

# 1 Optimal Control of Pitch/Travel with Feedback (LQ)

In this task we add feedback to the optimal controller that we developed in ??

## 1.1 LQ controller

*Briefly explain LQ controller. Especially, but not limited to, what is the role of the matrices  $Q$  and  $R$ ? Justify your choice of weights.*

An LQ, or linear-quadratic, regulator is an optimal feedback controller that can be applied to a linear model  $\Delta x = A\Delta x_i + B\Delta u_i$  with a quadratic cost function:

$$J = \sum_{i=0}^{\infty} \Delta x_{i+1}^{\top} Q \Delta x_{i+1} + \Delta u_i^{\top} R \Delta u_i, \quad Q \geq 0, \quad R > 0 \quad (1)$$

Here  $\Delta x = x - x^*$  and  $\Delta u = u - u^*$  are deviations from the optimal trajectory.

The matrix  $Q$  and the scalar  $R$  are weights in the optimization problem. The value of  $Q$  determines how much deviation in the state value should be penalized, while the value of  $R$  determines how much input-usage should be punished. This allows the designer to optimize the regulator to the specific implementation: A system where the input is cheap (like the helicopter used in this assignment) would have a relatively small value of  $R$  compared to  $Q$ .

## 1.2 Model Predictive Control

*Answer 10.3.1.3 here.*

## 1.3 Experimental results

*Printouts of data from relevant experiments (plots). Discussion and analysis of the results. Answer 10.3.2.5 here.*

## 1.4 MATLAB and Simulink

*Code and diagrams go here*