

Tips, Formulae and shortcuts for Linear equations

By

CRACKU.IN

Cracku Tip 1 – Linear equations

- Linear equations is one of the foundation topics in the Quant section of CAT.
- Hence, fundamentals of this concept are useful in solving the questions of the other topics by assuming the unknown values as variables.
- Be careful of silly mistakes in this topic as that is how students generally lose marks here.
- Generally, the number of equations needed to solve the given problem is equal to the number of variables

Free CAT Mock Test: <https://cracku.in/cat-mock-test>

Cracku Tip 2 – Linear equations

- A linear equation is an equation which gives straight line when plotted on a graph.
- Linear equations can be of one variable or two variable or three variable.
- Let a , b , c and d are constants and x , y and z are variables. A general form of single variable linear equation is $ax+b = 0$.
- A general form of two variable linear equation is $ax+by = c$.
- A general form of three variable linear equation is $ax+by+cz = d$.

Cracku Tip 3 – Linear equations

Equations with two variables:

- Consider two equations $ax+by = c$ and $mx+ny = p$. Each of these equations represent two lines on the x-y co-ordinate plane. The solution of these equations is the point of intersection.
- If $\frac{a}{m} = \frac{b}{n} \neq \frac{c}{p}$ then the slope of the two equations is equal and so they are parallel to each other. Hence, no point of intersection occurs. Therefore no solution.
- If $\frac{a}{m} \neq \frac{b}{n}$ then the slope is different and so they intersect each other at a single point. Hence, it has a single solution.
- If $\frac{a}{m} = \frac{b}{n} = \frac{c}{p}$ then the two lines are same and they have infinite points common to each other. So, infinite solutions occurs

Cracku Tip 4 – Linear equations

General Procedure to solve linear equations:

- Aggregate the constant terms and variable terms
- For equations with more than one variable, eliminate variables by substituting equations in their place.
- Hence, for two equations with two variables x and y , express y in terms of x and substitute this in the other equation.
- For Example, let $x+y = 14$ and $x+4y = 26$ then $x = 14-y$ (from equation 1) substituting this in equation 2, we get $14-y+4y = 26$. Hence, $y = 4$ and $x = 10$.

Cracku Tip 5 – Linear equations

General Procedure to solve linear equations:

For equations of the form $ax+by = c$ and $mx+ny = p$, find the LCM of b and n . Multiply each equation with a constant to make the y term coefficient equal to the LCM. Then subtract equation 2 from equation 1.

Example:

Let $2x+3y = 13$ and $3x+4y = 18$ are the given equations (1) and (2).

- LCM of 3 and 4 is 12.
- Multiplying (1) by 4 and (2) by 3, we get $8x+12y = 52$ and $9x+12y = 54$.
- $(2)-(1)$ gives $x=2, y=3$

Download CAT Formulas PDF: <https://cracku.in/blog/cat-formulas-pdf/>

Cracku Tip 6 – Linear equations

- If the system of equations has n variables with $n-1$ equations then the solution is indeterminate
- If system of equations has n variables with $n-1$ equations with some additional conditions like the variables are integers then the solution may be determinate
- If system of equations has n variables with $n-1$ equations then some combination of variables may be determinable.
- For example, if $ax+by+cz = d$ and $mx+ny+pz = q$, if a, b, c are in Arithmetic progression and m, n and p are in AP then the sum $x+y+z$ is determinable.

Cracku Tip 7 – Linear equations

Equations with three variables:

Let the equations be $a_1x+b_1y+c_1z = d_1$, $a_2x+b_2y+c_2z = d_2$ and $a_3x+b_3y+c_3z = d_3$. Here we define the following matrices.

$$D = \begin{bmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{bmatrix} \quad D_x = \begin{bmatrix} d_1 & b_1 & c_1 \\ d_2 & b_2 & c_2 \\ d_3 & b_3 & c_3 \end{bmatrix} \quad D_y = \begin{bmatrix} a_1 & d_1 & c_1 \\ a_2 & d_2 & c_2 \\ a_3 & d_3 & c_3 \end{bmatrix} \quad D_z = \begin{bmatrix} a_1 & b_1 & d_1 \\ a_2 & b_2 & d_2 \\ a_3 & b_3 & d_3 \end{bmatrix}$$

- If Determinant of $D \neq 0$, then the equations have a unique solution.
- If Determinant of $D = 0$, and at least one but not all of the determinants D_x , D_y or D_z is zero, then no solution exists.
- If Determinant of $D = 0$, and all the three of the determinants D_x , D_y and D_z are zero, then there are infinitely many solution exists.
- Determinant can be calculated by $D = a_1(b_2c_3-c_2b_3)-b_1(a_2c_3-c_2a_3)+c_1(a_2b_3-b_2a_3)$

Enroll To CAT Courses: <https://cracku.in/cat/pricing>

**Want a free guidance for CAT from
IIM alumni**

Whatsapp 'CAT' to +91 7661025559

Cracku.in

Download Important Questions & Answers PDF Below:

[Verbal Ability & Reading comprehension](#)

[Data Interpretation](#)

[Logical Reasoning](#)

[Quantitative Aptitude](#)



Get Important MBA Updates

[Whatsapp](#)

[Telegram](#)

[Join FB CAT Group](#)

[Best CAT Preparation Free Android App](#)

