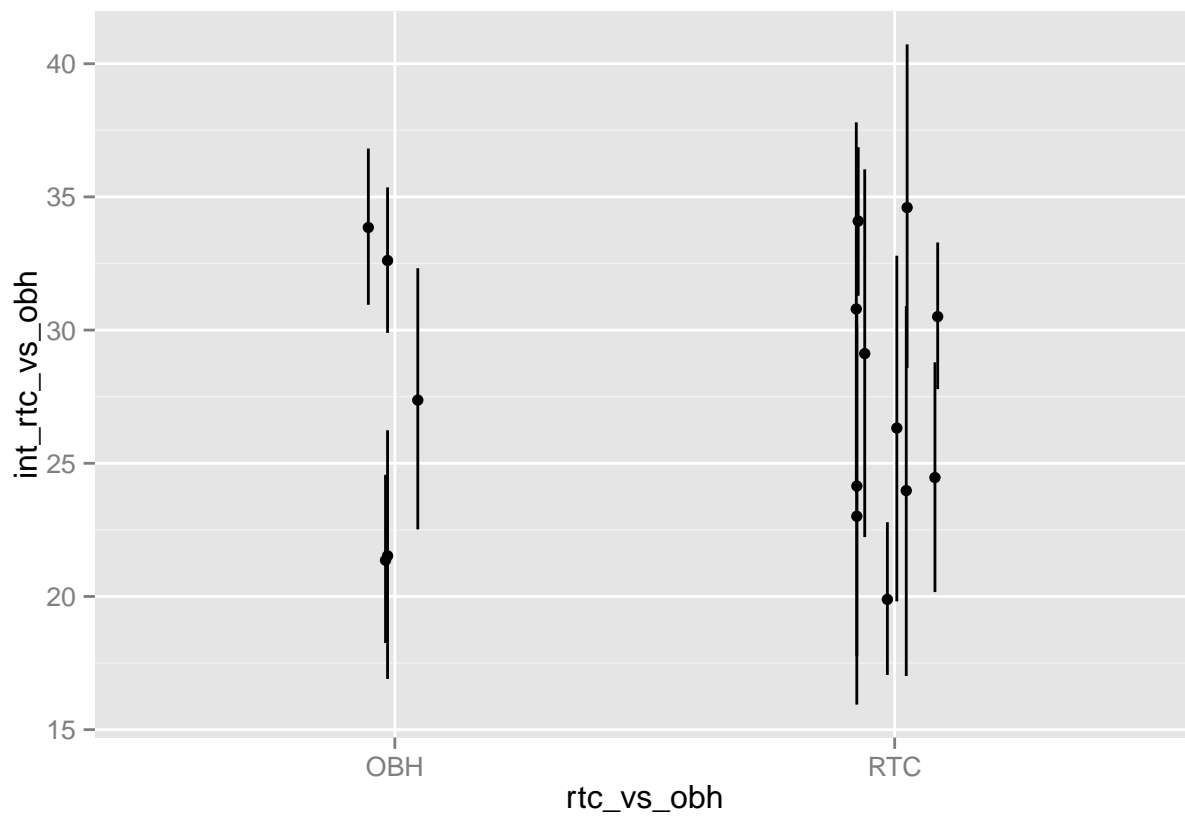
## Extract coefficients for minutes of group therapy
int_group <-coef(fit_hier_vint_group)$new_ID[,1]
se_int_group <- se.ranef(fit_hier_vint_group)$new_ID[,1]
int_by_group <-
  data.frame(dose_tidy$new_ID, minutes_group_therapy, int_group, se_int_group)
limits_group <- aes(ymax = int_group + se_int_group, ymin = int_group - se_int_group)

```

```
ggplot(int_by_group, aes(x = minutes_group_therapy, y = int_group)) +
  geom_pointrange(limits_group, position = position_jitter(width = 2))
```



```
## Extract coefficients for rtc_vs_obh
int_rtc_vs_obh <- coef(fit_hier_vint_rtc_vs_obh)$new_ID[,1]
se_int_rtc_vs_obh <- se.ranef(fit_hier_vint_rtc_vs_obh)$new_ID[,1]
int_by_rtc_vs_obh <-
  data.frame(dose_tidy$new_ID, rtc_vs_obh, int_rtc_vs_obh, se_int_rtc_vs_obh)
limits_rtc_vs_obh <- aes(ymax = int_rtc_vs_obh + se_int_rtc_vs_obh,
  ymin = int_rtc_vs_obh - se_int_rtc_vs_obh)
ggplot(int_by_rtc_vs_obh, aes(x = rtc_vs_obh, y = int_rtc_vs_obh)) +
  geom_pointrange(limits_rtc_vs_obh, position = position_jitter(width = 0.1))
```



This all looks fine, but we perform a check to make sure that errors bars really are correlated with sample size.

```
## Sample size check
sample_check <- data.frame(dose_tidy$new_ID, n = dose_tidy$n, rtc_vs_obh, int_rtc_vs_obh, se_int_rtc_vs_obh)
ggplot(sample_check, aes(x = n, y = int_rtc_vs_obh)) +
  geom_pointrange(limits_rtc_vs_obh, position = position_jitter(width = 0.1))
```

