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Assignment Lesson8

1. Find encoder and decoder of LZ78? If we have:

Input string: "abdcaedbdcecabbdeacb"

2. Find encoder and decoder of LZ77? If we have:

Input string: "cdaabbefacbdegfeeabfedegg"

Answers

1. Find encoder and decoder of LZ78? If we have:

Input string: "abdcaedbdcecabbdeacb"

- + Encoder
 - Find all different character "a, b, c, d, e" and based dictionary

| Entry | Codeword |
|-------|----------|
| | |
| a | 1 |
| b | 2 |
| С | 3 |
| d | 4 |
| е | 5 |

Based Dictionary

| a | b | d | c | a | e | d | b | d | c | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

- > Start from "a".
 - "a" has in the base dictionary
 - So, we take "ab".
 - "ab" doesn't have in the dictionary.
 - We add "ab" to output dictionary.
 - The last codeword is 5.
 - New codeword must be 6.

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |

Find next character:

| a | b | d | c | a | e | d | Ъ | d | c | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

- > Start from "d".
 - "d" has in the base dictionary

- So, we take "dc".
- "dc" doesn't have in the dictionary.
- We add "dc" to output dictionary.
- The last codeword is 6.
- New codeword must be 7.

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |
| dc | 7 | <4,3> |

| a | b | d | С | a | e | d | b | d | c | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

Start from "a".

- "a" has in the base dictionary
- So, we take "ae".
- "ae" doesn't have in the dictionary.
- We add "ae" to output dictionary.
- The last codeword is 7.
- New codeword must be 8.

| Entry | Codeword | Output | |
|-------|----------|--------|--|
| ab | 6 | <1,2> | |
| dc | 7 | <4,3> | |
| ae | 8 | <1,5> | |

> Find next character:

| a | b | d | c | a | e | d | b | d | c | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

> Start from "d".

- "d" has in the base dictionary
- So, we take "db".
- "db" doesn't have in the dictionary.
- We add "db" to output dictionary.
- The last codeword is 8.
- New codeword must be 9.

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |
| de | 7 | <4,3> |
| ae | 8 | <1,5> |
| db | 9 | <4,2> |

> Find next character:

| a | b | d | С | a | e | d | b | d | c | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

Start from "d".

- "d" has in the base dictionary
- So, we take "dc".

- "dc" has in the dictionary
- So, we take "dce"
- "dce" doesn't have in the dictionary.
- We add "dce" to output dictionary.
- The last codeword is 9.
- New codeword must be 10.

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |
| dc | 7 | <4,3> |
| ae | 8 | <1,5> |
| db | 9 | <4,2> |
| dce | 10 | <7,5> |

| a | b | d | c | a | e | d | b | d | С | e | c | a | Ъ | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

Start from "c".

- "c" has in the base dictionary
- So, we take "ca".
- "ca" doesn't have in the dictionary.
- We add "ca" to output dictionary.
- The last codeword is 10.
- New codeword must be 11.

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |
| dc | 7 | <4,3> |
| ae | 8 | <1,5> |
| db | 9 | <4,2> |
| dce | 10 | <7,5> |
| ca | 11 | <3,1> |

> Find next character:

| a | b | d | С | a | e | d | Ъ | d | С | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

> Start from "b".

- "b" has in the base dictionary
- So, we take "bb".
- "bb" doesn't have in the dictionary.
- We add "bb" to output dictionary.
- The last codeword is 11.
- New codeword must be 12.

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |
| dc | 7 | <4,3> |
| ae | 8 | <1,5> |
| db | 9 | <4,2> |

| dce | 10 | <7,5> |
|-----|----|-------|
| ca | 11 | <3,1> |
| bb | 12 | <2,2> |

| a | b | d | С | a | e | d | b | d | С | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

> Start from "d".

- "d" has in the base dictionary
- So, we take "de".
- "de" doesn't have in the dictionary.
- We add "de" to output dictionary.
- The last codeword is 12.
- New codeword must be 13.

| Entry | Codeword | Output | |
|-------|----------|--------|--|
| ab | 6 | <1,2> | |
| dc | 7 | <4,3> | |
| ae | 8 | <1,5> | |
| db | 9 | <4,2> | |
| dce | 10 | <7,5> | |
| ca | 11 | <3,1> | |
| bb | 12 | <2,2> | |
| de | 13 | <4,5> | |

> Find next character:

| a | b | d | С | a | e | d | Ъ | d | С | e | c | a | b | b | d | e | a | c | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

> Start from "a".

- "a" has in the base dictionary
- So, we take "ac".
- "ac" doesn't have in the dictionary.
- We add "ac" to output dictionary.
- The last codeword is 13.
- New codeword must be 14.

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |
| dc | 7 | <4,3> |
| ae | 8 | <1,5> |
| db | 9 | <4,2> |
| dce | 10 | <7,5> |
| ca | 11 | <3,1> |
| bb | 12 | <2,2> |
| de | 13 | <4,5> |
| ac | 14 | <1,3> |

| a | b | d | c | a | e | d | b | d | С | e | c | a | b | b | d | e | a | С | b | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | |

- > Start from "b".
 - "b" has in the base dictionary
 - But, there is no next character (EOF)
 - We just add codeword to "Output".

| Entry | Codeword | Output |
|-------|----------|--------|
| ab | 6 | <1,2> |
| dc | 7 | <4,3> |
| ae | 8 | <1,5> |
| db | 9 | <4,2> |
| dce | 10 | <7,5> |
| ca | 11 | <3,1> |
| bb | 12 | <2,2> |
| de | 13 | <4,5> |
| ac | 14 | <1,3> |
| EOF | EOF | <2,> |

➤ We need to use base Dictionary and encoder:

| Entry | Codeword |
|-------|----------|
| a | 1 |
| b | 2 |
| С | 3 |
| d | 4 |
| e | 5 |

Base Dictionary

$$\Rightarrow \text{ Encoder} = \{ <1,2>, <4,3>, <1,5>, <4,2>, <7,5>, <3,1>, <2,2>, <4,5>, <1,3>, <2,> \}$$

> Next, build an output dictionary

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

- ➤ Output Dictionary start from <1,2>
 - Codeword: "1" is "a" and "2" is "b"
 - Entry is "ab".
 - So, output is also "ab".
 - New codeword is 6.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <1,2> | 6 | ab | ab |

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

- ➤ Output Dictionary start from <4,3>
 - Codeword: "4" is "d" and "3" is "c"
 - Entry is "dc".
 - So, output is also "dc".
 - New codeword is 7.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | dc | dc |

Next, build an output dictionary

| <1,2 | > <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|------|---------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Outp | ut | | | | | | | | | |

- Output Dictionary start from <1,5>
 - Codeword: "1" is "a" and "5" is "e"
 - Entry is "ae".
 - So, output is also "ae".
 - New codeword is 8.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | dc | dc |
| <1,5> | 8 | ae | ae |

Next, build an output dictionary

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

- ➤ Output Dictionary start from <4,2>
 - Codeword: "4" is "d" and "2" is "b"
 - Entry is "db".
 - So, output is also "db".
 - New codeword is 9.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | dc | dc |
| <1,5> | 8 | ae | ae |
| <4,2> | 9 | db | db |

Next, build an output dictionary

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

> Output Dictionary start from <7,5>

- Codeword: "7" is "dc" and "5" is "e"
- Entry is "dce".
- So, output is also "dce".
- New codeword is 10.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | dc | dc |
| <1,5> | 8 | ae | ae |
| <4,2> | 9 | db | db |
| <7,5> | 10 | dce | dce |

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

➤ Output Dictionary start from <3,1>

- Codeword: "3" is "c" and "1" is "a"
- Entry is "ca".
- So, output is also "ca".
- New codeword is 11.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | de | dc |
| <1,5> | 8 | ae | ae |
| <4,2> | 9 | db | db |
| <7,5> | 10 | dce | dce |
| <3,1> | 11 | ca | ca |

Next, build an output dictionary

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

➤ Output Dictionary start from <2,2>

- Codeword: "2" is "b" and "2" is "b"
- Entry is "bb".
- So, output is also "bb".
- New codeword is 12.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | dc | dc |
| <1,5> | 8 | ae | ae |
| <4,2> | 9 | db | db |
| <7,5> | 10 | dce | dce |
| <3,1> | 11 | ca | ca |
| <2,2> | 12 | bb | bb |

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

- > Output Dictionary start from <4,5>
 - Codeword: "4" is "d" and "5" is "e"
 - Entry is "de".
 - So, output is also "de".
 - New codeword is 13.

| Input | Codeword | Entry | Output |
|---|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | dc | dc |
| <1,5> | 8 | ae | ae |
| <4,2> | 9 | db | db |
| <7,5> | 10 | dce | dce |
| <3,1> | 11 | ca | ca |
| <1,2> <4,3> <1,5> <4,2> <7,5> <3,1> <2,2> | 12 | bb | bb |
| <4,5> | 13 | de | de |

Next, build an output dictionary

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

- Output Dictionary start from <1,3>
 - Codeword: "1" is "a" and "3" is "c"
 - Entry is "ac".
 - So, output is also "ac".
 - New codeword is 14.

| Input | Codeword | Entry | Output |
|---|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| | 7 | dc | dc |
| <1,5> | 8 | ae | ae |
| <4,2> | 9 | db | db |
| <7,5> | 10 | dce | dce |
| <3,1> | 11 | ca | ca |
| <2,2> | 12 | bb | bb |
| <4,3> <1,5> <4,2> <7,5> <3,1> <2,2> <4,5> <1,3> | 13 | de | de |
| <1,3> | 14 | ac | ac |

Next, build an output dictionary

| <1,2> | <4,3> | <1,5> | <4,2> | <7,5> | <3,1> | <2,2> | <4,5> | <1,3> | <2,> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----|
| Output | | | | | | | | | | |

- Output Dictionary start from <2,>
 - Codeword: "2" is "b" and "" is "eof"
 - Entry is "b".
 - So, output is also "b".
 - New codeword is EOF.

| Input | Codeword | Entry | Output |
|---|----------|-------|--------|
| <1,2> | 6 | ab | ab |
| <4,3> | 7 | dc | dc |
| <1,5> | 8 | ae | ae |
| <4,2> | 9 | db | db |
| <7,5> | 10 | dce | dce |
| <3,1> | 11 | ca | ca |
| <2,2> | 12 | bb | bb |
| <4,5> | 13 | de | de |
| <1,2> <4,3> <1,5> <4,2> <7,5> <3,1> <2,2> <4,5> <1,3> | 14 | ac | ac |
| <2,> | EOF | ь | b |

Thus, Decoder = abdcaedbdcecabbacb

2. Find encoder and decoder of LZ78? If we have:

Input string: "cdaabbefacbdegfeeabfedegg"

+ Encoder

Find all different character "a, b, c, d, e, f, g" and based dictionary

| Entry | Codeword |
|-------|----------|
| a | 1 |
| b | 2 |
| С | 3 |
| d | 4 |
| е | 5 |
| f | 6 |
| g | 7 |

Based Dictionary

| С | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- > Start from "c".
 - "c" has in the base dictionary
 - So, we take "cd".
 - "cd" doesn't have in the dictionary.
 - We add "cd" to output dictionary.
 - The last codeword is 7.
 - New codeword must be 8.

| Entry | Codeword | Output |
|-------|----------|--------|
| cd | 8 | <3,4> |

> Find next character:

| С | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- > Start from "a".
 - "a" has in the base dictionary
 - So, we take "aa".
 - "aa" doesn't have in the dictionary.
 - We add "aa" to output dictionary.
 - The last codeword is 8.
 - New codeword must be 9.

| Entry | Codeword | Output |
|-------|----------|--------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |

| c | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- > Start from "b".
 - "b" has in the base dictionary
 - So, we take "bb".
 - "bb" doesn't have in the dictionary.
 - We add "bb" to output dictionary.
 - The last codeword is 9.
 - New codeword must be 10.

| Entry | Codeword | Output |
|-------|----------|--------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |

Find next character:

| c | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- Start from "e".
 - "e" has in the base dictionary
 - So, we take "ef".
 - "ef" doesn't have in the dictionary.
 - We add "ef" to output dictionary.
 - The last codeword is 10.
 - New codeword must be 11.

| Entry | Codeword | Output |
|-------|----------|--------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |

Find next character:

| С | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

> Start from "a".

- "a" has in the base dictionary
- So, we take "ac".
- "ac" doesn't have in the dictionary.
- We add "ac" to output dictionary.
- The last codeword is 11.
- New codeword must be 12.

| Entry | Codeword | Output |
|-------|----------|--------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |

| c | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

> Start from "b".

- "b" has in the base dictionary
- So, we take "bd".
- "bd" doesn't have in the dictionary.
- We add "bd" to output dictionary.
- The last codeword is 12.
- New codeword must be 13.

| Entry | Codeword | Output |
|-------|----------|--------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |
| bd | 13 | <2,4> |

> Find next character:

| c | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

> Start from "e".

- "e" has in the base dictionary
- So, we take "eg".
- "eg" doesn't have in the dictionary.
- We add "eg" to output dictionary.
- The last codeword is 13.
- New codeword must be 14.

| Entry | Codeword | Output |
|-------|----------|--------|
|-------|----------|--------|

| cd | 8 | <3,4> |
|----|----|-------------------------|
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |
| bd | 13 | <5,6> <1,3> <2,4> <5,7> |
| eg | 14 | <5,7> |

| С | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | EOF |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- > Start from "f".
 - "f" has in the base dictionary
 - So, we take "fe".
 - "fe" doesn't have in the dictionary.
 - We add "fe" to output dictionary.
 - The last codeword is 14.
 - New codeword must be 15.

| Entry | Codeword | Output |
|-------|----------|--------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |
| bd | 13 | <2,4> |
| eg | 14 | <5,7> |
| fe | 15 | <6,5> |

> Find next character:

| c | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | eof |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- > Start from "e".
 - "e" has in the base dictionary
 - So, we take "ea".
 - "ea" doesn't have in the dictionary.
 - We add "ea" to output dictionary.
 - The last codeword is 15.
 - New codeword must be 16.

| Entry | Codeword | Output |
|----------|----------|----------------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |
| bd | 13 | <2,4> |
| eg | 14 | <5,7> |
| eg fe | 15 | <6,5> <5,1> |
| ea | 16 | <5,1> |

| c | d | a | a | b | b | e | f | a | C | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | eof |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- > Start from "b".
 - "b" has in the base dictionary
 - So, we take "bf".
 - "bf" doesn't have in the dictionary.
 - We add "bf" to output dictionary.
 - The last codeword is 16.
 - New codeword must be 17.

| Entry | Codeword | Output |
|-------|----------|-------------------------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |
| bd | 13 | <2,4> |
| eg | 14 | <5,7> |
| fe | 15 | <6,5> |
| ea | 16 | <5,1> |
| bf | 17 | <5,7> <6,5> <5,1> <2,6> |

> Find next character:

| c | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | eof |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| start | | | | | | | | | | | | | | | | | | | | | | | | | |

- > Start from "e".
 - "e" has in the base dictionary
 - So, we take "ed".
 - "ed" doesn't have in the dictionary.
 - We add "ed" to output dictionary.
 - The last codeword is 17.
 - New codeword must be 18.

| Entry | Codeword | Output |
|-------|----------|-------------------------|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> <5,6> <1,3> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |
| bd | 13 | <2,4> <5,7> |
| eg | 14 | <5,7> |
| fe | 15 | <6,5> |
| ea | 16 | <5,1> |
| bf | 17 | <6,5> <5,1> <2,6> <5,4> |
| ed | 18 | <5,4> |

> Find next character:

| c | d | a | a | b | b | e | f | a | c | b | d | e | g | f | e | e | a | b | f | e | d | e | g | g | eof | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|--|
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|--|

| start | | | | | | | | | | | | | |
|-------|--|--|--|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | | | | | |

- > Start from "e".
 - "e" has in the base dictionary
 - So, we take "eg".
 - "eg" has in dictionary
 - So, we take "egg"
 - "egg" doesn't have in the dictionary.
 - We add "egg" to output dictionary.
 - The last codeword is 18.
 - New codeword must be EOF.

| Entry | Codeword | Output |
|-------|----------|---|
| cd | 8 | <3,4> |
| aa | 9 | <1,1> |
| bb | 10 | <2,2> |
| ef | 11 | <5,6> |
| ac | 12 | <1,3> |
| bd | 13 | <2,4> |
| eg | 14 | <5,7> |
| fe | 15 | <6,5> |
| ea | 16 | <5,1> |
| bf | 17 | <2,6> |
| ed | 18 | <3,4> <1,1> <2,2> <5,6> <1,3> <2,4> <5,7> <6,5> <1,5 <4,5 <1,4 <4,7> |
| egg | EOF | <14,7> |

Thus, Encoder = { <3,4>, <1,1>, <2,2>, <5,6>, <1,3>, <2,4>, <5,7>,<6,5>, <5,1>, <2,6>, <5,4>, <14,7>}

+ Decoder:

➤ We need to use base Dictionary and encoder:

| Entry | Codeword |
|-------|----------|
| a | 1 |
| b | 2 |
| С | 3 |
| d | 4 |
| e | 5 |
| f | 6 |
| g | 7 |

Base Dictionary

Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

> Output Dictionary start from <3,4>

- Codeword: "3" is "c" and "4" is "d"
- Entry is "cd".
- So, output is also "cd".
- New codeword is 8.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

> Output Dictionary start from <1,1>

- Codeword: "1" is "a"
- Entry is "aa".
- So, output is also "aa".
- New codeword is 9.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |

Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

> Output Dictionary start from <2,2>

- Codeword: "2" is "b"
- Entry is "bb".
- So, output is also "bb".
- New codeword is 10.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |

> Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

> Output Dictionary start from <5,6>

- Codeword: "5" is "e" and "6" is "f"
- Entry is "ef".
- So, output is also "ef".
- New codeword is 11.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

Output Dictionary start from <1,3>

- Codeword: "1" is "a" and "3" is "c"
- Entry is "ac".
- So, output is also "ac".
- New codeword is 12.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |
| <1,3> | 12 | ac | ac |

Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

> Output Dictionary start from <2,4>

- Codeword: "2" is "b" and "4" is "d"
- Entry is "bd".
- So, output is also "bd".
- New codeword is 13.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |
| <1,3> | 12 | ac | ac |
| <2,4> | 13 | bd | bd |

➤ Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

Output Dictionary start from <5,7>

- Codeword: "5" is "e" and "7" is "g"
- Entry is "eg".
- So, output is also "eg".
- New codeword is 14.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |
| <1,3> | 12 | ac | ac |

| <2,4> | 13 | bd | bd |
|-------|----|----|----|
| <5,7> | 14 | eg | eg |

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

Output Dictionary start from <6,5>

- Codeword: "6" is "f" and "5" is "e"
- Entry is "fe".
- So, output is also "fe".
- New codeword is 15.

| Input | Codeword | Entry | Output |
|-------------------------------------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <3,4> <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |
| <1,3> | 12 | ac | ac |
| <2,4> | 13 | bd | bd |
| <5,7> | 14 | eg | eg |
| <2,2> <5,6> <1,3> <2,4> <5,7> <6,5> | 15 | fe | fe |

Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

➤ Output Dictionary start from <5,1>

- Codeword: "5" is "e" and "1" is "a"
- Entry is "ea".
- So, output is also "ea".
- New codeword is 16.

| Input | Codeword | Entry | Output |
|---|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |
| <1,3> | 12 | ac | ac |
| <2,4> | 13 | bd | bd |
| <5,7> | 14 | eg | eg |
| <3,4> <1,1> <2,2> <5,6> <1,3> <2,4> <5,7> <6,5> <1,5> | 15 | fe | fe |
| <5,1> | 16 | ea | ea |

Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

Output Dictionary start from <2,6>

- Codeword: "2" is "b" and "6" is "f"
- Entry is "bf".
- So, output is also "bf".

• New codeword is 17.

| Input | Codeword | Entry | Output |
|---|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |
| <1,3> | 12 | ac | ac |
| <2,4> | 13 | bd | bd |
| <5,7> | 14 | eg | eg |
| <6,5> | 15 | fe | fe |
| <3,4> <1,1> <2,2> <5,6> <1,3> <2,4> <5,7> <6,5> <1,5> <2,6> | 16 | ea | ea |
| <2,6> | 17 | bf | bf |

> Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

➤ Output Dictionary start from <5,4>

- Codeword: "5" is "e" and "4" is "d"
- Entry is "ed".
- So, output is also "ed".
- New codeword is 18.

| Input | Codeword | Entry | Output |
|---|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |
| <5,6> | 11 | ef | ef |
| <1,3> | 12 | ac | ac |
| <2,4> | 13 | bd | bd |
| <5,7> | 14 | eg | eg |
| <6,5> | 15 | fe | fe |
| <5,1> | 16 | ea | ea |
| <3,4> <1,1> <2,2> <5,6> <1,3> <2,4> <5,7> <6,5> <1,5> <5,1> <2,6> <5,4> | 17 | bf | bf |
| <5,4> | 18 | ed | ed |

➤ Next, build an output dictionary

| <3,4> | <1,1> | <2,2> | <5,6> | <1,3> | <2,4> | <5,7> | <6,5> | <5,1> | <2,6> | <5,4> | <14,7> | EOF |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-----|
| Output | | | | | | | | | | | | |

Output Dictionary start from <14,7>

- Codeword: "14" is "eg" and "7" is "g"
- Entry is "egg".
- So, output is also "egg".
- New codeword is EOF.

| Input | Codeword | Entry | Output |
|-------|----------|-------|--------|
| <3,4> | 8 | cd | cd |
| <1,1> | 9 | aa | aa |
| <2,2> | 10 | bb | bb |

| <5,6> | 11 | ef | ef |
|--|-----|-----|-----|
| <1,3> | 12 | ac | ac |
| <2,4> | 13 | bd | bd |
| <5,7> | 14 | eg | eg |
| <6,5> | 15 | fe | fe |
| <5,1> | 16 | ea | ea |
| <2,6> | 17 | bf | bf |
| <5,4> | 18 | ed | ed |
| <5,6> <1,3> <2,4> <5,7> <6,5> <5,1> <2,6> <5,4> <14,7> | EOF | eeg | egg |

 $\textbf{Thus,}\ Decoder = cdaabbefacbdegfeeabfedegg$