

?
??
Generación
de
llaves
Encapsulado
Decapsulado

?

Keccak-p

?

Funciones

de

hash

224

256

384

512

SHA3-

256

Funciones

de

sal-

ida

ex-

ten-

dida

128

SHAKE-

256

Keccak-p

Keccak-p

El

an-

cho

de

la

per-

muta

$b \in$

$\{25, 50, 100, 200, 400, 800, 1600\}$

El

número

de

rón-

das

$n_r \in$

\mathbb{Z}

b
 $b/25$
 $l =$
 $\log_2(b/25)$
 \parallel
 0^j
 j
 $\text{len}(P)$
 P
 $Z(j)$
 j
 Z
 \equiv
 10010
 $Z(4) =$
 1
 $\text{trunc}_d(Z)$
 d
 Z
~~Keccak-p~~
 b
 S
 $A(x,y,z)$
 $x,y \in$
 $\{0,1,2,3,4\}$
 \hat{w}
 $??$
 $??$

$$(1) \quad \begin{matrix} S \\ A \\ A(x,y,z) = S(w \cdot (5y+x)+z) \\ S \\ A \\ S \end{matrix}$$

$$(2) \quad \begin{matrix} Linea(i,j) == A(i,j,0) \\ Plano(j) = Linea(0,j) \\ S = Plano(0) \end{matrix} \parallel \begin{matrix} A(i,j,1) \\ Linea(1,j) \\ Plano(1) \end{matrix} \parallel \parallel \begin{matrix} A(i,j,w-1) \\ Linea(4,j) \\ Plano(4) \end{matrix}$$

θ
 ρ
 χ
 t
 $A(x,y,z)$
 $A'(x,y,z)$
 t
 t_r
~~Transformada~~
 θ
 \oplus
 $A(x,y,z)$
 $C(x-$
 $1 \bmod 5, z)$
 $C(x+$
 $1 \bmod 5, z-$
 $1 \bmod w)$
 θ
~~Entrada:~~ A
~~Salida:~~ A'
 C

$$(3) \quad \begin{matrix} C(x,z) := A(x,0,z) \oplus A(x,1,z) \oplus A(x,2,z) \oplus A(x,3,z) \oplus A(x,4,z) \\ D \end{matrix}$$

$$(4) \quad D(x,z) := C(x-1 \bmod 5, z) \oplus C(x+1 \bmod 5, z-1 \bmod w)$$

$$(5) \quad \begin{matrix} A'(x,y,z) := A(x,y,z) \oplus D(x,z) \end{matrix}$$

A'
~~Transformada~~
 ρ
 $??$
 $x = 3x = 4x = 0x = 1x = 2$
 $y = 2$
 $y = 1$
 $y = 0$
 $y = 4$
 $y = 3$
 ρ
 ρ
~~Entrada:~~ A
~~Salida:~~ A'
 $(x,y,z) :=$
 $(0,0,z)$

$$(6) \quad A'(0,0,z) := A(0,0,z)$$

Transformada

(x, y)

??

$$x = 3x = 4x = 0x = 1x = 2$$

$$y = 2$$

$$y = 1$$

$$y = 0$$

$$y = 4$$

$$y = 3$$

$A'(x, y)$

(x', y')

A

Entrada: A

Salida: A'

$$A(x, y, z) := A(x + 3y \bmod 5, x, z)$$

(8)

A'

Transformada

??

?

?

$A(x, y, z)$

$A'(x, y, z)$

χ
Entrada: A
Salida: A'
 $A'(x, y, z) := A(x, y, z) \oplus \{[A(x+1 \bmod 5, y, z) \oplus 1] \& A(x+2 \bmod 5, y, z)\}$

(9)

A'
Transformada
 $(0, 0)$

i_r
Entrada: Ai_r
Salida: A'
 $A'(x, y, z) := A(x, y, z)$

(10)

RC
 $\ell =$
 $\log_2(b/25)$
 $RC(2^j - 1) := \text{rc}(j + 7i_r)$

(11)

$A'(0, 0, z) := A'(0, 0, z) \oplus RC(z)$

(12)

A'
 $\text{rc}(t)$
 t
Entrada: t
Salida: $\text{rc}(t)$
 $t \bmod 255 =$
 0
 255
 $R \mid \overline{R}$
 $R \mid R$
 $R[0] :=$
 $R[0] \oplus$
 $R[8] \mid$
 $R[4] :=$
 $R[4] \oplus$
 $R[8] \mid$
 $R[5] :=$
 $R[5] \oplus$
 $R[8] \mid$
 $R[6] :=$
 $R[6] \oplus$
 $R[8] \mid$
 $R :=$
 $\text{Trunc}_8[R]$
 $R[0]$

$$\begin{aligned} &\text{Rnd}(A, i_r) \\ &\text{Rnd}(A, i_r) = \iota(\chi(\pi(\rho(\theta(A))))), i_r) \end{aligned} \tag{13}$$

Keccak-p(b, n_r)

n_r
Rnd

b
Entrada: $S n_r$

Salida: S'

S
 A

$i_r n_r$
Rnd(A, i_r)

A
 S'

S
 b'

S'
sponge[f, pad, r](N, d)

N
 Z

d
 f

pad
 r

b
 f

sponge

??
 f

b
 f

keccak-p

$$c = b - r \tag{14}$$

r
 d

sponge
 ?
 sponge
Entrada: Nd
Salida:
 $P = N || \text{pad}(r, \text{len}(N))$
 (15) $n = \text{len}(P)r$
 (16) $c =$
 $b =$
 $S =$
 0^b
 P_0, \dots, P_{n-1}
 $P =$
 $P_0 || \dots || P_{n-1}$
 $S = f(S \oplus (P_i || 0^c))$
 (17) Z
 $Z = Z || \text{Trunc}_r(S)$
 (18) $d \leq$
 $\text{len}(Z)$
 $\text{Trunc}_d(S)$
 $S = f(S)$
 (19) sponge
 pad10*1
 x
 P
 $m + \text{len}(P) = \lambda x$
 (20) pad10*1
Entrada: xm
Salida:
 $j = -m - 2 \bmod x$
 (21) $P = 1 || 0^j || 1$
 (22) P
 $b = 1600$
 $\text{Keccak}[c](N, d)$
 $\text{Keccak}[c](N, d) = \text{sponge}[\text{Keccak-p}(1600, 24), \text{pad10*1}, 1600 - c](N, d)$
 (23) SHA3-224(M)Keccak($M || 01, 224$)
 SHA3-256(M)Keccak($M || 01, 256$)
 SHA3-384(M)Keccak($M || 01, 384$)
 SHA3-512(M)Keccak($M || 01, 512$)
 SHAKE128(M, d)Keccak($M || 1111, d$)
 SHAKE256(M, d)Keccak($M || 1111, d$)
 ?
Resistencia
 a
 la
 col-
 isión
Resistencia
 a
 preim-
 gen
 h
 $\text{hash}(x) =$
 h
Resistencia
 a
 preim-
 gen
 Se-
 cun-
 daria
 x_1
 x_2
 $\text{hash}(x_1) =$
 $\text{hash}(x_2)$

$$\begin{array}{c}
 ? \\
 ? \\
 ? \\
 \mathcal{B} = \\
 \{0,\ldots,255\} \\
 \mathcal{B}^k \\
 \mathcal{B}^* \\
 \parallel \\
 +k \\
 \mathcal{B} \\
 \mathcal{C} \\
 \mathcal{C} \\
 b \\
 c=a||b
 \end{array}
 \tag{24}$$

$$\begin{array}{c}
 b=c+l \\
 (25)
 \end{array}$$

$$\begin{array}{c}
 v[i] \\
 v \\
 i \\
 A[i][j] \\
 i \\
 j \\
 A \\
 A^T \\
 [x] \\
 x \\
 [2,3] = \\
 2 \\
 [2,5] = \\
 3 \\
 [2,8] = \\
 3 \\
 \|x\| \\
 \alpha \\
 r' = r mod^{\pm} \alpha \implies -\alpha 2 < r' \leq \alpha 2
 \end{array}
 \tag{26}$$

$$\begin{array}{c}
 r' = r mod^+ \alpha \implies 0 \leq r' < \alpha \\
 (27)
 \end{array}$$

$$\begin{array}{c}
 \mathcal{S} \leftarrow \\
 \mathcal{S} \\
 \mathcal{S} \\
 \mathcal{S} \\
 \mathcal{S}
 \end{array}$$

$$\mathcal{O}(n^2)$$

$$\mathcal{O}(n\log(n))$$

$$R_q$$

$$(28) \quad R_qZ_q[X]X^n+1$$

$$q=3329$$

$$256$$

$$n|(q-1)$$

$$n|(q-1)$$

$$Z_q$$

$$_0^n$$

$$q>1$$

$$Z_q^n|(q-1)$$

$$\omega_{Z_q}$$

$$\Omega=\{1,\omega,\omega^2,\ldots,\omega^{n-1}\}$$

$$(29) \quad H_{G_{q-1}}$$

$$H_{G_{q-1}}$$

$$n|(q-1)$$

$$G_{q-1}$$

$$\alpha^{q-1}=1$$

$$(30) \quad G_{q-1}$$

$$G_{q-1}=\{1,\alpha,\alpha^2,\ldots,\alpha^{q-2}\}$$

$$(31) \quad \omega$$

$$\omega=\alpha^{\frac{q-1}{n}},$$

$$(32) \quad \omega^n=\alpha^{q-1}=1,$$

$$(33) \quad 0\leq k\leq k\cdot\frac{q-1}{n}<q-1\Rightarrow\omega^k\neq 1.$$

$$(34) \quad \omega_{Z_q}$$

$$\frac{X^{256}+1}{Z_qn^q}$$

$$(35) \qquad \hat{a}_j=\sum_{i=0}^{n-1}\phi^{i(2j+1)}a_jmodq$$

$$(36) \qquad a_i=n^{-1}\sum_{j=0}^{n-1}\phi^{-i(2j+1)}\hat{a}_jmodq$$

$$\begin{array}{l} \phi\\ \phi^2=\\ \omega\\ Z_q\\ n^{-1}\\ Z_q\\ ?\\ G(x)=\\ 5+\\ 6x+\\ 7x^2+\\ 8x^3=\\ g=[5,6,7,8]\\ Z_{7681}\\ \phi=1925\\ \hat{g} \end{array}$$

$$(37) \qquad \hat{g}=\phi^0\phi^1\phi^2\phi^3\phi^0\phi^3\phi^6\phi^1\phi^0\phi^5\phi^2\phi^7\phi^0\phi^7\phi^6\phi^5.5678=1192533836468164684298192515756338312131121342985756.5678=24\begin{array}{l} \phi=\\ 1925\\ Z_{7681}\\ \phi^{-1}=\\ 1213\\ n=4\\ p^{-1}=\\ 5761 \end{array}$$

$$(38) \qquad g=n^{-1}\phi^0\phi^0\phi^0\phi^0\phi^{-1}\phi^{-3}\phi^{-5}\phi^{-7}\phi^{-2}\phi^{-6}\phi^{-2}\phi^{-6}\phi^{-3}\phi^{-1}\phi^{-7}\phi^{-5}.\hat{g}=576111111213575664681925429833834298338357561\begin{array}{l} R_qZ_q[X]X^n+1\\ g\\ h \end{array}$$

$$(39) \qquad g.h=NTT^{-1}(NTT(g)\circ NTT(h))\begin{array}{l} \circ\\ Z_q[X] \end{array}$$

$$\mathcal{O}(n\log(n))$$

$$(40) \quad \phi^{k+2n} = \phi^k$$

$$(41) \quad \begin{array}{l} \phi^{k+n} = \phi^{-k} \\ ? \end{array}$$

$$(42) \quad \hat{a}_j = \sum_{i=0}^{n-1} \phi^{i(2j+1)} a_j mod q = \sum_{i=0}^{n/2-1} \phi^{4ij+2i} a_{2i} + \phi^{2j+1} \sum_{i=0}^{n/2-1} \phi^{4ij+2i} a_{2i+1} mod q$$

$$\begin{array}{l} A_j = \\ \sum_{i=0}^{n/2-1} \phi^{4ij+2i} a_{2i} \\ B_j = \\ \sum_{i=0}^{n/2-1} \phi^{4ij+2i} a_{2i+1} \\ \phi \end{array}$$

$$(43) \quad \hat{a}_j = A_j + \phi^{4ij+2i} B_j mod q$$

$$(44) \quad \hat{a}_{j+n/2} = A_j - \phi^{4ij+2i} B_j mod q$$

$$\begin{array}{l} A_j \\ B_j \\ \mathcal{Y} \\ \mathcal{O}(n\log(n)) \\ ? \\ R_q \\ \{\xi,\xi^3,\ldots,\xi^{255}\} \\ \xi = \\ 17 \end{array}$$

$$X^{256}+1=\prod_{i=0}^{127}(X^2-\xi^{2i+1})$$

$$(45) \quad \begin{array}{l} ? \\ \hat{f} \in \\ R_q \\ NTT(f) = \hat{f} = \left(\hat{f}_0 + \hat{f}_1 X, \hat{f}_2 + \hat{f}_3 X, ..., \hat{f}_{254} + \hat{f}_{255} X\right) \end{array}$$

$$(46) \quad \begin{array}{l} \hat{f}_{2i} = \sum_{j=0}^{127} f_{2j} \xi^{(2i+1)j} \\ \hat{f}_{2i+1} = \sum_{j=0}^{127} f_{2j+1} \xi^{(2i+1)j} \end{array}$$

$$(47) \quad \begin{array}{l} -1 \\ fg \in \\ R_q \end{array}$$

$$(48) \quad h=f.g=NTT^{-1}\left[NTT(f)\circ NTT(g)\right]$$

$$(49) \quad \begin{array}{l} \hat{h} = \\ \hat{f}^\circ \\ \hat{g} = \\ NTT(f)^\circ \\ NTT(g) \\ \hat{h}_{2i} + \hat{h}_{2i+1} X = (\hat{f}_{2i} + \hat{f}_{2i+1}) (\hat{g}_{2i} + \hat{g}_{2i+1}) mod \left(X^2 - \xi^{2i+1}\right) \end{array}$$

$$\begin{array}{l} ?? \\ \mathcal{O}(n^2) \\ -1 \\ \mathcal{O}(n\log(n)) \\ \hat{f} \\ \hat{g} \\ \hat{h} \\ \hat{B} = \\ \{b_1,...,b_n\} \end{array}$$

$$\mathcal{A} = \mathcal{L}(B) = \left\{ \sum_{i \in n} z_i b_i : z \in Z^n \right\}$$

$$(50)$$

$$\begin{array}{l}
?? \\
q_n \\
sk \\
pk \\
Z_q[x]/(X^n+ \\
1) \\
0 \\
\textbf{Entrada: } qn \\
\textbf{Salida: } skpk \\
q \in \\
R_q \\
sk, e \in \\
R_q \\
b := a \cdot sk + e \\
(51) \quad (sk, pk := \\
a || b) \\
pk \\
z \in \\
\{0, 1\}^n \\
y \\
0 \\
\textbf{Entrada: } pkzqn \\
\textbf{Salida: } uv \\
r, e_1, e_2 \in \\
R_q \\
u
\end{array}$$

$$\begin{array}{l}
u := a \cdot r + e_1 mod^+ q \\
(52) \quad v
\end{array}$$

$$\begin{array}{l}
v := b \cdot r + e_2 + \lfloor q2 \rfloor \cdot z mod^+ q \\
(53) \quad (u, v) \\
y \\
\tilde{r} = \\
\tilde{e} - \\
\tilde{s} \cdot \\
e_1 + \\
e_2 \\
\| \varepsilon \| < \\
q/4 \\
2^{-174} \\
?
\end{array}$$

0

Entrada: $skuvqn$

Salida: z

z'

(54) $z' := v - u \cdot s = (r \cdot e - s \cdot e_1 + e_2) + \lfloor q2 \rfloor \cdot z \bmod^+ q$

(z'_i)

$\mathbf{1.1:}$

0

(55) $d_i(0) := \|z'_i \bmod^\pm \lfloor q2 \rfloor\|$

$\mathbf{1.2:}$

$\lfloor q2 \rfloor$

(56) $d_i(q2) := \|\lfloor q2 \rfloor - d_i(0)\|$

$d_i(0) <$

$d_i(q2)$

\hat{z}

0

\hat{z}

$\hat{1}$

$\hat{z}?$

\hat{z}

R_q

d

$s \in R_q^d(\text{elvectorsecreto}) A \in R_q^{d \times d}(\text{lamatrizpblica}, \text{muestreada} R_q^{d \times d})$

ρ

$\in R_q^d(\text{elvectordeerror}, \text{concoeficientespequeos})$

$b \in$

$R_q^d(\text{laparejaresultante})$

$b =$

$A:$

$s+$

$e \in$

R_q^d

(A, b)

$R_q^{d \times d} \times$

R_q^d

d

A

$n \ k \ q \ \eta_1 \eta_2 d_u d_v \ \delta \ pk(\text{bytes}) sk(\text{bytes}) c(\text{bytes})$

25643329 2 2 11 5 2⁻¹⁷⁴ 3168(32) 1568 1568

$\overline{n_{256}}$

$k =$

$4 =$

$q =$

3329

$n|(q-$

1)

η_1

η_2

d_u

d_v

δ

(32)

?

?

(pk)

(sk)

??

$Parse(x)$

a_i

$\log_2(q) \approx$

11.

$\frac{1}{2} <$

$\frac{1}{q}$

$CBD_\eta(x)$

$B \in$

$\mathcal{B}^{64\eta}$

$f \in$

R_q

$Encode_k(x)$

$B \in$

\mathcal{B}^{32l}

$f \in$

R_q

Salida: $pk \in \mathcal{B}^{12 \cdot k \cdot n/8 + 32}$ $sk \in \mathcal{B}^{24 \cdot k \cdot n/8 + 96}$

$d, z \in$

\mathcal{B}^{32}

p, σ

d

$$(57) \quad (\rho, \sigma) := SHA3 - 512(d)$$

$\hat{A}[i][j] :=$

$Parse[SHAKE - 128(\rho, j, i)]$

$N :=$

0

$s[i] :=$

$CBD_{\eta_1}[SHAKE - 256(\sigma, N)]$

$N :=$

$N+$

1

$e[i] :=$

$CBD_{\eta_1}[SHAKE - 256(\sigma, N)]$

$N :=$

$N+$

1

$\hat{s} := NTT(s)$

$\hat{e} := NTT(e)$

$\hat{t} := \hat{A} \circ \hat{s} + \hat{e}$

$$(58) \quad pk := Encode_{12}(\hat{t} mod^+ q) || \rho$$

$$(59) \quad \hat{b}$$

$\hat{\rho}$

\hat{A}

$sk := Encode_{12}(\hat{s} mod^+ q) || pk || SHA3 - 256(pk) || z$

$$(60) \quad (pk, sk)$$

\mathcal{C}

pk

\mathcal{P}

γ

$Compress_q(x, y)$

$Decompress_q(x, y)$

$Decode_k(x)$

$f \in$

R_q

$B \subseteq$

\mathcal{B}^{32l}

Entrada: $pk \in \mathcal{B}^{12 \cdot k \cdot n/8 + 32} m \in \mathcal{B}^{32} \gamma \in \mathcal{B}^{32}$

Salida: $c \in \mathcal{B}^{d_u \cdot k \cdot n/8 + d_v \cdot n/8}$

$N :=$

0

$r[i] :=$

$CBD_{\eta_1}[SHAKE - 256(\gamma, N)]$

r

$N :=$

1

$N +$

1

$e_1[i] :=$

$CBD_{\eta_2}[SHAKE - 256(\gamma, N)]$

$N :=$

$N +$

1

$e_2[i] :=$

$CBD_{\eta_2}[SHAKE - 256(\gamma, N)]$

$\hat{r} := NTT(r)$

$u := NTT^{-1}(\hat{A}^T \circ \hat{r}) + e_1$

$v := NTT^{-1}(\hat{t}^T \circ \hat{r}) + e_2 + Decompress_q[Decode_1(m), 1]$

$c_1 := Encode_{d_u}[Compress_q(u, d_u)]$

$c_2 := Encode_{d_v}[Compress_q(v, d_v)]$

(61)

$c :=$

$c_1 || c_2$

pk

κ

k

Entrada: $pk \in \mathcal{B}^{12 \cdot k \cdot n/8 + 32}$

Salida: $c \in \mathcal{B}^{d_u \cdot k \cdot n/8 + d_v \cdot n/8} k \in \mathcal{B}^*$

$\hat{t} := Decode_{12}(pk)$

$p := pk + 12 \cdot k \cdot n/8$

(62)

\hat{A}^T

\hat{p}'

m', κ, γ

m'

$m := SHA3 - 256(m')$

$(\kappa, \gamma) := SHA3 - 512[m || SHA3 - 256(pk)]$

(63)

$c \leftarrow CifradoKyber(pk, m, \gamma)$

(64)

$k := SHAKE - 256[\kappa || SHA3 - 256(c)]$

(65)

c, k

c

sk

k

Entrada: $c \in \mathcal{B}^{d_u \cdot k \cdot n/8 + d_v \cdot n/8} sk \in \mathcal{B}^{24 \cdot k \cdot n/8 + 96}$

Salida: $k \in \mathcal{B}^*$

u

s

$u := Decompress_q[Decode_{d_u}(c, d_u)]$

$v := Decompress_q[Decode_{d_v}(c + d_u \cdot k \cdot n/8, d_v)]$

$\hat{s} := Decode_{12}(sk)$

(66)

m'

$m' := Encode_1[Compress_q(v - NTT^{-1}(\hat{s}^T \circ NTT(u)), 1)]$

(67)

m'

pk

γ

c'

$pk := sk + 12 \cdot k \cdot n/8$

$h := sk + 24 \cdot k \cdot n/8 + 32$

$(\kappa, \gamma) := SHA3 - 512[m' || h]$

$c' \leftarrow CifradoKyber(pk, m', \gamma)$

(68)

z

$z := sk + 24 \cdot k \cdot n/8 + 64$

(69)

$c :=$

c

$K :=$

$SHAKE - 256[\kappa || SHA3 - 256(c)]$

$K :=$

$SHAKE - 256[z || SHA3 - 256(c)]$

$?$

$R_q = Z_q X^n + 1$

(70)

$\overline{B_{56}}$

$\overline{q_{13}}$

$?$

$?$

$?$

$$\begin{aligned}
& \begin{matrix} ? \\ (a, u) \\ (a, b) \\ a \leftarrow \mathcal{U}(R_q^{l \times l}) \\ s \leftarrow \beta_\mu(R_q^{l \times 1}) \\ b \in R_p^{l \times 1} \\ b = \lfloor pq(A \cdot s) \rfloor \end{matrix} \\
(82) \quad & \begin{matrix} \mathcal{U} \\ \beta_\mu \\ \sigma^\mu = \\ \sqrt{\mu/2} \\ l \\ \mathbf{bits}(x, i, j) \end{matrix}
\end{aligned}$$

$$\mathbf{bits}(x, i, j) = [x \gg (i-j)] \& (2^j - 1) = \begin{cases} x 2^{i-j \bmod +j} \\ \neq \\ i x \bmod +j \end{cases} \text{ si } j = i$$

$$\begin{aligned}
(83) \quad & \begin{matrix} \mathbf{Entrada:} \quad qpn l \mu \\ \mathbf{Salida:} \quad sk b A \\ A \in R_q^{l \times l} \\ sk \in R_q^{l \times 1} \\ \beta_\mu \\ b \in R_p^{l \times 1} \end{matrix} \\
(84) \quad & \begin{matrix} b := \mathbf{bits}(A \cdot s + h, \varepsilon_q, \varepsilon_p) \\ (sk, b, A) \\ \hat{\varepsilon}_i^i = \\ \log_2(i) \\ h \in R_q \\ 2^{\varepsilon_q - \varepsilon_p - 1} \\ \mathbf{Entrada:} \quad pk A qpt n l \mu \\ \mathbf{Salida:} \quad ss' b' c \\ s' \in R_q^{l \times 1} \\ \beta_\mu \\ b' \in R_p^{l \times 1} \\ v' \in R_p \\ A \\ b \end{matrix}
\end{aligned}$$

$$\begin{aligned}
& \begin{matrix} b' := \mathbf{bits}(A^T \cdot s' + h, \varepsilon_q, \varepsilon_p) \\ v' := b \cdot \mathbf{bits}(s', \varepsilon_p, \varepsilon_p) + h_1 \end{matrix} \\
(85) \quad & \begin{matrix} c \in R_t \\ v' \end{matrix}
\end{aligned}$$

$$\begin{aligned}
(86) \quad & \begin{matrix} c := \mathbf{bits}(v', \varepsilon_p - 1, \varepsilon_t) \\ ss \end{matrix}
\end{aligned}$$

$$\begin{aligned}
(87) \quad & \begin{matrix} ss' := \mathbf{bits}(v', \varepsilon_p, 1) \\ (ss', b', c) \\ h_1 \in R_q \\ 2^{\varepsilon_q - \varepsilon_p - 1} \\ \mathbf{Entrada:} \quad sk b' cpt \\ \mathbf{Salida:} \quad ss \\ v \in R_p \end{matrix}
\end{aligned}$$

$$\begin{aligned}
(88) \quad & \begin{matrix} v := b'^T \cdot \mathbf{bits}(s, \varepsilon_p, \varepsilon_p) + h_1 \\ ss \end{matrix}
\end{aligned}$$

$$\begin{aligned}
(89) \quad & \begin{matrix} ss := \mathbf{bits}(v - 2^{\varepsilon_p - \varepsilon_t - 1} \cdot c + h_2), \varepsilon_p, 1 \\ ss \\ h_2 \in \end{matrix}
\end{aligned}$$

Salida: $pk \in \mathcal{B}^{n \cdot l \cdot \varepsilon_p / 8 + 32} sk \in \mathcal{B}^{n \cdot l \cdot \varepsilon_q / 8 + n \cdot l \cdot \varepsilon_p / 8 + 96}$

$\overset{A}{z}$
 $seed_A$
 $seed_s$
 $z \in$
 B^{32}
 $seed_A$
 $seed_A := \text{SHAKE-128}(seed_A, 32)$

(105) $\overset{A}{buf} := \text{SHAKE-128}(seed_A, l^2 \cdot n \cdot \varepsilon_q / 8)$

(106) $\overset{buf}{l^2 \cdot}$
 $\overset{buf}{\varepsilon_q}$
 $k :=$
 0
 $A[i, j][k] :=$
 $buf[k]$
 $k :=$
 $k +$
 1
 $buf := \text{SHAKE-128}(seed_s, l \cdot n \cdot \mu / 8)$

(107) $\overset{buf}{2 \cdot}$
 $\overset{buf}{h}$
 $\mu / 2$
 $k :=$
 0
 $s[i, j] :=$
 $\text{HammingWeight}(buf[k]) -$
 $\text{HammingWeight}(buf[k +$
 $1]) \bmod^+ q$
 $k :=$
 $k +$
 2
 b

$b := (A^T \circ s + h \bmod^+ q) / 2^{\varepsilon_q - \varepsilon_p}$
(108)

$pk := seed_A || \text{POLVEC}_q 2\text{BS}(b)$

(109) $sk := z || \text{SHA3-256}(pk) || pk || \text{POLVEC}_q 2\text{BS}(s)$

(110) (pk, sk)

$\overset{c}{pk}$
 $\overset{n}{\gamma}$
 $\text{BS2POLVEC}_x(y)$

$\overset{y}{l}$
 $\overset{k}{256/8}$

$\overset{R_x^{l \times 1}}{\text{POL}_x 2\text{BS}(y)}$

$\overset{y}{R_x}$

$\overset{k}{256/8}$

Entrada: $pk \in \mathcal{B}^{n \cdot l \cdot \varepsilon_p / 8 + 32} m \in \mathcal{B}^{32} \gamma \in \mathcal{B}^{32}$

Salida: $c \in \mathcal{B}^{n \cdot l \cdot \varepsilon_p / 8 + n \cdot \varepsilon_t / 8}$

$\overset{A}{pk'}$

$\overset{pk}{s'}$
 $\overset{b'}$

$$(111) \quad b' := (A \circ s' + h \bmod^+ q) / 2^{\varepsilon_q - \varepsilon_p}$$

$$(112) \quad \overset{b}{b} := \text{BS2POLVEC}_p(pk')$$

$$(113) \quad \overset{v'}{c} := b^T \circ (s' \bmod^+ p) \bmod^+ p$$

$$(114) \quad \overset{c}{c} := (v' - m \cdot 2^{\varepsilon_p - 1} + h_1 \bmod^+ p) / 2^{\varepsilon_p - \varepsilon_t}$$

$\overset{c}{\text{POL}_T 2\text{BS}(c)} || \text{POLVEC}_p 2\text{BS}(b')$

$\overset{pk}{c}$
 $\overset{k}{\text{Entrada: } pk \in \mathcal{B}^{n \cdot l \cdot \varepsilon_p / 8 + 32}}$

$\overset{m}{\text{Salida: } c \in \mathcal{B}^{n \cdot l \cdot \varepsilon_p / 8 + n \cdot \varepsilon_t / 8} k \in \mathcal{B}^*}$
 $\overset{m}{\mathcal{B}^{32}}$
 $\overset{pk}{buf}$

$$(115) \quad \overset{m}{\gamma} := \text{SHA3-256}(m)$$

$$(116) \quad \overset{hash_{pk}}{c} := \text{SHA3-256}(pk)$$

$$(117) \quad \overset{buf}{k} := hash_{pk} || m$$

$$(118) \quad \overset{(\gamma || r)}{c, k} := \text{SHA3-512}(buf)$$

$\begin{matrix} c \\ s \\ k \end{matrix}$
Entrada: $c \in \mathcal{B}^{n \cdot l \cdot \varepsilon_p / 8 + n \cdot \varepsilon_t / 8}$ $sk \in \mathcal{B}^{n \cdot l \cdot \varepsilon_q / 8 + n \cdot l \cdot \varepsilon_p / 8 + 96}$
Salida: $k \in \mathcal{B}^*$
 $\begin{matrix} s \\ k' \\ z \\ s \end{matrix}$

$$(119) \quad s := \text{BS2POLVEC}_q(sk')$$

$$(120) \quad \begin{matrix} (c_m || ct) := c \\ m' \end{matrix}$$

$$(121) \quad \begin{matrix} c_m := c_m \cdot 2^{\varepsilon_p - \varepsilon_t} \\ b' := \text{BS2POLVEC}_p(ct) \\ m' := (b'^T \circ (smod^+ p) - c_m + h_2 mod^+ p) / 2^{\varepsilon_p - 1} \\ m \\ m := \text{POL}_2\text{BS}(m') \end{matrix}$$

$$(122) \quad \gamma$$

$$(123) \quad (\gamma || r) := \text{SHA3-512}(buf)$$

$$(124) \quad \begin{matrix} c' \\ \mathcal{E}' \\ c' := \text{Cifrado Saber}(pk, m, \gamma) \\ k \end{matrix}$$

$$(125) \quad \begin{matrix} k := \text{SHA3-256}(r || \text{SHA3-256}(c')) \\ k \end{matrix}$$

$$(126) \quad k := \text{SHA3-256}(z || \text{SHA3-256}(c'))$$

$$\begin{array}{l} ? \\ \mathfrak{z} \\ \mathcal{U} \\ F_2 \\ F_2^n \\ \mathcal{U} \\ \mathcal{R} = \\ F_2[x]/(C^n - \\ 1) \\ ? \\ \omega(x) \\ \mathfrak{H} \\ (X^n - \\ 1)/(X - \\ 1) \\ \mathcal{R} \\ u,v \in \\ \mathcal{U} \\ \mathcal{R} = \\ \mathcal{U} \end{array}$$

$$(127) \qquad w_k = \sum_{i+j=k \bmod +n} u_i \cdot v_j \forall k \in 0,,n-1$$

$$\begin{array}{l} \mathbf{rot}(h) \\ \mathcal{U} \in \\ \mathfrak{z} \\ h: \\ x^i \end{array}$$

$$\begin{array}{l} v=(v_0,,v_{n-1})\in F_2^n \\ \mathbf{rot}(v)=(\,v\,)_0 \\ v_{n-1} \\ v_1^1 \\ v_0^1 \\ v_2^0 \end{array}$$

$$\begin{array}{l} v_{n-1} \\ v_{n-2} \\ v_0 \end{array}$$

$$(128)$$

$$(129) \qquad \begin{array}{l} u,v \in \\ \mathcal{U} \\ u \cdot v = u \cdot \mathbf{rot}(v)^T = (\mathbf{rot}(u) \cdot v^T)^T = v \cdot u \end{array}$$

$$\begin{array}{l} C \\ \mathfrak{U} \\ \mathfrak{k} \\ [n,k] \\ \mathcal{R} \\ \mathfrak{k}_\gamma \in \\ F_2^{k \times n} \end{array}$$

$$(130) \qquad \begin{array}{l} C = \{m \cdot G, m \in F_2^k\} \\ H \in \\ F_2^{(n-k) \times n} \\ C^\perp \\ C \end{array}$$

$$(131) \qquad \begin{array}{l} C = \{v \in F_2^n | H \cdot v^T = 0\} \\ C^T = \{u \cdot \bar{H}, u \in F_2^k\} \end{array}$$

$$(132) \qquad \begin{array}{l} v \in \\ F_2^n \\ H \cdot v^T \rightarrow s \text{ if } v \in C \rightarrow H \cdot v^T = 0 \end{array}$$

$$(133) \qquad \begin{array}{l} C[n,k] \in \\ \mathcal{R} \\ d = \min_{u,v \in C, u \neq v} \omega(u-v) \end{array}$$

$$\begin{array}{l} \delta \\ \mathfrak{f}^+ \\ \mathcal{U} \\ \mathcal{U} \end{array}$$