

Reflections 2: Array query

1) Maximum subarray problem

$O(n^2)$ solution:

```
max=0;
```

```
arr=[-1,2,3,4,5,6]
```

```
l1=len(arr)
```

```
sum=0
```

```
for i in range(l1): #l1 is the array length
```

```
    for j in range(l1):
```

```
        sum= sum+arr[i] + arr[j]
```

```
        print(sum)
```

```
        if(sum>max):
```

```
            max=sum
```

```
print(max)
```

we can also have an another array to store cumulative results for every 'i'

This works with input size is 10^3 but when input size increases we need to find more optimal solution so



Yessss!. Kadane's algorithm

K	<i>is for kindness, you always show.</i>
A	<i>is for aptitudes, your special capabilities shine</i>
D	<i>is for desire, your thoughts do aspire.</i>
A	<i>is for adaptable, whenever things change</i>
N	<i>is for notable, distinguished are your feats</i>
E	<i>is for enamoured, forever will your children be with you and wide spread your algorithm.</i>

Okay Enough of it Now!.

Kadane's algorithm works in Time complexity $O(n)$

Dynamic programming approach:

Reflections 2: Array query

If the sub array would end at any particular index, what would be my maximum contiguous subarray sum?

Steps:

- At a given index, i should choose between the max of two numbers $\max(n1, n2)$ where $n1$ is the value at previous index and $n2$ is the value at the given index plus the value at $n1$ (previous index).
- Whichever is the max its value is stored as value at that given index.

```
def max_subarray(A):
```

```
    max_ending_here = max_so_far = A[0]
```

```
    for x in A[1:]:
```

```
        max_ending_here = max(x, max_ending_here + x)
```

```
        max_so_far = max(max_so_far, max_ending_here)
```

```
    return max_so_far
```

This is $O(n)$ solution for Maximum subarray problem

2) LookUp Table Technique:

This technique is used when input is n^5 , we precompute the results in form a table and query this table for any input.

It uses memory space of $n*n$ bytes and efficiency is $O(n*n)$ and fetch time is $O(1)$.

The memory utilization is more compared to others since 2D matrix is constructed for a given array.

3) Square-Root Decomposition:

It builds a 1D array of size= $\sqrt{\text{size of original array}}$ And query is fetched in $O(\sqrt{n})$ time where n is the size of the original array.

block - 0			block - 1			block - 2		
8			11			15		
0	1	2	3	4	5	6	7	8
1	5	2	4	6	1	3	5	7

Reflections 2: Array query

This original array is divided into $\sqrt{\text{size}(\text{original array})}$ ie here $\text{len}(\text{arr})=8$ and number of blocks formed by sqrt decomposition is Three and hence the search space is reduced
Eg if index 6 is given some query 1) we do $6/3$ ie query index/number of blocks we get 2 and
2) To find its index in that block we do mod operation ie $6\%3$ we get 0 hence we query at index 0 of block 2

Demerits

When the search space is between these blocks we will have to combine two blocks and search for the query index.

This can be overcome by Segment Trees.

PS: Explanation on segment trees will be added in the next commit.