## Code Listing

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```
1 from src.datasets import set_seed
from src.patchwisemodel import PatchWiseModel
3 from src.imagewisemodels import BaseCNN, DynamicCapsules, NazeriCNN
      , VariationalCapsules, SRCapsules
4 from src.mixedmodels import VariationalMixedCapsules, EffNet
5 from argparse import Namespace
7 if __name__ == "__main__":
      set_seed()
9
       args_patch_wise = Namespace(
10
          batch_size=32,
11
           lr=0.001,
           epochs=100,
13
           augment=True,
14
          flip=False,
15
           workers=4,
16
17
           classes=4,
           input_size=[3, 512, 512],
18
19
           output_size=[3, 64, 64],
           predefined_stats=True,
20
           data_path="./data/ICIAR2018/patchwise_dataset",
21
22
           checkpoint_path="./models/Checkpoints/",
           name="_patchwise_"
23
24
25
26
       args_img_wise = Namespace(
           lr=0.001,
27
           epochs=9,
28
29
           augment=True,
          flip=False,
30
           workers=4,
31
           classes=4,
32
           routings=3,
33
34
           lam_recon=0.392,
           pose_dim=4,
35
           batch_size=8,
           arch=[64,16,16,16],
37
           input_size=[3, 64, 64],
output_size=[3, 64, 64],
38
39
           data_path="./data/ICIAR2018/imagewise_dataset",
40
41
           checkpoint_path="./models/Checkpoints/",
           name="_imagewise_",
42
           predefined_stats=False
```

```
44
      # Example
46
47
      patch_wise_model = PatchWiseModel(args_patch_wise)
48
      patch_wise_model.train_model(args_patch_wise)
49
50
      patch_wise_model.test(args_patch_wise, voting=True)
      patch_wise_model.test_separate_classes(args_patch_wise)
51
      patch_wise_model.test_training(args_patch_wise)
52
      patch_wise_model.plot_metrics()
53
      patch_wise_model.save_checkpoint("./models/")
54
      patch_wise_model.save_model("./models/")
56
57
      image_wise_model = EffNet(args_img_wise)
      image_wise_model.train_model(args_img_wise)
58
       image_wise_model.test(args_img_wise, True)
59
60
      image_wise_model.test_separate_classes(args_img_wise)
      image_wise_model.test_training(args_img_wise)
61
62
      image_wise_model.plot_metrics()
      image_wise_model.save_checkpoint("./models/")
63
      image_wise_model.save_model("./models/")
```

Listing 1: main.py

```
from os.path import split
import torchvision.transforms as transforms
3 from torch.utils.data import DataLoader
4 from tqdm import tqdm
5 import numpy as np
6 import torchvision
7 import random
8 import torch
9 import torch
10 import os
12 VALIDATION_SET = 0.15
13 TRAINING_SET = 0.7
14 \text{ TEST\_SET} = 0.15
MEANS = [0.4731, 0.3757, 0.4117]
17 \text{ STD} = [0.3731, 0.3243, 0.3199]
19 IMAGE_SIZE = (2816, 3072)
20 CROPPED_IMAGE_SIZE = (1536, 2048)
gradeD_LABELS = ["Grade 1", "Grade 2", "Grade 3"]
BACH_LABELS = ["Benign", "InSitu", "Invasive", "Normal"]
BREAKHIS_LABELS = ["Benign", "Malignant"]
24 SEED = 123
26 PATCH_SIZE = 512
27 STRIDE = 256
28
29 def imshow(img):
30
      import matplotlib.pyplot as plt
      npimg = img.numpy()
31
      plt.imshow(np.transpose(npimg, (1, 2, 0)))
      plt.show()
33
```

```
35 def set_seed(seed=SEED):
       torch.backends.cudnn.deterministic = True
       torch.backends.cudnn.benchmark = False
37
       torch.manual_seed(seed)
38
      torch.cuda.manual_seed_all(seed)
39
      np.random.seed(seed)
40
41
      random.seed(seed)
42
43 def compute_normalization_stats(root_dir, test_set=TEST_SET,
       training_set=TRAINING_SET, val_set=VALIDATION_SET):
       from tqdm import tqdm
44
       set_seed(SEED)
45
       assert test_set + training_set + val_set == 1, "Train/Test/Val
46
      Set sizes incorrect"
      BATCH_SIZE = 1
47
48
49
       t = transforms.Compose([
           transforms.Resize(IMAGE_SIZE),
50
51
           transforms.ToTensor()
52
53
       data = torchvision.datasets.ImageFolder(root=root_dir+"/
54
      Histopathological_Graded", transform=t)
55
       size = int((training_set+val_set)*len(data))
56
57
       test\_size = len(data) - (size)
       train_data, _ = torch.utils.data.random_split(data, [size,
58
       test_size])
59
      data_loader = DataLoader(train_data, batch_size=BATCH_SIZE,
60
      num_workers=0)
      # Compute normalization metrics
61
      mean = 0.
62
      std = 0.
63
64
65
       # Training images
       i = 0
66
67
       for inputs, _ in tqdm(data_loader):
          input = inputs[0]
68
69
          temp = input.view(3, -1)
70
71
          mean += temp.mean(1)
           std += temp.std(1)
72
           i += 1
73
74
      print("Printing Normalization Metrics")
75
      mean /= size
76
       std /= size
77
      print("Means:", mean)
78
       print("Std:", std)
79
80
81 def split_test_train_val(root_dir, test_set=TEST_SET, training_set=
      TRAINING_SET, val_set=VALIDATION_SET, dataset="Databiox"):
       from tqdm import tqdm
82
83
       set_seed(SEED)
       assert test_set + training_set + val_set == 1, "Train/Test/Val
84
      Set sizes incorrect"
```

```
BATCH_SIZE = 1
85
       if dataset == "Databiox":
87
           t = transforms.Compose([
88
                transforms.Resize(IMAGE_SIZE),
89
                transforms.CenterCrop(CROPPED_IMAGE_SIZE),
90
91
                transforms.ToTensor()
           ])
92
           data = torchvision.datasets.ImageFolder(root=root_dir+"/
93
       Histopathological_Graded", transform=t)
            LABELS = GRADED_LABELS
94
       elif dataset == "BACH":
95
           t = transforms.Compose([
96
                transforms.Resize(CROPPED_IMAGE_SIZE),
97
                transforms.ToTensor()
98
99
100
           data = torchvision.datasets.ImageFolder(root=root_dir+"/
       ICIAR2018_BACH_Challenge/Photos", transform=t)
           LABELS = BACH_LABELS
       elif dataset == "BreakHis":
           t = transforms.Compose([
                transforms.Resize((PATCH_SIZE,PATCH_SIZE)),
                transforms.ToTensor()
106
           1)
           data = torchvision.datasets.ImageFolder(root=root_dir+"/
       BreaKHis_v1/histology_slides/breast", transform=t)
           LABELS = BREAKHIS_LABELS
108
109
           print("Dataset not recognised")
110
       train_size = int(training_set*len(data))
113
       val_size = int(val_set*len(data))
114
       test_size = len(data) - (train_size + val_size)
train_data, test_data, val_data = torch.utils.data.random_split
115
116
       (data, [train_size, test_size, val_size])
       train_data_loader = DataLoader(train_data, batch_size=
       BATCH_SIZE, num_workers=0)
       test_data_loader = DataLoader(test_data, batch_size=BATCH_SIZE,
118
        num_workers=0)
       val_data_loader = DataLoader(val_data, batch_size=BATCH_SIZE,
119
       num_workers=0)
       print("Number of training images:", len(train_data), "Number of
120
        test images:", len(test_data), "Number of validation images:",
        len(val_data))
       if not os.path.exists(root_dir):
123
           os.makedirs(root_dir)
124
       if dataset == "BreakHis":
125
           for t in ["train", "test", "validation"]:
126
                for i in range(len(LABELS)):
127
                    if not os.path.exists(root_dir + t + "/" + LABELS[i
128
       ]):
                        os.makedirs(root_dir + t + "/" + LABELS[i])
129
           for i, (inputs, labels) in tqdm(enumerate(train_data_loader
130
```

```
torchvision.utils.save_image(inputs, root_dir + "/train
       /" + LABELS[labels[0].item()] + "/image_" + str(i) + ".JPG")
           for i, (inputs, labels) in tqdm(enumerate(val_data_loader))
               torchvision.utils.save_image(inputs, root_dir + "/
       validation/" + LABELS[labels[0].item()] + "/image_" + str(i) +
       ".JPG")
           for i, (inputs, labels) in tqdm(enumerate(test_data_loader)
134
               torchvision.utils.save_image(inputs, root_dir + "/test/
       " + LABELS[labels[0].item()] + "/image_" + str(i) + ".JPG")
       else:
136
           for mode in ["/imagewise_dataset/", "/patchwise_dataset/"]:
               for t in ["train", "test", "validation"]:
138
                   for i in range(len(LABELS)):
139
                        if not os.path.exists(root_dir + mode + t + "/"
140
        + LABELS[i]):
                            os.makedirs(root_dir + mode + t + "/" +
141
       LABELS[i])
142
           # Training images
143
           i = 0
144
           for inputs, labels in tqdm(train_data_loader):
145
146
               input = inputs[0]
               # ImageWise
147
               patches = input.unfold(1, PATCH_SIZE, PATCH_SIZE).
148
       unfold(2, PATCH_SIZE, PATCH_SIZE)
               patches = patches.permute(1,2,0,3,4).contiguous()
149
               patches = patches.contiguous().view(-1, 3, PATCH_SIZE,
       PATCH_SIZE)
               for j, patch in enumerate(patches):
                   torchvision.utils.save_image(patch, root_dir + "/
       imagewise_dataset/train/" + LABELS[labels[0].item()] + "/image_
       " + str(i) + "patch_" + str(j) + ".JPG")
153
               # PatchWise
154
               patches = input.unfold(1, PATCH_SIZE, STRIDE).unfold(2,
        PATCH_SIZE, STRIDE)
               patches = patches.permute(1,2,0,3,4).contiguous()
156
               patches = patches.contiguous().view(-1, 3, PATCH_SIZE,
157
       PATCH_SIZE)
               for j, patch in enumerate(patches):
158
                   torchvision.utils.save_image(patch, root_dir + "/
159
       patchwise_dataset/train/" + LABELS[labels[0].item()] + "/image_
        + str(i) + "patch_" + str(j) + ".JPG")
               i += 1
160
161
           # Validation images
162
           i = 0
           for inputs, labels in tqdm(val_data_loader):
164
               input = inputs[0]
165
               # ImageWise
               patches = input.unfold(1, PATCH_SIZE, PATCH_SIZE).
167
       unfold(2, PATCH_SIZE, PATCH_SIZE)
168
               patches = patches.permute(1,2,0,3,4).contiguous()
               patches = patches.contiguous().view(-1, 3, PATCH_SIZE,
169
       PATCH_SIZE)
```

```
for j, patch in enumerate(patches):
                    torchvision.utils.save_image(patch, root_dir + "/
171
       imagewise_dataset/validation/" + LABELS[labels[0].item()] + "/
       image_" + str(i) + "patch_" + str(j) + ".JPG")
               # PatchWise
173
174
               patches = input.unfold(1, PATCH_SIZE, STRIDE).unfold(2,
        PATCH_SIZE, STRIDE)
               patches = patches.permute(1,2,0,3,4).contiguous()
               patches = patches.contiguous().view(-1, 3, PATCH_SIZE,
       PATCH_SIZE)
               for j, patch in enumerate(patches):
                   torchvision.utils.save_image(patch, root_dir + "/
178
       patchwise_dataset/validation/" + LABELS[labels[0].item()] + "/
       image_" + str(i) + "patch_" + str(j) + ".JPG")
179
180
           # Test images
181
           i = 0
           for inputs, labels in tqdm(test_data_loader):
183
                input = inputs[0]
184
               # ImageWise
185
               patches = input.unfold(1, PATCH_SIZE, PATCH_SIZE).
186
       unfold(2, PATCH_SIZE, PATCH_SIZE)
               patches = patches.permute(1,2,0,3,4).contiguous()
187
               patches = patches.contiguous().view(-1, 3, PATCH_SIZE,
       PATCH SIZE)
189
               for j, patch in enumerate(patches):
                    torchvision.utils.save_image(patch, root_dir + "/
190
       imagewise_dataset/test/" + LABELS[labels[0].item()] + "/image_"
        + str(i) + "patch_" + str(j) + ".JPG")
191
               # PatchWise
192
               patches = input.unfold(1, PATCH_SIZE, STRIDE).unfold(2,
        PATCH_SIZE, STRIDE)
               patches = patches.permute(1,2,0,3,4).contiguous()
               patches = patches.contiguous().view(-1, 3, PATCH_SIZE,
       PATCH_SIZE)
196
               for j, patch in enumerate(patches):
                    torchvision.utils.save_image(patch, root_dir + "/
197
       patchwise_dataset/test/" + LABELS[labels[0].item()] + "/image_"
        + str(i) + "patch_" + str(j) + ".JPG")
               i += 1
198
199
   def check_res(root_dir):
200
       import matplotlib.pyplot as plt
201
       sizes = {}
202
       data = torchvision.datasets.ImageFolder(root=root_dir+"/
203
       Histopathological_Graded", transform=transforms.Compose([
       transforms.ToTensor()]))
       data_loader = DataLoader(data , batch_size=1, num_workers=0)
204
       for inputs, _ in tqdm(data_loader):
205
206
           t = inputs.shape
           if t in sizes:
207
208
               sizes[t] +=1
209
           else:
              sizes[t] = 1
210
```

Listing 2: src/datasets.py

```
# For the docs
import matplotlib.pyplot as plt
4 # Data
from torch.utils.data import DataLoader, ConcatDataset
6 import torchvision.transforms as transforms
7 from .datasets import MEANS, STD
8 from tqdm import tqdm
9 import torchvision
10 import PIL
11
12 # Training
13 import torch.optim as optim
14 import torch.nn as nn
15 import numpy as np
16 import torch
17 import copy
18 import time
19 import os
20
# For testing we want to get a whole image in patches
22 BATCH_SIZE = 12
23
24 class Model(nn.Module):
25
26
      Basic module class, imagewise, patchwise and mixed models
      inherit from this one, overwriting the propagate method
27
28
      def __init__(self, args):
          super(Model, self).__init__()
29
30
           self.name = args.name
          self.time = str(time.strftime(', %Y-%m-%d_%H-%M'))
31
32
          if "breakhis" in args.data_path.lower():
33
               self.breakhis = True
34
35
           else:
               self.breakhis = False
36
37
      def init_device(self):
38
           """ Sends model to CPU / GPU """
39
           self.device = torch.device("cuda" if torch.cuda.
40
      is_available() else "cpu")
          self.to(self.device)
41
42
          print(self)
43
44
           print("Parameters:", sum(p.numel() for p in super(Model,
      self).parameters()))
           print("Trainable parameters:", sum(p.numel() for p in super
       (Model, self).parameters() if p.requires_grad))
          print("Using:", self.device)
```

```
47
48
           # Additional Info when using cuda
           if self.device.type == 'cuda':
49
               print(torch.cuda.get_device_name(0))
50
               print('Memory Usage:')
51
               print('Allocated:', round(torch.cuda.memory_allocated
       (0)/1024**3,1), 'GB')
               print('Cached:
                                ', round(torch.cuda.memory_reserved(0)
       /1024**3,1), 'GB')
55
       def train_model(self, args, path=None):
           """ Main Training loop with data augmentation, early
56
      stopping and scheduler """
           print('Start training network: {}\n'.format(time.strftime('
      %Y/%m/%d %H:%M')))
58
59
           if not args.predefined_stats:
               means = [0.5, 0.5, 0.5]
60
61
               std = [0.5, 0.5, 0.5]
           else:
62
               means = MEANS
63
               std = STD
64
65
           validation_transforms = transforms.Compose([
66
               transforms.ToTensor(),
67
68
               transforms.Normalize(mean=means, std=std)
          1)
69
70
71
           if args.augment:
72
               Create versions of the dataset for each augmentation as
73
        in https://arxiv.org/abs/1803.04054 and others
74
               augmenting = [
75
                   # 0 degrees
76
77
                   transforms.Compose([
                        transforms.ColorJitter(hue=.05, saturation=.05)
78
                        transforms.ToTensor(),
79
                        transforms.Normalize(mean=means, std=std)
80
                   ]),
81
                   # 90 degrees
82
83
                   transforms.Compose([
                        transforms.RandomRotation((90, 90), resample=
84
      PIL. Image.BILINEAR),
                        transforms.ColorJitter(hue=.05, saturation=.05)
85
86
                        transforms.ToTensor(),
                        transforms.Normalize(mean=means, std=std)
87
                   ]),
88
                   # 180 degrees
89
                   transforms.Compose([
90
                        transforms.RandomRotation((180, 180), resample=
91
      PIL. Image. BILINEAR),
                        transforms.ColorJitter(hue=.05, saturation=.05)
92
                       transforms.ToTensor(),
93
```

```
transforms.Normalize(mean=means, std=std)
94
95
                    ]),
                    # 270 degrees + flip
96
                    transforms.Compose([
97
                        transforms.RandomRotation((270, 270), resample=
98
       PIL. Image. BILINEAR),
                        transforms.ColorJitter(hue=.05, saturation=.05)
                        transforms.ToTensor(),
                        transforms.Normalize(mean=means, std=std)
                    ])
               ]
103
104
105
                if args.flip:
                    augmenting += [
106
                        transforms.Compose([
107
108
                            transforms.RandomVerticalFlip(p=1.),
                            transforms.ColorJitter(hue=.05, saturation
109
       =.05),
                            transforms.ToTensor(),
                            transforms.Normalize(mean=means, std=std)
111
                        ]),
                        transforms.Compose([
113
114
                            transforms.RandomVerticalFlip(p=1.),
                            transforms.RandomRotation((90, 90),
       resample=PIL.Image.BILINEAR),
                            transforms.ColorJitter(hue=.05, saturation
       =.05),
                            transforms.ToTensor(),
                            transforms.Normalize(mean=means, std=std)
118
                        ]),
119
                        transforms.Compose([
120
                            transforms.RandomVerticalFlip(p=1.),
121
                            transforms.RandomRotation((180, 180),
       resample=PIL.Image.BILINEAR),
                            transforms.ColorJitter(hue=.05, saturation
123
       =.05),
                            transforms.ToTensor(),
                            transforms.Normalize(mean=means, std=std)
126
                        transforms.Compose([
127
                            transforms.RandomVerticalFlip(p=1.),
128
                            transforms.RandomRotation((270, 270),
129
       resample=PIL.Image.BILINEAR),
                            transforms.ColorJitter(hue=.05, saturation
130
       =.05),
                            transforms.ToTensor(),
                            transforms.Normalize(mean=means, std=std)
132
                        ])
133
                    ]
134
                train_data_loader = DataLoader(
136
137
                    ConcatDataset([
                        torchvision.datasets.ImageFolder(root=args.
       data_path + "/train", transform=t) for t in augmenting
                    ]),
139
                    batch_size=args.batch_size, shuffle=True,
140
```

```
num_workers=args.workers
141
142
           else:
143
                training_transforms = transforms.Compose([
144
                    transforms.RandomHorizontalFlip(),
145
146
                    transforms.RandomVerticalFlip(),
                    transforms.RandomRotation(10, resample=PIL.Image.
147
       BILINEAR),
                    transforms.ColorJitter(hue=.05, saturation=.05),
148
                    transforms.ToTensor(),
149
                    transforms.Normalize(mean=means, std=std)
                train_data = torchvision.datasets.ImageFolder(root=args
       .data_path + "/train", transform=training_transforms)
                train_data_loader = DataLoader(train_data, batch_size=
153
       args.batch_size, shuffle=True, num_workers=args.workers)
154
           val_data = torchvision.datasets.ImageFolder(root=args.
       data_path + "/validation", transform=validation_transforms)
           val_data_loader = DataLoader(val_data, batch_size=args.
       batch_size, shuffle=True, num_workers=args.workers)
158
           print("Using ", len(train_data_loader.dataset), "training
       samples")
           print("Using ", len(val_data_loader.dataset), "validation
       samples")
           optimizer = optim.Adam(self.parameters(), lr=args.lr)
161
           scheduler = optim.lr_scheduler.StepLR(optimizer, step_size
       =20, gamma=0.1)
           criterion = nn.CrossEntropyLoss()
           start_epoch = 0
164
165
           # If checkpoint provided load states
167
           if path:
               optimizer, start_epoch = self.load_ckp(path, optimizer)
169
               print("Model loaded, trained for ", start_epoch, "
       epochs")
           # keeping track of losses
           self.train_losses = []
172
           self.valid_losses = []
173
           self.train_acc = []
           self.val_acc = []
           since = time.time()
176
177
178
           # For "early stopping"
           best_model_wts = copy.deepcopy(self.state_dict())
179
           best_acc = 0.
181
           for epoch in range(start_epoch, args.epochs):
182
183
               print('Epoch {}/{}'.format(epoch+1, args.epochs))
               print('-' * 10)
185
               # Each epoch has a training and validation phase
186
               for phase in ['train', 'val']:
187
```

```
if phase == 'train':
188
                         super(Model, self).train() # Set model to
       training mode
                         dataloader = train_data_loader
190
                    else:
191
                        super(Model, self).eval() # Set model to
       evaluate mode
                        dataloader = val_data_loader
194
195
                    running_loss = 0.0
                    running_corrects = 0
196
197
                    # Iterate over data.
198
                    for inputs, labels in tqdm(dataloader):
199
                        inputs = inputs.to(self.device)
200
                        labels = labels.to(self.device)
201
202
                        # zero the parameter gradients
203
204
                        optimizer.zero_grad()
205
                        # Training here
206
                        with torch.set_grad_enabled(phase == 'train'):
207
                             # Overwrite this for each model
208
                             loss, preds = self.propagate(inputs, labels
209
       , criterion)
210
                             _, preds = torch.max(preds, 1)
                             # backward + optimize only if in training
212
       phase
                             if phase == 'train':
213
214
                                 loss.backward()
                                 optimizer.step()
215
216
                        # statistics
                        running_loss += loss.item() * inputs.size(0)
218
219
                        running_corrects += torch.sum(preds == labels.
       data)
220
                    # Adjust learning rate
221
222
                    if phase == 'train':
                        scheduler.step()
223
224
225
                    # Data metrics
                    epoch_loss = running_loss /len(dataloader.dataset)
226
                    epoch_acc = running_corrects.double() / len(
227
       dataloader.dataset)
228
                    print('{} Loss: {:.4f} Acc: {:.4f}'.format(
229
                        phase, epoch_loss, epoch_acc))
230
231
                    if phase == 'train':
                        self.train_losses.append(epoch_loss)
233
234
                        self.train_acc.append(epoch_acc)
                    else:
235
236
                        self.valid_losses.append(epoch_loss)
                        self.val_acc.append(epoch_acc)
238
```

```
# deep copy the model
239
                    if phase == 'val' and epoch_acc > best_acc:
240
                        best_acc = epoch_acc
241
                        best_model_wts = copy.deepcopy(self.state_dict
242
       ())
                        checkpoint = {
243
244
                             'epoch': epoch + 1,
                             'state_dict': best_model_wts,
245
                             'optimizer': optimizer.state_dict(),
246
247
                             'loss': criterion
248
                        file_name = "checkpoint_"+ str(epoch + 1) +
249
       args.name + self.time + ".ckpt"
                        torch.save(checkpoint, args.checkpoint_path +
       file_name)
251
           # Finished
           time_elapsed = time.time() - since
253
254
           print('Training complete in {:.0f}m {:.0f}s'.format(
                time_elapsed // 60, time_elapsed % 60))
255
           print('Best Validation Accuracy: {:4f}'.format(best_acc))
256
257
           # load best model weights and save checkpoint
258
259
           self.load_state_dict(best_model_wts)
260
       def propagate(self, inputs, labels, criterion=None):
261
              Default Training step - some models use this """
262
           outputs = self(inputs)
263
264
           if criterion:
                loss = criterion(outputs, labels)
265
266
                loss = 0
267
           return loss, outputs
268
269
270
       def plot_metrics(self, path, pr=False, pl=True):
271
             "" Plots accuracy and loss side-by-side """
272
273
           # Plotting on HPC throws error
           if pl:
274
                # Loss
275
                plt.subplot(1, 2, 1)
                plt.plot(self.train_losses, label='Training loss')
277
                plt.plot(self.valid_losses, label='Validation loss')
278
                plt.xlabel("Epochs")
279
                plt.ylabel("Loss")
280
281
                plt.legend(frameon=False)
                plt.savefig(path + "loss.png")
282
283
                # Accuracy
284
                plt.subplot(1, 2, 2)
285
                plt.plot(self.train_acc, label='Training Accuracy')
286
                plt.plot(self.val_acc, label='Validation Accuracy')
287
                plt.xlabel("Epochs")
                plt.ylabel("Acc")
289
290
                plt.legend(frameon=False)
                plt.savefig(path + "accuracy.png")
291
```

```
if pr:
293
                print(self.train_losses, self.valid_losses, self.
       train_acc, self.val_acc, sep="\n")
       def test(self, args, voting=False):
296
            """ Test on patched dataset ""
297
298
            if not args.predefined_stats:
299
                means = [0.5, 0.5, 0.5]
300
                std = [0.5, 0.5, 0.5]
301
302
                means = MEANS
303
                std = STD
304
305
            test_data = torchvision.datasets.ImageFolder(root=args.
306
       data_path + "/test", transform=transforms.Compose([
307
                transforms.ToTensor(),
                transforms.Normalize(mean=means, std=std)
308
309
           1))
            test_data_loader = DataLoader(test_data, batch_size=
310
       BATCH_SIZE, shuffle=False, num_workers=args.workers)
311
            super(Model, self).eval()
312
313
            with torch.no_grad():
                patch_acc = 0
314
                image_acc_maj = 0
                image_acc_sum = 0
316
                image_acc_max = 0
317
                conf = []
318
                for images, labels in tqdm(test_data_loader):
319
                    images = images.to(self.device)
                    labels = labels.to(self.device)
321
                    _, preds = self.propagate(images, labels)
322
                     _, predicted = torch.max(preds, 1)
323
                    patch_acc += (predicted == labels).sum().item()
324
325
                    if not self.breakhis and voting:
327
                        # Voting
                        preds = preds.cpu()
328
                        predicted = predicted.cpu()
329
                        maj_prob = (args.classes - 1) - np.argmax(np.
331
       sum(np.eye(args.classes)[np.array(predicted).reshape(-1)], axis
       =0)[::-1])
       sum_prob = (args.classes - 1) - np.argmax(np.
sum(np.exp(preds.numpy()), axis=0)[::-1])
                        max_prob = (args.classes - 1) - np.argmax(np.
       max(np.exp(preds.numpy()), axis=0)[::-1])
334
                         confidence = np.sum(np.array(predicted) ==
       maj_prob) / predicted.size(0)
                        conf.append(np.round(confidence * 100, 2))
337
                         if labels.data[0].item() == maj_prob:
339
                             image_acc_maj += 1
340
                        if labels.data[0].item() == sum_prob:
341
```

```
image_acc_sum += 1
342
343
                        if labels.data[0].item() == max_prob:
344
                            image_acc_max += 1
345
346
           patch_acc /= len(test_data_loader.dataset)
347
           print('Test Accuracy of the model: {:.2f}'.format(patch_acc
348
350
           if not self.breakhis and voting:
                print('Average Confidence: {:.2f}'.format(sum(conf)/len
351
       (conf)))
                image_acc_maj /= (len(test_data_loader.dataset)/12)
352
353
                image_acc_sum /= (len(test_data_loader.dataset)/12)
                image_acc_max /= (len(test_data_loader.dataset)/12)
354
355
356
                print('Test Accuracy of the model on with majority
       voting: {:.2f}'.format(image_acc_maj))
                print('Test Accuracy of the model on with sum voting:
       {:.2f}'.format(image_acc_sum))
                print('Test Accuracy of the model on with max voting:
       {:.2f}'.format(image_acc_max))
359
360
       def test_separate_classes(self, args):
            """ Tests the model on each class separately and reports
361
       classification metrics """
           if not args.predefined_stats:
362
                means = [0.5, 0.5, 0.5]
363
                std = [0.5, 0.5, 0.5]
364
365
           else:
                means = MEANS
366
                std = STD
367
368
           test_data = torchvision.datasets.ImageFolder(root=args.
369
       data_path + "/test", transform=transforms.Compose([
                transforms.ToTensor(),
                transforms.Normalize(mean=means, std=std)
371
372
           ]))
           test_data_loader = DataLoader(test_data, batch_size=args.
373
       batch_size, num_workers=args.workers)
           conf_matrix = torch.zeros(args.classes, args.classes)
374
375
376
           super(Model, self).eval()
           with torch.no_grad():
377
                for images, labels in tqdm(test_data_loader):
378
                    images = images.to(self.device)
379
                    labels = labels.to(self.device)
380
                    _, predicted = self.propagate(images, labels)
381
                    _, predicted = torch.max(predicted, 1)
382
                    predicted = predicted.tolist()
383
                    labels = labels.tolist()
384
385
386
                    for t, p in zip(labels, predicted):
                        conf_matrix[t, p] += 1
387
388
           print('Confusion matrix\n', conf_matrix)
389
390
```

```
TP = conf_matrix.diag()
            for c in range(args.classes):
392
                idx = torch.ones(args.classes)
393
                idx = idx.type(torch.BoolTensor)
394
                idx[c] = 0
395
                # all non-class samples classified as non-class
396
397
               TN = conf_matrix[idx.nonzero(as_tuple=False)[:, None],
       idx.nonzero(as_tuple=False)].sum() #conf_matrix[idx[:, None],
       idx].sum() - conf_matrix[idx, c].sum()
398
                # all non-class samples classified as class
                FP = conf_matrix[idx, c].sum()
399
                # all class samples not classified as class
400
                FN = conf_matrix[c, idx].sum()
401
402
                print('Class {}\nTP {}, TN {}, FP {}, FN {}'.format(
403
                    c, TP[c], TN, FP, FN))
404
405
                print('Sensitivity {:.2f}, Specificity {:.2f}, F1 {:.2f
       }, Accuracy {:.2f}'.format(
                    TP[c] / (TP[c]+FN), TN / (TN + FP), 2*TP[c] / (2*TP
       [c] + FP + FN), ((TP[c] + TN) / (TP[c] + TN + FP + FN))))
       def test_training(self, args):
408
           """ Test on patched training dataset for debugging """
409
410
           if not args.predefined_stats:
411
                means = [0.5, 0.5, 0.5]
412
                std = [0.5, 0.5, 0.5]
413
414
           else:
               means = MEANS
415
                std = STD
416
417
           train_data = torchvision.datasets.ImageFolder(root=args.
418
       data_path + "/train", transform=transforms.Compose([
                transforms.ToTensor(),
419
420
                transforms.Normalize(mean=means, std=std)
           1))
421
           train_data_loader = DataLoader(train_data, batch_size=args.
422
       batch_size, shuffle=True, num_workers=args.workers)
423
           super(Model, self).eval()
424
           with torch.no_grad():
425
                correct = 0
426
                for images, labels in tqdm(train_data_loader):
427
                    images = images.to(self.device)
428
                    labels = labels.to(self.device)
429
                    _, predicted = self.propagate(images, labels)
430
                    _, predicted = torch.max(predicted, 1)
431
432
                    correct += (predicted == labels).sum().item()
433
           print('Training Accuracy of the model: {:.2f}'.format(
       correct / len(train_data_loader.dataset)))
435
436
       def save_model(self, path):
            """ Save model after training has finished """
437
           file_name = path + self.name + self.time + ".ckpt"
438
           torch.save(self.state_dict(), file_name)
439
           print("Model saved:", file_name)
440
```

```
return file_name
441
442
       def load(self, path):
443
            """ Load pre-trained weights """
444
           try:
445
                if os.path.exists(path):
446
                    print('Loading model...')
447
                    self.load_state_dict(torch.load(path, map_location=
448
       self.device))
449
           except:
                print('Failed to load pre-trained network with path:',
450
       path)
451
452
       def load_ckp(self, checkpoint_fpath, optimizer):
            """ To continue training we need more than just saving the
453
       weights ""'
454
           checkpoint = torch.load(checkpoint_fpath, map_location=self
       .device)
455
           self.load_state_dict(checkpoint['state_dict'])
           optimizer.load_state_dict(checkpoint['optimizer'])
456
           return optimizer, checkpoint['epoch']
```

Listing 3: src/model.py

```
import torch.nn.functional as F
2 from .model import Model
3 import torch.nn as nn
5
  class PatchWiseModel(Model):
6
      A CNN classifier that is used by the image-wise networks to
      downscale the images
9
      by feeding them though the convolutional layers of the trained
      patchwise net.
10
11
      def __init__(self, args, original_architecture=False):
          super(PatchWiseModel, self).__init__(args)
12
13
           if original_architecture:
14
               This is the original architecture proposed in: https://
      arxiv.org/abs/1803.04054
16
               self.features = nn.Sequential(
17
                   # Block 1
18
                   nn.Conv2d(in_channels=args.input_size[0],
19
      out_channels=16, kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(16),
20
21
                   nn.ReLU(inplace=True),
                   nn.Conv2d(in_channels=16, out_channels=16,
22
      kernel_size=3, stride=1, padding=1),
23
                   nn.BatchNorm2d(16),
                   nn.ReLU(inplace=True),
24
25
                   nn.Conv2d(in_channels=16, out_channels=16,
      kernel_size=2, stride=2),
                   nn.BatchNorm2d(16),
                   nn.ReLU(inplace=True),
27
```

```
# Block 2
29
                   nn.Conv2d(in_channels=16, out_channels=32,
      kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(32),
31
                   nn.ReLU(inplace=True),
                   nn.Conv2d(in_channels=32, out_channels=32,
33
       kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(32),
34
                   nn.ReLU(inplace=True),
35
                   nn.Conv2d(in_channels=32, out_channels=32,
36
      kernel_size=2, stride=2),
                   nn.BatchNorm2d(32),
37
                   nn.ReLU(inplace=True),
38
39
                   # Block 3
40
                   nn.Conv2d(in_channels=32, out_channels=64,
41
      kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(64),
42
43
                   nn.ReLU(inplace=True),
                   nn.Conv2d(in_channels=64, out_channels=64,
44
       kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(64),
45
                   nn.ReLU(inplace=True),
46
                   nn.Conv2d(in_channels=64, out_channels=64,
47
      kernel_size=2, stride=2),
                   nn.BatchNorm2d(64),
48
                   nn.ReLU(inplace=True),
49
50
                   # Block 4
51
                   nn.Conv2d(in_channels=64, out_channels=128,
52
       kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(128),
53
                   nn.ReLU(inplace=True),
54
                   nn.Conv2d(in_channels=128, out_channels=128,
      kernel_size=3, stride=1, padding=1),
56
                   nn.BatchNorm2d(128),
                   nn.ReLU(inplace=True),
58
                   nn.Conv2d(in_channels=128, out_channels=128,
      kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(128),
59
                   nn.ReLU(inplace=True),
60
61
62
                   # Block 5
                   nn.Conv2d(in_channels=128, out_channels=256,
63
       kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(256),
                   nn.ReLU(inplace=True),
65
                   nn.Conv2d(in_channels=256, out_channels=256,
66
      kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(256)
67
                   nn.ReLU(inplace=True),
68
                   nn.Conv2d(in_channels=256, out_channels=256,
69
      kernel_size=3, stride=1, padding=1),
                   nn.BatchNorm2d(256),
70
71
                   nn.ReLU(inplace=True),
72
                   nn.Conv2d(in_channels=256, out_channels=args.
```

```
output_size[0], kernel_size=1, stride=1),
75
           else:
76
               Smaller version using 10 conv layers instead of 16
77
78
79
               self.features = nn.Sequential(
                    # Block 1
80
                    nn.Conv2d(in_channels=args.input_size[0],
81
       out_channels=16, kernel_size=3, stride=1, padding=1),
                    nn.BatchNorm2d(16),
82
                    nn.ReLU(inplace=True),
83
                    nn.Conv2d(in_channels=16, out_channels=16,
84
       kernel_size=3, stride=1, padding=1),
                    nn.BatchNorm2d(16),
85
                    nn.ReLU(inplace=True),
86
87
                    nn.Conv2d(in_channels=16, out_channels=16,
       kernel_size=2, stride=2),
                    nn.BatchNorm2d(16),
                    nn.ReLU(inplace=True),
89
90
                    # Block 2
91
                    nn.Conv2d(in_channels=16, out_channels=32,
92
       kernel_size=3, stride=1, padding=1),
                    nn.BatchNorm2d(32),
93
                    nn.ReLU(inplace=True),
94
                    nn.Conv2d(in_channels=32, out_channels=32,
95
       kernel_size=3, stride=1, padding=1),
                    nn.BatchNorm2d(32),
96
                    nn.ReLU(inplace=True),
97
                    nn.Conv2d(in_channels=32, out_channels=32,
       kernel_size=2, stride=2).
                    nn.BatchNorm2d(32),
99
                    nn.ReLU(inplace=True),
100
                    # Block 3
                    nn.Conv2d(in_channels=32, out_channels=64,
       kernel_size=3, stride=1, padding=1),
                    nn.BatchNorm2d(64),
104
105
                    nn.ReLU(inplace=True),
                    nn.Conv2d(in_channels=64, out_channels=64,
106
       kernel_size=3, stride=1, padding=1),
107
                    nn.BatchNorm2d(64),
                    nn.ReLU(inplace=True),
108
                    nn.Conv2d(in_channels=64, out_channels=64,
109
       kernel_size=2, stride=2),
                    nn.BatchNorm2d(64),
                    nn.ReLU(inplace=True),
111
                    nn.Conv2d(in_channels=64, out_channels=args.
113
       output_size[0], kernel_size=1, stride=1),
114
115
           # The classification layer
116
           self.classifier = nn.Sequential(
117
               nn.Linear(args.output_size[0] * args.output_size[1] *
118
       args.output_size[2], args.classes),
```

```
119
120
            self.initialize_weights()
121
122
           # This will send net to device, so only call here
            self.init_device()
124
125
       def initialize_weights(self):
126
            """ As in https://arxiv.org/abs/1803.04054 """
127
            for m in self.modules():
128
                if isinstance(m, nn.Conv2d):
129
                    nn.init.kaiming_normal_(m.weight, nonlinearity='
130
       relu')
131
                    if m.bias is not None:
                        m.bias.data.zero_()
133
                elif isinstance(m, nn.BatchNorm2d):
134
                    m.weight.data.fill_(1)
135
136
                    m.bias.data.zero_()
137
                elif isinstance(m, nn.Linear):
138
                    m.weight.data.normal_(0, 0.01)
139
                    m.bias.data.zero_()
140
141
       def forward(self, x):
142
           x = self.features(x)
143
           x = x.view(x.size(0), -1)
144
           x = self.classifier(x)
145
           x = F.\log_softmax(x, dim=1)
146
           return x
147
```

Listing 4: src/patchwisemodel.py

```
1 # Base Models
from .patchwisemodel import PatchWiseModel
3 from .model import Model
5 # Dynamic
6 from .DynamicCaps.capsulelayers import DenseCapsule, PrimaryCapsule
7 from .DynamicCaps.capsulenet import caps_loss
9 # Varcaps
10 from .VarCaps import layers
from .VarCaps import vb_routing
13 # SR Capsules
14 from .SRCaps.modules import SelfRouting2d
15
16 # Data
import torchvision.transforms as transforms
18 from torch.utils.data import DataLoader
19 from .datasets import MEANS, STD
20 import torchvision
21
22 # Training
23 from torch.autograd import Variable
24 import torch.nn.functional as F
25 import torch.nn as nn
```

```
26 import numpy as np
27 import torch
28
29
30 class ImageWiseModels(Model):
31
32
      Base Image-Wise model, variants inherit from this class
      it assigns a hopefully trained patchwise net to the model to
33
      use for forward passes
34
      def __init__(self, args, patchwise, original_architecture):
35
36
           super(ImageWiseModels, self).__init__(args)
37
38
           if patchwise is not None:
               self.patch_wise_model = patchwise
39
           else:
40
41
               print("Creating untrained patchwise model")
               self.patch_wise_model = PatchWiseModel(args,
42
      original_architecture=original_architecture)
43
      def propagate(self, inputs, labels, criterion=None):
44
           inputs = self.patch_wise_model.features(inputs)
45
           outputs = self(inputs)
46
47
           if criterion:
               loss = criterion(outputs, labels)
48
49
               loss = 0
50
51
           return loss, outputs
52
  class BaseCNN(ImageWiseModels):
53
       """ Simpler CNN baseline than Nazeri """
       def __init__(self, args, patchwise=None, original_architecture=
55
          super(BaseCNN, self).__init__(args, patchwise,
56
      original_architecture)
           self.cnn_layers = nn.Sequential(
58
59
               # Convolutional Layer 1
               nn.Conv2d(args.input_size[0], 32, kernel_size=5, stride
60
      =1, bias=False),
               nn.BatchNorm2d(32),
61
               nn.ReLU(inplace=True),
62
63
               nn.MaxPool2d(3, 1),
64
               # Convolutional Layer 2
65
               nn.Conv2d(32, 32, kernel_size=5, stride=1, bias=False),
66
               nn.BatchNorm2d(32),
67
68
               nn.ReLU(inplace=True),
               nn.MaxPool2d(3, 1),
69
70
               # Convolutional Layer 3
71
               nn.Conv2d(32, 16, kernel_size=5, stride=1, bias=False),
72
73
               nn.BatchNorm2d(16),
               nn.ReLU(inplace=True),
74
               nn.MaxPool2d(3, 1),
75
          )
76
```

```
self.device = torch.device("cuda:0" if torch.cuda.
78
       is_available() else "cpu")
           self.to(self.device)
79
80
           self.set_linear_layer(args)
81
82
           # This will send net to device, so only call here
83
           self.init_device()
84
       def forward(self, x):
86
           x = self.cnn_layers(x)
87
           x = x.view(x.size(0), -1)
88
           x = self.linear_layers(x)
89
90
           return x
91
       def set_linear_layer(self, args):
92
            """ Pytorch has no nice way of connecting CNNs with the
93
       denselayers, this code sets the dimensions correctly on the fly
           train_data = torchvision.datasets.ImageFolder(root=args.
94
       data_path + "/train", transform=transforms.Compose([
               transforms.ToTensor(),
95
                transforms.Normalize(mean=MEANS, std=STD)
96
97
           1))
           train_data_loader = DataLoader(train_data, batch_size=args.
98
       batch_size, shuffle=True, num_workers=args.workers)
           super(BaseCNN, self).train() # Set model to training mode
99
           data, _ = next(iter(train_data_loader))
#data = data[0]
           x = data.to(self.device)
           x = self.patch_wise_model.features(x)
           x = self.cnn_layers(x)
104
           print("Setting Linear Layer with shape:", x.shape)
106
           self.linear_layers = nn.Sequential(
107
108
               nn.Linear(x.size(1)*x.size(2)*x.size(3), 64),
               nn.ReLU(inplace=True),
               nn.Dropout(0.5)
               nn.Linear(64, 32)
111
112
               nn.ReLU(inplace=True),
113
               #nn.Dropout(0.5),
               nn.Linear(32, args.classes) # NO softmax, bc it is in
114
       crossentropy loss
           self.to(self.device)
116
117
   class NazeriCNN(ImageWiseModels):
118
       """ CNN imagewise network as in https://arxiv.org/abs
119
       /1803.04054 """
       def __init__(self, args, patchwise=None, original_architecture=
       False):
           super(NazeriCNN, self).__init__(args, patchwise,
       original_architecture)
123
           self.features = nn.Sequential(
               # Block 1
124
               nn.Conv2d(in_channels=args.input_size[0], out_channels
125
```

```
=64, kernel_size=3, stride=1, padding=1),
                nn.BatchNorm2d(64),
                nn.ReLU(inplace=True),
127
                nn.Conv2d(in_channels=64, out_channels=64, kernel_size
128
       =3, stride=1, padding=1),
                nn.BatchNorm2d(64),
129
130
                nn.ReLU(inplace=True),
                nn.Conv2d(in_channels=64, out_channels=64, kernel_size
131
       =2, stride=2),
                nn.BatchNorm2d(64),
                nn.ReLU(inplace=True),
133
134
                # Block 2
135
136
                nn.Conv2d(in_channels=64, out_channels=128, kernel_size
       =3, stride=1, padding=1),
                nn.BatchNorm2d(128),
137
138
                nn.ReLU(inplace=True),
                nn.Conv2d(in_channels=128, out_channels=128,
139
       kernel_size=3, stride=1, padding=1),
                nn.BatchNorm2d(128),
140
141
                nn.ReLU(inplace=True)
                nn.Conv2d(in_channels=128, out_channels=128,
142
       kernel_size=2, stride=2),
143
                nn.BatchNorm2d(128),
                nn.ReLU(inplace=True),
144
145
                nn.Conv2d(in_channels=128, out_channels=1, kernel_size
146
       =1, stride=1),
147
148
149
            self.classifier = nn.Sequential(
                nn.Linear(1 * 16 * 16, 128),
150
                nn.ReLU(inplace=True),
151
                nn.Dropout(0.5),
153
154
                nn.Linear (128, 128),
                nn.ReLU(inplace=True),
155
156
                nn.Dropout(0.5),
157
158
                nn.Linear(128, 64),
                nn.ReLU(inplace=True),
159
                nn.Dropout(0.5),
160
161
                nn.Linear(64, args.classes),
162
163
           # This will send net to device, so only call here
           self.init_device()
166
167
       def forward(self, x):
168
           x = self.features(x)
169
           x = x.view(x.size(0), -1)
171
           x = self.classifier(x)
           x = F.\log_softmax(x, dim=1)
173
           return x
174
175
       def initialize_weights(self):
```

```
""" As in https://arxiv.org/abs/1803.04054 """
176
177
           for m in self.modules():
                if isinstance(m, nn.Conv2d):
178
                    nn.init.kaiming_normal_(m.weight, nonlinearity='
179
       relu')
                    if m.bias is not None:
180
181
                        m.bias.data.zero_()
182
                elif isinstance(m, nn.BatchNorm2d):
183
                    m.weight.data.fill_(1)
184
                    m.bias.data.zero_()
185
186
                elif isinstance(m, nn.Linear):
187
                    m.weight.data.normal_(0, 0.01)
188
                    m.bias.data.zero_()
189
190
   class DynamicCapsules(ImageWiseModels):
191
       A Capsule Network adapted from https://github.com/XifengGuo/
193
       CapsNet-Pytorch
       def __init__(self, args, patchwise=None, original_architecture=
195
       False):
           super(DynamicCapsules, self).__init__(args, patchwise,
196
       original_architecture)
           self.output_size = args.output_size
197
           self.classes = args.classes
198
           self.routings = args.routings
199
           self.lam_recon = args.lam_recon
200
           self.device = torch.device("cuda:0" if torch.cuda.
201
       is_available() else "cpu")
202
           # Layer 1: Just a conventional Conv2D layer
203
           self.conv1 = nn.Conv2d(args.output_size[0], 64, kernel_size
204
       =9, stride=1, padding=0)
205
           # Layer 2: Conv2D layer with 'squash' activation, then
206
       reshape to [None, num_caps, dim_caps]
           self.primarycaps = PrimaryCapsule(64, 64, 8, kernel_size=9,
207
        stride=2, padding=0)
208
           # Layer 3: Capsule layer. Routing algorithm works here.
209
210
           self.digitcaps = DenseCapsule(in_num_caps=4608, in_dim_caps
       =8,
                                           out_num_caps=args.classes,
211
       out_dim_caps=16, routings=self.routings, device=self.device)
212
213
           # Decoder network.
           self.decoder = nn.Sequential(
214
                nn.Linear(16*args.classes, 512),
215
               nn.ReLU(inplace=True),
               nn.Linear(512, 1024),
217
218
                nn.ReLU(inplace=True),
               nn.Linear(1024, args.output_size[0] * args.output_size
219
       [1] * args.output_size[2]),
               nn.Sigmoid()
221
```

```
222
            self.relu = nn.ReLU()
224
           # This will send net to device, so only call here
225
           self.init_device()
226
227
228
       def forward(self, x, y=None):
           x = self.relu(self.conv1(x))
229
           x = self.primarycaps(x)
230
231
           x = self.digitcaps(x)
232
           length = x.norm(dim=-1)
           if y is None: # during testing, no label given. create one
       -hot coding using 'length'
               index = length.max(dim=1)[1]
234
               y = Variable(torch.zeros(length.size()).scatter_(1,
       index.view(-1, 1).cpu().data, 1.).to(self.device))
236
           reconstruction = self.decoder((x * y[:, :, None]).view(x.
       size(0), -1))
           return length, reconstruction.view(-1, *self.output_size)
237
238
       def propagate(self, inputs, labels, criterion=None):
239
           labels = torch.zeros(labels.size(0), self.classes).to(self.
240
       device).scatter_(1, labels.view(-1, 1), 1.) # change to one-
       hot coding
           inputs = self.patch_wise_model.features(inputs)
241
            if criterion:
242
               y_pred, x_recon = self(inputs, labels)
243
               loss = caps_loss(labels, y_pred, inputs, x_recon, self.
244
       lam_recon) # compute loss
245
                y_pred, x_recon = self(inputs) # No y in testing
246
                loss = 0
247
           return loss, y_pred
248
249
   class VariationalCapsules(ImageWiseModels):
250
251
       Capsule Routing via Variational Bayes based on https://github.
252
       com/fabio-deep/Variational-Capsule-Routing
253
       def __init__(self, args, patchwise=None, original_architecture=
254
       False):
           super(VariationalCapsules, self).__init__(args, patchwise,
255
       original_architecture)
256
            self.output_size = args.output_size
257
           self.n_classes = args.classes
258
           self.routings = args.routings
259
260
           self.P = args.pose_dim
261
           self.PP = int(np.max([2, self.P*self.P]))
262
           self.A, self.B, self.C, self.D = args.arch
263
264
265
           # Layer 1: Just a conventional Conv2D layer
           self.Conv_1 = nn.Conv2d(self.output_size[0], self.A,
266
       kernel_size=5, stride=2, bias=False)
           nn.init.kaiming_uniform_(self.Conv_1.weight)
267
268
```

```
self.BN_1 = nn.BatchNorm2d(self.A)
269
           self.PrimaryCaps = layers.PrimaryCapsules2d(in_channels=
       self.A, out_caps=self.B,
               kernel_size=1, stride=1, pose_dim=self.P)
           self.ConvCaps_1 = layers.ConvCapsules2d(in_caps=self.B,
273
       out_caps=self.C,
               kernel_size=3, stride=2, pose_dim=self.P)
274
275
           self.ConvRouting_1 = vb_routing.VariationalBayesRouting2d(
276
       in_caps=self.B, out_caps=self.C,
               kernel_size=3, stride=2, pose_dim=self.P,
               cov='diag', iter=args.routings,
278
               alpha0=1., m0=torch.zeros(self.PP), kappa0=1.,
279
               Psi0=torch.eye(self.PP), nu0=self.PP+1)
280
281
282
           self.ConvCaps_2 = layers.ConvCapsules2d(in_caps=self.C,
       out_caps=self.D,
               kernel_size=3, stride=1, pose_dim=self.P)
283
284
           self.ConvRouting_2 = vb_routing.VariationalBayesRouting2d(
       in_caps=self.C, out_caps=self.D,
               kernel_size=3, stride=1, pose_dim=self.P,
286
287
               cov='diag', iter=args.routings,
               alpha0=1., m0=torch.zeros(self.PP), kappa0=1.,
288
               Psi0=torch.eye(self.PP), nu0=self.PP+1)
289
290
291
           self.ClassCaps = layers.ConvCapsules2d(in_caps=self.D,
       out_caps=self.n_classes,
               kernel_size=1, stride=1, pose_dim=self.P, share_W_ij=
292
       True, coor_add=True)
293
           self.ClassRouting = vb_routing.VariationalBayesRouting2d(
294
       in_caps=self.D, out_caps=self.n_classes,
               kernel_size=12, stride=1, pose_dim=self.P, # adjust
295
       final kernel_size K depending on input H/W, for H=W=32, K=4.
               cov='diag', iter=args.routings,
296
297
               alpha0=1., m0=torch.zeros(self.PP), kappa0=1.,
               Psi0=torch.eye(self.PP), nu0=self.PP+1, class_caps=True
298
299
           # This will send net to device, so only call here
300
           self.init_device()
301
302
       def forward(self, x):
303
                   [?, A, F, F]
304
           # Out
           x = F.relu(self.BN_1(self.Conv_1(x)))
305
           # Out
                    a [?, B, F, F], v [?, B, P, P, F, F]
306
           a,v = self.PrimaryCaps(x)
307
                     a [?, B, 1, 1, 1, F, F, K, K], v [?, B, C, P*P,
           # Out
       1, F, F, K, K]
           a,v = self.ConvCaps_1(a, v, self.device)
309
                    a [?, C, F, F], v [?, C, P, P, F, F]
310
           # Out
          311
       1, F, F, K, K]
          a,v = self.ConvCaps_2(a, v, self.device)
313
```

```
# Out a [?, D, F, F], v [?, D, P, F, F]
314
315
           a,v = self.ConvRouting_2(a, v, self.device)
                     a [?, D, 1, 1, 1, F, F, K, K], v [?, D, n_classes
           # Out
316
       , P*P, 1, F, F, K, K]
           a,v = self.ClassCaps(a, v, self.device)
317
           # Out
                    yhat [?, n_classes], v [?, n_classes, P, P]
318
319
           yhat, v = self.ClassRouting(a, v, self.device)
           return yhat
321
322
   class SRCapsules(ImageWiseModels):
323
       Self Routing Capsules based on https://github.com/coder3000/SR-
       CapsNet
       def __init__(self, args, patchwise=None, original_architecture=
326
           super(SRCapsules, self).__init__(args, patchwise,
       original_architecture)
328
           planes = 16
329
           last_size = 14
330
           self.num\_caps = 16
331
332
333
           self.conv1 = nn.Conv2d(args.input_size[0], 256, kernel_size
       =7, stride=2, padding=1, bias=False)
           self.bn1 = nn.BatchNorm2d(256)
           self.conv_a = nn.Conv2d(256, self.num_caps, kernel_size=5,
       stride=1, padding=1, bias=False)
           self.conv_pose = nn.Conv2d(256, self.num_caps*planes,
336
       kernel_size=5, stride=1, padding=1, bias=False)
           self.bn_a = nn.BatchNorm2d(self.num_caps)
           self.bn_pose = nn.BatchNorm2d(self.num_caps*planes)
338
339
           self.conv_caps = SelfRouting2d(self.num_caps, self.num_caps
340
       , planes, planes, kernel_size=3, stride=2, padding=1, pose_out=
       True)
           self.bn_pose_conv_caps = nn.BatchNorm2d(self.num_caps*
341
       planes)
342
           self.fc_caps = SelfRouting2d(self.num_caps, args.classes,
343
       planes, 1, kernel_size=last_size, padding=0, pose_out=False)
344
345
           # This will send net to device, so only call here
           self.init_device()
346
347
           self.loss = nn.NLLLoss()
348
           self.loss.to(self.device)
349
350
       def forward(self, x):
351
           out = F.relu(self.bn1(self.conv1(x)))
           a, pose = self.conv_a(out), self.conv_pose(out)
353
           a, pose = torch.sigmoid(self.bn_a(a)), self.bn_pose(pose)
354
355
           a, pose = self.conv_caps(a, pose)
357
           pose = self.bn_pose_conv_caps(pose)
358
           a, _ = self.fc_caps(a, pose)
359
```

```
360
361
            out = a.view(a.size(0), -1)
           out = out.log()
362
           return out
363
364
       def propagate(self, inputs, labels, criterion=None):
365
366
            inputs = self.patch_wise_model.features(inputs)
           y_pred = self(inputs)
367
            if criterion:
369
                loss = self.loss(y_pred, labels)
370
            else:
                loss = 0
371
            return loss, y_pred
372
```

Listing 5: src/imagewisemodels.py

```
# Base model
2 from .model import Model
4 # Variational Capsules
5 from .VarCaps import layers
6 from .VarCaps import vb_routing
8 # EfficientNet
9 from efficientnet_pytorch import EfficientNet
10
11 # Training
12 import torch.nn.functional as F
13 import torch.nn as nn
14 import numpy as np
15 import torch
16 import time
17
# For testing we want to get a whole image in patches
19 BATCH_SIZE = 12
20
21 class VariationalMixedCapsules(Model):
22
23
      Capsule Routing via Variational Bayes based on https://github.
      com/fabio-deep/Variational-Capsule-Routing
24
25
      def __init__(self, args):
26
           super(VariationalMixedCapsules, self).__init__(args)
27
           self.output_size = args.output_size
28
           self.n_classes = args.classes
29
          self.routings = args.routings
30
31
32
          self.P = args.pose_dim
          self.PP = int(np.max([2, self.P*self.P]))
33
34
          self.A, self.B, self.C, self.D = args.arch
35
          K = 12
36
37
           self.features = nn.Sequential(
               # Block 1
38
               nn.Conv2d(in_channels=args.input_size[0], out_channels
      =16, kernel_size=3, stride=1, padding=1),
               nn.BatchNorm2d(16),
```

```
nn.ReLU(inplace=True),
41
               nn.Conv2d(in_channels=16, out_channels=16, kernel_size
      =3, stride=1, padding=1),
               nn.BatchNorm2d(16),
43
               nn.ReLU(inplace=True),
44
               nn.Conv2d(in_channels=16, out_channels=16, kernel_size
45
      =2, stride=2),
               nn.BatchNorm2d(16),
46
               nn.ReLU(inplace=True),
47
48
49
               nn.Conv2d(in_channels=16, out_channels=32, kernel_size
      =3, stride=1, padding=1),
51
               nn.BatchNorm2d(32),
               nn.ReLU(inplace=True),
               nn.Conv2d(in_channels=32, out_channels=32, kernel_size
53
      =3, stride=1, padding=1),
               nn.BatchNorm2d(32),
54
55
               nn.ReLU(inplace=True),
               nn.Conv2d(in_channels=32, out_channels=32, kernel_size
56
      =2, stride=2),
               nn.BatchNorm2d(32),
               nn.ReLU(inplace=True),
58
59
               # Block 3
60
               nn.Conv2d(in_channels=32, out_channels=64, kernel_size
61
      =3, stride=1, padding=1),
               nn.BatchNorm2d(64),
62
               nn.ReLU(inplace=True),
63
               nn.Conv2d(in_channels=64, out_channels=64, kernel_size
64
      =3, stride=1, padding=1),
               nn.BatchNorm2d(64).
65
               nn.ReLU(inplace=True),
66
               nn.Conv2d(in_channels=64, out_channels=64, kernel_size
67
      =2, stride=2),
               nn.BatchNorm2d(64),
68
               nn.ReLU(inplace=True),
69
70
               nn.Conv2d(in_channels=64, out_channels=args.output_size
71
       [0], kernel_size=1, stride=1),
72
73
74
           # Layer 1: Just a conventional Conv2D layer
           self.Conv_1 = nn.Conv2d(args.input_size[0], self.A,
75
      kernel_size=5, stride=2, bias=False)
76
          nn.init.kaiming_uniform_(self.Conv_1.weight)
77
           self.Conv_2 = nn.Conv2d(self.A, self.A, kernel_size=5,
78
      stride=2, bias=False)
           nn.init.kaiming_uniform_(self.Conv_2.weight)
80
           self.Conv_3 = nn.Conv2d(self.A, self.A, kernel_size=3,
81
      stride=2, bias=False)
          nn.init.kaiming_uniform_(self.Conv_3.weight)
82
83
           self.BN_1 = nn.BatchNorm2d(self.A)
84
           self.PrimaryCaps = layers.PrimaryCapsules2d(in_channels=
```

```
self.A, out_caps=self.B,
               kernel_size=1, stride=1, pose_dim=self.P)
87
           self.ConvCaps_1 = layers.ConvCapsules2d(in_caps=self.B,
88
       out_caps=self.C,
               kernel_size=3, stride=2, pose_dim=self.P)
89
90
           self.ConvRouting_1 = vb_routing.VariationalBayesRouting2d(
91
       in_caps=self.B, out_caps=self.C,
92
               kernel_size=3, stride=2, pose_dim=self.P,
               cov='diag', iter=args.routings,
93
               alpha0=1., m0=torch.zeros(self.PP), kappa0=1.,
94
               Psi0=torch.eye(self.PP), nu0=self.PP+1)
95
96
           self.ConvCaps_2 = layers.ConvCapsules2d(in_caps=self.C,
97
       out_caps=self.D,
98
               kernel_size=3, stride=1, pose_dim=self.P)
99
           self.ConvRouting_2 = vb_routing.VariationalBayesRouting2d(
100
       in_caps=self.C, out_caps=self.D,
               kernel_size=3, stride=1, pose_dim=self.P,
               cov='diag', iter=args.routings,
               alpha0=1., m0=torch.zeros(self.PP), kappa0=1.,
               Psi0=torch.eye(self.PP), nu0=self.PP+1)
104
           self.ClassCaps = layers.ConvCapsules2d(in_caps=self.D,
106
       out_caps=self.n_classes,
               kernel_size=1, stride=1, pose_dim=self.P, share_W_ij=
       True, coor_add=True)
108
           self.ClassRouting = vb_routing.VariationalBayesRouting2d(
       in_caps=self.D, out_caps=self.n_classes,
               kernel_size=K, stride=1, pose_dim=self.P, # adjust
       final kernel_size K depending on input H/W, for H=W=32, K=4.
               cov='diag', iter=args.routings,
               alpha0=1., m0=torch.zeros(self.PP), kappa0=1.,
112
               Psi0=torch.eye(self.PP), nu0=self.PP+1, class_caps=True
       )
114
           # This will send net to device, so only call here
           self.init_device()
116
117
       def forward(self, x):
118
           x = self.features(x)
119
           # Out
                     [?, A, F, F]
120
121
           x = F.relu(self.BN_1(self.Conv_1(x)))
           # Out
                    a [?, B, F, F], v [?, B, P, P, F, F]
           a,v = self.PrimaryCaps(x)
123
           # Out
                    a [?, B, 1, 1, 1, F, F, K, K], v [?, B, C, P*P,
124
       1, F, F, K, K]
           a,v = self.ConvCaps_1(a, v, self.device)
                    a [?, C, F, F], v [?, C, P, P, F, F]
           a,v = self.ConvRouting_1(a, v, self.device)
127
           # Out
                     a [?, C, 1, 1, 1, F, F, K, K], v [?, C, D, P*P,
       1, F, F, K, K]
           a,v = self.ConvCaps_2(a, v, self.device)
129
           # Out a [?, D, F, F], v [?, D, P, P, F, F]
130
```

```
a,v = self.ConvRouting_2(a, v, self.device)
                     a [?, D, 1, 1, 1, F, F, K, K], v [?, D, n_classes
       , P*P, 1, F, F, K, K]
           a,v = self.ClassCaps(a, v, self.device)
133
                    yhat [?, n_classes], v [?, n_classes, P, P]
           # Out
134
           yhat, v = self.ClassRouting(a, v, self.device)
135
136
           return yhat
137
   class EffNet(Model):
138
139
       EfficientNet based on the implementation https://github.com/
140
       lukemelas/EfficientNet-PyTorch
141
142
       def __init__(self, args):
143
           super(EffNet, self).__init__(args)
144
145
           self.time = str(time.strftime('%Y-%m-%d_%H-%M'))
146
147
           self.device = torch.device("cuda:0" if torch.cuda.
       is_available() else "cpu")
           self.output_size = args.output_size
           self.n_classes = args.classes
149
151
           self.model = EfficientNet.from_pretrained('efficientnet-b0')
           num_ftrs = self.model._fc.in_features
           self.model._fc = nn.Sequential(
               nn.Linear(num_ftrs, 128),
154
               nn.ReLU(),
155
               nn.Linear(128, self.n_classes)
157
158
           for param in self.model.parameters():
159
160
                param.requires_grad = False
161
162
           for param in self.model._fc.parameters():
               param.requires_grad = True
           # This will send net to device, so only call here
165
           self.init_device()
166
167
       def propagate(self, inputs, labels, criterion=None):
168
169
           outputs = self.model(inputs)
           if criterion:
                loss = criterion(outputs, labels)
171
           else:
               loss = 0
173
           return loss, outputs
```

Listing 6: src/mixedmodels.py

```
7 import torch.nn.functional as F
8 from torch.autograd import Variable
10
def squash(inputs, axis=-1):
12
13
       The non-linear activation used in Capsule. It drives the length
       of a large vector to near 1 and small vector to 0
       :param inputs: vectors to be squashed
14
       :param axis: the axis to squash
15
       :return: a Tensor with same size as inputs
16
17
      norm = torch.norm(inputs, p=2, dim=axis, keepdim=True)
18
       scale = norm**2 / (1 + norm**2) / (norm + 1e-8)
19
       return scale * inputs
20
21
22
class DenseCapsule(nn.Module):
24
      The dense capsule layer. It is similar to Dense (FC) layer. Dense layer has 'in_num' inputs, each is a scalar, the
25
       output of the neuron from the former layer, and it has 'out_num
26
       ' output neurons. DenseCapsule just expands the
       output of the neuron from scalar to vector. So its input size =
27
        [None, in_num_caps, in_dim_caps] and output size = \
       [None, out_num_caps, out_dim_caps]. For Dense Layer,
       in_dim_caps = out_dim_caps = 1.
29
       :param in_num_caps: number of cpasules inputted to this layer
30
       :param in_dim_caps: dimension of input capsules
31
       :param out_num_caps: number of capsules outputted from this
       laver
       :param out_dim_caps: dimension of output capsules
33
       : \verb"param" routings: number of iterations for the routing algorithm"
34
35
           __init__(self, in_num_caps, in_dim_caps, out_num_caps,
36
      out_dim_caps, device, routings=3):
37
           super(DenseCapsule, self).__init__()
           self.in_num_caps = in_num_caps
38
           self.in_dim_caps = in_dim_caps
39
40
           self.out_num_caps = out_num_caps
           self.out_dim_caps = out_dim_caps
41
           self.routings = routings
42
           self.device = device
43
           self.weight = nn.Parameter(0.01 * torch.randn(out_num_caps,
44
        in_num_caps, out_dim_caps, in_dim_caps))
45
      def forward(self, x):
46
           # x.size=[batch, in_num_caps, in_dim_caps]
47
           # expanded to
                             [batch, 1,
                                                     in_num_caps,
       in_dim_caps, 1]
           # weight.size
                                     out_num_caps, in_num_caps,
49
       out_dim_caps, in_dim_caps]
           # torch.matmul: [out_dim_caps, in_dim_caps] x [in_dim_caps,
        1] -> [out_dim_caps, 1]
           # => x_hat.size =[batch, out_num_caps, in_num_caps,
51
      out_dim_caps]
```

```
x_hat = torch.squeeze(torch.matmul(self.weight, x[:, None,
52
      :, :, None]), dim=-1)
53
           # In forward pass, 'x_hat_detached' = 'x_hat';
54
          # In backward, no gradient can flow from 'x_hat_detached'
      back to 'x_hat'.
56
          x_hat_detached = x_hat.detach()
57
           # The prior for coupling coefficient, initialized as zeros.
59
           # b.size = [batch, out_num_caps, in_num_caps]
           b = Variable(torch.zeros(x.size(0), self.out_num_caps, self
60
       .in_num_caps)).to(self.device)
61
           assert self.routings > 0, 'The \'routings\' should be > 0.'
62
           for i in range(self.routings):
63
               # c.size = [batch, out_num_caps, in_num_caps]
64
65
               c = F.softmax(b, dim=1)
66
               \mbox{\tt\#} At last iteration, use 'x_hat' to compute 'outputs'
67
      in order to backpropagate gradient
               if i == self.routings - 1:
                   # c.size expanded to [batch, out_num_caps,
69
      in_num_caps, 1
70
                   # x_hat.size
                                         [batch, out_num_caps,
      in_num_caps, out_dim_caps]
                   # => outputs.size=
                                         [batch, out_num_caps, 1,
71
            out_dim_caps]
                   outputs = squash(torch.sum(c[:, :, :, None] * x_hat
       , dim=-2, keepdim=True))
                   # outputs = squash(torch.matmul(c[:, :, None, :],
73
      x_hat)) # alternative way
               else: # Otherwise, use 'x_hat_detached' to update 'b'.
       No gradients flow on this path.
                   outputs = squash(torch.sum(c[:, :, :, None] *
      x_hat_detached, dim=-2, keepdim=True))
                   # outputs = squash(torch.matmul(c[:, :, None, :],
76
      x_hat_detached)) # alternative way
77
                                         =[batch, out_num_caps, 1,
                   # outputs.size
78
             out_dim_caps]
                   # x_hat_detached.size=[batch, out_num_caps,
      in_num_caps, out_dim_caps]
                   # => b.size
                                         =[batch, out_num_caps,
      in_num_caps]
                   b = b + torch.sum(outputs * x_hat_detached, dim=-1)
81
82
           return torch.squeeze(outputs, dim=-2)
83
84
85
  class PrimaryCapsule(nn.Module):
87
      Apply Conv2D with 'out_channels' and then reshape to get
88
      capsules
       :param in_channels: input channels
89
90
       :param out_channels: output channels
       :param dim_caps: dimension of capsule
91
      :param kernel_size: kernel size
```

```
:return: output tensor, size=[batch, num_caps, dim_caps]
93
94
       def __init__(self, in_channels, out_channels, dim_caps,
95
       kernel_size, stride=1, padding=0):
           super(PrimaryCapsule, self).__init__()
96
           self.dim_caps = dim_caps
97
98
           self.conv2d = nn.Conv2d(in_channels, out_channels,
       kernel_size=kernel_size, stride=stride, padding=padding)
       def forward(self, x):
100
           outputs = self.conv2d(x)
           outputs = outputs.view(x.size(0), -1, self.dim_caps)
102
           return squash(outputs)
```

Listing 7: src/DynamicCaps/capsulelayers.py

```
2 Author: Xifeng Guo, E-mail: 'guoxifeng1990@163.com', Github: 'https
     ://github.com/XifengGuo/CapsNet-Pytorch'
5 import torch
6 from torch import nn
8 def caps_loss(y_true, y_pred, x, x_recon, lam_recon):
      Capsule loss = Margin loss + lam_recon * reconstruction loss.
10
      :param y_true: true labels, one-hot coding, size=[batch,
      classes
      :param y_pred: predicted labels by CapsNet, size=[batch,
      classesl
      :param x: input data, size=[batch, channels, width, height]
14
      :param x_recon: reconstructed data, size is same as 'x'
      :param lam_recon: coefficient for reconstruction loss
15
      :return: Variable contains a scalar loss value.
16
17
      L = y_{true} * torch.clamp(0.9 - y_{pred}, min=0.) ** 2 + 
18
19
          0.5 * (1 - y_{true}) * torch.clamp(y_pred - 0.1, min=0.) ** 2
      L_margin = L.sum(dim=1).mean()
20
21
      L_recon = nn.MSELoss()(x_recon, x)
22
      return L_margin + lam_recon * L_recon
24
```

Listing 8: src/DynamicCaps/capsulenet.py

```
import torch
import torch.nn as nn
import torch.nn.functional as F

import math

eps = 1e-12

class SelfRouting2d(nn.Module):
    def __init__(self, A, B, C, D, kernel_size=3, stride=1, padding =1, pose_out=False):
    super(SelfRouting2d, self).__init__()
```

```
self.A = A
12
           self.B = B
13
           self.C = C
14
           self.D = D
15
16
           self.k = kernel_size
17
           self.kk = kernel_size ** 2
           self.kkA = self.kk * A
19
20
21
           self.stride = stride
           self.pad = padding
22
23
           self.pose_out = pose_out
24
25
           if pose_out:
26
               self.W1 = nn.Parameter(torch.FloatTensor(self.kkA, B*D,
27
       C))
               nn.init.kaiming_uniform_(self.W1.data)
28
29
           self.W2 = nn.Parameter(torch.FloatTensor(self.kkA, B, C))
30
           self.b2 = nn.Parameter(torch.FloatTensor(1, 1, self.kkA, B)
31
32
           nn.init.constant_(self.W2.data, 0)
33
           nn.init.constant_(self.b2.data, 0)
34
35
       def forward(self, a, pose):
36
           # a: [b, A, h, w]
37
           # pose: [b, AC, h, w]
38
           b, _{-}, h, w = a.shape
39
40
41
           # [b, ACkk, 1]
           pose = F.unfold(pose, self.k, stride=self.stride, padding=
42
       self.pad)
43
          l = pose.shape[-1]
44
           # [b, A, C, kk, 1]
           pose = pose.view(b, self.A, self.C, self.kk, 1)
45
           # [b, 1, kk, A, C]
46
           pose = pose.permute(0, 4, 3, 1, 2).contiguous()
# [b, 1, kkA, C, 1]
47
48
           pose = pose.view(b, 1, self.kkA, self.C, 1)
49
50
51
           if hasattr(self, 'W1'):
               # [b, 1, kkA, BD]
52
               pose_out = torch.matmul(self.W1, pose).squeeze(-1)
53
               # [b, 1, kkA, B, D]
54
               pose_out = pose_out.view(b, 1, self.kkA, self.B, self.D
55
      )
56
           # [b, 1, kkA, B]
57
           logit = torch.matmul(self.W2, pose).squeeze(-1) + self.b2
58
59
60
           # [b, 1, kkA, B]
           r = torch.softmax(logit, dim=3)
61
62
           # [b, kkA, 1]
63
64
           a = F.unfold(a, self.k, stride=self.stride, padding=self.
```

```
pad)
           # [b, A, kk, 1]
           a = a.view(b, self.A, self.kk, 1)
66
           # [b, 1, kk, A]
67
           a = a.permute(0, 3, 2, 1).contiguous()
68
           # [b, 1, kkA, 1]
69
           a = a.view(b, 1, self.kkA, 1)
70
71
           # [b, 1, kkA, B]
72
73
           ar = a * r
           # [b, 1, 1, B]
74
           ar_sum = ar.sum(dim=2, keepdim=True)
75
           # [b, 1, kkA, B, 1]
76
77
           coeff = (ar / (ar_sum)).unsqueeze(-1)
78
           # [b, 1, B]
79
           # a_out = ar_sum.squeeze(2)
80
           a_out = ar_sum / a.sum(dim=2, keepdim=True)
81
82
           a_out = a_out.squeeze(2)
83
           # [b, B, 1]
84
           a_out = a_out.transpose(1,2)
85
86
87
           if hasattr(self, 'W1'):
               # [b, 1, B, D]
88
                pose_out = (coeff * pose_out).sum(dim=2)
89
                # [b, 1, BD]
90
                pose_out = pose_out.view(b, 1, -1)
91
                # [b, BD, 1]
92
                pose_out = pose_out.transpose(1,2)
93
94
           oh = ow = math.floor(1**(1/2))
95
96
           a_{out} = a_{out.view}(b, -1, oh, ow)
97
           if hasattr(self, 'W1'):
98
99
                pose_out = pose_out.view(b, -1, oh, ow)
100
                pose_out = None
102
           return a_out, pose_out
103
```

Listing 9: src/SRCaps/modules.py

```
1 import torch
2 import numpy as np
3 import torch.nn as nn
4 import torch.nn.functional as F
6
  class PrimaryCapsules2d(nn.Module):
      ''', Primary Capsule Layer''
      def __init__(self, in_channels, out_caps, kernel_size, stride,
           padding=0, pose_dim=4, weight_init='xavier_uniform'):
9
           super().__init__()
10
11
           self.A = in_channels
12
           self.B = out_caps
13
          self.P = pose_dim
self.K = kernel_size
14
```

```
self.S = stride
16
           self.padding = padding
17
18
           w_kernel = torch.empty(self.B*self.P*self.P, self.A, self.K
19
       . self.K)
          a_kernel = torch.empty(self.B, self.A, self.K, self.K)
20
21
           if weight_init == 'kaiming_normal':
22
               nn.init.kaiming_normal_(w_kernel)
23
24
               nn.init.kaiming_normal_(a_kernel)
           elif weight_init == 'kaiming_uniform':
25
26
               nn.init.kaiming_uniform_(w_kernel)
               nn.init.kaiming_uniform_(a_kernel)
27
           elif weight_init == 'xavier_normal':
28
               nn.init.xavier_normal_(w_kernel)
29
               nn.init.xavier_normal_(a_kernel)
30
           elif weight_init == 'xavier_uniform':
31
               nn.init.xavier_uniform_(w_kernel)
32
33
               nn.init.xavier_uniform_(a_kernel)
34
           else:
               NotImplementedError('{} not implemented.'.format(
      weight_init))
36
                   [B*(P*P+1), A, K, K]
37
           # Out
           self.weight = nn.Parameter(torch.cat([w_kernel, a_kernel],
38
      dim=0))
39
           self.BN_a = nn.BatchNorm2d(self.B, affine=True)
40
           self.BN_p = nn.BatchNorm3d(self.B, affine=True)
41
42
      def forward(self, x): # [?, A, F, F]
43
44
           # Out
                     [?, B*(P*P+1), F, F]
45
           x = F.conv2d(x, weight=self.weight, stride=self.S, padding=
46
      self.padding)
47
                     ([?, B*P*P, F, F], [?, B, F, F])
          # Out
48
      +1), F, F]
           poses, activations = torch.split(x, [self.B*self.P*self.P,
49
      self.B], dim=1)
50
                    [?, B, P*P, F, F]
51
           poses = self.BN_p(poses.reshape(-1, self.B, self.P*self.P,
52
      *x.shape[2:]))
53
                     [?, B, P, P, F, F]
                                            [?, B, P*P, F, F]
54
           # Out
           poses = poses.reshape(-1, self.B, self.P, self.P, *x.shape
55
       [2:])
56
           # Out
                   [?, B, F, F])
57
           activations = torch.sigmoid(self.BN_a(activations))
58
59
60
          return (activations, poses)
61
62 class ConvCapsules2d(nn.Module):
      '''Convolutional Capsule Layer'''
63
     def __init__(self, in_caps, out_caps, pose_dim, kernel_size,
```

```
stride, padding=0,
           weight_init='xavier_uniform', share_W_ij=False, coor_add=
       False):
           super().__init__()
67
           self.B = in_caps
68
           self.C = out_caps
69
           self.P = pose_dim
           self.PP = np.max([2, self.P*self.P])
71
72
           self.K = kernel_size
           self.S = stride
73
74
           self.padding = padding
75
           self.share_W_ij = share_W_ij # share the transformation
76
       matrices across (F*F)
           self.coor_add = coor_add # embed coordinates
77
78
                     [1, B, C, 1, P, P, 1, 1, K, K]
79
           self.W_ij = torch.empty(1, self.B, self.C, 1, self.P, self.
80
       P, 1, 1, self.K, self.K)
           if weight_init.split('_')[0] == 'xavier':
82
               fan_in = self.B * self.K*self.K * self.PP # in_caps
83
       types * receptive field size
               fan_out = self.C * self.K*self.K * self.PP # out_caps
84
       types * receptive field size
               std = np.sqrt(2. / (fan_in + fan_out))
85
               bound = np.sqrt(3.) * std
86
87
               if weight_init.split('_')[1] == 'normal':
88
                   self.W_ij = nn.Parameter(self.W_ij.normal_(0, std))
               elif weight_init.split('_')[1] == 'uniform':
90
                   self.W_ij = nn.Parameter(self.W_ij.uniform_(-bound,
91
        bound))
92
                   raise NotImplementedError('{} not implemented.'.
93
       format(weight_init))
           elif weight_init.split('_')[0] == 'kaiming':
95
               # fan_in preserves magnitude of the variance of the
96
       weights in the forward pass.
               fan_in = self.B * self.K*self.K * self.PP # in_caps
97
       types * receptive field size
               # fan_out has same affect as fan_in for backward pass.
98
               # fan_out = self.C * self.K*self.K * self.PP # out_caps
99
        types * receptive field size
               std = np.sqrt(2.) / np.sqrt(fan_in)
               bound = np.sqrt(3.) * std
101
               if weight_init.split('_')[1] == 'normal':
103
                   self.W_ij = nn.Parameter(self.W_ij.normal_(0, std))
               elif weight_init.split('_')[1] == 'uniform':
106
                   self.W_ij = nn.Parameter(self.W_ij.uniform_(-bound,
        bound))
107
               else:
                   raise NotImplementedError('{} not implemented.'.
108
       format(weight_init))
```

```
109
            elif weight_init == 'noisy_identity' and self.PP > 2:
                b = 0.01 \# U(0,b)
111
                # Out
                          [1, B, C, 1, P, P, 1, 1, K, K]
112
                self.W_ij = nn.Parameter(torch.clamp(.1*torch.eye(self.
113
       P,self.P).repeat( \
                    1, self.B, self.C, 1, 1, 1, self.K, self.K, 1, 1) +
114
                    torch.empty(1, self.B, self.C, 1, 1, 1, self.K,
       self.K, self.P, self.P).uniform_(0,b), \
                    \max=1).permute(0, 1, 2, 3, -2, -1, 4, 5, 6, 7))
117
               raise NotImplementedError('{} not implemented.'.format(
118
       weight_init))
119
            if self.padding != 0:
120
                if isinstance(self.padding, int):
                    self.padding = [self.padding]*4
123
       def forward(self, activations, poses, device): # ([?, B, F, F],
        [?, B, P, P, F, F])
                                 Τn
            if self.padding != 0:
                activations = F.pad(activations, self.padding) #
127
       [1,1,1,1]
                poses = F.pad(poses, self.padding + [0]*4) #
128
       [0,0,1,1,1,1]
129
           if self.share_W_ij: # share the matrices over (F*F), if
130
       class caps layer
                self.K = poses.shape[-1] # out_caps (C) feature map
       size
132
           self.F = (poses.shape[-1] - self.K) // self.S + 1 #
133
       featuremap size
134
                      [?, B, P, P, F', F', K, K]
                                                        [?, B, P, P, F, F]
136
           poses = poses.unfold(4, size=self.K, step=self.S).unfold(5,
        size=self.K, step=self.S)
137
           # Out
                      [?, B, 1, P, P, 1, F', F', K, K]
                                                             [?, B, P, P,
138
        F', F', K, K]
           poses = poses.unsqueeze(2).unsqueeze(5)
139
140
                      [?, B, F', F', K, K]
                                                [?, B, F, F]
141
           activations = activations.unfold(2, size=self.K, step=self.
142
       S).unfold(3, size=self.K, step=self.S)
143
           # Out
                      [?, B, 1, 1, 1, F', F', K, K]
                                                         [?, B, F', F',
144
       K, K]
           activations = activations.reshape(-1, self.B, 1, 1, 1, *
145
       activations.shape[2:4], self.K, self.K)
146
       # Out [?, B, C, P, P, F', F', K, K] ([?, 1, F', F', K, K] * [1, B, C, 1, P, P, 1, 1, K, K])
                                                          ([?, B, 1, P, P
147
           V_ji = (poses * self.W_ij).sum(dim=4) # matmul equiv.
148
149
```

```
# Out [?, B, C, P*P, 1, F', F', K, K] [?, B, C, P,
150
       P, F', F', K, K]
           V_ji = V_ji.reshape(-1, self.B, self.C, self.P*self.P, 1, *
       V_{ji.shape[-4:-2]}, self.K, self.K)
           if self.coor_add:
153
               if V_ji.shape[-1] == 1: # if class caps layer (
154
       featuremap size = 1)
                   self.F = self.K # 1->4
156
               # coordinates = torch.arange(self.F, dtype=torch.
       float32) / self.F
               coordinates = torch.arange(self.F, dtype=torch.float32)
158
       .add(1.) / (self.F*10)
               i_vals = torch.zeros(self.P*self.P,self.F,1).to(device)
159
               j_vals = torch.zeros(self.P*self.P,1,self.F).to(device)
160
161
               i_vals[self.P-1,:,0] = coordinates
               j_vals[2*self.P-1,0,:] = coordinates
162
163
               if V_ji.shape[-1] == 1: # if class caps layer
164
                   # Out [?, B, C, P*P, 1, 1, 1, K=F, K=F] (class
165
       caps)
                   V_{ji} = V_{ji} + (i_{vals} + j_{vals}).reshape(1,1,1,self.
       P*self.P,1,1,1,self.F,self.F)
                   return activations, V_ji
167
168
                         [?, B, C, P*P, 1, F, F, K, K]
169
               V_ji = V_ji + (i_vals + j_vals).reshape(1,1,1,self.P*
       self.P,1,self.F,self.F,1,1)
           return activations, V_ji
```

Listing 10: src/VarCaps/layers.py

```
1 import torch
2 import numpy as np
3 import torch.nn as nn
4 import torch.nn.functional as F
  class VariationalBayesRouting2d(nn.Module):
6
       '', Variational Bayes Capsule Routing Layer'',
      def __init__(self, in_caps, out_caps, pose_dim,
8
               kernel_size, stride,
9
               alpha0, # Dirichlet
10
               m0, kappa0, # Gaussian
11
               Psi0, nu0, # Wishart
12
               cov='diag', iter=3, class_caps=False):
13
           super().__init__()
14
15
           self.B = in_caps
16
           self.C = out_caps
17
18
           self.P = pose_dim
           self.D = np.max([2, self.P*self.P])
19
           self.K = kernel_size
20
           self.S = stride
21
22
           self.cov = cov # diag/full
23
           self.iter = iter # routing iters
```

```
self.class_caps = class_caps
25
           self.n_classes = out_caps if class_caps else None
26
27
           # dirichlet prior parameter
28
           self.alpha0 = torch.tensor(alpha0).type(torch.FloatTensor)
29
           # self.alpha0 = nn.Parameter(torch.zeros(1,1,self.C
30
       ,1,1,1,1,1).fill_(alpha0)) learn it by backprop
31
                     [?, 1, C, P*P, 1, 1, 1, 1, 1]
32
           self.register_buffer('m0', m0.unsqueeze(0).repeat( \
33
               self.C,1).reshape(1,1,self.C,self.D,1,1,1,1,1)) #
34
      gaussian prior mean parameter
35
           # precision scaling parameter of gaussian prior over
36
      capsule component means
           self.kappa0 = kappa0
37
38
           # scale matrix of wishart prior over capsule precisions
39
40
           if self.cov == 'diag':
               # Out
                         [?, 1, C, P*P, 1, 1, 1, 1, 1]
41
               self.register_buffer('Psi0', torch.diag(Psi0).unsqueeze
42
       (0).repeat( \
                   self.C,1).reshape(1,1,self.C,self.D,1,1,1,1,1))
43
44
           elif self.cov == 'full':
45
                         [?, 1, C, P*P, P*P, 1, 1, 1, 1]
               # Out
46
               self.register_buffer('Psi0', Psi0.unsqueeze(0).repeat(
47
                   self.C,1,1).reshape(1,1,self.C,self.D,self.D
48
       ,1,1,1,1))
          # degree of freedom parameter of wishart prior capsule
50
      precisions
          self.nu0 = nu0
51
52
53
           # log determinant = 0, if PsiO is identity
          self.register_buffer('lndet_Psi0', 2*torch.diagonal(torch.
54
      cholesky(
               Psi0)).log().sum())
55
56
           \# pre compute the argument of the digamma function in E[ln]
      lambda_j[]
           self.register_buffer('diga_arg', torch.arange(self.D).
      reshape(
               1,1,1,self.D,1,1,1,1,1).type(torch.FloatTensor))
59
60
           # pre define some constants
61
           self.register_buffer('Dlog2',
62
               self.D*torch.log(torch.tensor(2.)).type(torch.
63
      FloatTensor))
           self.register_buffer('Dlog2pi',
64
               self.D*torch.log(torch.tensor(2.*np.pi)).type(torch.
      FloatTensor))
66
                     [K*K, 1, K, K] vote collecting filter
67
           # Out
           self.register_buffer('filter',
68
              torch.eye(self.K*self.K).reshape(self.K*self.K,1,self.K
69
```

```
,self.K))
                     [1, 1, C, 1, 1, 1, 1, 1] optional params
71
           self.beta_u = nn.Parameter(torch.zeros(1,1,self.C
       ,1,1,1,1,1,1))
           self.beta_a = nn.Parameter(torch.zeros(1,1,self.C
73
       ,1,1,1,1,1,1))
74
           self.BN_v = nn.BatchNorm3d(self.C, affine=False)
75
           self.BN_a = nn.BatchNorm2d(self.C, affine=False)
76
77
       # Out
                 [?, B, 1, 1, 1, F, F, K, K], [?, B, C, P*P, 1, F, F,
78
       K, K]
                 Τn
       def forward(self, a_i, V_ji, device):
79
80
           self.F_i = a_i.shape[-2:] # input capsule (B) votes feature
81
        map size (K)
           self.F_o = a_i.shape[-4:-2] # output capsule (C) feature
82
       map size (F)
           \tt self.N = self.B*self.F\_i[0]*self.F\_i[1] \# total num of
83
       lower level capsules
84
           # Out
                     [1, B, C, 1, 1, 1, 1, 1, 1]
85
86
           R_ij = (1./self.C) * torch.ones(1,self.B,self.C
       ,1,1,1,1,1,1, requires_grad=False).to(device)
           for i in range(self.iter): # routing iters
88
89
               # update capsule parameter distributions
90
               self.update_qparam(a_i, V_ji, R_ij)
91
92
               if i != self.iter-1: # skip last iter
93
                   # update latent variable distributions (child to
94
       parent capsule assignments)
                   R_ij = self.update_qlatent(a_i, V_ji)
95
96
           # Out
                     [?, 1, C, 1, 1, F, F, 1, 1]
97
98
           self.Elnlambda_j = self.reduce_poses(
               torch.digamma(.5*(self.nu_j - self.diga_arg))) \
99
                   + self.Dlog2 + self.lndet_Psi_j
100
                     [?, 1, C, 1, 1, F, F, 1, 1]
103
           self.Elnpi_j = torch.digamma(self.alpha_j) \
               - torch.digamma(self.alpha_j.sum(dim=2, keepdim=True))
           # subtract "- .5*ln|lmbda|" due to precision matrix,
106
       instead of adding "+ .5*ln|sigma|" for covariance matrix
           H_q_j = .5*self.D * torch.log(torch.tensor(2*np.pi*np.e)) -
107
        .5*self.Elnlambda_j # posterior entropy H[q*(mu_j, sigma_j)]
                     [?, 1, C, 1, 1, F, F, 1, 1] weighted negative
109
       entropy with optional beta params and R_j weight
           a_j = self.beta_a - (torch.exp(self.Elnpi_j) * H_q_j + self
       .beta_u) #* self.R_j
           # Out
                     [?, C, F, F]
           a_j = a_j.squeeze()
113
```

```
114
           # Out
                    [?, C, P*P, F, F]
                                            [?, 1, C, P*P, 1, F, F, 1,
       11
           self.m_j = self.m_j.squeeze()
116
117
           # so BN works in the classcaps layer
118
119
           if self.class_caps:
               # Out [?, C, 1, 1]
                                           [?, C]
120
               a_j = a_j[...,None,None]
121
                        [?, C, P*P, 1, 1] [?, C, P*P]
123
124
               self.m_j = self.m_j[..., None, None]
           # else:
                self.m_j = self.BN_v(self.m_j)
           # Out
                     [?, C, P*P, F, F]
128
           self.m_{j} = self.BN_{v}(self.m_{j}) \# use 'else' above to
129
       deactivate BN_v for class_caps
130
                                            [?, C, P*P, F, F]
           # Out
                    [?, C, P, P, F, F]
131
           self.m_j = self.m_j.reshape(-1, self.C, self.P, self.P, *
       self.F_o)
           # Out
134
                   [?, C, F, F]
           a_j = torch.sigmoid(self.BN_a(a_j))
136
           return a_j.squeeze(), self.m_j.squeeze() # propagate
       posterior means to next layer
138
       def update_qparam(self, a_i, V_ji, R_ij):
139
140
                    [?, B, C, 1, 1, F, F, K, K]
141
           R_{ij} = R_{ij} * a_i # broadcast a_i 1->C, and R_{ij} (1,1,1,1)
142
       ->(F,F,K,K), 1->batch
143
           # Out
                    [?, 1, C, 1, 1, F, F, 1, 1]
144
           self.R_j = self.reduce_icaps(R_ij)
145
146
           # Out
                    [?, 1, C, 1, 1, F, F, 1, 1]
147
148
           self.alpha_j = self.alpha0 + self.R_j
           # self.alpha_j = torch.exp(self.alpha0) + self.R_j # when
149
       alpha's a param
           self.kappa_j = self.kappa0 + self.R_j
150
           self.nu_j = self.nu0 + self.R_j
152
           # Out
                     [?, 1, C, P*P, 1, F, F, 1, 1]
153
           mu_j = (1./self.R_j) * self.reduce_icaps(R_ij * V_ji)
154
155
           # Out
                     [?, 1, C, P*P, 1, F, F, 1, 1]
156
           \# self.m_j = (1./self.kappa_j) * (self.R_j * mu_j + self.
       kappa0 * self.m0) # use this if self.m0 != 0
           self.m_j = (1./self.kappa_j) * (self.R_j * mu_j) # priors
       removed for faster computation
159
           if self.cov == 'diag':
160
              # Out [?, 1, C, P*P, 1, F, F, 1, 1] (1./R_j) not
161
       needed because Psi_j calc
```

```
sigma_j = self.reduce_icaps(R_ij * (V_ji - mu_j).pow(2)
       )
                # Out
                           [?, 1, C, P*P, 1, F, F, 1, 1]
164
                \# self.invPsi_j = self.Psi0 + sigma_j + (self.kappa0*
165
       self.R_{j} / self.kappa_{j}) \setminus
                      * (mu_j - self.m0).pow(2) # use this if m0 != 0
       or kappa0 != 1
                self.invPsi_j = self.Psi0 + sigma_j + (self.R_j / self.
       kappa_j) * (mu_j).pow(2) # priors removed for faster
       computation
168
                # Out
                           [?, 1, C, 1, 1, F, F, 1, 1] (-) sign as inv.
       Psi_j
                self.lndet_Psi_j = -self.reduce_poses(torch.log(self.
       invPsi_j)) # log det of diag precision matrix
            elif self.cov == 'full':
                #[?, B, C, P*P, P*P, F, F, K, K]
173
                sigma_j = self.reduce_icaps(
174
                    R_{ij} * (V_{ji} - mu_{j}) * (V_{ji} - mu_{j}).transpose(3,4)
                # Out
                          [?, 1, C, P*P, P*P, F, F, 1, 1] full cov,
       torch.inverse(self.Psi0)
                self.invPsi_j = self.Psi0 + sigma_j + (self.kappa0*self)
       .R_{j} / self.kappa_{j}) \setminus
                    * (mu_j - self.m0) * (mu_j - self.m0).transpose
179
       (3.4)
180
                # Out
                           [?, 1, C, F, F, 1, 1 , P*P, P*P]
181
                # needed for pytorch (*,n,n) dim requirements in .
182
       cholesky and .inverse
183
                self.invPsi_j = self.invPsi_j.permute
       (0,1,2,5,6,7,8,3,4)
                           [?, 1, 1, 1, C, F, F, 1, 1] (-) sign as inv.
185
       Psi_j
                self.lndet_Psi_j = -2*torch.diagonal(torch.cholesky(
186
                    self.invPsi_j), dim1=-2, dim2=-1).log().sum(-1,
187
       keepdim=True)[...,None]
188
       def update_qlatent(self, a_i, V_ji):
189
190
                      [?, 1, C, 1, 1, F, F, 1, 1]
191
           self.Elnpi_j = torch.digamma(self.alpha_j) \
                - torch.digamma(self.alpha_j.sum(dim=2, keepdim=True))
193
194
           # Out
                      [?, 1, C, 1, 1, F, F, 1, 1] broadcasting diga_arg
195
            self.Elnlambda_j = self.reduce_poses(
196
                {\tt torch.digamma(.5*(self.nu_j - self.diga\_arg)))} \  \  \, \\
197
                    + self.Dlog2 + self.lndet_Psi_j
198
199
           if self.cov == 'diag':
200
                         [?, B, C, 1, 1, F, F, K, K]
201
                # Out
                ElnQ = (self.D/self.kappa_j) + self.nu_j \setminus
202
                    * self.reduce_poses((1./self.invPsi_j) * (V_ji -
203
```

```
self.m_j).pow(2)
204
            elif self.cov == 'full':
205
                # Out [?, B, C, 1, 1, F, F, K, K]
Vm_j = V_ji - self.m_j
206
207
                ElnQ = (self.D/self.kappa_j) + self.nu_j * self.
208
       reduce_poses(
                    Vm_j.transpose(3,4) * torch.inverse(
209
                        self.invPsi_j).permute(0,1,2,7,8,3,4,5,6) *
210
       Vm_j)
211
                      [?, B, C, 1, 1, F, F, K, K]
            # Out
212
           lnp_j = .5*self.Elnlambda_j -.5*self.Dlog2pi -.5*ElnQ
213
214
           # Out
                    [?, B, C, 1, 1, F, F, K, K]
215
           p_j = torch.exp(self.Elnpi_j + lnp_j)
216
217
                      [?*B, 1, F', F']
                                             [?*B, K*K, F, F]
                                                                    [?, B,
218
       1, 1, 1, F, F, K, K]
            sum_p_j = F.conv_transpose2d(
219
                input=p_j.sum(dim=2, keepdim=True).reshape(
                    -1, *self.F_o, self.K*self.K).permute(0, -1, 1, 2).
221
       contiguous(),
                weight=self.filter,
                stride=[self.S, self.S])
223
224
                      [?*B, 1, F, F, K, K]
            sum_p_j = sum_p_j.unfold(2, size=self.K, step=self.S).
226
       unfold(3, size=self.K, step=self.S)
227
228
                      [?, B, 1, 1, 1, F, F, K, K]
            sum_p_j = sum_p_j.reshape([-1, self.B, 1, 1, 1, *self.F_o,
229
       self.K, self.K])
230
            # Out
                      [?, B, C, 1, 1, F, F, K, K] # normalise over
231
       out_caps j
           return 1. / torch.clamp(sum_p_j, min=1e-11) * p_j
232
233
       def reduce_icaps(self, x):
234
            return x.sum(dim=(1,-2,-1), keepdim=True)
235
236
237
       def reduce_poses(self, x):
           return x.sum(dim=(3,4), keepdim=True)
```

Listing 11:  $src/VarCaps/vb_routing.py$