

REKA HW 2

(1) Mechanical Bar - Schrod

(A)  $U_1 = V_1$

$U_2 = V_2 - \langle V_2, U_1 \rangle U_1$

$U_3 = V_3 - \langle V_3, U_1 \rangle U_1 - \langle V_3, U_2 \rangle U_2$

$= [1 \ 0 \ 0 \ 0 \ 0]^T$

$U_2 = [0 \ 1/\sqrt{2} \ 1/\sqrt{2} \ 0 \ 0]^T$

$U_3 = [0 \ 0 \ 1/\sqrt{2} \ 1/\sqrt{2}]^T$

$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1/\sqrt{2} & 0 \\ 0 & 1/\sqrt{2} & 0 \\ 0 & 0 & 1/\sqrt{2} \\ 0 & 0 & 1/\sqrt{2} \end{bmatrix}$

$V(V^T V)^{-1} V^T U = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & -1 \\ 1 & 0 & 0 \\ 1 & -1 & 1 \\ 0 & -1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 3 & 3 \\ 1 & 3 & 5 \end{bmatrix}^{-1} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \\ 0 \\ -1 \\ 0 \end{bmatrix}$

$= \begin{bmatrix} 1 \\ -1/2 \\ -1/2 \\ -1/2 \\ -1/2 \end{bmatrix}$

(B)

$U_2 = \begin{bmatrix} 1 \\ 1 \\ 0 \\ -1 \\ -1 \end{bmatrix} - \left( \begin{bmatrix} 1 \\ 1 \\ 0 \\ -1 \\ -1 \end{bmatrix} \begin{bmatrix} 1/\sqrt{2} \\ 0 \\ 1/\sqrt{2} \\ 1/\sqrt{2} \\ 0 \end{bmatrix} \right) \begin{bmatrix} 1 \\ 1 \\ 0 \\ -1 \\ 1 \end{bmatrix} \quad U_2 = \begin{bmatrix} 1/\sqrt{2} \\ 1/\sqrt{2} \\ 0 \\ -1/2 \\ -1/2 \end{bmatrix}$

Projector =  $\begin{bmatrix} 1/4 \\ 0 \\ -1/4 \\ -1/4 \end{bmatrix}$

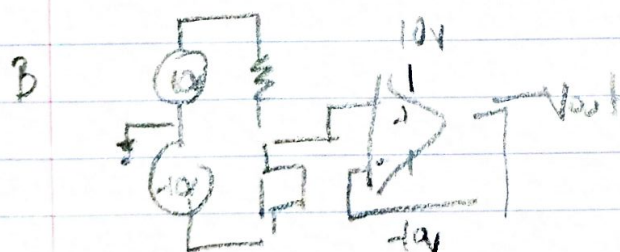
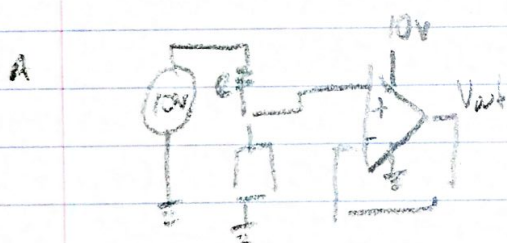
$$C \quad D_2 \begin{bmatrix} 1/\sqrt{3} & 0 & 1/\sqrt{3} & 1/\sqrt{3} & 0 \\ 1/2 & 1/2 & -1/2 & -1/2 & -1/2 \end{bmatrix} \begin{bmatrix} 1 & 1 & -1 \\ 0 & 1 & -1 \\ 1 & -1 & 1 \\ 0 & -1 & 1 \end{bmatrix} = \begin{bmatrix} \sqrt{3} & 0 & 0 \\ 0 & 2 & -2 \end{bmatrix}$$

2 How much is Too much  
- See IPython

3 Sparse Imaging  
- See IPython

4 Speeding Up OMP  
- See IPython

5 Pet Pet Design



6 Is 22168 fine  
yes, unless you don't so much

7 I would in this lower value