



gradeup

Sahi Prep Hai Toh Life Set Hai

HCF & LCM-2

Agenda

* Word Problems

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Agenda

* Word Problems on

HCF & LCM

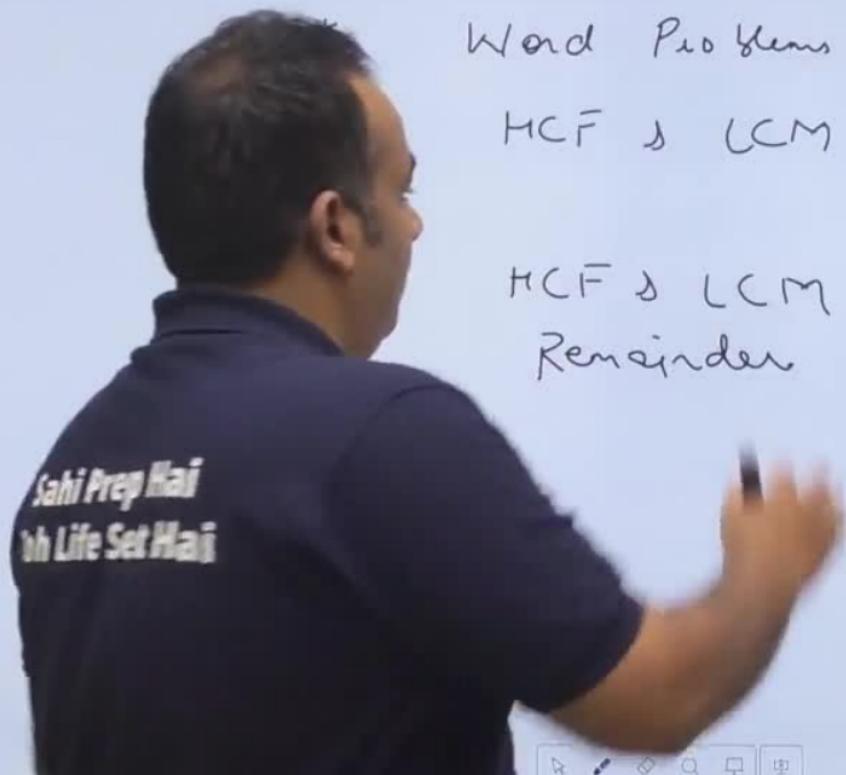
HCF & LCM with

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Agenda

Word Problems on

HCF & LCM

HCF & LCM with
Remainder

Agenda

* Word Problem

HCF & LCM → 28-30 min

* HCF & LCM +
Remainder

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Agenda

- * Word Problems on HCF & LCM → (28-30 min)

- * HCF & LCM with Remainder → 30 min

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Agenda

* Word Problems on

HCF & LCM \rightarrow (28-30 min)

HCF & LCM with
Remainder \rightarrow (30-32) min

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Practice Questions

Agenda

* Word Problems on

HCF & LCM with
Repetition → (28-30 min)

* HCF & LCM with

Repetition → (30-32) min

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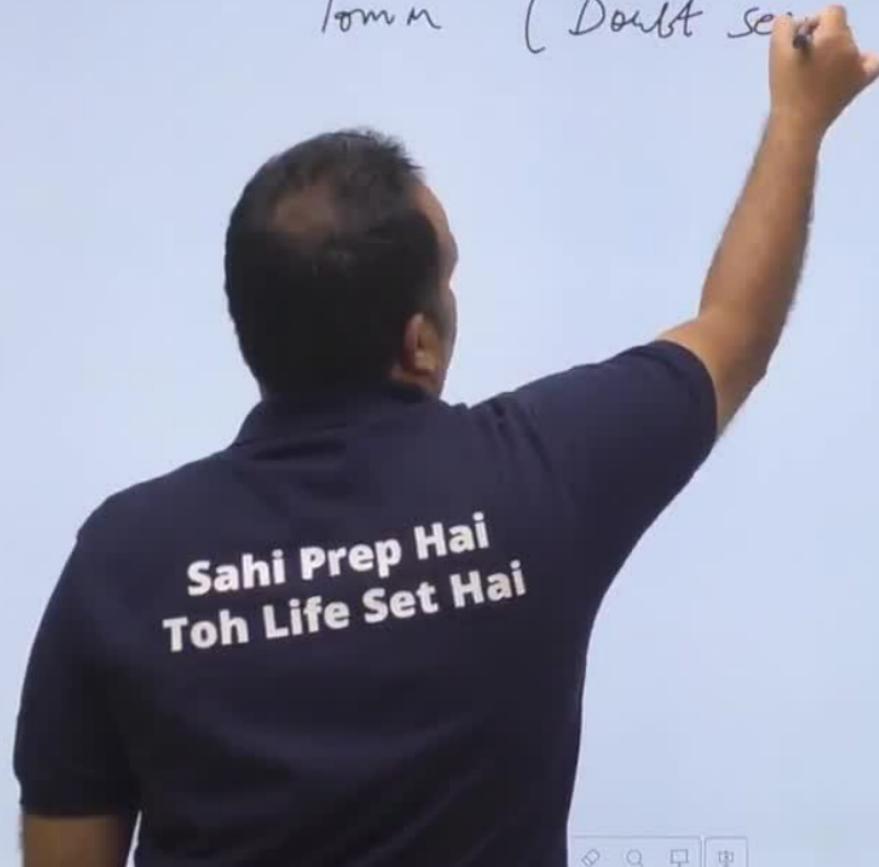
(22-24)

Agenda

- * Word Problems on
HCF & LCM → (28-30 min)
- * HCF & LCM with
Remainder → (30-32) min

Practice Question
(7-8)Q → (22-24) min

Tomor (Doubt se)



Tomorrow (Doubt session)

By 5pm sen

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Toh Life Set Hai

Tomorrow (Doubt session)

→ WhatsApp

→ Gradeup app

By 9 pm send your doubts

7 students

Tomorrow (Doubt session)

- WhatsApp
- Gradeup app

But send your doubts

Students



Tomorrow (Doubt session)

- WhatsApp
- Gradeup

By 5pm send your doubts

Only 7 students



Tomorrow (Doubt session)

- WhatsApp
- Gradeup app

By 5pm send your doubts

Only 7-8

9971658659

Name _____

Br.

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Tomorrow (Doubt session)

→ WhatsApp

→ app

By 5pm send your doubts

Only 7 students

{ 9971658659
Name
Batch Tim

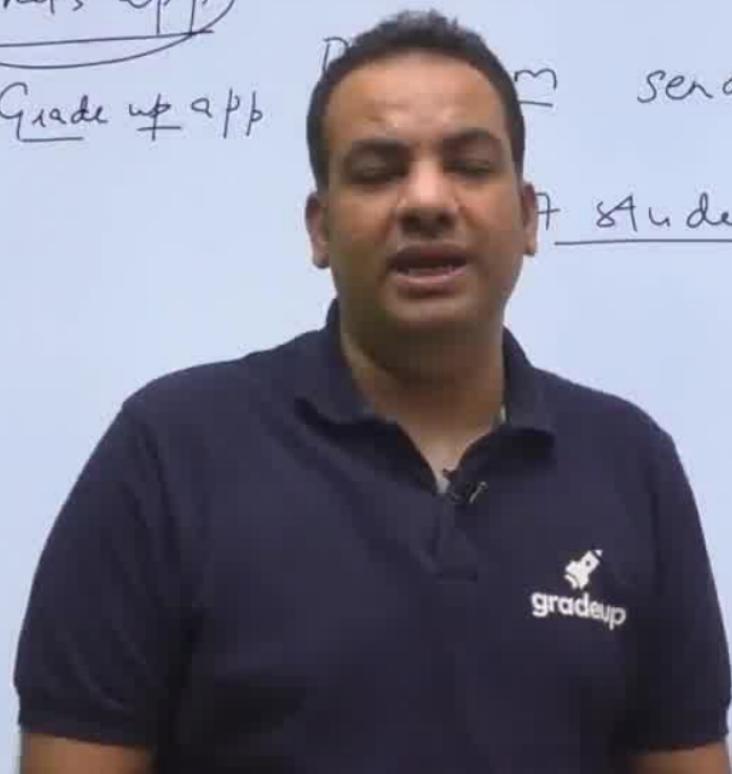
Tomorrow (Doubt session)

- WhatsApp
- Gradeup app

Please send your doubts

7 students

9971658659
Name _____
Batch Time _____



Agenda

* Word Problems on

HCF & LCM \rightarrow (28-30 min)

HCF & LCM with
Remainder \rightarrow (30-32) min

Practice Question

\rightarrow (22-24) min

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WORDS PROBLEMS ON HCF and LCM



WORDS PROBLEMS ON HCF and LCM

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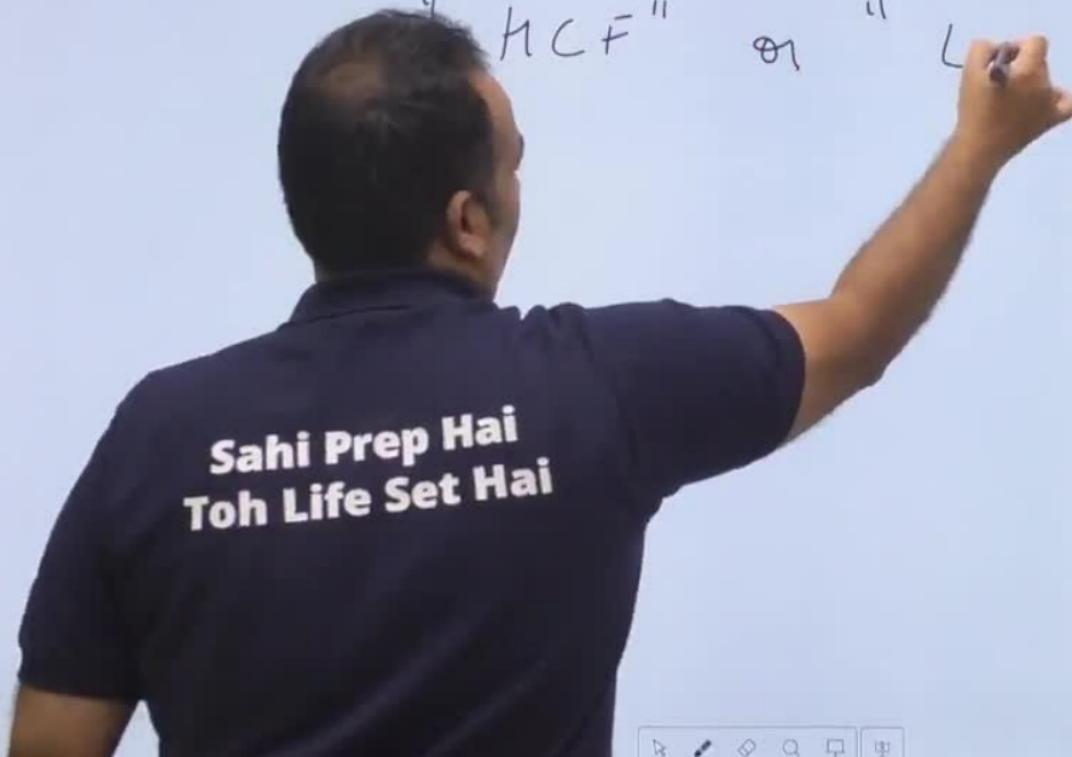


How to deci

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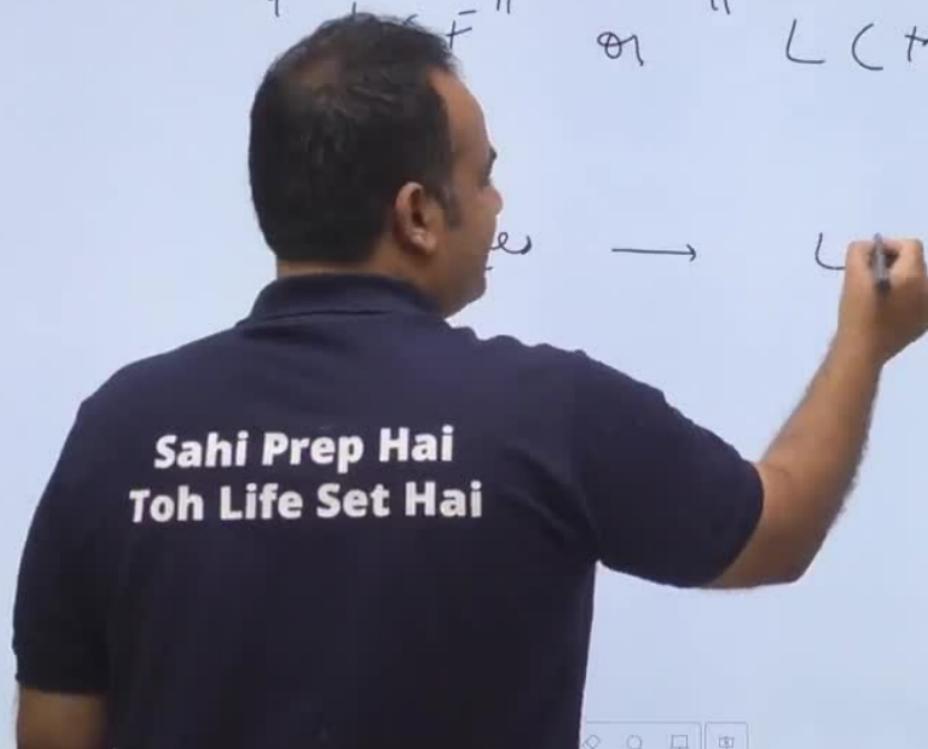
How to decide whether question is on

"HCF" or "L



How to decide whether question is on

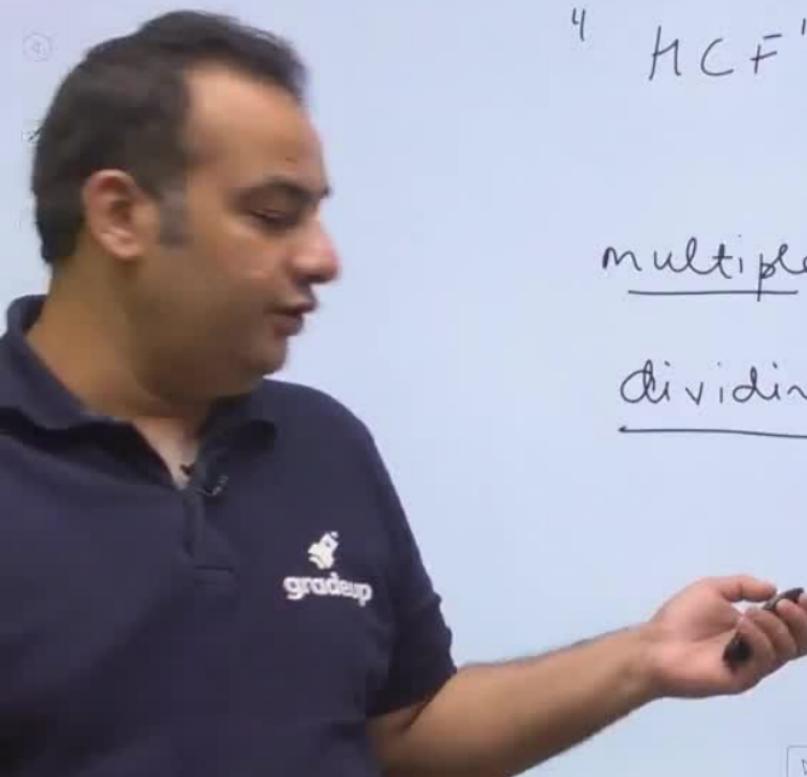
" LCM " or " LCM "



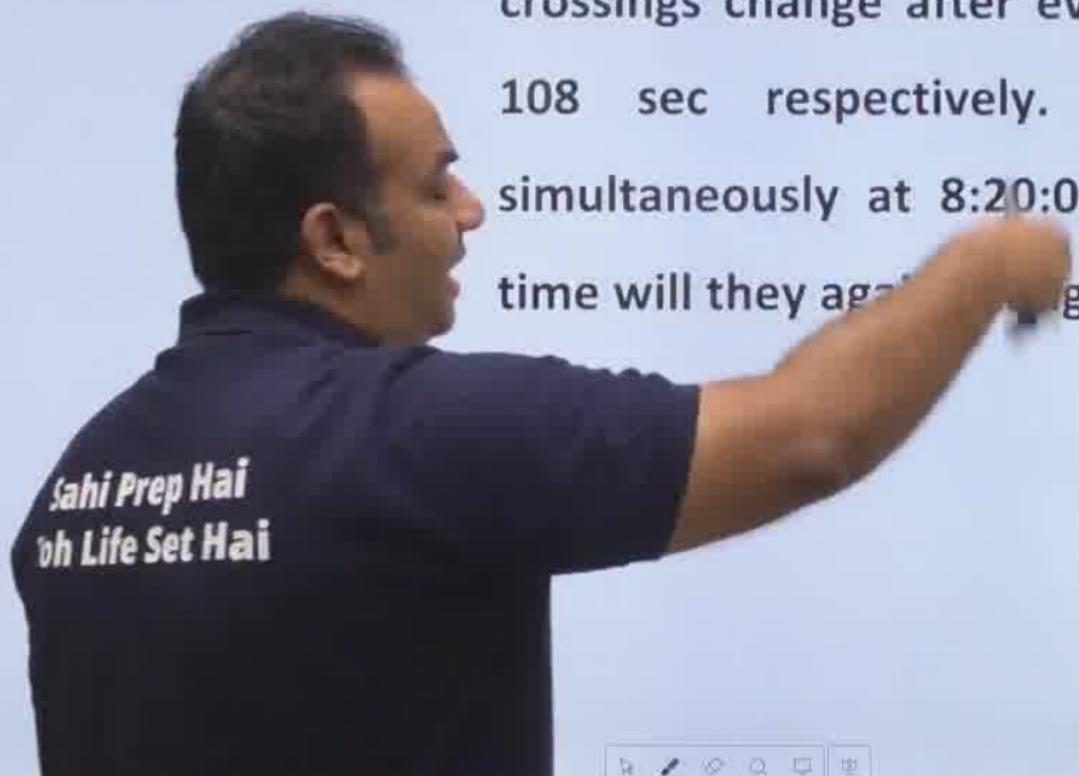
How to decide whether question is on

"HCF" or "LCM"

multiples → LCM }
dividing → HCF }



Example: The traffic lights at three different road crossings change after every 48 sec, 72 sec and 108 sec respectively. If they all change simultaneously at 8:20:00 hours, than at what time will they again change simultaneously?



48 72 108
96 144 216
144 216 324
1 1 1

Example: The traffic lights at three different road crossings change after every 48 sec, 72 sec and 108 sec respectively. If they all change simultaneously at 8:20:00 hours, than at what time will they again change simultaneously?

$$\begin{aligned}48 &= 2^4 \cdot 3^1 \\72 &= 2^3 \cdot 3^2 \\108 &= 2^2 \cdot 3^3\end{aligned}$$

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48 72 108
96 144 216
144 216 324
1 1 1
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Example: The traffic lights at three different road crossings change after every 48 sec, 72 sec and 108 sec respectively. If they all change simultaneously at 8:20:00 hours, than at what time will again change simultaneously?

48

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$$\text{LCM} = 2^4 \cdot 3^3$$

48	72	108
24	144	216
144	216	324
1	1	1
1	1	1
1	1	1

Example: The traffic lights at three different road crossings change after every 48 sec, 72 sec and respectively. If they all change simultaneously at 8:20:00 hours, than at what time they again change simultaneously?

$$\text{LCM} = 2^4 \cdot 3^3$$

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48 72 108
96 144 216
144 216 324
1 1 1
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Example: The traffic lights at three different road crossings change after every 48 sec, 72 sec and 108 sec respectively. If they all change simultaneously at 8:20:00 hours, than at what time will they again change simultaneously?

$$\text{LCM} = 2^4 \cdot 3^3 \\ = 432 \text{ sec}$$

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48	72	108
24	144	216
144	216	324
1	1	1
1	1	1
1	1	1

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$$\begin{aligned} \text{LCM} &= 2^4 \cdot 3^3 \\ &= 432 \text{ sec} \end{aligned}$$

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Toh Life Set Hai*

48	72	108
24	144	216
12	216	324
6	108	
3		
1		
1		
1		

Example: The traffic lights at three different road crossings change after every 48 sec, 72 sec and 108 sec respectively. If they all change simultaneously at 8:20:00 hours, than at what time will they again change simultaneously?

$$\text{LCM} = 2^4 \cdot 3^3$$
$$\frac{7}{6} = 432 \text{ sec}$$

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Answer: Traffic lights change after every 48, 72 and 108 sec

So all the traffic lights will simultaneously change after

LCM of 48, 72 and 108 sec = 432 sec

$$48 = 2^4 \times 3^1$$

$$72 = 2^3 \times 3^2$$

$$108 = 2^2 \times 3^3$$

$$\text{LCM of } 48, 72 \text{ and } 108 = 2^4 \times 3^3 = 432$$

$$432 \text{ sec} = 7 \text{ min } 12 \text{ sec}$$

Next simultaneously change will take place at 8:27:12 hours

Example: A, B, C start running at the same time and at the same point in a circular stadium. A complete a round in 252 seconds, B in 308 seconds and C in 198 seconds. After what time will they meet again at the starting point?



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$$252 = 2 \times 3^2 \times 7$$

C
B
A

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$$252 = 2^2 \cdot 3^2 \cdot 7^1$$
$$308 =$$

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$$252 = 2^2 \cdot 3^2 \cdot 7^1$$

$$308 = 2^2 \cdot 7^1 \cdot 11^1$$

$$198 = 2^1 \cdot 3^2 \cdot 11^1$$

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$$252 = 2^2 \cdot 3^2 \cdot 7^1$$

$$308 = 2^2 \cdot 7^1 \cdot 11^1$$

$$198 = 2^1 \cdot 3^2 \cdot 11^1$$

$$\text{LCM} = 2^2 \cdot 3^2 \cdot 7^1 \cdot 11^1$$

Example: A, B, C start running at the same time and at the same point in a circular stadium. A complete a round in 252 seconds, B in 308 seconds and C in 198

After what time will they meet again at the point?

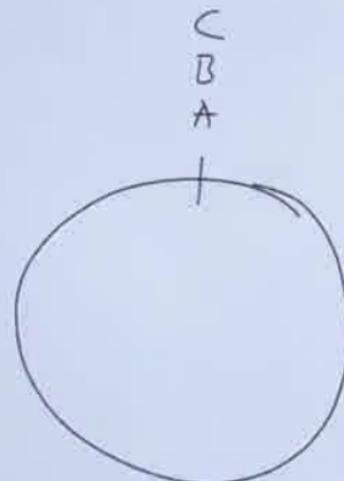
$$252 = 2^2 \cdot 3^2 \cdot 7^1$$

$$308 = 2^2 \cdot 7^1 \cdot 11^1$$

$$198 = 2^1 \cdot 3^2 \cdot 11^1$$

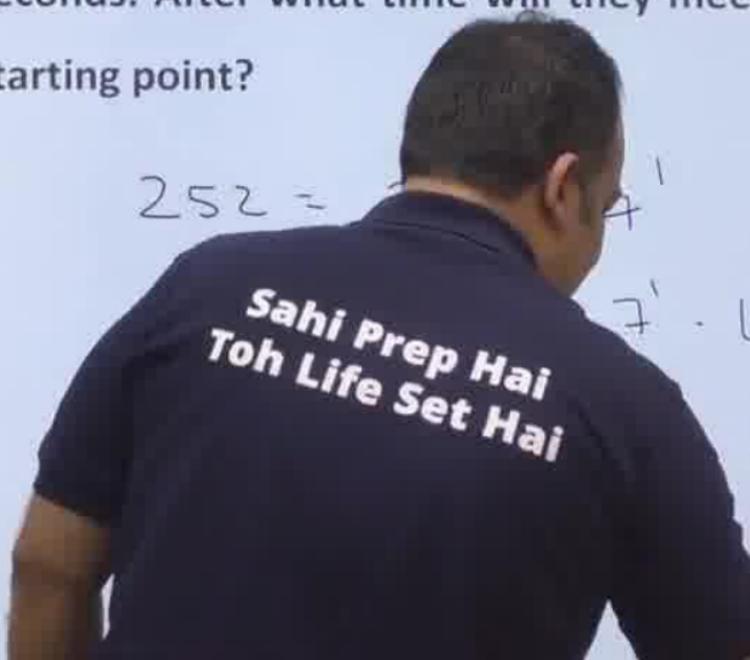
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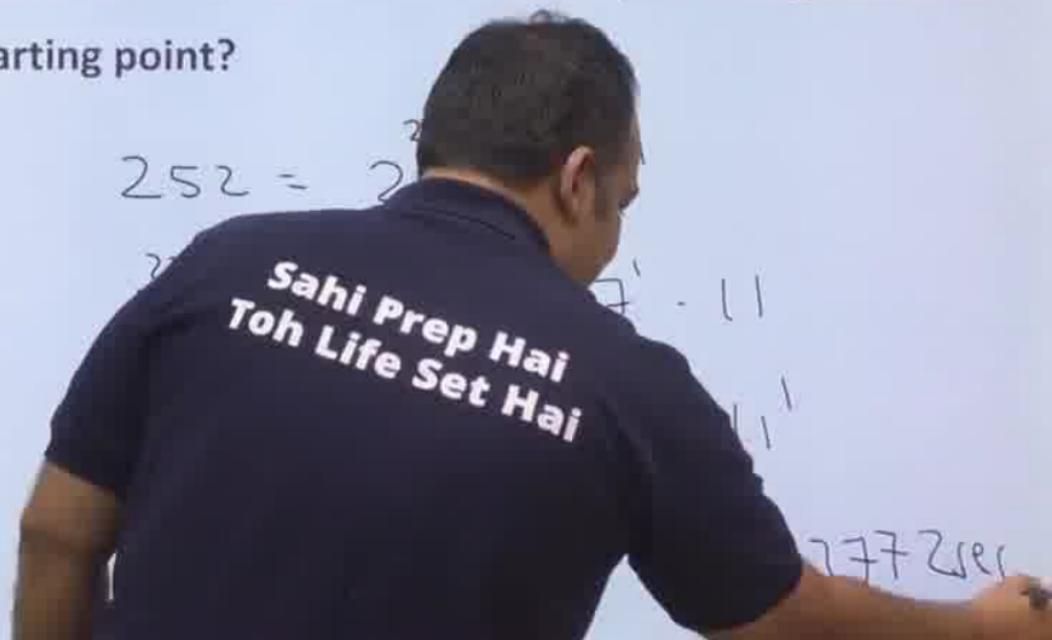
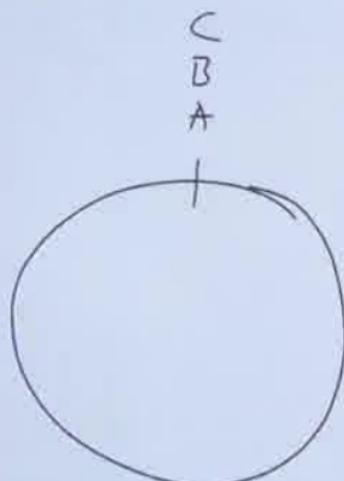


$$252 =$$

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Example: A, B, C start running at the same time and at the same point in a circular stadium. A complete a round in 252 seconds, B in 308 seconds and C in 198 seconds. After what time will they meet again at the starting point?



Answer: As A, B, C all running along a circular track from the same point and at same time.

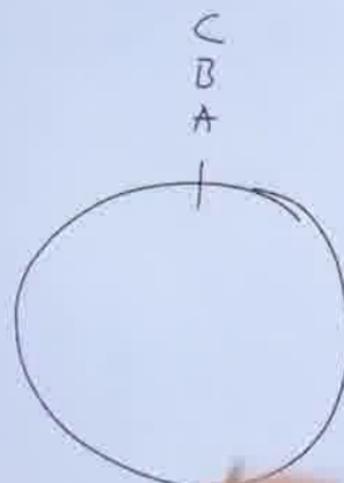
So A will reach at its starting point always after a multiple of 252 seconds similarly B and C after multiples of 308 and 198 seconds.

So required time for all of them to meet at the starting point is LCM of 252, 308 and 198 seconds

2	252, 308, 198
2	126, 154, 99
3	63, 77, 99
3	21, 77, 33
7	7, 77, 11
11	1, 11, 11
	1 1 1

$$\begin{aligned}&= 2 \times 2 \times 3 \times 3 \times 7 \times 11 = 2772 = 2772 \text{ seconds} \\&= 46 \text{ minutes } 12 \text{ seconds}\end{aligned}$$

Example: A, B, C start running at the same time and at the same point in a circular stadium. A complete a round in 252 seconds, B in 308 seconds and C in 198 seconds. After what time will they meet again at the starting point?



$$252 = 2^2 \cdot 3^2 \cdot 7^1$$

$$308 = 2^2 \cdot 7^1 \cdot 11^1$$

$$198 = 2^1 \cdot 3^2 \cdot 11^1$$

$$\text{L.C.M} = 2^2 \cdot 3^2 \cdot 7^1 \cdot 11^1 = \underline{\underline{2772 \text{ sec}}}$$

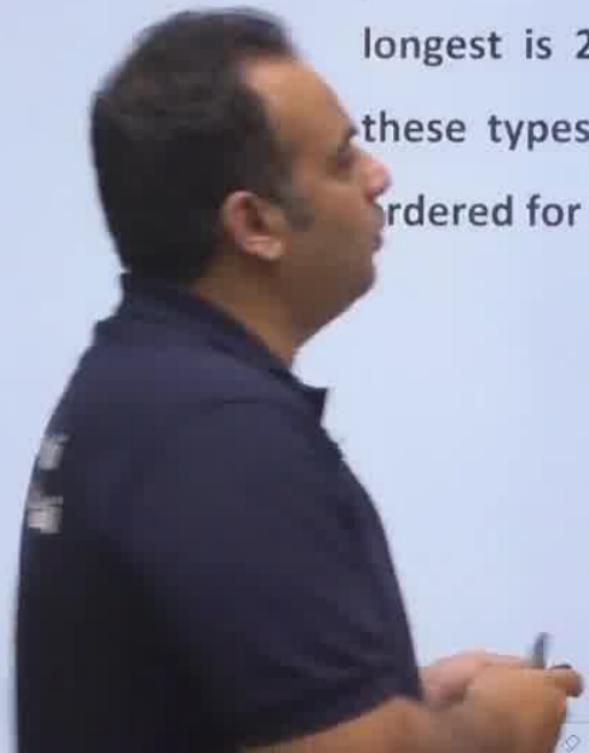
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252



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Example: A certain type of board is sold in lengths of multiples of 2 feet. The shortest board sold is 6 ft and the longest is 24 feet. A builder needs a large quantity of these types of board in $5\frac{1}{2}$ feet. Find the length to be ordered for which the waste is minimum.



Example: A certain type of board is sold in lengths of multiples of 2 feet. The shortest board sold is 6 ft and the longest is 24 feet. A builder needs a large quantity of types of board in $5\frac{1}{2}$ feet. Find the length to be cut for which the waste is minimum.



Ans: As the boards are sold in multiples of 2 feet and shortest board sold is 6 feet and longest board sold is 24 feet.

So board size that can be sold is

6, 8, 10, 12, 20, 22, 24

And the builder wants that the size of the board should be a multiple of $5\frac{1}{2}$ ie $5\frac{1}{2}$, $11, 16\frac{1}{2}, 22$

So for minimum waste the size should be a number which is a multiple of 2 and $5\frac{1}{2}$ both

LCM of 2 and $5\frac{1}{2}$

$$\text{LCM of } \frac{2}{1} \text{ and } \frac{11}{2} = \frac{\text{LCM of 2 and 11}}{\text{HCF of 1 and 2}} \Rightarrow \frac{22}{1} \Rightarrow 22$$

So length of the board to be ordered for minimum waste is 22 feet

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6, 8, 10, 12, 20, 22, 24

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$$\text{LCM of } \frac{2}{1} \text{ and } \frac{11}{2} = \frac{22}{1} \Rightarrow 22$$

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11, $16\frac{1}{2}$, 22

So for minimum waste the size of board is a number which is a multiple of 2 and $5\frac{1}{2}$ both

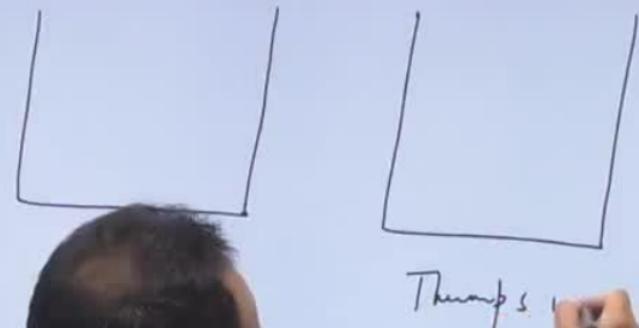
LCM of 2 and $5\frac{1}{2}$

$$\text{LCM of } \frac{2}{1} \text{ and } \frac{11}{2} = \text{LCM of } 1 \text{ and } 11 \Rightarrow 22$$

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So length of board required for minimum waste is 22 feet

No waste



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42 liter

60 liter

Thumps

Coke

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42 litres

Pepsi

60 litres

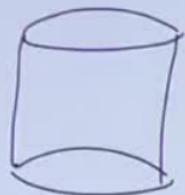
Thumps up

72 litres

Coke

mixing
many min cans

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42 litres

Pepsi

60 litres

Thums up

72 litres

Coke



No mixing



How many cans are reqd?

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42 liters

bts

60 liters

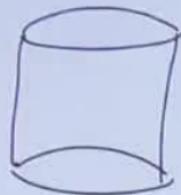
72 liters

Thumps up

Coke

o mix

min cans are req for this??



42 litres

60 litres

72 litres

P

Thumps up

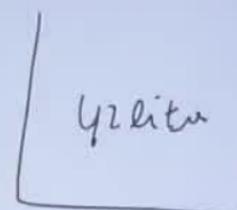
Coke

- No mixin
- How many cans are req for this??

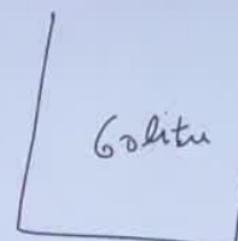
Sol^N

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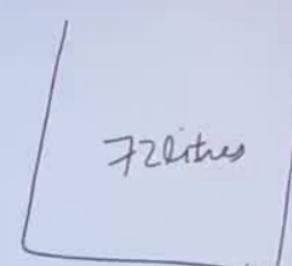
→ Factor



Pepsi



Thumps up



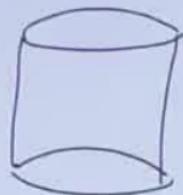
Coke

No m

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min cans are req for this??

Sign of can \rightarrow Factors of $(42, 60, 72)$



42 liters

Petrol

60 liters

Thumps up

72 liters

Coke

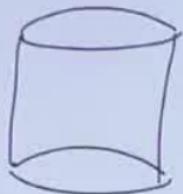
- No n
- How

in cars are req for this??

S

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→ factors of $(42, 60, 72)$



42 liters

60 liters

72 liters

Thumps up

Coke

- No mix
- How m

Sol^N

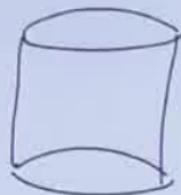
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cars

are req for this??

highest common

→ Factors (42, 60, 72)



42 liters

Pepsi

60 liters

Thums up

72 liters

Coke

- No mixin
- How many cans

are req for this??

Highest common

→ Factors of $(42, 60, 72)$

6

Sol N

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are req for this??

Highest Common Factor → Factors of $(42, 60, 72)$

$$\rightarrow \underline{6}$$



42 liters

60 liters

72 liters

Pepsi

7

Thums up

10

Coke

12

to mixing
How many

mix cans

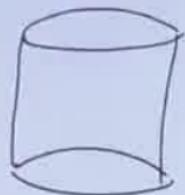
are req for this?

highest common

Can \rightarrow Factors of (42, 60, 72)

$$\begin{matrix} \nearrow & \searrow \\ \text{No of can} & \downarrow \end{matrix} \quad \begin{matrix} \nearrow & \searrow \\ & 6 \end{matrix}$$

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42 liters

Pepsi

60 liters

Thums up
10

72 liters

Coke
12

→ No mixing

→ How many bottles

are req for this??

Sol^N

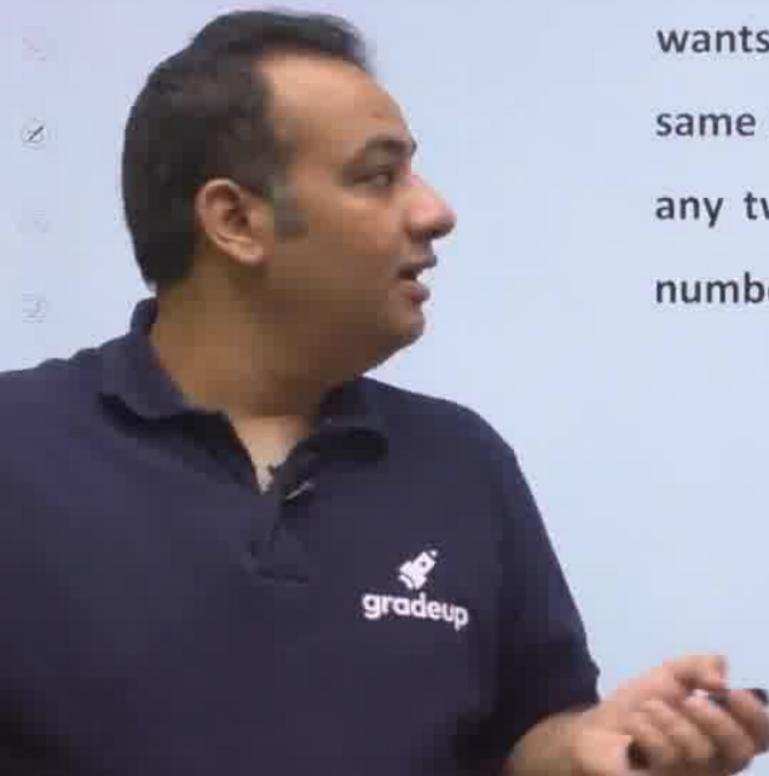
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Highest Common Factor of (42, 60, 72)

$$\begin{array}{r} 4 \\ \underline{\quad} \end{array}$$

$$\begin{array}{r} 2 \\ 9 \\ \underline{\quad} \end{array}$$

Example: A milk vendor has 21 litres of cow milk 42 litres of toned milk and 63 liters of double toned milk. If he wants to pack them in cans so that each can contains same number of litres of milk and does not want to mix any two kinds of milk in a can, then what is the least number of cans required?



Ans: As he wants to pack the milk in the cans so that each can contains same number of litres of milk.

So 21 litres of cow milk can be packed in packets of 1, 3, 7, 21 because these are factors of 21.

Similarly 42 and 63 can be packed in (1, 2, 3, 6, 7, 14, 21, 42) and (1, 3, 7, 9, 21, 63)

So to make size of all cans same we have to take common factors of (21, 42 and 63)
Common size can be (1, 3, 7, 21) but for least number of cans maximum size of each can is to be taken which is 21 litres.

Numbers of cans required

$$\frac{21}{21} + \frac{42}{21} + \frac{63}{21} = 1 + 2 + 3 \Rightarrow 6$$

—



Ques

Example: What is the least number of square tiles required to pave the floor of a room 42m and 24m broad.



Ans: As he wants to pack the milk in the cans so that each can contains same number of litres of milk.

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Numbers of cans required

$$\frac{21}{21} + \frac{42}{21} + \frac{63}{21} = 1 + 2 + 3 \Rightarrow \underline{\underline{6}}$$



Ques

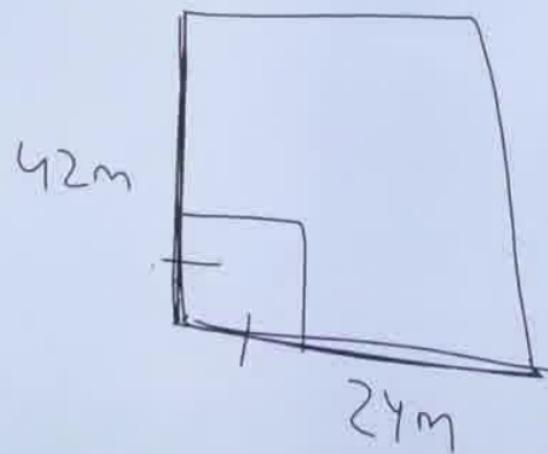
Example: What is the least number of square tiles required to pave the floor of a room 42m and 24m broad?



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Ques

Example: What is the least number of square tiles required to pave the floor of a room 42m and 24m broad.



$$\text{Size of Tile} = \text{HCF of } (42, 24)$$

$$= 6 \text{ m}$$

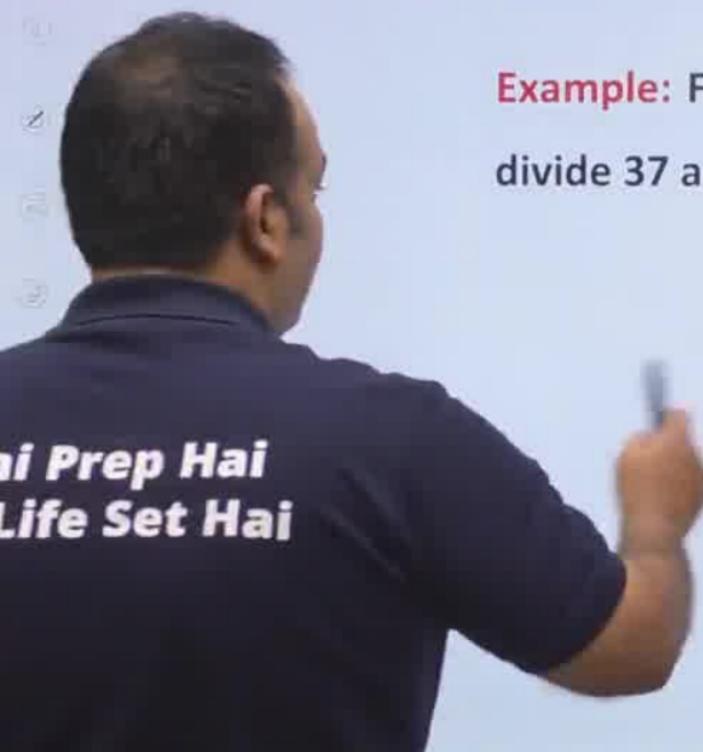
$$\text{No. of Tiles} = \frac{\text{Area of Floor}}{\text{Area of 1 Tile}}$$

$$= \frac{42 \times 24}{6 \times 6} = 28$$

HCF WITH REMAINDERS

Case I : When Remainders are given

Example: Find the greatest possible number with which when we divide 37 and 58 it leaves 2 and 3 as the respective remainders



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HCF WITH REMAINDERS

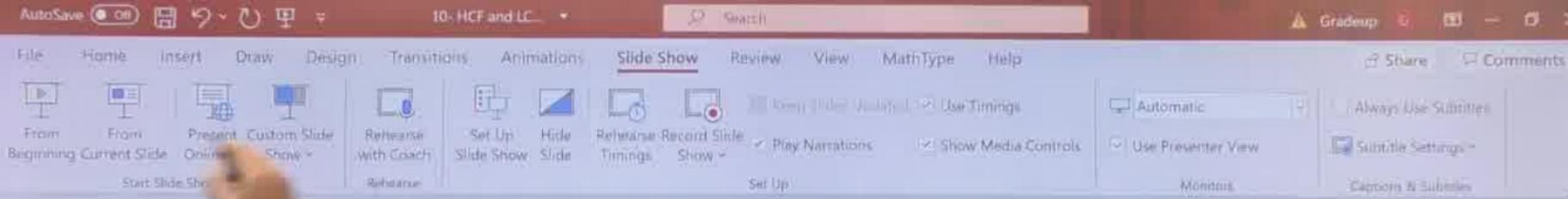
Case I : When Remainders are given

Example: Find the greatest possible number with which when we divide 37 and 58 it leaves 2 and 3 as the respective remainders

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11:34 AM



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- * Word Problems on
HCF & LCM → (28-30 min)
- * HCF & LCM with
Remainder → (30-32) min
- Practice Question
 $\frac{(7-8)Q}{}$ → (22-24) min

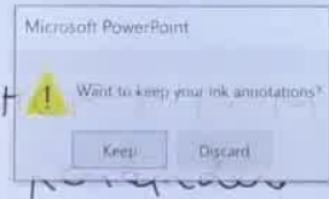
Step Hai
Set Hai

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Notes Display Settings

11:14 AM

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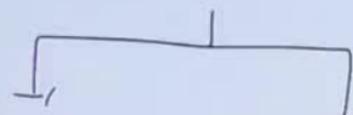
- * Word Problems on
HCF & LCM → (28-30 min)
- *  with → (30-32) min
- Practice Question
(7-8)Q → (22-24) min

MCF & LCM



HCF & LCM with Remainders

H C F



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HCF WITH REMAINDERS

Case I : When Remainders are given

Example: Find the greatest possible number with which when we divide 37 and 51 leaves 2 and 3 as the respective remainders

Largest possible value

$$\begin{array}{r} 37 \\ \hline -2 \\ 35 \end{array}$$

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Toh Life Set Hai**

HCF WITH REMAINDERS

Case I : When Remainders are given

Example: Find the greatest possible number with which when we divide 37 and 55 gives 2 and 3 as the respective remainders

Largest possible value of N

$$\begin{array}{r} 37 \\ \hline -2 \\ 35 \end{array}$$
$$\frac{35}{N} \quad R = 0$$
$$\begin{array}{r} 55 \\ \hline -3 \\ 52 \end{array}$$

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HCF WITH REMAINDERS

Case I : When Remainders are given

Ex : Find the greatest possible number with which when we divide 158 it leaves 2 and 3 as the respective remainders

Largest possible

$$\begin{array}{r} 35 \\ \hline N \\ R = 0 \end{array}$$

$$\begin{array}{r} 55 \\ \hline N \\ R = 0 \end{array}$$

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HCF WITH REMAINDERS

Case I : When Remainders are given

Example: Find the greatest possible number with which when we divide 37 and 58 it leaves 2 and 3 as the respective remainders

$$\begin{array}{r} 37 \\ \hline N \\ 35 \end{array} \quad R = 2 \quad \begin{array}{r} 35 \\ \hline N \\ 35 \end{array} \quad R = 0$$
$$\begin{array}{r} 58 \\ \hline N \\ 55 \end{array} \quad R = 3 \quad \begin{array}{r} 55 \\ \hline N \\ 55 \end{array} \quad R = 0$$

HCF WITH REMAINDERS

Case I : When Remainders are given

Example: Find the greatest possible number with which when we divide 37, it leaves 2 and 3 as the respective remainders

Largest possible $N = ?$

$$R = 2 \quad \frac{35}{N} \quad R = 0$$

$$R = 3 \quad \frac{55}{N} \quad R = 0$$

$$N = ?$$

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HCF WITH REMAINDERS

Case I : When Remainders are given

Example: Find the greatest possible number with which when we divide 37 and 58 it leaves 2 and 3 as the respective remainders

Largest possible
value of N

$$\frac{37}{N}$$

$$R =$$

$$\frac{35}{N}$$

$$R = 0$$

$$\frac{55}{N}$$

$$R = 0$$

$$(35, 55) = 5$$

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Ans: $\frac{37}{N}$ → Remainders = 2

$\frac{58}{N}$ → Remainders = 3

$$\begin{array}{r} \overline{)N\mid 37} \\ \overline{)2} \end{array} \quad \begin{array}{r} \overline{)N\mid 58} \\ \overline{)3} \end{array}$$

So If we subtract 2 from 37 ie 35 on division by N gives 0 as the Remainder similarly $(58 - 3) = 55$ on division by N gives 0 as the remainder.

$$\frac{35}{N} \text{ remainders} = 0 \text{ and } \frac{55}{N} \text{ remainders} = 0$$

So N is a factor of 35 and 55 ie N is a common factor and we have to find the greatest so we have to calculate HCF of 35 and 55.

HCF of 35 and 55 is 5

1. What is the greatest number which can divide
141, 186, 231 leaving the same remainder 1 in each
case?

- (A) 31
- (B) 5
- (C)
- (D) 35

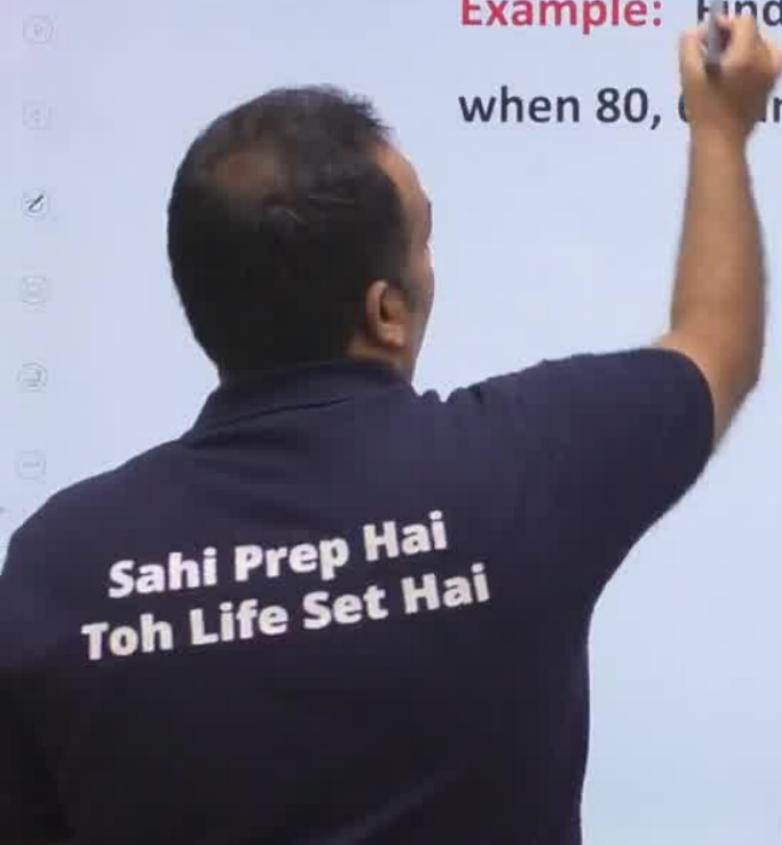
140, 185,

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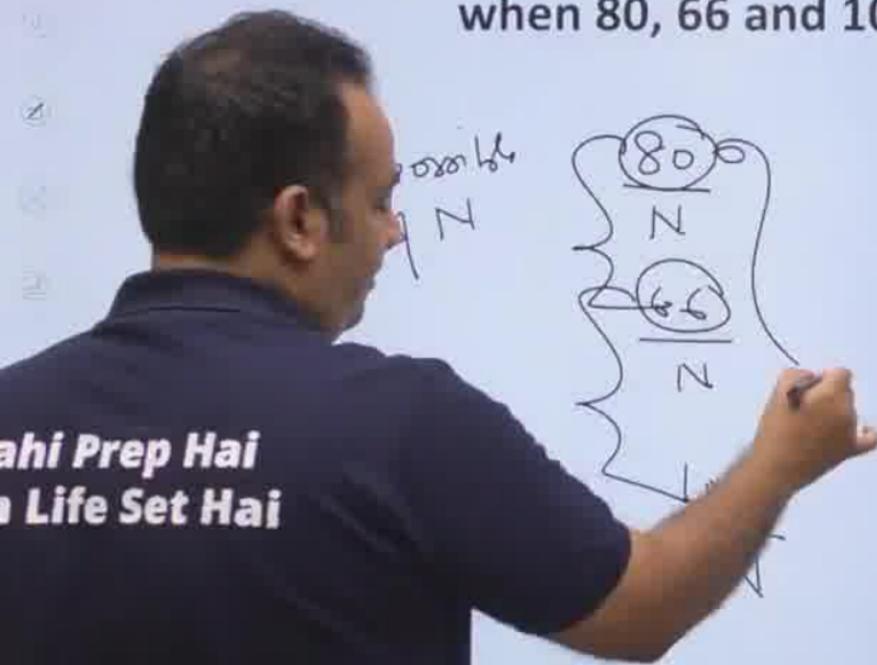
Case II : When Remainders are same but they are not given

Example: Find the largest possible number with which when 80, 88 and 108 are divided the remainders are same.



Case II : When Remainders are same but they are not given

Example: Find the largest possible number with which when 80, 66 and 108 are divided the remainders are same.



Rem

R

14, 42

R

R

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Case II : When Remainders are same but they are not given

Example: Find the largest possible number with which when 80, 66 and 108 are divided the remainders are same.

Largest possible
value of N

Rem

R

$$\text{HCF}(14, 42, 28)$$

R

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Ans: $\frac{80}{\text{---}}$

→ (R)

→ (R)

→ (R)

In this case, we take the HCF of differences of the given numbers.

HCF of $(80 - 66)$, $(108 - 66)$ and $(108 - 80)$

HCF of 14, 42 and 28 = 14

Hence 14 is the largest possible number which leaves same remainder when it divides 80, 108 and 66.

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Why we are taking the diff

$$\frac{N_1}{R} \quad R$$

$$N$$

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Toh Life Set Hai

Why we are taking the diff

$$\frac{N_1}{N} R$$

$$\frac{N_1 - R}{N}$$

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Why we are taking the diff

$$N_1 -$$

$$R$$

$$\frac{N_1 - R}{N}$$

$$\text{Rem} = 0$$

$$R$$

$$R$$

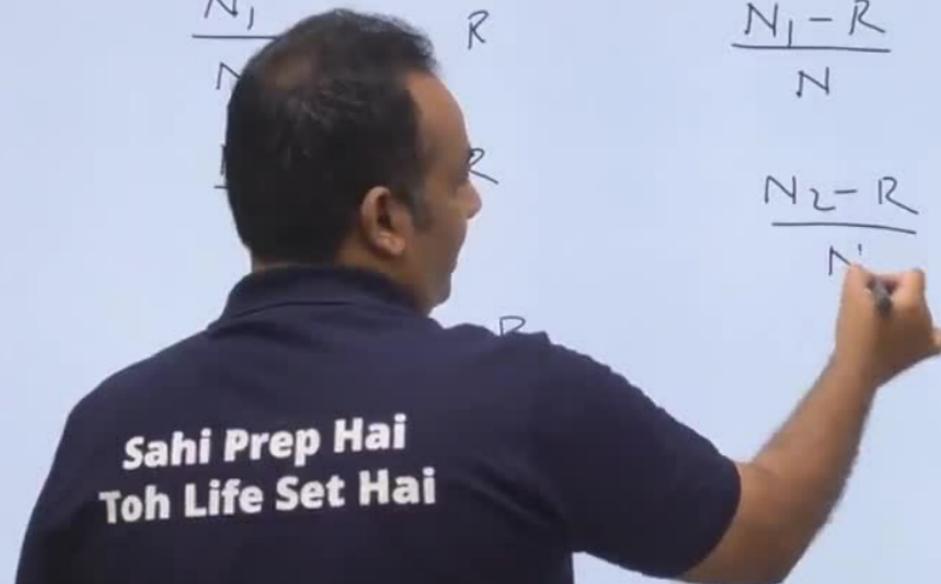
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why we are taking the diff

$$\frac{N_1}{N} R$$

$$\frac{N_1 - R}{N} \quad \text{Rem} = 0$$

$$\frac{N_2 - R}{N}$$



why we are taking the diff

N₁

R

$$\frac{N_1 - R}{N}$$

Rem = 0

R

$$\frac{N_2 - R}{N}$$

Rem = 0

R

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Toh Life Set Hai

why we are taking the diff

$$\frac{N_1}{N} R$$

$$\textcirclearrowleft \frac{N_1 - R}{N}$$

Rem = 0

$$\frac{N_2}{N} R$$

$$\textcirclearrowleft \frac{N_2 - R}{N}$$

Rem = 0

R

$$\frac{N_3 - R}{N}$$

Rem = 0

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why we are taking the diff

$$\frac{N_1}{N} R$$

$$\textcircled{C} \frac{N_1 - R}{N} \quad \text{Rem} = 0$$

$$\frac{N_2}{N} R$$

$$\textcircled{C} \frac{N_2 - R}{N} \quad \text{Rem} = 0$$

R

$$\textcircled{C} \frac{N_3 - R}{N} \quad \text{Rem} = 0$$

$$(N_1 - R_1)$$

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why we are taking the diff

12 $H \cdot x$

y

$H(y-x)$

$\left| \begin{array}{c} \frac{N_1}{N} \\ \frac{N_2}{N} \\ \frac{N_3}{N} \end{array} \right.$

R $\left(\begin{array}{c} N_1 - R \\ N_2 - R \\ N_3 - R \end{array} \right)$ Rem = 0

R $\left(\begin{array}{c} N_2 - R \\ N_3 - R \end{array} \right)$ Rem = 0

R $\left(\begin{array}{c} N_3 - R \end{array} \right)$ Rem = 0

HCF of $(N_1 - R, N_2 - R, N_3 - R)$

why we are taking the diff

$$12 = H \cdot x \quad \left| \begin{array}{c} \frac{N_1}{N} \\ \quad R \\ \end{array} \right. \quad \text{Rem} = 0$$

$$18 = H \cdot y \quad \left| \begin{array}{c} \frac{N_2}{N} \\ \quad R \\ \end{array} \right. \quad \text{Rem} = 0$$

$$18 - 12 = Hy - Hx \quad \left| \begin{array}{c} \frac{N_3 - R}{N} \\ \quad R \\ \end{array} \right. \quad \text{Rem} = 0$$

$$= 1 \quad \left(\begin{array}{c} N_1 - R \\ N_2 - R \\ N_3 - R \\ \hline N_1 - N_3 \end{array} \right)$$

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why we are taking the diff

$$12 = H \cdot x \quad \left| \begin{array}{c} \frac{N_1}{N} \\ R \\ \curvearrowright \frac{N_1 - R}{N} \end{array} \right. \quad \text{Rem} = 0$$

$$18 = H \cdot y \quad \left| \begin{array}{c} \frac{N_2}{N} \\ R \\ \curvearrowright \frac{N_2 - R}{N} \end{array} \right. \quad \text{Rem} = 0$$

$$\begin{aligned} 18 - 12 &= Hy - Hx \\ &= H(y-x) \end{aligned} \quad \left| \begin{array}{c} \frac{N_3}{N} \\ R \\ \curvearrowright \frac{N_3 - R}{N} \end{array} \right. \quad \text{Rem} = 0$$

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Practice Questions

- 1
- 2
- 3
- 4
- 5
- 6
- 7
- 8
- 9
- 10

2. Three drums contain 2527 litres, 1653 litres, and 2261 litres milk respectively. What is the biggest measure that can measure milk of each drum exactly?

- (A) 19 litre
- (B) 20 litre
- (C) 29 litre
- (D) 31 litre

HCF
Ques II

5. Let N be the greatest number that will divide 1305, 4665 and 6905 leaving the same remainder in each case. Then, sum of the digits in N is.

- (A) 4
- (B) 5
- (C) 6
- (D) 8

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33 C.

HCF
Ques II

5. Let N be the greatest number that will divide 1305, 4665 and 6905 leaving the same remainder in each case. Then, sum of the digits in N is.

- (A) 4
- (B) 5
- (C) 6
- (D) 8

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33(., 2)

HCF
Case II

5. Let N be the greatest number that will divide 1305, 4665 and 6905 leaving the same remainder in each case. Then, sum of the digits in N is.

- (A) 4
- (B) 5
- (C) 6
- (D) 8

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... , 2240

HCF
Con II

5. Let N be the greatest number that will divide 1305, 4665 and 6905 leaving the same remainder in each case. Then, sum of the digits in N is.

(A)

(C)

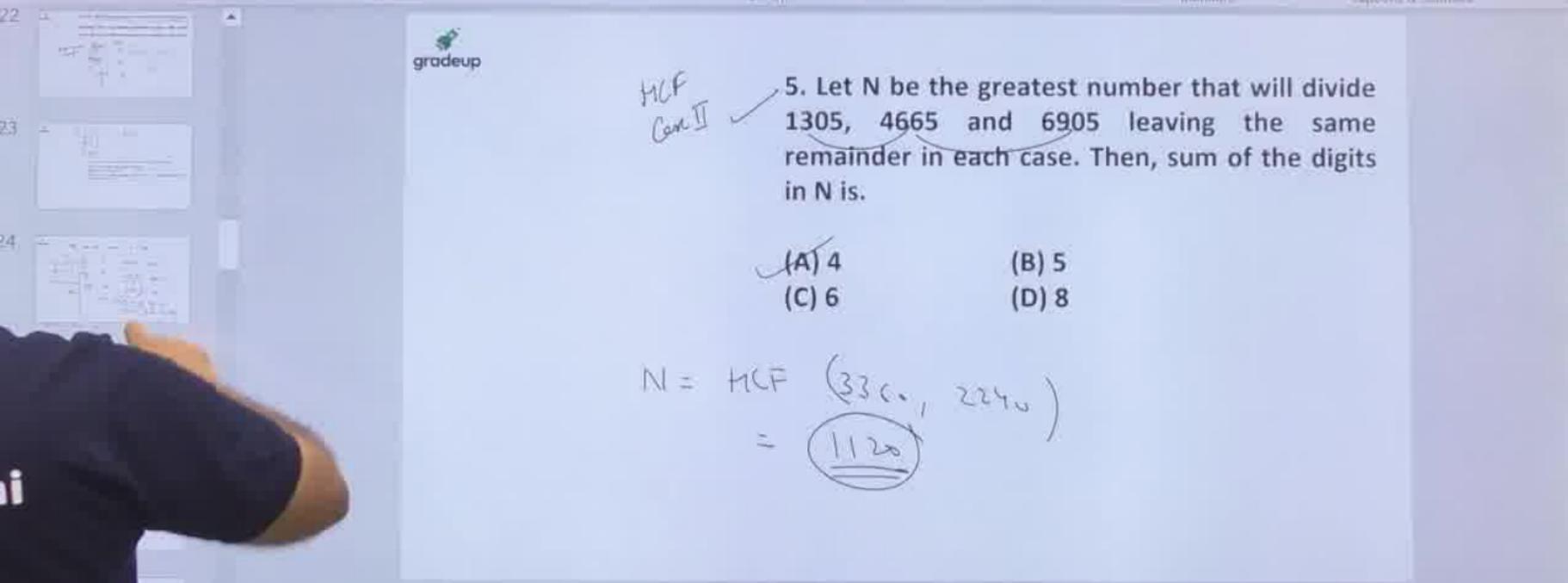
(B) 5

(D) 8



$$N = \text{HCF} (33\text{c}_0, 224_0)$$

1120



HCF **Com II** ✓ 5. Let N be the greatest number that will divide 1305, 4665 and 6905 leaving the same remainder in each case. Then, sum of the digits in N is.

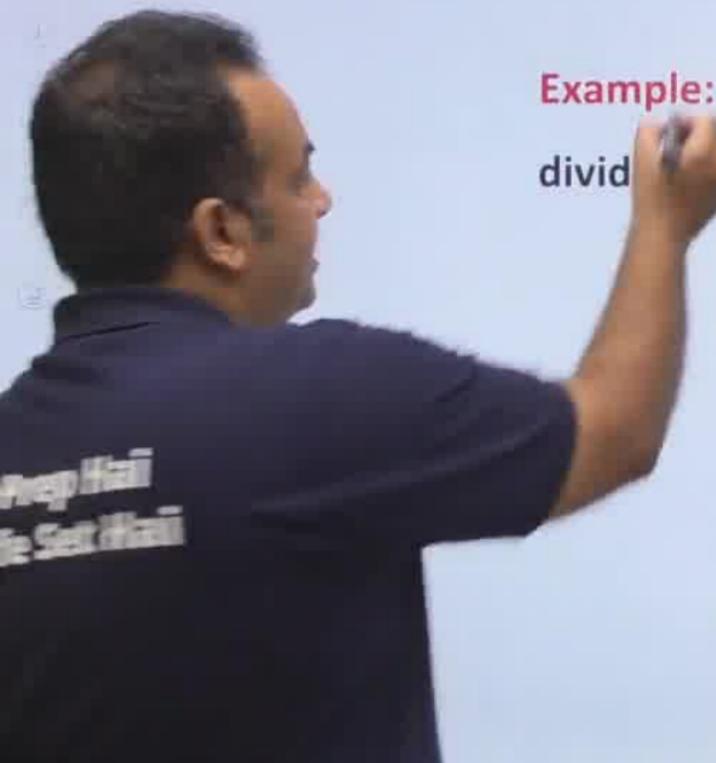
$$N = \text{HCF} \quad (330, 224) \\ = \boxed{\underline{1120}}$$

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LCM WITH REMAINDERS

Case I : When Remainders are same

Example: What is the least possible number which when divided by 7 and 8 in each case, it leaves the remainders 2?



LCM WITH REMAINDERS

Case I : When Remainders are same

Q: What is the least possible number which when divided by 7 and 8 in each case, it leaves the remainders 2?

Lowest

N

$$\frac{N}{7}$$

$$R = 2$$

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LCM WITH REMAINDERS

Case I : When Remainders are same

Example: What is the least possible number which when divided by 7 and 8 in each case, it leaves the remainders 2?

Lowest

$$\frac{N}{7} \quad R = (2)$$

2

LCM WITH REMAINDERS

Case I : When Remainders are same

Example: What is the least possible number which when divided by 7 and 8 in each case has the remainders 2?

Lowest
Number

$$\begin{array}{c} N \\ \hline 7 \end{array}$$

$R = 2$

$2 + c$

$\left\{ \begin{array}{l} N \\ 8 \end{array} \right.$

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LCM WITH REMAINDERS

Case I : When Remainders are same

Example: What is the least possible number which when divided by 7 and 8 in each case leaves the remainders 2?

Lowest
Number

$$\begin{array}{r} N \\ \hline 7 | \textcircled{2} \\ \textcircled{N} \end{array}$$

2 + 56

58

A man in a dark polo shirt with the text "Sahi Prep Hai Toh Life Set Hai" on the back is writing on the board.

LCM WITH REMAINDERS

Case I : When Remainders are same

Example: What is the least possible number which when divided by 7 and 8 in each case, it leaves the remainders 2?

$$\begin{array}{r} N \\ \hline 7) \overline{)R+2} \\ R = 2 \end{array}$$

$$\begin{aligned} & 2 + 56 \\ & = 58 \\ & \text{Smallest no} \end{aligned}$$

LCM WITH REMAINDERS

Case I : When Remainders are same

Example : What is the least possible number which when divided by 7 and 8 in each case, it leaves the remainders 2?

Lowest
Number

$$R = 2$$

$$2 + 56$$

$$= 58$$

Smallest no

Ans: $\frac{N}{7} \rightarrow \text{Remainder} = 2$

$\frac{N}{8} \rightarrow \text{Remainder} = 2$

As N is a number which on division by 7 gives a remainder of 2, it means N is 2 more than a multiple of 7 similarly N is 2 more than a multiple of 8.

So N is 2 more than a common multiple of 7 and 8.

least possible value of N

$= \underline{\text{LCM of 7 and 8}} + 2$

$= 56 + 2$

$= 58$

General form of N

$N = 56m + 2 \quad \text{where } (m = 0, 1, 2, \dots)$

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Ans: $\frac{N}{7} \rightarrow \text{Remainder} = 2$

$\frac{N}{8} \rightarrow \text{Remainder} = 2$

As N is a number which on division by 7 gives a remainder of 2, it means N is 2 more than a multiple of 7 similarly N is 2 more than a multiple of 8.

So N is 2 more than a common multiple of 7 and 8.

For least possible value of N

$N = (\underline{\text{LCM of 7 and 8}}) + 2$

$N = 56 + 2$

$N = 58$

So General form of N

$N = 56m + 2 \quad m \in \{1, 2, \dots\}$

General form of N
 $+ 56m$
0, 1, 2,

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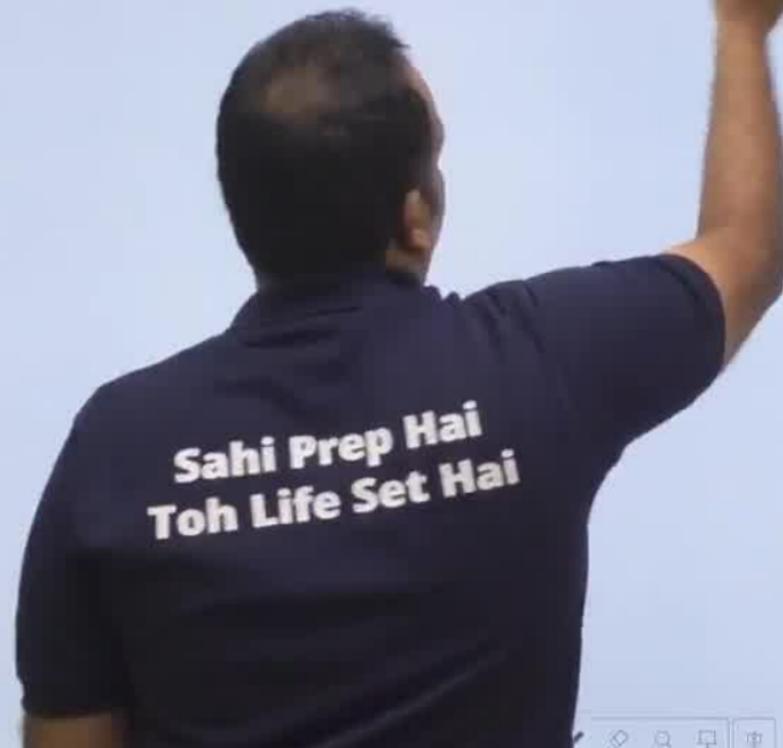
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eg

N

eg

$$\frac{N}{5} \quad R = 2$$



eg

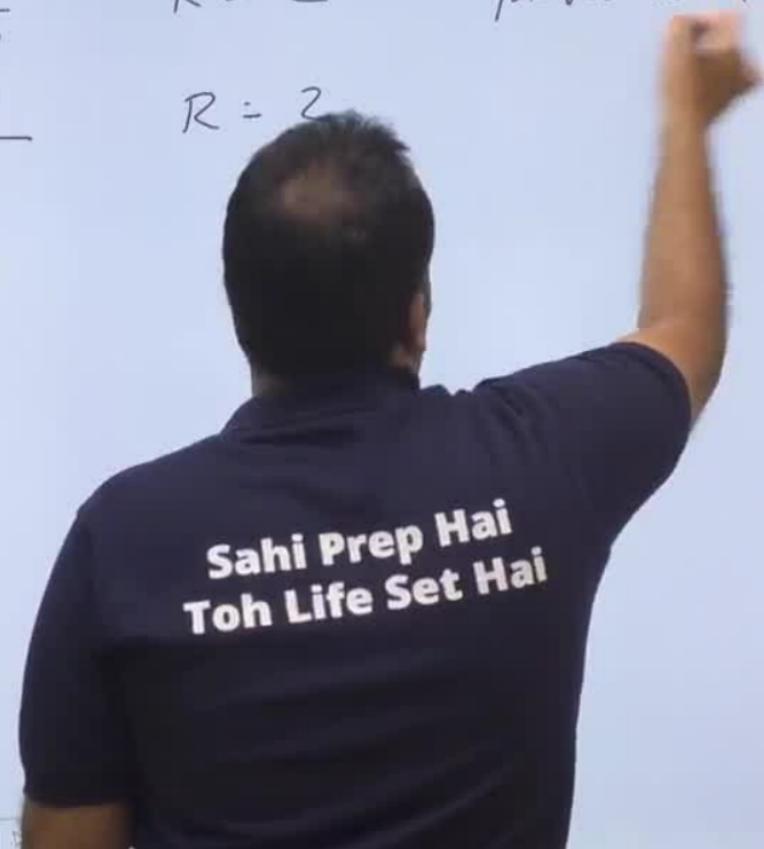
$$\frac{N}{5}$$

$$R = 2$$

General Form

$$\frac{N}{7}$$

$$R = 2$$



eg

$$\begin{array}{r} N \\ \hline 5 \\ N \\ \hline 7 \end{array}$$

$$R = 2$$

General Form

$$R = 2$$

$$2 + 35m$$

eg

$$\begin{array}{r} N \\ \hline 8 \end{array}$$

$$R = 3$$

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eg

$$\left\{ \begin{array}{c} \frac{N}{5} \\ \frac{N}{3} \end{array} \right.$$

$$R = 2$$

$$R = 2$$

General Form

$$2 + 35m$$

$$\frac{N}{8} \quad R = 3$$

$$\frac{N}{6} \quad R = 3$$

eg

$$\left\{ \begin{array}{c} N \\ \hline 5 \\ \hline N \\ \hline 3 \end{array} \right.$$

$$R = 2$$

$$R = 2$$

General Form

$$2 + 35m$$

eg

$$\frac{N}{8}$$

3

General

Sahi Prep Hai
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eg

$$\begin{array}{c} N \\ \hline 5 \\ \left\{ \begin{array}{c} N \\ \hline 3 \end{array} \right. \end{array}$$

$$R = 2$$

General Form

$$R = 2$$

$$2 + 35m$$

eg

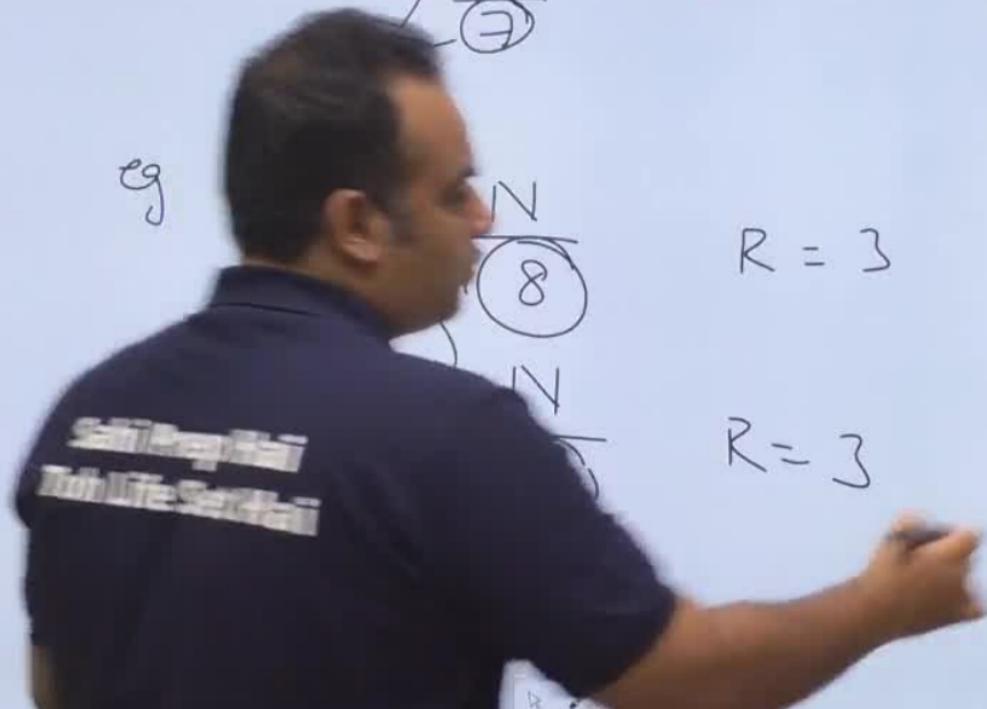
$$\begin{array}{c} N \\ \hline 8 \\ \left\{ \begin{array}{c} N \\ \hline 1 \end{array} \right. \end{array}$$

$$R = 3$$

General Form

$$3 +$$

$$R = 3$$



eg

$$\left\{ \begin{array}{c} N \\ \hline 5 \\ \hline N \\ \hline 3 \end{array} \right.$$

$$R = 2$$

General Form

$$R = 2$$

$$2 + 35m$$

$$\left\{ \begin{array}{c} N \\ \hline 2 \end{array} \right.$$

$$R = 3$$

General Form

$$3 + 24m$$

$$\left\{ \begin{array}{c} N \\ \hline 6 \end{array} \right.$$

$$R = 3$$

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eg

$$\left\{ \begin{array}{l} N \\ \textcircled{5} \\ N \\ \hline G \end{array} \right. \quad R = 2$$

General Form

$$2 + 35m$$

eg

$$\left\{ \begin{array}{l} N \\ \textcircled{1} \\ N \\ \hline D \end{array} \right. \quad R = 3$$

 $m \rightarrow 0$ General Form

$$3 + 24m$$

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eg

$$\left\{ \begin{array}{l} \frac{N}{5} \\ \frac{N}{3} \end{array} \right. \quad R = 2$$

General Form

$$2 + 35m$$

$$m \rightarrow 0, 1$$

eg

$$\left\{ \begin{array}{l} \frac{N}{5} \\ \frac{N}{3} \end{array} \right. \quad R = 3$$

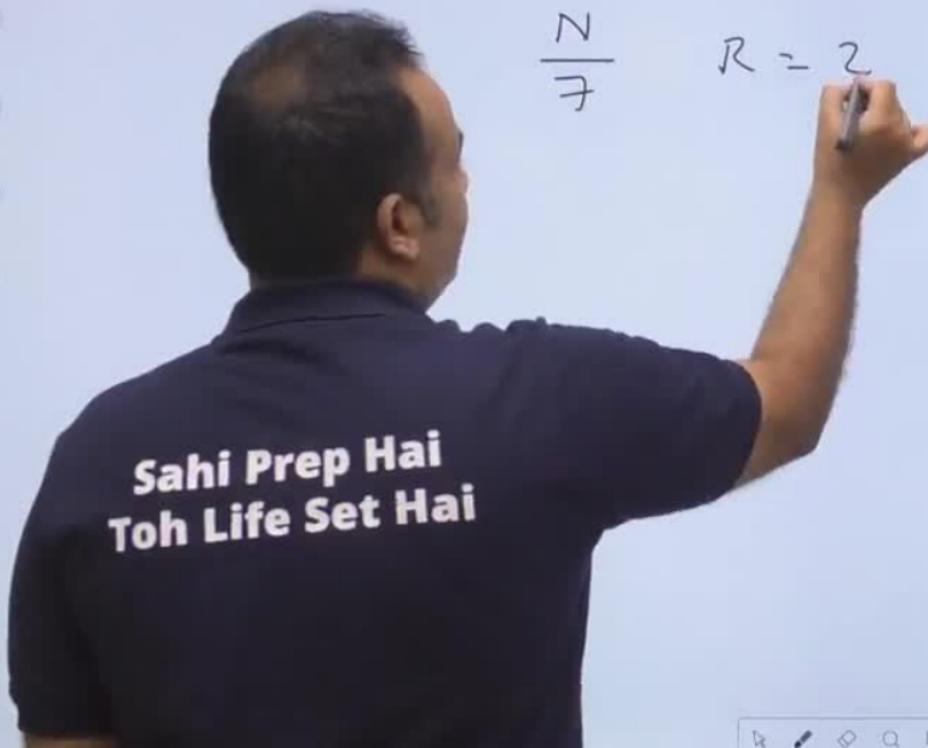
General Form

$$3 + 24m$$

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Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$\frac{N}{7} \quad R = 2$$



Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$R = 2$$

$$\frac{N}{?}$$

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Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

 $\frac{N}{7}$

$$R = 2$$

 $\frac{N}{8}$

$$R = 2$$

General

**Sahi Prep Hai
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Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

N

$$R = 2$$

$$\frac{N}{8}$$

$$R = 2$$

General Form

$$2 +$$

$$\begin{array}{r} 999 \\ \hline 9 \end{array}$$

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Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$\frac{N}{7} \quad R = 2$$

$$\frac{N}{8} \quad R = 2$$

General Form

2 +

$$\begin{array}{r} 1 \\ \hline 56 \Big) 9999 \\ 56 \\ \hline 432 \end{array}$$

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Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$\begin{array}{r} N \\ R = 2 \\ \hline 8 | N \\ R = 2 \end{array}$$

General Form

$$\begin{array}{r} 17 \\ \hline 56 | 9919 \\ 56 \\ \hline 439 \end{array}$$

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Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$\frac{N}{7} \quad R = 2$$

$$\frac{N}{8} \quad R = 2$$

General Form

2 +

$$\begin{array}{r} 17 \\ \hline 56 \left| \begin{array}{r} 9999 \\ -56 \\ \hline 439 \\ -392 \\ \hline 7 \end{array} \right. \end{array}$$

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Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

General Form

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$$\begin{array}{r} N \\ R = 2 \\ \hline 8 \end{array}$$

$$\begin{array}{r} 17 \\ \hline 56 \left| \begin{array}{r} 9999 \\ -56 \\ \hline 439 \\ -392 \\ \hline 47 \end{array} \right. \end{array}$$

Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$\frac{N}{7}$$

$$R = 2$$

$$\frac{N}{8}$$

$$R = 2$$

General Form

$$2 + 5x$$

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$$\begin{array}{r} 178 \\ \hline 9999 \\ 56 \\ \hline 439 \\ 392 \\ \hline 479 \\ 448 \\ \hline 31 \end{array}$$

Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$\frac{N}{7}$$

$$R = 2$$

$$\frac{N}{8} \quad R = 2$$

Given

$$\begin{array}{r} 178 \\ \hline 56 \left| \begin{array}{r} 9999 \\ -56 \\ \hline 439 \\ -392 \\ \hline 479 \\ -448 \\ \hline 31 \end{array} \right. \end{array}$$

Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

N R = 2 $\frac{N}{8}$ R = 2

General

2

$$\begin{array}{r} 178 \\ \hline 56 \longdiv{9999} \\ 56 \\ \hline 43 \\ 42 \\ \hline 1 \\ \end{array}$$

9999 - 31

$$\begin{array}{r} 9968 \\ \hline \end{array}$$

Example: Find the largest 4 digit number which on division by 7 and 8 gives 2 as the remainder in each case.

$$\frac{N}{7}$$

$$R = 2$$

$$\frac{N}{8}$$

$$R = 2$$

General Form

$$2 + 56m$$

$$56 \overline{)99} \quad 17$$

$$9999 - 31$$

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$$\begin{array}{r}
 9968 \\
 \hline
 + 2 \\
 \hline
 \end{array}$$

Ans: As we have seen the general form $N = 56m + 2$ in previous example, Now we have to find the largest 4 digit number.

$$\begin{array}{r} 178 \\ 56 \overline{)9999} \\ 56 \\ \hline 439 \\ 392 \\ \hline 479 \\ 448 \\ \hline 31 \end{array}$$

Largest 4 digit number is 9999

So $9999 \div 56$

So 9999 on division by 56 gives 31 as the remainder

$9999 - 31 = 9968$ is a multiple of 56

So largest 4 digit number which satisfy the above conditions is
 $9968 + 2 = 9970$

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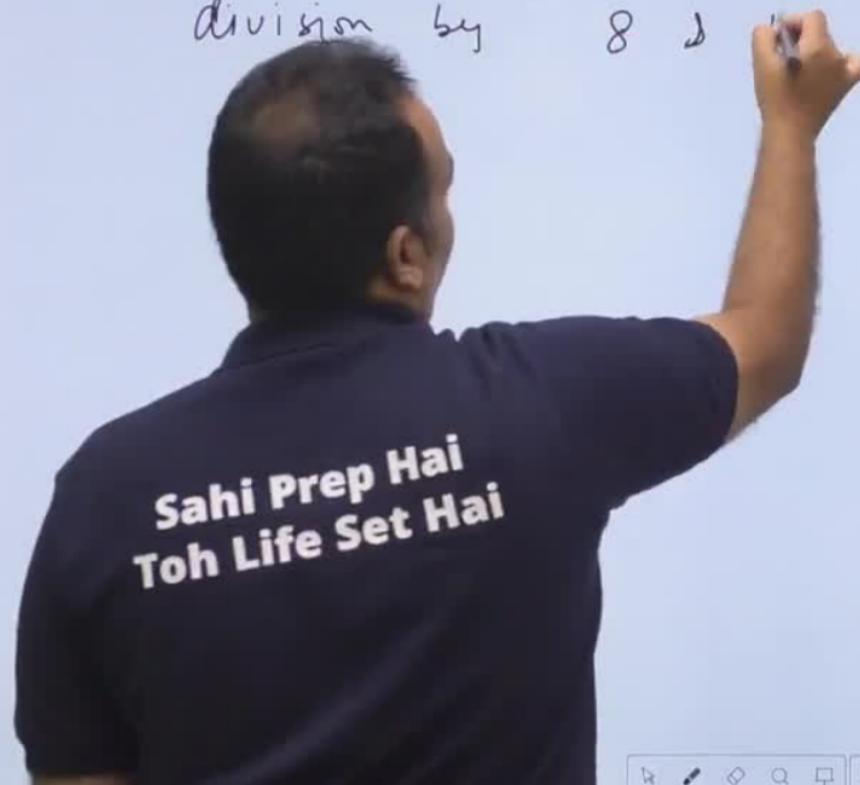
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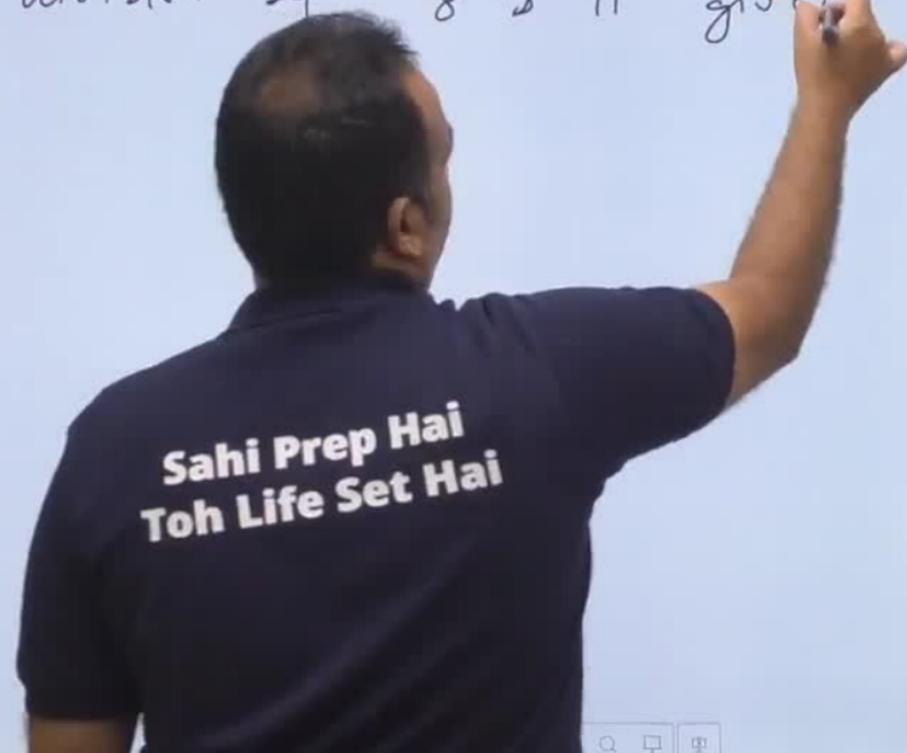
eg Find the smal



eg Find the smallest 5 digit no which on
division by 8 leaves remainder 3.



eg Find the smallest 5 digit no which on
division by 8 & 11 gives



eg Find the smallest 5 digit no which on
division by 8 & 11 gives 3 as the remainder
in $\square \square \square \square \square$?

$$\equiv 3$$

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eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case?

$$\frac{N}{8} \quad R = 3$$

$$\frac{N}{11} \quad R = ?$$

$$\begin{array}{r} 11 \\ \hline 88 \left| \begin{array}{r} 1000 \\ -88 \\ \hline 120 \end{array} \right. \end{array}$$

General Form

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eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case ??

$$\frac{N}{8} \quad R = 3$$

$$\frac{N}{11} \quad R = 3$$

General Form →

$$\begin{array}{r}
 & 1 & 1 & 3 \\
 \hline
 & 0 & 0 & 0 & 0 \\
 8 & \overline{)1} & 1 & 3 \\
 & - & 8 & 8 \\
 \hline
 & & 1 & 2 & 0 \\
 & & 8 & 8 \\
 \hline
 & & 3 & 2 & 0 \\
 & & 2 & 6 & 4 \\
 \hline
 & & & & 5
 \end{array}$$

*Sahi Prep Hai
Toh Life Set Hai*

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case?

$$\frac{N}{8} \quad R = 3$$

$$\frac{N}{11} \quad R = 3$$

+ 88 m

$$\begin{array}{r}
 & 1 & 1 & 3 \\
 88 & \overline{)10000} \\
 & 88 \\
 \hline
 & 120 \\
 & 88 \\
 \hline
 & 320 \\
 & 264 \\
 \hline
 & 56
 \end{array}$$

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case.

$$\frac{N}{8} \quad R$$

$$\frac{N}{11}$$

General

**Sahi Prep Hai
Toh Life Set Hai**

$$\begin{array}{r} 113 \\ \hline 88 | 10000 \\ 88 \\ \hline 120 \\ 88 \\ \hline 320 \\ 264 \\ \hline 56 \end{array}$$

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case

$$\frac{N}{8} \quad R = 3$$

$$\frac{N}{11} \quad R = 3$$

$$\begin{array}{r}
 & 113 \\
 88 & \overline{)10000} \\
 & 88 \\
 \hline
 & 120 \\
 & 88 \\
 \hline
 & 32 \\
 & 264 \\
 \hline
 & 56
 \end{array}$$

General Form

**Sahi Prep Hai
Toh Life Set Hai**

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case ??

$$\frac{N}{8} \quad R = 3$$

$$\frac{N}{11} \quad R$$

General Form

*Sahi Prep Hai
Toh Life Set Hai*

$$\begin{array}{r}
 & 113 \\
 88 \sqrt{10000} \\
 -88 \\
 \hline
 120 \\
 -88 \\
 \hline
 320 \\
 -264 \\
 \hline
 56
 \end{array}$$

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case

$$\frac{N}{8}$$

$$\frac{N}{11}$$

Genus

Sahi Prep Hai
Toh Life Set Hai

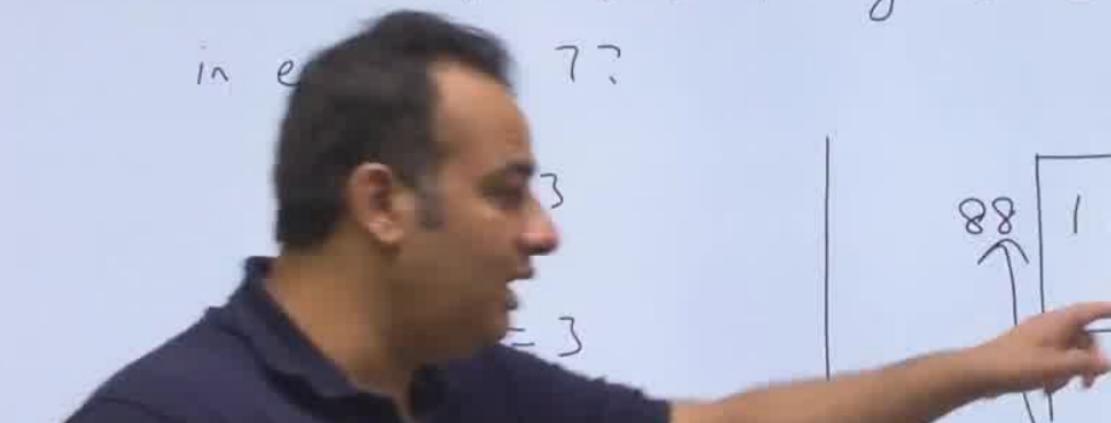
$$\begin{array}{r} 113 \\ \hline 88 | 10000 \\ 88 \\ \hline 120 \\ 88 \\ \hline 320 \\ 264 \\ \hline 56 \end{array}$$

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case?

$$\begin{array}{r} 113 \\ \hline 88 \quad | \quad 10000 \\ 88 \\ \hline 120 \\ 88 \\ \hline 320 \\ 264 \\ \hline 56 \end{array}$$

10032

56

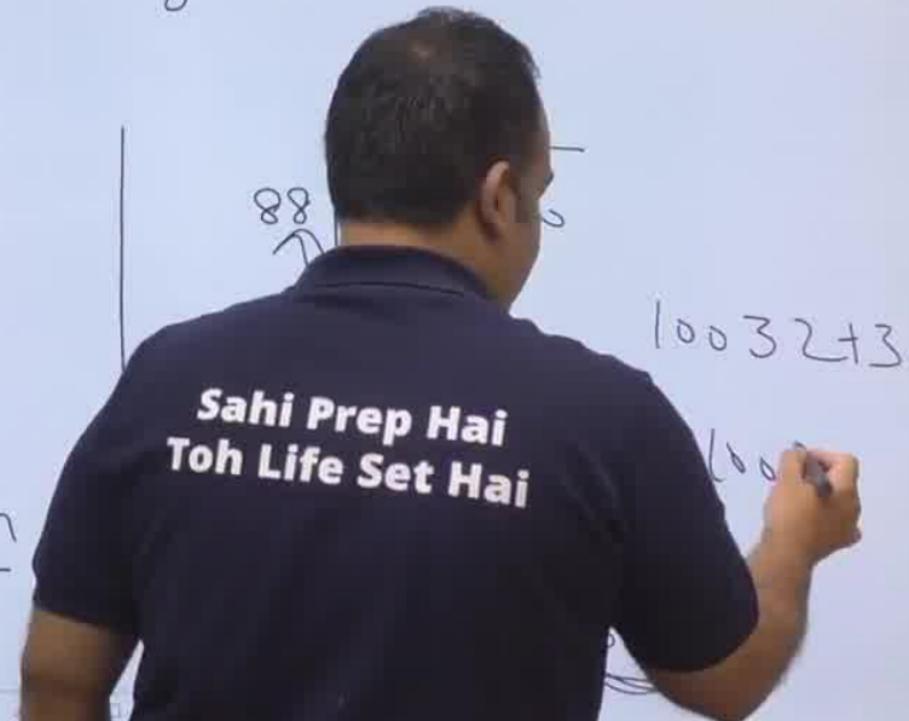


eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case?

$$\frac{N}{8} \ R = 3$$

$$\frac{N}{11} \ R = 3$$

General Form $\rightarrow 3 + 88m$



Case II : When the remainders are different for different divisors but the respective difference between the divisors and the remainders remain constant.

Example: What is the least possible number which when divided by 7 or 8 leaves a remainder of 3 and 4 respectively.

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the smallest 5 digit no. which on
8 & 11 gives 3 as the remainder
in each case ??

$$\frac{N}{8} \quad R=3$$

$$\frac{N}{11} \quad R=3$$

General Form $\rightarrow 3 + 88m$

$$\begin{array}{r} 113 \\ 10000 \\ \hline 88 \\ 120 \\ \hline 88 \\ 320 \\ \hline 24 \\ \hline 54 \end{array}$$

10032+3
10035

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10-HCF and LC

12:04 PM

What smallest no. 87

$$\begin{array}{r} 2 \\ 8 \sqrt{21} \\ \hline 16 \\ \hline 5 \end{array}$$

Sahi Prep Hai
Toh Life Set Hai

What smallest no. should be added to 21 so that

$$\begin{array}{r} 2 \\ 8 \sqrt{21} \\ \underline{-16} \\ 5 \end{array}$$

it become a multiple of 8

$$\underline{21+3}$$

$$\begin{array}{r} = 24 \\ \hline \end{array}$$

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case?

$$\frac{N}{8} \ R = 3$$

$$\frac{N}{11} \ R = 3$$

General Form $\rightarrow 3 + 88m$

113

10000
88 |
 88
 120
 88
 320
 264
 5

10032 ÷ 88

113

10035

5

eg Find the smallest 5 digit no which on division by 8 & 11 gives 3 as the remainder in each case

$$\frac{N}{8} \quad R = 3$$

$$\frac{N}{11} \quad R = 3$$

General Form

$$\begin{array}{r}
 & 113 \\
 \overline{)10000} \\
 & 88 \\
 \hline
 & 120 \\
 & 88 \\
 \hline
 & 320 \\
 & 320 \\
 \hline
 & 0 \\
 \end{array}$$

10032 + 3

10035

5

Case II : When the remainders are different for different divisors but the respective difference between the divisors and the remainders remain constant.

Example: What is the least possible number which when divided by 7 or 8 leaves a remainder of 3 and 4 respectively.

$$\begin{array}{c} N \\ \textcircled{7} \\ \textcircled{R-3} \\ N \\ \textcircled{R-4} \end{array}$$

Sahi Prep Hai
Toh Life Set Hai

Case II : When the remainders are different for different divisors but the respective difference between the divisors and the remainders remain constant.

Example: What is the smallest possible number which when divided by 7 or 8 leaves a remainder of 3 and 4 respectively.

$$7 - 3 = 4$$

$$8 - 4 = 4$$

Sahi Prep Hai
Toh Life Set Hai

Ans: $\frac{N}{7}$ Remainders = 3 Difference
 $7 - 3 = 4$

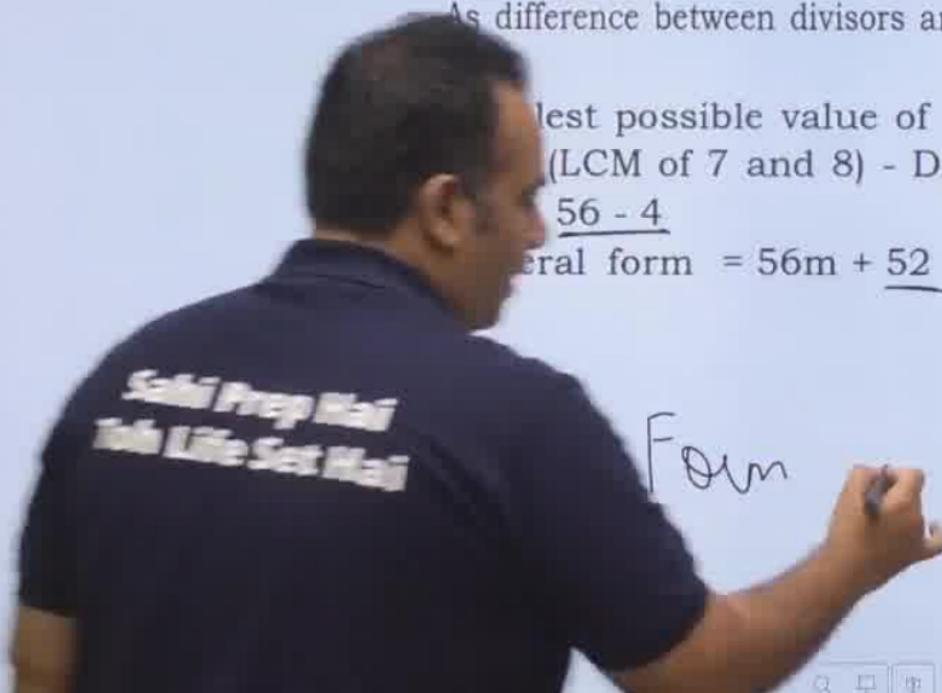
$$\frac{N}{8} \text{ Remainders} = 4 \quad 8 - 4 = 4$$

As difference between divisors and remainders is same, So Case II can be used.

lest possible value of N
(LCM of 7 and 8) - Difference

$$\underline{56 - 4}$$

General form = $56m + \underline{52}$



LCM
Con-I

4. Let the least number of six digits which when divided by 4, 6, 10, 15 leaves in each case same remainder 2 be N. the sum of digits in N is.

- (A) 3 (B) 5
- (C) 4 (D) 6

General Form

 $\rightarrow 2 +$

LCM
Con-I

4. Let the least number of six digits which when divided by 4, 6, 10, 15 leaves in each case same remainder 2 be N. the sum of digits in N is.

$$\begin{array}{r} N \\ \hline 4 \\ \textcircled{1} \end{array}$$

$$R = 2$$

$$\begin{array}{r} N \\ \hline 6 \\ \textcircled{2} \end{array}$$

$$R = 2$$

$$\begin{array}{r} N \\ \hline 10 \\ \textcircled{3} \end{array}$$

$$\begin{array}{r} N \\ \hline 15 \\ \textcircled{4} \end{array}$$

(B) 5

(D) 6

General Form

$$2 + 60m$$

Sahi Prep Mai
Toh Life Set Hai

LCM
Case-I

4. Let the least number of six digits which when divided by 4, 6, 10, 15 leaves in each case same remainder 2 be N. the sum of digits in N is.

$$R = 2$$

$$R = 2$$

$$R = 2$$

- (A) 3
(C) 4

- (B) 5
(D) 6

General Form

$$\rightarrow \underline{2 + 60m}$$

$$\begin{array}{r}
 166 \\
 60 \overline{)10000} \\
 -60 \\
 \hline
 400 \\
 -360 \\
 \hline
 40
 \end{array}
 \quad 10020 +$$

LCM
Ques-1

4. Let the least number of six digits which when divided by 4, 6, 10, 15 leaves in each case same remainder 2 be N. the sum of digits in N is.

$$\begin{array}{r} N \\ \hline 4 \\ \hline \end{array}$$

$$R = 2$$

$$\begin{array}{r} N \\ \hline 6 \\ \hline \end{array}$$

$$R = 2$$

$$\begin{array}{r} N \\ \hline 10 \\ \hline \end{array}$$

$$R = 2$$

$$\begin{array}{r} N \\ \hline 15 \\ \hline \end{array}$$

$$R = 2$$

- (A) 3
(C) 4

- (B) 5
(D) 6

General Form



Sahi Prep Hai
Toh Life Set Hai

$$10020 + 2$$

$$(100)$$

LCM
Con-1

4. Let the least number of six digits which when divided by 4, 6, 10, 15 leaves in each case same remainder 2 be N. the sum of digits in N is.

$$\begin{array}{c} N \\ \hline 4 \\ \hline \end{array}$$

$$R = 2$$

$$\begin{array}{c} N \\ \hline 6 \\ \hline \end{array}$$

$$R = 2$$

$$\begin{array}{c} N \\ \hline 10 \\ \hline \end{array}$$

$$R = 2$$

$$\begin{array}{c} N \\ \hline 15 \\ \hline \end{array}$$

$$R = 2$$

- (A) 3
(B) 5
(C) 4
(D) 6

Genius

$\begin{array}{r} 166 \\ \hline 400 \\ \hline 400 \\ \hline 0 \\ \hline \end{array}$
 $100 \times 2 + 2$
 $\begin{array}{r} 166 \\ - 360 \\ \hline 400 \\ - 400 \\ \hline 0 \\ \hline \end{array}$
 $100 \times 2 + 2$
 $\begin{array}{r} 166 \\ - 720 \\ \hline 400 \\ - 400 \\ \hline 0 \\ \hline \end{array}$
 $100 \times 2 + 2$

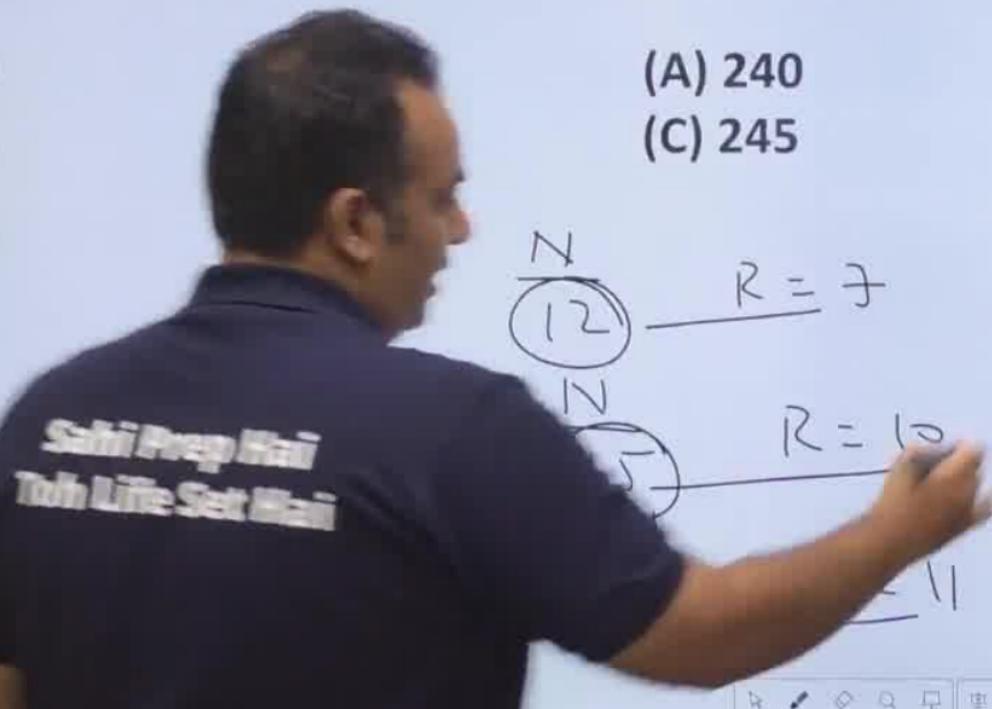
Sahi Prep Hai
Toh Life Set Hai

6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

- (A) 240
(C) 245

- (B) 235
(D) 260

$$\begin{array}{c} \text{N} \\ \hline 12 \\ \text{N} \end{array} \quad R = ?$$
$$\begin{array}{c} \text{N} \\ \hline 15 \\ \text{N} \end{array} \quad R = 10$$
$$\begin{array}{c} \text{N} \\ \hline 16 \\ \text{N} \end{array} \quad R = 11$$



6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

- (A) 40
(C) 45

- (B) 235
(D) 260

Sahi Prep Hai
Toh Life Set Hai

$$L = ?$$

$$R = 10$$

$$R = 11$$

$$\text{LCM}(12, 15, 16) - 5$$

$$240 - 5$$

$$= \underline{235}$$

~~12x + A~~

6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

- (A) 240
(C) 245

- (B) 235
(D) 260

$$\begin{array}{ccc} \frac{N}{12} & R = 7 \\ \frac{N}{15} & R = 10 \\ \frac{N}{16} & R = 11 \end{array}$$

$$\text{LCM}(12, 15, 16) - 5$$

$$240 - 5$$

$$= \underline{235}$$

~~(12x + A)~~

6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

A) 240
B) 245

C) ~~260~~
(B) 235

Sahi Prep Hai
Toh Life Set Hai

$$R = ?$$

$$R = 11$$

$$\text{LCM}(12, 15, 16) - 5$$

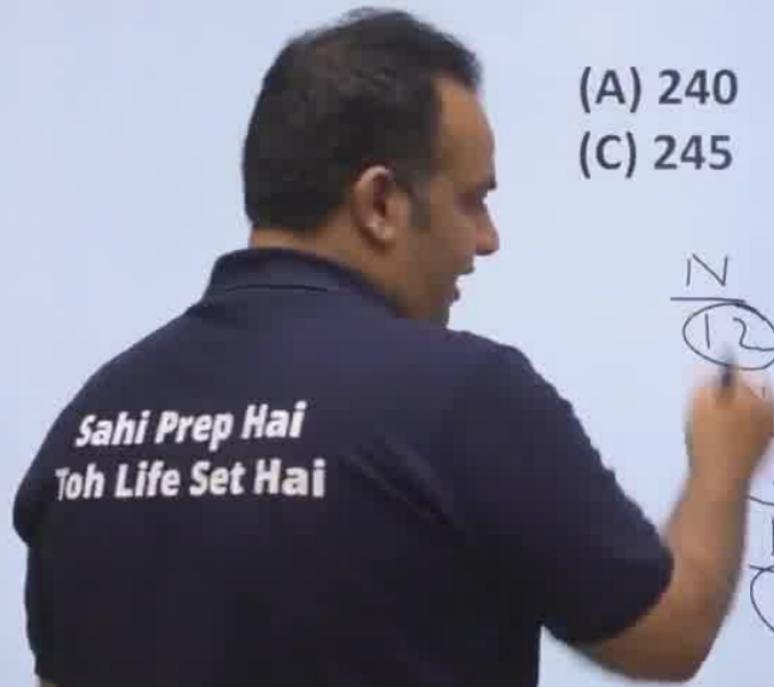
$$240 - 5$$

$$= \underline{\underline{235}}$$

6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

- (A) 240
(C) 245

- (B) 235
(D) 260



6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

- (A) 240
- (B) 235
- (C) 245
- (D) 260

Sahi Prep Hai
Toh Life Set Hai

$$\begin{array}{lll} N & R = 7 \\ \textcircled{15} & R = 10 & 240 - 5 \\ N & R = 11 & = 235 \end{array}$$

6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

$$\frac{12x+7}{4} \quad R=3$$

$$(B) 235$$

$$(D)$$

$$R=7$$

Sahi Prep Hai
Toh Life Set Hai

$$240 - 5 \\ = 235$$

$$R=11$$

What smallest no. should be added to 21 so that

$$\begin{array}{r} 2 \\ 8 \sqrt{21} \\ \underline{-16} \\ 5 \end{array}$$

it become a multiple of 8

$$\underline{21+3}$$

$$= \underline{\underline{24}}$$

↓ Amb

Case III : No condition

Example: What is the least possible number which when divided by 13 leaves the remainder 3 and when it is divided by 5 leaves the remainder 2.

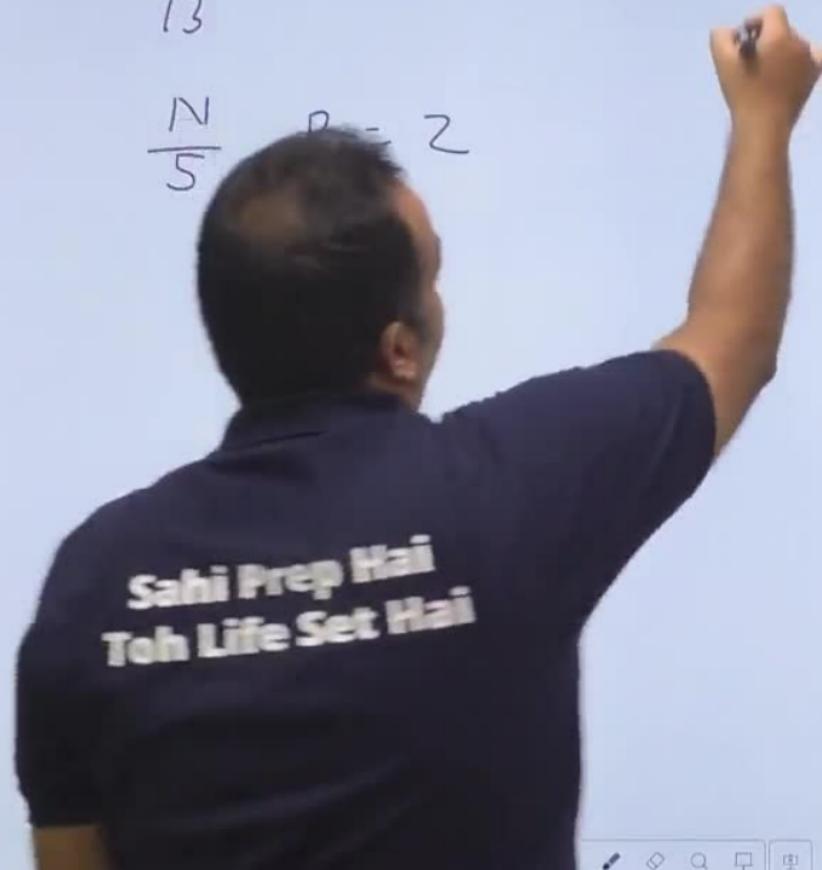
$$\frac{N}{13} \quad R = 3$$

$$\frac{N}{5} \quad R = 2$$



$$\frac{N}{13} \quad R = 3$$

$$\frac{N}{5} \quad R = 2$$



$$\frac{N}{13} \quad R = 3$$

$$13x + 3 = 5y + 2$$

$$\frac{N}{5}$$



$$\frac{N}{13} R = 3$$

$$13x + 3 = 5y + 2$$

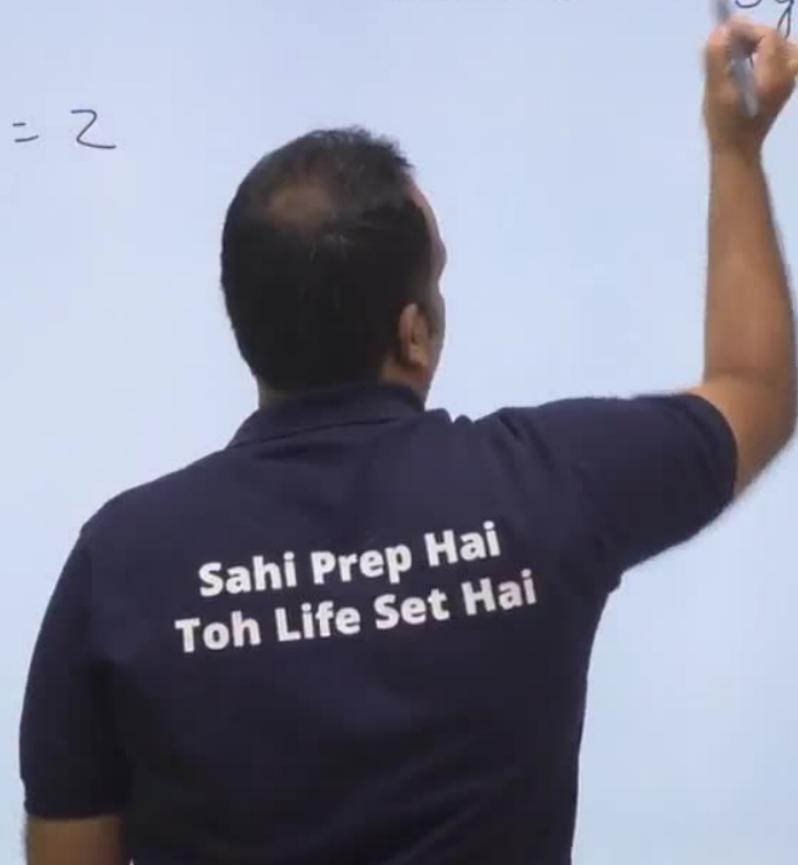
$$\frac{N}{5} R = ?$$



$$\frac{N}{13} \quad R = 3$$

$$13x + 3 = 5y + 2$$

$$\frac{N}{5} \quad R = 2$$



$$\frac{N}{13} R = 3$$

$$13x + 3 = 5y + 2$$

$$\frac{N}{5} R = ?$$

y

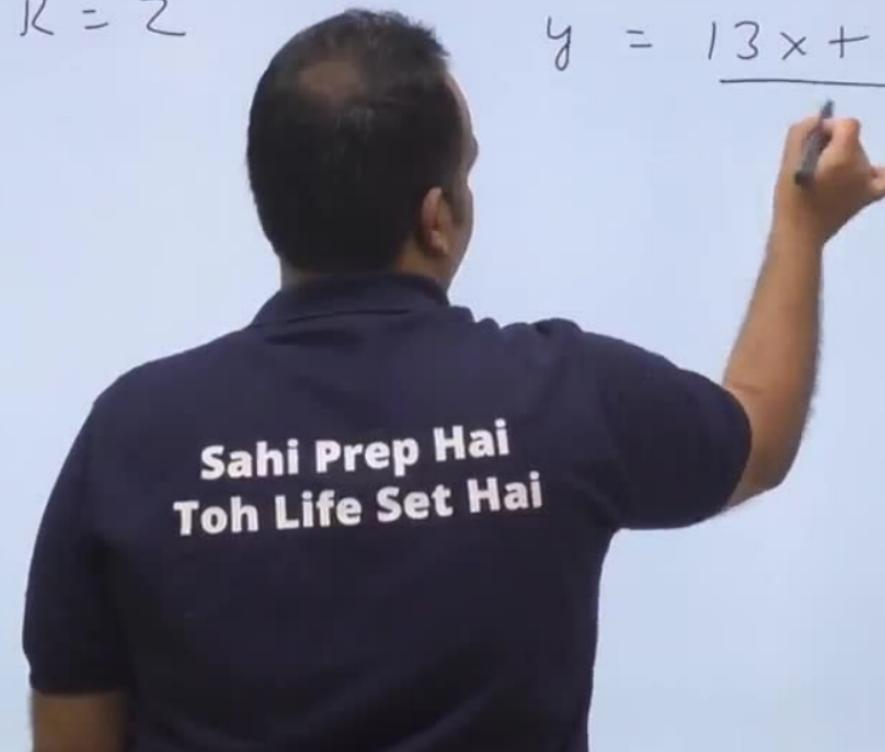
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Toh Life Set Hai

$$\frac{N}{13} \quad R = 3$$

$$13x + 3 = 5y + 2$$

$$\frac{N}{5} \quad R = 2$$

$$y = \underline{13x + 1}$$

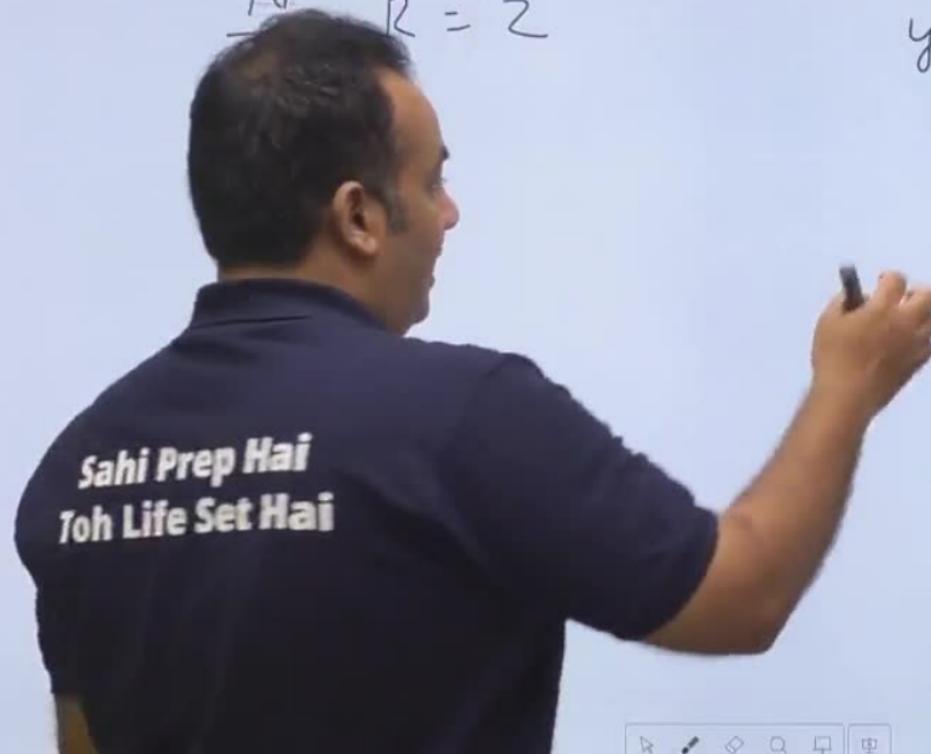


$$\frac{N}{13} R = 3$$

$$13x + 3 = \underline{\underline{5y + 2}}$$

$$\frac{N}{13} R = 2$$

$$y = \frac{13x + 1}{5}$$



$$\frac{N}{13} \quad R = 3$$

$$13x + 3 = 5y + 2$$

$$\frac{N}{5} \quad R = 2$$

$$y = \frac{13x - 1}{5}$$

Sahi Prep Hai
Toh Life Set Hai

$$\frac{N}{13} \quad R = 3$$

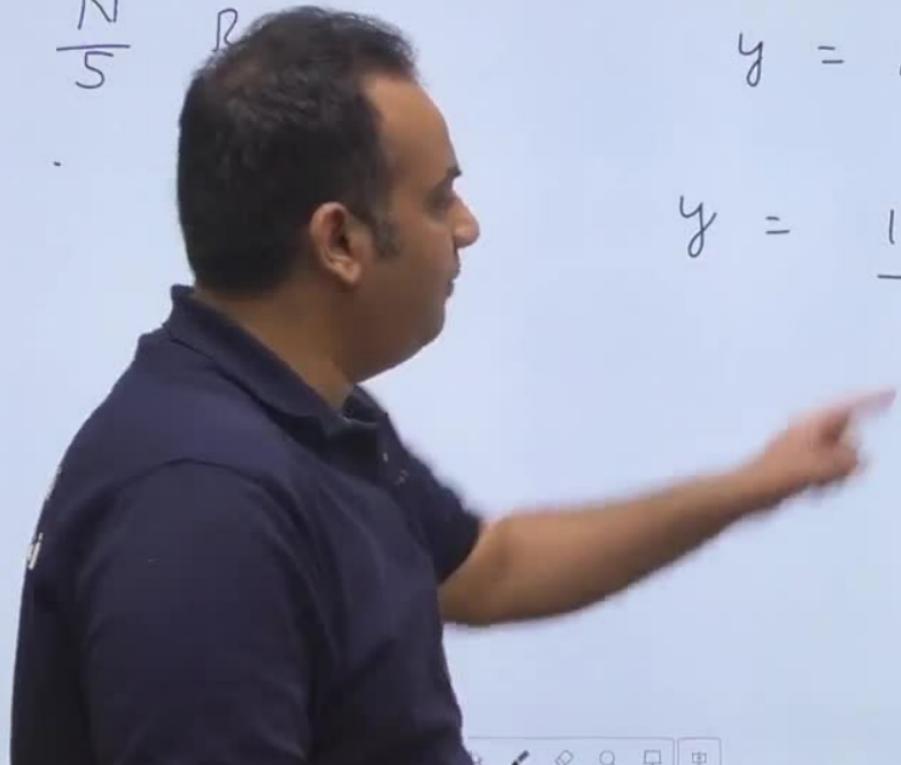
$$13x + 3 = 5y + 2$$

$$\frac{N}{5}$$

R

$$y = \frac{13x + 1}{5}$$

$$y = \frac{10x + (3x + 1)}{5}$$



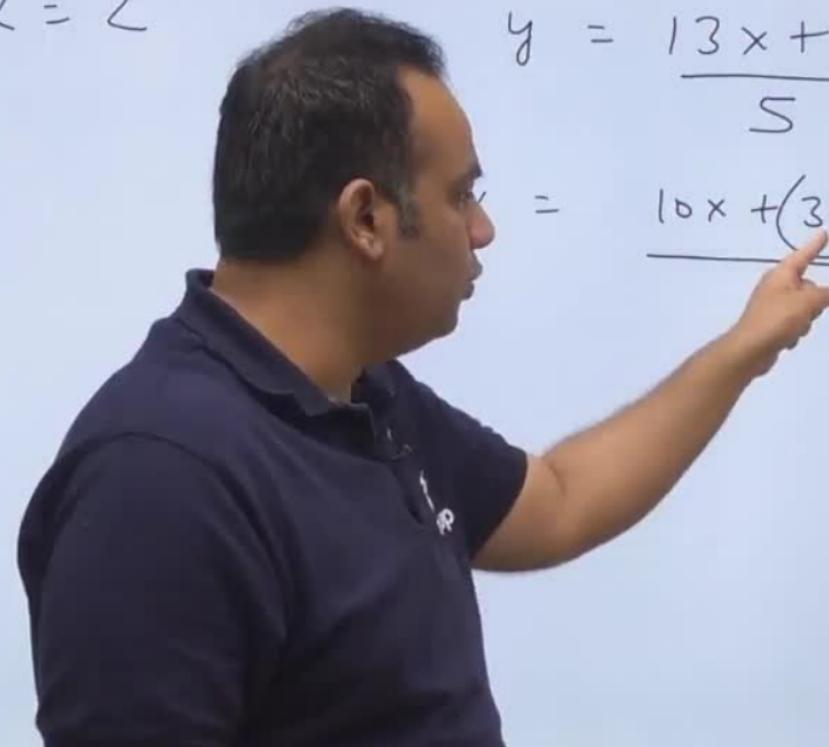
$$\frac{N}{13} R = 3$$

$$13x + 3 = \underline{\underline{5y + 2}}$$

$$\frac{N}{5} R = 2$$

$$y = \frac{13x + 1}{5}$$

$$y = \underline{\underline{10x + (3x + 1)}}$$



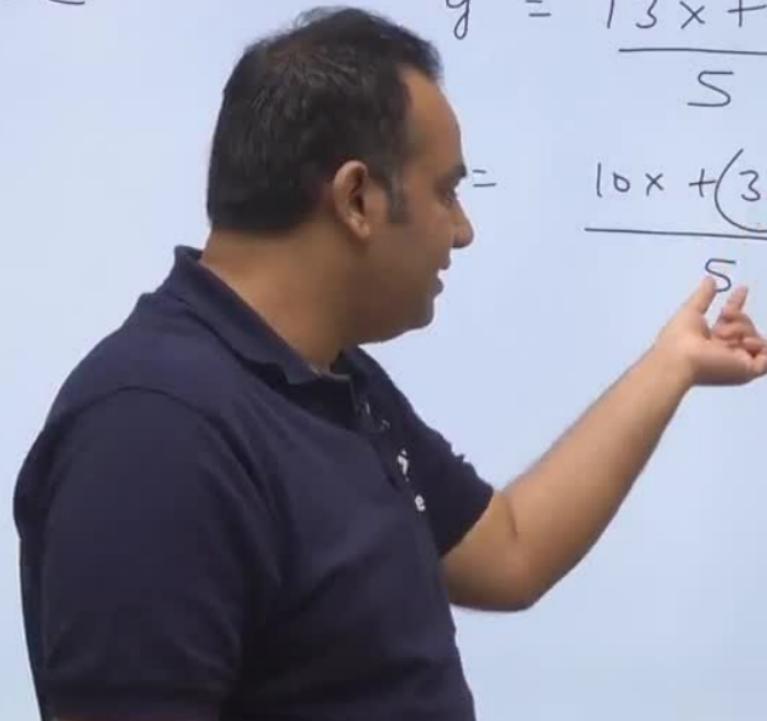
$$\frac{N}{13} R = 3$$

$$13x + 3 = \underline{\underline{5y + 2}}$$

$$\frac{N}{5} R = 2$$

$$y = \frac{13x + 1}{5}$$

$$= \frac{10x + (3x + 1)}{5}$$



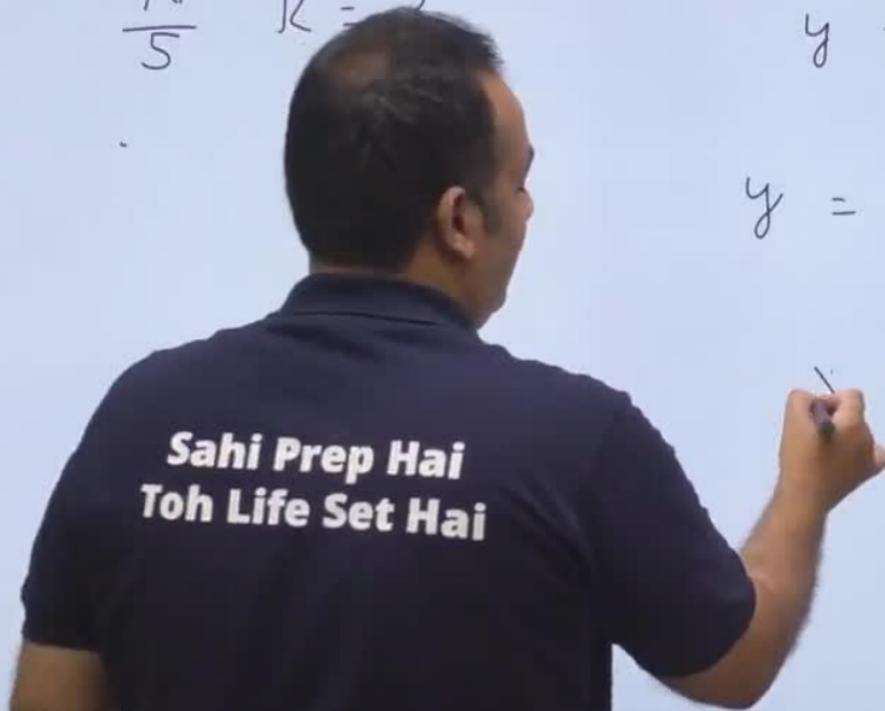
$$\frac{N}{13} R = 3$$

$$13x + 3 = 5y + 2$$

$$\frac{N}{5} R = 3$$

$$y = \frac{13x + 1}{5}$$

$$y = \frac{10x + (3x + 1)}{5}$$



$$\frac{N}{13} \quad R = 3$$

$$\frac{N}{2} \quad R = 2$$

$$\sqrt{13x+3} = 5y+2$$

$$y = \frac{13x+1}{5}$$

$$y = \frac{10x + (3x+1)}{5}$$

$$x = 3$$

Smallest
No.

Sahi Prep Hai
Toh Life Set Hai

$$42 + 65m$$

$$\frac{N}{13} \quad R = 3$$

$$\frac{N}{7} \quad R = 2$$

Smallest

No

Sahi Prep Hai
Toh Life Set Hai

$$\begin{aligned} 13x + 3 &= 5y + 2 \\ y &= \frac{13x + 1}{5} \\ y &= \frac{10x + (3x + 1)}{5} \\ &= 3 \end{aligned}$$

$$1 - 165m$$

$$\frac{N}{13} \quad R = 3$$

$$\frac{N}{5} \quad R = 2$$

$$\sqrt{13x+3} = 5y+2$$

$$y = \frac{13x+1}{5}$$

$$y = \frac{10x + (3x+1)}{5}$$

Smallest No. = 42

$x =$

General

**Sahi Prep Hai
Toh Life Set Hai**

BSM

$$\frac{N}{13}$$

$$R = 3$$

$$\frac{N}{5}$$

$$R = 2$$

Smallest No. = 42

General Form

$$\sqrt{13x+3} = 5y+2$$

$$y = \frac{13x+1}{5}$$

$$y = \frac{10x + (3x+1)}{5}$$

Sahi Prep Hai
Toh Life Set Hai



$$\frac{N}{17} \quad R = 15$$

$$R = 1$$



$$\frac{N}{17}$$

$$R = 15$$

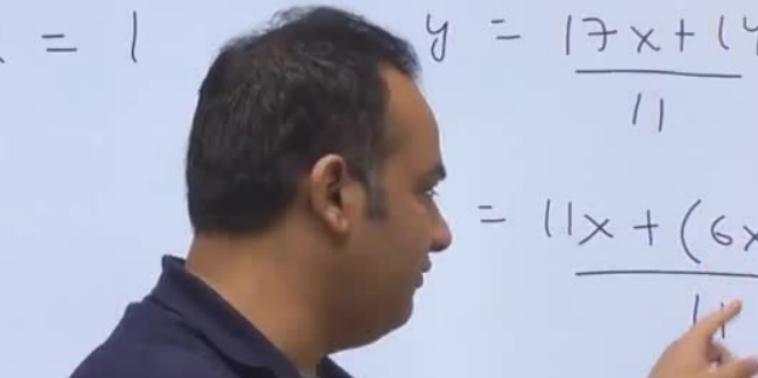
$$17x + 15 = 11y + 1$$

$$\frac{N}{11}$$

$$R = 1$$

$$y = \frac{17x + 14}{11}$$

$$= \frac{11x + (6x + 14)}{11}$$



$$\frac{N}{17}$$

$$R = 15$$

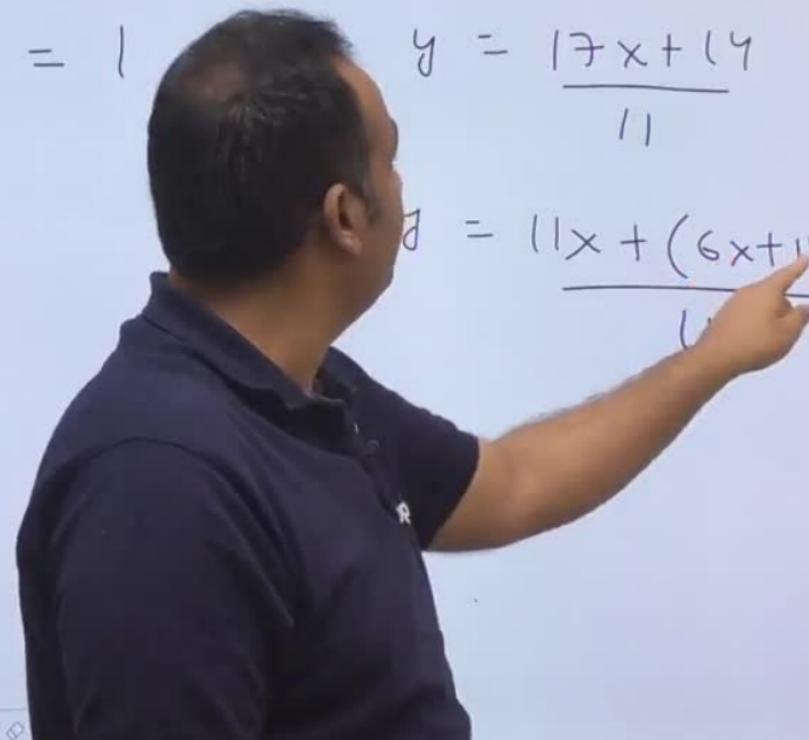
$$17x + 15 = 11y + 1$$

$$\frac{N}{11}$$

$$R = 1$$

$$y = \frac{17x + 14}{11}$$

$$d = \frac{11x + (6x + 14)}{11}$$



Smallest

Sahi Prep Hai
Toh Life Set Hai

$$\frac{N}{17}$$

$$R = 15$$

$$R = 1$$

00

$$0 + 187$$

$$17x + 15 = 11y + 1$$

$$y = \frac{17x + 14}{11}$$

$$y = \frac{11x + (6x + 14)}{11}$$

$$x = 5$$

$$\left\{ \begin{array}{l} N \\ 17 \\ \hline N \\ 11 \end{array} \right.$$

$$R = 15$$

$$R = 1$$

Smallest $\rightarrow 100$

Greatest $\rightarrow \underline{100 + 187m}$

$$17x + 15 = 11y + 1$$

$$y = \frac{17x + 14}{11}$$

$$y = \frac{11x + (6x + 14)}{11}$$

$$x = 5$$

HCF

(i)

$$\begin{array}{r} 37 \\ \text{N} \\ \overline{)58} \end{array} \quad R = 2 \checkmark$$

$$\begin{array}{r} 58 \\ \text{N} \\ \overline{)55} \end{array} \quad R = 3 \checkmark$$

$$\text{HCF}(35, 55) = 5$$

$$\begin{array}{r} 80 \\ \text{N} \\ \overline{)108} \\ \text{N} \end{array}$$

R
R
R

HCF(i) Largest

$$\begin{array}{r} 37 \\ N \\ \hline 58 \\ N \end{array} \quad R = 2 \quad R = 3$$

$$N = HCF(37, 58) = 5$$

(ii)

$$\begin{array}{r} 80 \\ N \\ \hline 108 \\ N \\ \hline 64 \end{array} \quad R$$

$$N = HCF(28, 14) = 14$$

LCM

I

Remainders are same

$$\begin{array}{r} N \\ \textcircled{7} \\ \hline N \\ \textcircled{8} \\ \hline 2 + 56m \end{array} \quad R = 2 \quad R = 3$$

$$\begin{array}{r} N \\ \textcircled{7} \\ \hline N \\ \textcircled{8} \\ \hline 2 + 56m \end{array} \quad R = 3$$

$$\begin{array}{r} N \\ \textcircled{7} \\ \hline N \\ \textcircled{8} \\ \hline 2 + 56m \end{array} \quad R = 4$$

**Sahi Prep Hai
Toh Life Set Hai**

HCF

(i)

$$\begin{array}{r} 37 \\ \text{N} \\ \hline 58 \\ \text{N} \end{array} \quad R=2 \checkmark$$

Largest

$$N = \text{HCF}(37, 58)$$

(ii)

$$\sum \frac{80}{N}$$

**Sahi Prep Hai
Toh Life Set Hai**

LCM

I

Remainder are same

$$\begin{array}{r} N \\ \text{7} \\ \text{N} \\ \hline 8 \\ \text{N} \end{array} \quad R=2$$

$2 + 56m$

II

$$\begin{array}{r} N \\ 7 \\ \hline 8 \\ \text{N} \end{array} \quad R=3$$

$$\begin{array}{r} N \\ 8 \\ \hline 8 \\ \text{N} \end{array} \quad R=4$$

HCF(i) largest

$$\begin{array}{r} 37 \\ N \\ \hline 58 \end{array} \quad R=2$$

$$\begin{array}{r} 58 \\ N \\ \hline 8 \end{array} \quad R=3$$

$$N = \text{HCF}(35, 55) = 5$$

(ii)

$$\begin{array}{r} 80 \\ N \\ \hline 9 \end{array} \quad R$$

*Sahi Prep Hai
Toh Life Set Hai*

$$N =$$

LCM

I

Remainders are same

$$\begin{array}{r} N \\ \textcircled{7} \\ \hline 8 \end{array} \quad R=2$$

$$2 + 56m$$

$$\begin{array}{r} N \\ \textcircled{7} \\ \hline 8 \end{array} \quad R=3$$

$$4 + 56m$$

$$52 + 56m$$

$$N \text{ and } M$$

HCF

(ii)

$$\begin{array}{r} 37 \\ N \\ \hline 58 \end{array} \quad R=2$$

$$\begin{array}{r} 58 \\ N \\ \hline 35 \end{array} \quad R=3$$

$$\text{HCF}(35, 58) = 5$$

$$\begin{array}{r} 80 \\ N \\ \hline 18 \\ | \\ 8 \\ N \\ \hline 2 \end{array} \quad R$$

$$\begin{array}{r} 8 \\ N \\ \hline 2 \\ | \\ 4 \\ N \\ \hline 0 \end{array} \quad R$$

$$\begin{array}{r} 4 \\ N \\ \hline 0 \\ | \\ 8 \\ N \\ \hline 4 \end{array} \quad R$$

LCM

I

Remainders are same

$$\begin{array}{c} N \\ \textcircled{7} \\ N \\ \textcircled{8} \\ \hline 2 + 56m \end{array} \quad R=2$$

II

$$\begin{array}{c} N \\ \textcircled{7} \\ N \\ \textcircled{8} \\ \hline \end{array} \quad R=3$$

$$\begin{array}{c} N \\ \textcircled{7} \\ N \\ \textcircled{8} \\ \hline \end{array} \quad R=4$$

$$\begin{array}{l} 52 + 56m \\ \text{Ns (mod } N \text{)} \end{array}$$

1. What is the greatest number which can divide
141, 186, 231 leaving the same remainder 1 in each
case?

(A) 31

~~(B) 5~~

(C) 45

(D) 35

$$\text{HCF } (140, 185, 230)$$

$$\Rightarrow \begin{smallmatrix} 5 \\ 2 \\ 1 \end{smallmatrix}$$

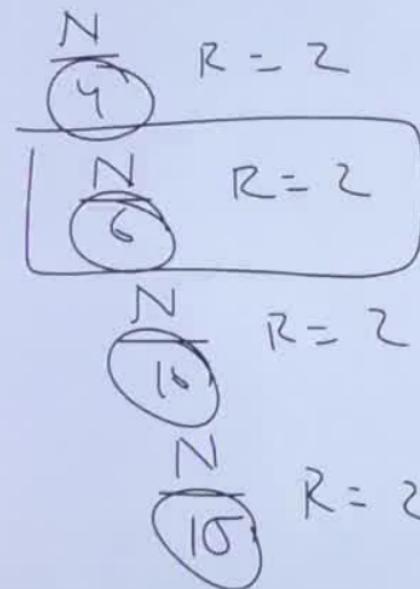
2. Three drums contain 2527 litres, 1653 litres, and 2261 litres milk respectively. What is the biggest measure that can measure milk of each drum exactly?

- (A) 19 litre
- (B) 20 litre
- (C) 29 litre
- (D) 31 litre

3. Six bells commence tolling together and toll at intervals of 2, 4, 6, 8, 10 and 12 seconds respectively. In 30 minutes, How many times do they toll together?

$$\frac{6^{n+2}}{2} \text{ LCM } (\text{am}-1)$$

4. Let the least number of six digits which when divided by 4, 6, 10, 15 leaves in each case same remainder 2 be N. the sum of digits in N is.



- (A) 3 (B) 5
(C) 4 (D) 6

General Form

$$\rightarrow \underline{2+60m}$$

$$\begin{array}{r}
 166 \\
 \hline
 60 \overline{)1000\ 00} \\
 \underline{-60} \quad 100020 + 2 \\
 \underline{400} \\
 \underline{360} \quad 100022 \\
 \underline{-400} \\
 \underline{\underline{360}}
 \end{array}$$

MCF
Cont II

5. Let N be the greatest number that will divide 1305, 4665 and 6905 leaving the same remainder in each case. Then, sum of the digits in N is.

- (A) 4 (B) 5
 (C) 6 (D) 8

$$N = \text{HCF} (33_{(0)}, 224_0) \\ = \boxed{\underline{1120}}$$

$$\cancel{12x+7} \\ \cancel{4} \quad R=3$$

6. What is the least number which when divided by 12, 15, 16 leaves 7, 10, 11 as remainder respectively?

(A) 240

(C) 245 \times

(B) 235

(D) 260

$$\begin{array}{r} N \\ \cancel{12} \\ R = 7 \end{array}$$

$$\begin{array}{r} N \\ \cancel{15} \\ R = 10 \end{array}$$

$$\begin{array}{r} N \\ \cancel{16} \\ R = 11 \end{array}$$

$$240 - 5$$

$$= 235$$

7. The length of two pencils are 24 cm and 42 cm. If we want to equal their size, then minimum number of pencils of same size?

- (A) 6
- (B) 11
- (C) 12
- (D) None of these

9. The least multiple of 13, when divided by 4, 5, 6, 7 and 8 leaves remainder 2 in each case?

- (A) 2520
- (B) 842
- (C) 2522
- (D) 840

10. 68 m long and 51 m wide floor of a hall is to be passed with square tile. What is minimum no of square tile?

- (a) 17 (b) 12
- (c) 4 (d) 3

11. A gardener has 3 type of flowers in numbers 76, 151, and 226. He makes bunches of equal size in maximum number of flowers, then one flower remain extra among each type of flowers. Find number of flowers in each bunch?

- (A) 25
- (B) 50
- (C) 75
- (D) None of these

12. The largest of five digit number which when increased by 45 is divisible by 60, 65, 75, 80 exactly?

- (A) 87360
- (B) 87315
- (C) 87405
- (D) None of these

Ans. (d)



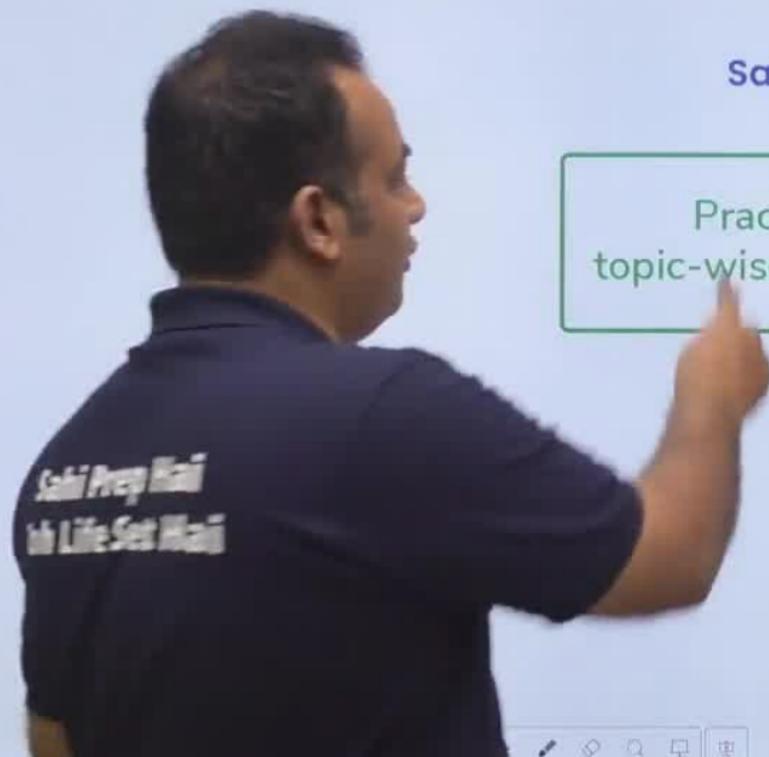


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