

A college professor believes that if the grade for internal examination is high in a class, the grade for external examination will also be high. A random sample of 7 students in that class was selected, and the data is given below: Input 0.1 0.2 0.3 0.4 0.5 0.6 0.7 Target 1.2 1.4 1.55 1.75 2.01 2.2 2.35 Write a python program for linear regression using a single neuron (with proper activation function) on the above dataset, and find the coefficients  $w_1$  and  $b$ . Predict the external marks if internal marks are 0.15. Draw the scatter plot between Internal Exam and External Exam. Draw a straight line with red line using above  $w_1$ ,  $w_2$  and  $b$ .

```
In [1]: import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
# Input data
internal_marks = np.array([0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7])
external_marks = np.array([1.2, 1.4, 1.55, 1.75, 2.01, 2.2, 2.35])
```

```
In [2]: class LinearRegression:
def __init__(self):
    self.w1 = None
    self.b = None
def fit(self, X, y):
    X_mean = np.mean(X)
    y_mean = np.mean(y)
    nums=np.sum((X-X_mean)*(y-y_mean))
    den=np.sum((X-X_mean)**2)
    self.w1=nums/den
    self.b=y_mean-self.w1*X_mean

def predict_model(self,X):
    return self.w1*X+self.b
```

```
In [3]: model=LinearRegression()
```

```
In [4]: model.fit(internal_marks,external_marks)
```

```
In [5]: w1=model.w1
b=model.b
```

```
In [6]: print("W1:",w1)
print("b:",b)
```

```
W1: 1.9678571428571432
b: 0.9928571428571425
```

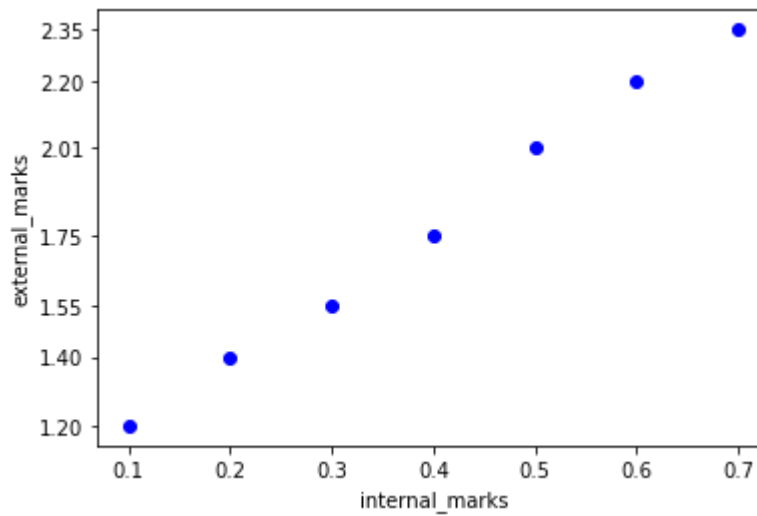
```
In [7]: int_marks=0.15
external_marks_pred=model.predict_model(int_marks)
```

```
In [8]: print("External marks for internal_marks 0.15 is:",external_marks_pred)
```

```
External marks for internal_marks 0.15 is: 1.288035714285714
```

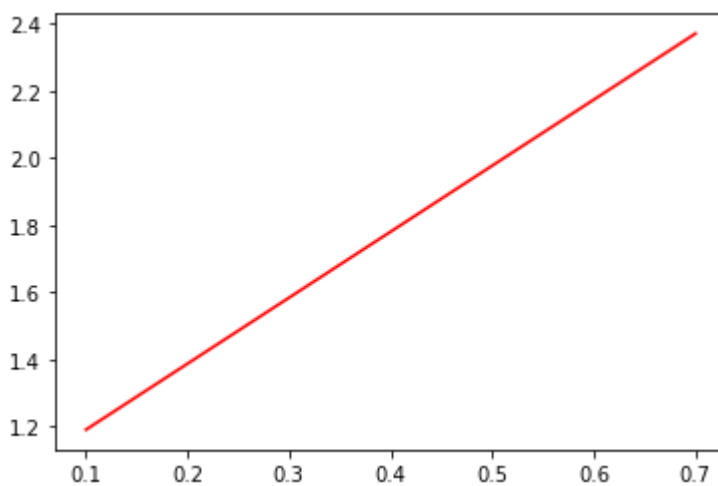
```
In [9]: p1=plt.scatter(internal_marks,external_marks,color='blue',label='Data point')
plt.xticks(internal_marks)
plt.yticks(external_marks)
plt.xlabel('internal_marks')
plt.ylabel('external_marks')
```

Out[9]: Text(0, 0.5, 'external\_marks')



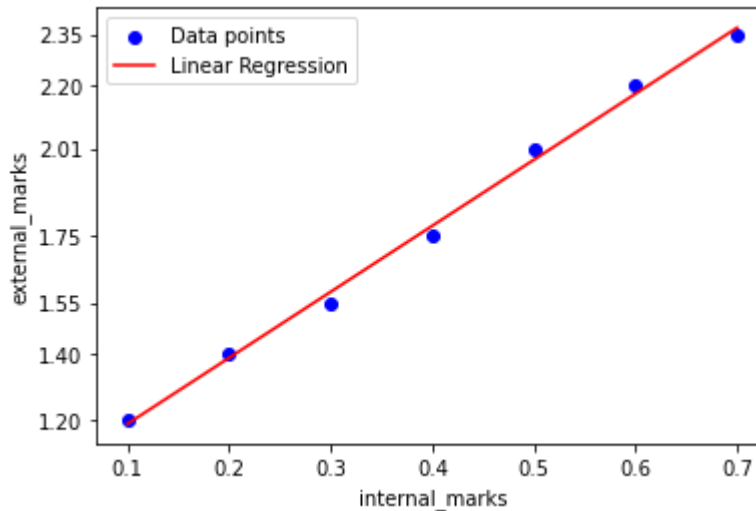
```
In [10]: ext_marks_pred=model.predict_model(internal_marks)
```

```
In [11]: p2=plt.plot(internal_marks,ext_marks_pred,color='red',label='Linear Regress')
```



```
In [12]: p1=plt.scatter(internal_marks,external_marks,color='blue',label='Data point')
plt.xticks(internal_marks)
plt.yticks(external_marks)
plt.xlabel('internal_marks')
plt.ylabel('external_marks')
p2=plt.plot(internal_marks,ext_marks_pred,color='red',label='Linear Regression')
plt.legend()
```

Out[12]: <matplotlib.legend.Legend at 0x1edc9b1d990>



Generate 51 points for  $y = 1 / (1 + \exp(-3x))$ , where  $x \in [-2, 3]$ . Use this dataset to train sigmoid neuron using gradient descent learning algorithm. Draw two curves with different colours, for target and output(y) of the trained neuron.

```
In [13]: import numpy as np
import matplotlib.pyplot as plt
```

```
In [14]: x=np.linspace(-2,3,51)
y=1/(1+np.exp(-3*x))
```

```
In [15]: x
```

```
Out[15]: array([-2. , -1.9, -1.8, -1.7, -1.6, -1.5, -1.4, -1.3, -1.2, -1.1, -1. ,
        -0.9, -0.8, -0.7, -0.6, -0.5, -0.4, -0.3, -0.2, -0.1,  0. ,  0.1,
         0.2,  0.3,  0.4,  0.5,  0.6,  0.7,  0.8,  0.9,  1. ,  1.1,  1.2,
         1.3,  1.4,  1.5,  1.6,  1.7,  1.8,  1.9,  2. ,  2.1,  2.2,  2.3,
         2.4,  2.5,  2.6,  2.7,  2.8,  2.9,  3. ])
```

```
In [16]: y
```

```
Out[16]: array([0.00247262, 0.00333481, 0.00449627, 0.0060598 , 0.00816257,  
                0.01098694, 0.01477403, 0.01984031, 0.02659699, 0.03557119,  
                0.04742587, 0.06297336, 0.0831727 , 0.10909682, 0.14185106,  
                0.18242552, 0.23147522, 0.2890505 , 0.35434369, 0.42555748,  
                0.5 , 0.57444252, 0.64565631, 0.7109495 , 0.76852478,  
                0.81757448, 0.85814894, 0.89090318, 0.9168273 , 0.93702664,  
                0.95257413, 0.96442881, 0.97340301, 0.98015969, 0.98522597,  
                0.98901306, 0.99183743, 0.9939402 , 0.99550373, 0.9966519,  
                0.99752738, 0.99816706, 0.99864148, 0.99899323, 0.99925397,  
                0.99944722, 0.99959043, 0.99969655, 0.99977518, 0.99983344,  
                0.99987661])
```

```
In [17]: class SigmoidNeuron:  
    def __init__(self):  
        self.w=np.random.rand(1)  
        self.b=np.random.rand(1)  
  
    def sigmoid(self,x):  
        return 1/(1+np.exp(-x))  
  
    def forward_propogation(self,x):  
        return self.sigmoid(self.w*x+self.b)  
  
    def back_propogation(self,x,y,lr):  
        y_pred=self.forward_propogation(x)  
        w_diff=(y_pred-y)*(y_pred)*(1-y_pred)*x  
        b_diff=(y_pred-y)*(y_pred)*(1-y_pred)  
        self.w=self.w-lr*w_diff  
        self.b=self.b-lr*b_diff
```

```
In [18]: model=SigmoidNeuron()
```

```
In [19]: epochs=100  
         learning_rate=0.01
```

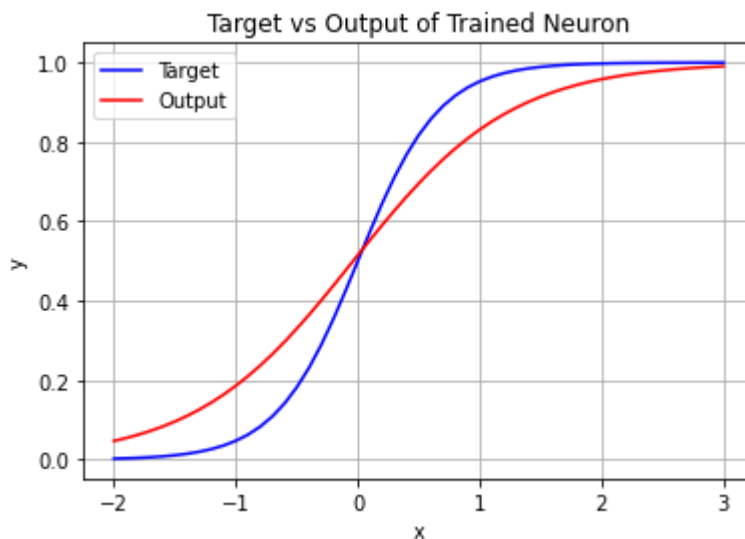
```
In [20]: for epoch in range(epochs):  
         for i in range(len(x)):  
             model.back_propogation(x[i],y[i],learning_rate)
```

```
In [21]: y_out=model.forward_propogation(x)
```

```
In [22]: y_out
```

```
Out[22]: array([0.04696534, 0.05433288, 0.06278004, 0.07243988, 0.08345372,
                0.09596886, 0.11013531, 0.12610125, 0.14400714, 0.16397853,
                0.18611739, 0.21049268, 0.23713021, 0.26600294, 0.29702242,
                0.33003272, 0.36480785, 0.40105373, 0.43841524, 0.47648837,
                0.51483673, 0.55301119, 0.59057066, 0.62710222, 0.66223845,
                0.69567065, 0.72715705, 0.75652594, 0.78367402, 0.80856101,
                0.8312016 , 0.85165584, 0.87001912, 0.88641242, 0.90097351,
                0.91384939, 0.9251901 , 0.93514389, 0.94385366, 0.95145448,
                0.95807204, 0.96382183, 0.96880878, 0.97312748, 0.9768625 ,
                0.98008901, 0.98287347, 0.98527439, 0.98734307, 0.98912434,
                0.9906573 ])
```

```
In [23]: plt.plot(x, y, label='Target', color='blue')
plt.plot(x, y_out, label='Output', color='red')
plt.xlabel('x')
plt.ylabel('y')
plt.title('Target vs Output of Trained Neuron')
plt.legend()
plt.grid(True)
plt.show()
```



```
In [ ]:
```