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EE16A Homework 11

Question 1: Mechanical Correlation

```
In [51]: import numpy as np
         def vector compare(desired vec, test vec):
             """This function compares two vectors, returning a number.
             The test vector with the highest return value is regarded as being closest to the
             # Hint: Use transpose for the first argument of np.dot
             # YOUR CODE HERE
             return np.dot(np.transpose(desired vec), test vec)
         def crossCorrelate(vec1, vec2):
             output = []
             for i in range(len(vec2)):
                 output.append(vector_compare(vec1, vec2))
                 vec2 = np.roll(vec2, 1)
             return output
         def autoCorrelate(vec1):
             return crossCorrelate(vec1, vec1)
         array1 = np.array([2, -2, 2, -2, -2, -2, 2, 2])
         array2 = np.array([1, 2, 3, 4, 5, 6, 7, 6, 5, 4])
         print (autoCorrelate(array1))
         print (crossCorrelate(array1, array2))
         [40, -8, 8, -8, 8, -40, 8, -8, 8, -8]
         [-6, 6, 10, 22, 18, 6, -6, -10, -22, -18]
```

Question 2: GPS Receivers

```
In [52]: %pylab inline
import numpy as np
import matplotlib.pyplot as plt
import scipy.io
```

Populating the interactive namespace from numpy and matplotlib

```
In [53]: ## RUN THIS FUNCTION BEFORE YOU START THIS PROBLEM
         ## This function will generate the gold code associated with the satellite ID using li
         ## The satellite_ID can be any integer between 1 and 24
         def Gold_code_satellite(satellite_ID):
             codelength = 1023
             registerlength = 10
             # Defining the MLS for G1 generator
             register1 = -1*np.ones(registerlength)
             MLS1 = np.zeros(codelength)
             for i in range(codelength):
                 MLS1[i] = register1[9]
                 modulo = register1[2]*register1[9]
                 register1 = np.roll(register1,1)
                 register1[0] = modulo
             \# Defining the MLS for G2 generator
             register2 = -1*np.ones(registerlength)
             MLS2 = np.zeros(codelength)
             for j in range(codelength):
                 MLS2[j] = register2[9]
                 modulo = register2[1]*register2[2]*register2[5]*register2[7]*register2[8]*regi
                 register2 = np.roll(register2,1)
                 register2[0] = modulo
             delay = np.array([5,6,7,8,17,18,139,140,141,251,252,254,255,256,257,258,469,470,47
             G1 out = MLS1;
             shamt = delay[satellite ID - 1]
             G2 out = np.roll(MLS2, shamt)
             CA code = G1 out * G2 out
             return CA_code
```

Part (a)

```
In [58]: # Can see huge amount of noise

def array_correlation(array1, array2):
    """ This function should return two arrays or a matrix with one row corresponding the offset and other to the correlation value
    """

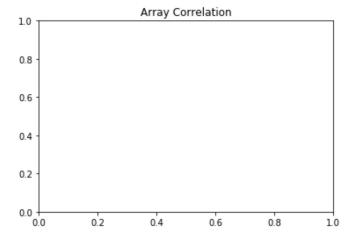
    return np.correlate(array1, array2, full)

# Plot the auto-correlation of satellite 10 with itself. Your signal should be centere # at offset = 0.
# Use plt.plot or plt.stem to plot.

# Plot the autocorrelation:
plt.title("Array Correlation")
corr = array_correlation(Gold_code_satellite(10), Gold_code_satellite(10))
plt.plot(corr)
```

```
TypeError
                                          Traceback (most recent call last)
<ipython-input-58-a4b044904941> in <module>()
     14 # Plot the autocorrelation:
     15 plt.title("Array Correlation")
---> 16 corr = array correlation(Gold code satellite(10), Gold code satellite(10))
     17 plt.plot(corr)
<ipython-input-58-a4b044904941> in array correlation(array1, array2)
      6
      7
----> 8
           return np.correlate(array1, array2, full)
     10 # Plot the auto-correlation of satellite 10 with itself. Your signal shoul
d be centered
C:\Program Files\Anaconda\lib\site-packages\numpy\core\numeric.py in correlate(a,
v, mode)
            11 11 11
    973
    974
          mode = _mode_from_name(mode)
          return multiarray.correlate2(a, v, mode)
--> 975
    976
    977
```

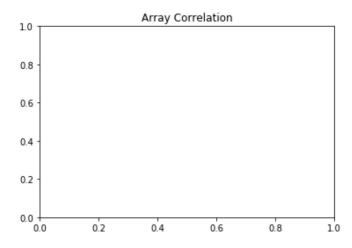
TypeError: an integer is required (got type function)



Part (b)

```
In [59]: plt.title("Array Correlation")
        corr = array_correlation(Gold_code_satellite(10), Gold_code_satellite(13))
        plt.plot(corr)
        ______
                                               Traceback (most recent call last)
        <ipython-input-59-5bfc934b72c5> in <module>()
              1 plt.title("Array Correlation")
        ----> 2 corr = array_correlation(Gold_code_satellite(10), Gold_code_satellite(13))
              3 plt.plot(corr)
        <ipython-input-58-a4b044904941> in array_correlation(array1, array2)
              6
              7
        ----> 8
                   return np.correlate(array1, array2, full)
             10 # Plot the auto-correlation of satellite 10 with itself. Your signal shoul
        d be centered
        C:\Program Files\Anaconda\lib\site-packages\numpy\core\numeric.py in correlate(a,
        v, mode)
            973
            974
                   mode = mode from name(mode)
        --> 975
                   return multiarray.correlate2(a, v, mode)
            976
```

TypeError: an integer is required (got type function)



Part (c)

977

```
In []: ## THIS IS A HELPER FUNCTION FOR PART C
    def integernoise_generator(length_of_noise):
        noise_array = np.random.randint(2, size = length_of_noise)
        noise_array = 2 * noise_array - np.ones(size(noise_array))
        return noise_array

plt.title("Array Correlation")
    corr = array_correlation(Gold_code_satellite(10), Gold_code_satellite(13))
    plt.plot(corr)
```

Part (d)

```
In []: ## THIS IS A HELPER FUNCTION FOR PART D

def gaussiannoise_generator(length_of_noise):
    noise_array = np.random.normal(0, 1, length_of_noise)
    return noise_array

plt.title("Array Correlation")
    corr = array_correlation(Gold_code_satellite(10), gaussiannoise_generator(1023))
    plt.plot(corr)
```

Part (e)

```
In []: ## USE 'np.load' FUNCTION TO LOAD THE DATA
## USE DATA1.NPY AS THE SIGNAL ARRAY

# YOUR CODE HERE
```

Part (f)

```
In []: ## USE DATA2.NPY AS THE SIGNAL ARRAY

# YOUR CODE HERE
```

Part (g)

In [26]: %matplotlib inline

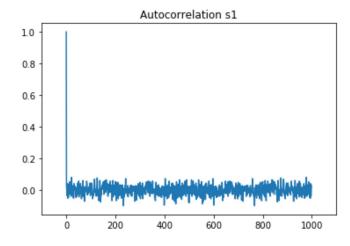
```
In [ ]: ## USE DATA3.NPY AS THE SIGNAL ARRAY

# YOUR CODE HERE
```

Question 3: Finding Signals in Noise

Part (a)

```
In [35]: # Generate a random normalized vector for s1
          # Running this cell again will generate a new random vector
          s1 = rand_normed_vector(N)
          # Compute all the inner products of s1 with shifted versions of s1
          # (i.e., the cross-correlation of s1 with s1)
          corr = cross_corr(s1, s1)
          # The inner product \langle s1, s1^{(1)} \rangle is:
          print(corr[1])
          # np.roll circularly shifts the signal,
          # so the above inner product could be computed as:
          print(np.dot(s1, np.roll(s1,1)))
          # Plot the autocorrelation:
          plt.title("Autocorrelation s1")
          plt.plot(corr)
          x1, x2, y1, y2 = plt.axis()
          plt.axis([x1-50, x2+50, y1, y2])
          0.028
```



Part (b)

0.028

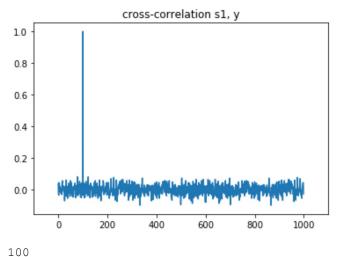
```
In [37]: y = np.roll(s1, 100) # Received y = s1 shifted by 10

# Compute the cross-correlation (all the inner products of y with shifted versions of corr = cross_corr(s1, y)

# Plot plt.title("cross-correlation s1, y") plt.plot(corr)

x1,x2,y1,y2 = plt.axis() plt.axis([x1-50,x2+50,y1,y2]) plt.show()

# Find the index of maximum correlation (inner product) print(np.argmax(corr))
```



Part (c)

0.054

Part (d)

This is the code from part (b) but with the received signal \vec{y} , which is corrupted by noise.

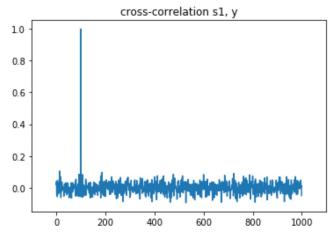
```
In [42]: s1 = rand_normed_vector(N)
    n = rand_normed_vector(N)
    y = np.roll(s1, 100) + 0.1*n

corr = cross_corr(s1, y)

plt.title("cross-correlation s1, y")
plt.plot(corr)

x1,x2,y1,y2 = plt.axis()
plt.axis([x1-50,x2+50,y1,y2])
plt.show()

# Find the index of maximum correlation (inner product)
```

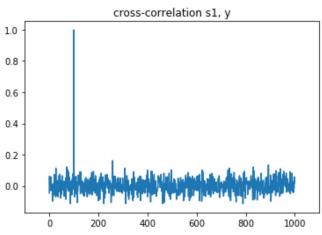


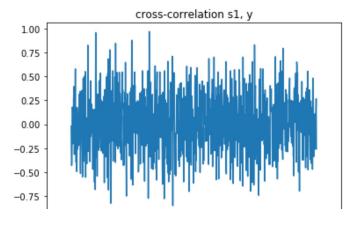
Out[42]: 100

Part (e)

Copy the code provided for part (d), but modify it appropriately, so that the noise is higher. You should generate two cross-correlation plots, one for each noise level in the question. (You can just copy the code from part (d) twice.)

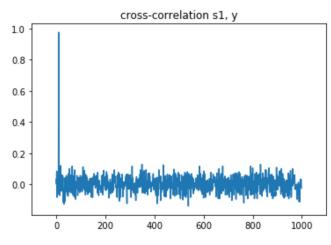
```
In [43]: | s1 = rand_normed_vector(N)
         n = rand_normed_vector(N)
         y = np.roll(s1, 100) + n
         corr = cross_corr(s1, y)
         plt.title("cross-correlation s1, y")
         plt.plot(corr)
         x1, x2, y1, y2 = plt.axis()
         plt.axis([x1-50, x2+50, y1, y2])
         plt.show()
         # Find the index of maximum correlation (inner product)
         np.argmax(corr)
         s1 = rand_normed_vector(N)
         n = rand_normed_vector(N)
         y = np.roll(s1, 100) + 10*n
         corr = cross_corr(s1, y)
         plt.title("cross-correlation s1, y")
         plt.plot(corr)
         x1, x2, y1, y2 = plt.axis()
         plt.axis([x1-50,x2+50,y1,y2])
         plt.show()
          # Find the index of maximum correlation (inner product)
```

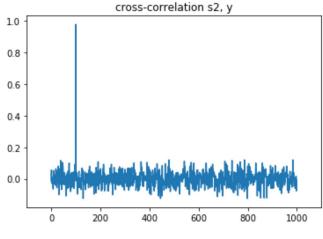




Part (f)

```
In [44]: s1 = rand normed vector(N)
         s2 = rand_normed_vector(N)
         y = np.roll(s1, 10) + np.roll(s2, 100)
          # Compute cross-correlations:
         corr_s1_y = cross_corr(s1, y)
         corr_s2_y = cross_corr(s2, y)
         # Plot cross-correlations:
         plt.title("cross-correlation s1, y")
         plt.plot(cross corr(s1, y))
         x1, x2, y1, y2 = plt.axis()
         plt.axis([x1-50,x2+50,y1,y2])
         plt.show()
         plt.title("cross-correlation s2, y")
         plt.plot(cross corr(s2, y))
         x1, x2, y1, y2 = plt.axis()
         plt.axis([x1-50, x2+50, y1, y2])
         plt.show()
         j = np.argmax(corr_s1_y) # find the first signal delay (max index of correlation)
         k = np.argmax(corr_s2_y) # find the second signal delay
         print(j, k)
```



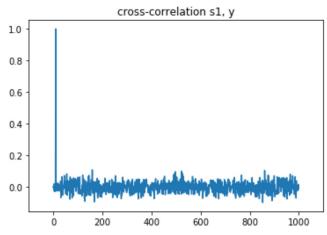


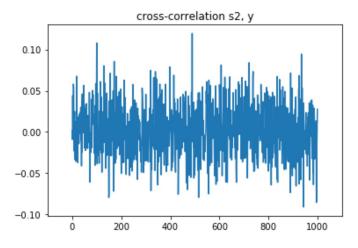
10 100

Part (g)

This is the same code as in part (f) but with a slight modification to how the received signal y generated. Run the below cell a few times to test for different choices of random signals.

```
In [45]: s1 = rand normed vector(N)
         s2 = rand normed vector(N)
         y = np.roll(s1, 10) + 0.1*np.roll(s2, 100)
          # Compute cross-correlations:
         corr s1 y = cross corr(s1, y)
         corr_s2_y = cross_corr(s2, y)
          # Plot cross-correlations:
         plt.title("cross-correlation s1, y")
         plt.plot(cross_corr(s1, y))
         x1,x2,y1,y2 = plt.axis()
         plt.axis([x1-50, x2+50, y1, y2])
         plt.show()
         plt.title("cross-correlation s2, y")
         plt.plot(cross_corr(s2, y))
         x1, x2, y1, y2 = plt.axis()
         plt.axis([x1-50,x2+50,y1,y2])
```





Part (h)

```
In [46]: corr_sl_y = cross_corr(sl, y)
    j = np.argmax(corr_sl_y) # find the first signal delay
    print(j)

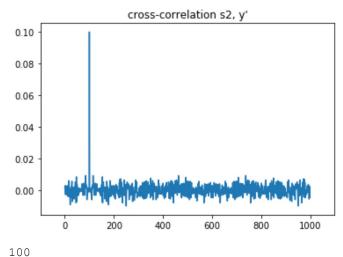
# Subtract out the contribution of the first signal
    y_prime = y - np.roll(sl, j)

# Correlate the residual against the second signal
    corr_s2_y = cross_corr(s2, y_prime)

# Plot
    plt.title("cross-correlation s2, y'")
    plt.plot(corr_s2_y)
    x1,x2,y1,y2 = plt.axis()
    plt.axis([x1-50,x2+50,y1,y2])
    plt.show()

k = np.argmax(corr_s2_y) # find the second signal delay by looking at the index of max
    print(k)
```

10



Part (i)

Part (j)

This is the same code as in part (i) but with noise added to the received signal \vec{y} .

```
In [48]: s1 = rand_normed_vector(N)
    s2 = rand_normed_vector(N)
    n = rand_normed_vector(N)

y = 0.7*np.rol1(s1, 10) + 0.5*np.rol1(s2, 100) + 0.1*n

corr_s1_y = cross_corr(s1, y)
    j = np.argmax(corr_s1_y) # find the first signal delay

corr_s2_y = cross_corr(s2, y)
    k = np.argmax(corr_s2_y) # find the second signal delay

print(j, k)

# Once we have found the shifts, estimate the coefficients as inner products:
    a1 = np.dot(y, np.rol1(s1, j))
    a2 = np.dot(y, np.rol1(s2, k))

print(a1, a2)

10 100
    0.7124 0.5188
```

Question 5: Image Analysis

```
In [ ]: def plot_circle(a, d, e):
            You can use this function to plot circles with parameters a,d,e.
            The parameters are described in the homework pdf.
            You can comment out the line that starts with `plt.title`
            because this makes assumptions regarding the title of your plot.
            is circle = d**2 + e**2 - 4*a > 0
            assert is circle, "Not a circle"
            XLIM LO = -1
            XLIM\ HI = 3
            YLIM LO = -2
            YLIM\ HI = 2
            X COUNT = 400
            Y COUNT = 400
            x = np.linspace(XLIM LO, XLIM HI, X COUNT)
            y = np.linspace(YLIM_LO, YLIM_HI, Y_COUNT)
            x, y = np.meshgrid(x, y)
            f = lambda x, y: a*(x**2 + y**2) + d*x + e*y
            c1 = plt.contour(x, y, f(x,y), [1], colors='r')
            plt.axis('scaled')
            plt.xlabel('x')
            plt.ylabel('y')
                                      In [ ]: def plot_ellipse(a, b, c, d, e):
            You can use this function to plot ellipses with parameters a-e.
            The parameters are described in the homework pdf.
            You can comment out the line that starts with `plt.title`
            because this makes assumptions regarding the title of your plot.
            is ellipse = b**2 - 4*a*c < 0
            assert is_ellipse, "Not an ellipse"
            XLIM LO = -1
            XLIM\ HI = 3
            YLIM LO = -2
            YLIM HI = 2
            X COUNT = 400
            Y COUNT = 400
            x = np.linspace(XLIM LO, XLIM HI, X COUNT)
            y = np.linspace(YLIM LO, YLIM HI, Y COUNT)
            x, y = np.meshgrid(x, y)
            f = lambda x, y: a*x**2 + b*x*y + c*y**2 + d*x + e*y
            c1 = plt.contour(x, y, f(x,y), [1], colors='r')
            plt.axis('scaled')
            plt.xlabel('x')
            plt.ylabel('y')
            plt.title(r'${:.2f}x^2 {:+.2f}yy {:+.2f}y^2 {:+.2f}y$'.format(a,b,c,d,e)}
In [ ]: | # Here is an example of plot_ellipse.
        # This plots (x-1)**2 + (y-1)**2 = 1,
        # which is a circle centered at (1,1).
        plt.figure(figsize=(6,6))
```

You may find plt.scatter (http://matplotlib.org/api/pyplot_api.html) useful for plotting the points.

Part (c)

```
In [ ]: def plot_circle(a, d, e):
           You can use this function to plot circles with parameters a,d,e.
           The parameters are described in the homework pdf.
           You can comment out the line that starts with `plt.title`
           because this makes assumptions regarding the title of your plot.
           is circle = d**2 + e**2 - 4*a > 0
           assert is_circle, "Not a circle"
           XLIM LO = -1
           XLIM\ HI = 3
           YLIM LO = -2
           YLIM HI = 2
           X COUNT = 400
           Y_COUNT = 400
           x = np.linspace(XLIM_LO, XLIM_HI, X_COUNT)
           y = np.linspace(YLIM LO, YLIM HI, Y COUNT)
           x, y = np.meshgrid(x, y)
           f = lambda x, y: a*(x**2 + y**2) + d*x + e*y
           c1 = plt.contour(x, y, f(x,y), [1], colors='r')
           plt.axis('scaled')
           plt.xlabel('x')
           plt.ylabel('y')
```

Part (d)

```
In [ ]: def plot_ellipse(a, b, c, d, e):
            You can use this function to plot ellipses with parameters a-e.
            The parameters are described in the homework pdf.
            You can comment out the line that starts with `plt.title`
            because this makes assumptions regarding the title of your plot.
            is ellipse = b**2 - 4*a*c < 0
            assert is_ellipse, "Not an ellipse"
            XLIM LO = -1
            XLIM HI = 3
            YLIM LO = -2
            YLIM\ HI = 2
            X COUNT = 400
            Y_COUNT = 400
            x = np.linspace(XLIM LO, XLIM HI, X COUNT)
            y = np.linspace(YLIM_LO, YLIM_HI, Y_COUNT)
            x, y = np.meshgrid(x, y)
            f = lambda x, y: a*x**2 + b*x*y + c*y**2 + d*x + e*y
            c1 = plt.contour(x, y, f(x,y), [1], colors='r')
            plt.axis('scaled')
            plt.xlabel('x')
            plt.ylabel('y')
            plt.title(r'\{:.2f\}x^2 {:+.2f}y^2 {:+.2f}y^2 {:+.2f}y$'.format(a,b,c,d,e)}
```