



ALGEBRA-1



Agenda

* Basics of Algebraic
Formulas —> (60-65) min

* Renaining Part of Simplification > 25 min





ALGEBRAIC FORMULAS

1.
$$(a+b)^2 = a^2 + 2ab + b^2$$

2.
$$(a-b)^2 = a^2 - 2ab + b^2$$

3.
$$a^2-b^2=(a-b)(a+b)$$

Eg.
$$\frac{(469+174)^2-(469-174)^2}{469\times174}=?$$

- (a) 2
- (c) 295

(d) 643

49B 98



Ans. (b)

Eg. Simplify:
$$\frac{(359+256)^2+(359-256)^2}{359\times359+256\times256}$$

- (a) 1089
- (b) 615
- (c) 516
- (d) 2

$$\frac{(a+5)^{2}+(a-5)^{2}}{a^{2}+b^{2}} = \frac{2(a+b^{2})}{a^{2}+b^{2}}$$



Ans. (d)

4.
$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab+bc+ca)$$

Eg. If
$$x + y + z = 13$$

 $x^2 + y^2 + z^2 = 71$
Find: $xy + yz + zx = ??$

$$(x+y+z)^{2} = (x^{2}+y^{2}+z^{2}) + 2(xy+yz+zx)$$

$$169 = 71+2k$$

$$k = 49$$

$$xy+yz+zx = 49$$

Eg. If
$$a + b + c = 20$$

 $a^2 + b^2 + c^2 = 100$
Find: $ab + bc + ca = ??$

DATA INCONSISTENT

for Real value
$$a^2 + b^2 + c^2 > ab + bc + ca$$

Reason:

$$a^2 + b^2 + c^2 \ge ab + bc + ca$$

$$\frac{a^{2}+b^{2}+c^{2}}{2} - ab - bc - ca$$

$$\frac{1}{2} \left[2a^{2}+2b^{2}+ac^{2}-2ab-2bc-2ca \right]$$

$$\frac{1}{2} \left[a^{2}+a^{2}+b^{2}+b^{2}+c^{2}+c^{2}-2ab-2bc-2ca \right]$$

$$\frac{1}{2} \left[a^{2}+a^{2}+b^{2}+b^{2}+c^{2}+c^{2}-2ab-2bc-2ca \right]$$

$$= \frac{1}{2} \left[(a-y)^{2}+(b-c)^{2}+(c-a)^{2} \right] > 0$$

$$T - TI > 0$$

$$T > T$$

5.
$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

5.
$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$
 $(a+b)^3 + (a-b)^3 = 2(a^3 + 3ab^2)$
6. $(a-b)^3 = a^3 - b^3 - 3ab(a-b)$ $(a+b)^3 - (a-b)^3 = 2(b^3 + 3a^2b)$

6.
$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

$$(a+b)^3 - (a-b)^3 = 2(b^3 + 3a^2b)$$

Eg.
$$0.8 \times 0.8 \times 0.8 + 0.2 \times 0.2 \times 0.2 + 3 \times 0.8 \times 0.2 = ?$$

- (a) 2
- (b) 1
- (c) 27.634
- (d) 2.7634

$$=(0.8+0.2)^3=1$$



Ans. (b)



Eg. Find the value of $(7+4\sqrt{3})^{-3}+(7-4\sqrt{3})^{-3}$

$$\frac{1}{7} \left(\frac{1}{7446}\right)^{3} + \left(\frac{1}{746}\right)^{3}$$

$$\frac{1}{7446} + \left(\frac{1}{7446}\right)^{3} + \left(\frac{1}{7446}\right)^{3}$$

$$\frac{1}{7446} + \left(\frac{1}{7446}\right)^{$$



7.
$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

 $x^3 + 1 = (x + 1)(x^2 - x + 1)$

8.
$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

 $x^3 - 1 = (x - 1)(x^2 + x + 1)$

Eg.
$$\left(\frac{147 \times 147 + 147 \times 143 + 143 \times 143}{147 \times 147 \times 147 - 143 \times 143 \times 143}\right) = ?$$

(a)
$$\frac{1}{4}$$

$$(b)$$
 290

(c)
$$\frac{1}{290}$$

$$(d)$$
 4



Ans. (a)

gradeup

$$a^{3} + b^{3} + c^{3} - 3abc = (a + b + c)(a^{2} + b^{2} + c^{2} - ab - bc - ca)$$

$$or$$

$$= \frac{1}{2}(a + b + c)((a - b)^{2} + (b - c)^{2} + (c - a)^{2})$$

$$\frac{3}{4}$$
 $\frac{3}{4}$ $\frac{3}$

$$\frac{3+b^{3}+c^{3}-3abc}{2}$$
 = $\frac{(a+b+c)(a^{2}+b^{2}+c^{2}-ab-bc-ca)}{0R}$
 $\frac{1}{2}(a+b+c)((a-b)^{2}+(b-c)^{2}+(c-a)^{2})$

2) If atstc=0
4

$$a^3 + c^3 - 3ebc$$

2 2 2 2 2 2 0 = 0 value of 32-56+7c find the 492+652+10c2 88^{4} \rightarrow a=b=c $\frac{59^{2}}{209^{2}}$ $\left(\frac{1}{4}\right)^{2}$ the value of 22+3b+5c 109 => \$9 (9-35+C) (99-35+C) (304 be determed)



Eg. Find the value of : $52^3 - 27^3 - 25^3$



N X 25

-> Shoutcut

N x 100

25 x(52)

1300

(92)x 25

Eg. If
$$\frac{m^2 + p^2 + k^2}{mp + pk + km} = 1$$

Find
$$\frac{m+p}{k} + \frac{m+k}{p} + \frac{p+k}{m} = ??$$

$$m^{2}+p^{2}+k^{2}-mp-pk-km=0$$
 $m=p=k$



Eg. If
$$a = 93$$
, $b = 103$, $c = 98$
 $a^2 + b^2 + c^2 - ab - bc - ca = ??$

$$a^{2}+b^{2}+c^{2}-ab-bc-ca=\frac{1}{2}\left[(a-b)^{2}+(b-c)^{2}+(c-a)^{2} \right]$$

$$= \frac{1}{2} \left[\frac{100 + 35 + 35}{45} \right]$$

$$= \frac{1}{2} \left[\frac{75}{45} \right]$$



Eg. If
$$a = 50$$
, $b = 54$, $c = 56$
 $a^3 + b^3 + c^3 - 3abc = ??$



Eg. If
$$a + b + c = 15$$
, $a^2 + b^2 + c^2 = 83$

$$a^3 + b^3 + c^3 - 3abc = ??$$

$$= \left(2 + 5 + c\right) \left(2 + b\right) + c - 2b - b(-2a)$$

$$(a+b+c)^{2} = a^{2}+b^{2}+c^{2}+2(ab+bc+ca)$$

 $225 = 83+2(ab+bc+ca)$
 $ab+bc+cq = 71$



Eg.
$$\frac{(34)^3 + (30)^3 + (36)^3 - 3 \times 34 \times 30 \times 36}{(34)^2 + (30)^2 + (36)^2 - 34 \times 30 - 34 \times 36 - 30 \times 36} = ?$$

- (a) 3352
- (b) 1296
- (0) 100
 - (d) 1156

$$\frac{a^{3}+b^{3}+c^{3}-3abc}{a^{2}+b^{2}+c^{2}-ab-bc-ca}$$

$$= \left(\begin{array}{c} a+b+c \\ \end{array} \right)$$

$$= \left(\begin{array}{c} 100 \\ \end{array} \right)$$



Ans. (c)

Eg. If
$$a = 6$$
, $b = -7$, $c = -5$

Find:
$$\frac{a^3 + b^3 + c^3 - 3abc}{a^2 + b^2 + c^2 - ab - bc - ca} = ??$$

$$a = 7$$
 $b = -3$ $c = -5$

$$\frac{a^{3}+3^{3}+c^{3}-3abc}{(a-b)^{2}+(b-c)^{2}+(c-a)^{2}} = \frac{2}{2}$$

$$\frac{1}{2}(a+b+c) = \frac{-1}{2}$$

$$\left(-1/2\right)$$



Ans. -6

Eg. If
$$a - b = 9$$
, $b - c = 7$, $c - a = 5$

Find:
$$\frac{a^3 + b^3 + c^3 - 3abc}{(a+b+c)} = ??$$



Ans. Data inconsistent

$$a-5=9$$
 $5-c=7$
 4
 $-(c)$
 $5-c=7$
 4
 $-(c)$
 $6-a=5$



SIMPLIFICATION

Q25.
$$999\frac{1}{7} + 999\frac{2}{7} + 999\frac{3}{7} + 999\frac{4}{7} + 999\frac{5}{7} + 999\frac{6}{7}$$
 is simplified to :

(a) 5997

(b) 5979

(c) 5994

(d) 2997



Q26. The value of
$$4 - \frac{5}{1 + \frac{1}{3 + \frac{1}{2 + \frac{1}{4}}}}$$
 is

(a)
$$\frac{1}{8}$$

(c)
$$\frac{1}{16}$$

(d)
$$\frac{1}{}$$

(b) $\frac{1}{64}$

$$\begin{vmatrix} 2 \\ 1 \\ = 1 \end{vmatrix}$$

$$(|1|)^{2} = |2|$$

$$(|1|)^{2} = |232|$$

$$(|1|1)^{2} = |23432|$$

Q27. The value of (11111)2 is

- (a) 12344321
- (c) 123454321

- (b) 121212121
- (d) 11344311



Netc

12345679 X (9K)

- KKKKKKKK (9thnes) Q28. 12345679 × 72 is equal to :

(a) 88888888

(b) 99999998

(c) 88888888

(d) 898989898

->

88888888

eg 12345679 X 54

-

66666666

Q29. If
$$\frac{37}{13} = 2 + \frac{1}{x + \frac{1}{y + \frac{1}{z}}}$$
,

where x, y, z are natural numbers, then x, y, z are:



Ans. (b)



SQUARE ROOT OF IRRATIONAL NUMBERS

$$Eg. \sqrt{7+4\sqrt{3}} = ??$$

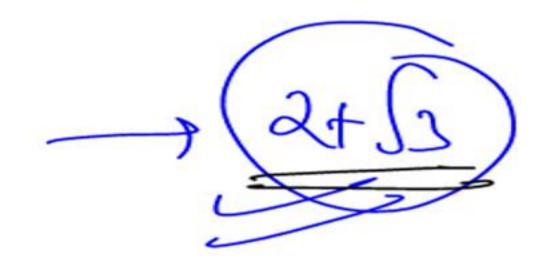
$$\sqrt{7+4\sqrt{3}} = \sqrt{(q+5)^2} = \sqrt{a+5}$$

$$\frac{7+4\sqrt{3}}{7+4\sqrt{3}} = \sqrt{4+5} + \sqrt{4+5}$$

$$\int_{a^{2}+b^{2}} = 7$$

$$\int_{ab} = 2\sqrt{3}$$

$$\int_{a=2} = 5 = \sqrt{3}$$



eg
$$\sqrt{19+8\sqrt{3}}$$
 $19+8\sqrt{3} = a^2+b^2+2ab$

eg
$$\sqrt{27-1052}$$
 = a^2+b^2-2ab $a^2+b^2=27$ $a^2+b^2=552$

Eg.
$$\sqrt{37+20\sqrt{3}}=??$$

$$\frac{2}{4} + \frac{2}{5} = 37$$



Eg.
$$\sqrt{33-20\sqrt{2}}=??$$

$$a^{2} + b^{2} = 33$$
 $ab = 10 \sqrt{2}$
 $= 2.5. \sqrt{2}$
 $q.b = 2 \sqrt{2}.5$

$$\frac{2\sqrt{2} - 5}{5 - 2\sqrt{2}}$$

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Q30. If
$$M = \sqrt{3 - \sqrt{5} + \sqrt{9 - 4\sqrt{5}}}$$
 and $N = \sqrt{\sqrt{7} - 1 - \sqrt{11 - 4\sqrt{7}}}$

$$\frac{1}{M+N}$$



Ans. (b)

Note:

$$\sqrt{2+\sqrt{3}} = \frac{\sqrt{3}+1}{\sqrt{2}}$$

$$\sqrt{2-\sqrt{3}} = \frac{\sqrt{3}-1}{\sqrt{2}}$$





SIMPLIFICATION PRACTICE QUESTIONS



Q1.
$$\sqrt{1+\sqrt{1+\sqrt{1+\dots}}}$$

- (a) equals 1
- (b) lies between 0 and 1
- (c) lies between 1 and 2
- (d) is greater than 2



Ans. (c)



Q2. If m =
$$\sqrt{5+\sqrt{5+\sqrt{5+\dots}}}$$
 and n = $\sqrt{5-\sqrt{5-\sqrt{5-\dots}}}$, then among the following the relation between m and n holds is (a) m - n + 1 = 0 (b) m + n - 1 = 0

(a)
$$m - n + 1 = 0$$

(c) $m + n + 1 = 0$

(d)
$$m - n - 1 = 0$$



Ans. (d)



Q3. Find the value of $\sqrt{63-2\sqrt{63-2\sqrt{63-2\sqrt{63-....??}}}$



Ans. 7



Q4. The value of
$$\frac{1}{\sqrt{(12-\sqrt{140})}} - \frac{1}{\sqrt{(8-\sqrt{60})}} - \frac{2}{\sqrt{10+\sqrt{84}}}$$
 is : (a) 0 (b) 1 (c) 2 (d) 3



Ans. ()



J-Aug
If
$$x = 5 - \sqrt{21}$$
, then the value of $\frac{\sqrt{x}}{\sqrt{32 - 2x} - \sqrt{21}}$

(a)
$$\frac{1}{\sqrt{2}} \left(\sqrt{3} - \sqrt{7} \right)$$
 (b) $\frac{1}{\sqrt{2}} \left(\sqrt{7} - \sqrt{3} \right)$

(b)
$$\frac{1}{\sqrt{2}} \left(\sqrt{7} - \sqrt{3} \right)$$

(c)
$$\frac{1}{\sqrt{2}} \left(\sqrt{7} + \sqrt{3} \right)$$
 (d) $\frac{1}{\sqrt{2}} \left(7 - \sqrt{3} \right)$

(d)
$$\frac{1}{\sqrt{2}} (7 - \sqrt{3})$$



Ans. ()



Q6. Find the value of
$$\frac{1}{5}$$
 + 999 $\frac{494}{495}$ × 99

(a) 90000

(c) 90900

(b) 99000

(d) 99990



Ans. ()



Q7.
$$\left(999 \frac{999}{1000} \times 7\right)$$
 is equal to:

(a)
$$6993\frac{7}{1000}$$
 (b) $7000\frac{7}{1000}$

(b)
$$7000\frac{7}{1000}$$

(c)
$$6633\frac{7}{1000}$$
 (d) $6999\frac{993}{1000}$

d)
$$6999 \frac{993}{1000}$$



Ans. ()

Q8. The value of
$$1 - \frac{a}{1 - \frac{1}{1 + \frac{a}{1 - a}}}$$
 is

(b)
$$1 - a$$





Q9. The smallest of
$$\sqrt{8} + \sqrt{5}$$
, $\sqrt{7} + \sqrt{6}$, $\sqrt{10} + \sqrt{3}$ and

$$\sqrt{11} + \sqrt{2}$$
 is:

(a)
$$\sqrt{8} + \sqrt{5}$$
 (b) $\sqrt{7} + \sqrt{6}$

(c)
$$\sqrt{10} + \sqrt{3}$$
 (d) $\sqrt{11} + \sqrt{2}$

(b)
$$\sqrt{7} + \sqrt{6}$$

(d)
$$\sqrt{11} + \sqrt{2}$$





Q10. The greatest among $\sqrt{7}-\sqrt{5},\ \sqrt{5}-\sqrt{3},\ \sqrt{9}-\sqrt{7},\sqrt{11}-\sqrt{9}$ is

(a)
$$\sqrt{7} - \sqrt{5}$$
 (b) $\sqrt{5} - \sqrt{3}$

(b)
$$\sqrt{5} - \sqrt{3}$$

(c)
$$\sqrt{9} - \sqrt{7}$$
 (d) $\sqrt{11} - \sqrt{9}$





Q11. The smallest among the numbers 2^{250} , 3^{150} , 5^{100} and 4^{200}

(a) 4²⁰⁰

(b) 5¹⁰⁰

(c) 3¹⁵⁰

(d) 2²⁵⁰





Q12. Arranging the following in ascending order 3³⁴, 2⁵¹, 7¹⁷ we get

(a)
$$3^{34} > 2^{51} > 7^{17}$$

(b)
$$7^{17} > 2^{51} > 3^{34}$$

(c)
$$3^{34} > 7^{17} > 2^{51}$$

(d)
$$2^{51} > 3^{34} > 7^{17}$$



Q13. The simplified value of :

$$\left\{ \left[1 + \frac{1}{10 + \frac{1}{10}} \right) \left[1 + \frac{1}{10 + \frac{1}{10}} \right] - \left[1 - \frac{1}{10 + \frac{1}{10}} \right) \left[1 - \frac{1}{10 + \frac{1}{10}} \right] \right\} \div \left\{ \left[1 + \frac{1}{10 + \frac{1}{10}} \right] \left[1 - \frac{1}{10 + \frac{1}{10}} \right] \right\}$$

(a)
$$\frac{4040}{10101}$$

(b)
$$\frac{100}{101}$$

(d)
$$\frac{90}{101}$$





Q14. The ascending order of

 $(2.89)^{0.5}$, $2-(0.5)^2$, $\sqrt{3}$ and $\sqrt[3]{0.008}$ is

(a)
$$2-(0.5)^2$$
, $\sqrt{3}$, $\sqrt[3]{0.008}$, $(2.89)^{0.5}$

(b)
$$\sqrt[3]{0.008}$$
, $(2.89)^{0.5}$, $\sqrt{3}$, $2-(0.5)^2$

(c)
$$\sqrt[3]{0.008}$$
, $\sqrt{3}$, $(2.89)^{0.5}$, $2-(0.5)^2$

(d)
$$\sqrt{3}$$
, $\sqrt[3]{0.008}$, $2-(0.5)^2$, $(2.89)^{0.5}$





Q15. What is the value of:

$$\left[\frac{1}{\sqrt{9}-\sqrt{8}}\right] - \left[\frac{1}{\sqrt{8}-\sqrt{7}}\right] + \left[\frac{1}{\sqrt{7}-\sqrt{6}}\right] - \left[\frac{1}{\sqrt{6}-\sqrt{5}}\right] + \left[\frac{1}{\sqrt{5}-\sqrt{4}}\right]$$

(a) 6

(c) -7

(b) 5

(d) -1





Q16. If
$$\frac{97}{19} = a + \frac{1}{b + \frac{1}{c}}$$
,

where a, b and c are positive integers, then what is the sum of a, b and c?

(a) 16

(b) 9

(c) 20

(d) 18





Q17. Find the value of expression of :

$$\frac{4^{n} \times 20^{m-1} \times 12^{m-n} \times 15^{m+n-2}}{16^{m} \times 5^{2m+n} \times 9^{m-1}}$$

(a) 500

(c) 200

(b) 1

(d) 1/500





Q18. Find the square root of $7 + \sqrt{48}$

(a)
$$2 - \sqrt{3}$$

(c)
$$3 + \sqrt{2}$$

(b)
$$2 + \sqrt{3}$$

(d) $3 - \sqrt{2}$

d)
$$3-\sqrt{2}$$



11.016

Q19. If $\sqrt{6} = 2.449$, then the value of

$$\frac{\sqrt{6}}{2} - \frac{12}{\sqrt{6}} + \sqrt{216}$$
 is equal to:

(a) 11.021 (b) 12.067 (c) 13.079 (d) 12.187

(d) 12.187





Q20. Find the value of:

$$\left(1-\frac{1}{3}\right)\left(1-\frac{1}{4}\right)\left(1-\frac{1}{5}\right)....\left(1-\frac{1}{100}\right)$$

$$(\mathbf{a})\frac{1}{5}$$

(a)
$$\frac{1}{5}$$
 (b) $\frac{1}{10}$

(c)
$$\frac{1}{50}$$

(d)
$$\frac{2}{5}$$

