

Classification of Handwritten digits

Pseudocode

Pre-Requisites:

- **Pandas:** A powerful and flexible library for data manipulation and analysis, providing high-performance data structures like the DataFrame.
- **NumPy:** The fundamental library for scientific computing in Python, providing a high-performance multidimensional array object and tools for working with these arrays.
- **Matplotlib.pyplot:** A plotting library that provides a MATLAB-like interface for creating a wide variety of static, animated, and interactive visualizations

Function Definition:

Model Definition (DNN Class)

- **Initialize DNN:**
 - Store layer sizes.
 - Create weight matrices for each layer with random values, including bias weights.
- **Sigmoid Function:**
 - Calculate $1 / (1 + \exp(-\text{input} * 0.01))$.
- **Predict Function:**
 - Take input data.
 - For each layer:
 - Add a bias term to the input.
 - Calculate the weighted sum of inputs.
 - Apply the sigmoid function.
 - Return the output of the last layer.

- **Train Function:**

- Take input data and true label.
- Perform a forward pass (using steps similar to predict) to get the output and intermediate layer outputs.
- Calculate the error at the output layer.
- Perform backpropagation to calculate gradients for each weight matrix.
- Update weights using gradients and a learning rate.
- Return the calculated error.

Main Code Execution:

Data Loading and Preprocessing

- Load training data (images and labels) from mnist_train_small.csv.
- Normalize image pixel values to be between 0 and 1.
- One-hot encode the labels.
- Load test data (images and labels) from mnist_test.csv.
- Normalize test image pixel values.

3. Model Training

- Create a DNN model instance with specified layer sizes.
- Initialize a queue to track recent errors.
- Loop for a specified number of training steps:
 - Randomly select a training sample and its corresponding encoded label.
 - Train the model using the selected sample and label.
 - Add the calculated error to the error queue.
 - Periodically (e.g., every 1000 steps):
 - Print the current step and average error from the queue.
 - Display the image of the training sample.
 - Print the model's prediction for the training sample.

4. Model Testing

- Initialize a counter for correct predictions.
- Loop through each sample in the test data:
 - Get the model's prediction for the test image.
 - Compare the prediction to the true label.
 - If the prediction is correct, increment the counter.
- Calculate the percentage of correct predictions.
- Print the percentage of correct predictions.

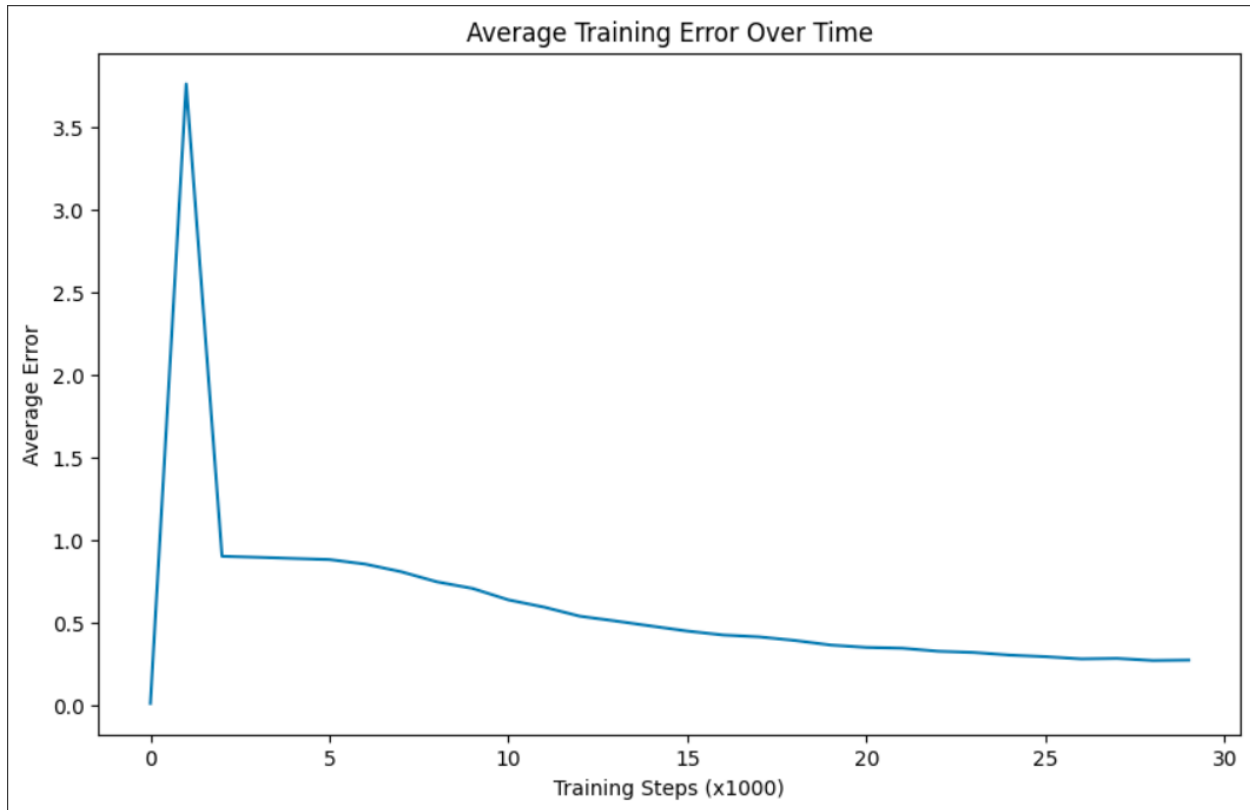
Comparision [Increase in Neurons]:

[C] - Code Execution as-is from the article: Here is the error percentage for every 1000 steps:

Step	Average Error
0	0.0085422
1000	1.407
2000	0.898235
3000	0.897382
4000	0.892662
5000	0.88387
6000	0.867767
7000	0.8378
8000	0.779796
9000	0.743291
10000	0.692835
11000	0.653548
12000	0.583941
13000	0.56098
14000	0.509175
15000	0.478133

16000	0.469609
17000	0.455497
18000	0.426183
19000	0.382638
20000	0.382546
21000	0.340882
22000	0.34964
23000	0.335699
24000	0.335802
25000	0.335712
26000	0.314881
27000	0.289233
28000	0.27962
29000	0.270752

Percentage of Correct Prediction: 88.06%

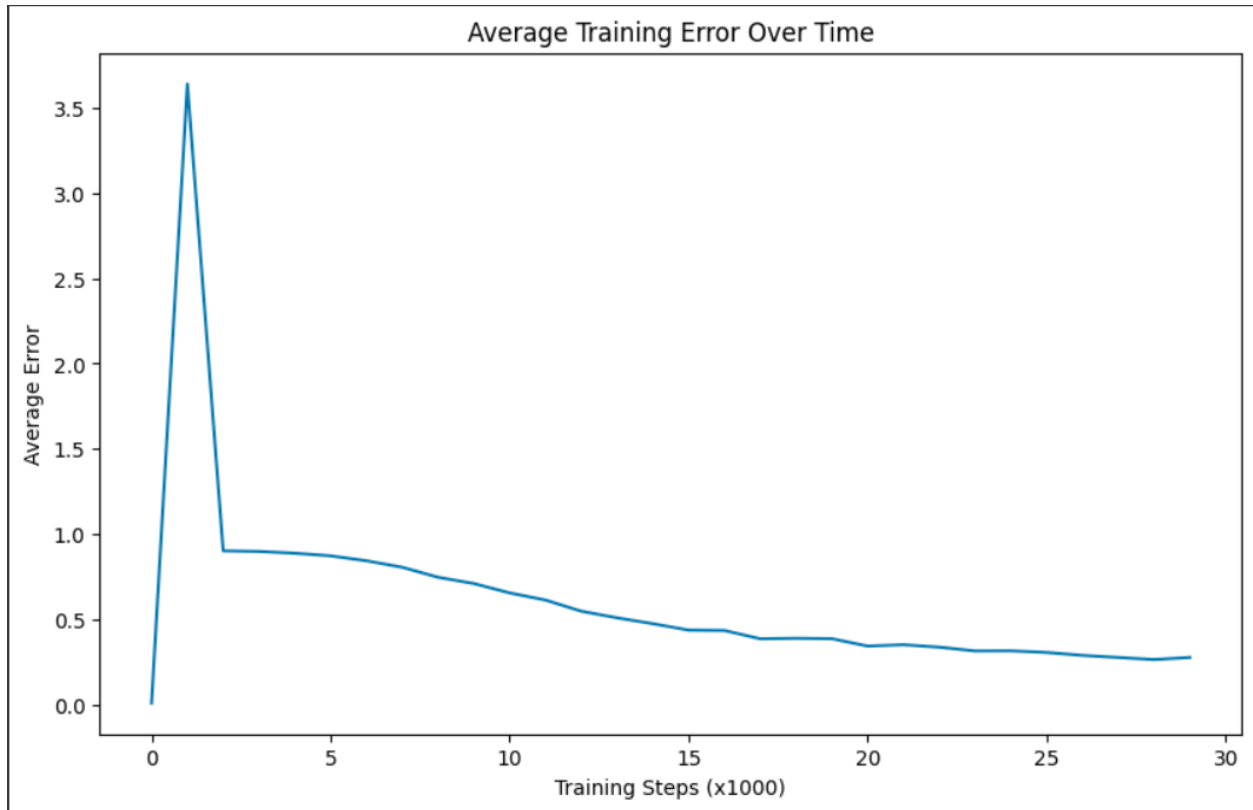


[D] - Neurons increased from 1250 to 2000 and below is the error rate per 1000 steps:

Step	Average Error
0	0.008959
1000	3.639592
2000	0.901995
3000	0.898259
4000	0.887977
5000	0.872487
6000	0.843606
7000	0.805622
8000	0.746954
9000	0.710006
10000	0.655241
11000	0.613281
12000	0.547981
13000	0.509071

14000	0.474802
15000	0.437017
16000	0.43482
17000	0.386118
18000	0.389009
19000	0.386681
20000	0.343399
21000	0.351219
22000	0.337011
23000	0.314855
24000	0.315485
25000	0.306064
26000	0.288852
27000	0.276523
28000	0.264435
29000	0.276673

Percentage of Correct Prediction: 87.59%



Conclusion:

Increasing the number of neurons in the hidden layers from 1250 to 2000 did not improve the network's performance. The observation is that performance degraded, going from 88.06% to 87.59%.

References:

1. **Kaggle.** (2018). **MNIST in CSV.** Retrieved from <https://www.kaggle.com/datasets/oddrational/mnist-in-csv>