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Train two models, multinomial naive Bayes and binarized naive Bayes, both with add-1 smoothing, on the following document counts for key sentiment words, with positive or negative class assigned as noted.

doc "good" "poor" "great" (class)

d1. 3 0 3 pos

d2. 0 1 2 pos

d3. 1 3 0 neg

d4. 1 5 2 neg

d5. 0 2 0 neg

Use both naive Bayes models to assign a class (pos or neg) to this sentence:

A good, good plot and great characters, but poor acting. Do the two models agree or disagree?

Answer:

Count of positive documents (pos): 2

Count of negative documents (neg): 3

Total number of documents: 5

$P(\text{class} = \text{pos}) = 2/5$

$P(\text{class} = \text{neg}) = 3/5$

Calculating the probabilities of each word occurring in each class:

$P(\text{good}|\text{pos}) = (3 + 1) / (3 + 1 + 1) = 4/5$

$P(\text{good}|\text{neg}) = (1 + 1) / (1 + 3 + 1) = 2/6 = 1/3$

$P(\text{poor}|\text{pos}) = (0 + 1) / (3 + 1 + 1) = 1/5$

$P(\text{poor}|\text{neg}) = (3 + 1) / (1 + 3 + 1) = 4/6 = 2/3$

$P(\text{great}|\text{pos}) = (3 + 1) / (3 + 1 + 1) = 4/5$

$P(\text{great}|\text{neg}) = (0 + 1) / (1 + 3 + 1) = 1/6$

Now, to classify the sentence "A good, good plot and great characters, but poor acting" using the multinomial Naive Bayes model, we need to calculate the probabilities for each class.

$$\begin{aligned} P(\text{class} = \text{pos}|\text{sentence}) &= P(\text{pos}) * P(\text{good}|\text{pos})^2 * P(\text{poor}|\text{pos}) * P(\text{great}|\text{pos}) \\ &= (2/5) * (4/5)^2 * (1/5) * (4/5) \\ &= 128/625 \end{aligned}$$

$$\begin{aligned} P(\text{class} = \text{neg}|\text{sentence}) &= P(\text{neg}) * P(\text{good}|\text{neg})^2 * P(\text{poor}|\text{neg}) * P(\text{great}|\text{neg}) \\ &= (3/5) * (1/3)^2 * (2/3) * (1/6) \\ &= 2/45 \end{aligned}$$

So that $P(\text{class} = \text{pos}|\text{sentence}) = 128/625$

$P(\text{class} = \text{neg}|\text{sentence}) = 2/45$