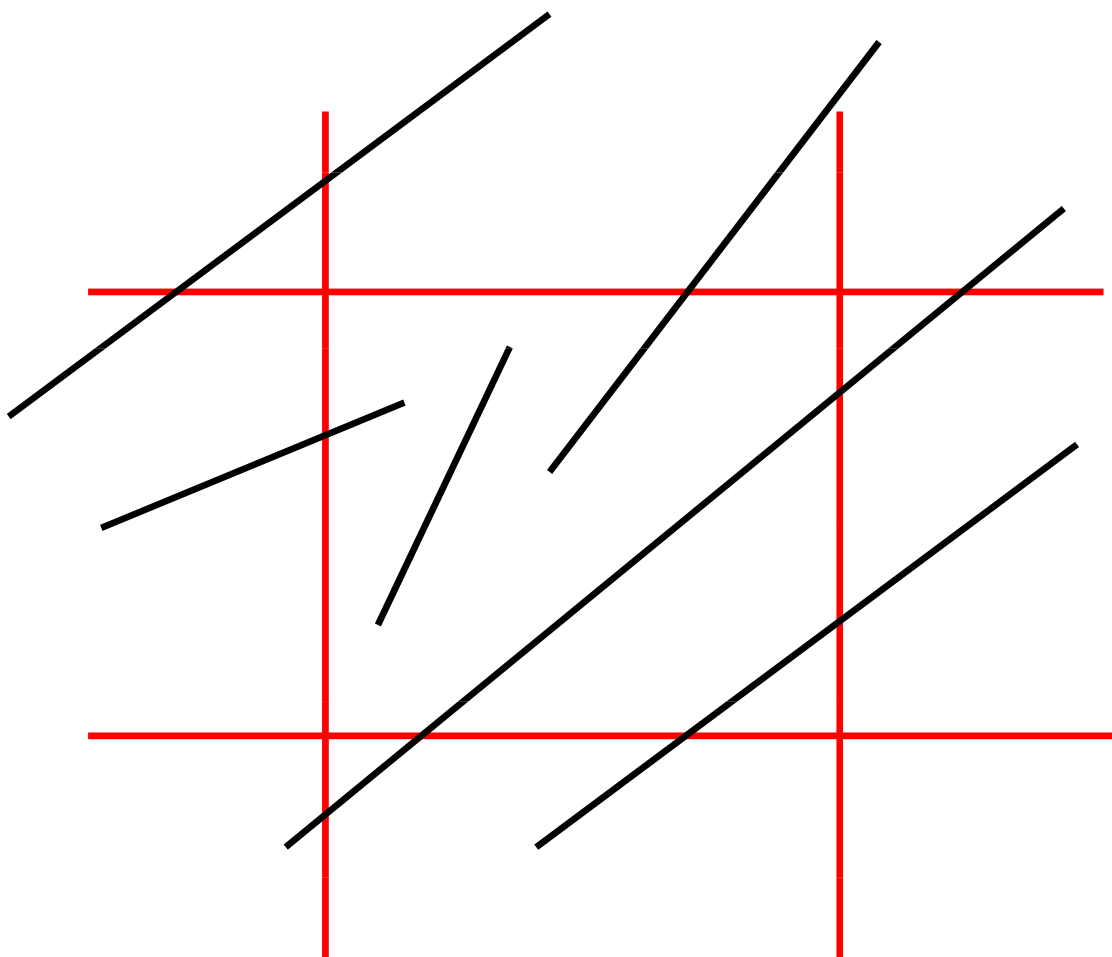


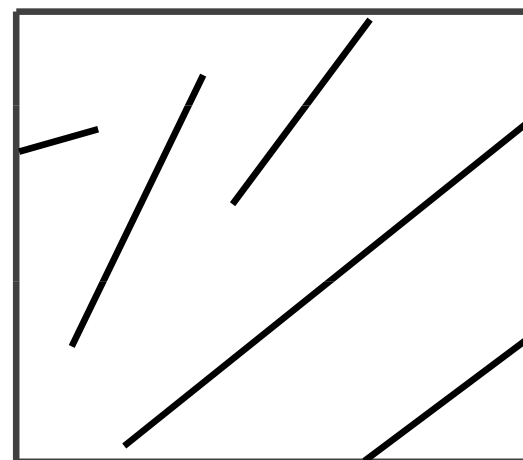
CLIPPING:

LINES and POLYGONS



INPUT

OUTPUT



Solving Simultaneous equations using parametric form of a line:

$$P(t) = (1-t)P_0 + tP_1$$

where, $P(0) = P_0$; $P(1) = P_1$

Solve with respective pairs:

$$t_{lx} = \frac{K_x - X_0}{X_1 - X_0}$$

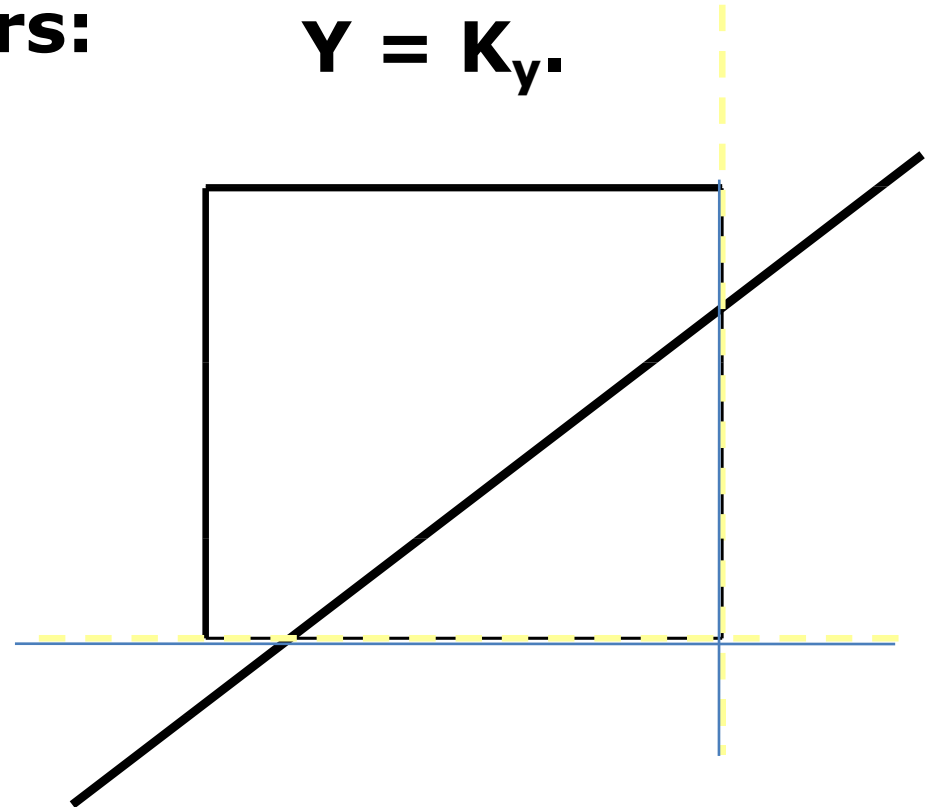
$$t_{ly} = \frac{K_y - Y_0}{Y_1 - Y_0}$$

Vertical Line:

$$X = K_x;$$

Horizontal Line:

$$Y = K_y.$$



In general, solve for two sets of simultaneous equations for the parameters:

t_{edge} and t_{line}

Check if they fall within range [0 - 1].

i.e. Rewrite

$$P(t) = P_0 + t(P_1 - P_0)$$

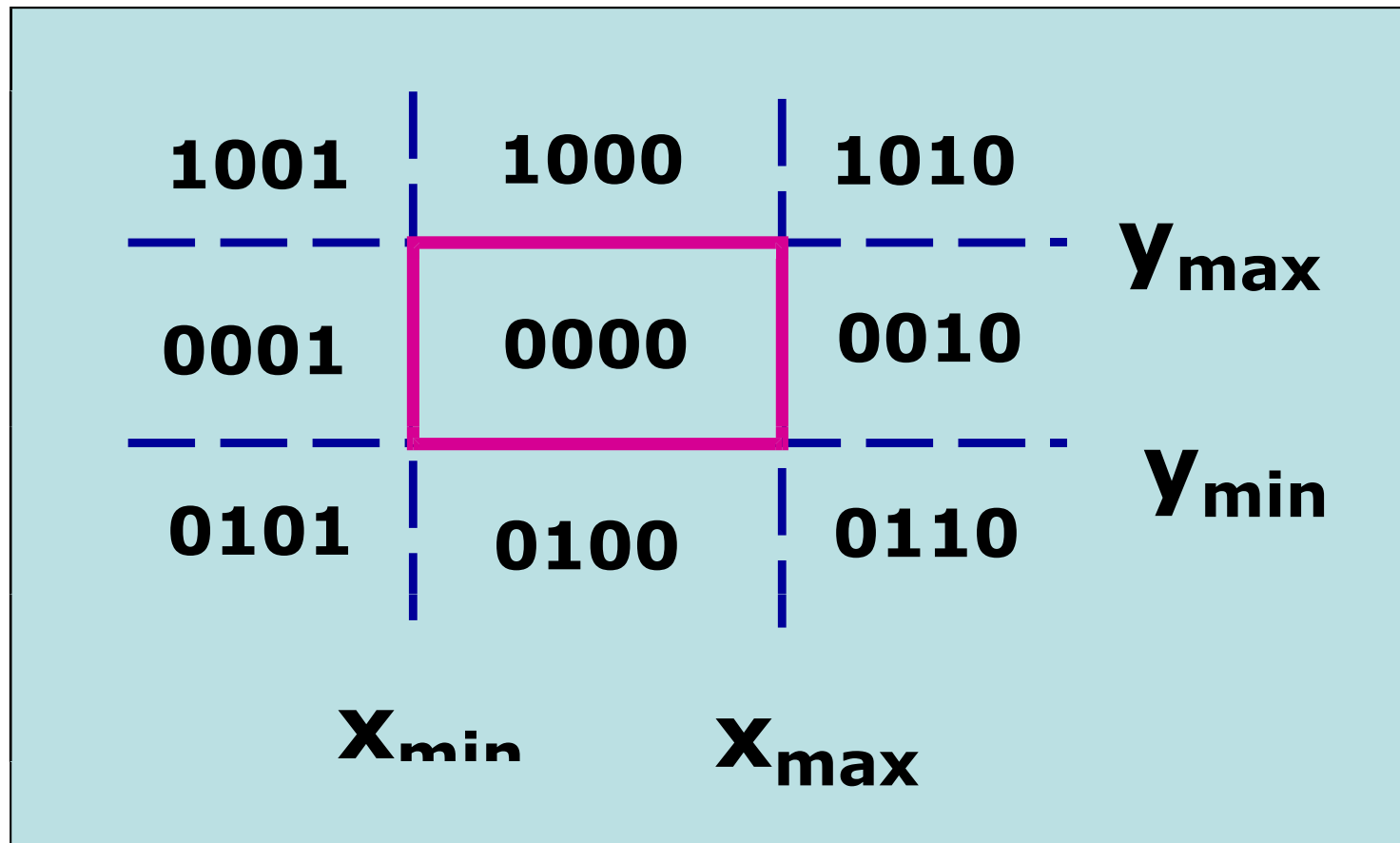
and Solve:

$$t_1 (P_1 - P_0) - t_2 (P_1 - P_0) = P_0 - P_0$$

Cohen-Sutherland

Line Clipping

Region Outcodes:



Bit Number	1	0
FIRST (MSB)	Above Top edge $Y > Y_{\max}$	Below Top edge $Y < Y_{\max}$
SECOND	Below Bottom edge $Y < Y_{\min}$	Above Bottom edge $Y > Y_{\min}$
THIRD	Right of Right edge $X > X_{\max}$	Left of Right edge $X < X_{\max}$
FOURTH (LSB)	Left of Left edge $X < X_{\min}$	Right of Left edge $X > X_{\min}$

First Step: Determine the bit values of the two end-points of the line to be clipped.

To determine the bit value of any point, use:

$$\begin{aligned} b_1 &= \text{sgn}(Y_{\max} - Y); & b_2 &= \text{sgn}(Y - Y_{\min}); \\ b_3 &= \text{sgn}(X_{\max} - X); & b_4 &= \text{sgn}(X - X_{\min}); \end{aligned}$$

Use these end-point codes to locate the line.

Various possibilities:

If both endpoint codes are [0000], the line lies completely inside the box, no need to clip. This is the simplest case (e.g. L_1).

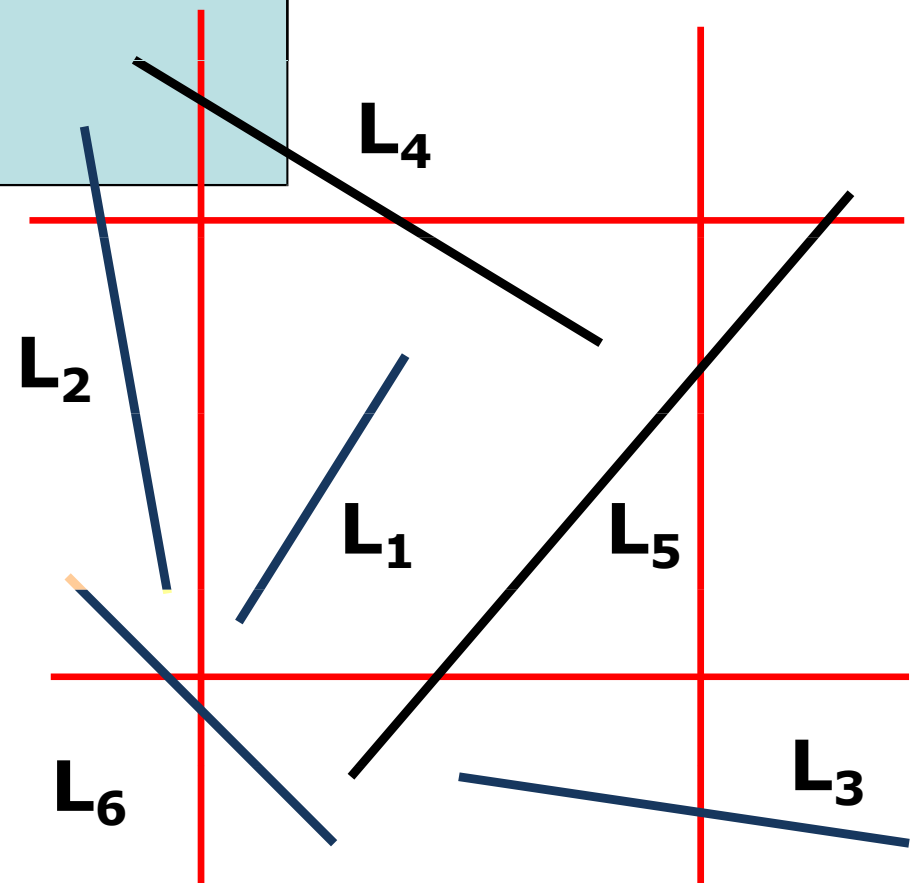
Any line has 1 in the same bit positions of both the endpoints, it is guaranteed to lie outside the box completely (e.g. L_2 and L_3).

1001	1000	1010	
0001	0000	0010	y_{\max}
0101	0100	0110	y_{\min}
	x_{\min}	x_{\max}	

• Neither completely reject nor inside the box:

Lines: L_4 and L_5 , - needs more processing.

What about Line L_6 ?



**Processing of lines, neither Completely
IN or OUT; e.g. Lines: L_4 , L_5 and L_6 .**

Basic idea:

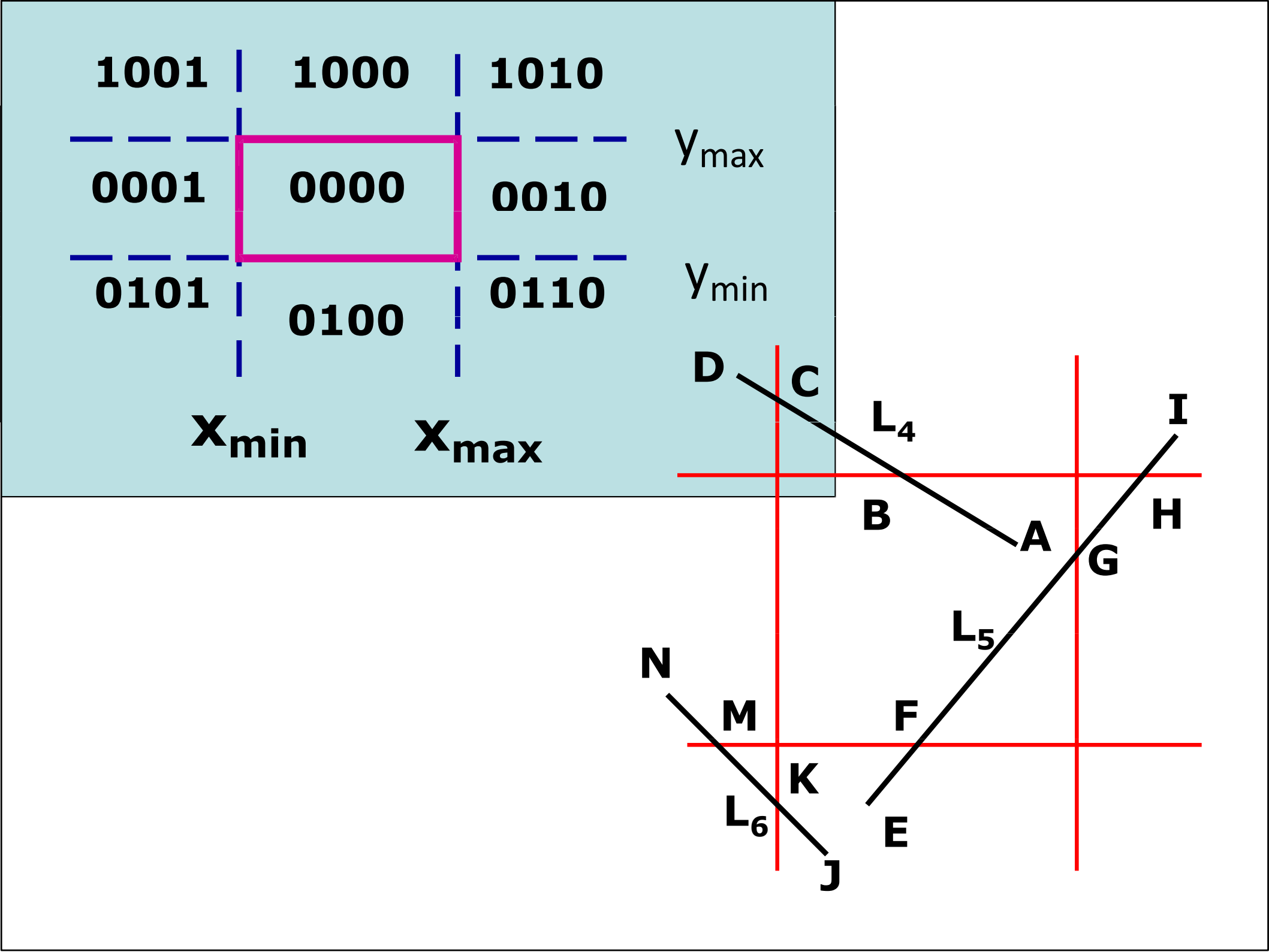
**Clip parts of the line in any order (consider
from top or bottom).**

Algorithm Steps:

**Compute outcodes of both endpoints to
check for trivial acceptance or rejection
(AND logic).**

**If not so, obtain an endpoint that lies outside
the box (at least one will ?).**

**Using the outcode, obtain the edge that is
crossed first.**



**Coordinates for intersection,
w.r.t edge:**

**Inputs: Endpoint coordinates:
(X_0 , Y_0) and (X_1 , Y_1)**

OUTPUT:

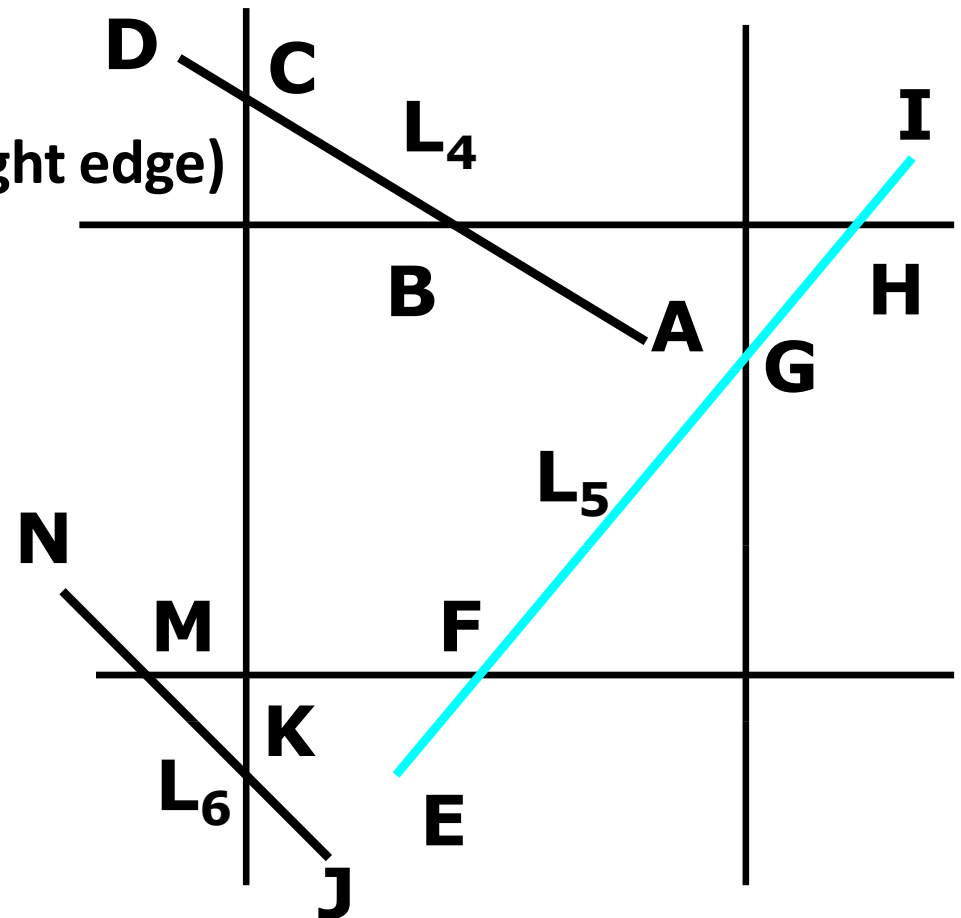
**Edge for clipping (obtained using
outcode of current endpoint).**

Obtain corresponding intersection points

- **CLIP (replace the endpoint by the intersection point) w.r.t. the edge.**
- **Compute the outcode for the updated endpoint and repeat the iteration, till it is 0000.**
- **Repeat the above steps, if the other endpoint is also outside the area.**

e.g. Take Line L_5 (endpoints -E and I):
E has outcode 0100 (to be clipped w.r.t. bottom edge);

- So EI is clipped to FI; Outcode of F is 0000; But outcode of I is 1010; Clip (w.r.t. top edge)
- to get FH.
- Outcode of H is 0010; Clip (w.r.t. right edge)



to get FG;

Since outcode of G
is 0000, display the
final result as FG.

Formulas for clipping w.r.t. edge, in cases of:

Top Edge :

$$X = X_0 + (X_1 - X_0) * \frac{(Y_{max} - Y_0)}{(Y_1 - Y_0)}$$

Bottom Edge:

$$X = X_0 + (X_1 - X_0) * \frac{(Y_{min} - Y_0)}{(Y_1 - Y_0)}$$

Right Edge:

$$Y = Y_0 + (Y_1 - Y_0) * \frac{(X_{max} - X_0)}{(X_1 - X_0)}$$

Left edge:

$$Y = Y_0 + (Y_1 - Y_0) * \frac{(X_{min} - X_0)}{(X_1 - X_0)}$$

Liang-Barsky

Line Clipping

Consider parametric equation of a line segment:

$$X = X_1 + u \Delta X ; Y = Y_1 + u \Delta Y, \quad 0 \leq u \leq 1.$$

where,

$$\Delta X = X_2 - X_1 ; \Delta Y = Y_2 - Y_1$$

A point is considered to be within a rectangle, iff

$$XW_{\min} \leq X_1 + u \Delta X \leq XW_{\max} ;$$

$$YW_{\min} \leq Y_1 + u \Delta Y \leq YW_{\max} .$$

Each of these four inequalities, can be expressed as:

$$u.p_k = q_k \quad k = 1,2,3,4$$

where, the parameters are defined as:

$$p_1 = -\Delta X, \quad q_1 = X_1 - XW_{\min}$$

$$p_2 = \Delta X, \quad q_2 = XW_{\max} - X_1$$

$$p_3 = -\Delta Y, \quad q_3 = Y_1 - YW_{\min}$$

$$p_4 = \Delta Y, \quad q_4 = YW_{\max} - Y_1$$

Based on these four inequalities, we can find the following conditions of line clipping:

•If $p_k = 0$, the line is parallel to the corresponding clipping boundary:

$K = 1 \rightarrow$	Left
$K = 2 \rightarrow$	Right
$K = 3 \rightarrow$	Bottom
$K = 4 \rightarrow$	Top

• If for any k , for which $p_k = 0$:

$q_k < 0$, the line is completely outside the boundary

$q_k \geq 0$, the line is inside the parallel clipping boundary.

If $p_k < 0$, the line proceeds from the outside to the inside of the particular clipping boundary (visualize infinite extensions in both).

If $p_k > 0$, the line proceeds from the inside to the outside of the particular clipping boundary (visualize infinite extensions in both).

In both these cases, the intersection parameter is calculated as:

$$u = q_k / p_k$$

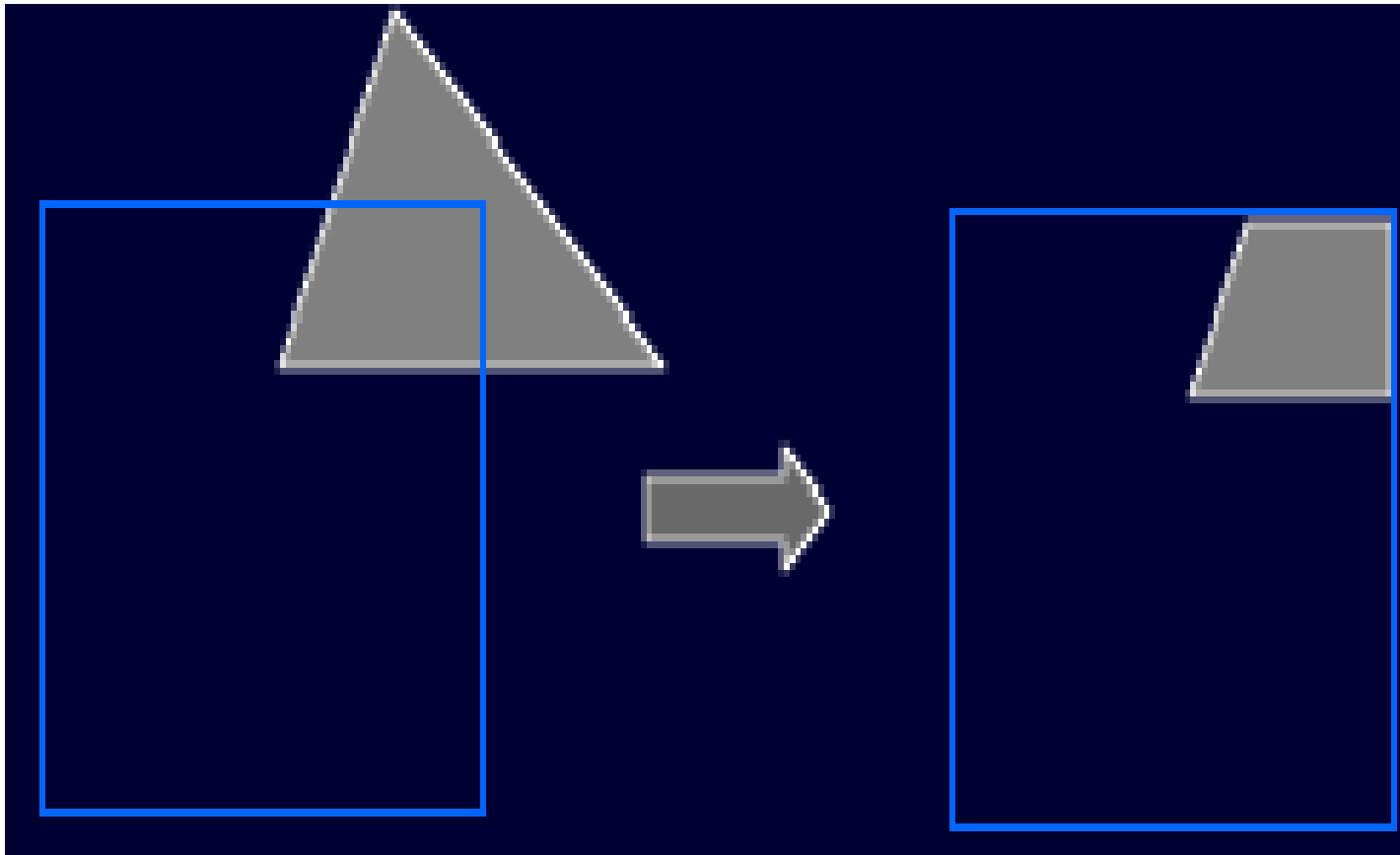
The Algorithm:

- **Initialize line intersection parameters to:**
 $u_1 = 0; u_2 = 1;$
- **Obtain p_i, q_i ; for $i = 1, 2, 3, 4$.**
- **Using p_i, q_i - find if the line can be rejected or the intersection parameters must be adjusted.**
- **If $p_k < 0$, update u_1 as:**
$$\max[0, (q_k / p_k)], k = 1-4$$
- **If $p_k > 0$, update u_2 as:**
$$\min[1, (q_k / p_k)], k = 1-4$$
- **After update, if $u_1 > u_2$: reject the line.**

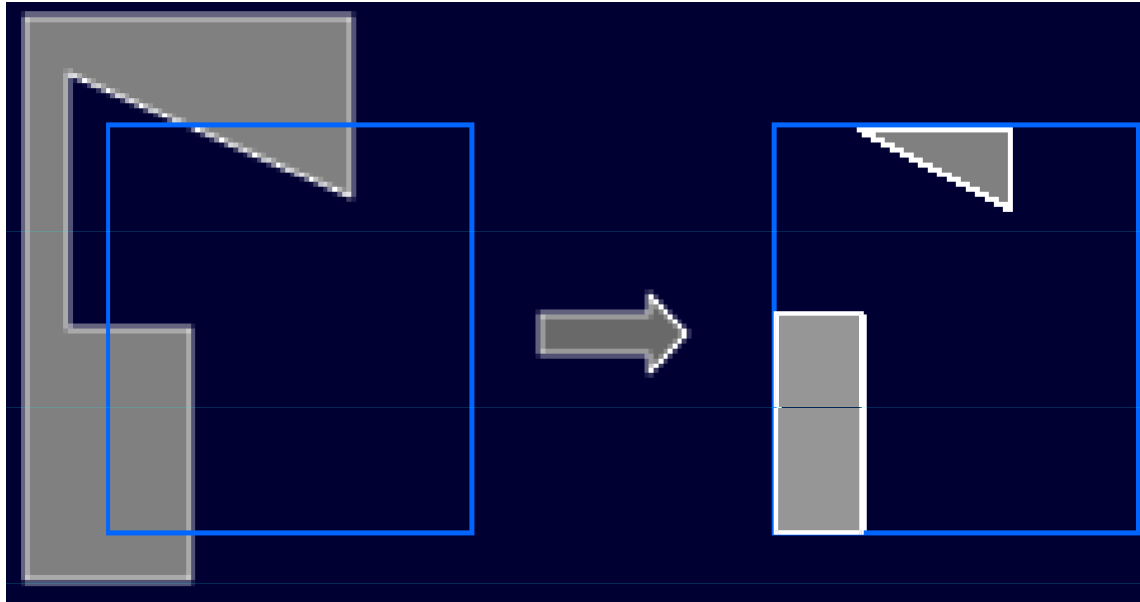
POLYGON

CLIPPING

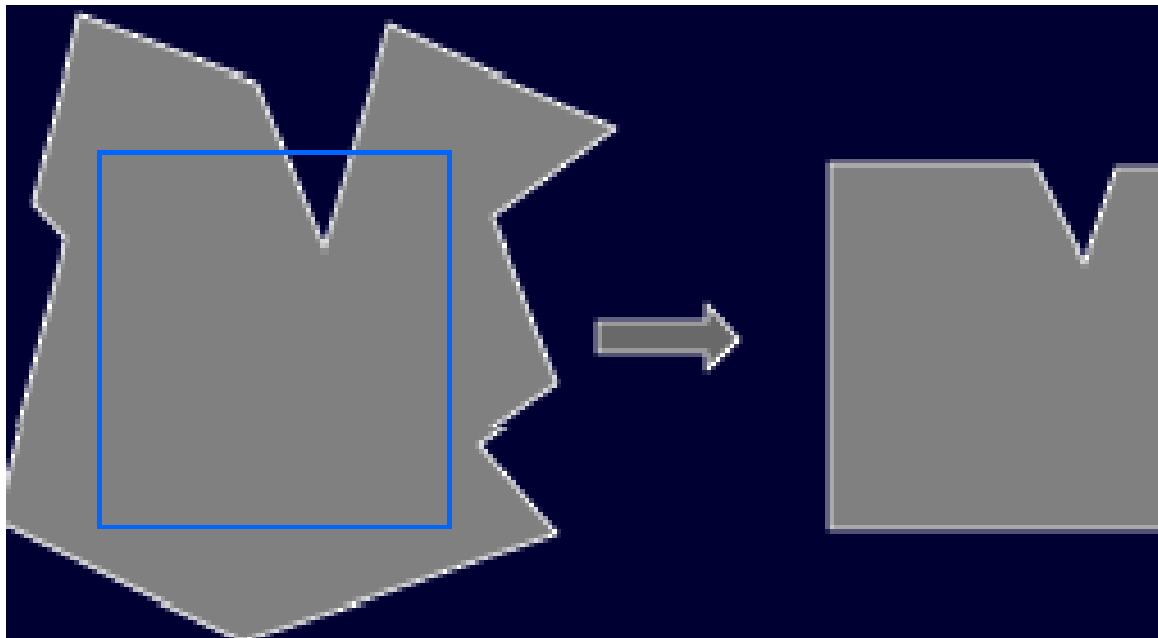
Examples of Polygon Clipping



CONVEX SHAPE



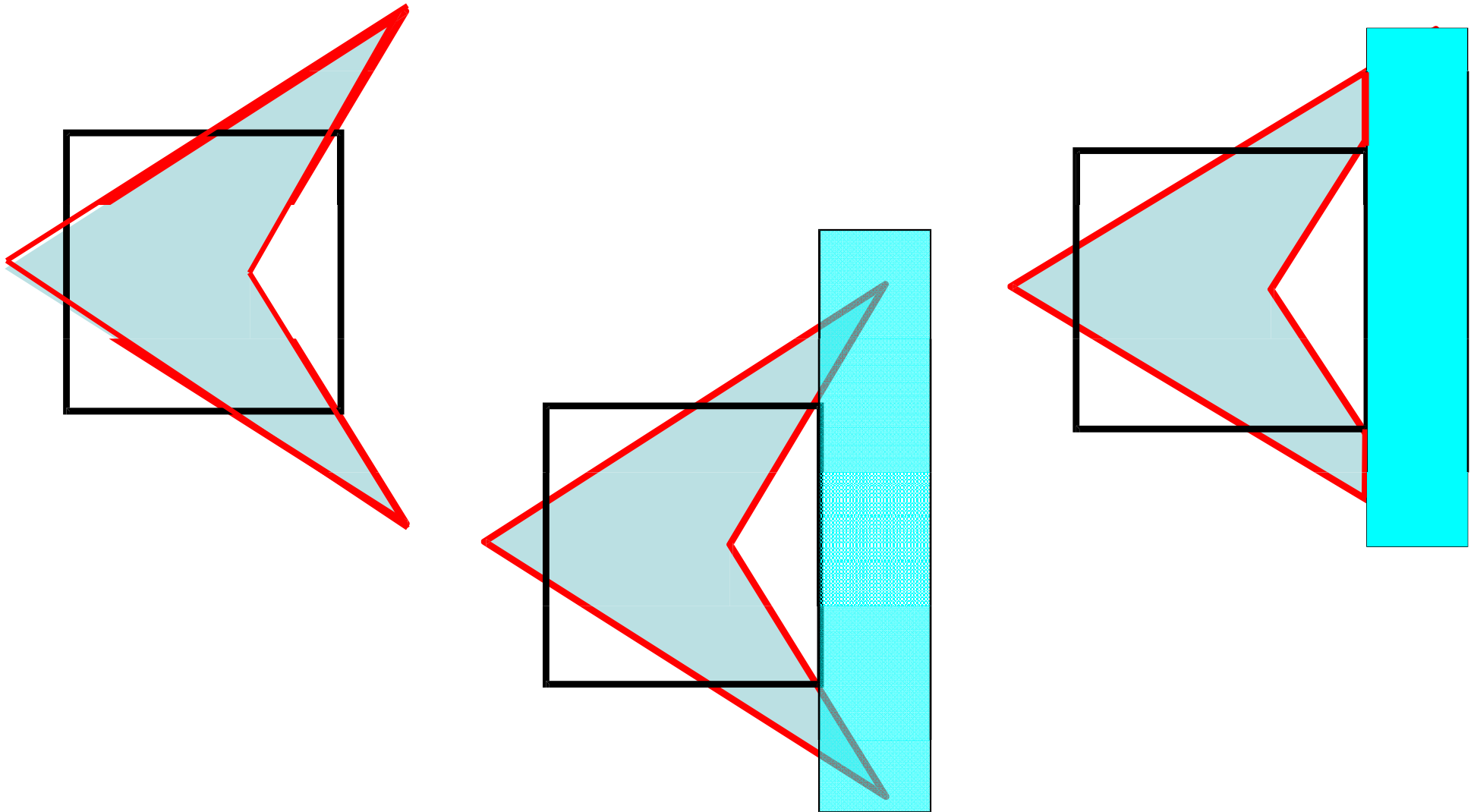
MULTIPLE
COMPONENTS

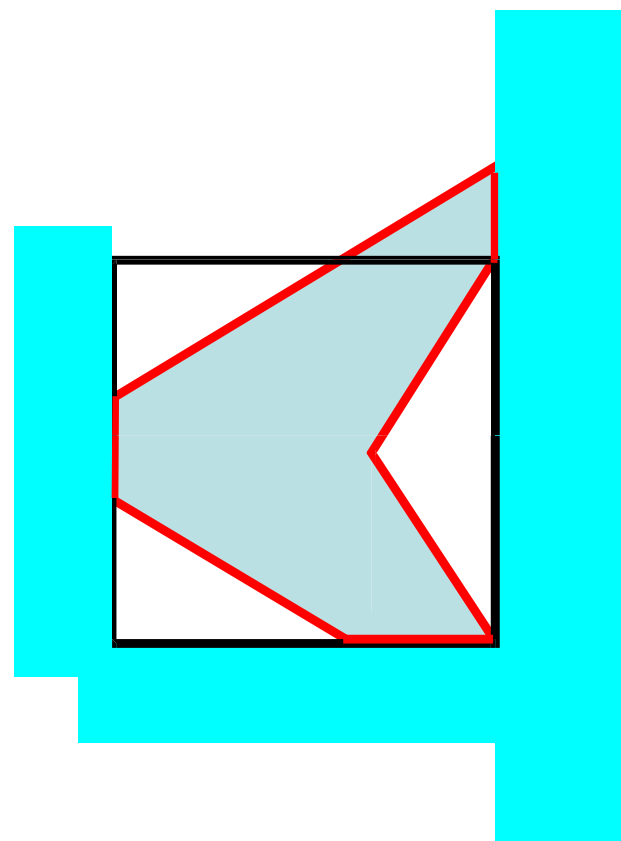
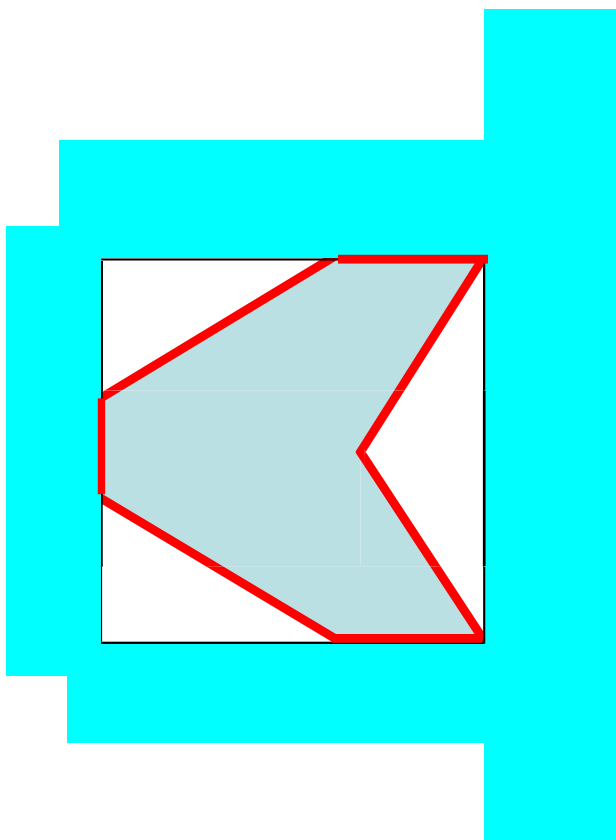
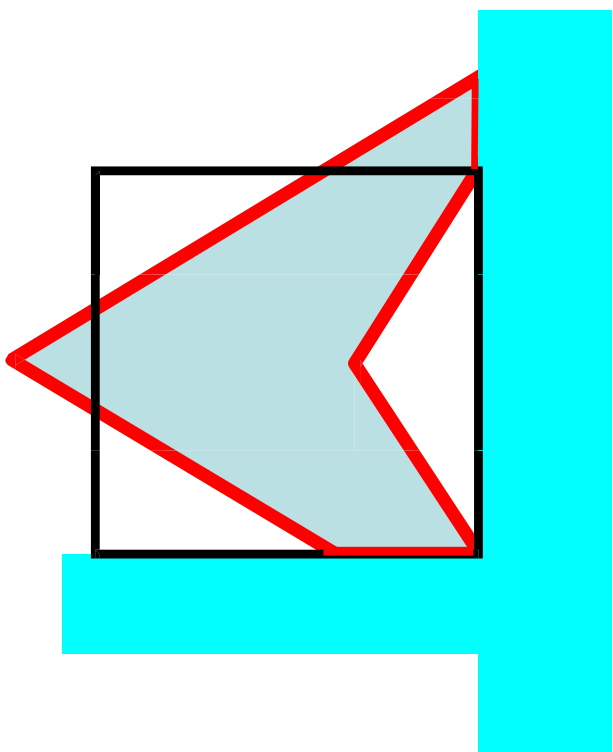


**CONCAVE
SHAPE**

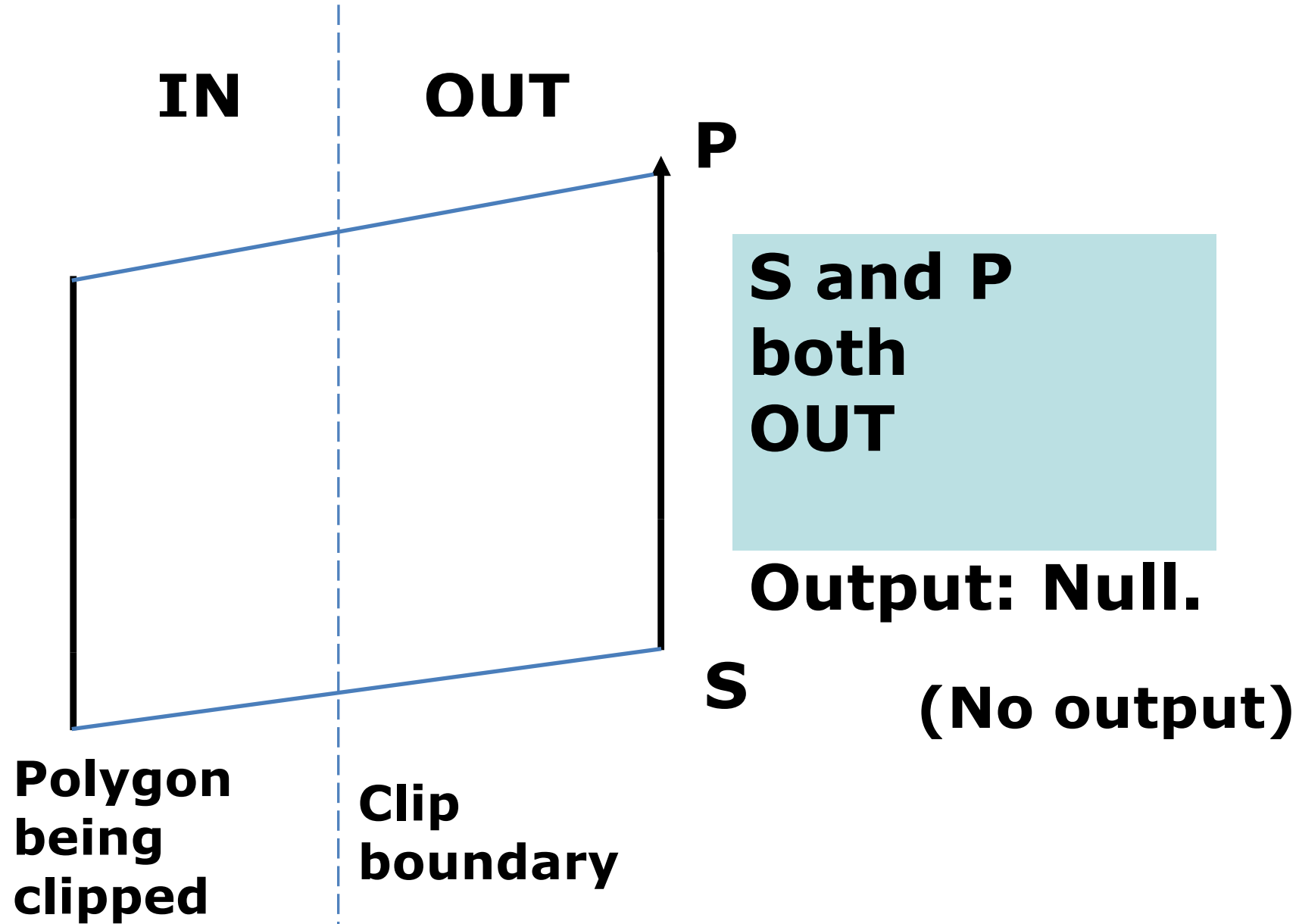
Methodology: CHANGE position of vertices for each edge by line clipping

May have to add new vertices to the list.

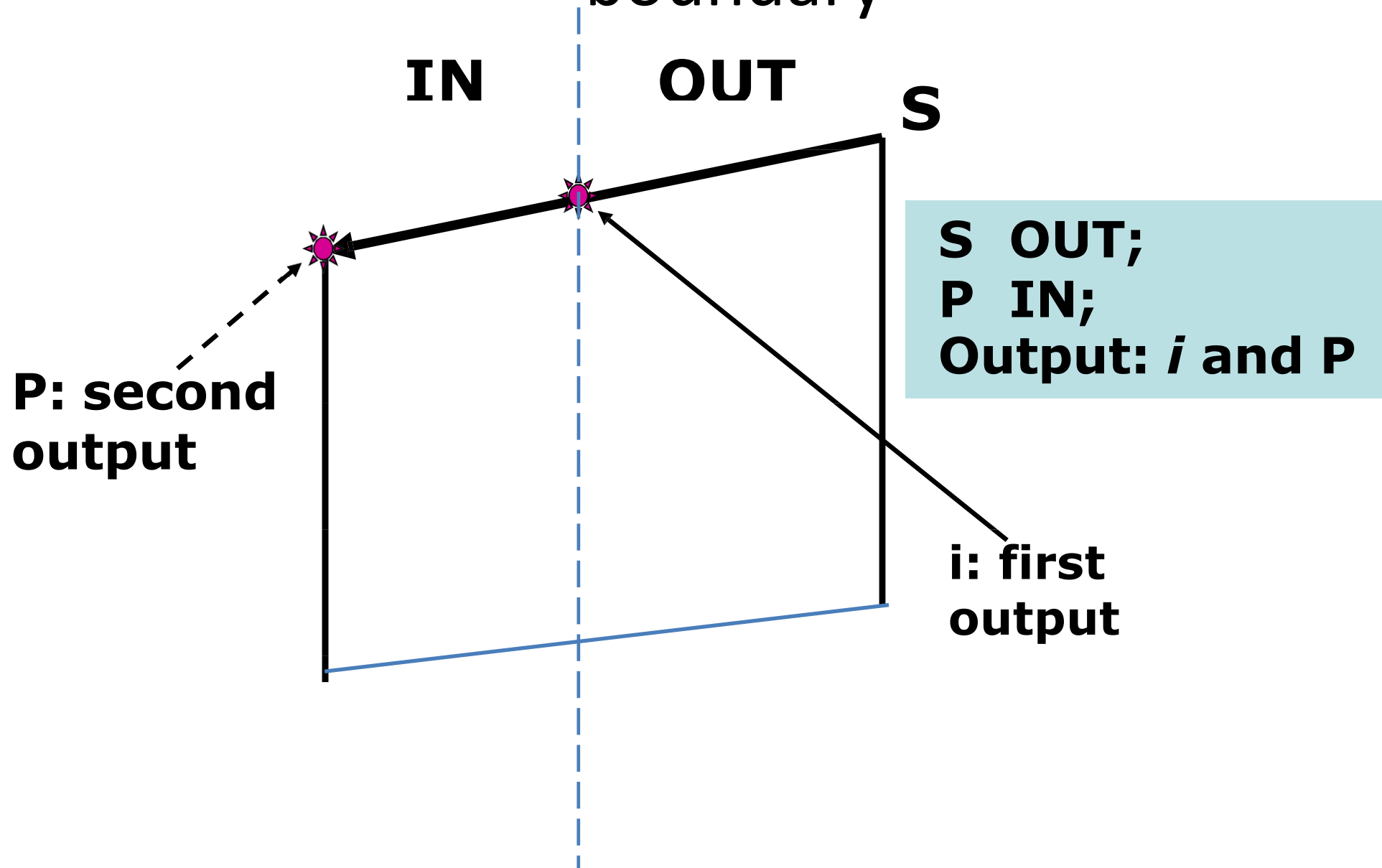




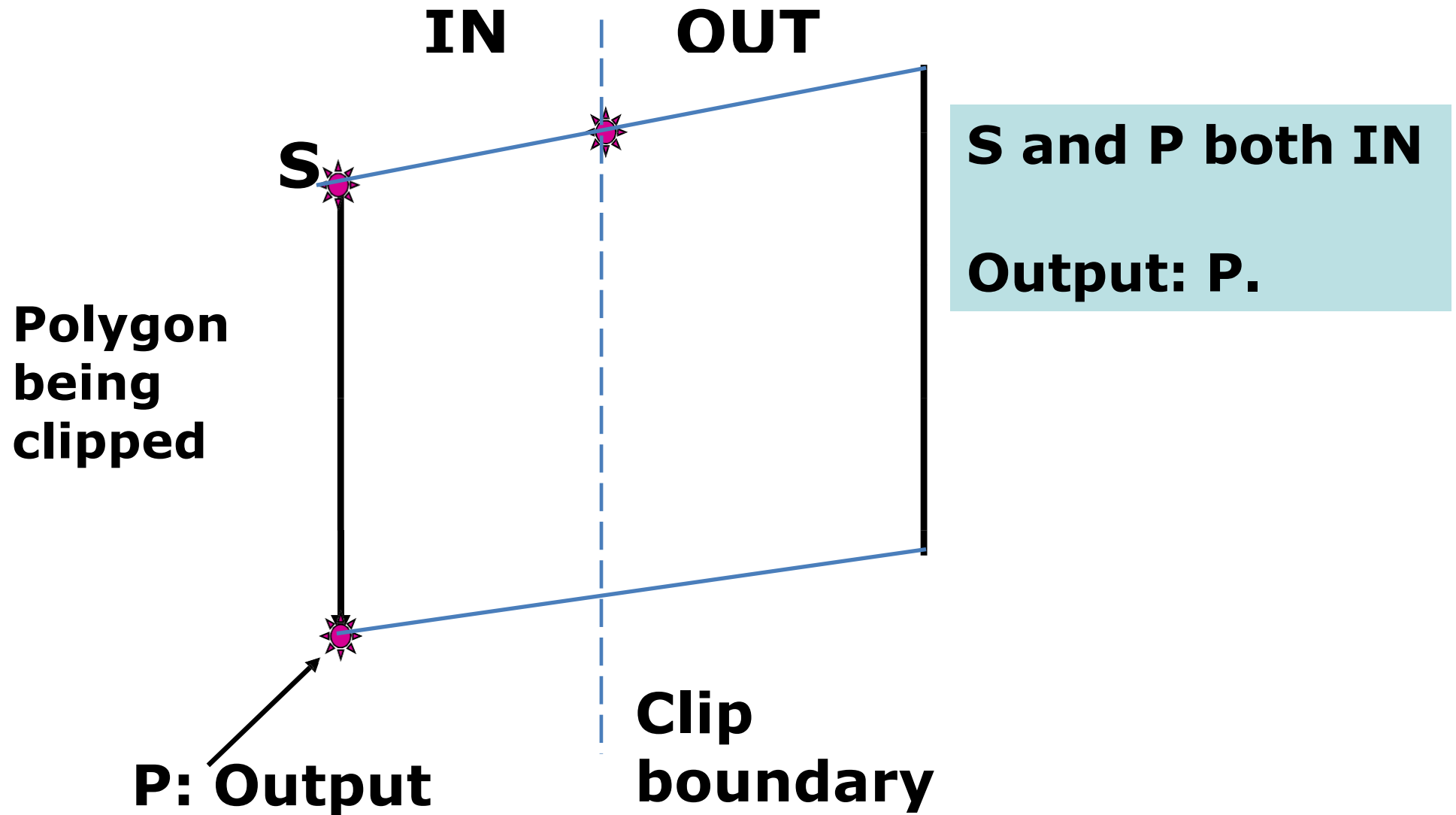
Processing of Polygon vertices against boundary



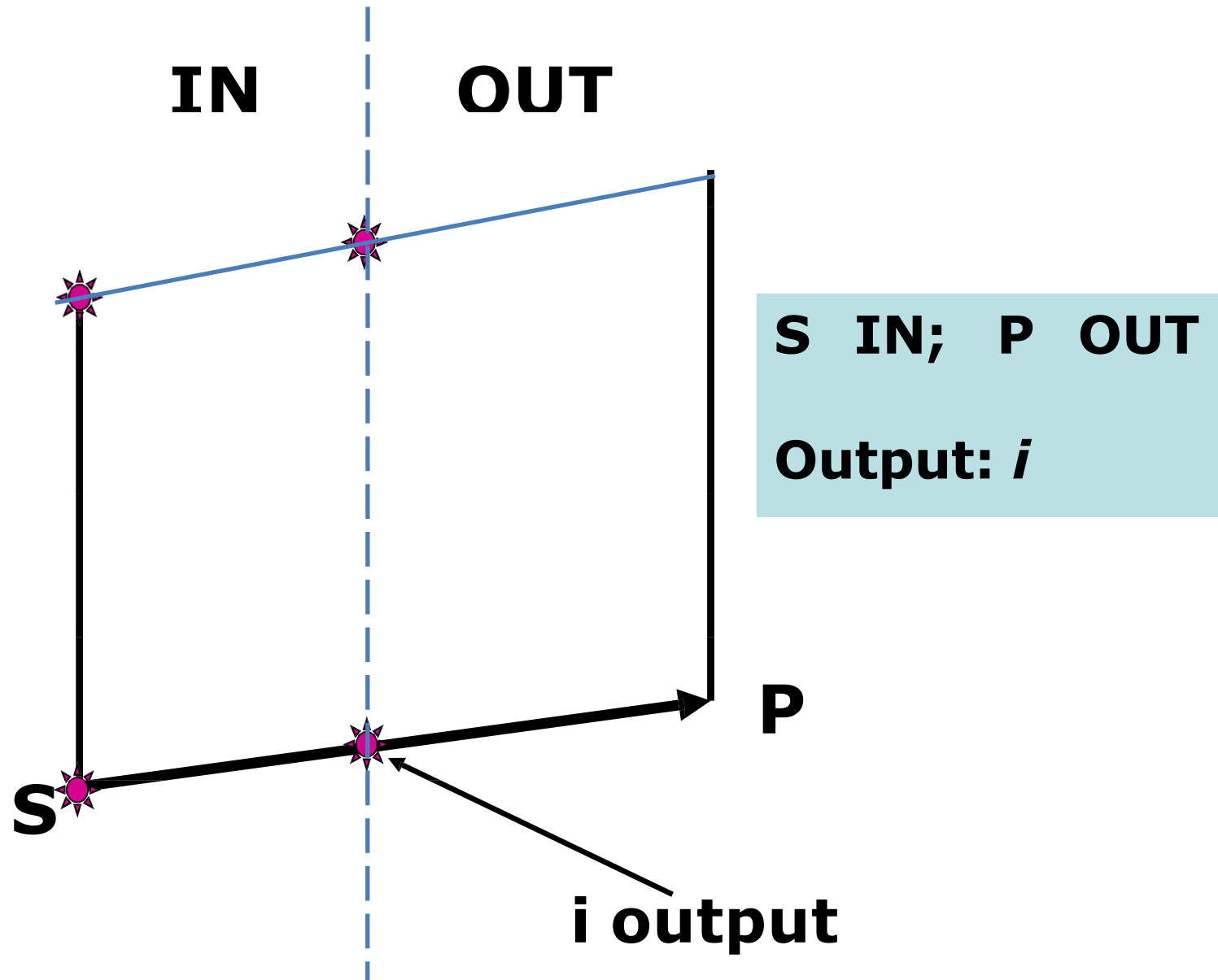
Processing of Polygon vertices against boundary



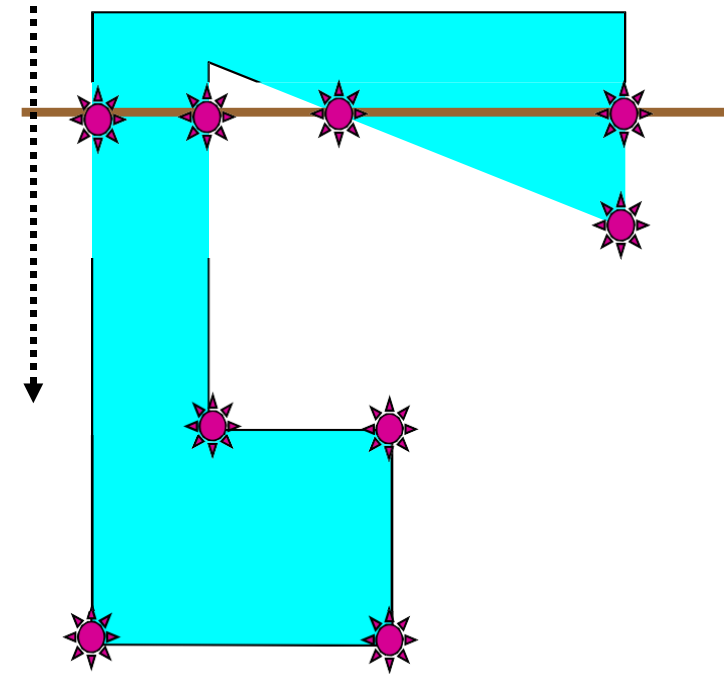
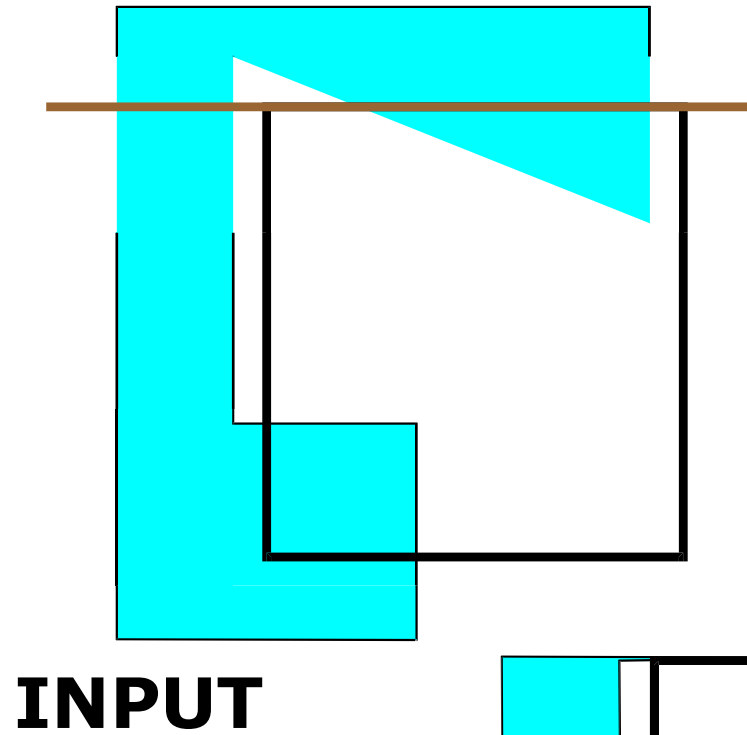
Processing of Polygon vertices against boundary



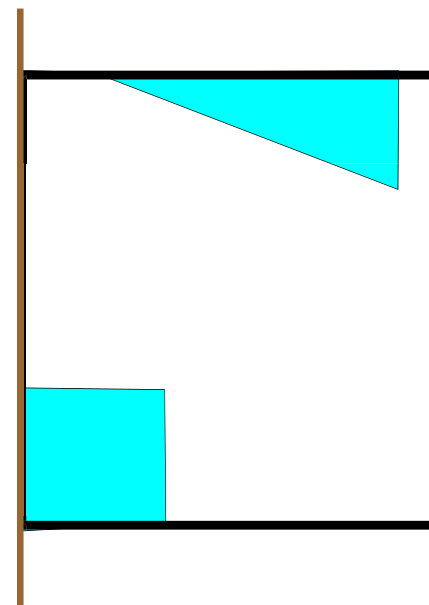
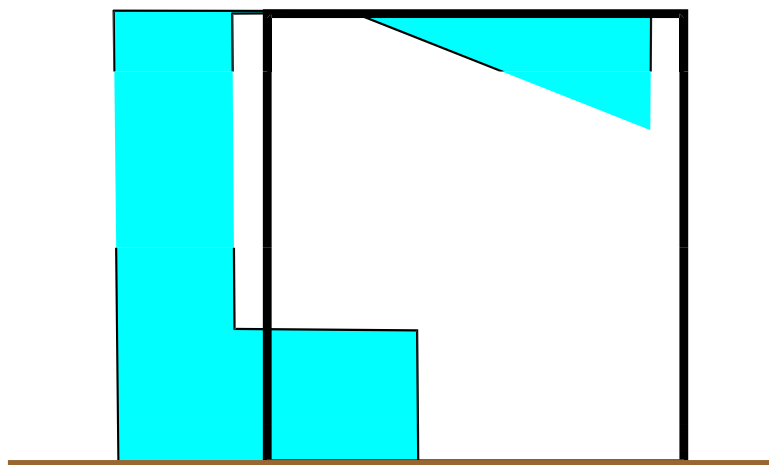
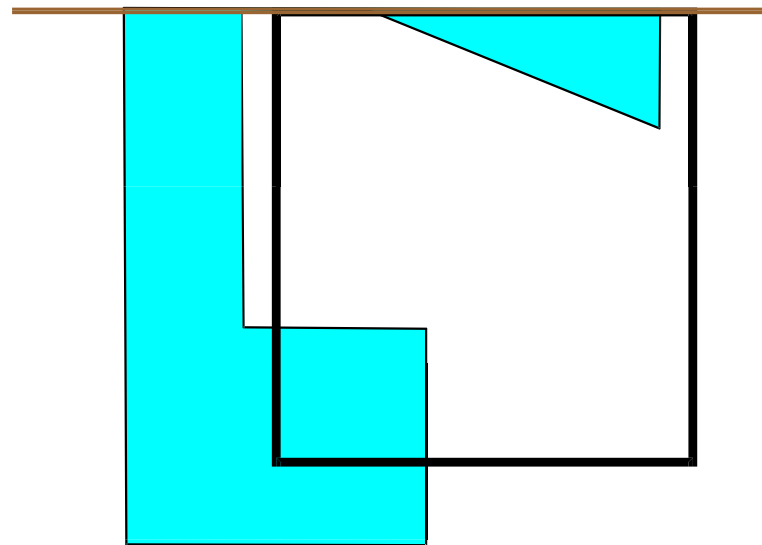
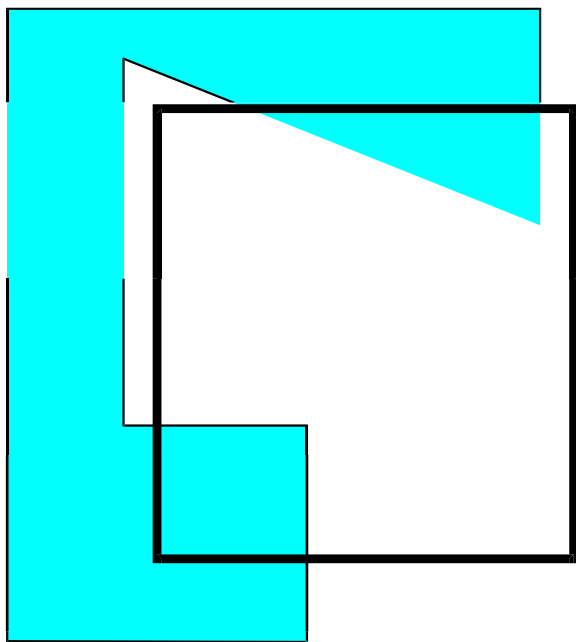
Processing of Polygon vertices against boundary

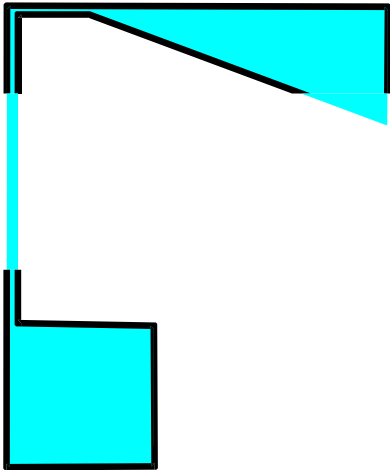


Problems with multiple components

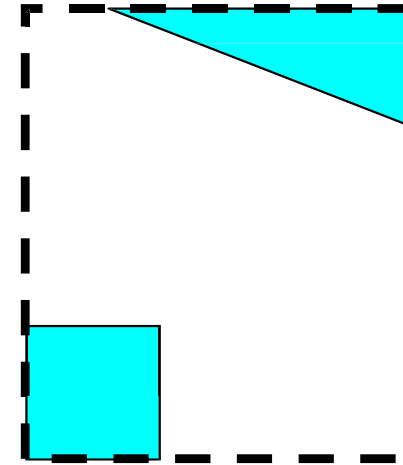


Problems with multiple components





Now output is as above

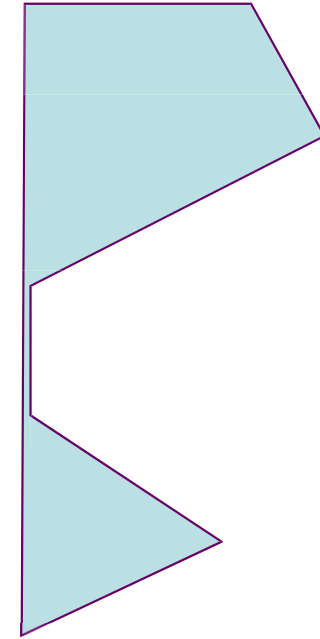
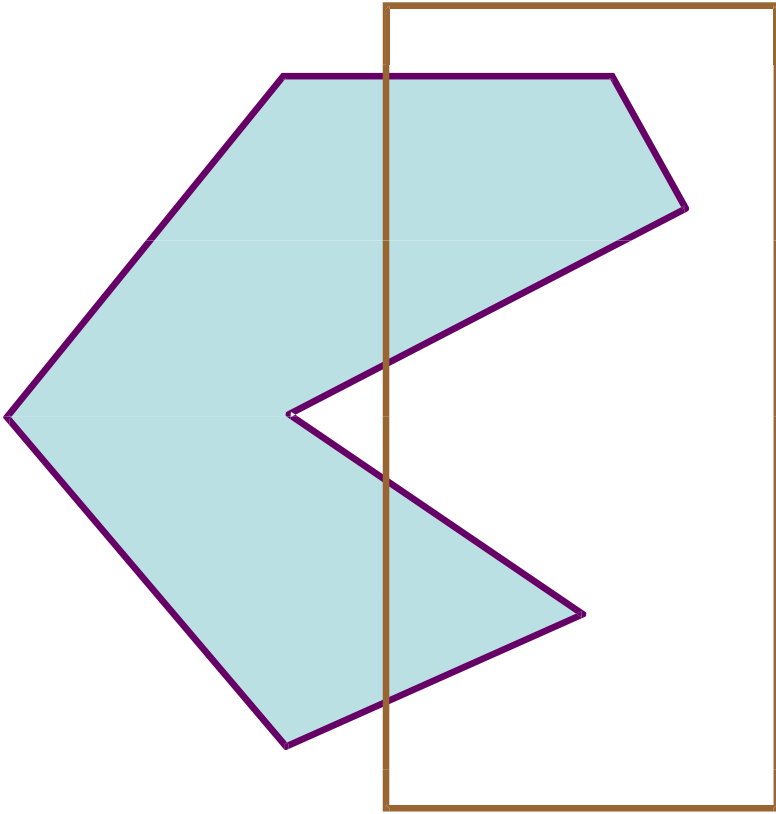


Desired Output

Any Idea ??

**– the modified
Weiler-Atherton
algorithm**

Solution for multiple
components



**For say, clockwise processing of polygons,
follow:**

- **For OUT -> IN pair, follow the polygon
boundary**

- For IN -> OUT pair, follow Window boundary
in clockwise direction**

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follow:**

- **For OUT -> IN pair, follow the polygon boundary**

**For IN -> OUT pair, follow Window boundary
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