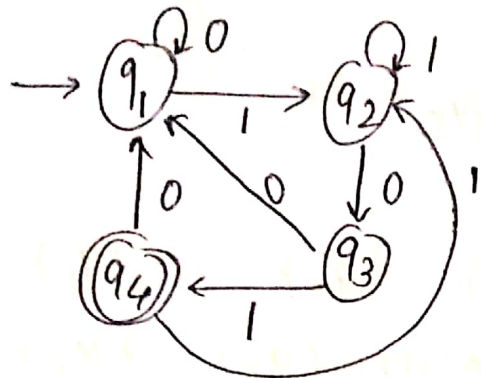


Ardent's
Therm

Ardent's Theorem - if $R = Q + RP$ then $R = QP^*$

Find Reg. expr. corresponding to



$$q_1 = q_1 0 + q_3 0 + q_4 0 + \epsilon \quad \text{--- (1)}$$

[ϵ as q_1 is Initial]

$$q_2 = q_1 1 + q_2 1 + q_4 1 \quad \text{--- (2)}$$

$$q_3 = q_2 0 \quad \text{--- (3)} \quad q_4 = q_3 1 \quad \text{--- (4)}$$

put (4) in (2)

$$q_2 = q_1 1 + q_2 1 + q_2 0 1$$

$$q_2 = q_1 (1 + 0 1 1)^* \quad \text{--- (5)}$$

put (3) and (4) in eq. (1)

$$q_1 = q_1 0 + q_2 0 0 + q_2 0 1 0 + \epsilon$$

$$= q_1 0 + q_2 (0 0 + 0 1 0) + \epsilon$$

$$= q_1 0 + q_1 (1 + 0 1 1)^* (0 0 + 0 1 0) + \epsilon$$

$$= \epsilon (0 + 1 (1 + 0 1 1)^* (0 0 + 0 1 0))^* \quad \text{--- (6)}$$

put eq (5) in eq. (6)

$$q_4 = q_1 (1 + 0 1 1)^* 0 1$$

$$= (0 + 1 (1 + 0 1 1)^* (0 0 + 0 1 0))^* 1 (1 + 0 1 1)^* 0 1$$