



gradeup

Sahi Prep Hai Toh Life Set Hai

Unit Digit

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Digit

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Agenda

*

Concepts

Examples

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Agenda

* Theory & Concepts

With solved

→ 45 min

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* Theory & Concepts

With solved examples →

(47)

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Agenda

* Theory & Concepts

With solved examples $\rightarrow (45-47)$ min

Practice Qs $\rightarrow (43-45)$

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Agenda

* Theory & Concepts

Solved examples
(10 examples)

→ (45-47) min

Practice Questions
(15Q)

→ (43-45) min

Meaning of Unit digit

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Meaning of Unit digit

U

3 4

Natural

Remainder

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Meaning of Unit digit

$$\begin{array}{r} 348 \\ = \end{array}$$

Natural No

10 remainder \rightarrow Unit digit

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How to find the unit digit of a given expression?

To find the unit digit of a given expression, we don't have to evaluate the complete expression, only evaluate the unit digits of all the numbers & perform the required operation to get the unit digit of the resultant expression.

Example: Find the unit digit of $12 \times 13 \times 14$.

Solution: To find the unit digit we multiply $2 \times 3 \times 4 = 24$

Unit digit of the expression is 4.

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How to find the unit digit of a given expression?

To find the unit digit of a given expression, we don't have to evaluate the complete expression, only evaluate the unit digits of all the numbers & perform the required operation to get the unit digit of the resulting expression.

Suppose we have to find the unit digit of $\underline{12} \times \underline{13} \times \underline{14}$.

In this case to find the unit digit we multiply $\underline{2} \times \underline{3} \times \underline{4} = \underline{24}$.

So the unit digit of the expression is 4.

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Eg.1 Find unit digit of $628 + 493 + 589$

Ans. $8 + 3 + 9 = 20 \rightarrow 0$

Eg.2 Find the unit digit of $128 \times 693 \times 584 \times 677$

8×3

Ans.

2

unit digit = 2

Smart People Think
Think in the Smart Way

Eg.1 Find unit digit of $\underline{628} + \underline{493} + \underline{589}$

Ans. $8 + 3 + 9 = 20 \rightarrow \underline{\underline{0}}$



Eg.2 Find unit digit of $\underline{128} \times \underline{693} \times \underline{584} \times \underline{677}$

Ans.

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Concept of Cyclicity

This concept is used to find the unit digit of a bigger expressions where exponents are involved.

So when a number n is raised to any power m , the digit in the unit place of the resulting expression can be determined without actually evaluating the complete expression. Number when raised to powers will give values in which the unit digits of the resulting expression follow's a cyclic pattern.

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Cyclicity \rightarrow "Pattern"

$\left\{ \begin{array}{l} 1 \rightarrow \\ 2 \rightarrow \\ 3 \rightarrow M \\ 4 \rightarrow S \\ 5 \rightarrow \\ 6 \rightarrow \end{array} \right.$

Student

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Cyclicity \rightarrow "Pattern"

1 \rightarrow CGL

\rightarrow CHSL

\rightarrow MTS

\rightarrow CGL

\rightarrow CHSL

\rightarrow MTS

Student No \rightarrow 50

Cyclicity \rightarrow "Pattern"

$\left\{ \begin{array}{l} 1 \rightarrow \text{CGL} \\ 2 \rightarrow \text{CHSL} \\ 3 \rightarrow \text{MTS} \\ 4 \rightarrow \text{SC} \\ 5 \rightarrow \\ 6 \rightarrow \end{array} \right.$

Student No \rightarrow 50

$$\begin{array}{r} 16 \\ 3 \overline{) 50} \\ \underline{3} \\ 20 \\ \underline{18} \\ 2 \end{array}$$

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$1^{\text{st}} \rightarrow \text{Mon}$
 $2 \rightarrow \text{Tue}$ ✓
 $3 \rightarrow \text{Wed}$
 $4 \rightarrow \text{Th}$
 $5 \rightarrow \text{Fri}$
 $6 \rightarrow \text{Sat}$
 $7 \rightarrow \text{Sun}$

$100^{\text{th}} \text{ day}$

14
 $\overline{) 100}$
 7
 $\underline{30}$
 28
 $\underline{2}$

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$1^{\text{st}} \rightarrow \text{Mon}$
 $2 \rightarrow \text{Tue}$ ✓
 $3 \rightarrow \text{Wed}$
 $4 \rightarrow \text{Thur}$
 $5 \rightarrow \text{Fri}$
 $6 \rightarrow \text{Sat}$
 $7 \rightarrow \text{Sun}$

$$\begin{array}{r}
 100^{\text{th}} \text{ day} \\
 \hline
 14 \\
 7 \overline{) 100} \\
 \underline{7} \\
 30 \\
 \underline{28} \\
 2
 \end{array}$$

$$\begin{array}{r}
 35^{\text{th}} \text{ day} \\
 \hline
 5 \\
 7 \overline{) 35} \\
 \underline{35} \\
 0
 \end{array}$$

Prep Hai
 Set Hai

$1^{st} \rightarrow \text{Mon}$
 $2 \rightarrow \text{Tue}$ ✓
 $3 \rightarrow \text{Wed}$
 $4 \rightarrow \text{Thurs}$
 $5 \rightarrow \text{Fri}$
 $6 \rightarrow \text{Sat}$
 $7 \rightarrow \text{Sun}$

100^{th} day

14

35^{th} day

$$\begin{array}{r}
 5 \\
 7 \overline{) 35} \\
 \underline{35} \\
 0
 \end{array}$$

Sunday

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How to use cyclicity to Evaluate Unit digit

Powers of 2

$$2^1 = 2$$

$$2^2 = 4$$

$$2^3 = 8$$

$$2^4 = 16$$

$$2^5 = 32$$

$$2^6 = 64$$

$$2^7 = 128$$

$$2^8 = 256$$

$$2^9 = 512$$

$$2^{10} = 1024$$

$$2^{11} = 2048$$

$$2^{12} = 4096$$

$$2^{13} = 8192$$

$$2^{14} = 16384$$

$$2^{15} = 32768$$

$$2^{16} = 65536$$

Unit digit repeats after a cycle of 4
So cyclicity of unit digit of 2 is 4.

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Find unit digit of

(i) 59

(ii) 62466
 832

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2345678

Find unit digit of

(i) $59 \rightarrow \textcircled{8} \checkmark$

(ii) $832 \rightarrow 62466 \rightarrow 4$

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787654321

Find unit digit of

(i) $2^{59} \rightarrow 8$ ✓

(ii) $62466 \rightarrow 4$

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56787654321

2

Find unit digit of

(i) $2^{59} \rightarrow \textcircled{8} \checkmark$

(ii) $(1583\underline{2})^{624\underline{66}} \rightarrow 4$

(iii) $(2)^{1234567876543\underline{21}} \rightarrow \underline{\underline{2}}$

Eg4. Find the unit digit of 2^{33} .

Ans. To find the unit digit of 2^{33} divide the power 33 by 4 (because cyclicity of unit digit of 2 is 4) & find the remainder. Based on the value of the remainder, you can find the unit digit

In case of powers of 2, if

Remainder = 1 \rightarrow Unit digit = 2

Remainder = 2 \rightarrow Unit digit = 4

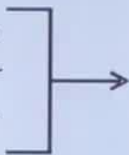
Remainder = 3 \rightarrow Unit digit = 8

Remainder = 0 \rightarrow Unit digit = 6

$$\begin{array}{r} 33 \\ 4 \end{array} \text{ Remainder is } 1, \text{ so } \underline{\underline{\text{unit digit} = 2}}$$

Powers of 3

$$\begin{array}{l}
 3^1 = \underline{3} \\
 3^2 = \underline{9} \\
 3^3 = \underline{27} \\
 3^4 = \underline{81} \\
 3^5 = 3 \\
 3^6 = 9 \\
 3^7 = 7 \\
 3^8 = 1
 \end{array}$$



Unit digit repeats after a cycle of 4
So cyclicity of unit digit of 3 is 4.

Eg5. Find the unit digit of 3^{142} .

Ans. To find the unit digit of 3^{142} divide the power 142 by 4 (because cyclicity of unit digit of 3 is 4) & find the remainder based on the value of the remainder, you can find the unit digit.

In case of powers of 3

Remainder = 1 \rightarrow Unit digit = 3

Remainder = 2 \rightarrow Unit digit = 9

Remainder = 3 \rightarrow Unit digit = 7

Remainder = 0 \rightarrow Unit digit = 1

$142 \div 4 = 35$ remainder = 2 so unit digit = 9

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Find unit digit of

$$3^{595}$$

$$(13)^{84}$$

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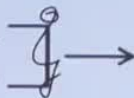
Find unit digit of

(i) $\frac{95}{\underline{\underline{\quad}}} \rightarrow 3^3$

(ii) $\frac{584}{\quad}$

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Powers of 4

$$\begin{aligned} 4^1 &= 4 \\ 4^2 &= 16 \\ 4^3 &= 64 \end{aligned}$$


Unit digit repeats after a cycle of 4
So cyclicity of unit digit of 4 is 2.

Note :

4^{Odd}	\longrightarrow	4
4^{Even}	\longrightarrow	6

Powers of 5

$$5^1 = \underline{5}$$

$$5^2 = \underline{25}$$

Unit digit is same for all the powers of 5
So cyclicity of unit digit of 5 is 1.

5^{any}



5

|

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Eg7. Find the unit digit of 7^{1248}

Ans. To find the unit digit of 7^{1248} , Divide the power 1248 by 4 (because cyclicity of the unit digit of 7 is 4) and find the remainder. Based on the value of the remainder, you can find the unit digit.

In case of powers of 7 if,

Remainder = 1 \rightarrow Unit digit = 7

Remainder = 2 \rightarrow Unit digit = 9

Remainder = 3 \rightarrow Unit digit = 3

Remainder = 0 \rightarrow Unit digit = 1

So, $\frac{1248}{4}$ Remainder = 0, so unit digit = 1



Find unit digit of

(i) $\underline{\underline{14}} \rightarrow 7^2 \rightarrow 9$

(ii) $\underline{\underline{891}} \rightarrow$

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Eg8. Find the unit digit of $8^{\underline{343}}$.

To find the unit digit of 8^{343} divide the power of 343 by 4 (because cyclicity of the unit digit of 8 is 4) & find the remainder. Based on the value of the remainder, you can find the unit digit.

In case of powers of 8 if

Remainder = 1 \rightarrow Unit digit = 8

Remainder = 2 \rightarrow Unit digit = 4

Remainder = 3 \rightarrow Unit digit = 2

Remainder = ④ \rightarrow Unit digit = 6

So, $\frac{343}{4}$ Remainder = 3, so unit digit = 2

Eg9. Find the unit digit of 9^{64} .

Ans. To find the unit digit of 9^{64} , divide the power 64 by 2 (because cyclicity of unit digit of 9 is 2) & find the remainder based on the value of the remainder, you can find the unit digit.

In case of powers of 9 if,

Remainder = 1 \rightarrow Unit digit = 9

Remainder = 0 \rightarrow Unit digit = 1

$$\frac{64}{2} \text{ Remainder is 0. So unit digit = 1} \quad \checkmark$$

Note : $9^{\text{Odd}} \rightarrow 9$

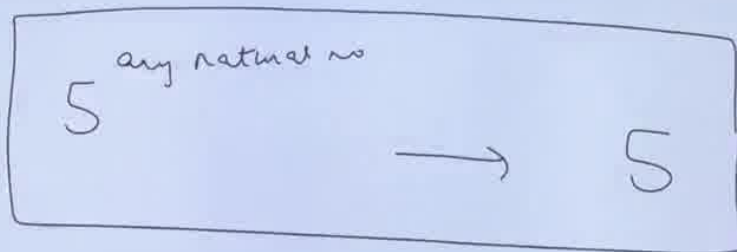
$9^{\text{Even}} \rightarrow 1$

Powers of 5

$$5^1 = \underline{5}$$

$$5^2 = \underline{25}$$

Unit digit is same for all the powers of 5
So cyclicity of unit digit of 5 is 1.



Eg4. Find the unit digit of 2^{33} .

Ans. To find the unit digit of 2^{33} divide the power 33 by 4 (because cyclicity of unit digit of 2 is 4) & find the remainder. Based on the value of the remainder, you can find the unit digit

In case of powers of 2, if

Remainder = 1 \rightarrow Unit digit = 2

Remainder = 2 \rightarrow Unit digit = 4

Remainder = 3 \rightarrow Unit digit = 8

Remainder = 0 \rightarrow Unit digit = 6

$\frac{33}{4}$ Remainder is 1, so unit digit = 2



Powers of 3

$$3^1 = \underline{3}$$

$$3^2 = \underline{9}$$

$$3^3 = \underline{27}$$

$$3^4 = \underline{81}$$

$$3^5 = 3$$

$$3^6 = 9$$

$$3^7 = 7$$

$$3^8 = 1$$

Unit digit repeats after a cycle of 4
So cyclicity of unit digit of 3 is 4.

Summary

CYCLICITY TABLE		
Digit	Cyclicity	Cyclic Pattern of Unit digit
	1	0
	1	1
	4	2, 4, 8, 6
	4	3, 9, 7, 1
	5	4, 6
	5	5
	6	6
	4	7, 9, 3, 1
	4	8, 4, 2, 6
	2	9, 1

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Summary

CYCLICITY TABLE		
Unit Digit	Cyclic	Cyclic Pattern of Unit digit
0		0
1		1
2		2, 4, 6
3		3, 9, 7, 1
4		4, 6
5		5
6		6, 9, 3, 1
7		8, 4, 2, 6
8		9, 1

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Summary

$$(-0)^{-} = 0$$

$$(-1)^{-} = 1$$

$$(-5)^{-} = 5$$

$$(-6)^{-} = 6$$

CYCLICITY TABLE		
Unit Digit	Cyclicity	Cyclic Pattern of Unit digit
0		0
1		1
2		2, 4, 8, 6
3		3, 9, 7, 1
4		4, 2, 6, 8
5		5
6		6
7		7, 1, 3, 9
8		8, 4, 2, 6
9		9, 1

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Summary

$$(-0)^{-} = 0$$

$$(-1)^{-} = 1$$

$$(-5)^{-} = 5$$

$$(-6)^{-} = 6$$

CYCLICITY TABLE		
Unit Digit	Cyclicity	Cyclic Pattern of Unit digit
0	1	0
1	1	1
2	4	2, 4, 8, 6
3	4	3, 9, 7, 1
4	2	4, 6
5	1	5
6	1	6
7	4	7, 9, 3, 1
8	4	8, 4, 2, 6
9	1	9, 1

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Summary

$$(-0)^{-} = 0$$

$$(-1)^{-} = 1$$

$$(-5)^{-} = 5$$

$$(-6)^{-} = 6$$

CYCLICITY TABLE		
Unit Digit	Cyclicity	Cyclic Pattern of Unit digit
0	1	0
1	1	1
2		2, 4, 8, 6
3		3, 9, 7, 1
4		4, 6
5		5
6		6
7		7, 9, 3, 1
8		8, 4, 2, 6

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Summary

$$(-0)^{-} = 0$$

$$(-1)^{-} = 1$$

$$(-5)^{-} = 5$$

$$(-6)^{-} = 6$$

CYCLICITY TABLE		
Unit Digit	Cyclicity	Cyclic Pattern of Unit digit
0	1	0
1	1	1
2	4	2, 4, 8, 6
3	4	3, 9, 7, 1
4	2	4, 6
5	1	5
6	1	6
7	4	7, 9, 3, 1
8	4	8, 4, 2, 6
9	2	9, 1

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Concept of Mother Cyclicity

As we can see that the cyclicity of all the unit digits is either 2 or 4. So if we forget the cyclicity of a digit, we can assume cyclicity to be 4 to get the correct answer.

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Concept of Mother Cyclicity

As we can see that the cyclicity of all the unit digits are either 1, 2 or 4. So if we forget the cyclicity of any digit, we assume cyclicity to be 4 to get the unit digit of a number.

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Power

4

First Power

Concept of Mother Cyclicity

As we can see that the cyclicity of all the unit digits are either 1, 2 or 4. So if we forget the cyclicity of any digit, we assume cyclicity to be 4 to get the unit digit of the number.

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Power
4

$n = 1$

$= 2$

First Power

Concept of Mother Cyclicity

As we can see that the cyclicity of all the unit digits are either 1, 2 or 4. So if we forget the cyclicity of any digit, we can assume the cyclicity to be 4 to get the unit digit of the power.

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Power

4

First Power

Second Power

Concept of Mother Cyclicity

As we can see that the cyclicity of all the unit digits are either 1, 2 or 4. So if we forget the cyclicity of any digit, we can take the cyclicity to be 4 to get the unit digit of the

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Power

4

First Power

Second Power

Third Power

Concept of Mother Cyclicity

As we can see that the cyclicity of all the unit digits are either 1, 2 or 4. So if we forget the cyclicity of any digit, we can assume cyclicity to be 4 to get the unit digit of the number.

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First Power

Second Power

Third Power

Fourth Power

Eg. 10 Find the unit digit of

2^{749} , 3^{658} , 4^{690} , 8^{123} , 7^{340} , 9^{126}

749

$\rightarrow 2^1 \rightarrow 2$

$\rightarrow 3^2$

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Any Doubt



Any Doubt



Eg1. $(\underline{\underline{582}})^{\underline{\underline{675}}} + (\underline{\underline{583}})^{\underline{\underline{675}}}$

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Eg2. $(143)^{\underline{143}} - (142)^{143}$

$$3^{43} -$$

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Eg2. $(143)^{\underline{143}} - (14\underline{2})^{\underline{143}}$

$$3^{43} - 2^{43}$$

$$- 8$$

$$- 1$$

$$\textcircled{9}$$

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Eg3. Find the unit digit of product of all prime numbers.

3 · 5 · 7 · 11

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✓ ans
For SSC

Eg4. Find the unit digit of

$$(\underline{348})^{\underline{757}} \times (\underline{383})^{482} \times (\underline{367})^{415}$$

57

X

3⁸²

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✓ ans
For SSC

Eg4. Find the unit digit of

$$(348)^{757} \times (383)^{482} \times (367)^{415}$$

$$8^{57} \times 3^{82} \times 7^{15}$$

$$8 \times 9$$

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Toh Life Set Hai**

✓ ans
For SSC

Eg4. Find the unit digit of

$$(\underline{348})^{\underline{757}} \times (\underline{383})^{\underline{482}} \times (\underline{367})^{\underline{415}}$$

$$8^{7} \times 3^{2} \times 7^{5}$$

$$9 \times 3$$

**Sahi Prep Hai
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✓ ans
For SSC

Eg4. Find the unit digit of

$$(348)^{757} \times (383)^{482} \times (367)^{415}$$

$$8 \times 3^{82} \times 7^{15}$$

$$8 \times 9 \times 3$$

$$6$$

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Toh Life Set Hai

✓ ans
For SSC

Eg4. Find the unit digit of

$$(348)^{757} \times (383)^{482} \times (367)^{415}$$

$$3^{82} \times 7^{15}$$

3

6

✓

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✓ ans
For SSC

Eg4. Find the unit digit of

$$(348)^{757} \times (383)^{482} \times (367)^{415}$$

$$8^{757} \times 3^{482} \times 7^{415}$$

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Eg5. $1! + 2! + 3! + \dots + 50!$

$$1! = 1$$

$$2! = 2$$

$$3! = 6$$

$$4! = 24$$

$$5! = 120$$

$$1 + 2 + 6 + 24 + 120$$

Note

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from

Eg5. $1! + 2! + 3! + \dots 50!$

$$1! = 1$$

$$2! = 2$$

$$3! = 6$$

$$4! = 24$$

$$5! = 120$$

$$1 + 2 + 6 + 24 + 120$$

Note :

A

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Forward

Eg5. $1! + 2! + 3! + \dots 50!$

$$1! = 1$$

2

$$1 + 2 + 6 + 4 + 0$$

120

All Factorials from 5 onwards ends
in "ZERO"

$$12 = 2^2 3^1$$

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$$\frac{(2^2 3^1)^{55}}{3^{11}} +$$

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$$12 = 2^2 \cdot 3^1$$

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

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$$12 = 2^2 \cdot 3^1$$

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$$\frac{(2^2 \cdot 3^1)^{55}}{3^{11}} + \frac{(2^3)^{48}}{(2^4)^{18}}$$

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$$12 = 2^2 \cdot 3^1$$

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$$\frac{(2^2 \cdot 3^1)^{55}}{3^{11}} + \frac{(2^3)^{48}}{(2^4)^{18}}$$

$$\frac{110}{3} \cdot 55$$

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$$12 = 2^2 \cdot 3^1$$

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$$\frac{(2^2 \cdot 3^1)^{55}}{3^{11}} + \frac{(2^3)^{48}}{(2^4)^{18}}$$

$$\frac{2^{110} \cdot 3^{55}}{3^{11}} + \frac{2^{144}}{2^{72}}$$

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$$12 = 2^2 \cdot 3^1$$

$$2^{110} \cdot 3^{44} + 2^{72}$$

$$4 \cdot 1 + 6$$

$$= 11$$

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$$\frac{(2^2 \cdot 3^1)^{55}}{3^{11}}$$

$$\frac{2^{110} \cdot 3^{55}}{3^{11}}$$

$$+ \frac{(2^3)^4}{(2^4)^{18}}$$

$$+ \frac{2^{12}}{2^{72}}$$

9971658659

9971658659

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$$12 = 2^2 \cdot 3^1$$

$$2^{110} = 3^{44}$$

$$4 \cdot 11$$

$$=$$

$$\frac{(2^2 \cdot 3^1)^{55}}{3^{11}} + \frac{(2^3)^{48}}{(2^4)^{18}}$$

$$\frac{2^{110} \cdot 3^{55}}{3^{11}} + \frac{2^{144}}{2^{72}}$$

$$2^{110-11} + 2^{144-72}$$

$$2^{99} + 2^{72}$$

Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$\frac{(2^2 \cdot 3^1)^{55}}{3^{11}} + \frac{(2^3)^{48}}{(2^4)^{18}}$

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Eg6. $\frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}}$

$$= \frac{(2^2 \cdot 3^1)^{55}}{3^{11}} + \frac{(2^3)^{48}}{(2^4)^{18}}$$

$$= \frac{2^{110} \cdot 3^{55}}{3^{11}} + \frac{2^{144}}{2^{72}}$$

$$= 2^{110} \cdot 3^{44} + 2^{72}$$

$$= 6$$

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Eg7. $(1!)^1 + (2!)^2 + (3!)^3 + \dots (100!)^{100}$

$$1^1 + 2^2 + 6^3 + 24^{24} + \dots$$

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Eg7. $(1!)^1 + (2!)^2 + (3!)^3 + \dots (100!)^{100}$

$$1^1 + 2^2 + 6^3 + 24^{24} + \dots$$

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Eg7. $(1!)^1 + (2!)^2 + (3!)^3 + \dots (100!)^{100}$

$$1^1 + 2^2 + 6^3 + 24^4 + \dots + \dots$$

$$4 + 6 + 61$$

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Eg7. $(1!)^1 + (2!)^2 + (3!)^3 + \dots + (100!)^{100}$

$$1^1 + 2^2 + 6^3 + 24^4 + \dots$$

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Eg7. $(1!)^1 + (2!)^2 + (3!)^3 + \dots\dots\dots(100!)^{100}$

$1^1 + 2^2 + 6^3 + 24^4 + 120^5 + \dots$

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Eg7. $(1!)^1 + (2!)^2 + (3!)^3 + \dots (100!)^{100}$

$$1^1 + (2)^2 + 6^3 + 24^4 + (120)^5 + \dots$$

$$1 + \dots + 6 + \dots$$

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Eg8. $\underline{32}^{33^{34}}$

Step 1 \rightarrow $2^{33^{34}}$

Cycli + y

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Eg8. 32³³³⁴

Step 1 → 2³³ → 2³⁴
 + 4 of 2 4

Step 2

Sahi Prep Hai
 Toh Life Set Hai



Eg9. $37^{39^{41}}$

$$7^{39^{41}}$$

$$\frac{39^{41}}{4} = \frac{(-1)^{41}}{4}$$

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Eg9. $37^{39^{41}}$

$*$

\pm

39^{41}

$$\frac{(-1)^{41}}{4} = -\frac{1}{4}$$

**Sahi Prep Hai
Toh Life Set Hai**

Eg9. $37^{39^{41}}$

$\textcircled{*}$ $37^{39^{41}} \rightarrow 7^?$

$\textcircled{\neq}$

$\frac{-1}{4} \rightarrow = \frac{3}{11}$

Sahi Prep Hai
Toh Life Set Hai

Eg9. $37^{39^{41}}$

$\textcircled{*}$ $7^{39^{41}} \rightarrow 7^3 \rightarrow \textcircled{3}$

$\textcircled{-}$ $7^{41} = (-1)^{41} = -1 \rightarrow 3$

Sahi Prep Hai
Tuh Life Set Hai

From Beginning Custom Show Present online Custom Slide Show Rehearse with Coach Rehearse Set Up Slide Show Hide Slide Rehearse Timings Record Slide Show Keep Slides Updated Use Timings Play Narrations Show Media Controls Monitors Always Use Subtitles Subtitle Settings Captions & Subtitles

Click to add title

Click to add subtitle

Click to add notes

Find unit digit of 30^3

29

28

27

26

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Find unit digit of $30^{31^{32}}$

$9 \equiv 23$
 24
 25
 26
 27
 28
 29

9 odd

Sahi Prep Hai
Toh Life Set Hai

Find unit digit of $30^{31^{32}}$

$27^{28^{29}}$

odd

odd

\Rightarrow

$9^{\text{odd}} \rightarrow 9$

$9^{\text{even}} \rightarrow 1$

**Sahi Prep Hai
Toh Life Set Hai**

Eg10. $9^{23^{32}}$

$$9^{\text{odd}} = 9$$

(i)

(ii)

9

**Sahi Prep Hai
Toh Life Set Hai**

Eg10. $9^{23^{32}}$

$$9^{\text{odd}} = 9$$

(i) $9^{24^{25}}$

(ii)

(iii) (9^{25})

**Sahi Prep Hai
Toh Life Set Hai**

Eg10. $9^{23^{32}}$

$$9^{\text{odd}} = 9$$

(i)

(ii)

$$9^{25^{24}}$$

$$9^{\text{odd}}$$

$$(iii) \left(9^{25}\right)^{24}$$

$$9$$

**Sahi Prep Hai
Toh Life Set Hai**

Eg10. $9^{23^{32}}$

$$9^{\text{odd}} = 9$$

(i) 9^5
even

(ii) $9^{25^{24}}$
odd

(iii) $(9^{25})^{24}$
even

9 ✓

1 ✓

Eg10. $9^{23^{32}}$

$$9^{\text{odd}} = 9$$

(i)

$$9^{24^{25}}$$

9 even

① ✓

(ii)

$$(9^{25})^{24}$$

9 even

① ✓

Eg11. $4^{29^{30}} - 4^{30^{29}}$

odd - 4 even

**Sahi Prep Hai
Toh Life Set Hai**

Eg11. $4^{29^{30}} - 4^{30^{29}}$

odd - 4 even

1 - 6 = -2

**Sahi Prep Hai
Toh Life Set Hai**

PyQ of SSC

Eg12. If the unit digit of $833 \times 856 \times 43N$ is $N+2$, then what is the value of N ?

- (a) 2
- (b) 3
- (c) 4
- (d) 6

Sahi Prep Hai
Toh Life Set Hai

PYQ of SSC

Eg12. If the unit digit of $\underline{833} \times \underline{856} \times \underline{43N}$ is $\underline{N+2}$, then what is the value of \underline{N} ?

(a) 2

(b) 3

3. 6.

Sahi Prep Hai
Toh Life Set Hai

PyQ of SSC

Eg12. If the unit digit of $\underline{833} \times \underline{856} \times \underline{43N}$ is $\underline{N+2}$, then what is the value of \underline{N} ?

(a) 2

(b) 3

(c)

$$3 \cdot 6 \cdot N \rightarrow N+2$$

$$(a) \quad 3 \cdot 6 \cdot 2$$

**Sahi Prep Hai
Toh Life Set Hai**

PyQ of SSC

Eg12. If the unit digit of $\underline{833} \times \underline{856} \times \underline{43N}$ is $\underline{N+2}$, then what is the value of \underline{N} ?

(a) 2

(b) 3

$$3 \cdot 6 \cdot N \rightarrow N+2$$

$$(a) \quad 3 \cdot 6 \cdot 2 \rightarrow 2+2 \quad \times$$

$$(b) \quad 3 \cdot 6 \cdot 3$$

**Sahi Prep Hai
Toh Life Set Hai**

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots 99^{99!} + 100^{100!}$

Level of this question $\uparrow\uparrow$

Sahil Prep Hall
Jinh Life Set Hall

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots 99^{99!} + 100^{100!}$

$$1^{1!} + 2^{2!} + 3^{3!} + 4^{4!} + 5^{5!} + 6^{6!} + \dots$$

Sahi Prep Hai
Toh Life Set Hai

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots 99^{99!} + 100^{100!}$

$$1^{1!} + 2^{2!} + 3^{3!} + 4^{4!} + 5^{5!} + 6^{6!} + 7^{7!} + \dots$$

Sahi Prep Hai
Toh Life Set Hai

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots 99^{99!} + 100^{100!}$

$$1^{1!} + 2^{2!} + 3^{3!} + 4^{4!} + 5^{5!} + 6^{6!} + 7^{7!} + 8^{8!} + 9^{9!} + 10^{10!}$$

$$11^{11!} + 12^{12!} + 13^{13!} + \dots + 20^{20!}$$

Sahi Prep Hai
Toh Life Set Hai

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots + 99^{99!} + 100^{100!}$

$$1^{1!} + 2^{2!} + 3^{3!} + 4^{4!} + 5^{5!} + 6^{6!} + 7^{7!} + 8^{8!} + 9^{9!} + 10^{10!}$$

$$11^{11!} + 12^{12!} + 13^{13!} + \dots + 20^{20!}$$

$$91^{91!} + 92^{92!} + \dots + 100^{100!}$$

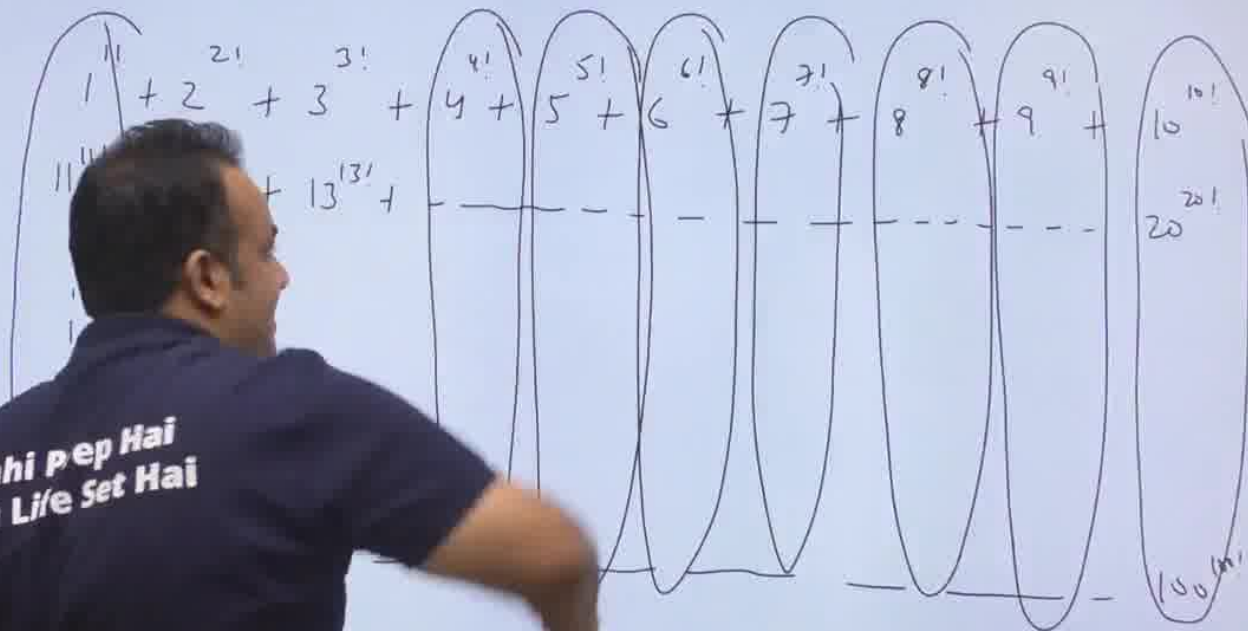
Sahi Prep Hai
Toh Life Set Hai

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots + 99^{99!} + 100^{100!}$

$$\begin{array}{cccccccccccc}
 & 1! & 2! & 3! & 4! & 5! & 6! & 7! & 8! & 9! & 10! \\
 1 & + 2 & + 3 & + 4 & + 5 & + 6 & + 7 & + 8 & + 9 & + 10 & + \dots \\
 11^{1!} & + 12^{12!} & + \dots & + 20^{20!} & + \dots & + 100^{100!}
 \end{array}$$

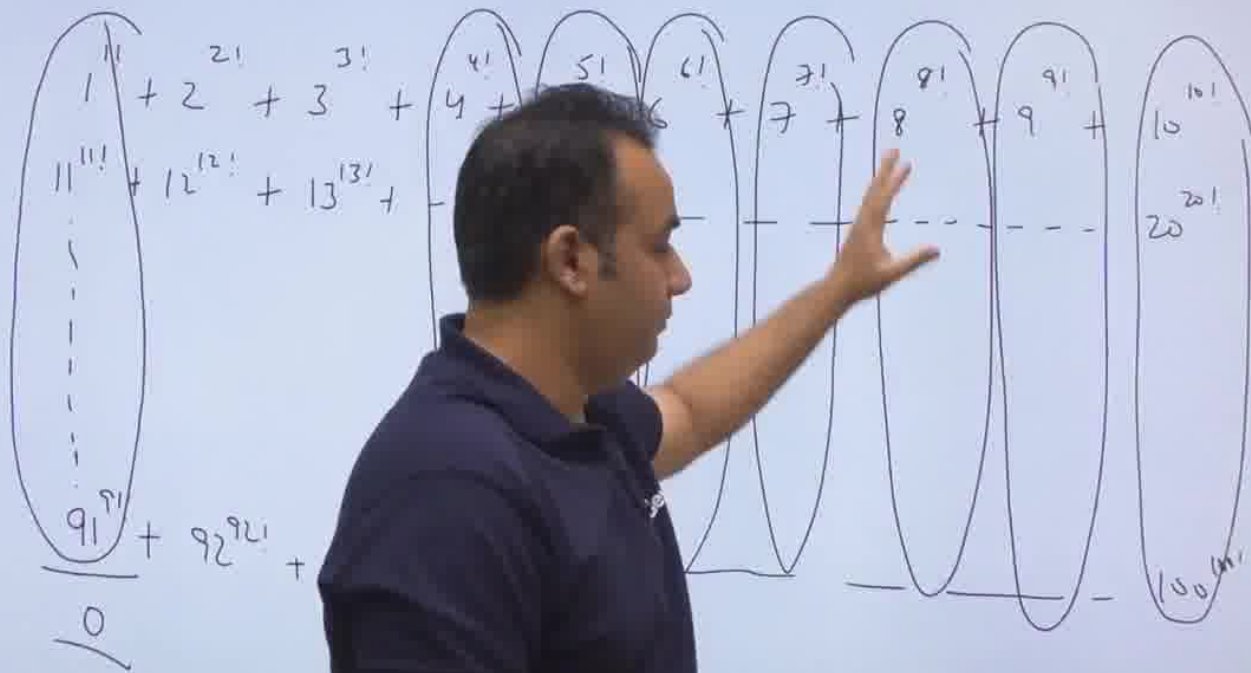
The diagram shows a vertical list of terms: $1^{1!}, 11^{1!}, 12^{12!}, \dots, 91^{9!}, 100^{100!}$. A vertical dashed line is drawn to the left of the terms, and a horizontal dashed line is drawn below the terms. The term $100^{100!}$ is circled.

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots + 99^{99!} + 100^{100!}$



Sahi pep Hai
Toh Life Set Hai

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots + 99^{99!} + 100^{100!}$



Ans.

$$\begin{array}{r} 24 \\ 4 \overline{) 2} \end{array}$$

$$\begin{array}{r} 34 \\ 9 \overline{) 3} \end{array}$$

$$\begin{array}{r} 12' \\ 6 \overline{) 12} \\ 22' \\ \vdots \\ 92' \end{array}$$

$$\begin{array}{r} 13' \\ 1 \overline{) 13} \\ \vdots \\ 93' \end{array}$$

$$8 + 8$$

Sahi Prep Hai
Toh Life Set Hai

Eg14. $1^{1!} + 2^{2!} + 3^{3!} + \dots + 99^{99!} + 100^{100!}$

Sahi Prep Hai
Toh Life Set Hai

Ans.

$$2^{2'}$$

$$3^{2'}$$

Sahi Prep Hai
Toh Life Set Hai

Ans.

$$2^{2!}$$

$$3^{3!}$$

$$12^{12!}$$

$$13^{13!}$$

}

1

$$93^{93}$$

**Sahi Prep Hai
Toh Life Set Hai**

Ans.

$$\textcircled{4} \quad \frac{2^{2'}}{2}$$

$$\frac{2^{12'}}{2^{22'}}$$

$$\frac{3^{3'}}{3}$$

$$\frac{13^{13'}}{13}$$

$$\frac{93^{931}}{93}$$

Sahi Prep Hai
Toh Life Set Hai

PyQ of SSC

Eg12. If the unit digit of $\underline{833} \times \underline{856} \times \underline{43N}$ is $\underline{N+2}$, then what is the value of N ?

(a) 2

(b) 3

(c) 4

(d) 6

$$3 \cdot 6 \cdot N \rightarrow N+2$$

$$(a) \quad 3 \cdot 6 \cdot 2 \rightarrow 2+2 \quad \times$$

$$(b) \quad 3 \cdot 6 \cdot 3 \rightarrow 3+2 \quad \times$$

$$(c) \quad 3 \cdot 6 \cdot 4 \rightarrow 4+2 \quad \times$$

Eg15. $1^1 + 2^2 + 3^3 + 4^4 + \dots 100^{100}$

HOMEWORK