

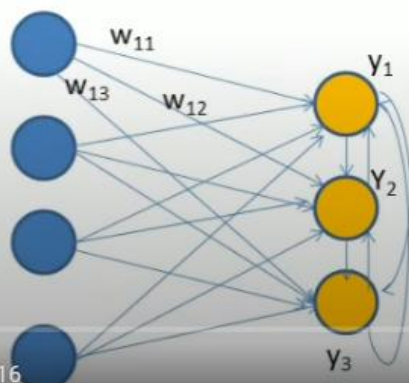
#### 4.1.1.1 Introduction to Competitive Learning

- Competitive learning is a type of unsupervised learning model used in machine learning and artificial intelligence systems.
- In this unsupervised training model output units are said to be in competition for input patterns. During training, the output unit that provides the highest activation to a given input pattern is declared the winner and its weights are moved closer to the input pattern, whereas the rest of the neurons are left unchanged.
- This strategy is also called winner-take-all since only the winning neuron is updated. Output units may have lateral inhibitory connections so that a winner neuron can inhibit others by an amount proportional to its activation level.
- The winner-take-all networks are the networks that are based on the competitive learning rule and will use the strategy where it chooses the neuron with the greatest total inputs as a winner. The connections between the output neurons show the competition between them and one of them would be 'ON' which means it would be the winner and others would be 'OFF'.

- The output neurons of a neural network compete among themselves to become active(fired).
- In Hebbain Learning, several output neurons may be active-but in Competitive-only single output neuron is active at any one time.
- This feature helps to classify a set of input patterns.

Three basic elements to competitive learning rule:

1. a set of neurons that are all the same (excepts for synaptic weights)
2. limit imposed on the strength of each neuron
3. a mechanism that permits the neurons to compete -> **a winner-takes-all**



inhibited connection at output layer  
excited connection btw input and output layer



0:02 / 13:16



## **components and their contributions to the network's function:.**

### **1. \*\*Input Layer\*\*:**

- The input layer receives the raw input data, which could be features from a dataset or sensory data from the environment.
- Each neuron in the input layer represents a feature or a component of the input data.

### **2. \*\*Competitive Layer (Winner-Take-All Layer)\*\*:**

- This layer contains neurons that compete with each other to become active.
- The competitive nature of this layer ensures that only one neuron becomes active at a time, typically the one with the highest activation or closest match to the input pattern.
- Neurons in this layer are often interconnected with lateral inhibitory connections, meaning when one neuron becomes active, it suppresses the activity of neighboring neurons.

### **3. \*\*Weights\*\*:**

- Each connection between neurons in the input layer and the competitive layer has an associated weight.
- These weights determine the strength of influence that each input feature has on the activation of neurons in the competitive layer.
- During training, the weights are adjusted to enhance the competition among neurons and improve the network's ability to recognize patterns.

### **4. \*\*Activation Function\*\*:**

- The activation function of the neurons in the competitive layer determines their output based on the weighted sum of inputs.
- Common activation functions used in competitive learning include the sigmoid, softmax, or threshold functions.
- The activation function helps in quantifying the similarity between the input pattern and the weights associated with each neuron.

### **5. \*\*Learning Rule\*\*:**

- Competitive learning typically employs a learning rule that updates the weights based on the input patterns and the competition among neurons.
- The most commonly used learning rule in competitive learning is Hebbian learning, where connections between neurons that are simultaneously active are strengthened.

### **6. \*\*Output Layer (optional)\*\*:**

- The output layer could perform additional processing or classification based on the winning neuron's activity in the competitive layer.

### **\*\*Advantages:\*\***

1. **\*\*Unsupervised Learning:\*\*** Competitive learning enables unsupervised learning, making it valuable for tasks where labeled data is scarce or unavailable.
2. **\*\*Self-Organization:\*\*** The network autonomously organizes input data into clusters or representations, facilitating pattern recognition and feature extraction.
3. **\*\*Efficiency:\*\*** It is computationally efficient, as it typically requires minimal computational resources compared to other learning paradigms.
4. **\*\*Robustness:\*\*** Competitive learning can adapt to changes in the input space, making it robust against variations and noise in the data.

### **\*\*Limitations:\*\***

1. **\*\*Sensitivity to Initialization:\*\*** Performance may depend heavily on the initial configuration of weights and parameters, leading to potential convergence issues.
2. **\*\*Limited Representational Power:\*\*** While effective for simple clustering tasks, competitive learning may struggle with complex data distributions or high-dimensional inputs.
3. **\*\*Difficulty in Scaling:\*\*** Scaling competitive learning to large datasets or high-dimensional spaces can be challenging due to computational constraints and memory requirements.
4. **\*\*Lack of Interpretability:\*\*** The resulting representations or clusters may lack interpretability, making it challenging to understand the underlying structure of the data.

### **Applications of competitive networks**

1. Vector quantization
2. Analyze raw data
3. Bibliographic classification
4. Image browsing systems
5. Medical diagnosis (visualization of data and
6. Speech recognition
7. Data compression
8. Separating sound sources
9. Environmental modeling
10. Feature extraction
11. Dimensionality reduction
12. Optimization



ART model is unsupervised in nature and consists of,

1. Input unit layer -  $L_1$  layer or the comparison field where in the inputs are processed.

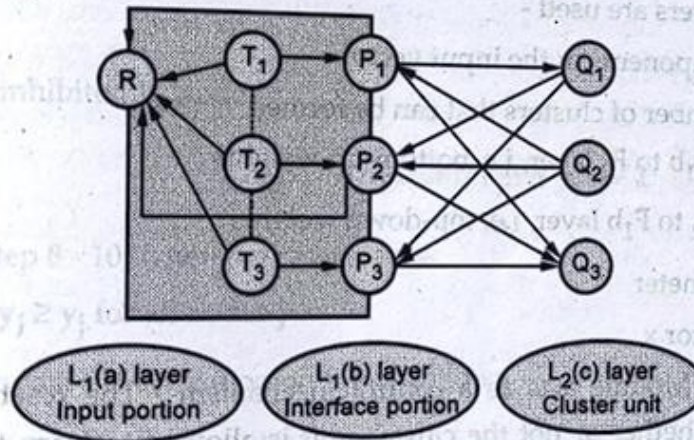


Fig. 4.1.6 ART1 - Layer 1

**L<sub>1a</sub> layer Input portion** - In ART1, there would be no processing in this portion rather than having the input vectors only. It is connected to F<sub>1b</sub> layer interface portion.

**L<sub>1b</sub> layer Interface portion** - This portion combines the signal from the input portion with that of F<sub>2</sub> layer. F<sub>1b</sub> layer is connected to F<sub>2</sub> layer through bottom up weights  $b_{ij}$  and F<sub>2</sub> layer is connected to F<sub>1b</sub> layer through top down weights  $t_{ji}$ .

2. Layer 2 - F<sub>2</sub> layer or the recognition field which consists of the clustering units. This is a competitive layer. The unit having the largest net input is selected to learn the input pattern. The activation of all other cluster unit are set to 0.

ART (Adaptive Resonance Theory) networks are a class of neural networks designed for unsupervised learning and pattern recognition tasks. One popular version of ART networks is the ART 1 network, which is designed for binary input patterns.

#### **\*\*i) Architecture (Input layer, Interface layer, Recognition layer):\*\***

- **\*\*Input Layer:\*\*** This layer receives the input data. In ART networks, the input is typically binary, consisting of binary features. Each node in this layer corresponds to an input feature.

- **Interface Layer:** This layer is responsible for comparing the input pattern with existing prototypes stored in memory. It computes the similarity between the input pattern and each stored prototype. This similarity computation often involves computing the dot product or some other similarity metric.

- **Recognition Layer:** This layer determines whether the input pattern matches an existing category or if it is distinct enough to form a new category. If the input pattern matches an existing category, it is assigned to that category. If not, a new category is created, and the input pattern becomes the prototype for that category.

### **ii) Working:**

1. **Input Presentation:** An input pattern is presented to the network.
2. **Comparison with Prototypes:** The input pattern is compared with existing prototypes stored in memory. This comparison is done in the interface layer using a similarity measure.
3. **Vigilance Test:** If the similarity between the input pattern and an existing prototype exceeds a certain threshold called the vigilance parameter, the input pattern is considered to match that prototype.
4. **Category Assignment:** If a match is found, the input pattern is assigned to the corresponding category. If not, a new category is created, and the input pattern becomes the prototype for this new category.
5. **Weight Update:** The network's weights are updated based on the matched prototype and the input pattern. This helps the network adapt to similar patterns in the future.

### **iii) Training:**

Training an ART network involves presenting a set of input patterns to the network and updating its weights and prototypes based on the input patterns and their similarity to existing prototypes. The vigilance parameter plays a crucial role during training, as it determines how similar an input pattern must be to an existing prototype to be considered a match. The training process continues until the network converges to a stable state, where further presentations of input patterns do not significantly alter the network's weights or categories.

**\*\*iv) Implementation:\*\***

```
def train(inputs,b,t,rho,learning_rate,n):
    print("Initially the Bottom-up weights b=",b,"\n")
    print("Initially the Top-down weights t = ",t,"\n")
    for s in inputs:
        print("S = ",s)
        norm_s=np.sum(s)
        print("||s|| = ",norm_s,"\n")
        x=s
        y=np.dot(x,b)
        print("y = bij*xi ",y)
        J=np.argmax(y)
        print("Winner J = ",J,"\n")

        xi=s*t[J]
        print("xi = Si*tJi = ",xi)
        norm_x=np.sum(xi)
        print("||x||",norm_x,"\n")
        test_reset=norm_x/norm_s
        print("||x||/||s|| = ",test_reset)
        print("rho = ",rho)
        if(test_reset>=rho):
            print("Reset is False \n")
            for i in range(n):
                b[i][J]=learning_rate*xi[i]/(learning_rate-1+norm_x)
                t[J][i]=xi[i]
            print("bij(new) = ",b,"\n")
            print("tji(new) = ",t,"\n")
```

### Types of Adaptive Resonance Theory (ART)

The ARTs can be classified as follows :

- **ART1** - It is the simplest and the basic ART architecture. It is capable of clustering binary input values.
- **ART2** - It is extension of ART1 that is capable of clustering continuous - valued input data.
- **Fuzzy ART** - It is the augmentation of fuzzy logic and ART.
- **ARTMAP** - It is a supervised form of ART learning where one ART learns based on the previous ART module. It is also known as predictive ART.
- **FARTMAP** - This is a supervised ART architecture with Fuzzy logic included.

### Advantages of Adaptive Learning Theory (ART)

1. It can be utilized with different techniques to give more precise outcomes.
2. It is stable and is not disturbed by a wide variety of inputs provided to its network.
3. It doesn't ensure any stability in forming clusters.
4. It can be used in variety fields such as face recognition, embedded system and robotics, target recognition, medical diagnosis, signature verification, etc.
5. It has benefit over competitive learning that the competitive learning can not include new clusters when considered necessary but ART can.

## **explanation of the ART (Adaptive Resonance Theory) network:**

ART networks are a class of neural networks designed for unsupervised learning and pattern recognition tasks

The key idea behind ART networks is to dynamically organize information into categories or clusters in a way that allows for incremental learning and adaptation to new patterns without forgetting previously learned knowledge

ART networks consist of multiple layers, including an input layer, an interface layer, and a recognition layer. These layers work together to compare incoming patterns with existing prototypes, create new categories if necessary, and update the network's internal representation of patterns

One of the most well-known variants of ART is the ART 1 network, which is designed for binary input patterns. It employs a mechanism called the vigilance parameter to control the creation of new categories based on the similarity between input patterns and existing prototypes.

Overall, ART networks provide a flexible framework for organizing and learning from data in a self-organizing manner, making them suitable for various applications such as pattern recognition, clustering, and cognitive modeling.

## **features of ART (Adaptive Resonance Theory) networks:**

1. **\*\*Unsupervised Learning\*\***: ART networks are primarily designed for unsupervised learning tasks, where the network learns to categorize input patterns without explicit guidance or labels.
2. **\*\*Incremental Learning\*\***: They support incremental learning, allowing the network to adapt to new input patterns without forgetting previously learned knowledge.
3. **\*\*Dynamic Category Formation\*\***: ART networks dynamically organize information into categories or clusters based on the similarity between input patterns and existing prototypes.
4. **\*\*Vigilance Control\*\***: They incorporate a vigilance parameter that controls the creation of new categories, determining the network's sensitivity to new input patterns.



5. **Flexible Architecture**: ART networks can have varying architectures, including different numbers of layers and nodes, making them adaptable to different tasks and data types.
6. **Robustness to Noise**: They exhibit robustness to noise and variations in input patterns, thanks to their ability to adjust the vigilance parameter and update category boundaries accordingly.
7. **Applications**: ART networks find applications in various domains, including pattern recognition, clustering, cognitive modeling, and adaptive control systems.

**ART (Adaptive Resonance Theory) can be utilized for character recognition tasks in the following steps:**

1. **Preprocessing**:

- Convert the characters into a suitable format, such as binary pixel representations or feature vectors. Normalize the input to ensure consistency across different characters.

2. **Network Setup**:

- Design an ART network architecture suitable for character recognition. This typically includes an input layer to receive the character representations, an interface layer for comparison, and a recognition layer to store prototypes of different characters.

3. **Training**:

- Present a dataset of labeled character images to the ART network.
- The network dynamically creates categories (prototypes) for different characters based on the similarity between input patterns and existing prototypes.
- Adjust the vigilance parameter to control the network's sensitivity to variations within characters and to determine when new categories should be created.



#### 4. **\*\*Recognition\*\***:

- Given a new character image, present it to the trained ART network.
- The network compares the input pattern with existing prototypes stored in the recognition layer.
- If a match is found above the vigilance threshold, the input pattern is classified as the corresponding character.
- If no match is found, a new category may be created if the input pattern sufficiently differs from existing prototypes.

#### 5. **\*\*Adaptation\*\***:

- As new character images are encountered, the ART network continues to adapt and refine its categories based on the input patterns it receives. This ensures that the network remains effective in recognizing characters even in the presence of variations or noise in the input data.

#### 6. **\*\*Evaluation and Refinement\*\***:

- Evaluate the performance of the ART network on a separate test dataset to assess its accuracy and generalization ability.
- Fine-tune the network parameters, such as the vigilance parameter and the network architecture, based on the evaluation results to improve performance if necessary.

By following these steps, ART can effectively learn to recognize characters from input images, demonstrating its capability for character recognition tasks.

Consider an ART-I network with input vector  $[1, 1, 0, 0]$ ,  $[0, 0, 1, 0]$ ,  $[1, 1, 1, 0]$  and  $[1, 1, 1, 1]$ , want to produce clustering with following data, number of inputs  $n = 4$ , clusters to be formed  $m = 3$  and vigilance parameter  $\rho = 0.5$ , Compute the result of the first iteration and comment on clustering

## Learning Vector Quantization

### 1. Input:

- Training data  $\{(\mathbf{x}_i, y_i)\}_{i=1}^N$ , where  $\mathbf{x}_i$  is the input vector and  $y_i$  is the corresponding class label.
- Initial prototypes  $\mathbf{w}_j$  with their class labels  $c_j$ .
- Learning rate  $\alpha$ .

### 2. Output: Adjusted prototypes.

### 3. Steps:

1. Initialize prototypes  $\mathbf{w}_j$  and assign each a label  $c_j$ .

2. For each training sample  $(\mathbf{x}_i, y_i)$ :  $D(j) = \sum_{i=1}^m (\mathbf{x}_i - \mathbf{w}_j)^2$

1. Find the nearest prototype  $\mathbf{w}_j$ .

2. Update the prototype:

- If  $c_j = y_i$ :

$$\mathbf{w}_j \leftarrow \mathbf{w}_j + \alpha(\mathbf{x}_i - \mathbf{w}_j)$$

- If  $c_j \neq y_i$ :

$$\mathbf{w}_j \leftarrow \mathbf{w}_j - \alpha(\mathbf{x}_i - \mathbf{w}_j)$$

3. Reduce  $\alpha$  over time.

4. Repeat until convergence or  $\downarrow$  a set number of iterations.

Learning Vector Quantization (LVQ) is a prototype-based supervised machine learning algorithm used for classification tasks. It's particularly useful for situations where the interpretability of the model is crucial, as it provides intuitive prototype vectors that can be easily understood and analyzed.

### ### Key Concepts

1. **Prototypes**: LVQ uses prototype vectors to represent different classes. Each prototype is associated with a specific class label.
2. **Training Process**: The algorithm adjusts the positions of the prototypes during training to better represent the data distribution for each class.

3. **Winner-Takes-All**: The class of the closest prototype (the one with the smallest Euclidean distance to the input vector) is used to predict the class of new input data.

### ### Training Procedure

1. **Initialization**:

- Start with a set of prototypes, each randomly initialized or derived from the training data.

2. **Iteration**:

- For each training sample, find the nearest prototype using Euclidean distance.

- Adjust the position of the prototype:

- **If the prototype's class matches the sample's class**: Move the prototype closer to the sample.

- **If the prototype's class does not match the sample's class**: Move the prototype away from the sample.

3. **Learning Rate**: The adjustment made to the prototype's position is controlled by a learning rate, which typically decreases over time to fine-tune the positions gradually.

### ### Advantages and Disadvantages

**Advantages**:

- **Interpretable**: The prototypes provide a clear, interpretable summary of the data.

- **Simple**: The algorithm is straightforward and easy to implement.

- **Fast**: Typically faster than more complex models like neural networks.



### **\*\*Disadvantages\*\*:**

- **\*\*Sensitive to Initialization\*\***: The choice of initial prototypes can significantly affect performance.
- **\*\*Not Ideal for Non-Euclidean Spaces\*\***: LVQ assumes Euclidean distance, which may not be suitable for all data types.
- **\*\*Requires Careful Tuning\*\***: Parameters such as learning rate and number of prototypes need to be carefully tuned.

### **### Applications**

LVQ is useful in various domains where interpretability and simplicity are essential, such as:

- Medical diagnosis
- Fraud detection
- Customer segmentation

In summary, LVQ is a powerful tool for classification tasks that require interpretable models and can be effectively used with careful initialization and parameter tuning.

**Vector Quantization (VQ)** is a technique that involves partitioning a large set of vectors into clusters, each represented by a prototype vector. These prototype vectors, often referred to as codebook vectors or centroids, serve as a compact representation of the clusters. The process involves quantizing vectors from a high-dimensional space to a finite number of regions or clusters, which can be used for various purposes, such as data compression, signal processing, and pattern recognition.

### ### Key Concepts

1. **Codebook**: A collection of prototype vectors, where each vector represents a cluster.
2. **Quantization**: The process of mapping input vectors to the nearest prototype vector in the codebook.
3. **Distortion Measure**: A metric, typically Euclidean distance, used to measure the similarity between vectors and prototype vectors.

### ### Vector Quantization Process

- Begin with an initial set of prototype vectors (codebook vectors), often chosen randomly or through methods like k-means clustering.
- Each input vector is assigned to the nearest prototype vector based on the chosen distortion measure.
- Adjust the prototype vectors to better represent the clusters formed by the assigned input vectors. This is typically done by computing the centroid of each cluster and updating the prototype vectors to these centroids.
- Repeat the assignment and update steps until convergence, i.e., until the changes in prototype vectors are below a certain threshold.

### ### Pattern Clustering with Vector Quantization

In the context of pattern clustering, VQ is used to group similar patterns into clusters. Each cluster is represented by a prototype vector, which serves as the "typical" example of patterns within that cluster.

#### #### Steps for Pattern Clustering

- A set of patterns (vectors) that need to be clustered.
- Choose an initial set of prototype vectors. This can be done using various methods, such as random selection or k-means initialization.
- For each pattern, find the nearest prototype vector (using a distance metric like Euclidean distance) and assign the pattern to the corresponding cluster.
- For each cluster, recompute the prototype vector as the mean of all patterns assigned to that cluster.
- Repeat the assignment and update steps until the prototype vectors stabilize (i.e., change very little between iterations).
- The process converges when the prototype vectors do not change significantly between iterations, indicating that the clusters are stable.

Training Process

Initialization:

Initialize the codebook vectors randomly or using a method such as k-means clustering.

Assignment Step:

For each input vector, find the nearest codebook vector and assign the input vector to that codebook vector.

Update Step:

Update the codebook vectors to better represent the assigned input vectors. This can be done by averaging the assigned input vectors.

Iteration:

Repeat the assignment and update steps until the codebook vectors converge or a stopping criterion is met.

### ### Applications of Vector Quantization

1. **Data Compression**: VQ is used to compress data by encoding vectors using the nearest prototype vector's index, reducing the amount of storage required.
2. **Image and Audio Compression**: Reduces the size of images and audio files by quantizing pixel or audio sample values.
3. **Pattern Recognition**: Used in speech and image recognition to cluster similar patterns and improve recognition accuracy.

4. **Signal Processing**: Helps in reducing noise and compressing signals by quantizing signal values.

### ### Advantages and Disadvantages

#### **Advantages**:

- **Data Compression**: Reduces the storage and transmission requirements.
- **Simplification**: Converts complex data into a simpler representation.
- **Improved Efficiency**: Speeds up processing by reducing the number of unique vectors to consider.

#### **Disadvantages**:

- **Lossy Compression**: Introduces some loss of information due to quantization.
- **Initialization Sensitivity**: The initial choice of prototype vectors can affect the final clustering result.
- **Computational Cost**: Iterative process can be computationally intensive for large datasets.



**Adaptive pattern classification** refers to a class of algorithms and techniques used to identify patterns within data that can adjust or "adapt" to new data over time. These methods are particularly useful in environments where the underlying data distribution is dynamic, meaning it changes or evolves, requiring the classification system to update its model to maintain accuracy.

1. **\*\*Dynamic Learning\*\***: Unlike static classifiers that are trained once on a fixed dataset, adaptive classifiers continuously learn from new data. This ongoing learning process helps the classifier to stay relevant and accurate as new patterns emerge.
2. **\*\*Incremental Learning\*\***: This involves updating the classifier incrementally with each new piece of data rather than retraining it from scratch. Techniques such as online learning or incremental learning algorithms are often employed.
3. **\*\*Concept Drift\*\***: Adaptive classifiers are designed to handle concept drift, which occurs when the statistical properties of the target variable change over time. Detecting and adapting to concept drift is crucial for maintaining the performance of the classifier.
4. **\*\*Ensemble Methods\*\***: Many adaptive classifiers use ensemble methods, combining multiple models to improve robustness and accuracy. Techniques such as boosting, bagging, and stacking can be adapted to update individual models within the ensemble as new data becomes available.
5. **\*\*Neural Networks and Deep Learning\*\***: Adaptive neural networks, including deep learning models, can adjust their weights in response to new data. Methods like transfer learning and continual learning help these models retain previously learned information while integrating new patterns.
6. **\*\*Reinforcement Learning\*\***: In some cases, adaptive pattern classification can be framed as a reinforcement learning problem, where the classifier receives feedback from its environment and adjusts its parameters to improve performance.

### ### Applications

1. **Financial Markets**: Adaptive classifiers are used for stock price prediction, algorithmic trading, and fraud detection, where market conditions and fraudulent tactics can change rapidly.
2. **Healthcare**: These classifiers help in personalized medicine, where treatment plans are continuously updated based on new patient data and medical research.
3. **Speech and Image Recognition**: Adaptive classifiers improve the performance of speech recognition systems and image classifiers by learning from new accents, languages, and image datasets.
4. **Network Security**: In cybersecurity, adaptive classifiers detect and respond to new types of malware and network intrusions.

### ### Techniques

1. **Support Vector Machines (SVM)**: Adaptations of SVMs for online learning and incremental updates help in handling changing data distributions.
2. **Decision Trees and Random Forests**: Adaptive versions of these algorithms can adjust tree structures or replace trees within a forest based on new data.
3. **Bayesian Networks**: These probabilistic models can be updated incrementally to reflect new evidence, making them suitable for adaptive classification.
4. **K-Nearest Neighbors (KNN)**: Adaptive KNN approaches involve dynamically updating the stored instances based on the arrival of new data.

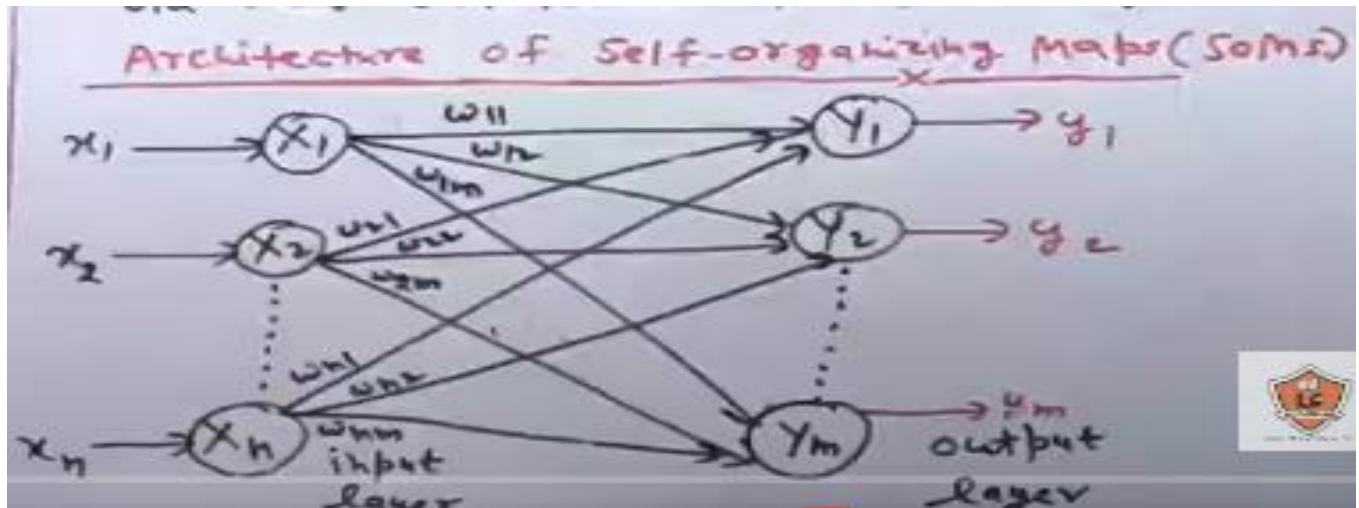
### ### Challenges

1. **Computational Efficiency**: Continuously updating models can be computationally intensive, requiring efficient algorithms and hardware.
2. **Data Storage**: Managing and storing the ever-growing datasets that adaptive classifiers use can be challenging.
3. **Stability-Plasticity Dilemma**: Balancing the need to adapt to new information (plasticity) while retaining previously learned knowledge (stability) is a critical challenge.

In summary, adaptive pattern classification is a powerful approach for dealing with dynamic and evolving datasets. Its ability to learn and adjust in real-time makes it highly applicable across various domains where static models would fail to maintain accuracy.

## Self-organization map (SOM)/ Kohonen Network

The Self-Organizing Map (SOM) algorithm, also known as Kohonen Map, is a type of artificial neural network used for unsupervised learning. It is particularly useful for visualizing and interpreting high-dimensional data by mapping it onto a lower-dimensional (usually two-dimensional) grid.



The SOM algorithm consists of a grid of neurons, where each neuron has an associated weight vector of the same dimension as the input data.

1. **Initialization**: The weight vectors of the neurons are initialized, often with small random values.
2. **Training**: For each input vector in the training dataset:
  - **Finding the Best Matching Unit (BMU)**: Identify the neuron whose weight vector is closest to the input vector, usually using Euclidean distance.
  - **Updating Weights**: Adjust the weight vectors of the BMU and its neighboring neurons to make them more similar to the input vector. The update rule typically involves a learning rate and a neighborhood function, both of which decrease over time.
3. **Iteration**: The training process is repeated for a specified number of iterations or until convergence. Over time, the neurons' weight vectors become organized in a way that reflects the input data distribution.



### ### Steps in Detail

#### 1. Initialization:

- Initialize the SOM grid with random weights for each neuron.

#### 2. Training:

- Repeat for each input vector  $\mathbf{x}$  in the dataset:

- **Competition:**

- Find the Best Matching Unit (BMU) neuron  $j$ :

$$j = \arg \min_i \|\mathbf{x} - \mathbf{w}_i\|$$

where  $\mathbf{w}_i$  is the weight vector of neuron  $i$  and  $\|\cdot\|$  denotes Euclidean distance.

$$w_i = \sum_{j=1}^n \sum_{k=1}^n (x_{kj} - w_{ij})^2$$

- **Cooperation:**

- Update the weights of the BMU and its neighbors:

$$\mathbf{w}_i(t+1) = \mathbf{w}_i(t) + \eta(t) \cdot h_{ci}(t) \cdot (\mathbf{x} - \mathbf{w}_i(t))$$

where:

- $\mathbf{w}_i(t)$  is the weight vector of neuron  $i$  at time  $t$ ,
- $\eta(t)$  is the learning rate at time  $t$ ,
- $h_{ci}(t)$  is the neighborhood function centered around the BMU  $c$  at time  $t$ , and
- $(\mathbf{x} - \mathbf{w}_i(t))$  represents the difference between the input vector and the current weight vector.

#### 3. Update Parameters:

- Decrease the learning rate  $\eta(t)$  and the neighborhood function  $h_{ci}(t)$  over time to gradually reduce the scope of adjustments.

#### 4. Termination:

- Repeat the training process for a specified number of iterations or until convergence.

#### Notation:

- $\mathbf{x}$ : Input vector.
- $\mathbf{w}_i$ : Weight vector of neuron  $i$ .
- $\eta(t)$ : Learning rate at time  $t$ .
- $h_{ci}(t)$ : Neighborhood function centered around the BMU  $c$  at time  $t$ .
- $\|\cdot\|$ : Euclidean distance.

### ### Applications of SOM for Feature Mapping

1. **Data Visualization**: SOMs can be used to create visual representations of high-dimensional data, making it easier to detect patterns, clusters, and anomalies.
2. **Clustering**: By mapping similar data points to nearby neurons, SOMs can effectively cluster data without predefined labels, making them useful for exploratory data analysis.
3. **Feature Extraction**: SOMs can identify important features and relationships within the data, which can then be used for further analysis or as input to other machine learning algorithms.
4. **Dimensionality Reduction**: By reducing the number of dimensions, SOMs help simplify complex datasets while retaining essential information.

### ### Example Use Case

Consider a dataset of customer profiles, each with multiple attributes such as age, income, and purchasing behavior. A SOM can be trained on this dataset to produce a two-dimensional map where each neuron represents a prototype customer profile. Similar customer profiles are mapped to nearby neurons, enabling easy visualization of different customer segments and their characteristics.

## **SOMs can be utilized for feature mapping:**

### **### 1. Dimensionality Reduction:**

SOMs project high-dimensional data onto a lower-dimensional grid, typically two-dimensional. This reduction in dimensionality allows for easier visualization and interpretation of complex datasets while retaining important information.

### **### 2. Topological Mapping:**

SOMs preserve the topological properties of the input space in the output grid. Neurons that are close to each other in the SOM grid represent input vectors with similar characteristics. Therefore, the SOM effectively maps the input data's topology onto a lower-dimensional space.

### **### 3. Clustering and Visualization:**

By organizing similar input vectors into nearby neurons, SOMs naturally form clusters in the output grid. These clusters represent groups of data points with similar features or characteristics. This clustering aids in exploratory data analysis and visualization, allowing users to identify patterns, trends, and anomalies in the data.

### **### 4. Feature Extraction:**

SOMs can extract and highlight important features from the input data. Neurons in the SOM grid that are frequently activated or represent dense regions of data indicate significant features or combinations of features present in the input space. These extracted features can then be used for further analysis or as inputs to downstream machine learning models.

### **### 5. Data Compression and Storage:**

SOMs compress the input data into a more compact representation while preserving relevant information. This compressed representation can be stored more efficiently, making SOMs useful for storing and transmitting large datasets.

### ### 6. Pattern Recognition:

SOMs can recognize and classify patterns present in the input data. By learning the underlying structure of the data, SOMs can identify similarities and differences between input vectors, enabling tasks such as image recognition, speech processing, and anomaly detection.