

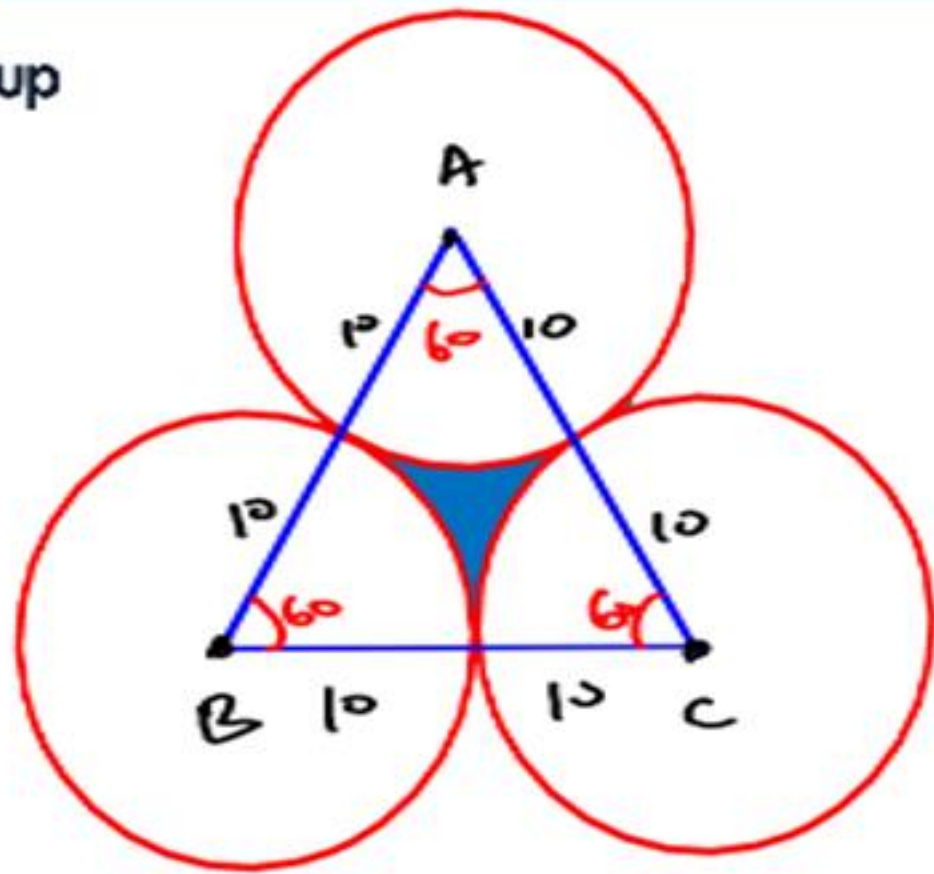


Sahi Prep Hai Toh Life Set Hai

# MENSURATION-2D

## Part – 3



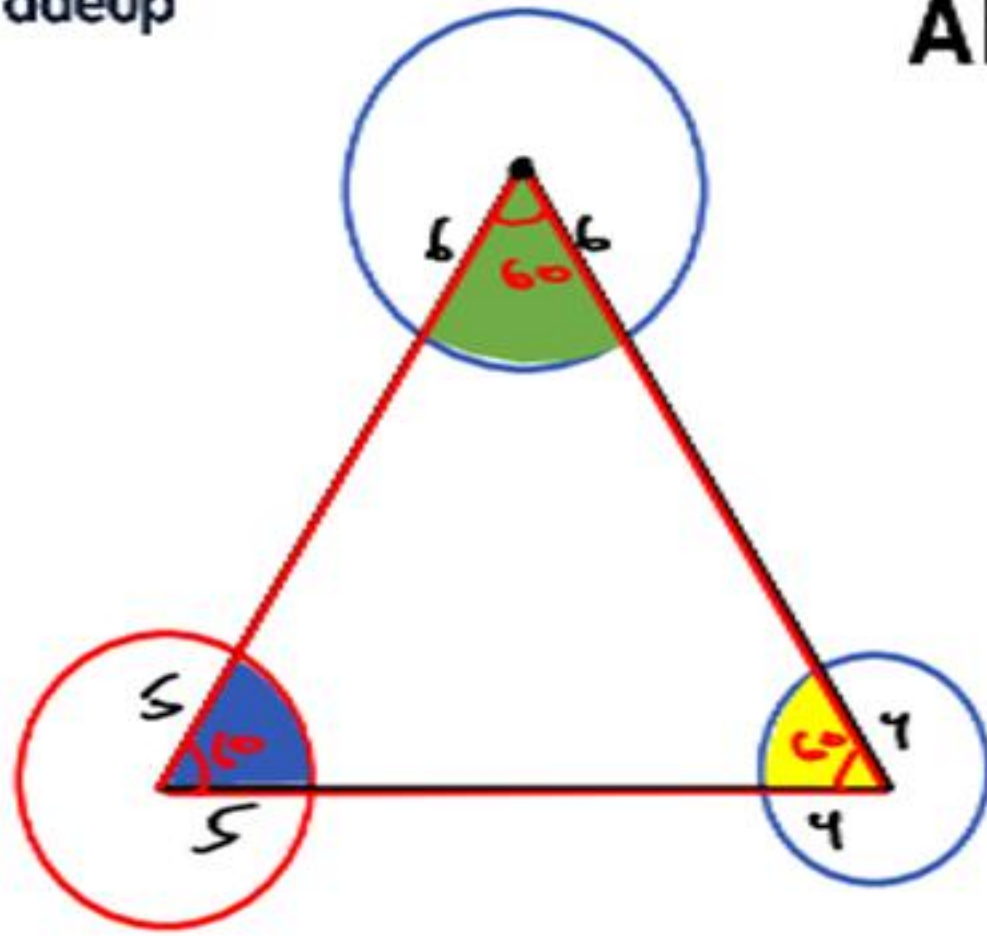


Eg. Radius of each of the circle is 10 cm. Find the area of shaded region.

$$\begin{aligned}
 \text{Area of shaded Part} &= \text{Area of } \triangle - \frac{1}{2} \text{ Circle} \\
 &= \frac{\sqrt{3}}{4} \cdot (20)^2 - \frac{1}{2} \pi \cdot 10^2 \\
 &= 100\sqrt{3} - 50\pi
 \end{aligned}$$

**Ans.**  $(100\sqrt{3} - 50\pi) \text{ cm}^2$

## AREA GRAZED BY COW



An equilateral triangle whose side is 20 cm. Find the area grazed by the cows if they are attached by rope of length 6 cm, 5 cm and 4 cm on the 3 vertices.

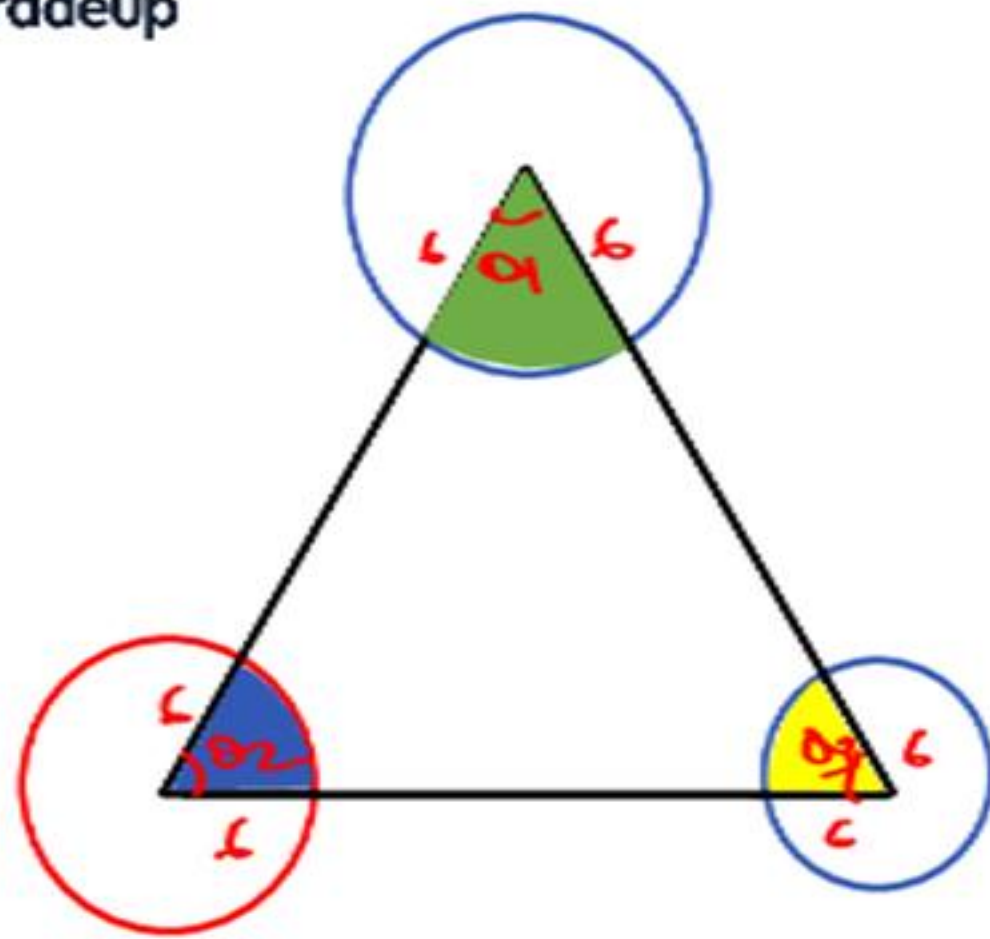
$$\frac{1}{6} \pi 6^2 + \frac{1}{6} \pi \cdot 5^2 + \frac{1}{6} \pi \cdot 4^2$$

$$\frac{1}{6} \cdot \frac{22}{7} [36 + 25 + 16]$$

$$\frac{1}{6} \cdot \frac{22}{7} \cdot 77 = \frac{121}{3} \text{ cm}^2$$

**Ans.**  $\frac{121}{3} \text{ cm}^2$





Eg. A triangle whose sides are 20 cm, 18 cm and 16 cm. Find the area grazed by the cows if they are attached by rope of length 6 cm on all the 3 vertices.

$$\frac{\pi \cdot 6^2 \cdot \theta_1}{360} + \frac{\pi \cdot 6^2 \cdot \theta_2}{360} + \frac{\pi \cdot 6^2 \cdot \theta_3}{360}$$

$$\frac{\pi \cdot 6^2}{360 \cdot 2} [180]$$

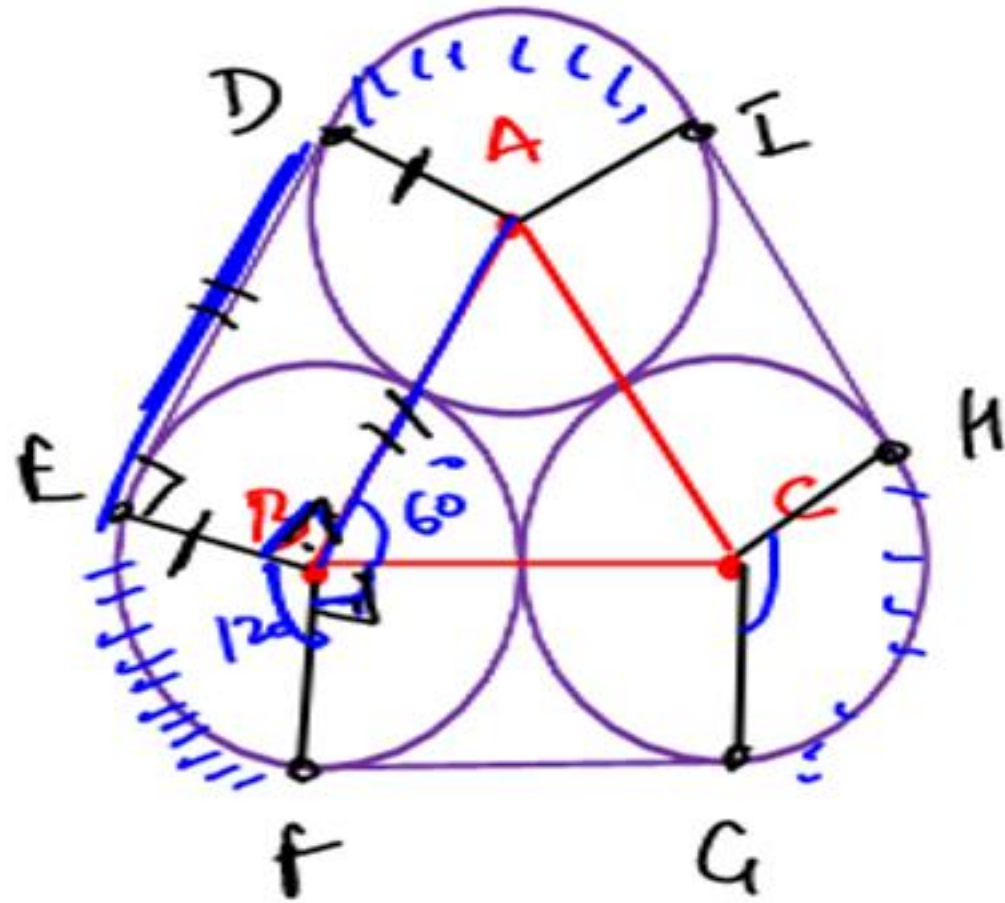
$$= \underline{\underline{18 \pi \text{ cm}^2}}$$

**Ans.**  $\frac{396}{7} \text{ cm}^2$



# LENGTH OF RUBBER BAND

✓.amp



If the radius of each circle is 10 cm.  
Find the length of rubber band.

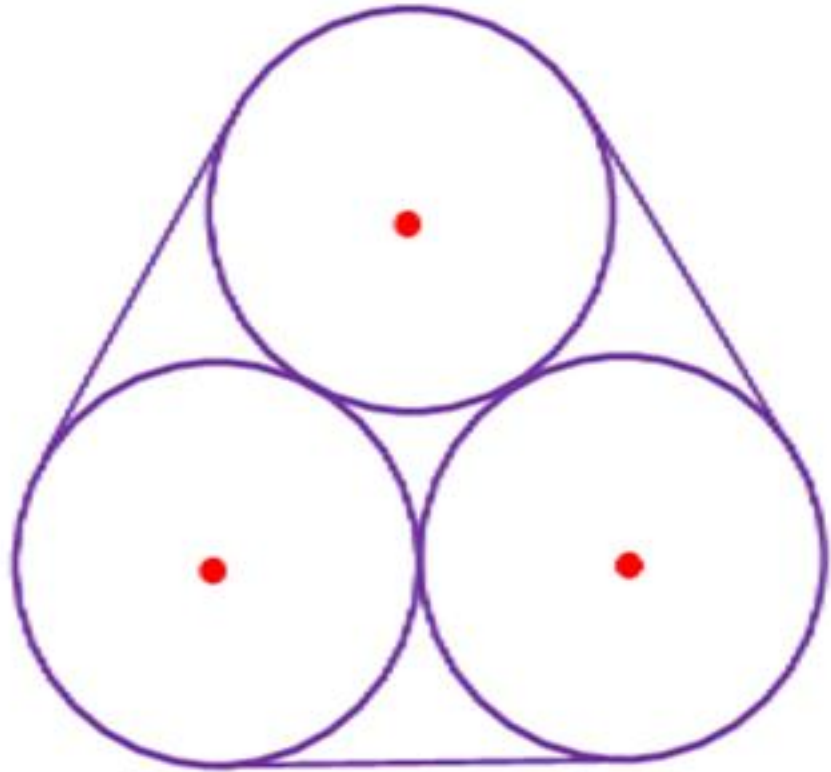
length of Rubber Band

$$= DE + FG + IH + \widehat{EF} + \widehat{GH} + \widehat{ID}$$

↓

$$20 + 20 + 20 + 2\pi \cdot 10$$

$$60 + 20\pi$$

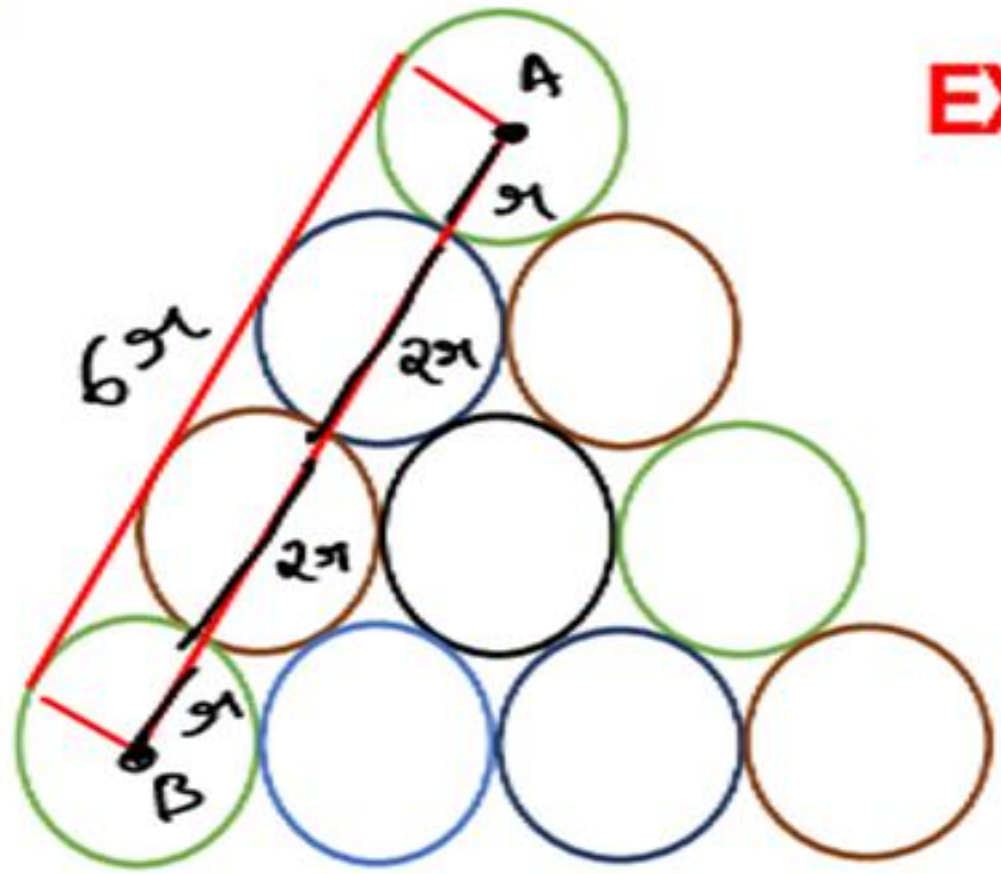


Shortcut



$$6R + 2\pi R$$





## EXTENSION OF RUBBER BAND QUESTIONS

Eg If radius of each circle is  $r$ . Find the length of Rubber band ??

$$\rightarrow \underline{18r + 2\pi r}$$



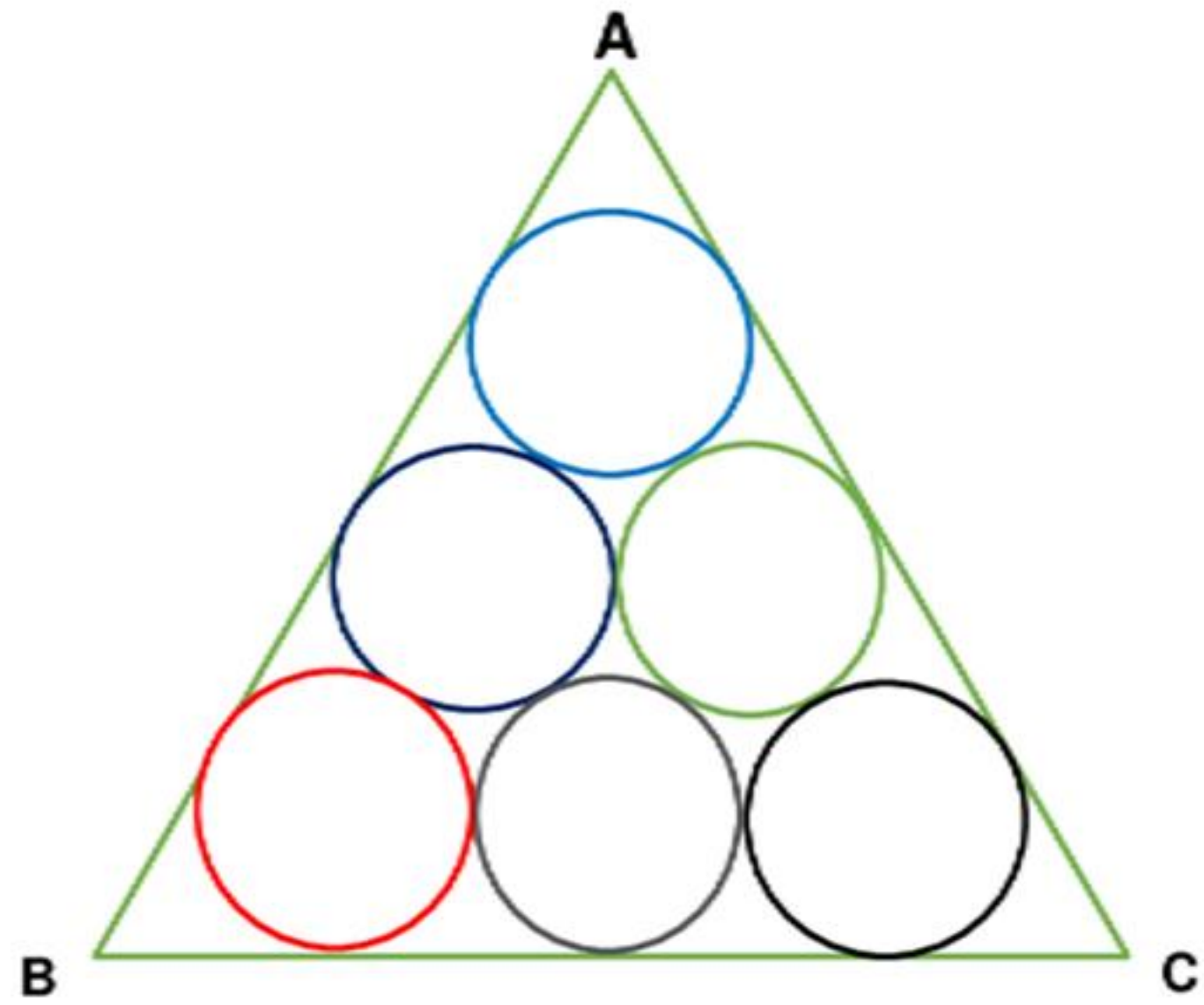


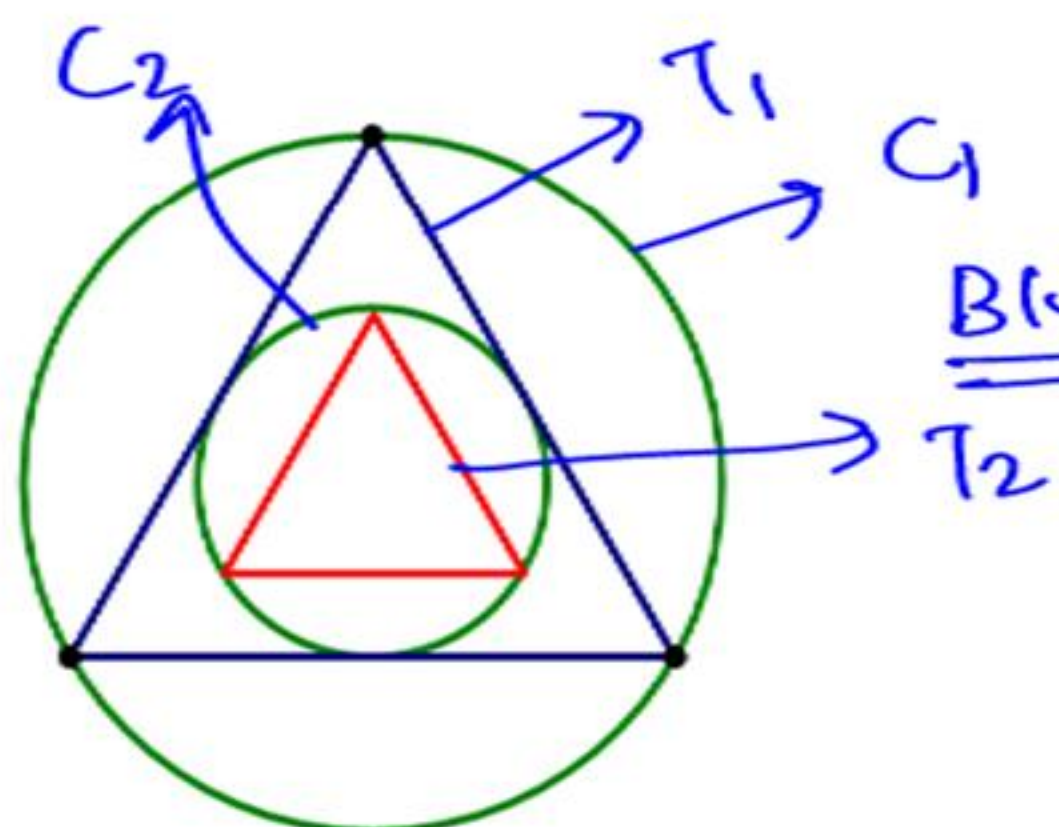












# Equilateral $\Delta$

Blue Triangle  $\rightarrow$  side  $S$

If  $r$  = inradius

$R$  = circumradius

$S$  = Side of equilateral triangle

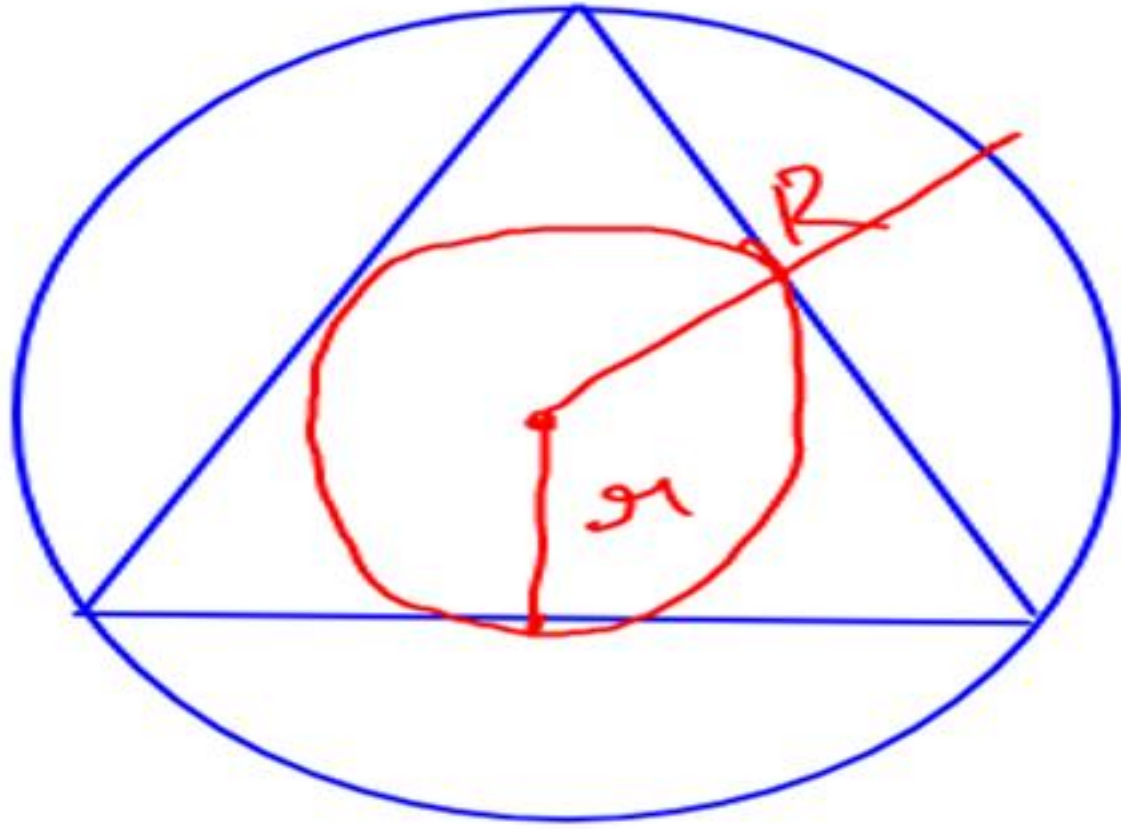
$$\frac{r_2}{r_1} = \frac{1}{2}$$

radius of  $C_2 = \frac{S}{2\sqrt{3}}$

radius of  $C_1 = \frac{S}{\sqrt{3}}$

$$\frac{\text{Side of } \Delta T_2}{\text{Side of } \Delta T_1} = \frac{1}{2}$$



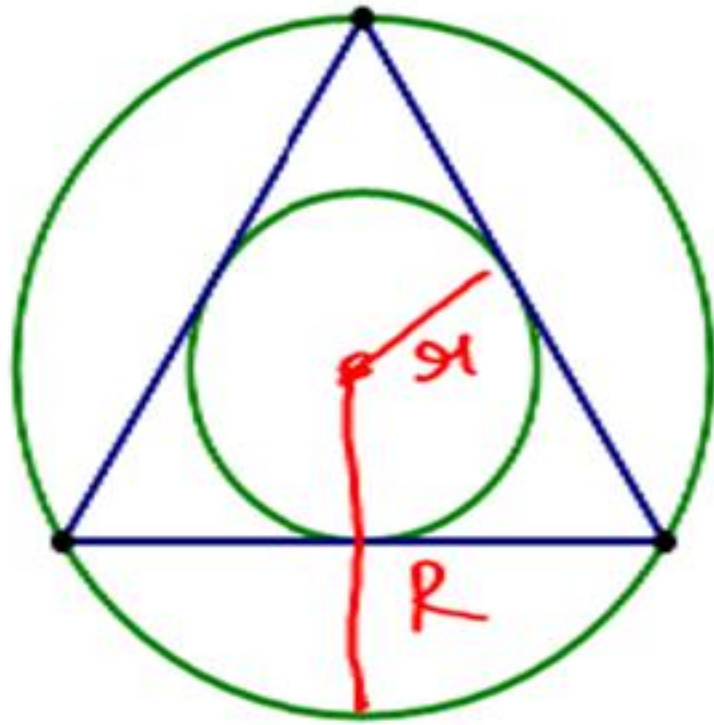


If side of eq  $\Delta = 12\text{cm}$

$$r = ?? \frac{12}{2\sqrt{3}} = 2\sqrt{3}$$

$$R = ?? \frac{12}{\sqrt{3}} = 4\sqrt{3}$$

## Equilateral $\Delta$



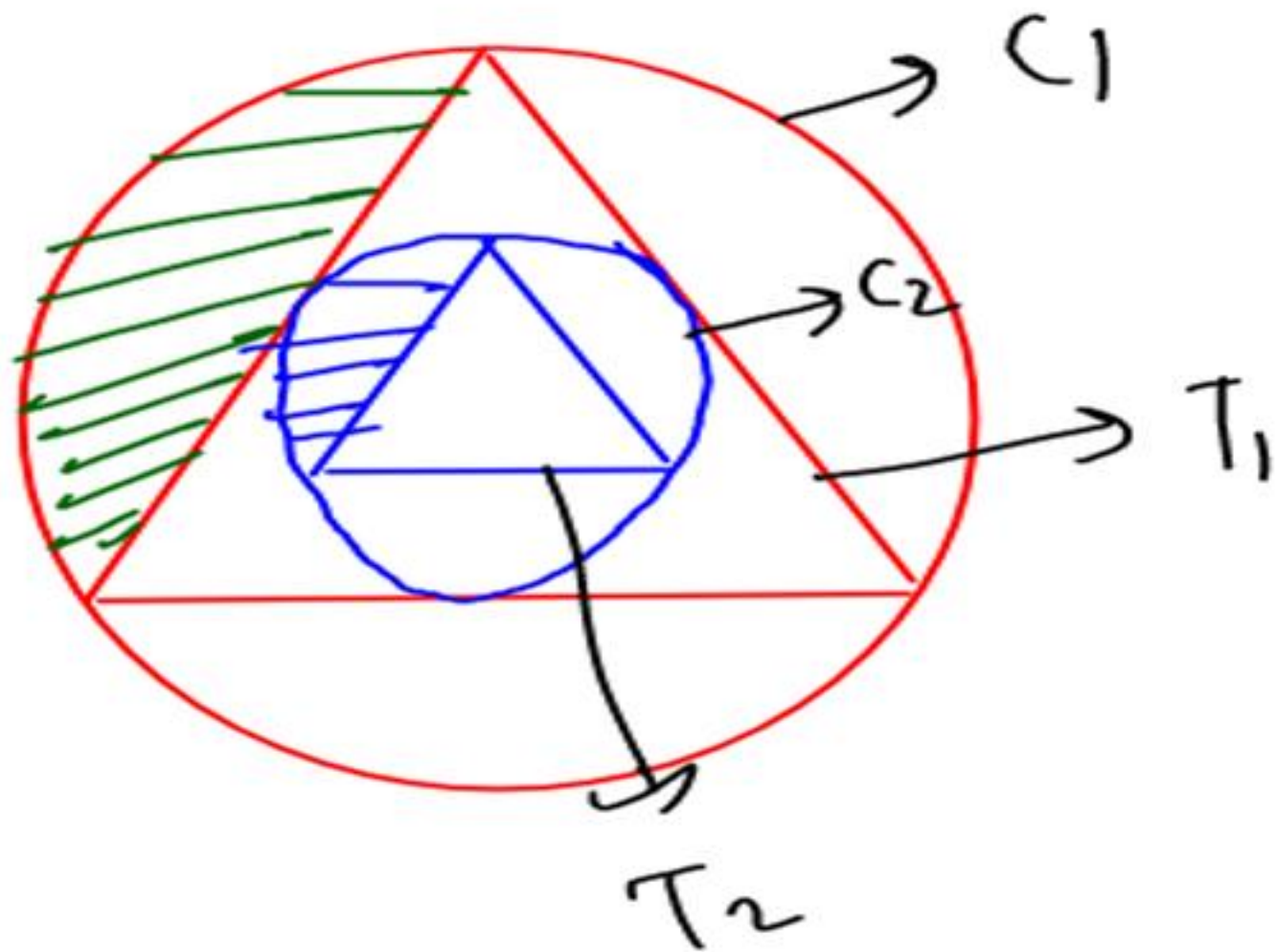
(i) Find :  $\frac{r}{R} \rightarrow \frac{1}{2}$

✓ (ii)  $\frac{\text{Area of incircle}}{\text{Area of circumcircle}} \rightarrow \frac{1}{4}$

(iii) Find the ratio of  $r : S : R$

$$\frac{S}{2\sqrt{3}} : S : \frac{S}{\sqrt{3}}$$

✓  $\boxed{1 : 2\sqrt{3} : 2}$



$$\frac{\text{radius of } C_1}{\text{radius of } C_2} = \frac{2}{1}$$

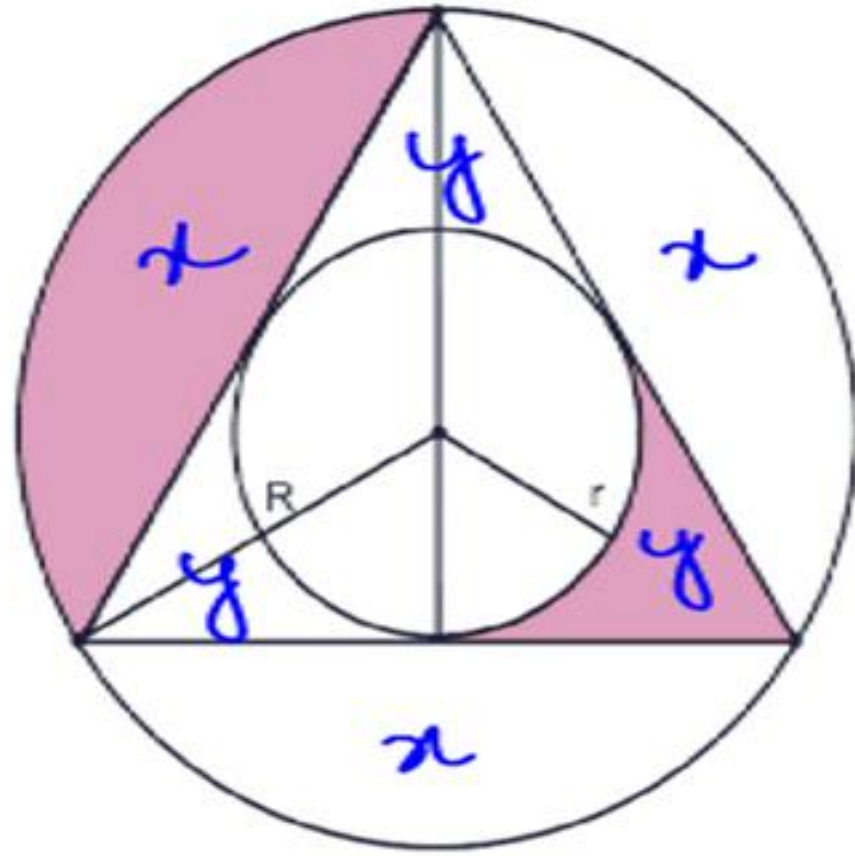
$$\frac{\text{side of } T_1}{\text{side of } T_2} = \frac{2}{1}$$

Green shaded  
Blue shaded

$$\frac{4}{1}$$



Eg. If side of an equilateral triangle is 12 cm. Find the area of shaded region.



Time 90 sec

$$x + y = ?$$

$$3x = \text{Area of Bigger Circle} - \text{Area of } \triangle \quad \text{--- (1)}$$

$$3y = \text{Area of } \triangle - \text{Area of smaller circle} \quad \text{--- (2)}$$

$$\text{(1)} + \text{(2)}$$

$$3(x+y) = \pi R^2 - \pi r^2$$

$$3(x+y) = \pi (4\sqrt{3})^2 - \pi (2\sqrt{3})^2$$

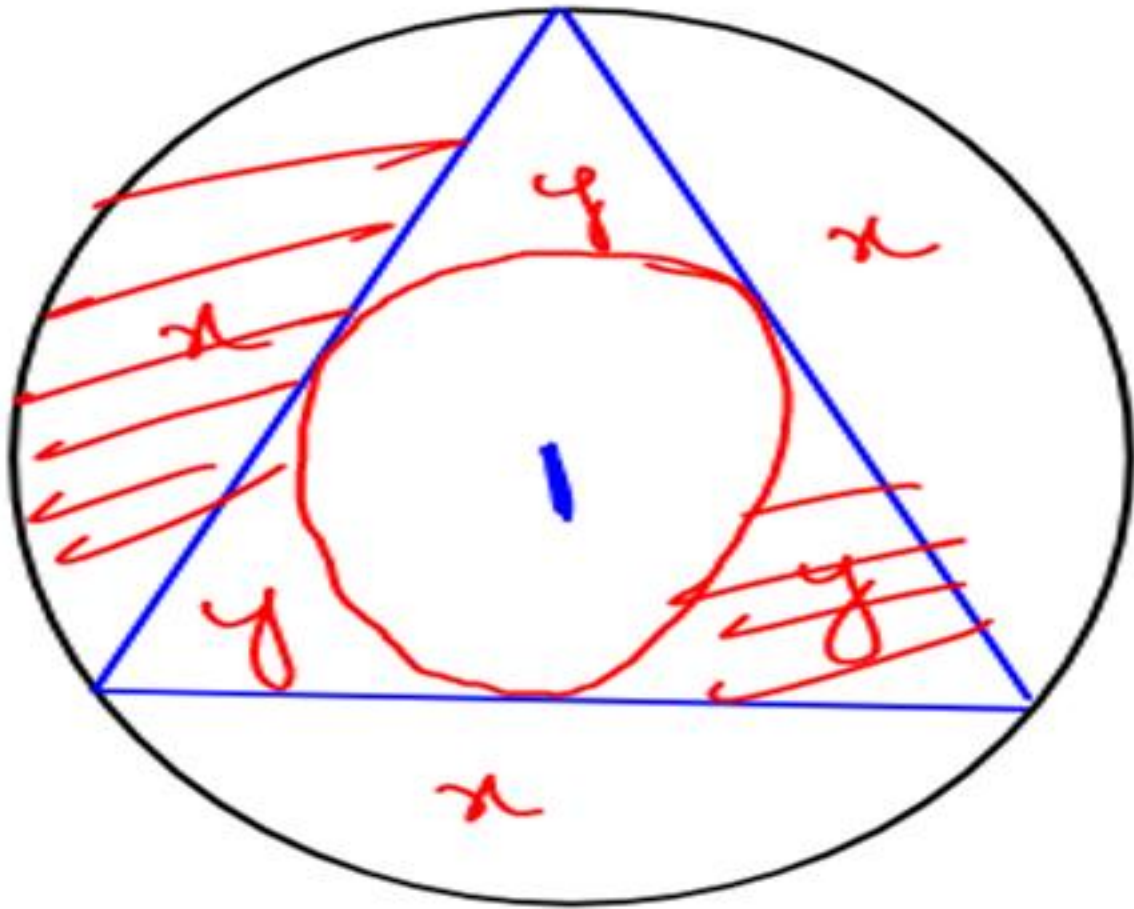
$$3(x+y) = 36\pi$$

$$\underline{\underline{x+y = 12\pi}}$$

Ans.  $12\pi$

$$S = 12\text{cm}$$

$$x+y$$



Let Area of smaller circle

→ 1 unit

Area of Bigger circle

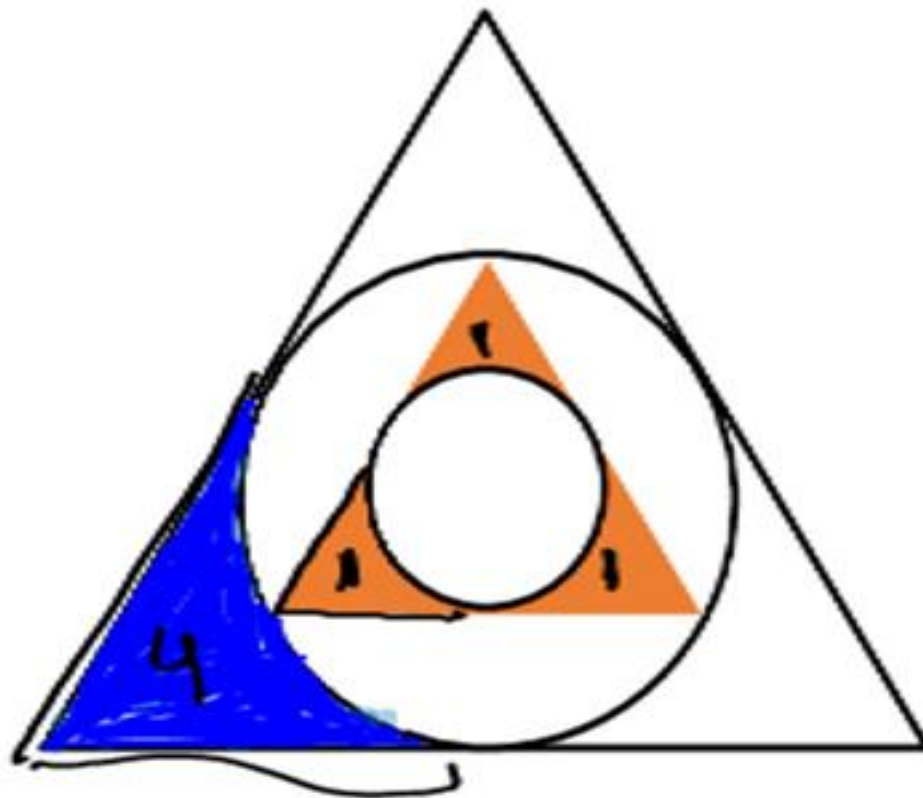
→ 4 unit

$$1 + 3y + 3x = 4$$

$$x + y = 1$$

$$\pi \cdot x^2 = \pi \left( \frac{12}{2\sqrt{3}} \right)^2 = \underline{\underline{12\pi}}$$

# Equilateral $\Delta$

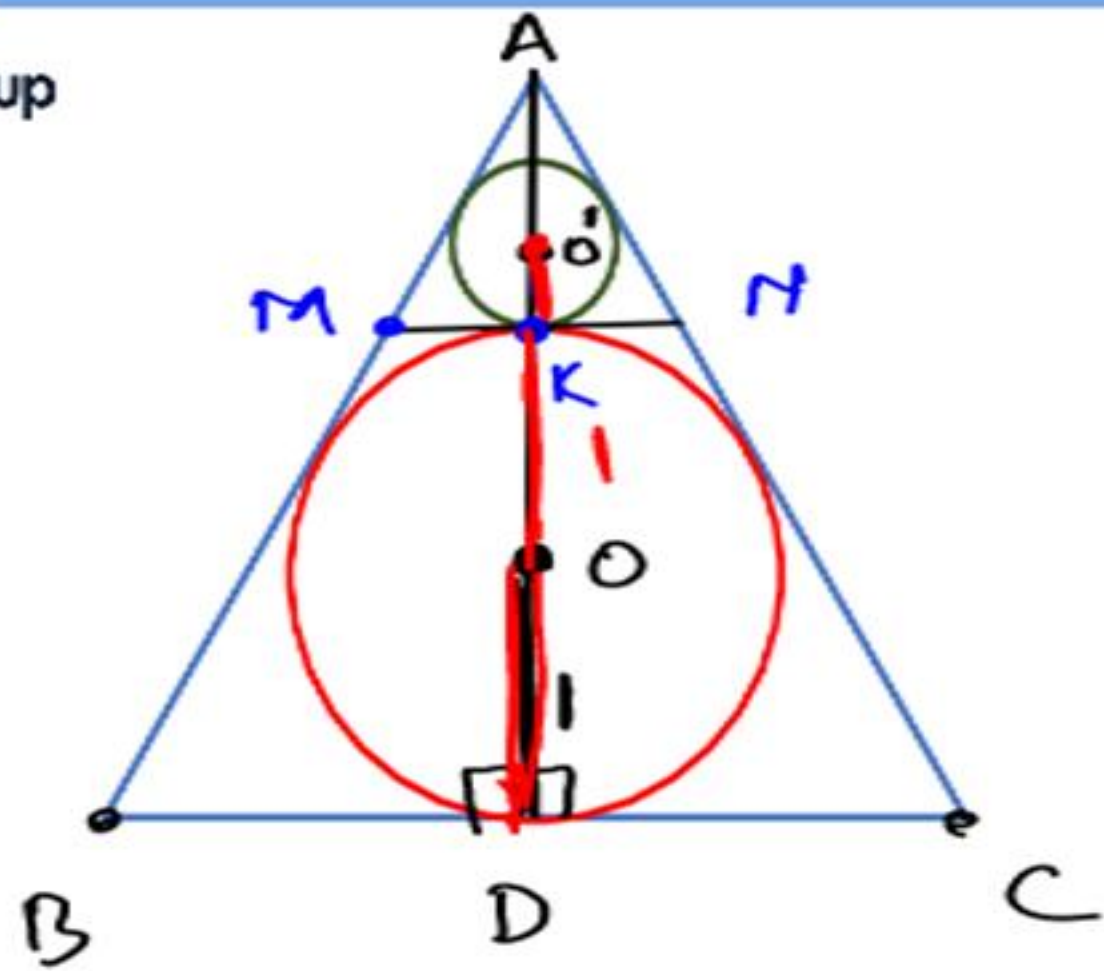


Eg. Find :  $\frac{\text{Area of Orange region}}{\text{Area of Blue region}}$

$$= \frac{3}{4}$$



**Ans. 3 : 4**



Equilateral  $\Delta$

Eg. Find :  $\frac{r}{R}$

$$= \frac{1}{3}$$

v. imp

$O \rightarrow$  Centroid  $\Delta ABC$

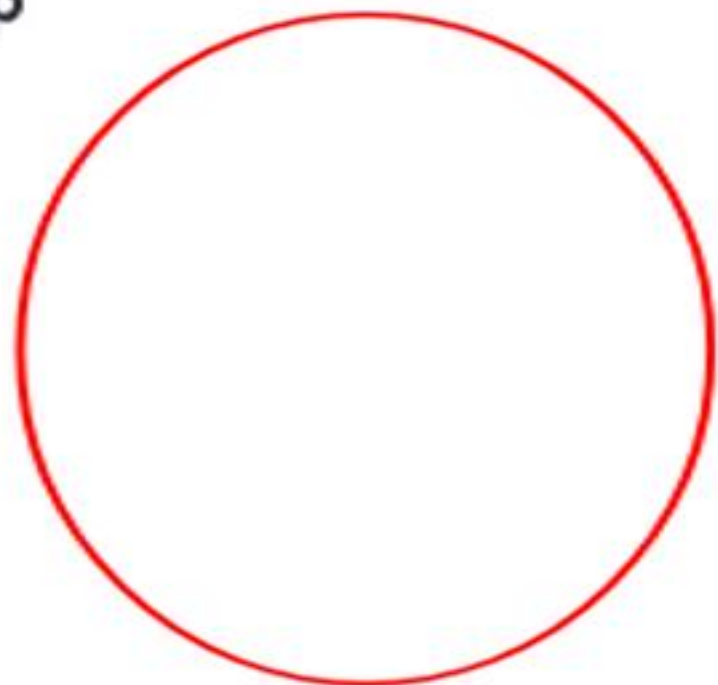
$$\frac{AO}{OD} = \frac{2}{1}$$

$$\begin{aligned} \text{If } OD = 1, \quad OK = 1 \\ AK = 1 \quad AO' = \frac{2}{3} \quad O'K = \frac{1}{3} \end{aligned}$$

$$\frac{O'K}{OK} = \frac{\frac{1}{3}}{1} = \frac{1}{3}$$

**Ans. 1 : 3**





$$\text{Area of Circle} \rightarrow \pi R^2$$

$$\underline{\underline{\text{Area of Circle}}} \propto \underline{\underline{R^2}}$$

$$\propto \underline{\underline{(\text{Diameter})^2}}$$

Radius  
Area

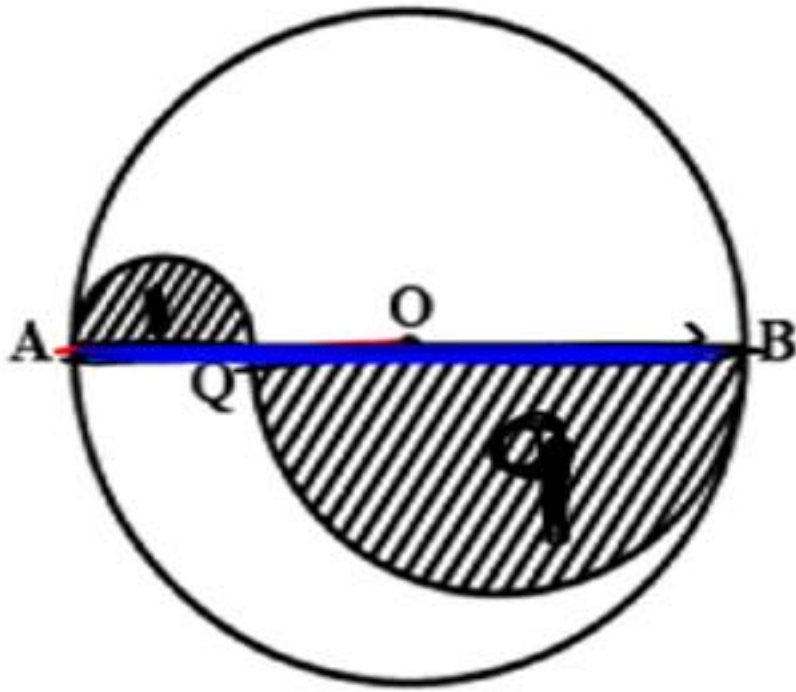
$C_1$   
3  
9  
✓✓

:

:

$C_2$   
5  
25  
✓✓

$C_1$   $C_2$   
Diameter 3 : 5  
Area 9 : 25



Diameter of bigger circle (AB) = 12 cm

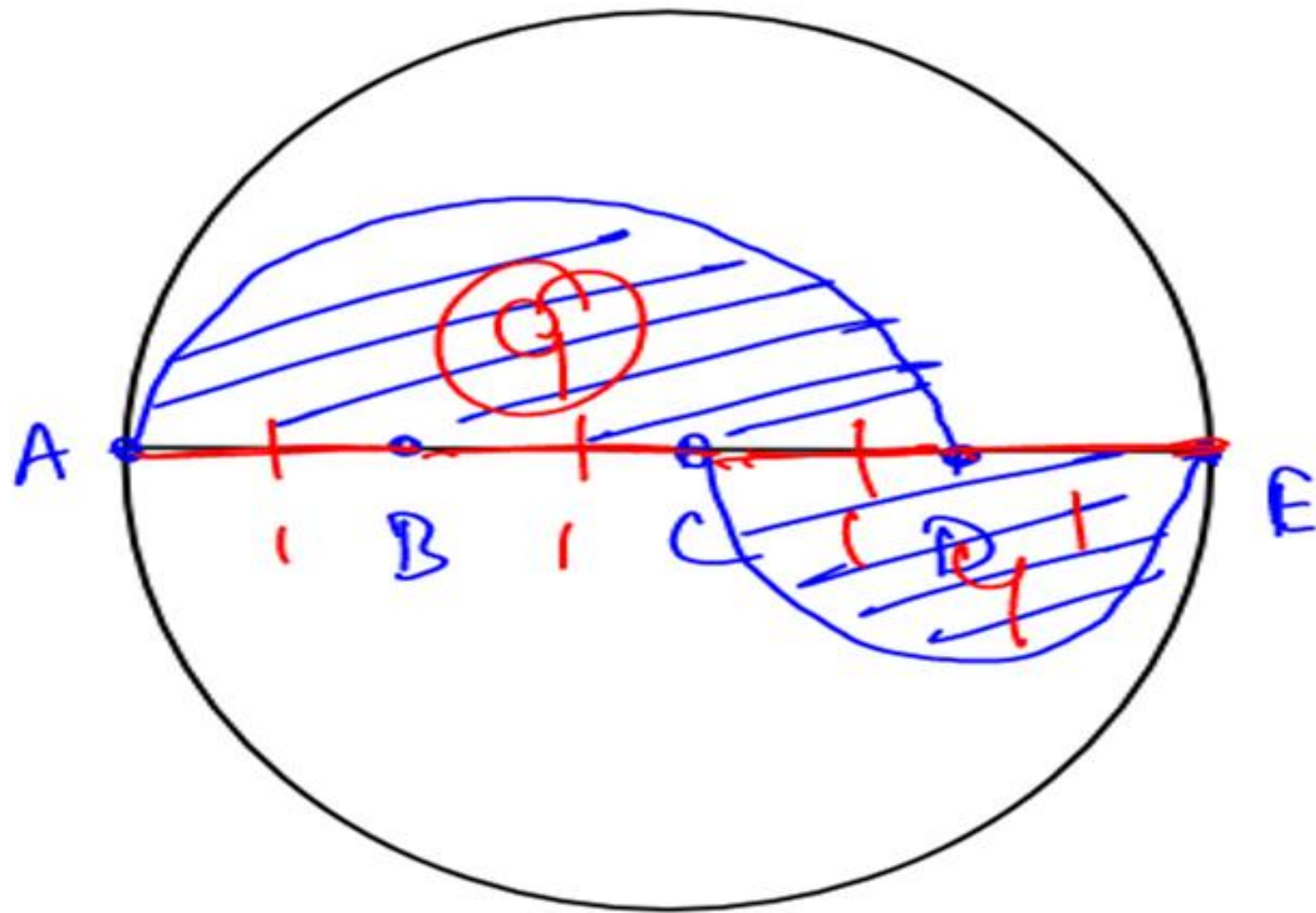
If  $AQ = QO$  and O is centre of the bigger circle

Semi-circles are drawn taking AQ and QB as diameter as shown in the figure.

Find :  $\frac{\text{Area of shaded part}}{\text{Area of complete circle}} = \frac{105}{3216}$

If  $AQ = 1$   $QO = 1$   $OB = 2$

**Ans. 5 : 16**

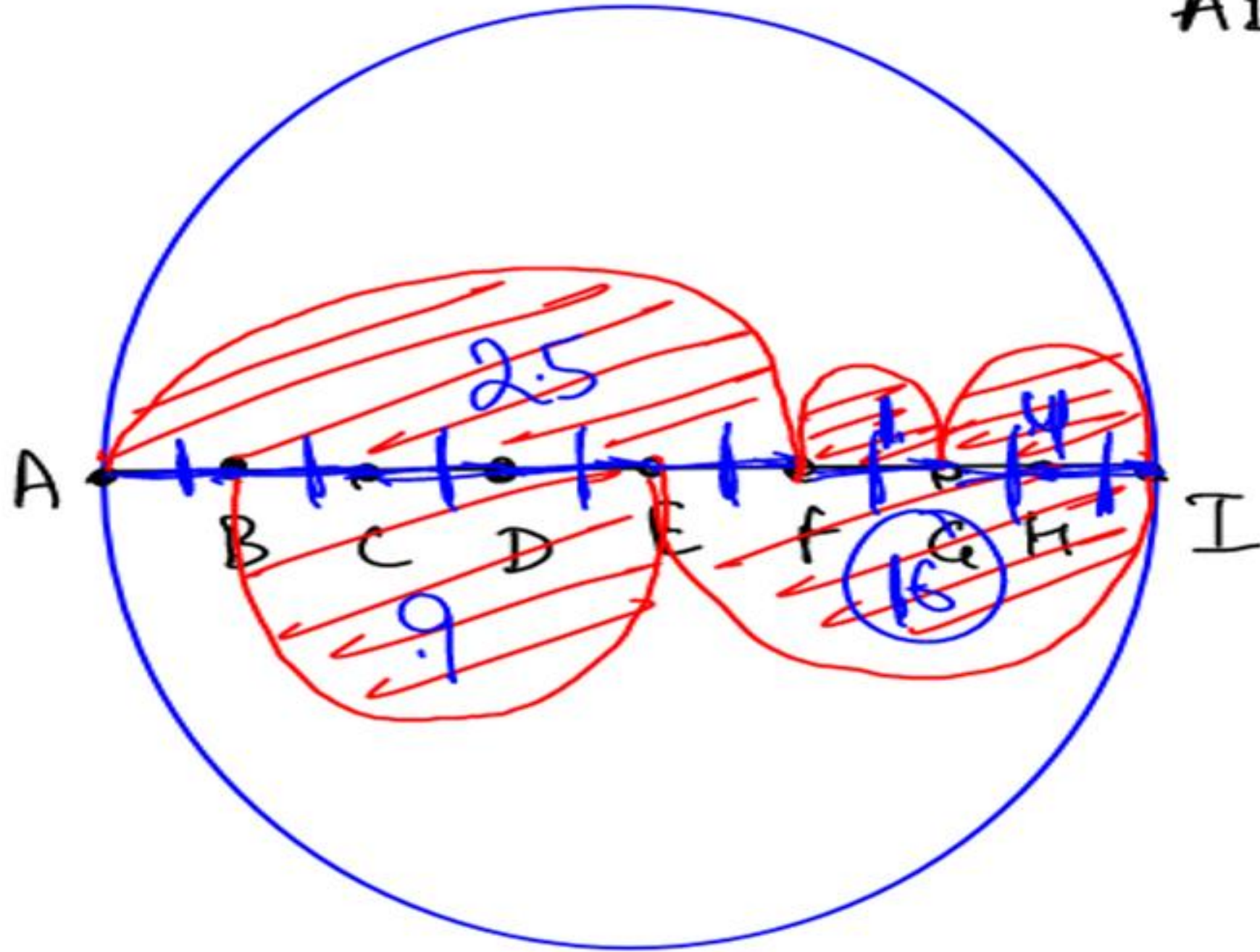


$$AB = BC = CD = DE$$

$$\frac{\text{Area of shaded}}{\text{Area of Complete Circle}} = \frac{13}{32}$$

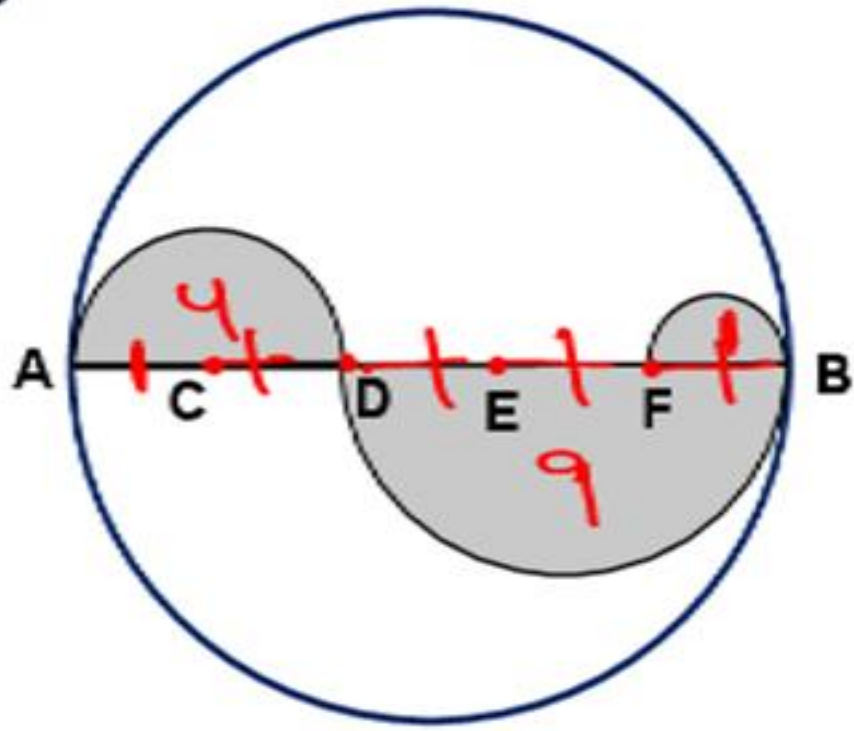


$$AB = BC = CD = DE = EF = FG = GH = HI$$



Shaded part  
Complete circle

$$= \frac{55}{128}$$



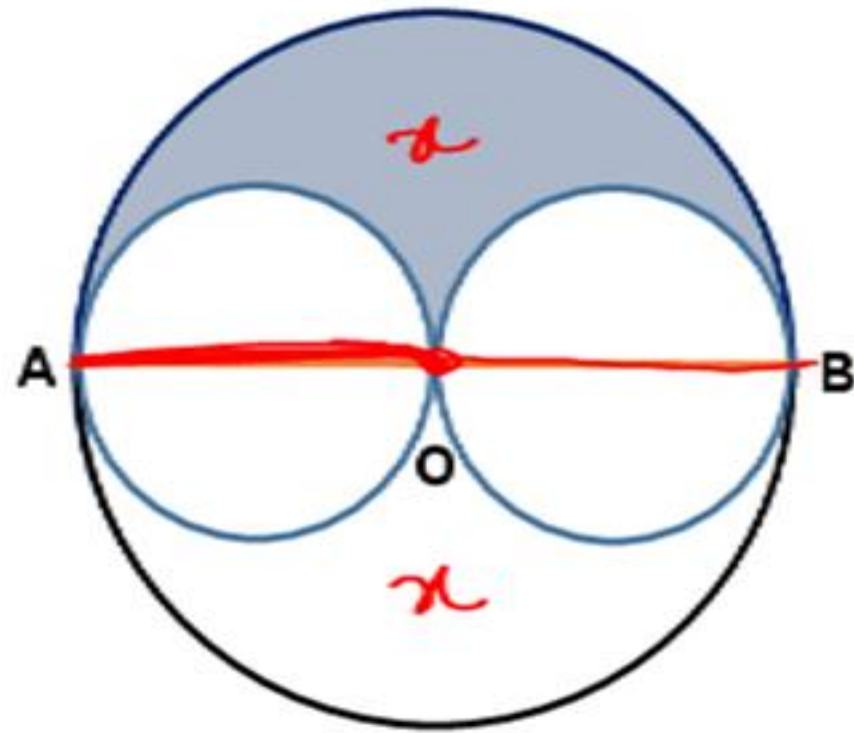
$AB = \text{Diameter of bigger circle}$

$AC = CD = DE = EF = FB$

Find :  $\frac{\text{Area of shaded part}}{\text{Area of complete circle}} = \frac{14}{25}$



**Ans. 7 : 25**



Eg. O is centre of larger circle.

AB is diameter

AB = 20 cm

Find the area of shaded part.

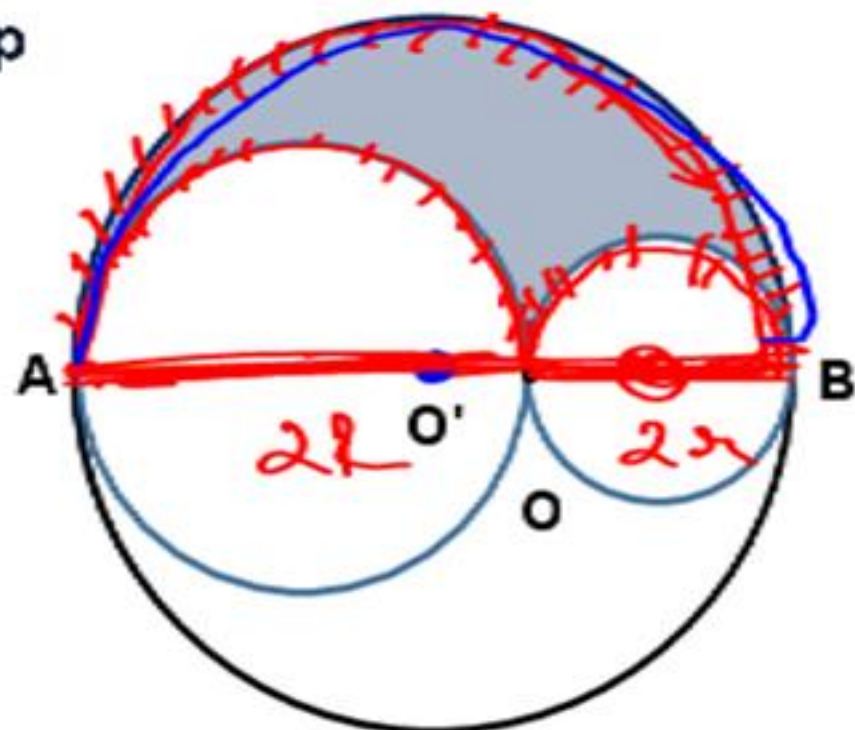
$$2x = \text{Area of Bigger circle} - 2 \text{ Area of smaller circle}$$

$$2x = \pi(10)^2 - 2(\pi 5^2)$$

$$2x = 50\pi$$

$$\boxed{x = 25\pi}$$

**Ans  $25\pi$**



O' is the centre of the larger circle

AB = 20 cm

AO and OB are diameters of smaller circle

(i) Find the area of shaded region.

(ii) Find circumference of shaded region.

$$2r + 2R = 20$$

$$r + R = 10$$

(i)  $\rightarrow$  Can't be determined b/c

we don't know the value of radius of smaller circles.

(ii)

$$\pi \cdot 10 + \pi \cdot r + \pi \cdot R$$

$$10\pi + \pi(R + r)$$

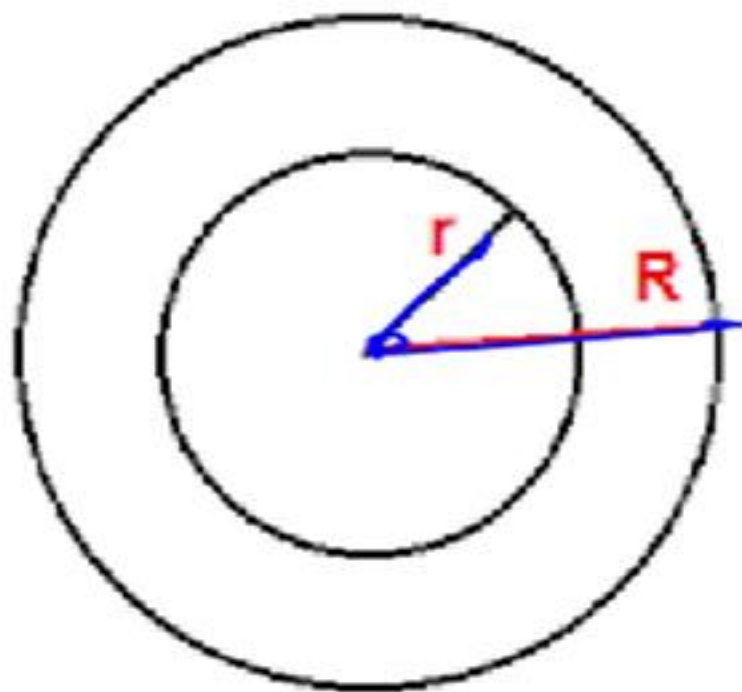
$$10\pi + \pi(10) = \underline{\underline{20\pi \text{ cm}}}$$



**Ans. (i) Can't be determined**

**(ii)  $20\pi$**

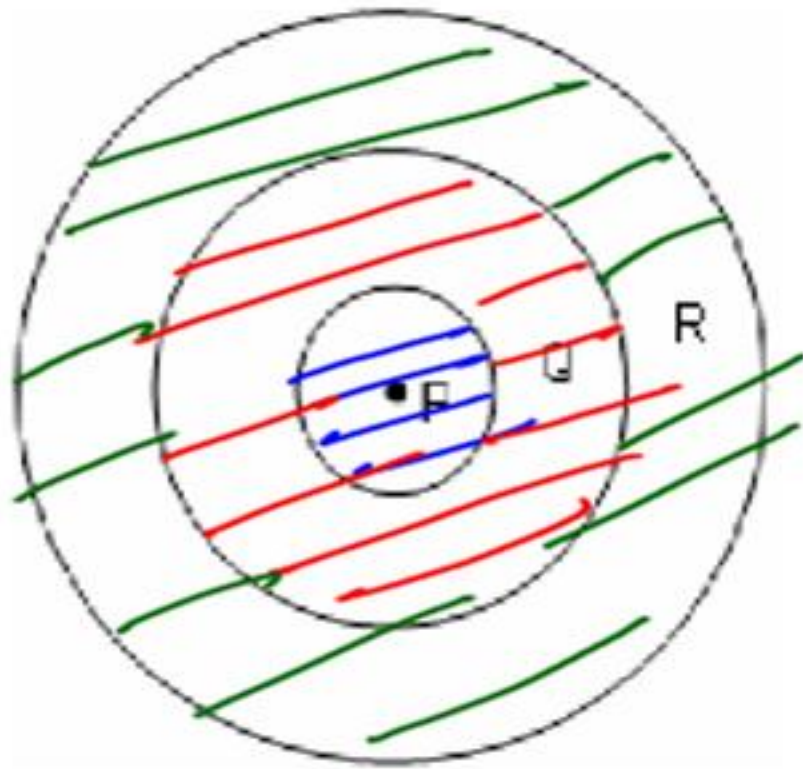
# CONCENTRIC CIRCLES



Circles with the same centre.

Radius of circles are in the ratio 1 : 2 : 3

Find the ratio of areas of region P : Q : R



Blue  
P

Red  
Q

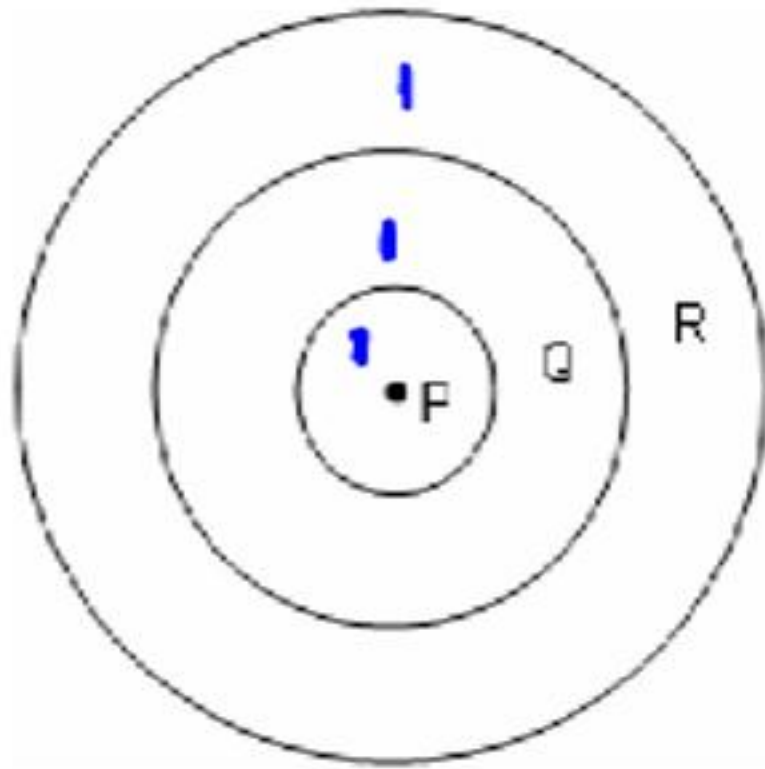
Green  
R

Area of circles  $\rightarrow$   $\begin{matrix} P \\ 1 \end{matrix} : \begin{matrix} P+Q \\ 4 \end{matrix} : \begin{matrix} P+Q+R \\ 9 \end{matrix}$

P : Q : R  
1 : 3 : 5 ✓

If area of region P, Q and R are equal and radius of the largest circle is 12 cm.

Find the radius of the smallest circle.



$$\frac{\text{Area of smallest circle}}{\text{Area of biggest circle}} = \frac{1}{3}$$

$$\frac{\text{radius of smallest circle}}{\text{radius of largest circle}} = \frac{1}{\sqrt{3}}$$

$$\frac{x}{12} = \frac{1}{\sqrt{3}} \quad \underline{\underline{x = 4\sqrt{3}}}$$



Ans.  $4\sqrt{3}$

Eg. If radius of a circle is reduced by  $n$ , then its area becomes half of its original area. Find the original radius of circle in terms of  $n$ .

	Radius	Area
Original	$R$	2
New	$R-n$	1

$$\frac{R}{R-n} = \frac{\sqrt{2}}{1}$$

$$R = \sqrt{2}R - \sqrt{2}n$$

$$R(\sqrt{2}-1) = \sqrt{2}n$$

$$R = \frac{\sqrt{2}n}{\sqrt{2}-1}$$

**Ans.**  $R = \frac{\sqrt{2}n}{\sqrt{2}-1}$

## REGULAR POLYGON

Area of a regular polygon of  $n$  sides where length of each side is  $a$

$$\text{Area} = \frac{na^2}{4} \cot\left(\frac{180}{n}\right)$$