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Subject : AI

Assignment - 3

Date : 20-01-2024

Give the problem state formulation for 8 puzzle problem

Theory	<p>Here's the problem state formulation for the 8-puzzle problem:</p> <p>1. Initial State:</p> <p>Represented as a 3x3 grid, where each cell contains a number from 1 to 8, or a blank space (0).</p> <p>2. Goal State:</p> <p>A specific configuration of the tiles, typically arranged in ascending order with the blank space in the bottom right corner.</p> <p>3. Operators:</p> <p>Actions that can be performed to transition between states. In the 8-puzzle, the operators are moving the blank space up, down, left, or right, swapping its position with an adjacent tile.</p> <p>4. Successor Function:</p> <p>Given a state, generates the set of states that can be reached by applying a single operator.</p> <p>5. Path Cost:</p> <p>The cost associated with transitioning between states. In the 8-puzzle, each move typically has a cost of 1.</p> <p>6. Solution:</p> <p>A sequence of operators that transforms the initial state into the goal state.</p>
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	<p>Additional Considerations:</p> <p>Heuristic Function: An estimate of the cost to reach the goal state from a given state. Used for informed search algorithms like A*.</p> <p>State Space Size: The 8-puzzle has a state space of $9!/2 = 181,440$ states.</p> <p>Search Algorithm: Various search algorithms can be used to solve the 8-puzzle, including:</p> <ul style="list-style-type: none"> Breadth-First Search (BFS) Depth-First Search (DFS) A* Search Iterative Deepening A* (IDA*) <p>Minimum Step Count:</p> <p>The minimum number of steps required to solve any solvable 8-puzzle configuration is not fixed. It depends on the particular arrangement of tiles in the initial state.</p> <p>However, using an efficient algorithm like A* often leads to solutions that are close to the minimum possible number of steps.</p> <p>Additional Insights:</p> <p>While 31 steps might seem lengthy, it's worth noting that the 8-puzzle has a vast number of possible states (over 180,000). Finding a solution in a reasonable amount of time is a testament to the effectiveness of the A* algorithm.</p>
<p>Problem Formulation</p>	<p>1. State:</p> <p>Represented as a 3x3 grid, where each cell contains a number from 1 to 8, or a blank space (0).</p> <p>2. Initial State:</p> <p>The specific configuration of tiles at the beginning of the puzzle.</p> <p>Can be any arrangement of the tiles, as long as it's possible to reach the goal state from it.</p>

3. Transition Model:

Defines how to move from one state to another.

In the 8-puzzle, the actions are moving the blank space up, down, left, or right, swapping it with an adjacent tile.

4. Actions:

The specific moves that can be performed:

Move blank up

Move blank down

Move blank left

Move blank right

5. Goal Test:

A function that determines if a given state is the goal state.

In the 8-puzzle, the goal state is typically when the tiles are arranged in ascending order with the blank space in the bottom right corner.

6. Path Cost:

The cost associated with each move.

In the 8-puzzle, each move typically has a cost of 1.

Example:

State: 7 2 4 | 5 0 6 | 8 3 1

Initial State: Same as above

Transition Model: Move blank up, down, left, or right

Action: Move blank right

Goal Test: Tiles in ascending order, blank in bottom right

Path Cost: 1 (for each move)