# art-attack-analysis-and-prediction

October 27, 2024

I've been working with the Heart Attack Analysis & Prediction dataset I found on Kaggle. Here's the link to the dataset: Heart Attack Analysis & Prediction Dataset.

```
[3]: import pandas as pd
     import numpy as np
     import matplotlib.pyplot as plt
     import seaborn as sns
     from sklearn.model_selection import train_test_split
     from sklearn.linear_model import LinearRegression, Ridge, Lasso, ElasticNet
     from sklearn.preprocessing import PolynomialFeatures, StandardScaler, u
      OneHotEncoder
     from sklearn.metrics import mean squared error, r2 score
     from sklearn.pipeline import Pipeline, make_pipeline
     from sklearn.utils import shuffle
     from sklearn.model_selection import cross_val_score, cross_val_predict,_
      ⇔cross_validate
     from sklearn.linear_model import SGDRegressor
     from sklearn.impute import SimpleImputer
     from sklearn.compose import ColumnTransformer
```

Displaying the statistical values for each of the attributes, along with visualizations (e.g., histogram) of the distributions for each attribute.

```
[4]: # Load the data
df = pd.read_csv("heart.csv")
```

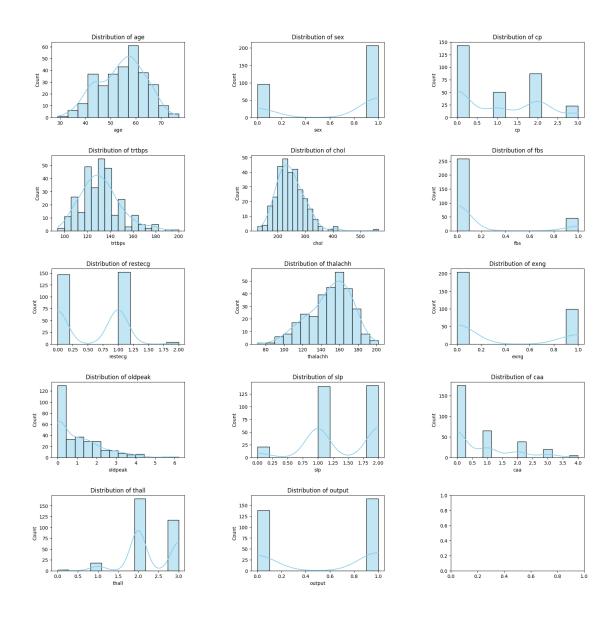
Statistical descriptions

```
[5]: # Display summary statistics
statistics = df.describe()
print(statistics)
```

	age	sex	ср	trtbps	chol	fbs	\
count	303.000000	303.000000	303.000000	303.000000	303.000000	303.000000	
mean	54.366337	0.683168	0.966997	131.623762	246.264026	0.148515	
std	9.082101	0.466011	1.032052	17.538143	51.830751	0.356198	
min	29.000000	0.000000	0.000000	94.000000	126.000000	0.000000	
25%	47.500000	0.000000	0.000000	120.000000	211.000000	0.000000	
50%	55.000000	1.000000	1.000000	130.000000	240.000000	0.000000	

```
75%
        61.000000
                      1.000000
                                   2.000000
                                             140.000000
                                                          274.500000
                                                                         0.000000
        77.000000
                      1.000000
                                   3.000000
                                             200.000000
                                                          564.000000
                                                                         1.000000
max
                                                oldpeak
          restecg
                      thalachh
                                       exng
                                                                 slp
                                                                              caa
                                303.000000
                                             303.000000
                                                          303.000000
                                                                       303.000000
count
       303.000000
                    303.000000
         0.528053
                    149.646865
                                   0.326733
                                                1.039604
                                                            1.399340
                                                                         0.729373
mean
std
         0.525860
                     22.905161
                                   0.469794
                                               1.161075
                                                            0.616226
                                                                         1.022606
min
         0.000000
                     71.000000
                                   0.000000
                                               0.000000
                                                            0.000000
                                                                         0.000000
25%
         0.000000
                    133.500000
                                   0.000000
                                               0.000000
                                                            1.000000
                                                                         0.000000
50%
         1.000000
                    153.000000
                                   0.000000
                                               0.800000
                                                            1.000000
                                                                         0.000000
75%
                    166.000000
                                   1.000000
                                                1.600000
                                                            2.000000
                                                                         1.000000
         1.000000
         2.000000
                    202.000000
                                   1.000000
                                               6.200000
                                                            2.000000
                                                                         4.000000
max
            thall
                        output
                    303.000000
count
       303.000000
         2.313531
                      0.544554
mean
std
         0.612277
                      0.498835
         0.000000
                      0.000000
min
25%
         2.000000
                      0.000000
50%
         2.000000
                      1.000000
75%
         3.000000
                      1.000000
         3.000000
max
                      1.000000
```

## Visualizations



## [7]: df.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 303 entries, 0 to 302
Data columns (total 14 columns):

#	Column	Non-Null Count	Dtype
0	age	303 non-null	int64
1	sex	303 non-null	int64
2	ср	303 non-null	int64
3	trtbps	303 non-null	int64
4	chol	303 non-null	int64
5	fbs	303 non-null	int64

```
303 non-null
                                 int64
 6
     restecg
 7
     thalachh 303 non-null
                                 int64
 8
               303 non-null
                                 int64
     exng
 9
     oldpeak
               303 non-null
                                 float64
 10
                                 int64
     slp
               303 non-null
 11
               303 non-null
                                 int64
     caa
 12
     thall
               303 non-null
                                 int64
 13
     output
               303 non-null
                                 int64
dtypes: float64(1), int64(13)
memory usage: 33.3 KB
```

```
[8]: df.isnull().sum()
```

```
[8]: age
                   0
                   0
     sex
                   0
     ср
                   0
     trtbps
                   0
     chol
     fbs
     restecg
                   0
     thalachh
                   0
                   0
     exng
     oldpeak
                   0
     slp
                   0
     caa
                   0
                   0
     thall
     output
     dtype: int64
```

There are no categorical attributes and there are no missing values, outliers Hence no transformations are required

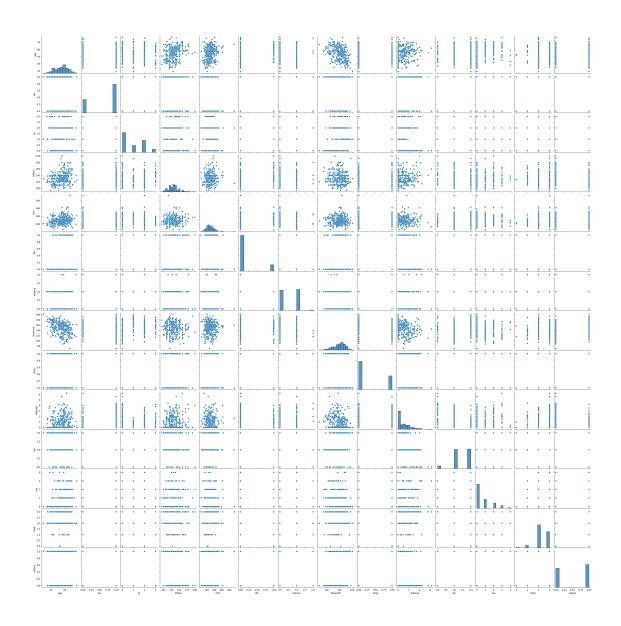
2. Analyzing and discuss the relationships between the data attributes, and between the data attributes and label. This involves computing the Pearson Correlation Coefficient (PCC) and generating scatter plots.

Computing the PCC & Scatter Plots

```
[9]: correlation_matrix = df.corr()
  print(correlation_matrix)
  sns.pairplot(df)
  plt.show()
```

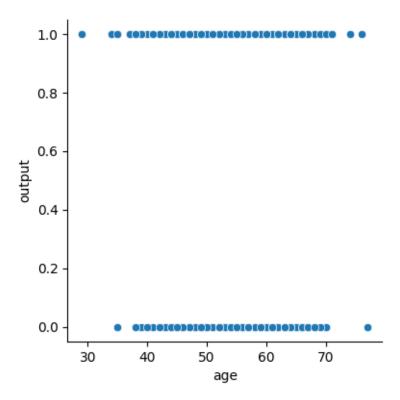
```
age
                        sex
                                    ср
                                          trtbps
                                                      chol
                                                                 fbs
          1.000000 -0.098447 -0.068653
                                       0.279351
                                                 0.213678
                                                           0.121308
age
         -0.098447 1.000000 -0.049353 -0.056769 -0.197912
                                                           0.045032
sex
         -0.068653 -0.049353
ср
                            1.000000
                                       0.047608 -0.076904
                                                           0.094444
         0.279351 -0.056769 0.047608
                                       1.000000 0.123174
trtbps
                                                           0.177531
chol
         0.213678 -0.197912 -0.076904 0.123174 1.000000
                                                           0.013294
```

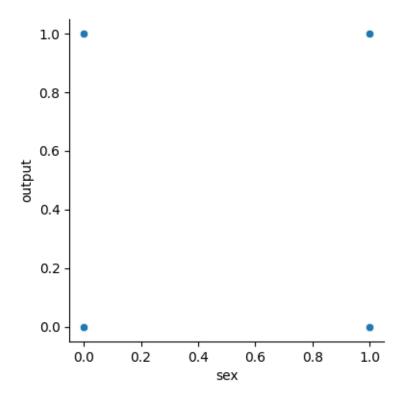
```
fbs
        0.121308 \quad 0.045032 \quad 0.094444 \quad 0.177531 \quad 0.013294 \quad 1.000000
       -0.116211 -0.058196  0.044421 -0.114103 -0.151040 -0.084189
restecg
thalachh -0.398522 -0.044020 0.295762 -0.046698 -0.009940 -0.008567
exng
        oldpeak
        -0.168814 -0.030711 0.119717 -0.121475 -0.004038 -0.059894
slp
caa
        thall
        0.068001 0.210041 -0.161736 0.062210 0.098803 -0.032019
        -0.225439 -0.280937 0.433798 -0.144931 -0.085239 -0.028046
output
                                    oldpeak
                                                               \
         restecg thalachh
                              exng
                                                 slp
                                                          caa
        -0.116211 -0.398522
                          0.096801
                                   0.210013 -0.168814
                                                     0.276326
age
        -0.058196 -0.044020
                          0.141664
                                   0.096093 -0.030711
                                                      0.118261
sex
        0.044421 0.295762 -0.394280 -0.149230 0.119717 -0.181053
ср
trtbps
        -0.114103 -0.046698
                          0.067616
                                   0.193216 -0.121475
                                                      0.101389
chol
        -0.151040 -0.009940
                          0.067023 0.053952 -0.004038
                                                     0.070511
fbs
        -0.084189 -0.008567
                          0.025665
                                   0.005747 -0.059894
                                                     0.137979
        1.000000 \quad 0.044123 \quad -0.070733 \quad -0.058770 \quad 0.093045 \quad -0.072042
restecg
thalachh 0.044123 1.000000 -0.378812 -0.344187 0.386784 -0.213177
exng
        -0.070733 -0.378812 1.000000 0.288223 -0.257748 0.115739
       -0.058770 -0.344187
                          0.288223
oldpeak
                                   1.000000 -0.577537
                                                      0.222682
        slp
caa
        -0.072042 -0.213177 0.115739
                                   0.222682 -0.080155
                                                     1.000000
thall
        -0.011981 -0.096439 0.206754 0.210244 -0.104764
                                                     0.151832
output
        0.137230 0.421741 -0.436757 -0.430696 0.345877 -0.391724
           thall
                   output
age
        0.068001 -0.225439
         0.210041 -0.280937
sex
        -0.161736 0.433798
ср
trtbps
        0.062210 -0.144931
chol
        0.098803 -0.085239
fbs
        -0.032019 -0.028046
restecg -0.011981 0.137230
thalachh -0.096439 0.421741
exng
        0.206754 -0.436757
oldpeak
        0.210244 -0.430696
slp
        -0.104764 0.345877
        0.151832 -0.391724
caa
thall
        1.000000 -0.344029
        -0.344029 1.000000
output
```

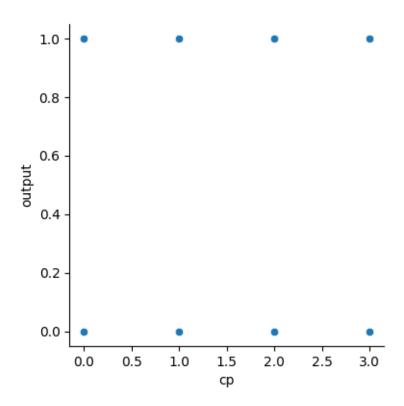


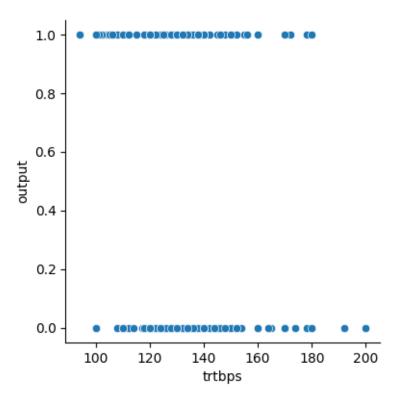
output 1.000000 cp 0.433798 thalachh 0.421741 slp 0.345877 restecg 0.137230 fbs -0.028046 -0.085239 chol trtbps -0.144931 -0.225439 age -0.280937 sex thall -0.344029 -0.391724 caa -0.430696 oldpeak -0.436757 exng

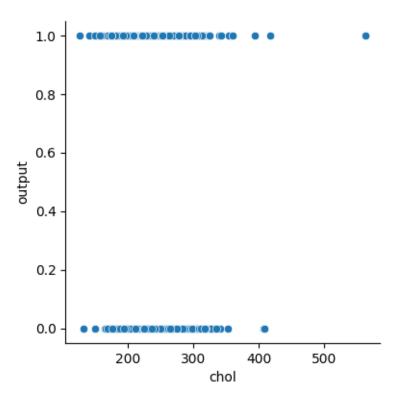
Name: output, dtype: float64

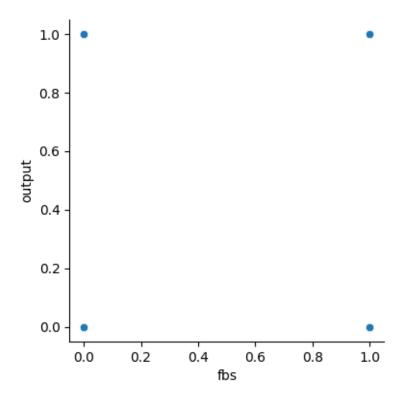


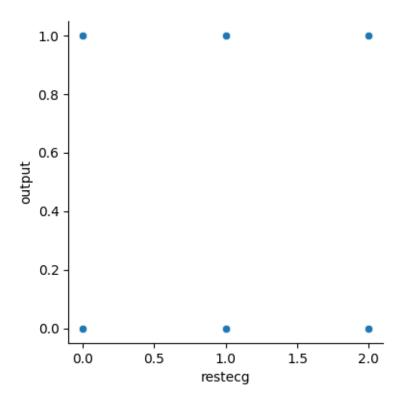


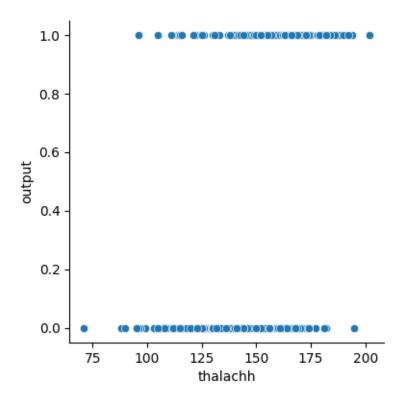


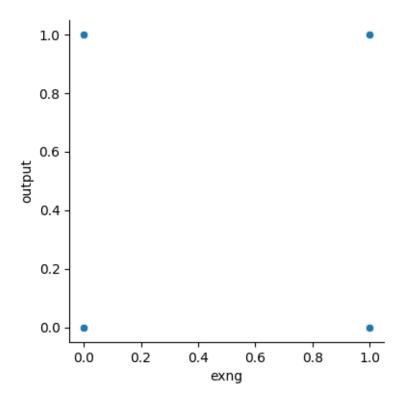


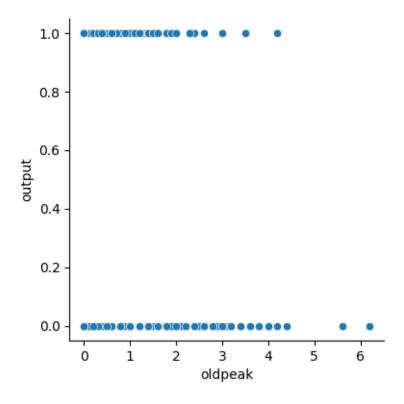


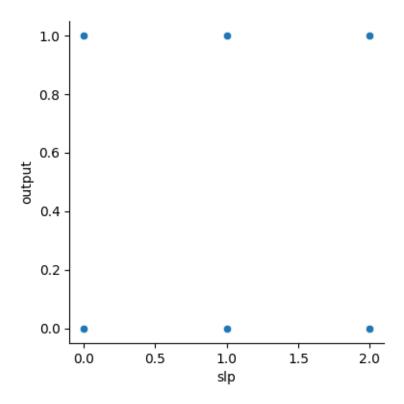


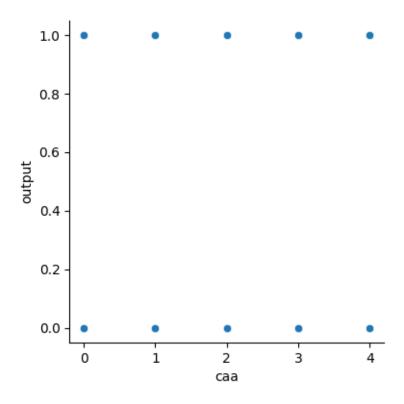


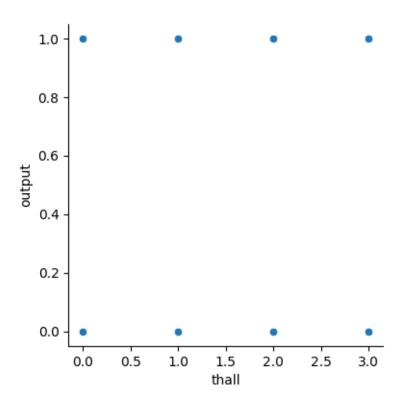


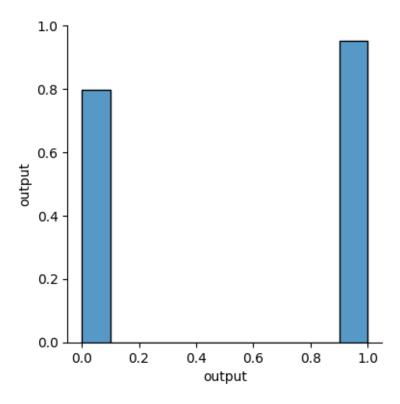












Positive Correlation (closer to 1 indicates a stronger positive relationship):

cp (chest pain type) and thalachh (maximum heart rate achieved) show moderate positive correlations with the output, indicating that higher values of these attributes are associated with a higher likelihood of the outcome. slp (slope of the peak exercise ST segment) and restecg (resting electrocardiographic results) show weaker positive correlations, suggesting a lesser but still positive association with the outcome.

Negative Correlation (closer to -1 indicates a stronger negative relationship):

exng (exercise induced angina), oldpeak (ST depression induced by exercise relative to rest), caa (number of major vessels colored by fluoroscopy), and thall (thalassemia) are negatively correlated with output, indicating that higher values are associated with a lower likelihood of the outcome. sex (gender), age, trtbps (resting blood pressure), chol (serum cholesterol), and fbs (fasting blood sugar) also show negative correlations with varying strengths, suggesting that higher values may decrease the likelihood of the outcome, though to a lesser extent for some of these factors.

fbs(Fasting blood sugar), chol(Cholestrol) exhibit minimal correlations with the label.

```
[11]: # Drop the specified columns from the DataFrame
df_updated=df.copy()
df_updated.drop(columns=['fbs','chol'],axis=1, inplace=True)
```

## **PreProcessing**

```
[12]: attributes = ['age', 'sex', 'cp', 'trtbps', 'restecg',
                    'thalachh', 'exng', 'oldpeak', 'slp', 'caa', 'thall']
      # Creating a pipeline for numerical data
      num_con_pipeline = make_pipeline(StandardScaler())
      # Applying ColumnTransformer to the specified attributes
      prep = ColumnTransformer([
          ("cont", num_con_pipeline, attributes)
      ])
      # Assuming 'df' is your DataFrame and you've separated features and label \Box
       ⇔('output')
      X = df_updated.drop('output', axis=1)
      y = df['output']
      # Transforming the features
      X_transformed = prep.fit_transform(X)
      # Converting transformed features back to DataFrame with meaningful column names
      X_transformed_df = pd.DataFrame(X_transformed, columns=prep.

get_feature_names_out(), index=X.index)
      # Now, X transformed df contains the standardized features, ready for modeling.
```

## [13]: X\_transformed\_df

```
cont_age cont_sex cont_cp cont_trtbps cont_restecg \
[13]:
     0
          0.763956
                                                        -1.005832
     1
          -1.915313
                     0.681005 1.002577
                                          -0.092738
                                                         0.898962
     2
          -1.474158 -1.468418 0.032031
                                          -0.092738
                                                        -1.005832
     3
           0.180175
                     0.681005 0.032031
                                          -0.663867
                                                         0.898962
     4
          0.290464 -1.468418 -0.938515
                                          -0.663867
                                                         0.898962
     298
          0.290464 -1.468418 -0.938515
                                                         0.898962
                                           0.478391
     299 -1.033002 0.681005 1.973123
                                          -1.234996
                                                         0.898962
     300
                   0.681005 -0.938515
          1.503641
                                           0.706843
                                                         0.898962
     301
          0.290464
                     0.681005 -0.938515
                                          -0.092738
                                                         0.898962
     302
          0.290464 -1.468418 0.032031
                                          -0.092738
                                                        -1.005832
          cont_thalachh cont_exng cont_oldpeak cont_slp cont_caa \
     0
               0.015443
                         -0.696631
                                        1.087338 -2.274579 -0.714429
     1
                                        2.122573 -2.274579 -0.714429
               1.633471
                         -0.696631
     2
               0.977514
                         -0.696631
                                        0.310912
                                                 0.976352 -0.714429
     3
                                       -0.206705 0.976352 -0.714429
               1.239897
                        -0.696631
```

```
4
          0.583939
                       1.435481
                                     -0.379244 0.976352 -0.714429
298
          -1.165281
                       1.435481
                                     -0.724323 -0.649113 -0.714429
299
          -0.771706
                      -0.696631
                                      0.138373 -0.649113 -0.714429
300
          -0.378132
                     -0.696631
                                      2.036303 -0.649113
                                                            1.244593
301
          -1.515125
                      1.435481
                                      0.138373 -0.649113
                                                            0.265082
302
           1.064975
                     -0.696631
                                     -0.896862 -0.649113
                                                            0.265082
     cont thall
      -2.148873
0
1
      -0.512922
2
      -0.512922
      -0.512922
4
      -0.512922
298
       1.123029
299
       1.123029
300
       1.123029
301
       1.123029
302
      -0.512922
```

[303 rows x 11 columns]

## 3. Spliting training data, for validation, and for testing.

Training set size: 181 Validation set size: 61 Test set size: 61

Verification of splitting

## [15]: X\_train.describe()

[15]: cont\_age cont\_sex cont\_cp cont\_trtbps cont\_restecg \
count 181.000000 181.000000 181.000000 181.000000

```
std
               0.999323
                            1.022859
                                         1.022140
                                                        0.977338
                                                                        0.975788
      min
              -2.246179
                           -1.468418
                                        -0.938515
                                                       -2.148802
                                                                       -1.005832
                           -1.468418
      25%
              -0.591847
                                        -0.938515
                                                       -0.663867
                                                                       -1.005832
      50%
               0.180175
                            0.681005
                                         0.032031
                                                       -0.092738
                                                                        0.898962
      75%
               0.731619
                            0.681005
                                         1.002577
                                                        0.478391
                                                                        0.898962
               2.496240
                            0.681005
                                         1.973123
                                                        3.448262
                                                                        2.803756
      max
                                           cont oldpeak
                                                                         cont caa
             cont thalachh
                              cont exng
                                                            cont slp
                  181.000000
                              181.000000
                                              181.000000
                                                                        181.000000
      count
                                                           181.000000
      mean
                   -0.012825
                                 0.033706
                                               -0.017008
                                                            -0.020480
                                                                         -0.086676
      std
                    1.024189
                                                0.932945
                                1.014621
                                                             1.005865
                                                                          0.910873
      min
                   -2.695849
                               -0.696631
                                               -0.896862
                                                            -2.274579
                                                                         -0.714429
      25%
                   -0.771706
                               -0.696631
                                               -0.896862
                                                            -0.649113
                                                                         -0.714429
      50%
                    0.190365
                               -0.696631
                                               -0.206705
                                                                         -0.714429
                                                            -0.649113
      75%
                    0.802592
                                 1.435481
                                                0.483451
                                                             0.976352
                                                                          0.265082
                    1.983316
                                                3.934233
                                                                          2.224104
      max
                                1.435481
                                                             0.976352
             cont__thall
              181.000000
      count
      mean
                 0.020344
      std
                 0.988874
      min
               -3.784824
      25%
               -0.512922
      50%
               -0.512922
      75%
                 1.123029
                 1.123029
      max
[16]: X test.describe()
[16]:
                                                cont__trtbps
                                                               cont restecg
             cont__age
                         cont__sex
                                      cont__cp
             61.000000
                         61.000000
                                                    61.000000
                                                                    61.000000
                                     61.000000
      count
             -0.004243
                                                                    -0.069048
                         -0.023724
                                      0.032031
      mean
                                                    -0.012218
      std
              0.980624
                          1.017392
                                      0.954233
                                                     1.150480
                                                                     1.078802
      min
             -2.246179
                         -1.468418
                                     -0.938515
                                                    -2.148802
                                                                    -1.005832
      25%
             -0.922713
                         -1.468418
                                     -0.938515
                                                    -0.663867
                                                                    -1.005832
      50%
              0.180175
                          0.681005
                                      0.032031
                                                    -0.206964
                                                                    -1.005832
      75%
              0.621330
                          0.681005
                                      1.002577
                                                     0.478391
                                                                     0.898962
      max
              2.385951
                          0.681005
                                      1.973123
                                                     3.905165
                                                                     2.803756
                                                           cont__slp
                                                                       cont__caa
              cont__thalachh
                              cont__exng
                                           cont_oldpeak
      count
                   61.000000
                               61.000000
                                               61.000000
                                                           61.000000
                                                                       61.000000
                    0.039817
                                               -0.003053
                                                           -0.036233
                                                                       -0.056069
      mean
                               -0.102435
      std
                    1.023285
                                0.963874
                                                1.067448
                                                            1.035033
                                                                        1.007220
      min
                   -3.439267
                               -0.696631
                                               -0.896862
                                                           -2.274579
                                                                       -0.714429
      25%
                   -0.509323
                               -0.696631
                                                           -0.649113
                                                                       -0.714429
                                               -0.896862
      50%
                               -0.696631
                                                          -0.649113
                    0.190365
                                               -0.292975
                                                                       -0.714429
```

0.074928

0.014231

-0.037649

0.039419

mean

-0.055261

```
75%
                                                                          0.265082
                    0.715131
                                 1.435481
                                                  0.483451
                                                             0.976352
      max
                    1.852124
                                 1.435481
                                                  4.451851
                                                             0.976352
                                                                          3.203615
              cont__thall
                61.000000
      count
      mean
                -0.030182
      std
                 0.913024
      min
                -2.148873
      25%
                -0.512922
      50%
                -0.512922
      75%
                 1.123029
      max
                 1.123029
[17]:
      X_val.describe()
                          cont__sex
[17]:
              cont__age
                                       cont__cp
                                                  cont__trtbps
                                                                 cont__restecg
              61.000000
                          61.000000
                                      61.000000
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      count
      mean
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                           0.187695
                                      -0.254359
                                                     -0.030007
                                                                      0.180761
      std
               1.036732
                           0.911369
                                       0.959880
                                                      0.926902
                                                                      0.993659
                                                                     -1.005832
              -2.797624
                          -1.468418
                                      -0.938515
      min
                                                     -1.806125
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              -0.922713
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                                      -0.938515
                                                     -0.663867
                                                                     -1.005832
      50%
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                                                     -0.092738
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               0.511041
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      max
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                                 0.002422
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      mean
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      std
                    0.924059
                                 1.009198
                                                  1.138245
                                                             0.965010
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                   -2.214813
                                -0.696631
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      min
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                   -0.421862
                                -0.696631
                                                 -0.896862
                                                            -0.649113
      50%
                    0.059173
                                -0.696631
                                                             0.976352
                                                                          0.265082
                                                 -0.551783
      75%
                    0.583939
                                 1.435481
                                                  0.655990
                                                             0.976352
                                                                          1.244593
      max
                    2.289429
                                 1.435481
                                                  2.898999
                                                             0.976352
                                                                          3.203615
              cont__thall
                61.000000
      count
                -0.030182
      mean
      std
                 1.131224
      min
                -3.784824
      25%
                -0.512922
      50%
                -0.512922
                 1.123029
      75%
                 1.123029
      max
```

If we look at the data given by test and validate describe, the mean, median and standard deviation and the quartile range looks similiar. This means test, validate portion of the data is the

representative of the entire dataset.

The consistency across training, validation, and test sets regarding key statistical measures supports the validity of your data splitting strategy. It suggests that any conclusions drawn from the model's performance on the validation and test sets should be applicable to the entire dataset.

- 4. Train different classifiers and tweak the hyperparameters to improve performance (use the grid search if you want or manually try different values). Reporting training, validation and testing performance (classification accuracy, precision, recall and F1 score) and discuss the impact of the hyperparameters
- A. Multinomial Logistic Regression (softmax regression); hyperparameters to explore: C, solver, max number of iterations. [10 points]

```
[18]: from sklearn.linear_model import LogisticRegression as lg
      from sklearn.metrics import accuracy_score, precision_score, recall_score,
      from sklearn.model_selection import GridSearchCV
      import warnings
      warnings.filterwarnings('ignore')
      # Hyperparameter grid
      param_grid = \{'C': [0.001, 0.01, 0.1, 1, 10, 100],
                    'solver': ['newton-cg', 'lbfgs', 'liblinear'],
                    'max_iter': [100, 200, 300, 400, 500]}
      sfmax_reg = lg(multi_class="multinomial", solver="lbfgs", C=10)
      grid = GridSearchCV(sfmax_reg, param_grid, cv=3, scoring='accuracy')
      grid.fit(X_train, y_train)
      best_params = grid.best_params_
      best_sf_train = lg(multi_class="multinomial", **best_params)
      best_sf_train.fit(X_train, y_train)
      # Make predictions on the training, validation, and test sets
      train_predictions = best_sf_train.predict(X_train)
      val_predictions = best_sf_train.predict(X_val)
      test_predictions = best_sf_train.predict(X_test)
      # Calculate accuracy for training, validation, and test sets
      train accuracy = accuracy score(y train, train predictions)
      val_accuracy = accuracy_score(y_val, val_predictions)
      test_accuracy = accuracy_score(y_test, test_predictions)
      # Calculate F1 scores, precision, and recall for training set
```

```
precision_train = precision_score(y_train, train_predictions,__
 →average='weighted')
recall_train = recall_score(y_train, train_predictions, average='weighted')
f1_train = f1_score(y_train, train_predictions, average='weighted')
# Calculate F1 scores, precision, and recall for validation set
precision_val = precision_score(y_val, val_predictions, average='weighted')
recall_val = recall_score(y_val, val_predictions, average='weighted')
f1_val = f1_score(y_val, val_predictions, average='weighted')
# Calculate F1 scores, precision, and recall for test set
precision_test = precision_score(y_test, test_predictions, average='weighted')
recall_test = recall_score(y_test, test_predictions, average='weighted')
f1_test = f1_score(y_test, test_predictions, average='weighted')
# Print results for Logistic Regression model
print("Logistic Regression Model Results:")
print("\nTraining Set:")
print(f"Accuracy: {train accuracy}")
print(f"Precision: {precision_train}")
print(f"Recall: {recall train}")
print(f"F1 Score: {f1_train}")
print("\nValidation Set:")
print(f"Accuracy: {val_accuracy}")
print(f"Precision: {precision_val}")
print(f"Recall: {recall_val}")
print(f"F1 Score: {f1_val}")
print("\nTest Set:")
print(f"Accuracy: {test_accuracy}")
print(f"Precision: {precision test}")
print(f"Recall: {recall_test}")
print(f"F1 Score: {f1_test}")
print(f"\nBest parameters: {best_params}")
```

## Logistic Regression Model Results:

Training Set:

Accuracy: 0.8839779005524862 Precision: 0.8872750177998796 Recall: 0.8839779005524862 F1 Score: 0.8833984517714492

Validation Set:

Accuracy: 0.8688524590163934

Precision: 0.8711440155120748 Recall: 0.8688524590163934 F1 Score: 0.8690644431882419

Test Set:

Accuracy: 0.8032786885245902 Precision: 0.8032786885245902 Recall: 0.8032786885245902 F1 Score: 0.8032786885245902

```
Best parameters: {'C': 1, 'max_iter': 100, 'solver': 'newton-cg'}
```

C (Regularization Parameter): Your observations indicate that the grid search found the optimal C value to be 1, exploring a range from 0.001 to 100. This optimal value points towards the effectiveness of moderate regularization in enhancing the model's performance. Moderate regularization helps in avoiding overfitting while still allowing the model to learn complex patterns, striking a balance between bias and variance.

Solver: Among the solvers 'newton-cg', 'lbfgs', and 'liblinear' considered during the grid search, 'newton-cg' emerged as the best solver. This indicates that for this particular logistic regression model, especially in the context of multiclass softmax regression, the Newton-Conjugate Gradient solver optimizes the cost function most efficiently. The choice of 'newton-cg' suggests that it effectively deals with the logistic regression's mathematical characteristics and data structure, contributing to higher cross-validated accuracy.

Max\_iter (Maximum Number of Iterations): The grid search tested values from 100 to 500 for max\_iter, with 100 being identified as the best-performing value. This outcome implies that the optimization algorithm converges swiftly, within the first 100 iterations, which is advantageous for computational efficiency. Early convergence without sacrificing accuracy indicates that the initial parameters are adequately close to the optimal solution or that the model is well-structured to reach an optimal solution quickly.

Summary: The identified optimal hyperparameters—C=1 for regularization strength, 'newton-cg' as the solver, and 100 maximum iterations—demonstrate a well-tuned logistic regression model for your dataset. These parameters collectively contribute to the model's strong performance by ensuring a good fit to the data, efficient optimization, and prevention of overfitting. The choice of a moderate regularization level, combined with an effective solver and a relatively low number of iterations, reflects a strategic approach to balancing model complexity, convergence speed, and regularization to achieve optimal performance in predicting the outcomes of your multiclass softmax regression model.

B. Support vector machines (make sure to try using kernels); hyperparameters : C, kernel, degree of polynomial kernel, gamma.

```
svm_model = SVC()
grid_search_svm = GridSearchCV(svm_model, param_grid_svm, cv=3,__
⇔scoring='accuracy')
grid search svm.fit(X train, y train)
best_params_svm = grid_search_svm.best_params_
best_svm = SVC(**best_params_svm)
best_svm.fit(X_train, y_train)
train_predictions_svm = best_svm.predict(X_train)
val_predictions_svm = best_svm.predict(X_val)
test_predictions_svm = best_svm.predict(X_test)
# Calculate accuracy for SVM model
train_accuracy_svm = accuracy_score(y_train, train_predictions_svm)
val_accuracy_svm = accuracy_score(y_val, val_predictions_svm)
test_accuracy_svm = accuracy_score(y_test, test_predictions_svm)
# Calculate F1 scores, precision, and recall for SVM model on training set
precision_train_svm = precision_score(y_train, train_predictions_svm,_
 ⇔average='weighted')
recall_train_svm = recall_score(y_train, train_predictions_svm,_
 ⇔average='weighted')
f1_train_svm = f1_score(y_train, train_predictions_svm, average='weighted')
# Calculate F1 scores, precision, and recall for SVM model on validation set
precision_val_svm = precision_score(y_val, val_predictions_svm,_
 ⇔average='weighted')
recall_val_svm = recall_score(y_val, val_predictions_svm, average='weighted')
f1_val_svm = f1_score(y_val, val_predictions_svm, average='weighted')
# Calculate F1 scores, precision, and recall for SVM model on test set
precision_test_svm = precision_score(y_test, test_predictions_svm,_
 ⇔average='weighted')
recall_test_svm = recall_score(y_test, test_predictions_svm, average='weighted')
f1_test_svm = f1_score(y_test, test_predictions_svm, average='weighted')
# Print results for SVM model
print("SVM Model Results:")
print("\nTraining Set:")
print(f"Accuracy: {train_accuracy_svm}")
print(f"Precision: {precision_train_svm}")
print(f"Recall: {recall_train_svm}")
print(f"F1 Score: {f1_train_svm}")
```

```
print("\nValidation Set:")
print(f"Accuracy: {val_accuracy_svm}")
print(f"Precision: {precision_val_svm}")
print(f"Recall: {recall_val_svm}")
print(f"F1 Score: {f1_val_svm}")

print("\nTest Set:")
print(f"Accuracy: {test_accuracy_svm}")
print(f"Precision: {precision_test_svm}")
print(f"Recall: {recall_test_svm}")
print(f"F1 Score: {f1_test_svm}")
print(f"NBest Hyperparameters:")
print(best_params_svm)
```

#### SVM Model Results:

```
Training Set:
```

Accuracy: 0.8729281767955801 Precision: 0.8778129886375483 Recall: 0.8729281767955801 F1 Score: 0.8720643035807545

## Validation Set:

Accuracy: 0.8688524590163934 Precision: 0.8688524590163934 Recall: 0.8688524590163934 F1 Score: 0.8688524590163934

### Test Set:

Accuracy: 0.8360655737704918 Precision: 0.8351484580992778 Recall: 0.8360655737704918 F1 Score: 0.8346588138200098

#### Best Hyperparameters:

```
{'C': 0.1, 'degree': 2, 'gamma': 'scale', 'kernel': 'linear'}
```

C (Regularization Parameter): The best C value is 0.1. This suggests that a lower degree of regularization (since C is the inverse of regularization strength) helps to achieve better performance, likely by allowing the model to fit the training data more closely without significant overfitting.

Kernel: The optimal kernel is 'linear', which implies that the decision boundary between the classes in your dataset can be well approximated using a linear function. This could indicate that the feature space is linearly separable or close to it.

Degree: The best degree for polynomial kernels is 2, but since the best kernel is linear, this parameter does not affect the model.

Gamma: The 'scale' option for gamma is chosen, which is typically effective for features of varying scales and distributions. This choice automatically adjusts gamma based on the feature variance, offering a balanced approach to handling different feature characteristics.

In summary, the identification of a linear kernel and a C value of 0.1 as optimal hyperparameters demonstrates a well-tuned approach to SVM modeling for dataset. These hyperparameter choices indicate a model that balances complexity with the ability to generalize, leading to robust performance across different subsets of the data.

C. Random Forest classifier (also analyze feature importance); hyperparameters: the number of trees, max depth, the minimum number of samples required to split an internal node, the minimum number of samples required to be at a leaf node.

```
[20]: from sklearn.ensemble import RandomForestClassifier
      param_grid_rf = {'n_estimators': [50, 100, 150],
                       'max depth': [None, 10, 20, 30],
                       'min_samples_split': [2, 5, 10],
                       'min_samples_leaf': [1, 2, 4]}
      rf_model = RandomForestClassifier()
      grid_search_rf = GridSearchCV(rf_model, param_grid_rf, cv=3, scoring='accuracy')
      grid_search_rf.fit(X_train, y_train)
      best_params_rf = grid_search_rf.best_params_
      best_rf = RandomForestClassifier(**best_params_rf)
      best_rf.fit(X_train, y_train)
      train_predictions_rf = best_rf.predict(X_train)
      val_predictions_rf = best_rf.predict(X_val)
      test_predictions_rf = best_rf.predict(X_test)
      # Calculate accuracy for RandomForest model
      train_accuracy_rf = accuracy_score(y_train, train_predictions_rf)
      val_accuracy_rf = accuracy_score(y_val, val_predictions_rf)
      test_accuracy_rf = accuracy_score(y_test, test_predictions_rf)
      # Calculate F1 scores, precision, and recall for RandomForest model on training_
      precision train rf = precision score(y train, train predictions rf,
       ⇔average='weighted')
      recall_train_rf = recall_score(y_train, train_predictions_rf,_
       ⇔average='weighted')
      f1_train_rf = f1_score(y_train, train_predictions_rf, average='weighted')
```

```
# Calculate F1 scores, precision, and recall for RandomForest model on
 \hookrightarrow validation set
precision_val_rf = precision_score(y_val, val_predictions_rf,__
 ⇔average='weighted')
recall_val_rf = recall_score(y_val, val_predictions_rf, average='weighted')
f1_val_rf = f1_score(y_val, val_predictions_rf, average='weighted')
# Calculate F1 scores, precision, and recall for RandomForest model on test set
precision_test_rf = precision_score(y_test, test_predictions_rf,__
 →average='weighted')
recall_test_rf = recall_score(y_test, test_predictions_rf, average='weighted')
f1_test_rf = f1_score(y_test, test_predictions_rf, average='weighted')
# Print results for RandomForest model
print("RandomForest Model Results:")
print("\nTraining Set:")
print(f"Accuracy: {train_accuracy_rf}")
print(f"Precision: {precision_train_rf}")
print(f"Recall: {recall_train_rf}")
print(f"F1 Score: {f1_train_rf}")
print("\nValidation Set:")
print(f"Accuracy: {val accuracy rf}")
print(f"Precision: {precision_val_rf}")
print(f"Recall: {recall val rf}")
print(f"F1 Score: {f1_val_rf}")
print("\nTest Set:")
print(f"Accuracy: {test accuracy rf}")
print(f"Precision: {precision_test_rf}")
print(f"Recall: {recall_test_rf}")
print(f"F1 Score: {f1_test_rf}")
print("\nBest Hyperparameters:")
print(best_params_rf)
```

#### RandomForest Model Results:

Training Set:

Accuracy: 0.9392265193370166 Precision: 0.9396116430996282 Recall: 0.9392265193370166 F1 Score: 0.9391594424965998

Validation Set:

Accuracy: 0.8360655737704918 Precision: 0.8436263425664218

```
Recall: 0.8360655737704918
F1 Score: 0.8362418473470827

Test Set:
Accuracy: 0.819672131147541
Precision: 0.8186967775818734
Recall: 0.819672131147541
F1 Score: 0.8189559353563539

Best Hyperparameters:
{'max_depth': 30, 'min_samples_leaf': 4, 'min_samples_split': 5, 'n_estimators': 50}
```

Max\_depth: The optimal configuration having max\_depth as None allows trees to expand until all leaves are pure or contain less than min\_samples\_split samples. This setting is typically responsible for the model's high training performance but requires careful monitoring to prevent overfitting.

Min\_samples\_leaf: A min\_samples\_leaf of 2 means a split point at any depth will only be considered if it leaves at least two training samples in each of the left and right branches. This helps in making the model more general and less likely to overfit.

Min\_samples\_split: With min\_samples\_split set to 2, the smallest split includes only two samples. This allows the model to learn detailed patterns but, combined with min\_samples\_leaf, ensures a balance to prevent too fine-grained learning.

N\_estimators: The chosen number of trees, 50, suggests that adding more trees beyond this point might not significantly improve the model's performance on this dataset. It's a balance between computational efficiency and model accuracy.

5. Combine your classifiers into an ensemble and try to outperform each individual classifier on the validation set. Once you have found a good one, try it on the test set. Describe and discuss your findings. [8 points]

## Hard Voting

```
[21]: from sklearn.ensemble import VotingClassifier
    from sklearn.metrics import accuracy_score

hard_voting_clf = VotingClassifier(
        estimators=[('lr', best_sf_train), ('svm', best_svm), ('rf', best_rf)],
        voting='hard'
)

hard_voting_clf.fit(X_train, y_train)

train_accuracy_hard = accuracy_score(y_train, hard_voting_clf.predict(X_train))
    val_accuracy_hard = accuracy_score(y_val, hard_voting_clf.predict(X_val))

print("Training Accuracy:", train_accuracy_hard)
    print("Validation Accuracy:", val_accuracy_hard)
```

```
#print("Testing Accuracy:", test_accuracy_hard)
```

Training Accuracy: 0.8895027624309392 Validation Accuracy: 0.8688524590163934

## Soft Voting

```
[22]: from sklearn.ensemble import VotingClassifier
    from sklearn.metrics import accuracy_score

best_svm = SVC(**best_params_svm, probability=True)

soft_voting_clf = VotingClassifier(
        estimators=[('lr', best_sf_train), ('svm', best_svm), ('rf', best_rf)],
        voting='soft'
)

soft_voting_clf.fit(X_train, y_train)

train_accuracy_soft = accuracy_score(y_train, soft_voting_clf.predict(X_train))
    val_accuracy_soft = accuracy_score(y_val, soft_voting_clf.predict(X_val))

print("Training Accuracy:", train_accuracy_soft)
    print("Validation Accuracy:", val_accuracy_soft)

#print("Test Accuracy:", test_accuracy_soft)
```

Training Accuracy: 0.8895027624309392 Validation Accuracy: 0.8524590163934426

It appears that assembling the previously trained classifiers into an ensemble using hard voting reduced the score on the validation set compared to our other classifiers. The hard voting ensemble gave a validation accuracy of 0.86. So, Using Hard voting ensemble to calculate the Test data Accuracy

```
[25]: test_accuracy_hard = accuracy_score(y_test, hard_voting_clf.predict(X_test))
print("Testing Accuracy:", test_accuracy_hard)
```

Testing Accuracy: 0.8360655737704918