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Sahi Prep Hai Toh Life Set Hai

Factors & Consecutive Integers



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Factors & consecutive Integers



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Factors & Consecutive Integers



Factors ->



Factors → 65



Factors → (65 min - 70 min)



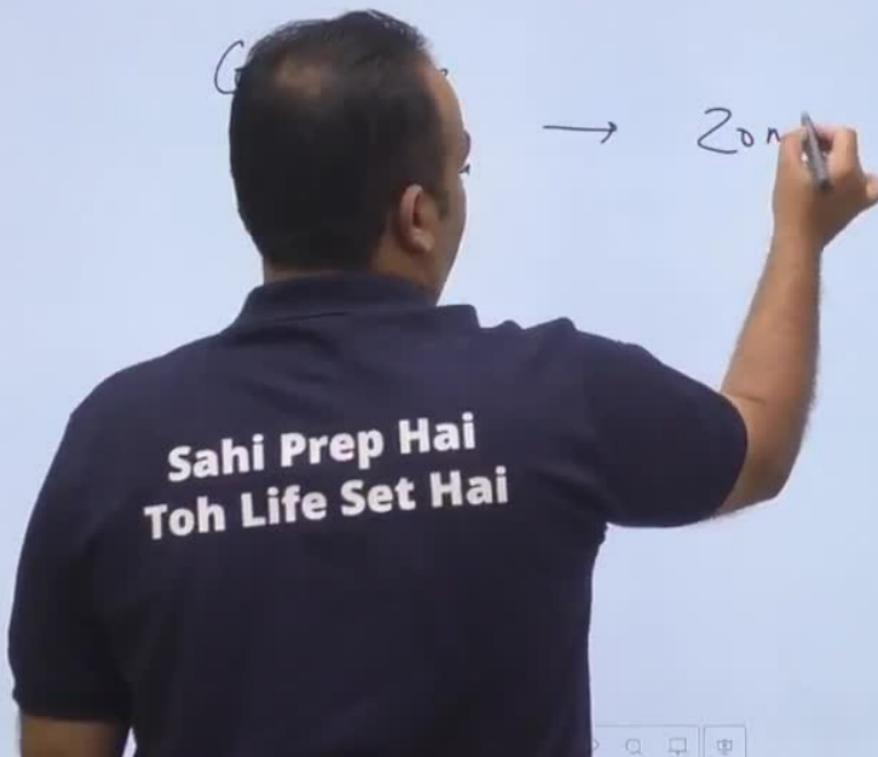
Factors → $(65\text{ min} - 70\text{ min})$

Consecutive

Integers

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Factors → $(65\text{ min} - 70\text{ min})$



Factors → $(65\text{ min} - 70\text{ min})$

Consecut

Int → 20 min - 25 min

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Factors → $(65\text{ min} - 70\text{ min})$

Consecutive
Integers → $20\text{ min} - 25\text{ min}$

Homework of
Factors

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Factors → $(65\text{ min} - 70\text{ min})$

Conse

I

20 min - 25 min

Ho
of

→

5 min

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Factors → $(65\text{ min} - 70\text{ min})$

Consecutive
Integers → $20\text{ min} - 25\text{ min}$

Homework of
Factors → 5 min

BASIC RULES OF EXPONENTS

$$X^a \cdot X^b = X^{a+b}$$

e.g. $2^7 \cdot 2^5 = 2^{12}$

$$\frac{X^a}{X^b} = X^{a-b}$$

e.g. $\frac{2^{11}}{2^5} = 2^6$

$$(X^a)^b = X^{a \cdot b}$$

e.g. $(2^3)^4 = 2^{12}$

$$(X)^0 = 1$$

e.g. $2^0 = 1$

$$(X)^{-m} = \frac{1}{X^m}$$

e.g. $2^{-3} = \frac{1}{2^3} = \frac{1}{8}$

BASIC RULES OF EXPONENTS

$$X^a \cdot X^b = X^{a+b}$$

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$$(X^a)^b = X^{ab}$$

e.g. $(2^3)^4 = 2^{12}$

$$(X^a)^0$$

$$2^0 = 1$$

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e.g. $2^{-3} = \frac{1}{2^3} = \frac{1}{8}$

BASIC RULES OF EXPONENTS

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$$(X)^0 = 1$$

e.g. $2^0 = 1$

$$(X)^{-n}$$

e.g. $2^{-3} = \frac{1}{2^3} = \frac{1}{8}$

$$X^{a^b} \neq X^{a \cdot b}$$



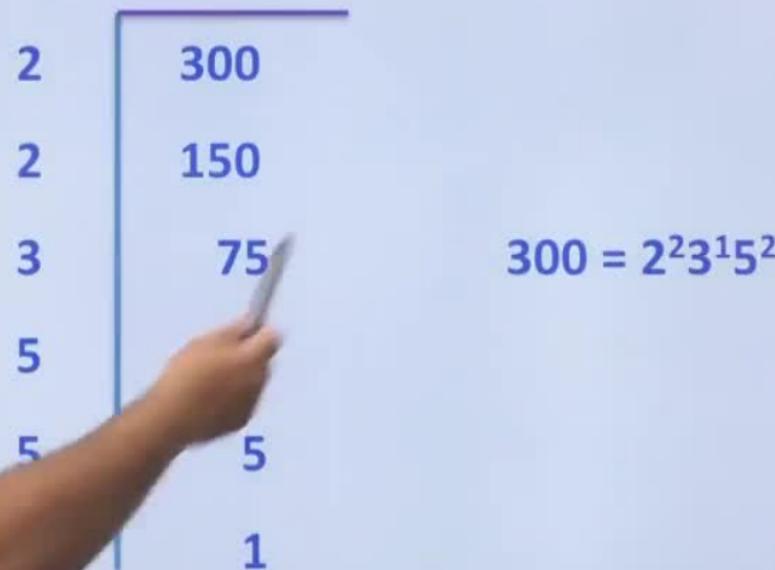
$$2^{3^4} = 2^{81}$$

$$2^{4^3} = 2^{64}$$



PRIME FACTORIZATION OF A NUMBER

Prime Factorization of a Number N= 300



eg

$$3^5^2 = 3^{25}$$

$$5^{8^3} = 5^{512}$$

$$3^{2^3} = 3^8$$

$$X^{a^b} \neq X^{a \cdot b}$$

$$2^{3^4} = 2^{81}$$

$$2^{4^3} = 2^{64}$$

eg

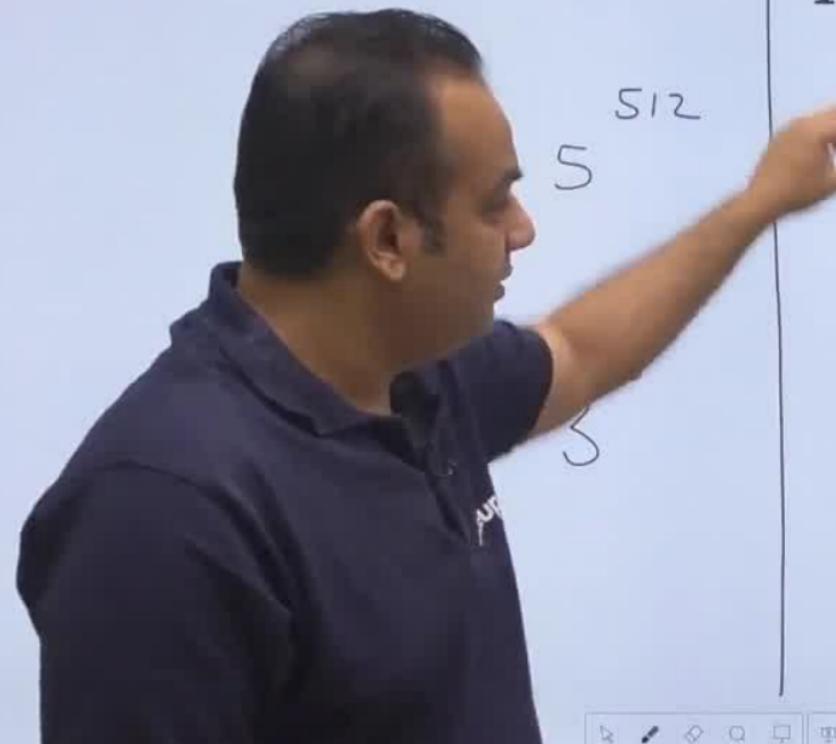
$$3^5 = 3^{25}$$

$$X^{a^b} \neq X^{a \cdot b}$$

$$5^{512}$$

$$2^{3^4} = 2^{81}$$

$$2^{4^3} = 2^{64}$$



eg

$$3^5 = 3^{25}$$
$$5^8 = 5^{12}$$

$$X^{a^b} \neq X^{a \cdot b}$$

$$2^{3^4} = 2^{81}$$

$$2^{4^3} = 2^{64}$$

FACTORS OF A NUMBER

$$12 \rightarrow 1, ?$$

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FACTORS OF A NUMBER

12 → 1, 2, 3, 4, 6, 12

HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$\begin{array}{r} 120 \\ 2 \sqrt{ } \\ 60 \\ 2 \sqrt{ } \\ 30 \\ 2 \sqrt{ } \\ 15 \\ 3 \sqrt{ } \\ 5 \end{array}$$

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HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$120 = 2^3 \cdot 3^1 \cdot 5^1$$

3+1

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HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$\begin{array}{r} 120 \\ 2 \end{array}$$

$$\begin{array}{r} 60 \\ 2 \end{array}$$

$$\begin{array}{r} 30 \\ 2 \end{array}$$

$$\begin{array}{r} 15 \\ 3 \end{array}$$

$$\begin{array}{r} 5 \\ 5 \end{array}$$

$$120 = 2^3 \cdot 3^1 \cdot 5^1$$

$$(3+1)(1+1)(1+1)$$

$$4 \cdot 2 \cdot 2$$

16 Factors

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HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$\begin{array}{r} 120 \\ 2 \sqrt{ } \\ 60 \\ 2 \sqrt{ } \\ 30 \\ 2 \sqrt{ } \\ 15 \\ 3 \sqrt{ } \\ 5 \\ 5 \sqrt{ } \\ 1 \end{array}$$

$$120 = 2^3 \cdot 3^1 \cdot 5^1$$

$$(3+1)(1+1)(1+1)$$

$$4 \cdot 2 \cdot 2$$

$$= 16 \text{ factors}$$



HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$\begin{array}{r} 120 \\ 2 \mid 60 \\ 2 \mid 30 \\ 2 \mid 15 \\ 3 \end{array}$$

$$120 = 2^3 \cdot 3^1 \cdot 5^1$$

$$(3+1)(1+1)(1+1)$$

$$4 \cdot 2 \cdot 2$$

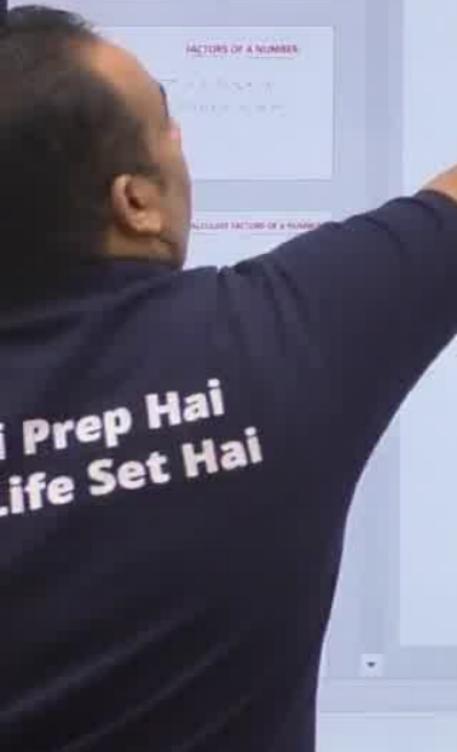
$$= 16 \text{ factors}$$





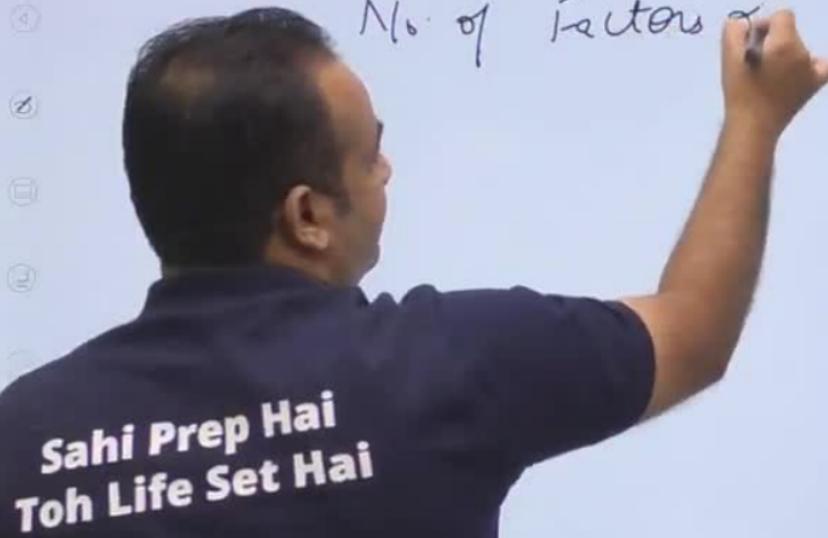
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- Click to add text



$$72 = 2^3 \cdot 3^2$$

No. of Factors \times



$$72 = 2^3 \cdot 3^2$$

No. of factors of 72 \Rightarrow 4, 3

\Rightarrow 1

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$$72 = 2^3 \cdot 3^2$$

Factors of 72 \Rightarrow 4 . 3
 \Rightarrow 12



If a number is of the form

$$N = P_1^a \cdot P_2^b \cdot P_3^c \dots$$

$$\text{No. of factors} = (a + 1) \cdot (b + 1) \cdot (c + 1) \dots$$

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P_2, P_3 are distinct prime numbers
and c are their exponents.



If a number is of the form

$$N = P_1^a \cdot P_2^b \cdot P_3^c \dots$$

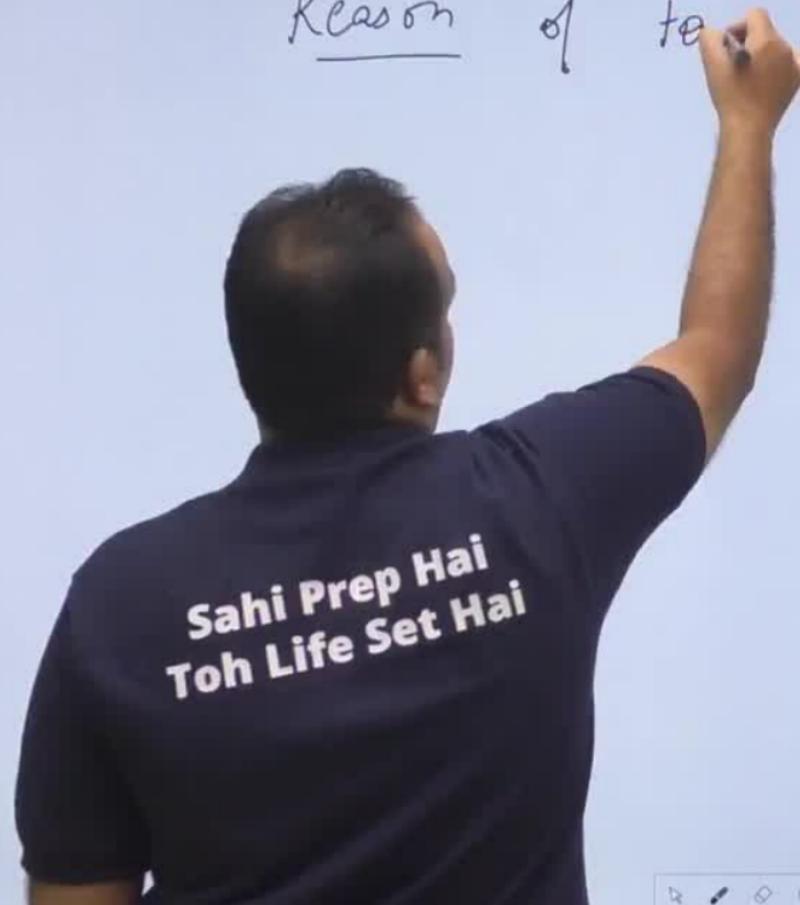
$$rs = (a + 1) \cdot (b + 1) \cdot (c + 1) \dots$$

where, P_1, P_2, P_3 are distinct prime numbers
and a, b and c are their exponents.

Reason

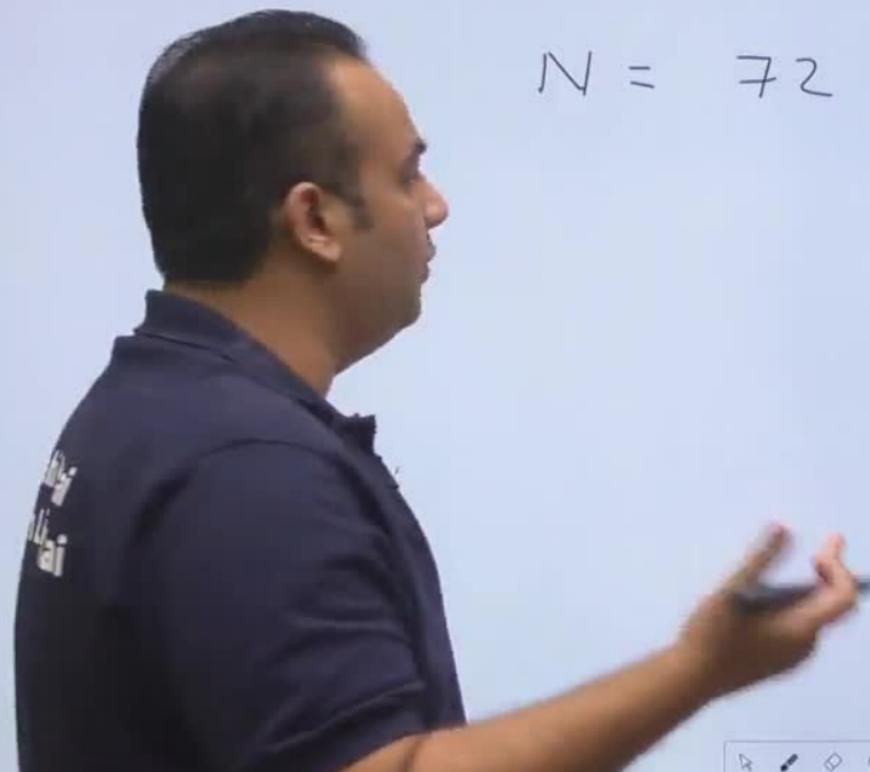
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Reason of fe



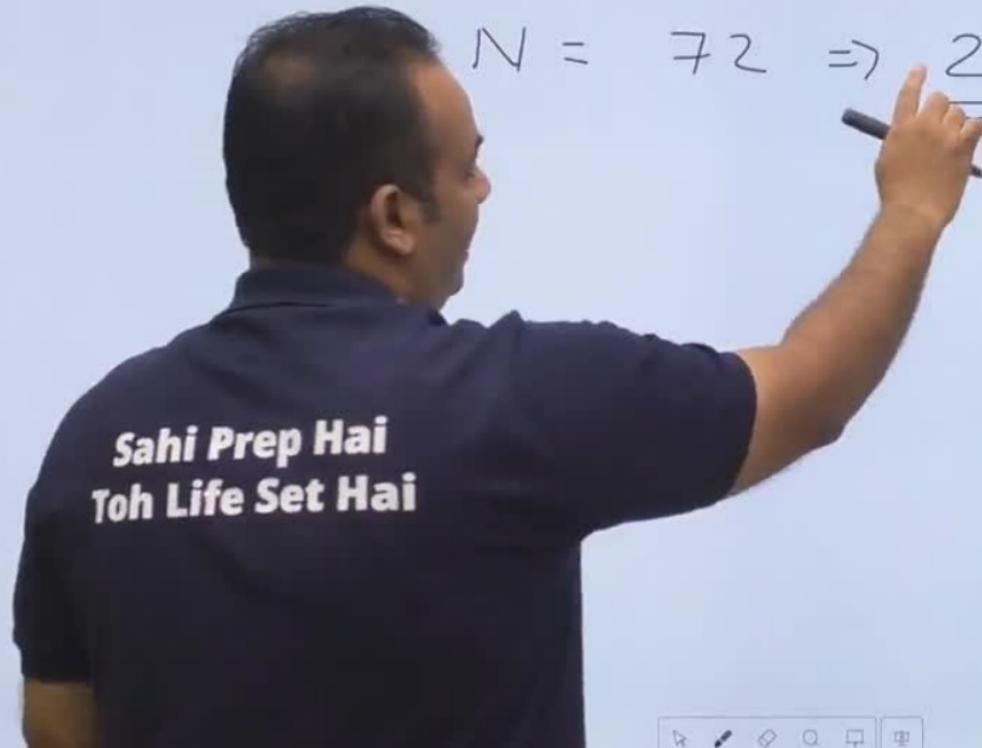
Reason of family

$$N = 72$$



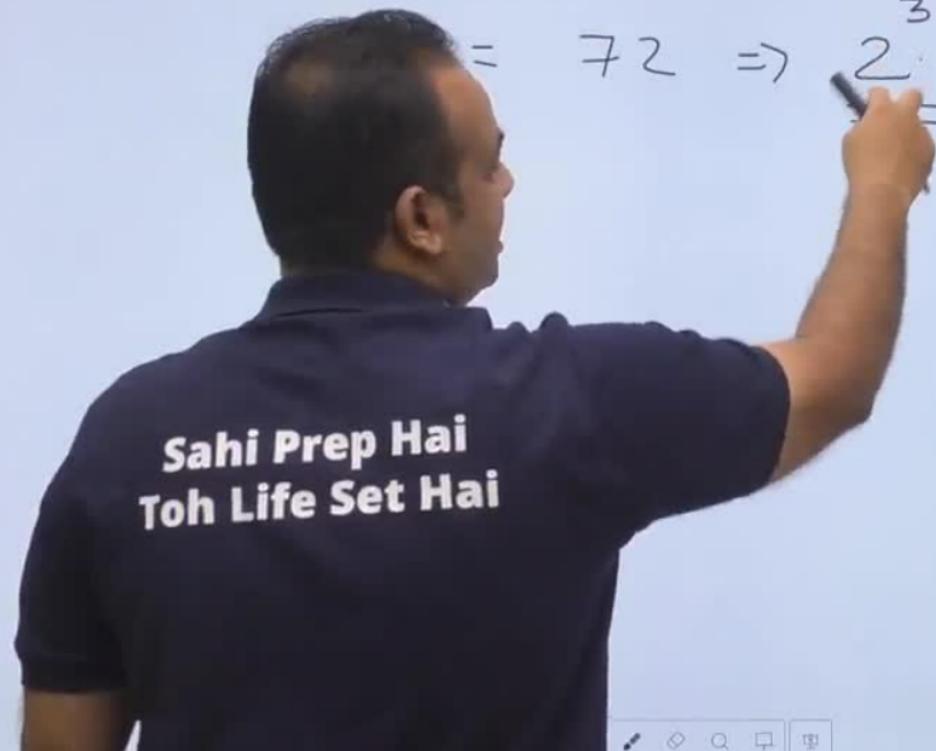
Reason of faults

$$N = 72 \Rightarrow 2^3 \cdot \underline{3^2}$$



Reason of failure

$$= 72 \Rightarrow 2^3 \cdot 3^2$$



Reason of family

$$N = 72 \quad \underline{\underline{2^3 \cdot 3^2}}$$

D
Q
C
B
E
M
R
V
S
U

$$\begin{array}{r} 2^1 \\ 2^2 \\ 2^3 \end{array}$$

Reason of faults

$$N = 72 \Rightarrow \underline{\underline{2^3 \cdot 3^2}}$$

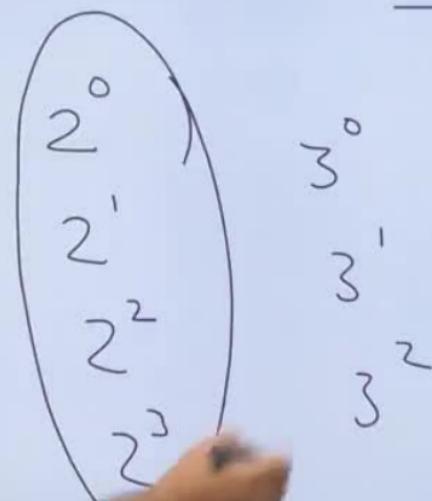
$$\begin{array}{r} 2^0 \\ 2^1 \\ - \\ 2^2 \end{array}$$

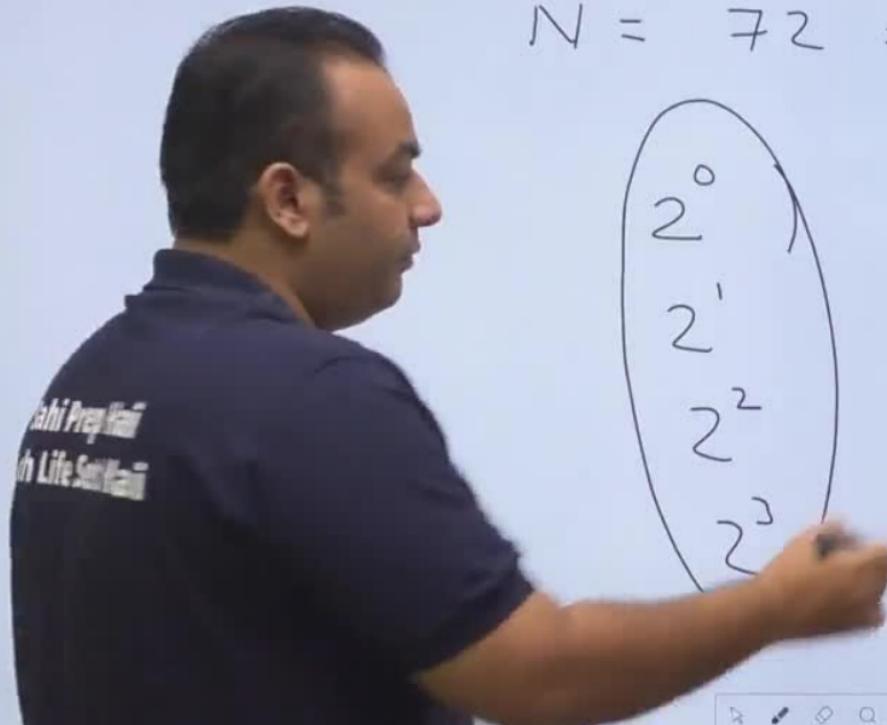
$$3^0$$

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Reason of formula

$$N = 72 \Rightarrow \underline{\underline{2^3 \cdot 3^2}}$$


$$\begin{array}{c} 2^0 \\ 2^1 \\ 2^2 \\ 2^3 \end{array}$$
$$\begin{array}{c} 3^0 \\ 3^1 \\ 3^2 \end{array}$$



Reason of formula

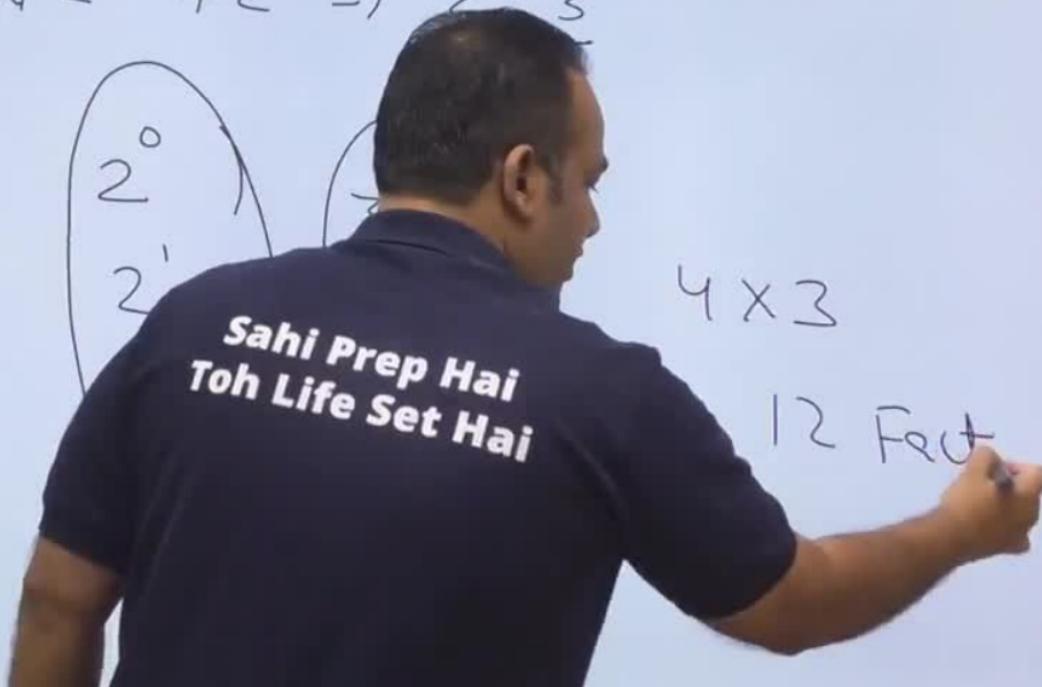
$$N = 72 \Rightarrow 2^3 \cdot 3^2$$



$$4 \times 3$$

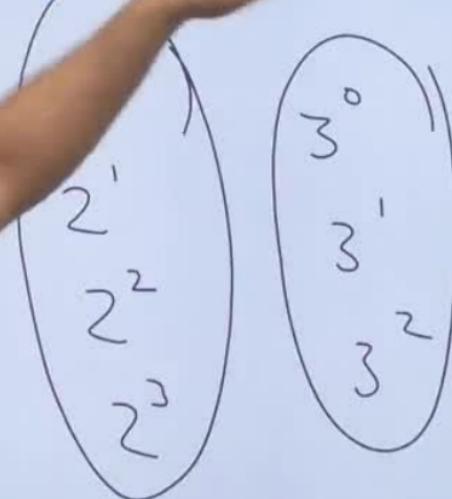
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12 Feet



Reason of formula

$$N = 72 \Rightarrow 2^3 \cdot 3^2$$



$$\begin{aligned} & 4 \times 3 \\ & = 12 \text{ Factors} \end{aligned}$$

Reason of formula

$$2^0 \cdot 3^0 = 1$$

$$2^0 \cdot 3^1 =$$

$$2^0 \cdot 3^2 =$$

$$2^0 \cdot 3^3 =$$

$$2^0 \cdot 3^4 =$$

$$2^0 \cdot 3^5 =$$

$$2^0 \cdot 3^6 =$$

$$2^0 \cdot 3^7 =$$

$$2^0 \cdot 3^8 =$$

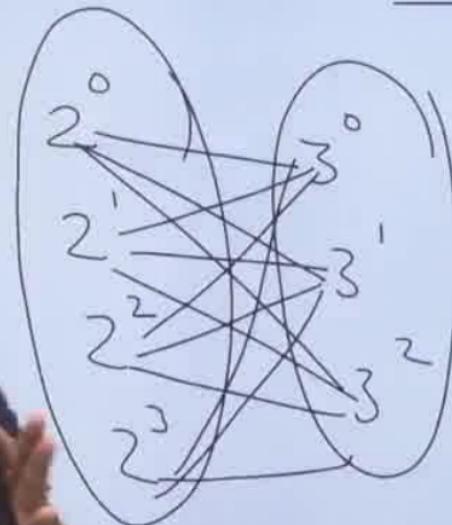
$$2^0 \cdot 3^9 =$$

$$2^0 \cdot 3^{10} =$$

$$2^0 \cdot 3^{11} =$$

$$2^0 \cdot 3^{12} =$$

$$N = 72 \Rightarrow \underline{\underline{2^3 \cdot 3^2}}$$



$$\begin{aligned}4 \times 3 \\= 12\end{aligned}$$

Factor

Reason of family

$$2^0 \cdot 3^0 = 1$$

$$2^0 \cdot 3^1 = 3$$

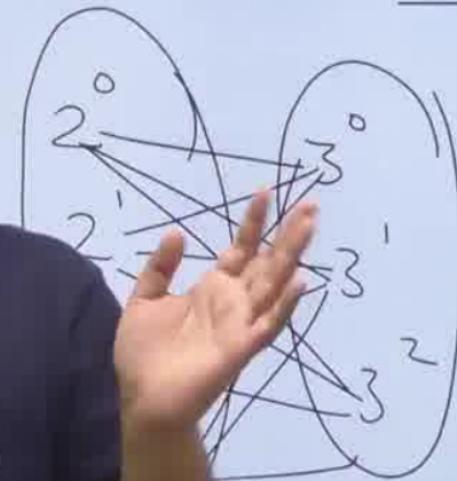
$$2^0 \cdot 3^2 = 9$$

$$2^0 \cdot 3^3 = 27$$

$$2^0 \cdot 3^4 = 81$$

$$2^0 \cdot 3^5 = 243$$

$$N = 72 \Rightarrow \underline{\underline{2^3 \cdot 3^2}}$$



$$\begin{aligned}4 \times 3 \\= 12\end{aligned}$$

Factory

Reason of factors

$$2^0 \cdot 3^0 = 1$$

$$2^0 \cdot 3^1 = 3$$

$$2^0 \cdot 3^2 = 9$$

$$2^1 \cdot 3^0 = 2$$

$$2^1 \cdot 3^1 = 6$$

$$2^1 \cdot 3^2 = 12$$

$$72 \Rightarrow \frac{2^3}{3^2}$$



$$\begin{aligned}4 \times 3 \\= 12 \text{ Factors}\end{aligned}$$

Reason of family

$$2^0 \cdot 3^0 = 1$$

$$2^0 \cdot 3^1 = 3$$

$$2^0 \cdot 3^2 = 9$$

$$2^1 \cdot 3^0 = 2$$

$$2^1 \cdot 3^1 = 6$$

$$2^2 \cdot 3^0 = 4$$

$$2^2 \cdot 3^1 = 12$$

$$2^3 \cdot 3^0 = 8$$

$$2^3 \cdot 3^1 = 24$$

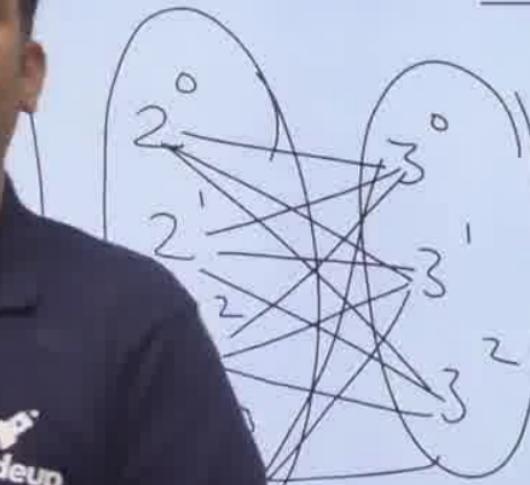
$$2^4 \cdot 3^0 = 16$$

$$2^4 \cdot 3^1 = 48$$

$$2^5 \cdot 3^0 = 32$$

$$2^5 \cdot 3^1 = 96$$

$$N = 72 \Rightarrow \underline{\underline{2^3 \cdot 3^2}}$$



$$\begin{aligned}4 \times 3 \\= 12\end{aligned}$$

Family

HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$\begin{array}{r} 120 \\ 2 \sqrt{ } \\ 60 \\ 2 \sqrt{ } \\ 30 \\ 2 \sqrt{ } \\ 15 \\ 3 \sqrt{ } \\ 5 \end{array}$$

$$120 = 2^3 \cdot 3^1 \cdot 5^1$$

$$(3+1)(1+1)(1+1)$$

$$4 \cdot 2 \cdot 2$$

$$= 16 \text{ factors}$$

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Set Hai

HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$120 = 2^3 \cdot 3^1 \cdot 5^1$$

$$(3+1) (1+1) (1+1)$$

$$2 \cdot 2$$

$$= 16 \text{ factors}$$

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Toh Life Set Hai**

HOW TO CALCULATE FACTORS OF A NUMBER

$$N = 120$$

$$\begin{array}{r} \boxed{120} \\ 2 \\ 60 \\ 2 \\ 30 \\ 2 \\ 15 \\ 3 \\ 5 \end{array}$$

$$120 = 2^3 \cdot 3^1 \cdot 5^1$$

$$(3+1)(1+1)(1+1)$$

$$4 \cdot 2 \cdot 2$$

$$= 16 \text{ factors}$$

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Toh Life Set Hai

$$72 = 2^3 \cdot 3^2$$

No. of factors of 72 \Rightarrow 4 . 3
 \Rightarrow 12



If a number is of the form

$$N = P_1^a \cdot P_2^b \cdot P_3^c \dots \dots \dots$$

No. of factors = $(a + 1) \cdot (b + 1) \cdot (c + 1) \dots \dots \dots$

P_1, P_2, P_3 are distinct prime numbers
a, b and c are their exponents.

Reason of factors

$$2^0 \cdot 3^0 = 1$$

$$2^0 \cdot 3^1 = 3$$

$$2^0 \cdot 3^2 = 9$$

$$2^1 \cdot 3^0 = 2$$

$$2^1 \cdot 3^1 = 6$$

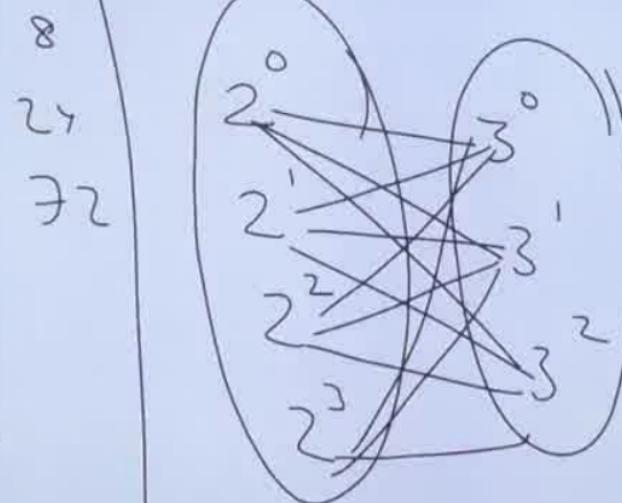
$$2^1 \cdot 3^2 = 18$$

$$2^2 \cdot 3^0 = 4$$

$$2^2 \cdot 3^1 = 12$$

$$2^2 \cdot 3^2 = 36$$

$$N = 72 \Rightarrow \underline{\underline{2^3 \cdot 3^2}}$$



$$4 \times 3 \\ = 12 \text{ Factors}$$

Find the Number of factors of

(i) 720

(ii) $2^3 3^4 5^6$

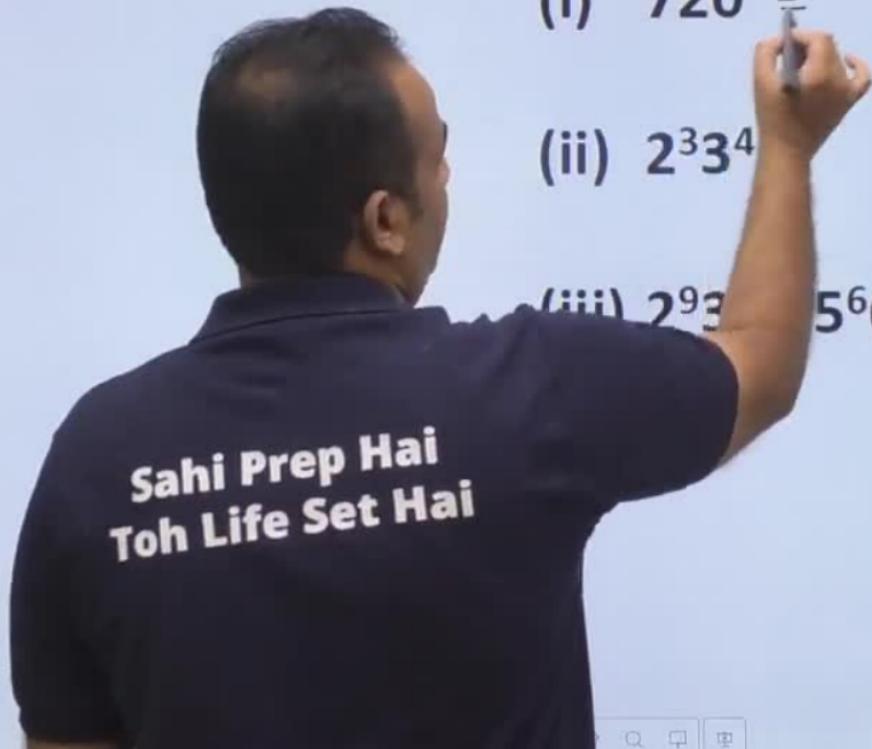
(iii) $2^9 3^8 4^7 5^6 6^5$

Find the Number of factors of

(i) 720

(ii) $2^3 3^4$

(iii) $2^9 3^7 5^6 6^5$

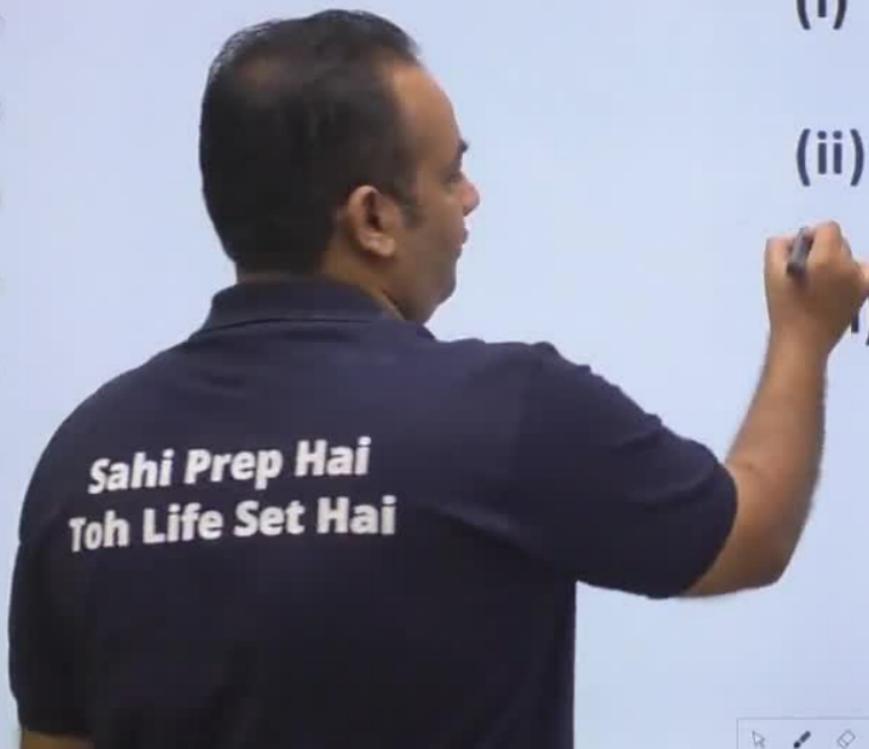


Find the Number of factors of

(i) $720 = 2^4 \cdot 3^2 \cdot 5^1$
 $\rightarrow 5 \cdot 3 \cdot 2 = 30$ ✓

(ii) $2^3 \cdot 3^4 \cdot 5^6$

(iii) $2^9 \cdot 3^8 \cdot 4^7 \cdot 5^6 \cdot 6^5$



$$2^9 \cdot 3^8 \cdot 4^7 \cdot 5^6 \cdot 6^5$$

$$= 2^9 \cdot 3^8 \cdot (2^2)^7 \cdot 5^6 \cdot (2 \cdot 3)^5$$

$$= 2^{14} \cdot 3^{13} \cdot 5^6 \cdot 2^5 \cdot 3^5$$

$$= 2^{19} \cdot 3^{18} \cdot 5^6$$

Find the Number of factors of

$$(i) 720 = 2^4 \cdot 3^2 \cdot 5^1$$

$$\rightarrow 5 \cdot 3 \cdot 2 = 30 \quad \checkmark$$

$$(ii) 2^3 \cdot 3^4 \cdot 5^6$$

$$\rightarrow 4 \cdot 5 \cdot 7 = 140 \quad \checkmark$$

$$(iii) 2^9 \cdot 3^8 \cdot 4^7 \cdot 5^6 \cdot 6^5$$

$$2^9 \cdot 3^8 \cdot 4^7 \cdot 5^6 \cdot 6^5$$

$$2^9 \cdot 3^8 \cdot (2^2)^7 \cdot 5^6 \cdot (2^1 \cdot 3^1)^5$$

$$\underline{2^9} \cdot \underline{3^8} \cdot \underline{2^{14}} \cdot 5^6$$

Find the Number of factors of

$$(i) \quad 720 = 2^4 \cdot 3^2 \cdot 5^1$$

$$\rightarrow 5 \cdot 3 \cdot 2 = \textcircled{30} \checkmark$$

$$(ii) \quad 2^3 \cdot 3^4 \cdot 5^6$$

$$\rightarrow 4 \cdot 5 \cdot 7 = \textcircled{140} \checkmark$$

$$(iii) \quad 2^9 \cdot 3^8 \cdot 4^7 \cdot 5^6 \cdot 6^5$$

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$$29 \times 98$$

$$= 29(100 - 2)$$

How to Calculate Odd Factors of a Number



How to Calculate Odd Factors of a Number



$$2^9 \cdot 3^8 \cdot 4^7 \cdot 5^6 \cdot 6^5$$

$$2^9 \cdot 3^8 \cdot (2^2)^7 \cdot 5^6 \cdot (2 \cdot 3)^5$$

$$= 2^9 \cdot 3^8 \cdot 2^{14}$$

Find the Number of factors of

$$(i) 720 = 2^4 \cdot 3^2 \cdot 5^1$$

$$\rightarrow 5 \cdot 3 \cdot 2 = \textcircled{30} \checkmark$$

$$(ii) 2^3 \cdot 3^4 \cdot 5^6$$

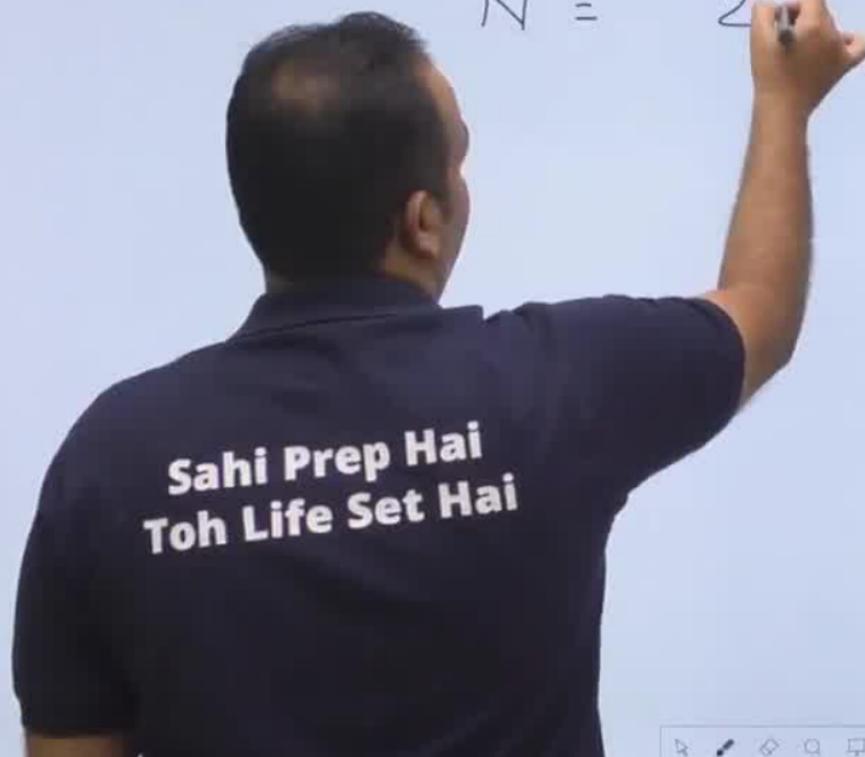
$$\rightarrow 4 \cdot 5 \cdot 7 = \textcircled{140} \checkmark$$

$$(iii) 2^9 \cdot 3^8 \cdot 4^7 \cdot 5^6 \cdot 6^5$$

$$\begin{aligned}
 &= 2^9 \times 3^8 \\
 &= 2^9 (100 - 2) = \underline{\underline{2842}}
 \end{aligned}$$

How to Calculate Odd Factors of a Number

$$N = 2^3$$



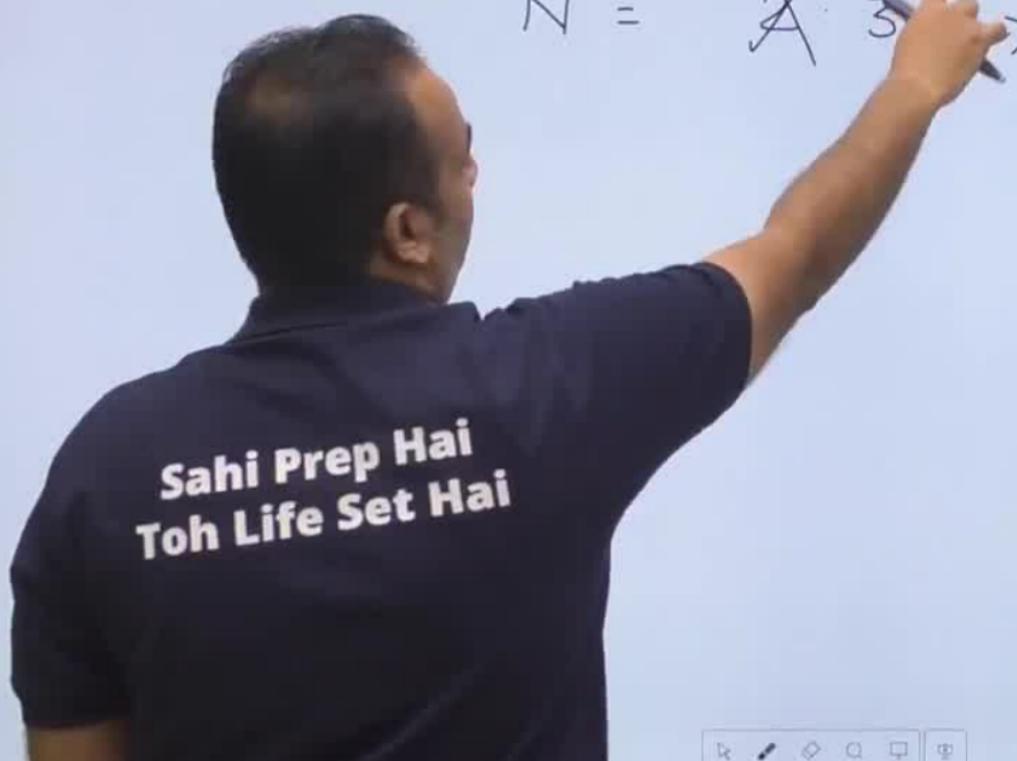
How to Calculate Odd Factors of a Number

$$N = 2^3 \cdot 3^2 \Rightarrow 72$$



How to Calculate Odd Factors of a Number

$$N = \cancel{3}^{\cancel{3}} \cdot 5^2 > 72$$



How to Calculate Odd Factors of a Number

$$N = \cancel{2} \cdot 3^2 \Rightarrow 72$$

No. of odd factors $\rightarrow 3$

$$A =$$

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How to Calculate Odd Factors of a Number

$$N = \cancel{2} \cdot 3^2 \Rightarrow 72$$

No. of odd factors $\rightarrow 3$

e.g. $A = 2^5 \cdot 3^8 \cdot 5^7$

No. of odd factors

of \square =

How to Calculate Odd Factors of a Number

$$N = \cancel{2} \times 3^2 \Rightarrow 72$$

No. of odd factors $\rightarrow 3$

$$A = \cancel{2} \times \cancel{3}^8 \times 5^7$$

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How to Calculate Odd Factors of a Number

$$N = \cancel{2} \times 3^2 \Rightarrow 72$$

odd factors $\rightarrow 3$

eg

$$= \cancel{2} \times 3^8 \times 5^7$$

$$= 9 \cdot 8$$

=

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How to Calculate Odd Factors of a Number

$$N = \cancel{2}^3 \cdot 3^2 \Rightarrow 72$$

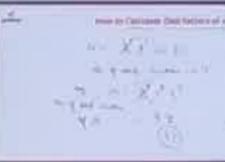
odd factors $\rightarrow 3$

eg $A = \cancel{2}^3 \cdot 5^7$

No of odd factor

$$\begin{aligned} \text{of } A &= 9 \cdot 8 \\ &= \boxed{72} \end{aligned}$$

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A man with his back to the camera is pointing upwards with his right index finger towards a Microsoft Word slide. He is wearing a dark blue t-shirt with white text that reads "ni Prep Hai" on the top line and "Life Set Hai" on the bottom line, with a small heart symbol between them. The Microsoft Word ribbon at the top shows tabs like File, Home, Insert, Design, Transitions, Animations, Slide Show, Review, View, MathType, and Help. The slide itself has a light blue background with a "gradeup" logo in the top left corner. The main text on the slide is "Click to add title" in a large, bold, dark font, followed by a bullet point "• Click to add text". The status bar at the bottom right shows the time as 11:24 AM.

AutoSave 08

S- Factors & Consecutive Integers (S5...)

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ni Prep Hai
Life Set Hai

Notes

11:24 AM

N -

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$$N = 3^a 5^b \cdot \cdot \cdot -$$

odd

even

=

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$$N = 2^a 3^b 5^c \dots -$$

No. of

Factors

$$= (b+1)$$

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$$N = 2^a 3^b 5^c \dots \dots$$

No. of odd

$$\text{Factors of } N = (b+1)(c+1) \dots \dots$$

Find the Number of odd factors of

(i) $2^3 3^4 5^6$

(ii) $3^8 5^7$

(iii) $2^6 5^4$

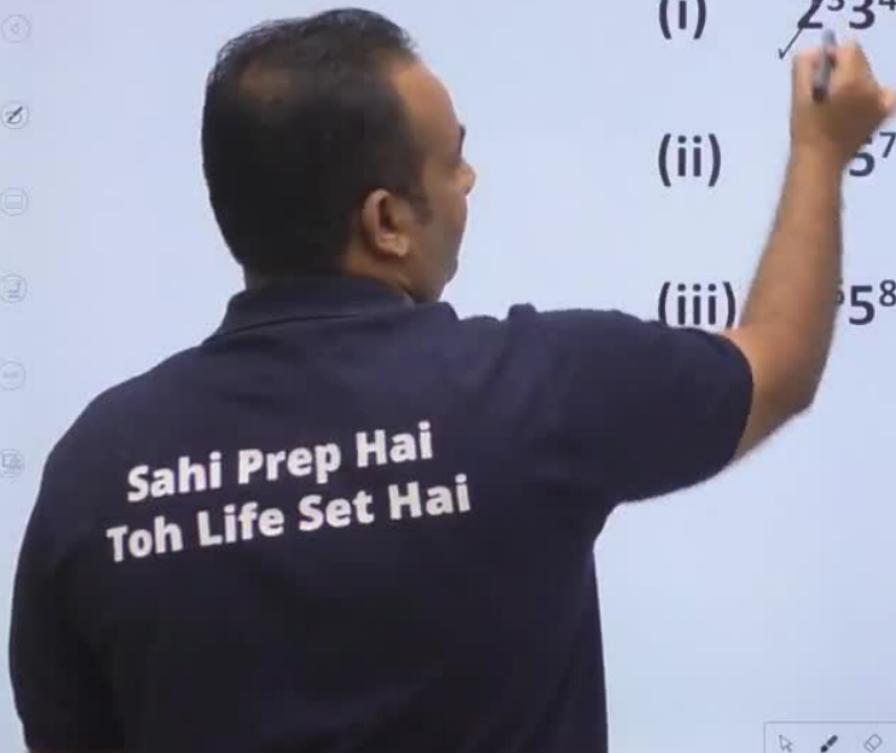
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Find the Number of odd factors of

(i) ~~$2^3 3^4 5^6$~~ →

(ii) ~~$2^5 5^7$~~

(iii) ~~$2^6 5^8$~~

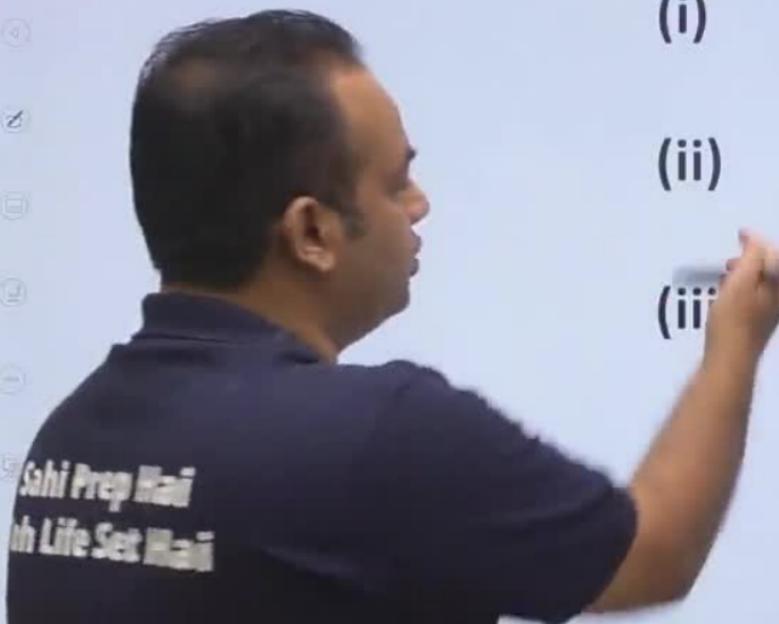


Find the Number of odd factors of

(i) $2^3 3^4 5^6 \rightarrow 5 \cdot 7 = 35$

(ii) $3^8 5^7$

(iii) $2^6 5^8$

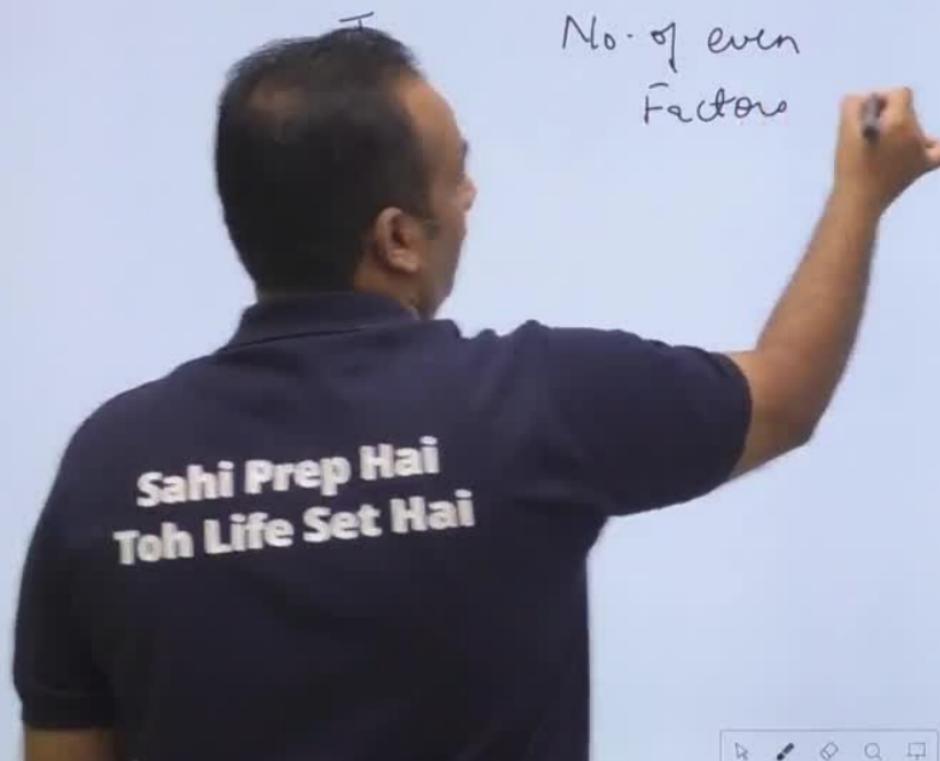


How to Calculate Even Factors of a Number



How to Calculate Even Factors of a Number

No. of even
Factors



How to Calculate Even Factors of a Number

I

No. of even
Factors

Total Factors - Odd Factors

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Toh Life Set Hai

How to Calculate Even Factors of a Number

$$\text{No. of even factors} =$$

Total Factors - Odd Factors

N

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How to Calculate Even Factors of a Number

I

No. of even
Factors =

Total Factors - Odd Factors

$$N = 2^3 \cdot 3^4 \cdot 5^6$$

Total Factors

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Toh Life Set Hai

How to Calculate Even Factors of a Number

I

$$\text{No. of even factors} =$$

$$\text{Total Factors} - \text{Odd Factors}$$

$$N = 2^3 \cdot 3^4 \cdot 5^6$$

$$\text{Total Factors} \rightarrow 4 \cdot 5 \cdot 7 = 140$$

$$\text{Odd Factors} \rightarrow$$

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How to Calculate Even Factors of a Number

I

No. of even
Factors =

Total Factors - Odd Factors

$$N = 2^3 \cdot 3^4 \cdot 5^6$$

$$\text{Total Factors} \rightarrow 4 \cdot 5 \cdot 7 = 140$$

$$\text{Odd Factor} \rightarrow 5 \cdot 7 = 35$$

Even Factor

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How to Calculate Even Factors of a Number

I

No. of even
Factors =

Total Factors - Odd Factors

$$N = 2^3 \cdot 3^4 \cdot 5^6$$

$$\text{Total Factors} \rightarrow 4 \cdot 5 \cdot 7 = 140$$

$$\text{Odd Factor} \rightarrow 5 \cdot 7 = 35$$

Factor -

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How to Calculate Even Factors of a Number

I

$$\text{No. of even factors} = \text{Total Factors} - \text{Odd Factors}$$

$$N = 2^3 \cdot 3^4 \cdot 5^6$$

$$\text{Total Factors} \rightarrow 4 \cdot 5 \cdot 7 = 140$$

$$\text{Odd Factor} \rightarrow 5 \cdot 7 = 35$$

$$\text{Even Factor} \rightarrow \underline{\underline{105}}$$



How to Calculate Even Factors of a Number



$$\text{Even factors} = \text{Total Factors} - \text{Odd Factors}$$

$$N = 2^3 \cdot 3^4 \cdot 5^6$$

$$\text{Total Factors} \rightarrow 4 \cdot 5 \cdot 7 = 140$$

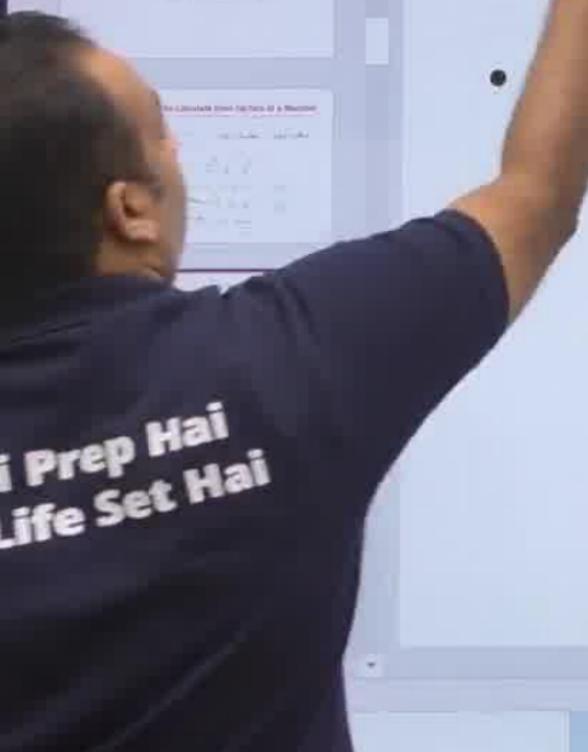
$$\text{Odd Factors} \rightarrow 5 \cdot 7 = 35$$

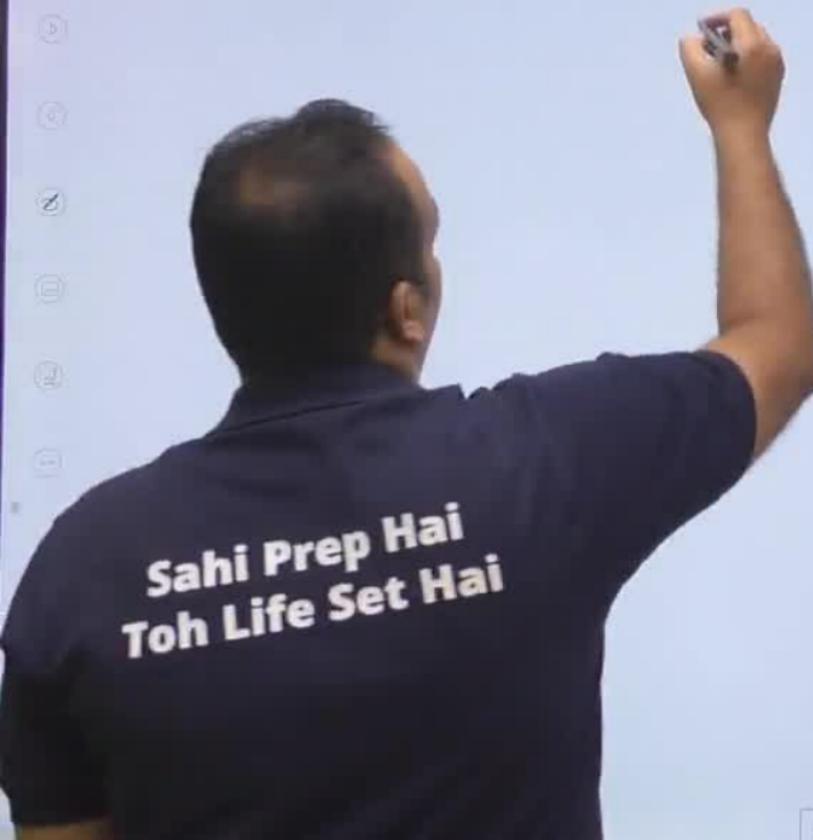
$$\text{Even Factors} \rightarrow \frac{140}{2} = 70$$



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- ck to add text





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1

II

$$N = 2^3 3^4 5^6$$

2^o

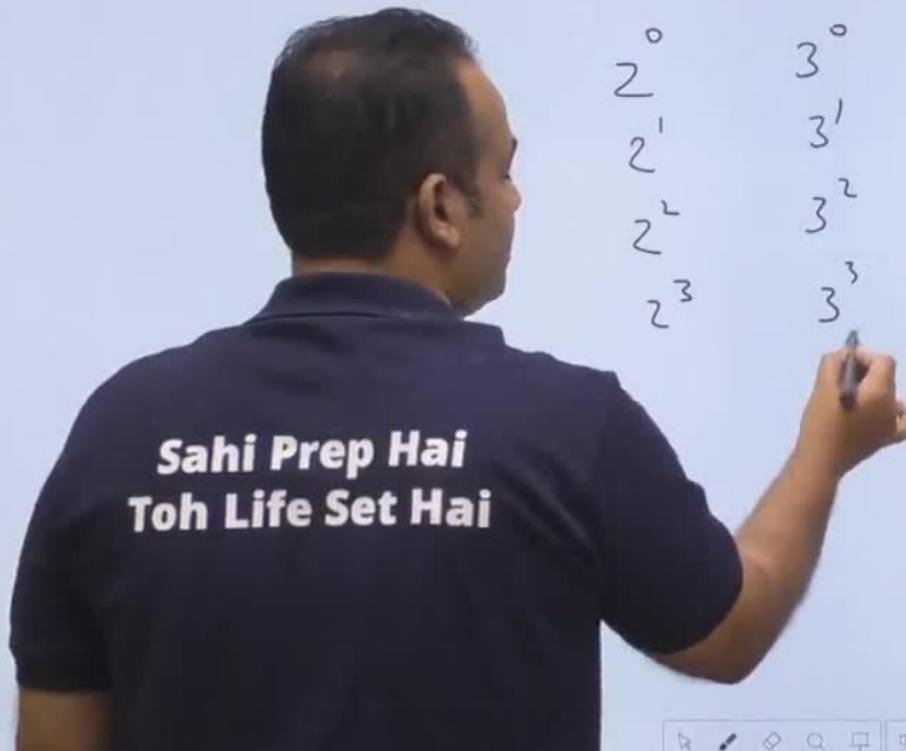
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z³

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II

$$N = 2^3 3^4 5^6$$

$$\begin{array}{ll} 2^0 & 3^0 \\ 2^1 & 3^1 \\ 2^2 & 3^2 \\ 2^3 & 3^3 \end{array}$$



II

$$N = 2^3 3^4 5^6$$

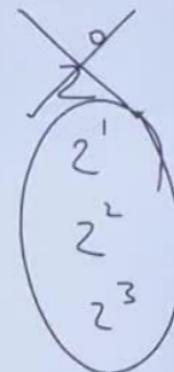
$$\begin{array}{ccc} 3^0 & 5^0 \\ 3^1 & 5^1 \\ 3^2 & 5^2 \\ 3^3 & 5^3 \\ 3^4 & 5^4 \end{array}$$

 2^3

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Toh Life Set Hai**

II

$$N = 2^3 3^4 5^6$$



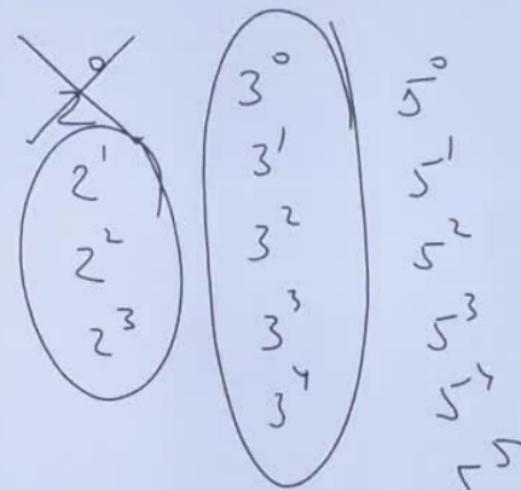
$$\begin{array}{ll} 3^0 & 5^0 \\ 3^1 & 5^1 \\ 3^2 & 5^2 \\ 3^3 & 5^3 \\ 3^4 & 5^4 \\ & 5^5 \\ & 5^6 \end{array}$$

?

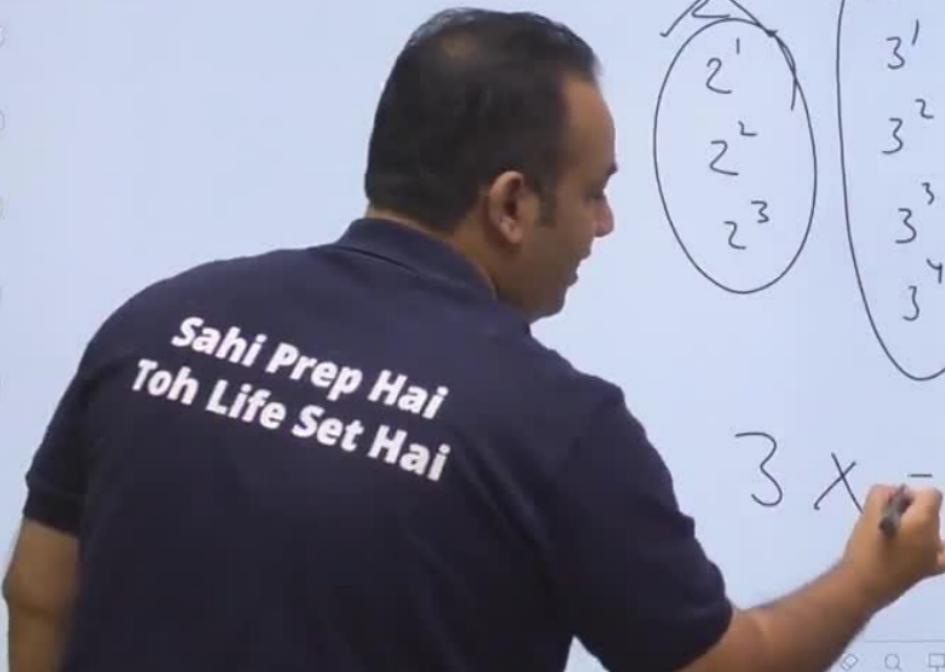
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II

$$N = 2^3 3^4 5^6$$



$$3 \times - \quad 5^6$$



II

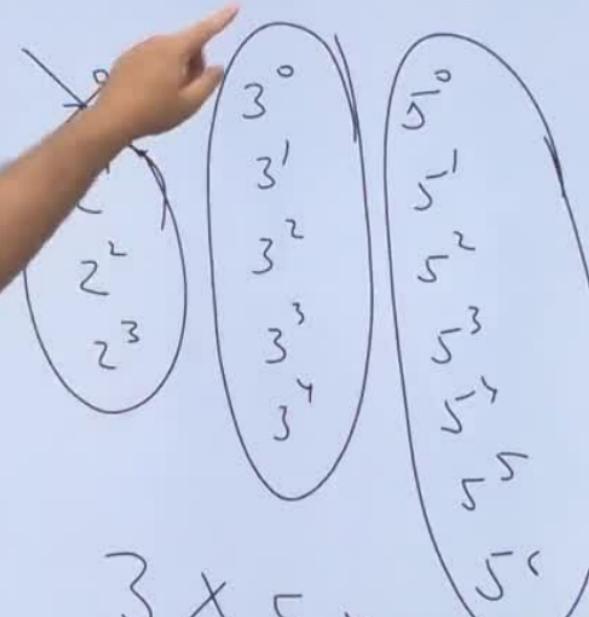
$$N = 2^3 \cdot 3^4 \cdot 5^6$$

The number N is shown as a product of prime factors raised to powers: $2^3 \cdot 3^4 \cdot 5^6$. This is visualized by three ovals containing the powers of each prime factor. The first oval contains powers of 2: $2^0, 2^1, 2^2, 2^3$. The second oval contains powers of 3: $3^0, 3^1, 3^2, 3^3, 3^4$. The third oval contains powers of 5: $5^0, 5^1, 5^2, 5^3, 5^4, 5^5, 5^6$.

$$3 \times 5 \times 7 = 105$$

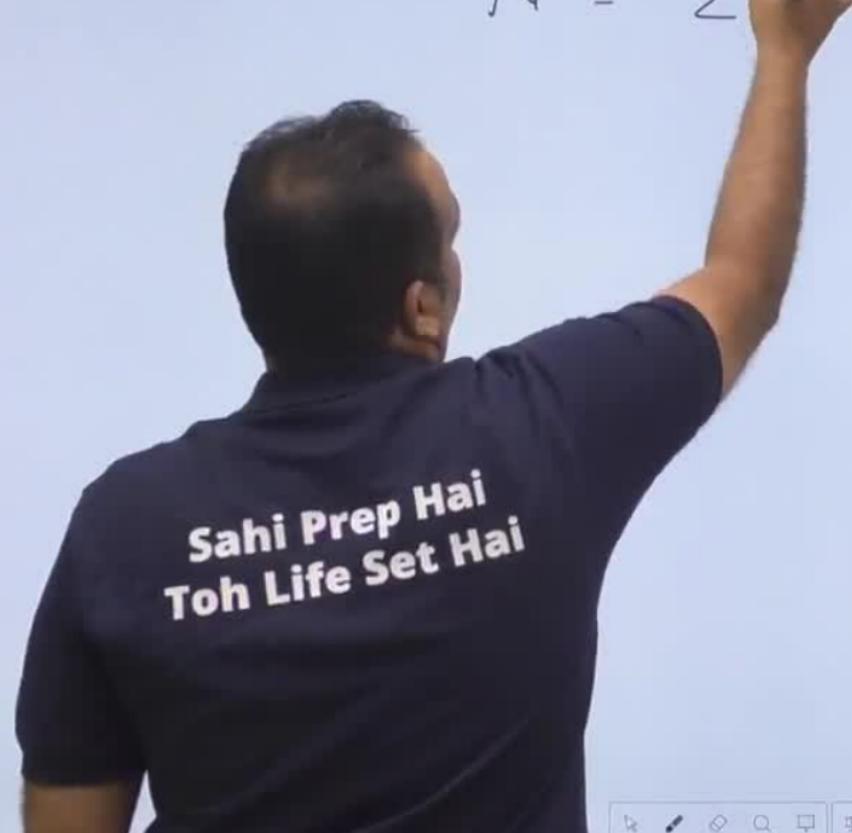
II

$$N = 2^3 3^4 5^6$$



$$3 \times 5 \times 7 = 105$$

$$N = 2^9$$



$$N = 2^a \cdot 3^b \cdot 5^c \cdots$$

No. of even
Factors

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$$N = 2^a \cdot 3^b \cdot 5^c \cdots$$

No. of
Factors

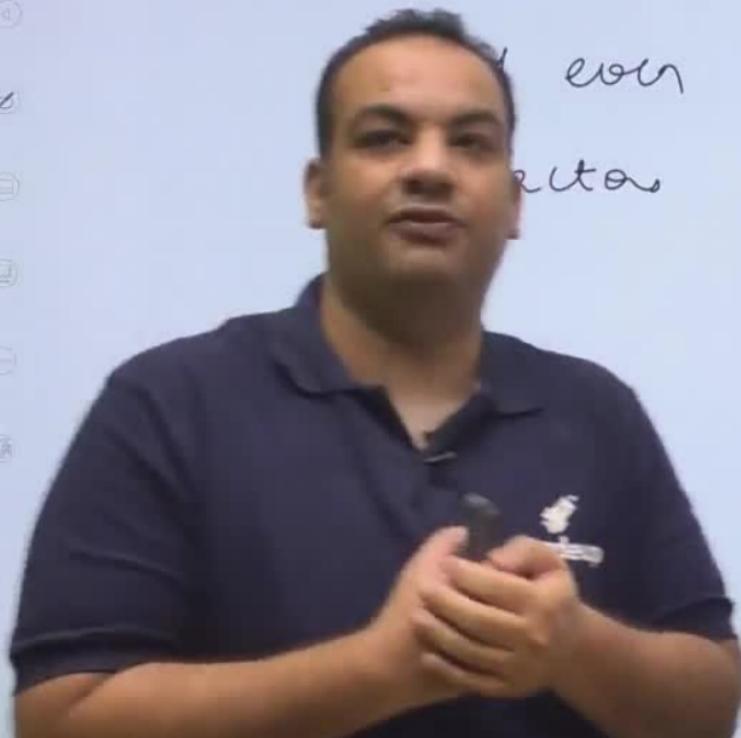
$$a(b+1)(c+1)$$

**Sahi Prep Hai
Toh Life Set Hai**

$$N = 2^a \cdot 3^b \cdot 5^c \cdots$$

even
actors

$$= a(b+1)(c+1) \cdots$$



Find the Number of Even factors of

(i) $2^3 3^4 5^6$

(ii) $3^8 5^7$

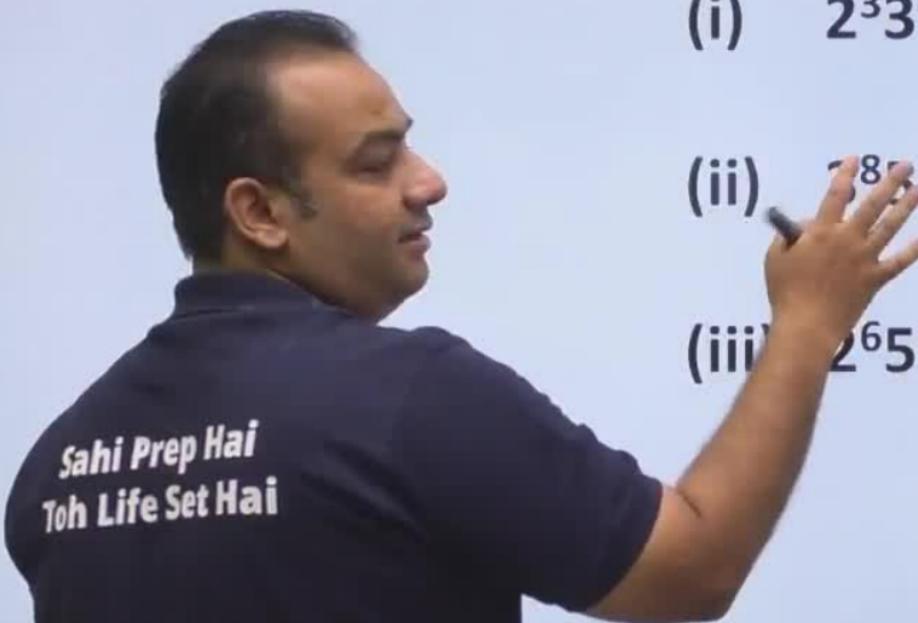
(iii) $2^6 5^8$

Find the Number of Even factors of

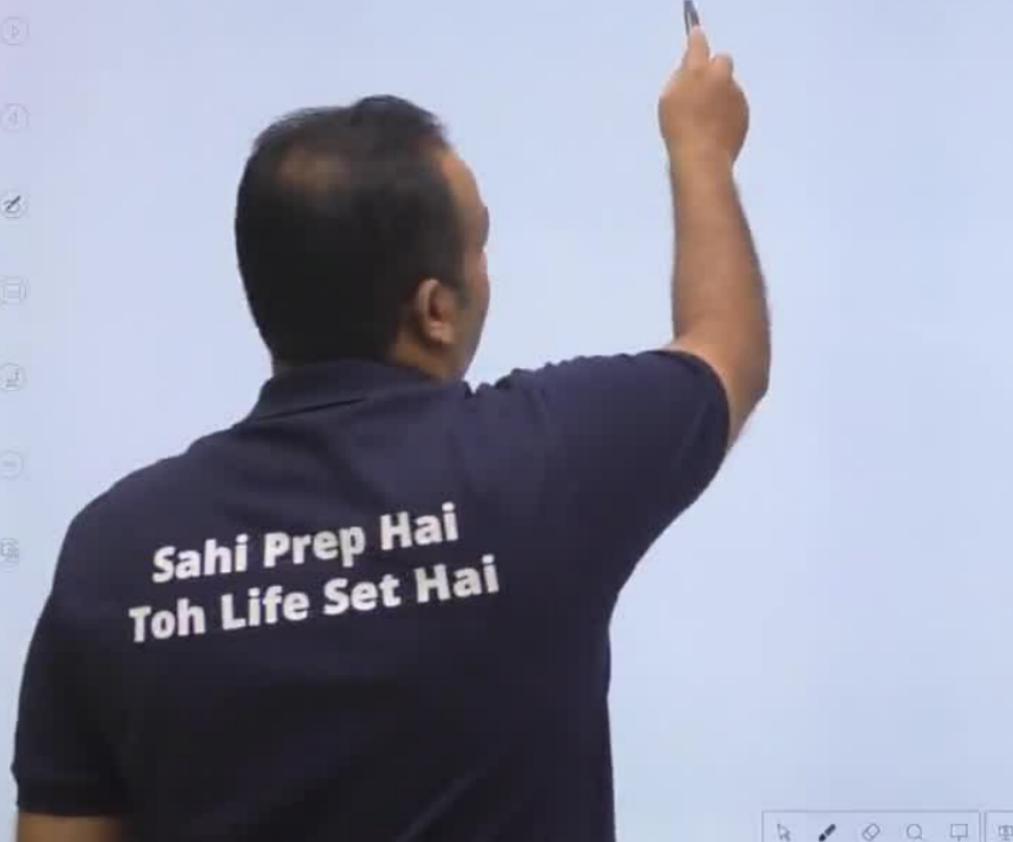
(i) $2^3 3^4 5^6 \rightarrow 3 \cdot 5 \cdot 7 = 105$

(ii) $2^8 3^7$

(iii) $2^6 5^8$



Perfect Square



Perfect Square

Perfect square = "Square of an integer"

$$0^2 = 0 \checkmark$$

$$1^2 = 1 \checkmark$$

$$2^2 = 4 \checkmark$$

$$3^2 = 9 \checkmark$$

$$4^2 = 16 \checkmark$$

Perfect Square

Perfect square = "Square of an integer"

$$0^2 = 0 \quad \checkmark$$

$$1^2 = 1 \quad \checkmark$$

$$2^2 = 4 \quad \times$$

$$3^2 = 9 \quad \times$$

$$4^2 = 16 \quad \times$$

is not a perfect square

$$1 \cdot p_1^y \cdot p_2^z \cdots -$$

next square

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Perfect Square

Perfect square = "Square of an integer"

$$0^2 =$$

$$1^2 =$$

18 is not a perfect square

$$N = p_1^x \cdot p_2^y \cdot p_3^z \dots$$

If N is a perfect square
then

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Perfect Square

Perfect square = "Square of an integer"

$$0^2 = 0$$

$$1^2 = 1$$

$$2^2$$

18 is not a perfect square

$$N = P_1^x \cdot P_2^y \cdot P_3^z \dots$$

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If N is a perfect square
then x, y & z are completely
di

Perfect Square

Perfect square = "Square of an integer"

$$0^2 = 0 \checkmark$$

$$1^2 = 1 \checkmark$$

$$2^2 = 4 \checkmark$$

$$3^2 = 9 \checkmark$$

$$4^2 = 16 \checkmark$$

18 is not a perfect square

$$N = P_1^x \cdot P_2^y \cdot P_3^z \dots$$

If N is a perfect square
then x, y & z are completely
div by 2

Perfect Square

Perfect square = "Square of an integer"

$$3^2 = 9 \quad \checkmark$$

$$2^2 = 4 \quad \checkmark$$

$$1^2 = 1 \quad \checkmark$$

$$0^2 = 0 \quad \checkmark$$

18 is not a perfect square

$$N = P_1^x \cdot P_2^y \cdot P_3^z \dots$$

If N is a perfect square
then x, y, z are completely
div by 2

How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?



How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{matrix} 2^0 \\ 2^1 \\ 2^2 \\ 2^3 \\ 2^4 \end{matrix}$$

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How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{ll} 2^0 & 3^0 \\ 2^1 & 3^1 \\ 2^2 & 3^2 \\ 2^3 & 3^3 \\ 2^4 & 3^4 \\ 2^5 & 3^5 \\ & 3^6 \\ & 3^7 \end{array}$$

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Toh Life Set Hai

How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{c} 2^0 \\ 3^0 \\ 3^1 \\ 3^2 \\ 3^3 \\ 3^4 \\ 3^5 \end{array}$$
$$\begin{array}{c} 5^0 \\ 5^1 \\ 5^2 \\ 5^3 \\ 5^4 \\ 5^5 \end{array}$$

$$3^8$$

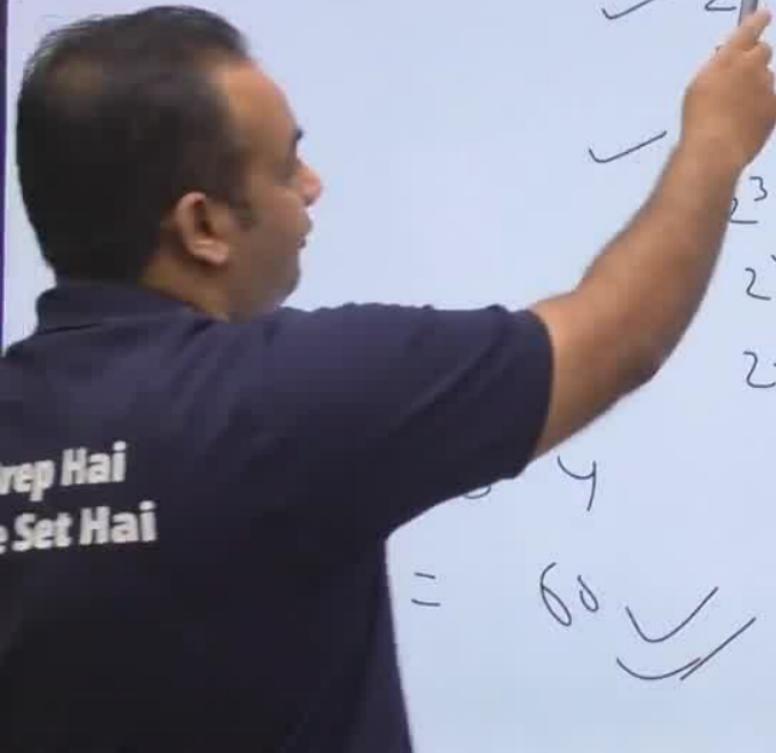
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Toh Life Set Hai

How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{ccc} \checkmark 2^0 & \checkmark 3^0 & 5^0 \\ 2^1 & 3^1 & 5^1 \\ \checkmark 2^2 & \checkmark 3^2 & 5^2 \\ 2^3 & 3^3 & 5^3 \\ \checkmark 2^4 & \checkmark 3^4 & 5^4 \\ 2^5 & 3^5 & 5^5 \\ & \checkmark 3^6 & 5^6 \\ & 3^7 & 5^7 \\ & \checkmark 3^8 & 5^8 \end{array}$$

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How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?



$$\begin{array}{cccc}
 \checkmark 2^1 & \checkmark 3^0 & \checkmark 5^1 \\
 \checkmark 2^2 & \checkmark 3^1 & \checkmark 5^2 \\
 \checkmark 2^3 & \checkmark 3^2 & \checkmark 5^3 \\
 \checkmark 2^4 & \checkmark 3^3 & \checkmark 5^4 \\
 \checkmark 2^5 & \checkmark 3^4 & \checkmark 5^5 \\
 & \checkmark 3^5 & \checkmark 5^6 \\
 & \checkmark 3^6 & \checkmark 5^7 \\
 & & \checkmark 5^8 \\
 = & 60 & \checkmark
 \end{array}$$

How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?



How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{c} 0/2/4 \\ 2 \\ 3 \\ 5 \end{array}$$

$$0/2/4/6/8$$

$$0/2/4/4$$

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How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{c} 0/2/4 \\ 2 \\ 3 \\ 0/2/4/6/8 \\ 5 \\ 0/2/4/6 \end{array}$$

$$3 \cdot 5 \cdot 4 = \underline{\underline{60}}$$

How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{c} 0/2/4 \\ 2 \\ 0/2/4/6/8 \\ 3 \\ 0/2/4/4 \\ 5 \end{array}$$

$$3 \cdot 5 \cdot 4 = \underline{\underline{60}}$$

$$2^{80} \cdot 3^{50}$$

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How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{c} 0/2/4 \\ 2 \\ 3 \\ 5 \end{array}$$

$$3^4 \cdot 5^2 \cdot 4 = \underline{\underline{60}}$$

$$2^8 \cdot 3^{5+1}$$

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How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{c} 0/2/4 \\ 2 \\ 0/2/4/6/8 \\ 3 \\ 0/2/4/4 \\ 5 \end{array}$$

$$3 \cdot 5 \cdot 4 = \underline{\underline{60}}$$

$$\begin{array}{c} 2^{80} \\ 3^{50} \\ 5^{11} \\ 41 \cdot 25 \cdot 6 \end{array}$$

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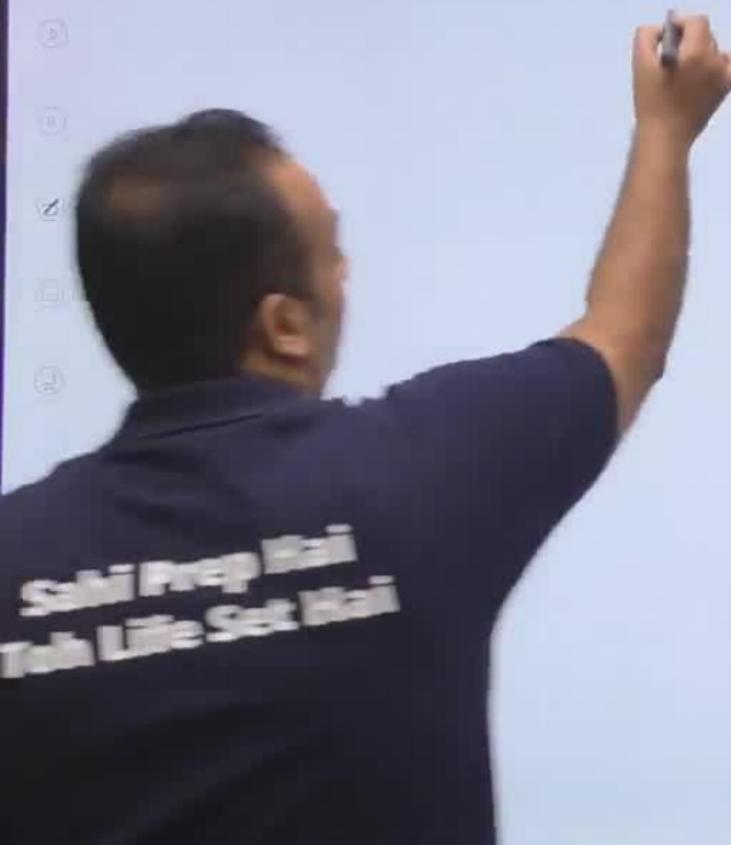
How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect squares?

$$\begin{array}{c} 0/2/4 \\ 2 \\ 3 \\ 5 \end{array}$$

$$3 \cdot 5 \cdot 4 = \underline{\underline{60}}$$

$$\begin{array}{cccc} 9 & 2^8 & 3^{50} & 5^{11} \\ \rightarrow & 41 \cdot 28 \cdot 6 \end{array}$$

Perfect Cube



Perfect Cube

$$1^3 = 1$$

$$2^3 = 8$$

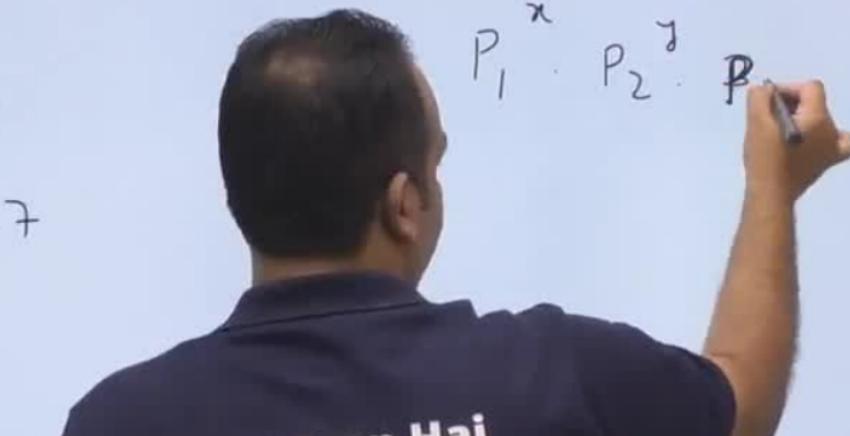
$$3^3 = 27$$

4

5

6

$$P_1^x \cdot P_2^y \cdot P_3^z$$



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Perfect Cube

$$1^3 = 1$$

8

27

$$N = P_1^x \cdot P_2^y \cdot P_3^z \dots$$

If N is a perfect cube
then

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Perfect Cube

Laser Pointer

Pen

Highlighter

Eraser

Erase

$$1^3 = 1$$

$$2^3 = 8$$

$$3^3 = 27$$

1

1

1

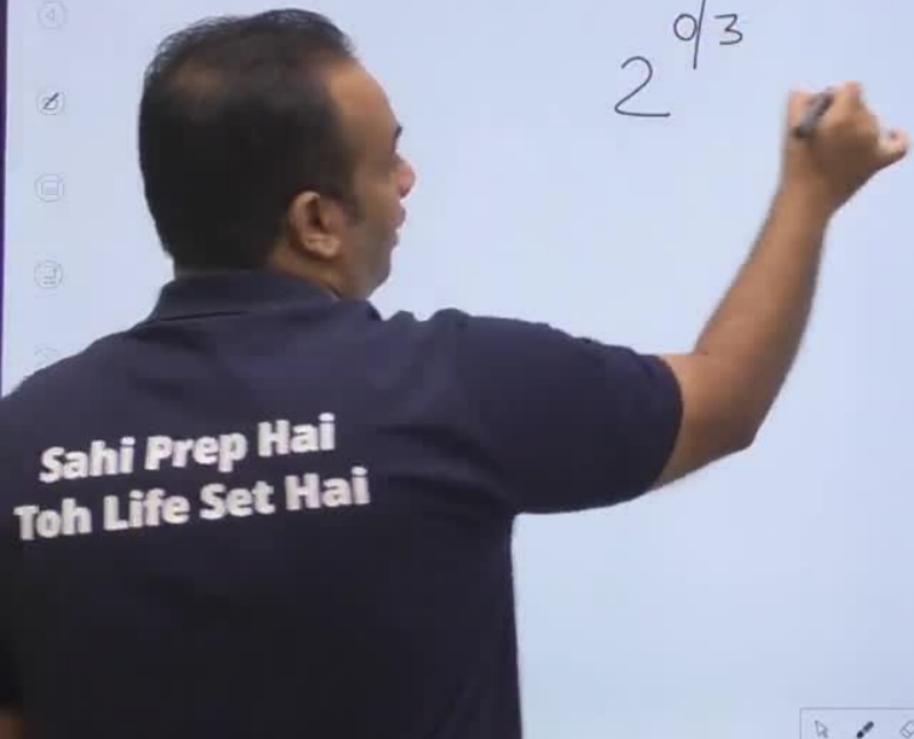
$$N = P_1^x \cdot P_2^y \cdot P_3^z \dots$$

If N is a perfect cube
then x, y, z are mult.

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Life Set Hai

How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect cubes?

$$2^{0/3}$$



How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect cubes?

$$\begin{array}{ccc} 2 & 0/3 & 0/3/6 \\ & & 5 & 0/3/6 \end{array}$$

$$2 \quad 3 = \underline{18}$$

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How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect cubes?

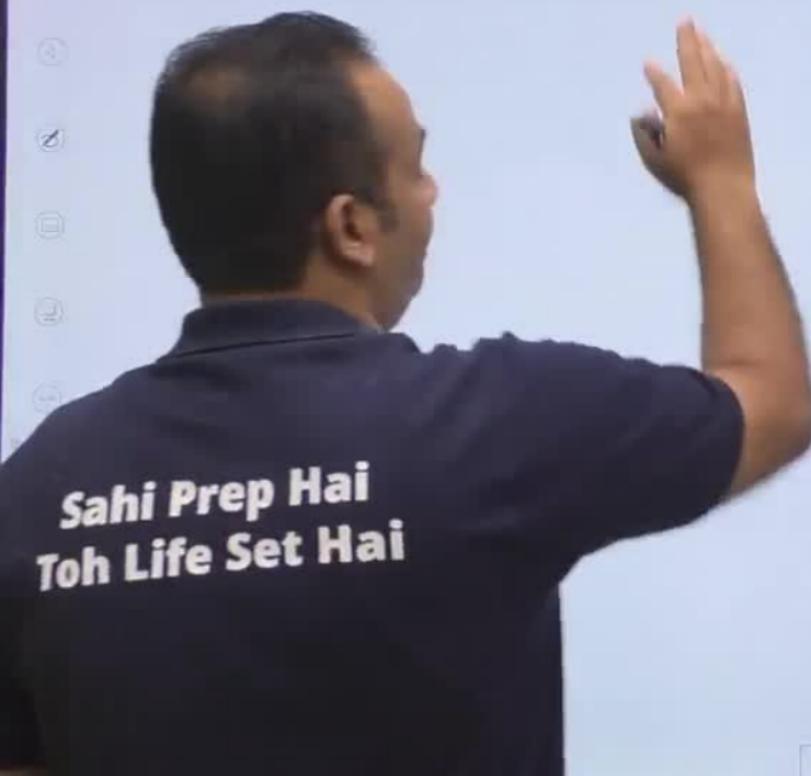
$$2^{0/3}$$

$$3^{0/3/6}$$

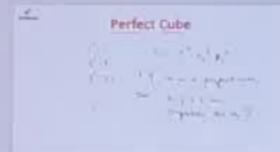
$$5^{0/3/6}$$

$$2 \cdot 3 \cdot 3 = 18 \\ \underline{\underline{}}$$

Q. How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are Prime?

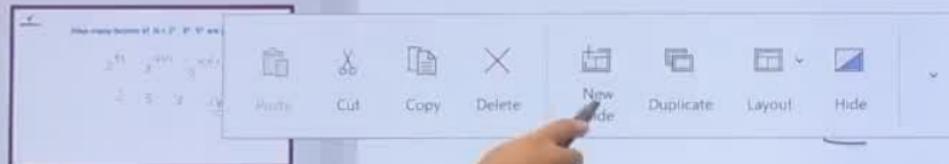


25



How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are perfect cubes?

26



27



Type here to search



Notes



11:44 AM

A person wearing a dark t-shirt with the text "prep Hai" and "Set Hai" is pointing their right index finger towards a Microsoft PowerPoint slide. The slide has a light blue background with two text boxes: one large box at the top containing the placeholder "Click to add title" and a smaller box below it containing "Click to add text". The Microsoft ribbon menu is visible at the top, showing tabs like File, Home, Insert, Design, Transitions, Animations, Slide Show, Review, View, MathType, and Help. The "Slide Show" tab is currently selected. The status bar at the bottom shows the time as 11:44 AM.

AutoSave

5- Factors & Consecutive Integers (SS...)

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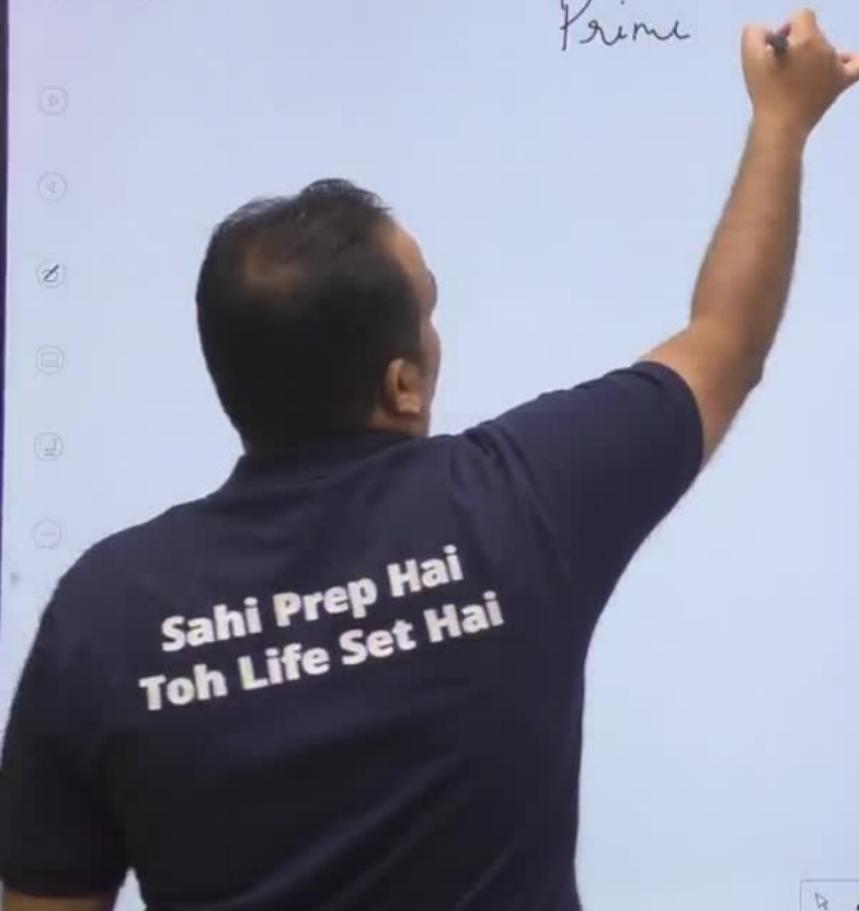
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prep Hai
Set Hai

Notes

11:44 AM

Prime



Prime Factors

$$72 \rightarrow 2^3 \cdot 3^2$$

factors of 72 →

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Toh Life Set Hai

Prime Factors

$$72 \rightarrow 2^3 \cdot 3^2$$

Factors of 72 → 1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

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Life Set Hai

Prime Factors

$$72 \rightarrow 2^3 \cdot 3^2$$

Factor of 72 → 1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

Factor of 7

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Prime Factors

$$72 \rightarrow 2^3 \cdot 3^2$$

Factor of

1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

Factors which are prime

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Toh Life Set Hai

Prime Factors

$$72 \rightarrow 2^3 \cdot 3^2$$

Factor of 72 → 1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

Factors of 72 which are prime is 2

) T

Prime Factors

$$72 \rightarrow 2^3 \cdot 3^2$$

Factors of 72 → 1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

Factors of 72 which are prime is $\underline{\underline{2}}$

BUT

SSC gives answer as $\underline{\underline{5}}$

Prime Factors

$$72 \rightarrow 2^3 \cdot 3^2$$

factors of 72 $\rightarrow 1, \cancel{2}, \cancel{3}, 4, 6, 8, 9, 12, 18, 24, 36, 72$

of which are prime is 2

Q U T

SSC gives answer 5

Q. How many factors of $N = 2^5 \cdot 3^8 \cdot 5^6$ are Prime?

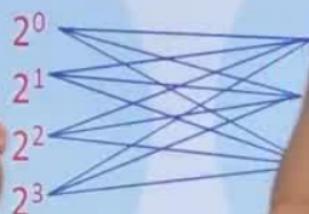
Correct answer

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Sum of Factors

Let Number = $72 = 2^3 \cdot 3^2$

2^0
 2^1
 2^2
 2^3



$$2^0 \cdot 3^0 + 2^0 \cdot 3^1 + 2^0 \cdot 3^2$$

$$2^1 \cdot 3^0 + 2^1 \cdot 3^1 + 2^1 \cdot 3^2$$

$$2^2 \cdot 3^0 + 2^2 \cdot 3^1 + 2^2 \cdot 3^2$$

$$2^3 \cdot 3^0 + 2^3 \cdot 3^1 + 2^3 \cdot 3^2$$

$$\frac{3^0(2^0 + 2^1 + 2^2 + 2^3) + 3^1(2^0 + 2^1 + 2^2 + 2^3) + 3^2(2^0 + 2^1 + 2^2 + 2^3)}{}$$

$$= (2^0 + 2^1 + 2^2 + 2^3)(3^0 + 3^1 + 3^2) = 195$$

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Teh Life Set Hai

Sum of Factors

Let Number = $72 = 2^3 \cdot 3^2$

$$\begin{matrix} 2^0 & & 3^0 \\ 2^1 & & 3^1 \\ 2^2 & & \\ 2^3 & & 3^2 \end{matrix}$$

$$2^0 \cdot 3^0 + 2^0 \cdot 3^1 + 2^0 \cdot 3^2$$

$$2^1 \cdot 3^0 + 2^1 \cdot 3^1 + 2^1 \cdot 3^2$$

$$2^2 \cdot 3^0 + 2^2 \cdot 3^1 + 2^2 \cdot 3^2$$

$$2^3 \cdot 3^0 + 2^3 \cdot 3^1 + 2^3 \cdot 3^2$$

$$3^0(2^0 + 2^1 + 2^2 + 2^3) + 3^1(2^0 + 2^1 + 2^2 + 2^3) + 3^2(2^0 + 2^1 + 2^2 + 2^3)$$

$$= (2^0 + 2^1 + 2^2 + 2^3)(3^0 + 3^1 + 3^2) = 195$$

Sum of Factors

Let Number = $72 = 2^3 \cdot 3^2$

$$\begin{matrix} 2^0 & & 3^0 \\ 2^1 & \nearrow & 3^1 \\ 2^2 & \nearrow & 3^2 \end{matrix}$$

$$2^0 \cdot 3^0 + 2^0 \cdot 3^1 + 2^0 \cdot 3^2$$

$$2^1 \cdot 3^0 + 2^1 \cdot 3^1 + 2^1 \cdot 3^2$$

$$2^2 \cdot 3^0 + 2^2 \cdot 3^1 + 2^2 \cdot 3^2$$

$$2^3 \cdot 3^0 + 2^3 \cdot 3^1 + 2^3 \cdot 3^2$$

$$3^0(2^0 + 2^1 + 2^2 + 2^3) + 3^1(2^0 + 2^1 + 2^2 + 2^3) + 3^2(2^0 + 2^1 + 2^2 + 2^3)$$

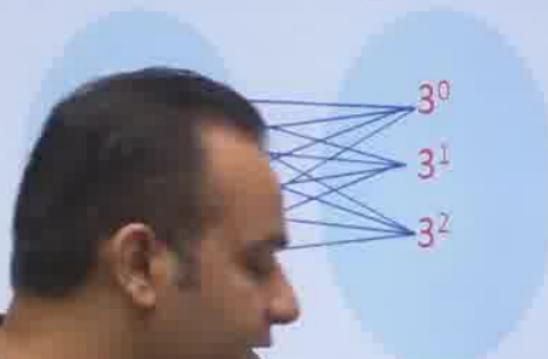
$$= (2^0 + 2^1 + 2^2 + 2^3)(3^0 + 3^1 + 3^2) = 195$$

$$\Rightarrow 1 + 2$$

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Toh Life Set Hai*

Sum of Factors

Let Number = $72 = 2^3 \cdot 3^2$



$$2^0 \cdot 3^0 + 2^0 \cdot 3^1 + 2^0 \cdot 3^2$$

$$2^1 \cdot 3^0 + 2^1 \cdot 3^1 + 2^1 \cdot 3^2$$

$$2^2 \cdot 3^0 + 2^2 \cdot 3^1 + 2^2 \cdot 3^2$$

$$2^3 \cdot 3^0 + 2^3 \cdot 3^1 + 2^3 \cdot 3^2$$

$$3^0(2^0 + 2^1 + 2^2 + 2^3) + 3^1(2^0 + 2^1 + 2^2 + 2^3) + 3^2(2^0 + 2^1 + 2^2 + 2^3)$$

$$= (2^0 + 2^1 + 2^2 + 2^3)(3^0 + 3^1 + 3^2) = 195$$

$$(1+2+4+8)(1+3+9) \\ (15 \cdot 13)$$

If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Sum of Factors = $(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$

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If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Sum of Factors

$$(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$$

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If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Number of Factors = $(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$

e.g.

$$N = 2^1 \cdot 3^1 \cdot 5^2$$

Sum of all the factors of N

If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Sum of divisors = $(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$

$$N = 2^t \cdot 3^1 \cdot 5^2$$

Sum

$$+ (2^0 + (2^1 + ($$

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If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Sum of divisors = $(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$

$$N = 2^1 \cdot 3^1 \cdot 5^2$$

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$$\rightarrow (2^0 + 2^1) (3^0 + 3^1) (5^0 + 5^1 + 5^2)$$

If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Sum of Factors = $(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$

eg. $= 2^1 \cdot 3^1 \cdot 5^2$

$\rightarrow (2^0 + 2^1) (3^0 + 3^1) (5^0 + 5^1 + 5^2)$
 $3 \cdot 4 \cdot 31$

S.
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If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Sum of Factors = $(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$

eg

$$2^1 \cdot 3^1 \cdot 5^2$$

Sum =

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$$(2^0 + 2^1) (3^0 + 3^1) (5^0 + 5^1 + 5^2)$$

$$3 \cdot 4 \cdot 31$$

$$\therefore \underline{372}$$

If $N = P_1^a \cdot P_2^b \cdot P_3^c$

Sum of Factors = $(P_1^0 + P_1^1 + \dots + P_1^a)(P_2^0 + P_2^1 + \dots + P_2^b)(P_3^0 + P_3^1 + \dots + P_3^c)$

eg $N = 2^1 \cdot 3^1 \cdot 5^2$

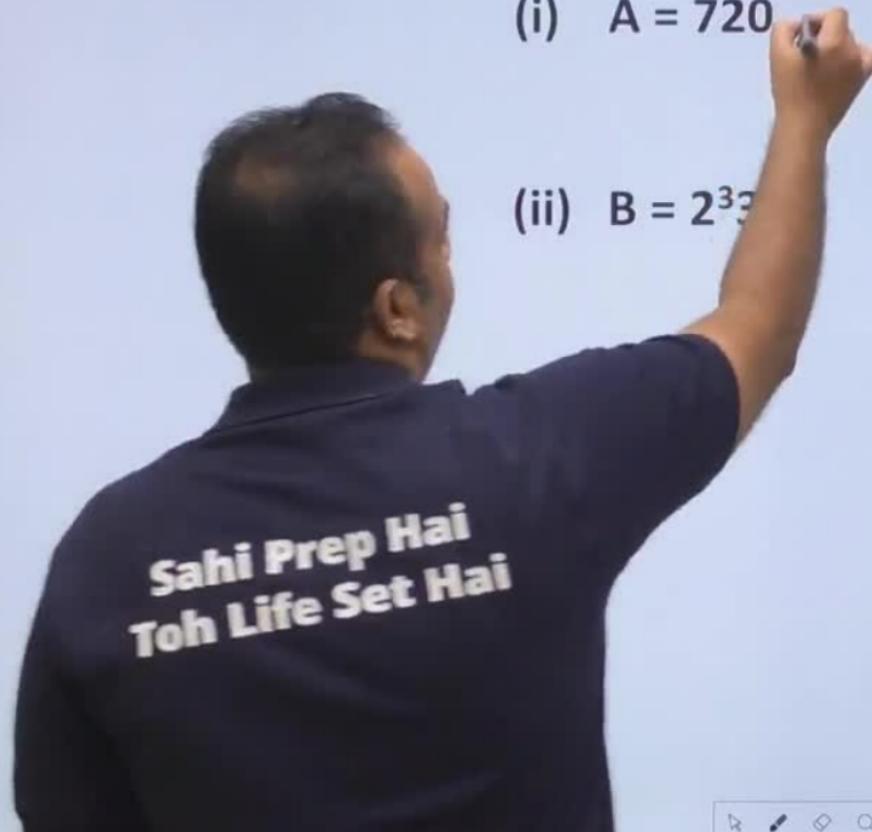
Sum of all the factors of $N \rightarrow (2^0 + 2^1) (3^0 + 3^1) (5^0 + 5^1 + 5^2)$

$$\begin{aligned} &= (1+2) (1+3) (1+5+25) \\ &= 3 \cdot 4 \cdot 31 \\ &= 372 \end{aligned}$$

Q. Find the sum of all the factors of:

(i) $A = 720$

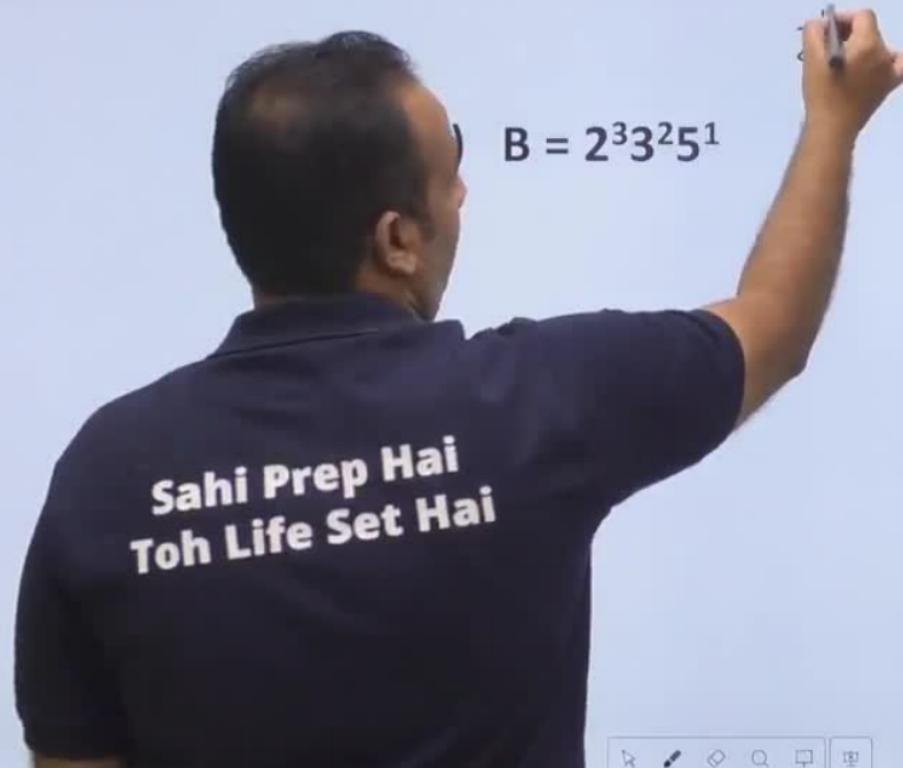
(ii) $B = 2^3 \cdot 3^2 \cdot 5$



Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

) $B = 2^3 \cdot 3^2 \cdot 5^1$

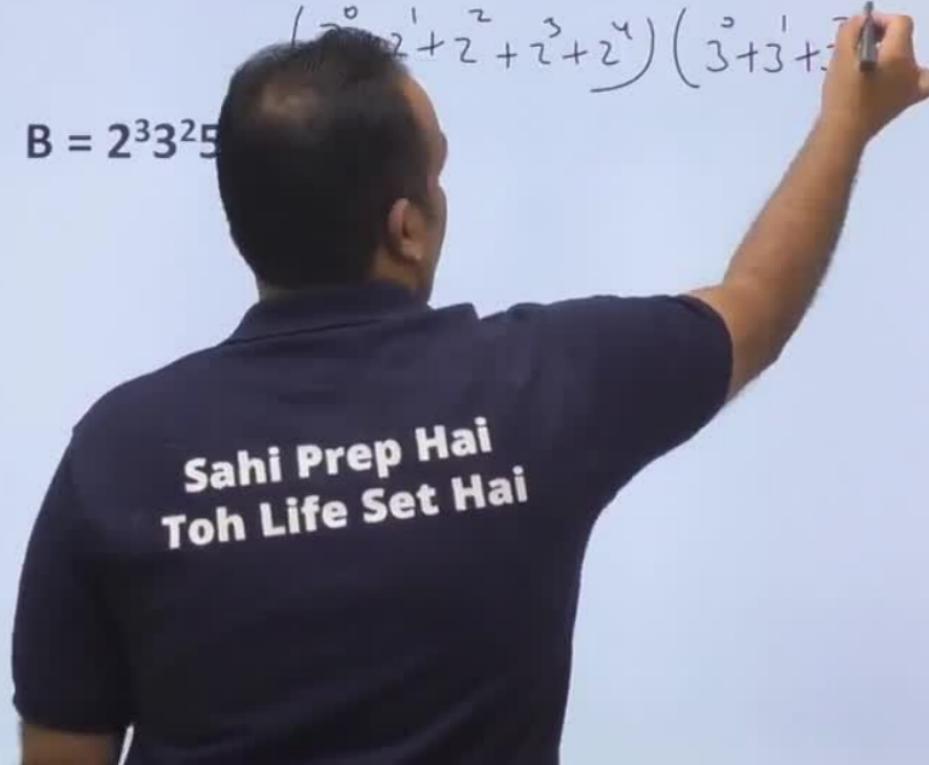


Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

$$(2^0 + 2^1 + 2^2 + 2^3 + 2^4)(3^0 + 3^1 + 3^2)$$

(ii) $B = 2^3 \cdot 3^2 \cdot 5^1$



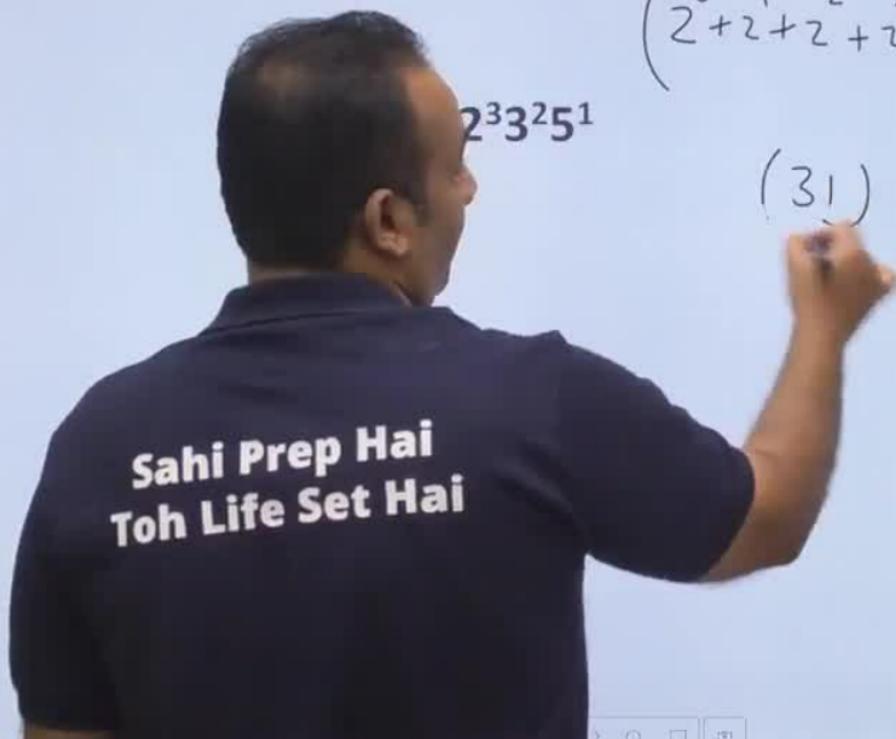
Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

$$(2^{+2} + 2^1 + 2^2 + 2^3 + 2^4)(3^{+3} + 3^1 + 3^2)(5^{+5} + 5^1)$$

$$2^3 3^2 5^1$$

$$(31)$$



Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

$$(2^0+2^1+2^2+2^3+2^4)(3^0+3^1+3^2)(5^0+5^1)$$

(ii) $B = ?$

$$(31)(13)$$

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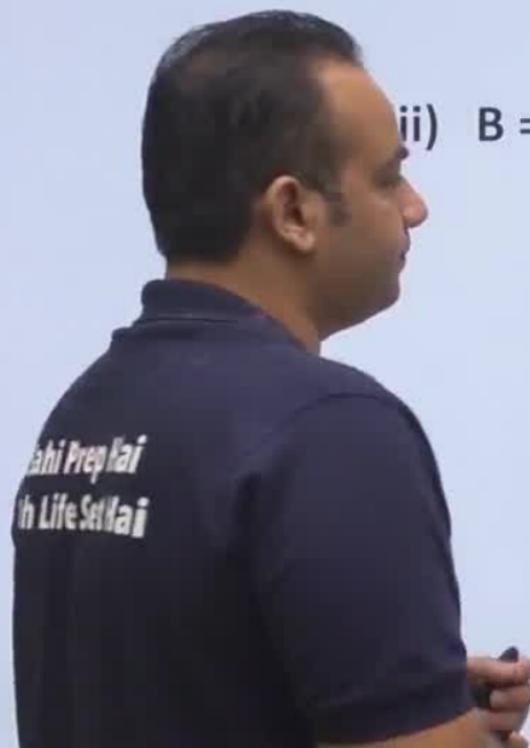
Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

$$(2^0+2^1+2^2+2^3+2^4)(3^0+3^1+3^2)(5^0+5^1)$$

ii) $B = 2^3 \cdot 3^2 \cdot 5^1$

$$(31)(13)(1)$$



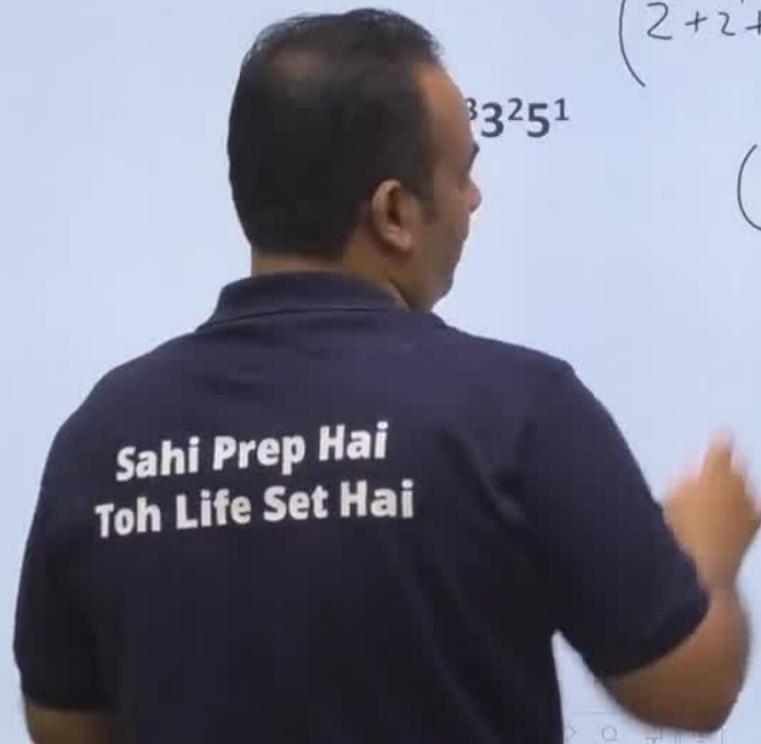
Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

$$(2^0+2^1+2^2+2^3+2^4)(3^0+3^1+3^2)(5^0+5^1)$$

$$3^2 \cdot 5^1$$

$$(31)(13)(1)$$



Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

$$(2^0+2^1+2^2+2^3+2^4)(3^0+3^1+3^2)(5^0+5^1)$$

(ii) $B = 2^3 \cdot 3^2 \cdot 5^1$

$$(31)(13)(1)$$

$$= \underline{2418}$$

170

Q. Find the sum of all the factors of:

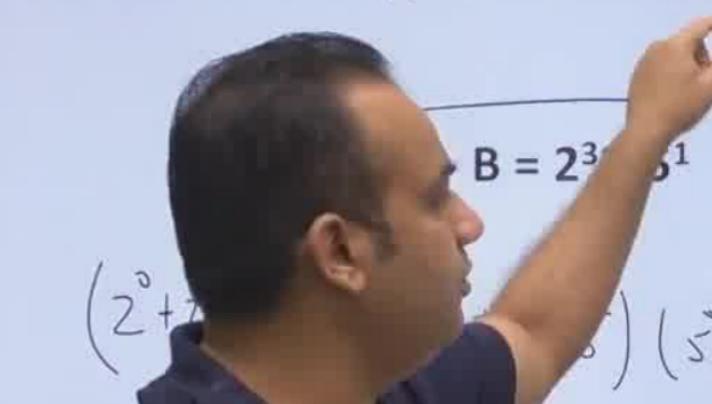
(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

$$\begin{aligned} & (2^0+2^1+2^2+2^3+2^4)(3^0+3^1+3^2)(5^0+5^1) \\ & (1)(13)(6) \\ & = \underline{\underline{2418}} \end{aligned}$$

Q. Find the sum of all the factors of:

(i) $A = 720 \rightarrow 2^4 \cdot 3^2 \cdot 5^1$

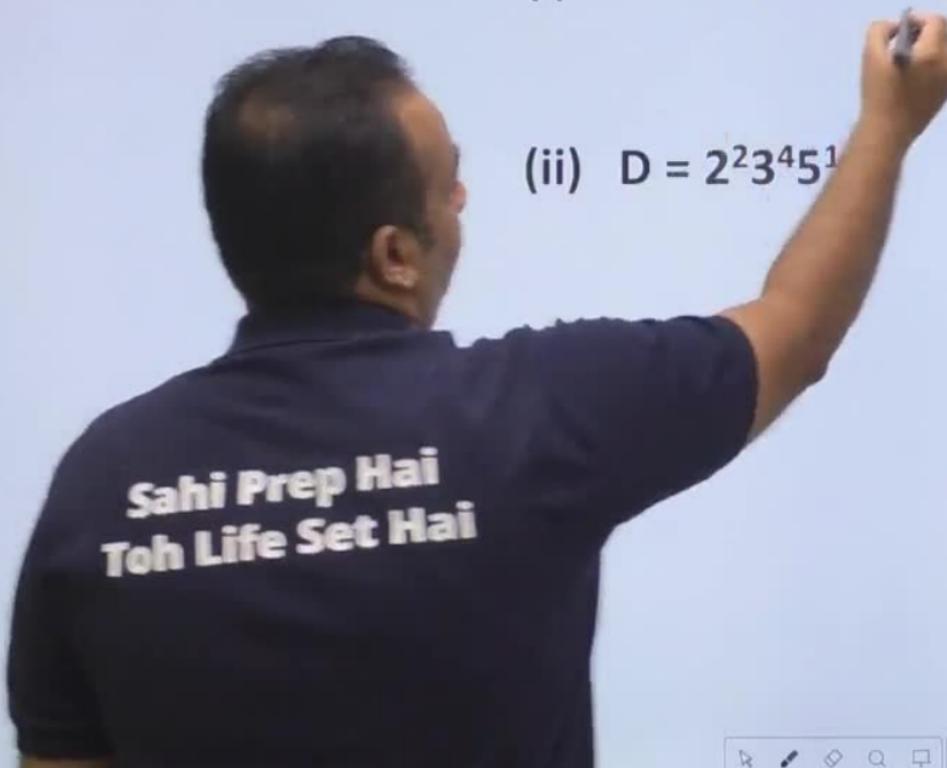
$$\begin{aligned}B &= 2^3 \cdot 3^1 \\&\quad \left(2^0+2^1+2^2+2^3+2^4\right) \left(3^0+3^1+3^2\right) \left(5^0+5^1\right) \\&\quad (31)(13)(6) \\&= \underline{2418}\end{aligned}$$



Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$

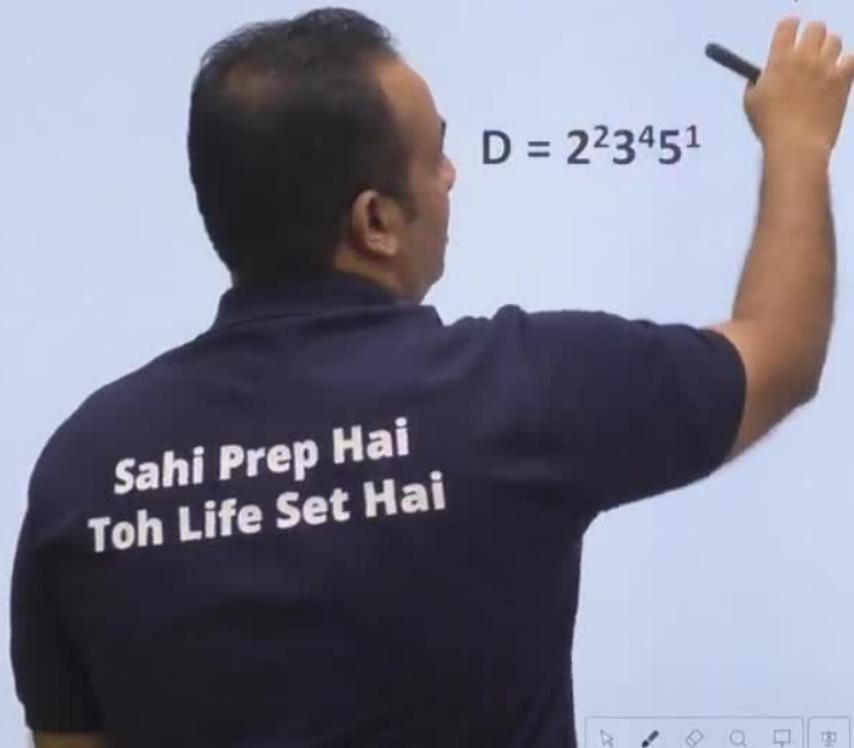
(ii) $D = 2^2 3^4 5^1$



Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $(2^1 + 2^2 + 2^3)(3^1 + 3^2 + 3^3)(5^1 + 5^0)$

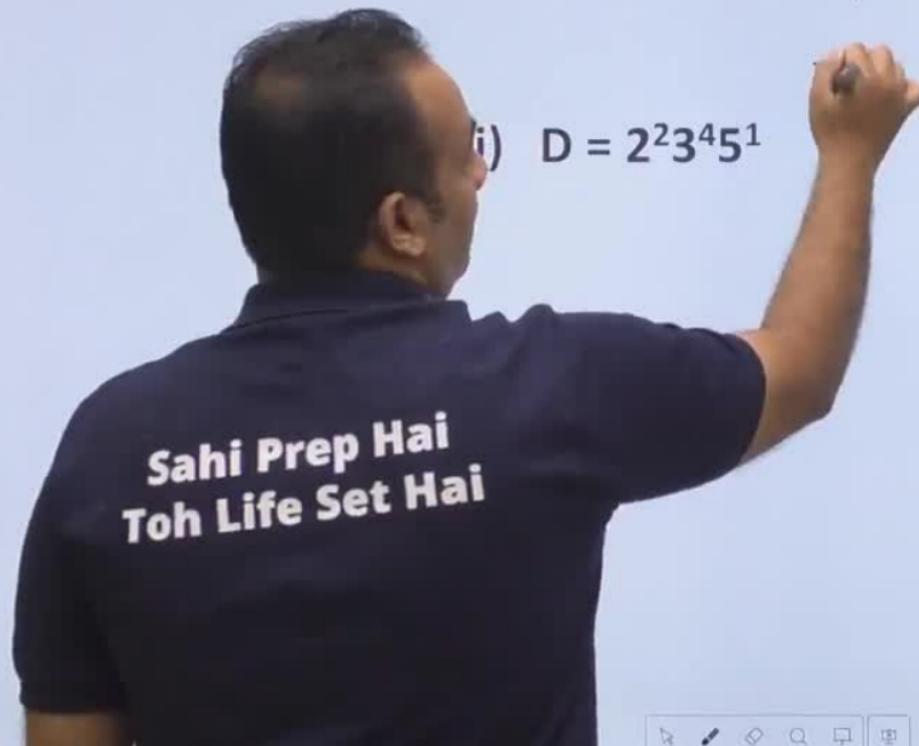
$D = 2^2 3^4 5^1$



Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $(2^1 + 2^2 + 2^3)(3^1 + 3^2 + 3^3)(5^1 + 5^0)$

(ii) $D = 2^2 3^4 5^1$



Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $(2^1 + 2^2 + 2^3)(3^1 + 3^2 + 3^3)(5^1 + 5^0)$

$\rightarrow 14 \cdot 13 \cdot 6$

45^1

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Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $(2^1 + 2^2 + 2^3)(3^0 + 3^1 + 3^2)(5^0 + 5^1)$
 $\rightarrow 14 \cdot 13 \cdot 6 = \underline{1092}$

(ii) $D = 2^2 3^4 5^1$

$$(2^1 + 2^2)(3^0 + 3^1 + 3^2 + 3^3 + 3^4)$$

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Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $(2^1 + 2^2 + 2^3)(3^1 + 3^2 + 3^3)(5^1 + 5^0)$

$$\rightarrow 14 \cdot 13 \cdot 6 = \underline{1092}$$

$$D = 2^2 3^4 5^1$$

$$(2^1 + 2^2)(3^1 + 3^2 + 3^3 + 3^4 + 3^5)(5^1 + 5^0)$$

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Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $(2^1 + 2^2 + 2^3)(3^1 + 3^2 + 3^3)(5^1 + 5^0)$
 $\rightarrow 14 \cdot 13 \cdot 6 = \underline{1092}$

(ii) $D = 2^2 3^4 5^1$

$$(2^1 + 2^2)(3^1 + 3^2 + 3^3 + 3^4 + 3^5)(5^1 + 5^0)$$
$$6 \cdot (12)$$

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Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $\left(2^1 + 2^2 + 2^3\right) \left(3^0 + 3^1 + 3^2\right) \left(5^0 + 5^1\right)$

$$\rightarrow 14 \cdot 13 \cdot 6 = \underline{1092}$$

(ii) $D = 2^5 5^1$

$$\left(2^1 + 2^2 + 2^3 + 2^4 + 2^5\right) \left(5^0 + 5^1\right)$$

$$(121)(6)$$

$$= \underline{4356}$$

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Toh Life Set Hai

Q. Find the sum of all even factors of:

(i) $C = 2^3 3^2 5^1$ $(2^1 + 2^2 + 2^3)(3^0 + 3^1 + 3^2)(5^0 + 5^1)$

$\rightarrow 13 \cdot 6 = \underline{1092}$

$D = 2^2 3^4 5^1$

$(2^1 + 2^2 + 2^3 + 2^4)(3^0 + 3^1 + 3^2 + 3^3 + 3^4)(5^0 + 5^1)$

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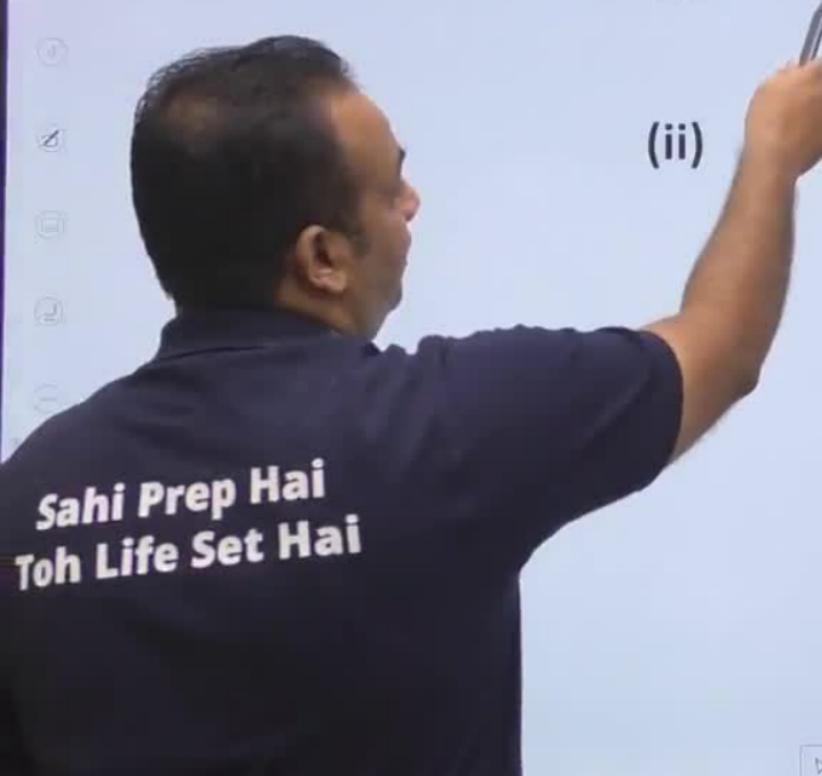
(-1) (c)

4356

Q. Find the sum of all odd factors of:

(i) $A = 2^4 3^3 5^1$

(ii) $3^2 5^3$



Q. Find the sum of all odd factors of:

(i) $A = 2^4 3^3 5^1 \rightarrow (3^0 + 3^1 + 3^2 + 3^3)(5^0 + 5^1)$

$$40 \cdot 6 = \underline{240}$$

(ii) $B = 3^2 5^3$

$$(3^0 + 3^1 + 3^2)$$

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Q. Find the sum of all odd factors of:

(i) $A = 2^4 3^3 5^1 \rightarrow (3^0 + 3^1 + 3^2 + 3^3)(5^0 + 5^1)$

$40 \cdot 6 = \underline{240}$

(ii) $B = 3^2 5^3$

$$(3^0 + 3^1 + 3^2) (5^0 + 5^1 + 5^2 + 5^3)$$

13

Q. Find the sum of all odd factors of:

(i) $A = 2^4 3^3 5^1 \rightarrow (3^0 + 3^1 + 3^2 + 3^3)(5^0 + 5^1)$

$$40 \cdot 6 = \underline{240}$$

(ii) $B = 3^2 5^3$

$$(3^0 + 3^1 + 3^2)(5^0 + 5^1 + 5^2 + 5^3)$$

$$13 \times 156$$

=

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Q. Find the sum of all odd factors of:

(i) $A = 2^4 3^3 5^1 \rightarrow (3^0 + 3^1 + 3^2 + 3^3)(5^0 + 5^1)$

$$40 \cdot 6 = \underline{240}$$

$$B = 3^2 5^3$$

$$(3^0 + 3^1 + 3^2)(5^0 + 5^1 + 5^2 + 5^3)$$

$$13 \times 156$$

$$2028$$

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Product of all the factors

$$72 = 2^3 \times 3^2$$

1 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72

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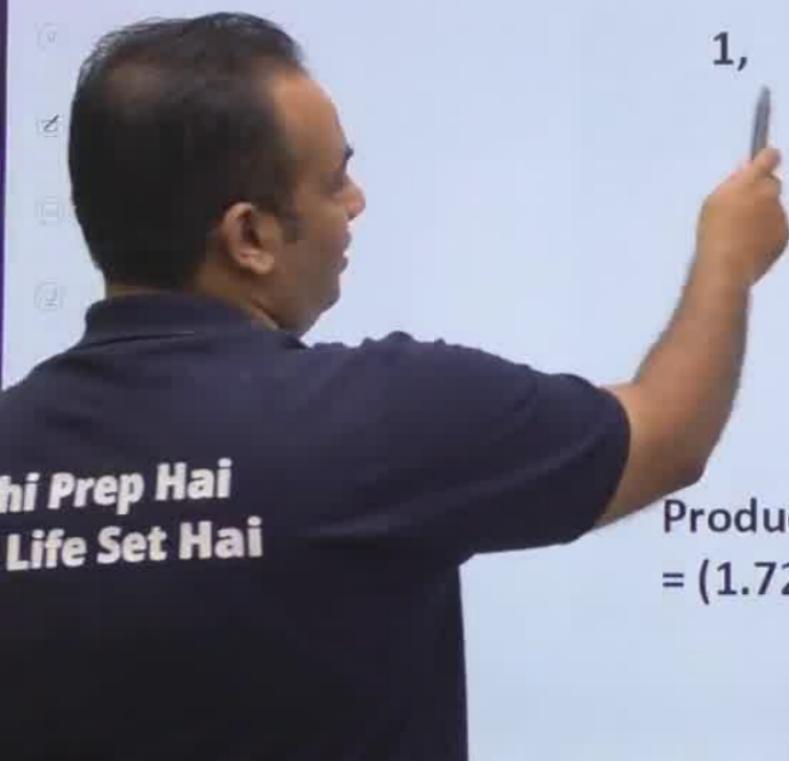
Product of all the factors of 72

$$= (1.72) (2.36) (3.24) (4.18) (6.12) (8.9) = (72)^6$$

Product of all the factors

$$72 = 2^3 3^2$$

1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72



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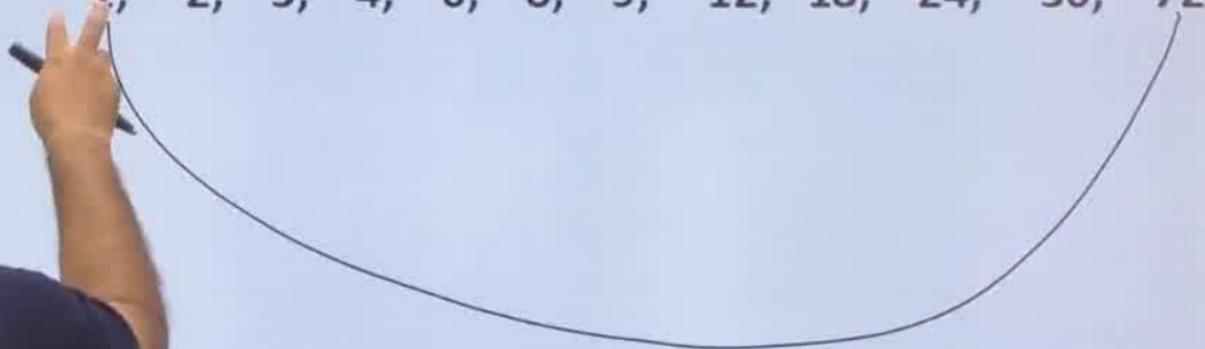
Product of all the factors of 72

$$= (1.72) (2.36) (3.24) (4.18) (6.12) (8.9) = (72)^6$$

Product of all the factors

$$\underline{72} = \underline{2^3} \underline{3^2}$$

1, 2, 3, 4, 6, 8, 9, 12, 18, 24, 36, 72



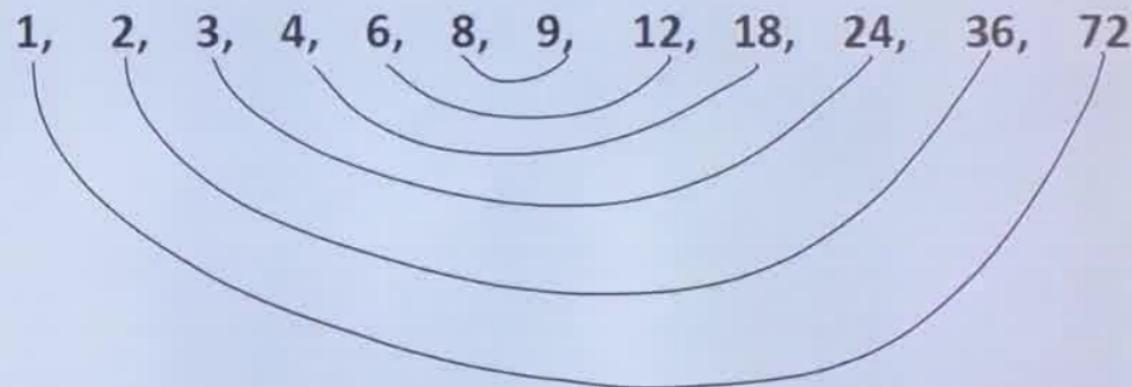
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Product of all the factors of 72

$$= (1.72) (2.36) (3.24) (4.18) (6.12) (8.9) = (72)^6$$

Product of all the factors

$$\underline{\underline{72}} = \underline{\underline{2^3 3^2}}$$

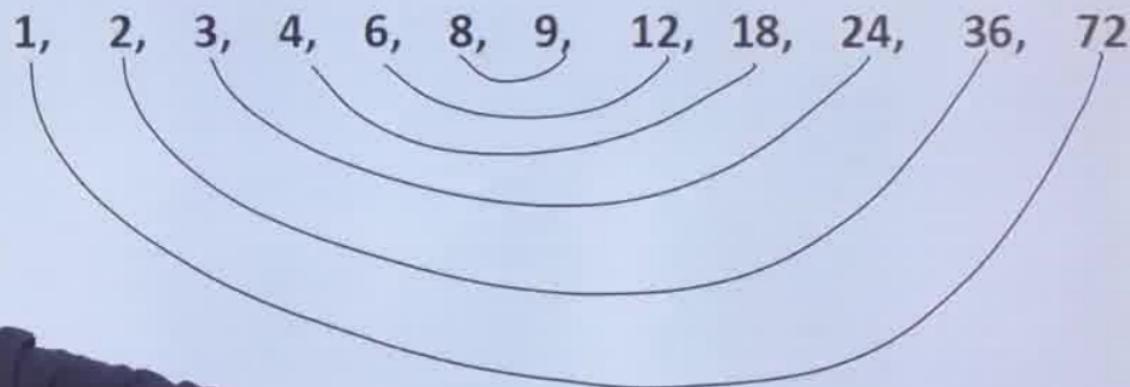


Product of all the factors of 72

$$(1.72) (2.36) (3.24) (4.18) (6.12) (8.9) = (72)^6$$

Product of all the factors

$$\underline{\underline{72}} = \underline{\underline{2^3 3^2}}$$



factors of 72

$$(1.72) (2.36) (3.24) (4.18) (6.12) (8.9) = (72)^6$$

Product of all the factors of N

Where $N = P_1^a P_2^b P_3^c$

n = number of factors of N

Product of all the factors of N

$$= (N)^{\frac{n}{2}}$$

Product of all the factors of N

Where $N = P_1^a P_2^b P_3^c$

n = number of factors of N

Product of all the factors of N

$$(N)^{\frac{n}{2}}$$

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Product of all the factors of N

Where $N = P_1^a P_2^b P_3^c$

n = number of factors of N

Product of all the factors of N

$$(N)^{\frac{n}{2}}$$

Product of all the factors of N

Where $N = P_1^a P_2^b P_3^c$

n = number of factors of N

Product of all the factors of N

$$= (N)^{\frac{n}{2}}$$

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Q. Find the product of all factors of

(i) $A = 200$

(ii) $= 100$

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Q. Find the product of all factors of

(i) $A = \underline{200}$

(ii) $B = \underline{100}$

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Q. Find the product of all factors of

$$200 = 2^3 5^2$$

No. of Factors
 $\rightarrow 4 \times 3 = 12$

- (i) $A = \underline{\underline{200}} \rightarrow (200)$
- (ii) $B = \underline{\underline{?}}$

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Q. Find the product of all factors of

$$200 = 2^3 5^2$$

No. of Factors
 $\rightarrow 4 \times 3 = 12$

(i) $A = \underline{\underline{200}} \rightarrow (200)$

(ii) $B = 100$

Q. Find the product of all factors of

$$200 = 2^3 5^2$$

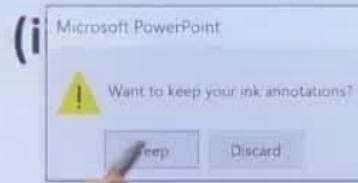
No. of Factors
 $\rightarrow 4 \times 3 = 12$

$$100 = 2^2 5^2$$

Factor = 9

(i) $A = \underline{\underline{200}}$

$$\rightarrow (200)^6$$



$$\rightarrow (100)^{\frac{9}{2}}$$

$$\rightarrow (10^x)^{\frac{9}{x}}$$

$$= 10^9$$



Factors & Consecutive Integers

$$200 = 2^3 5^2$$

No of Factors
 $\rightarrow 4 \times 3 = 12$

$$100 = 2^2 5^2$$

No of Factor = 9

Q. Find the product of all factors of

(i) $A = \underline{\underline{200}}$

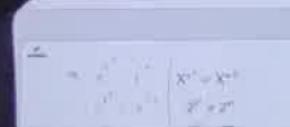
$$\rightarrow (200)^6$$

(ii) $B = \underline{100}$

$$\rightarrow (100)^{\frac{9}{2}}$$

$$\rightarrow (10^x)^{\frac{9}{x}}$$

$$= 10^9$$



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S- Factors & Consecutive Integers (SS...)

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Consecutive Integers

Click to add text

Consecutive Integer → 2 min - 25 min

Homework of Factor → 5 min

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Notes

12:04 PM

Consecutive Integer → 2 min - 25 min

Homework of Factor → 5 min

Factors → $(65\text{ min} - 70\text{ min})$

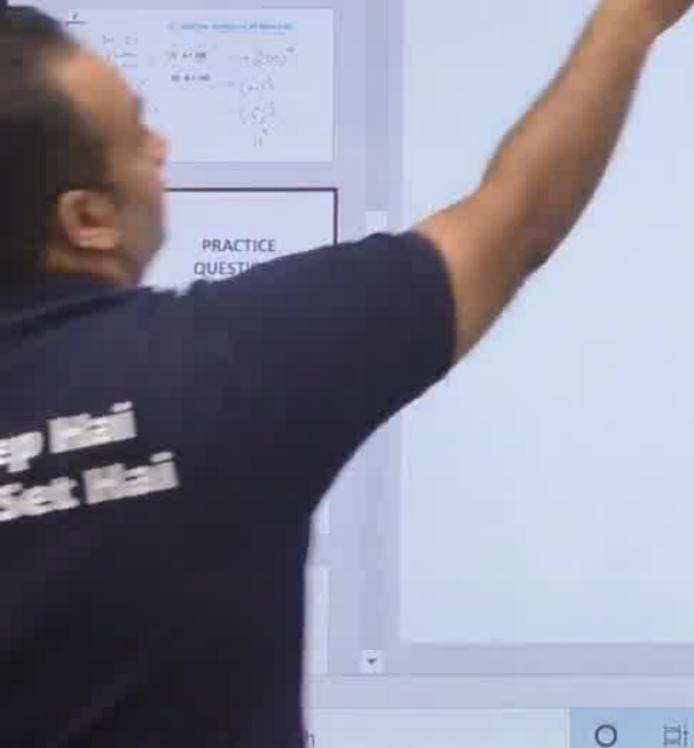
Consecutive
Integers → $\underline{20\text{ min} - 25\text{ min}}$

Homework of
Factors → $\underline{5\text{ min}}$

37



PRACTICE QUESTIONS



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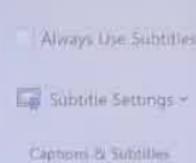
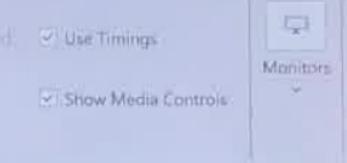
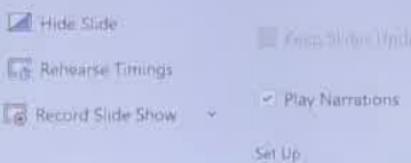
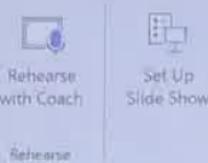
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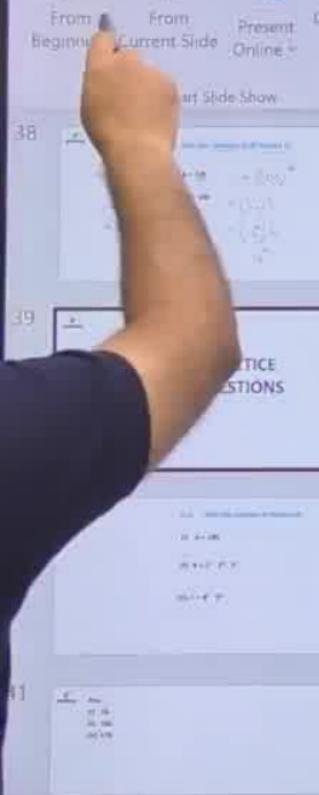
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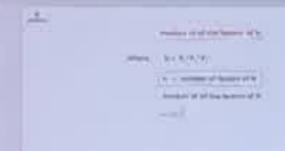
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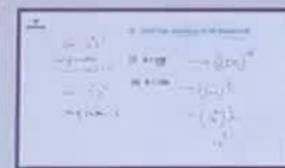
PRACTICE QUESTIONS



37



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PRACTICE
QUESTIONS

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For doing



For doing Factorization Fast

Tables (1-20)

Power of number

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For doing Factorization Fast

→ Tables (1-20)

→ Power of numbers

$$2^1 - 2^{10}$$

$$3^1 - 3^5$$

$$4^1 -$$

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For doing Factorization Fast

$$\rightarrow T = (1 - z_0)$$

\rightarrow of numbers

$$= 2^{10} \quad 5^1 - 5^1$$

$$6^1 - 6^1$$

$$7^1$$

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For doing Factorization Fast

→ Tables (1-20) + Squares (1-30)

→ Power of numbers

$$2^1 - 2^{10}$$

$$3^1 - 3^5$$

$$4^1 - 4^4$$

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For doing Factorization Fast

- Tables (1-20) → Squares (1-30)
- Power of numbers → Cubes (1-20)

$$\begin{array}{ccc} 2^1 - 2^{10} & 5^1 - 5^5 & 8^1 - 8^8 \\ 3^1 - 3^5 & 6^1 - 6^7 & 9^1 - 9^4 \\ 4^1 - 4^5 & 7^1 - 7^4 & \end{array}$$

cg

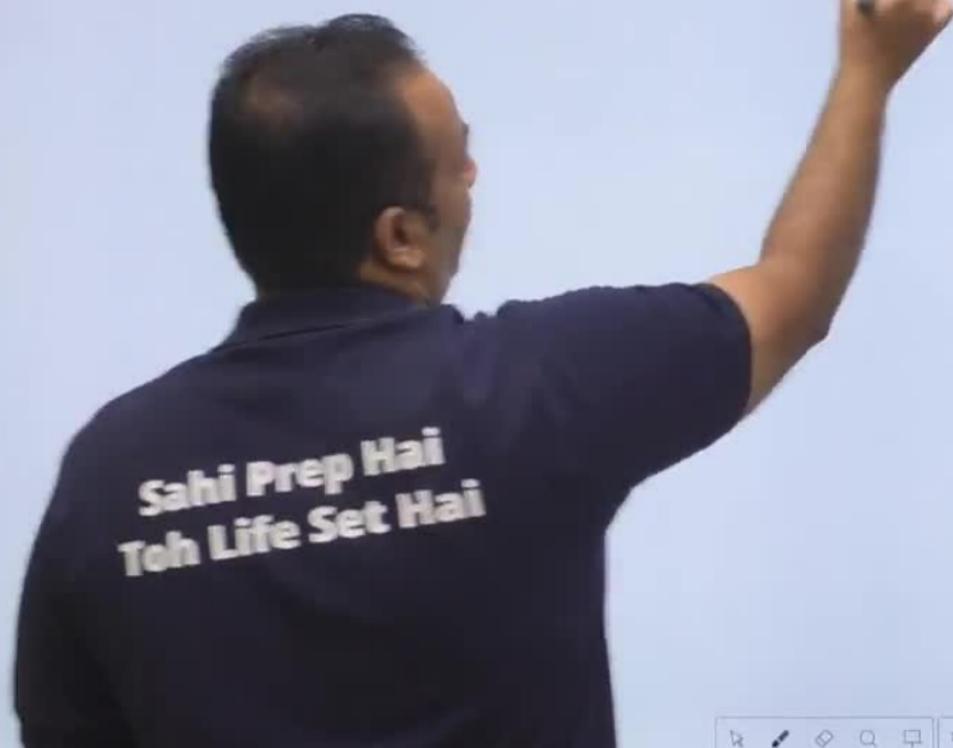
36°



Cg

$$36 \div = 2$$

5



Q

$$360^\circ \div = 2^2 \quad 5^2$$



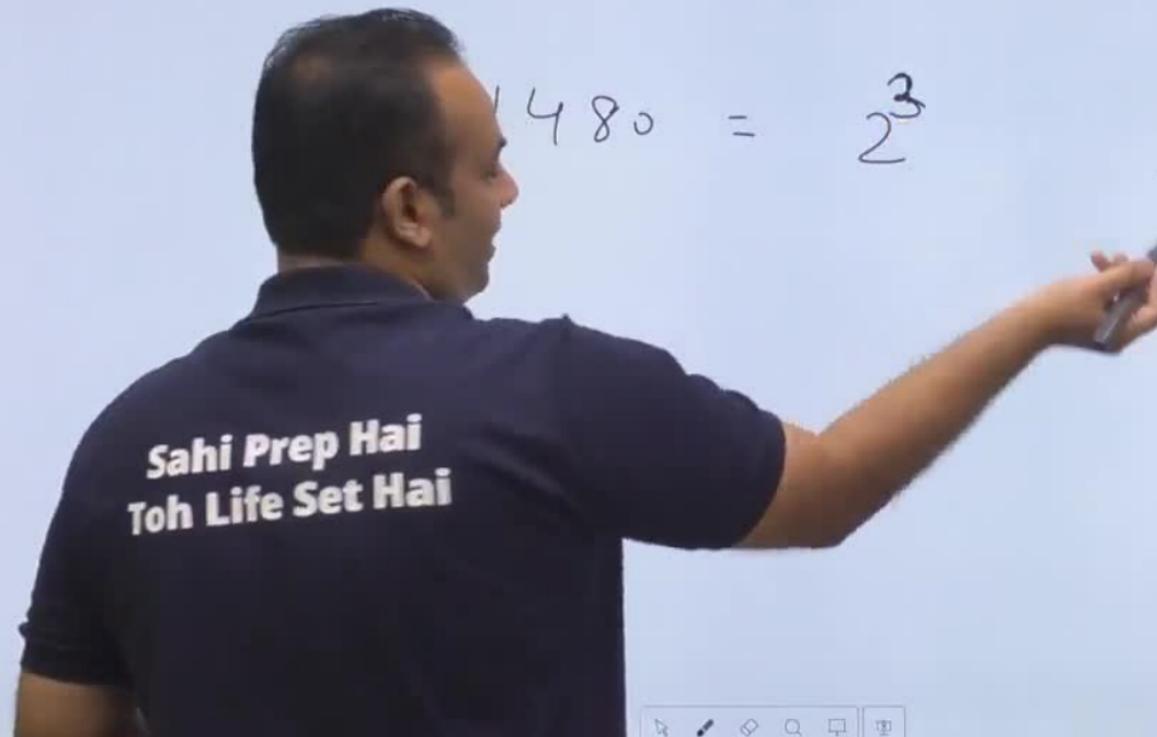
eg $360 = 2^4 \cdot 3^2 \cdot 5^2$

$$1480 = 2^2 \cdot 5^1$$

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Q9 $360^\circ = 2^4 \cdot 3^2 \cdot 5^2$

$$1480 = 2^3 \cdot 5^1$$

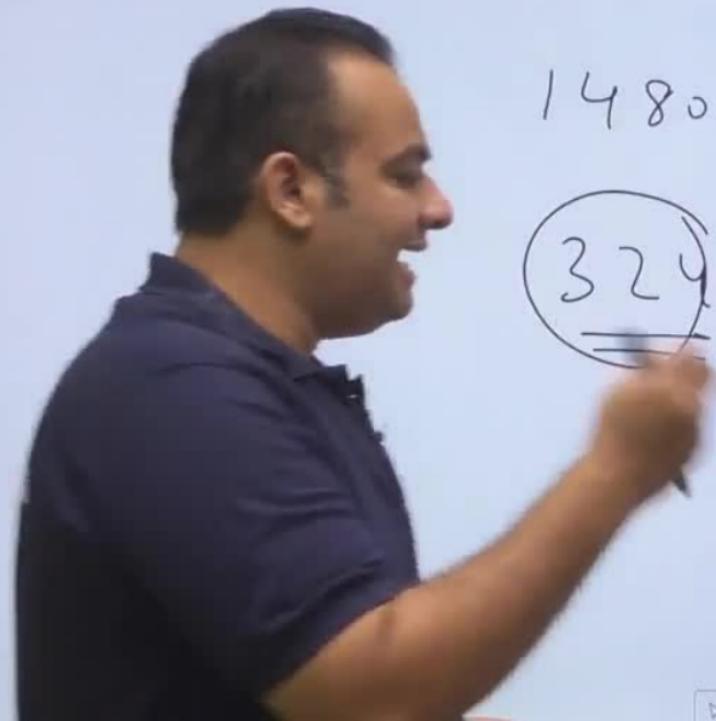


Q9

$$\textcircled{360}^{\circ} = 2^4 \cdot 3^2 \cdot 5^2$$

$$1480 = 2^3 \cdot 5^1 \cdot 37^1$$

$$\textcircled{324}^{\circ} = 2^4 \cdot 5^1$$



PRACTICE QUESTIONS





CONSECUTIVE INTEGERS

CONSECUTIVE INTEGERS



Consecutive Integers

If there are n consecutive integers then there must be exactly one integer which is completely divisible by n. If we take 3 consecutive integers, then there must be exactly one integer which is divisible by 3.

Example:

14, 15, 16

15 is divisible by 3

48, 49, 50

48 is divisible by 3

67, 68, 69

69 is divisible by 3

Consecutive Integers

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Example:



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Sahi Prep Hai
Teh Life Set Hai

Consecutive Integers

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**Sahi Prep Hai
Toh Life Set Hai**

Consecutive Integers

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Consecutive Integers

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Consecutive Integers

V Amp

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Example:

14, **15**, 16

15 is divisible by 3

48, 49, 50

48 is divisible by 3

67, 68, **69**

69 is divisible by 3

18, 19

99

15, **16**, 17, **18**

58, 59, 60, 61

Consecutive Integers

V Imp

If there are n consecutive integers then there must be exactly one integer which is completely divisible by n . If we take 3 consecutive integers, then there must be exactly one integer which is divisible by 3.

e:

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15 is divisible by 3

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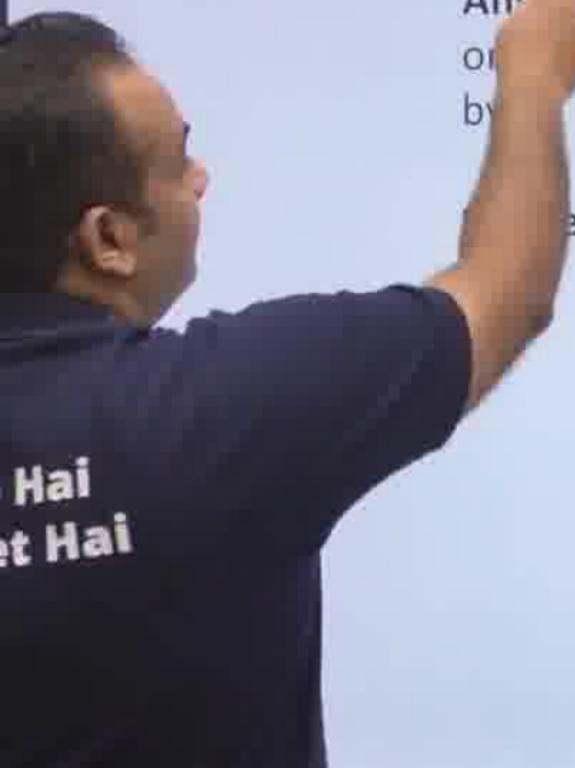
Sahi Prep Hai
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15, 16, 17, 18
58, 59, 60, 61

Q. The product of 3 consecutive natural numbers is always divisible by _____.

Ans. As in this question, there are 3 consecutive natural number so one number must be divisible by 3 and atleast one number is divisible by 2.

∴ The product of the numbers must be divisible by $3 \times 2 = 6$



Q. Find the largest natural number which completely divides the product of 4 consecutive natural numbers?

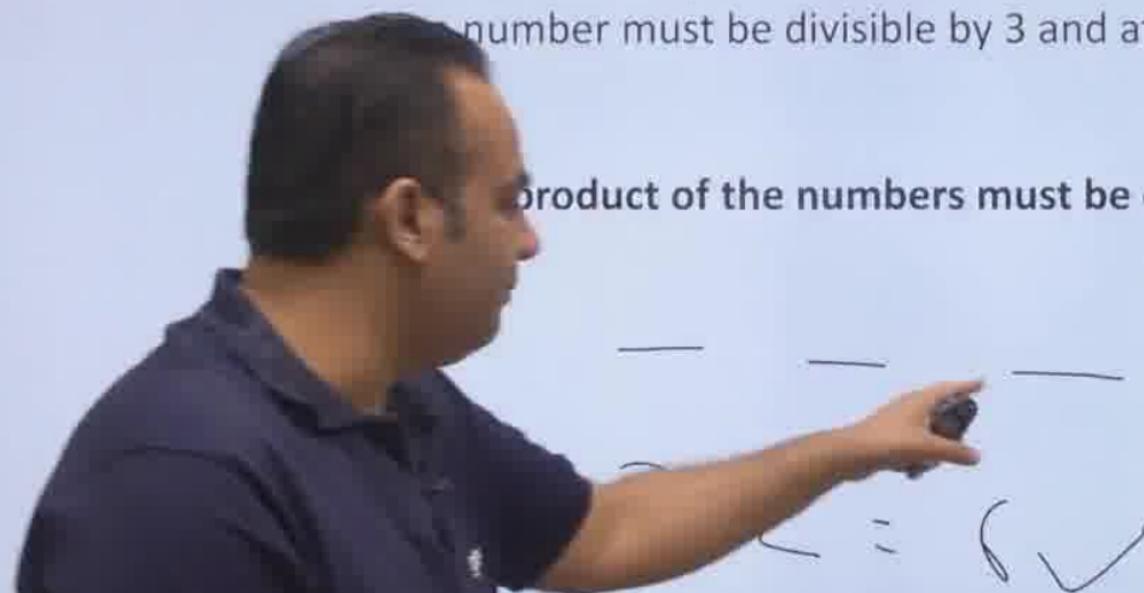
Ans: Let us take 4 consecutive natural numbers as $x, x+1, x+2, x+3$.
Out of these 4 numbers at least one is divisible by 3 and two must be even. As there are 2 consecutive even numbers, so one number out of them must be divisible by 4.

So we can say that the product of 4 consecutive natural numbers is divisible by $3 \times 2 \times 2 \times 2 = 24$

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Ans: As in this question, there are 3 consecutive natural number so one number must be divisible by 3 and atleast one number is divisible

product of the numbers must be divisible by $3 \times 2 = 6$

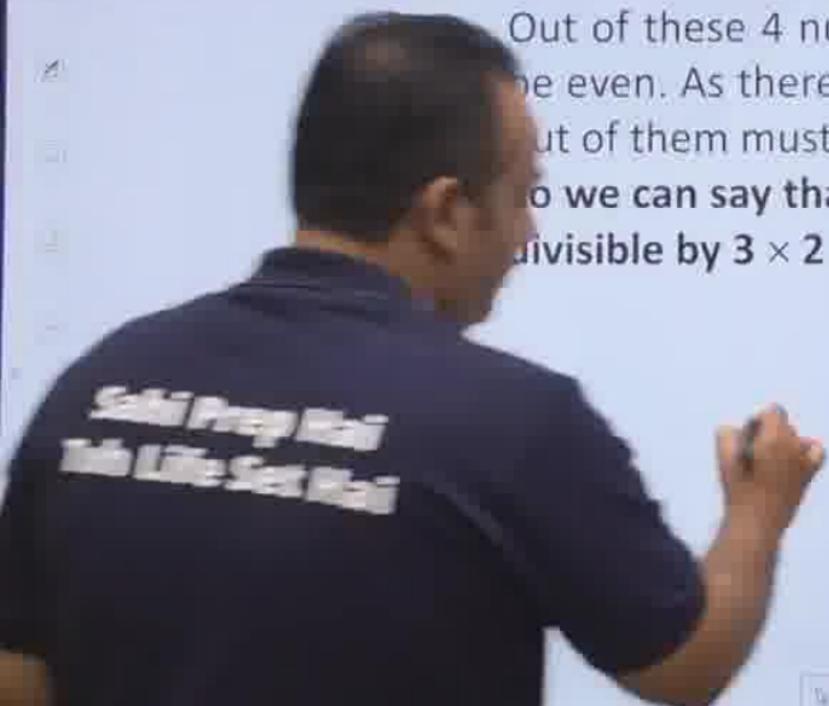


Q. Find the largest natural number which completely divides the product of 4 consecutive natural number ?

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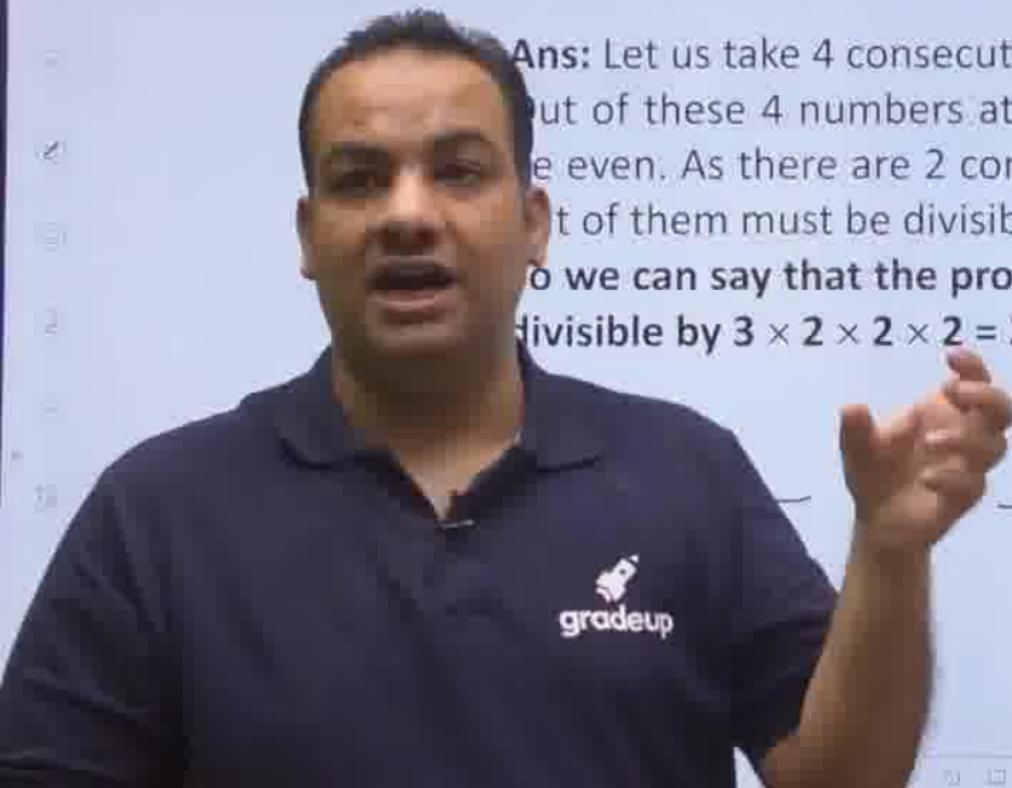
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Out of these 4 numbers atleast one is divisible by 3 and two must be even. As there are 2 consecutive even numbers, so one number out of them must be divisible by 4.

So we can say that the product of 4 consecutive natural number is divisible by $3 \times 2 \times 2 \times 2 = 24$



Q. Find the largest value of K which always divides $n(n^2 - 1)$ where n is a natural number.

Ans.

$$\begin{aligned}n(n^2 - 1) &= n(n - 1)(n + 1) \\&= (n - 1)(n)(n + 1)\end{aligned}$$

$n, (n-1), (n)$ and $(n+1)$ are three consecutive natural numbers so their product must be divisible by 6.



Q. Find the largest value of K which always divides $n(n^2 - 1)$ where n is a natural number.

Ans.

$$\begin{aligned}n(n^2 - 1) &= n(n - 1)(n + 1) \\&= (n - 1)(n)(n + 1)\end{aligned}$$

Now, $(n-1)$, (n) and $(n+1)$ are three consecutive natural numbers so their product must be divisible by 6.

Sahi Prep Hai
Toh Life Set Hai

1. If n is an integer, $(n^3 - n)$ is divisible by:

(A) 4

(B) 5

(C) 6

(D) 7

I

$$n = 1$$

$$1^3 - 1 = 0$$

$$n = 2$$

$$2^3 - 2 = 6$$

1. If n is an integer, $(n^3 - n)$ is divisible by:

(A) 4

(C) 6

(B) 5

(D) 7

$$n = 1$$

$$1^3 - 1 = 0$$

$$n = 2$$

$$2^3 - 2 = 6$$

II Concept

$$n(n^2 - 1)$$

$$n(n-1)(n+1)$$

$$\underline{(n-1)(n)(n+1)}$$

⑥

Ans. (C)

$$n^3 - n$$

$$= n(n^2 - 1)$$

$$= n(n - 1)(n + 1)$$

$$= (n - 1)(n)(n + 1)$$

As this is a product of 3 consecutive integers, so atleast one integer will be divisible by 2 and exactly one integer will be divisible by 3, so the product is divisible by 6.

OR

You can put values and eliminate the options.

2. Find the largest number which always divides the expression $(n^3-n)(n-2)$, where n is a natural number greater than 2?

- (A) 6
- (B) 12
- (C) 24
- (D) 48

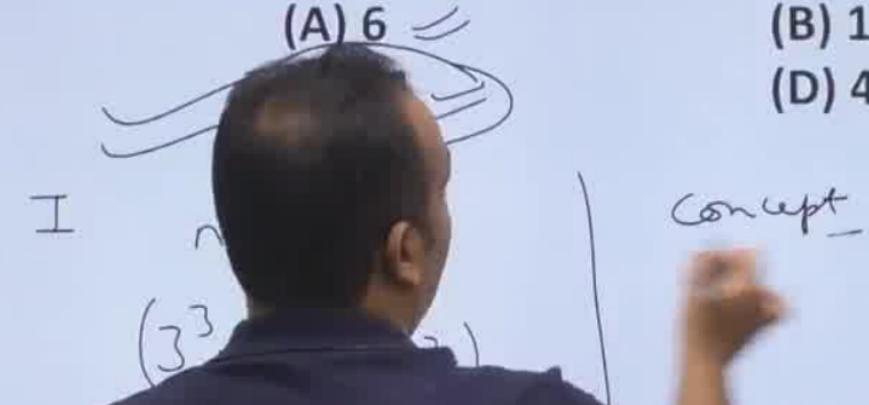


2. Find the largest number which always divides the expression $(n^3-n)(n-2)$, where n is a natural number greater than 2?

(A) 6

(B) 12

(D) 48



Sahi Prep Hai
Toh Life Set Hai

2. Find the largest number which always divides the expression $(n^3-n)(n-2)$, where n is a natural number greater than 2?

(A) 6

(C)

(B) 12

(D) 48

I

$$n = 3$$

$$(3^3 - 3)$$

=

Concept

$$n$$

Sahi Prep Hai
Toh Life Set Hai

2. Find the largest number which always divides the expression $(n^3-n)(n-2)$, where n is a natural number greater than 2?

(A) 6

24

(B) 12

48

I

$(n^3-n)(n-2)$

Concept

$(n^3-n)(n-2) \cap (n+1)$

*Sahi Prep Hai
Toh Life Set Hai*

2. Find the largest number which always divides the expression $(n^3-n)(n-2)$, where n is a natural number greater than 2?

(A) 6

(C) 24

(B) 12

(D) 48

I $n = 3$

$$(3^3 - 3)(3 - 2)$$

$$= 24$$

$$n = 4$$

$$60 - 2 = 12$$

concept

$$(n-2)(n-1) \quad n \quad (n+1)$$

$$\rightarrow 24$$

Ans. (C)

$$(n^3 - n) (n - 2)$$

$$= n(n^2 - 1)(n - 2)$$

$$= n(n - 1)(n + 1)(n - 2)$$

$$= (n - 2)(n - 1)(n)(n + 1)$$

Product of 4 consecutive integers is divisible by $1 \cdot 2 \cdot 3 \cdot 4 = 24$

OR

You can put values starting from $n = 3$

If $n = 3$

$$(27 - 3)(3 - 2) = 24 \text{ divisible by } 24$$

If $n = 4$

$$(60)(21) = 120 \text{ divisible by } 24$$

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

- (A) 16 (B) 12
(C) 10 (D) 8

$$n = 2$$

$$2^2(2^2 - 1)$$

Sahi Prep Hai
Toh Life Set Hai

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

(A) 16

(B) 12

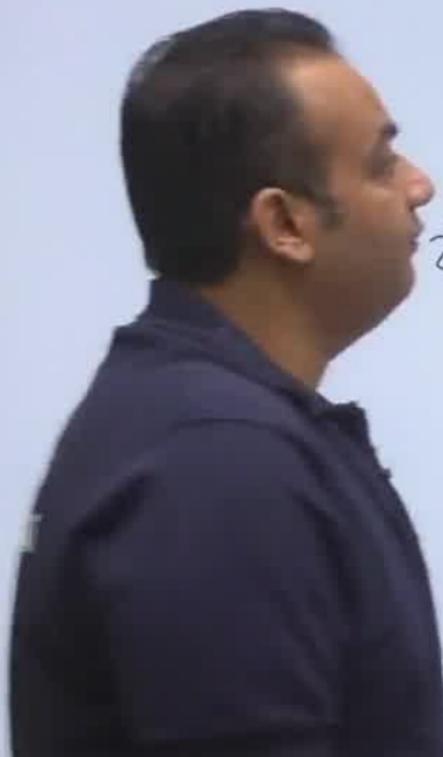
(C) 10

(D) 8

$$n = 2$$

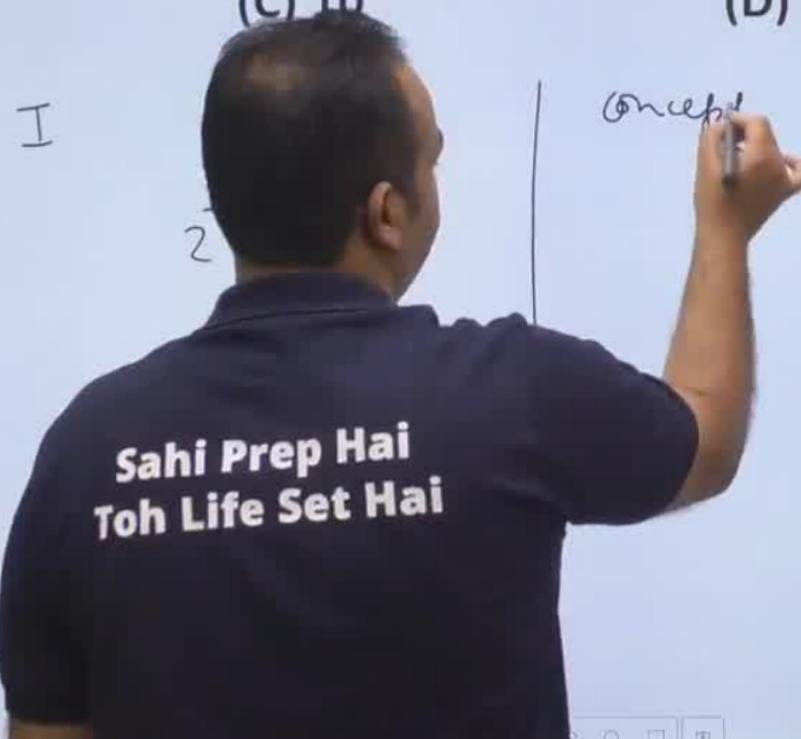
$$2^2(2^2-1)$$

$$= 12$$



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- (B) 12
- (C) 10
- (D) 8



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(B) 12

(C) 10

(D) 8

$$n = 2$$

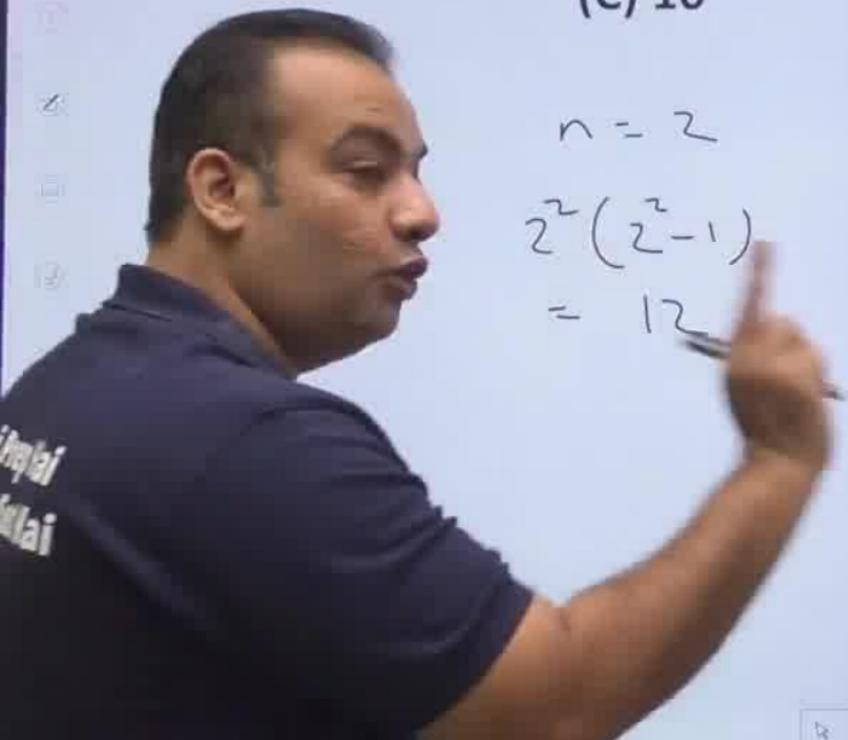
$$2^2(2^2-1)$$

$$= 12$$

concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot n \cdot (n+1) \right] n$$



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- (A) 16 (B) 12
(C) 10 (D) 8

I

 $n -$ 2^2 concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot n \cdot (n+1) \right] n$$

I $n \rightarrow$

Sahi Prep Hai
Toh Life Set Hai

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

- (A) 16 (B) 12
(C) 10 (D) 8

I

Concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot n \cdot (n+1) \right] n$$

I $n \rightarrow$ odd

II

Sahi Prep Hai
Toh Life Set Hai

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

- (A) 16 (B) 12
(C) 10 (D) 8

I

$$n = 3$$

$$2^2(2^2 - 1)$$

concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot n \cdot (n+1) \right] n$$

I $n \rightarrow$ odd $n \rightarrow$ even

Sahi Prep Hai
Toh Life Set Hai

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

- (A) 16
(C) 10

- (B) 12
(D) 8

I $n^2(n^2-1)$

concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot n \cdot (n+1) \right] n$$

I $n \rightarrow \text{odd}$

II $n \rightarrow \text{even}$

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

(A) 16

(B) 12

(C) 10

(D) 8

I

2

Sahi Prep Hai
Life Set Hai

Concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot n \cdot (n+1) \right] n$$

I $n \rightarrow$ odd

$n \rightarrow$ even

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

- (A) 16 (B) 12
(C) 10 (D) 8

$$= 2$$

$$(2^2 - 1)$$

$$= 12$$

concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot (n) \cdot (n+1) \right] n$$

I \rightarrow odd

$n \rightarrow$ even

Sahi Prep Hai
Toh Life Set Hai

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I

$$n = 2$$

concept

$$2^2(2^2 - 1)$$

$$= 12$$

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot n \cdot (n+1) \right] n$$

 \rightarrow odd \rightarrow 5

ex

Sahi Prep Mai
Toh Life Set Mai

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- (A) 16
(C) 10

- (B) 12
(D) 8

$$n = 2$$

$$(2^2 - 1)$$

$$= 12$$

concept

$$n \cdot n(n-1)(n+1)$$

$$\left[(n-1) \cdot \underbrace{n \cdot (n+1)}_{\text{odd}} \right] n$$

→ odd

$$6 \cdot 4 \rightarrow 24$$

∴ $n \rightarrow$ even

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- (A) 16 (B) 12
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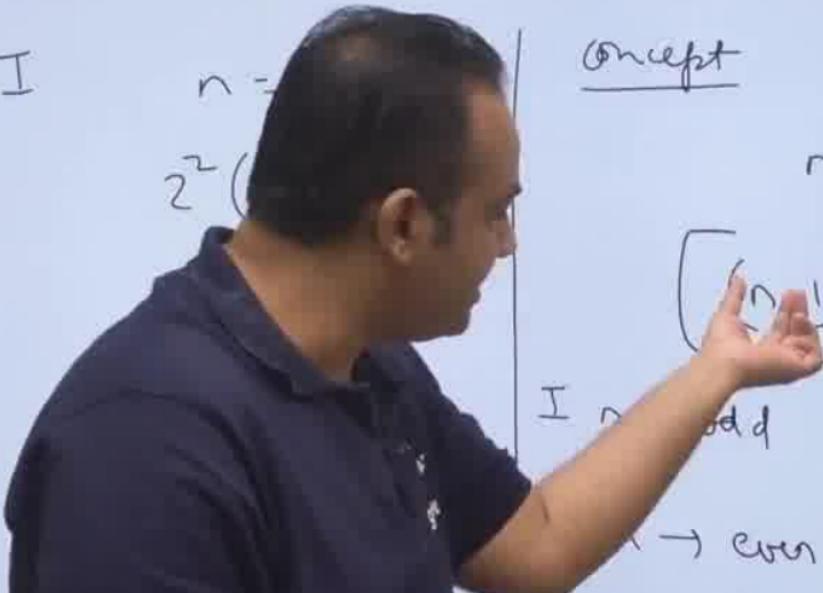
I $n =$ Concept

$2^2($ $n \cdot n(n-1)(n+1)$

$\left[(n-1) \cdot n \cdot (n+1) \right] n$

I n odd $6 \cdot 4 \rightarrow 24$

\rightarrow even



The image shows a man from the side, wearing a dark blue polo shirt, pointing his right index finger towards a whiteboard. On the whiteboard, there is handwritten mathematical notation and text. At the top left, it says 'I' followed by 'n ='. To the right of this, the word 'Concept' is underlined. Below 'n =' is the expression '2^2(' followed by a large bracket containing '(n-1) · n · (n+1)' with 'n' written below it. To the right of this bracketed expression is another 'n'. Below the main expression, the text 'I n odd' is written next to '6 · 4 → 24', where '24' is circled. At the bottom of the board, the word 'even' is written with an arrow pointing towards it.

3. If n is a natural number greater than 1 then $n^2(n^2 - 1)$ is, always divisible by which of the following?

(A) 16

(B) 12

(C) 10

(D) 8

I

$n = 2$

$$2^2(2^2 - 1)$$

$$= 12$$

upto

$$n \cdot n(n-1)(n+1)$$

$$\left[\underbrace{(n-1) \cdot n \cdot (n+1)}_{\text{n} \rightarrow \text{odd}} \right] n$$

\rightarrow odd

\rightarrow 24

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

(A) 16

(B) 12

(C) 10

(D) 8

$$n = 2$$

$$2^2(2^2 - 1)$$

$$= 12$$

concept

$$n \cdot n(n-1)(n+1)$$

$$\left[\underbrace{(n-1) \cdot n}_{\text{even}} \cdot (n+1) \right] n$$

I $n \rightarrow \text{odd}$

$$6 \cdot 4 \rightarrow 24$$

II $n \rightarrow \text{even}$

$$6 \cdot 2 = 12$$

3. If n is a natural number greater than 1 then $n^2(n^2-1)$ is, always divisible by which of the following?

- (A) 16
(C) 10

- (B) 12
(D) 8

I

concept

$$\begin{aligned}n \cdot n(n-1)(n+1) \\&\left[\underbrace{(n-1) \cdot n}_{\text{I } n \rightarrow \text{ odd}} \underbrace{(n+1)}_{\text{n}} \right] \\&6 \cdot 4 \rightarrow 24 \\&n \rightarrow \text{ even} \\&6 \cdot 2 = 12\end{aligned}$$

Ans. (B)

$$n^2(n^2 - 1)$$

$$= n^2(n - 1)(n + 1)$$

$$n \cdot (n - 1) \cdot (n) \cdot (n + 1)$$

As $n > 1$

Case I : When n is odd

$$n \cdot \boxed{(n - 1)(n)(n + 1)}$$

If n is odd we know that product of 3 consecutive integers is divisible by 6, but if n is odd then $(n - 1)$ and $(n+1)$ both are even, so we get one extra multiple of 2. So, product is divisible by 12.

Case II : If n is even

$$n \cdot \boxed{(n - 1)(n)(n + 1)}$$

$$2 \cdot 6 = 12$$

4. Find the largest natural number which always completely divides the product of four consecutive natural numbers.

(A) 6

(C) 24

(B) 12

(D) 120

The product of 4 consecutive integers is always divisible by 24

5. The difference between the squares of 2 consecutive odd integers is always divisible by ?

- (A) 3
(C) 7

- (B) 6
(D) 8

1 3

$3^2 - 1^2 = 8$

Step Hai
Set Hai

5. The difference between the squares of 2 consecutive odd integers is always divisible by ?

(A) 3

(C) 7

(B) 6

(D) 8

$$(1^2 - 3^2) = 1 - 9 = -8$$

$$(3^2 - 5^2) = 9 - 25 = -16$$

$$(5^2 - 7^2) = 25 - 49 = -24$$

Sahi Prep Hai
Toh Life Set Hai

5. The difference between the squares of 2 consecutive odd integers is always divisible by ?

(A) 3

(C) 7

(B) 6

(D) 8

I

II

$(2n+1), (2n+3)$

$2n+1$

*Sahi Prep Hai
Toh Life Set Hai*

5. The difference between the squares of 2 consecutive odd integers is always divisible by ?

- (A) 3
(C) 7

- (B) 6
(D) 8

I

$$1, 3$$

$$3^2 - 1^2$$

$$(2n+1), (2n+3)$$

$$3^2 - (2n+1)^2$$

*Sahi Prep Hai
Toh Life Set Hai*

5. The difference between the squares of 2 consecutive odd integers is always divisible by ?

- (A) 3
(C) 7

- (B) 6

I

1, 3

$$3^2 - 1^2 = 8$$

Sahi Prep Hai
Toh Life Set Hai

$(2n+1)$

$(2n+3)$

$(2n+1)^2$

$(4n^2 + 4n + 1)$

5. The difference between the squares of 2 consecutive odd integers is always divisible by ?

$$\begin{aligned} 3^2 - 3^2 \\ = 16 \end{aligned}$$

- (A) 3
- (B) 6
- (C) 7
- (D) 8

I

1, 3

$$3^2 - 1^2 = 8$$

$$(2n+1), (2n+3)$$

$$(2n+3)^2 - (2n+1)^2$$

$$(4n^2 + 12n + 9) - (4n^2 + 4n + 1)$$

$$= 8n + 8 \Rightarrow 8(n+1)$$

Ans: (D)

2 consecutive odd integers can be $(2x + 1)$ and $(2x - 1)$

$$(2x + 1)^2 - (2x - 1)^2$$

$$(4x^2 + 4x + 1) - (4x^2 - 4x + 1) = 8x$$

So difference between squares of 2 consecutive odd integers is always divisible by 8.

OR

You can eliminate options by putting values

Let, numbers are 3 and 1.

$$3^2 - 1^2 = 8$$

6. If a and b are two positive odd integers, then $(a^4 - b^4)$ is completely divisible by which of the following ?

- (A) 3
- (B) 6
- (C) 8
- (D) 12

Sahi Prep Hai
Toh Life Set Hai

Ans: (C)

$$a^4 - b^4$$

As a and b are odd numbers.

$$\begin{aligned}a^4 - b^4 &= (a^2 - b^2)(a^2 + b^2) \\&= (a - b)(a + b)(a^2 + b^2)\end{aligned}$$

↓ ↓ ↓
E E E
2 . . . 2

Sahi Prep Hai
Toh Life Set Hai

Ans: (C)

$$a^4 - b^4$$

As a and b are odd numbers.

$$\begin{aligned}a^4 - b^4 &= (a^2 - b^2)(a^2 + b^2) \\&= (a - b)(a + b)(a^2 + b^2) \\&\quad \downarrow \quad \downarrow \quad \downarrow \\&\quad E \quad E \quad E \\&\quad 2 \quad . \quad 2 \quad . \quad 2 \\&= 8\end{aligned}$$

7. If m and n are positive integers and $(m-n)$ is an even number, then (m^2-n^2) will always be divisible by ?

7. If m and n are positive integers and $(m-n)$ is an even number, then (m^2-n^2) will always be divisible by ?

$$5_1 \quad 1$$

$$5^2 - 1^2 = 24$$

$$5_1 \quad 3 \quad 16$$

$$5^2 - 3^2 = 16$$

- ~~(A) 4~~ ✓
~~(C) 8~~ ✓

- ~~(B) 6~~ ✓
~~(D) 12~~ ✓

$$4^2 - 2^2 \quad m - n = \underline{\text{even}}$$

$$= 12 \quad \underline{\text{odd} - \text{odd} = \text{even}}$$

$$\underline{\text{even} - \text{even} = \text{even}}$$



7. If m and n are positive integers and $(m-n)$ is an even number, then (m^2-n^2) will always be divisible by ?

$$5_1 \quad 1$$

$$5^2 - 1^2 = 24$$

$$5_1 \quad 3 \quad 16$$

$$5^2 - 3^2 = 16$$

~~(A) 4~~ ✓
~~(C) 8~~ ✓

~~(B) 6~~ ✓
~~(D) 12~~ ✓

$$4^2 - 2^2 \quad m - n = \underline{\text{even}}$$

$$= 12 \quad \underline{\text{odd} - \text{odd} = \text{even}}$$

$$\underline{\text{even} - \text{even} = \text{even}}$$



Ans: (A)

m and n are +ve integers.

$m - n = \text{Even number}$

It means,

I : m and n both are even.

II : m and n both are odd.

$$\text{Now } m^2 - n^2 = (m - n)(m + n)$$

$$\begin{matrix} & \downarrow & \downarrow \\ 2 & . & 2 \end{matrix}$$

$$= 4$$

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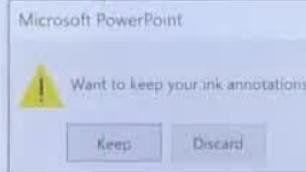
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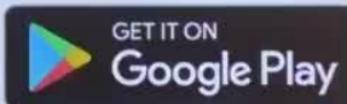
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↓ . ↓
2 . 2

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eg

o

cg



cg

c



Cg

$$n(n+1)(n+2)(n+3) + 24$$

is always

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eg

$$n(n+1)(n+2)(n+3) + 24$$

is always divisible by

(A)

(B)

6

-4

48

(C)

eg

$$n(n+1)(n+2)(n+3) + 24$$

always divisible by K
Find largest value of K

$$\underline{n=1}$$

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eg

$$n(n+1)(n+2)(n+3) + 24$$

is always divisible by K
Find largest value of K

$$\begin{array}{ll} n=1 & 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48 \\ n=2 & \end{array}$$

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eg

$$n(n+1)(n+2)(n+3) + 24$$

Always divisible by K
Find largest value of K

A $n=1 \quad 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$

B $n=2 \quad 2 \cdot 3 \cdot 4 \cdot 5$

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eg

$$n(n+1)(n+2)(n+3) + 24$$

is always divisible by K
Find largest value of K

$$6 \quad n=1 \quad 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

$$12 \quad n=2 \quad 2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

$$24 \quad n=3 \quad 3 \cdot 4 \cdot 5 \cdot 6 + 24 = 384$$

eg

$$n(n+1)(n+2)(n+3) + 24$$

always divisible by K
Find largest value of K

$$\underline{n=1} \quad 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

$$n=2 \quad 2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

$$n=3 \quad 3 \cdot 4 \cdot 5 \cdot 6 + 24 = 384$$

$$n=4 \quad 4 \cdot 5 \cdot 6 \cdot 7 + 24 = 864$$

$$n=5 \quad 5 \cdot 6 \cdot 7 \cdot 8$$

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eg

$$n(n+1)(n+2)(n+3) + 24$$

is always divisible by K
Find largest value of K

(A)

$$n=1 \quad 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

(D)

$$n=2 \quad 2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

$$n=3 \quad 3 \cdot 4 \cdot 5 \cdot 6 + 24 = 384$$

$$n=4 \quad 4 \cdot 5 \cdot 6 \cdot 7 + 24 = 864$$

$$5 \cdot 6 \cdot 7 \cdot 8$$

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eg

$$n(n+1)(n+2)(n+3) + 24$$

b always divisible by K
Find largest value of K

(A)

6

n=1

$$1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

(B)

12

n=2

$$2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

(C)

24

n=3

$$3 \cdot 4 \cdot 5 \cdot 6 + 24 = 384$$

(D)

48

n=4

$$4 \cdot 5 \cdot 6 \cdot 7 + 24 = 864$$

n=5

$$5 \cdot 6 \cdot 7 \cdot 8 + 24 = 1704$$

24

eg

$$\boxed{n(n+1)(n+2)(n+3)} + 24$$

is always divisible by K

Find largest value of K

$$n=1 \quad 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

$$n=2 \quad 2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

$$n=3 \quad 3 \cdot 4 \cdot 5 \cdot 6 + 24 = 384$$

$$n=4 \quad 4 \cdot 5 \cdot 6 \cdot 7 + 24 = 864$$

$$n=5 \quad 5 \cdot 6 \cdot 7 \cdot 8 + 24 = 1704$$

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24

48

24n + 24

eg

$$\boxed{n(n+1)(n+2)(n+3)} + 24$$

is always divisible by K
Find largest value of K

$$n=1 \quad 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

$$n=2 \quad 2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

$$n=3 \quad 3 \cdot 4 \cdot 5 \cdot 6 + 24 = 384$$

$$n=4 \quad 4 \cdot 5 \cdot 6 \cdot 7 + 24 = 864$$

$$n=5 \quad 5 \cdot 6 \cdot 7 \cdot 8 + 24 = 1704$$

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24

48

$$24n + 24 = \cancel{24}(x+1)$$

eg

$$\boxed{n(n+1)(n+2)(n+3)} + 24$$

b) always divisible by K
Find largest value of K

$$6 \quad \underline{n=1} \quad 1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

$$12 \quad n=2 \quad 2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

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$$n=5 \quad 5 \cdot 6 \cdot 7 \cdot 8 + 24 = \textcircled{1704}$$

$$24n + 24 = \cancel{24}(n+1)$$

eg

$$\boxed{n(n+1)(n+2)(n+3)} + 24$$

b) always divisible by K
 Find largest value of K

(A)

6

 $n=1$

$$1 \cdot 2 \cdot 3 \cdot 4 + 24 = 48$$

(B)

12

 $n=2$

$$2 \cdot 3 \cdot 4 \cdot 5 + 24 = 144$$

~~(C)~~

24

 $n=3$

$$3 \cdot 4 \cdot 5 \cdot 6 + 24 = 384$$

(D)

48

 $n=4$

$$4 \cdot 5 \cdot 6 \cdot 7 + 24 = 864$$

 $n=5$

$$5 \cdot 6 \cdot 7 \cdot 8 + 24 = \textcircled{1704}$$