

## Random Variable

Population vs. Sample.

Sample Bias

30 states  
10000  
⇒ 3L

$$\mu = \frac{1}{N} \sum_{i=1}^N x_i$$

(mu) → Population mean

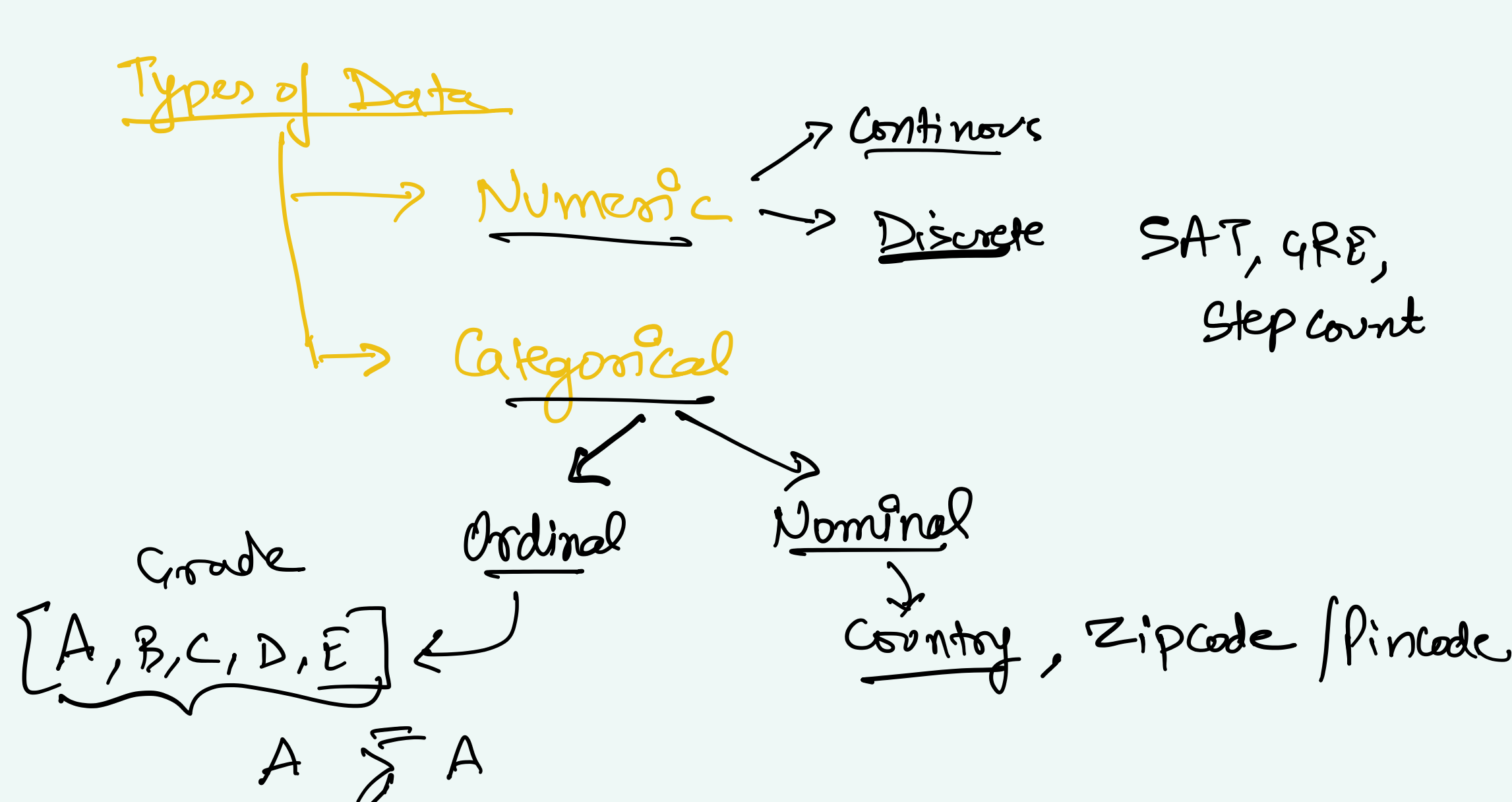
$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

Sample mean

→ Stratified Sampling

Data

↳ Structured  
↳ Unstructured (Deep Learning)



$x = [10, 5, 4, 11], 2000$   $n=6$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i = \frac{8+10+5+4+2+11}{6}$$

Summation

weighted mean

$$\bar{x} = \frac{\sum_{i=1}^n (x_i \cdot w_i)}{\sum_{i=1}^n w_i}$$

$w = [0.9, 1, 1, 1, 1, 1]$

$$\frac{8 \times 0.9 + 10 \times 1 + \dots}{0.9 + 1 + \dots}$$

Median

$x = [10, 8, 4, 1, 7, 3]$

median(x) = ① Sort the data  
② the middle value is the median

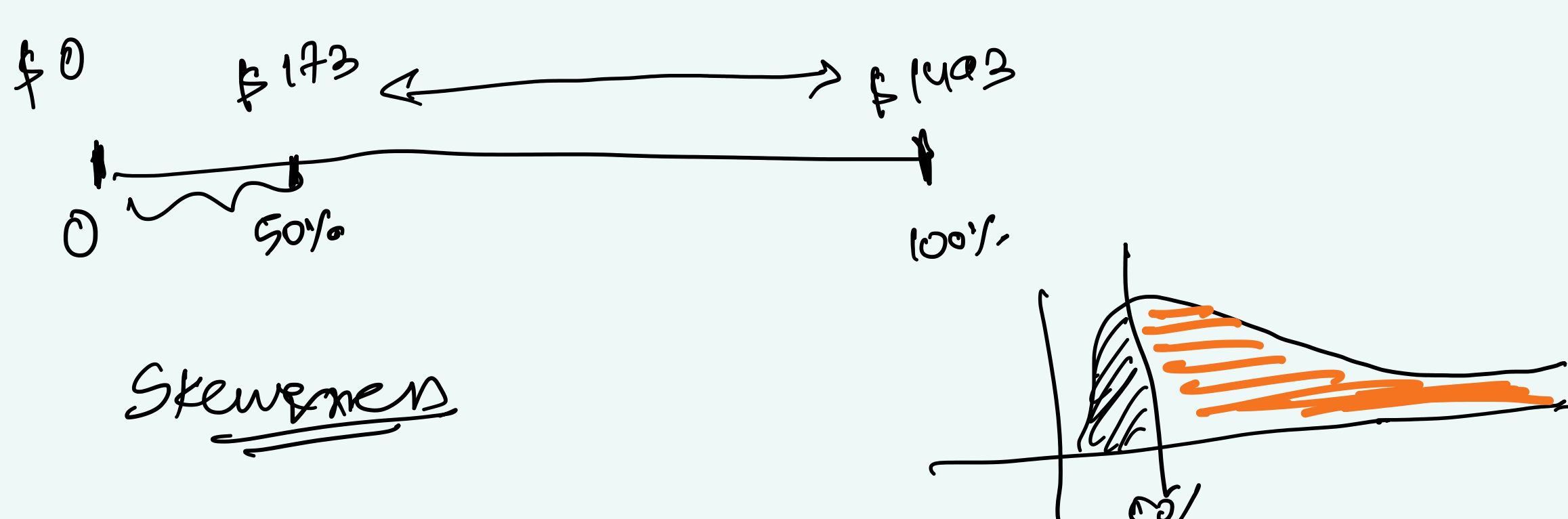
①  $[1, 3, 4, 7, 8, 10, 2000, 2500]$

✓  $n = \text{Even} \Rightarrow \text{avg} \left[ \frac{n}{2}, \frac{n+1}{2} \right] \approx 5.5$

✓  $n = \text{odd} \Rightarrow \left[ \frac{n+1}{2} \right] \approx 7$

$\frac{7+8}{2} \Rightarrow 7.5$

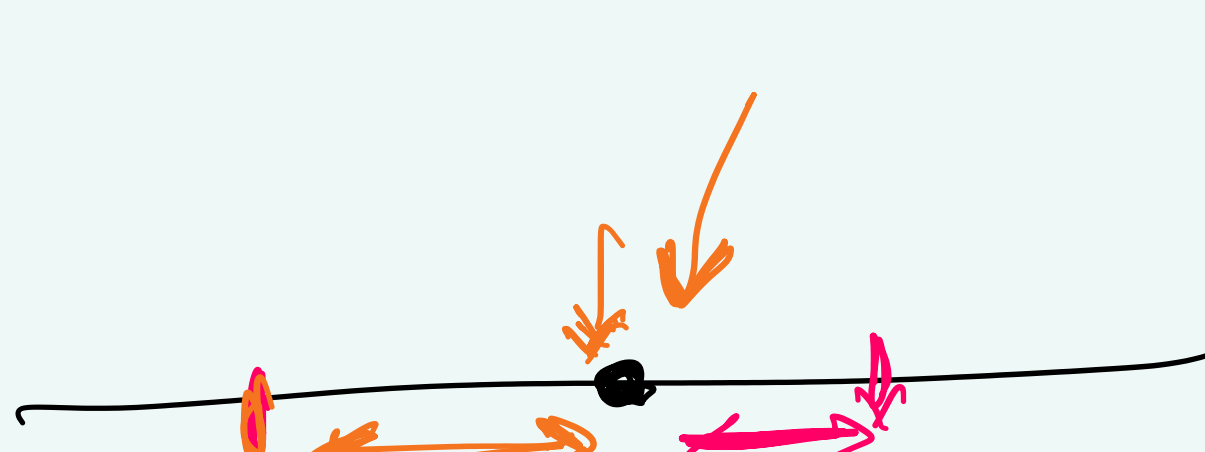
Mean vs. Median



Variability

Mean absolute deviation =  $\frac{1}{n} \sum_{i=1}^n |x_i - \bar{x}|$

- ① take mean
- ② Subtract mean from all the points (abs)
- ③ Mean(take)



Standard deviation / Variance

Variance =  $S^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$

$n-1$  : Bias Estimate

$S$  = Standard deviation.

Variance =  $S^2$

$S = \sqrt{\text{Variance}}$

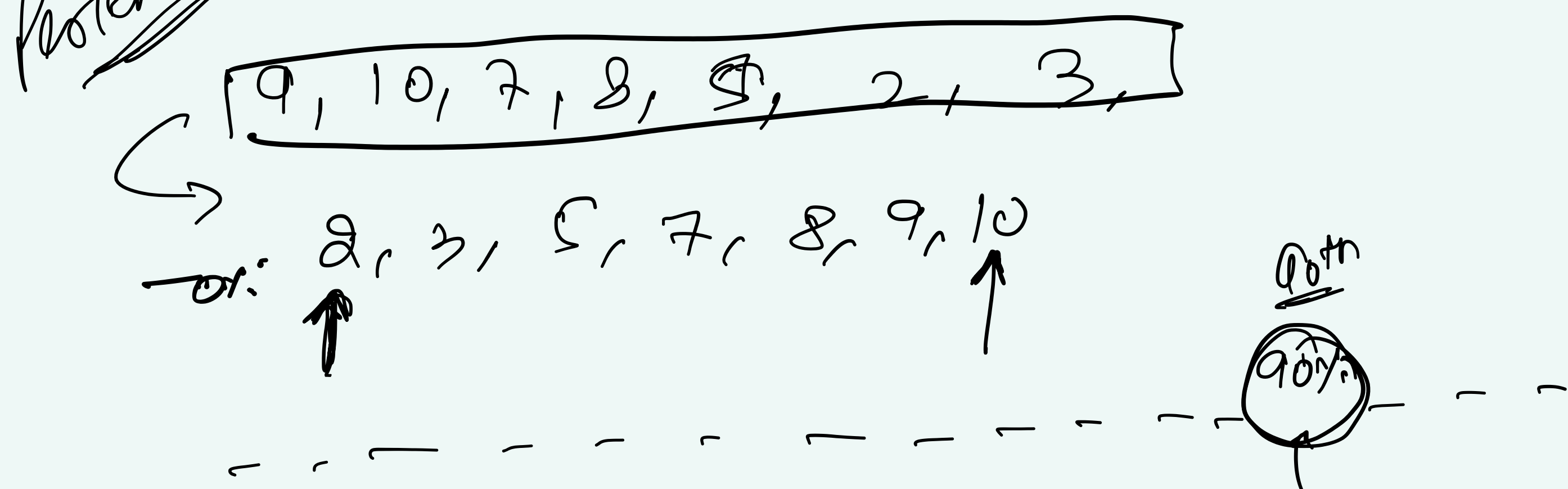
MAD

Median Absolute Deviation ⇒  $x = [x_1, x_2, x_3, \dots, x_n]$

median(x) = m

$\text{median}(|x_1 - m|, |x_2 - m|, |x_3 - m|, \dots, |x_n - m|)$

p<sup>th</sup> percentile → p values →  $x$



(parameter) vs. Statistic

$\mu$