

PERCENTAGES

$$\begin{aligned} 24\% \text{ of } 50 &= 12 \\ = 50\% \text{ of } 24 &= 12 \\ \hline A\% \text{ of } B &= B\% \text{ of } A \end{aligned}$$

$$\begin{aligned} 10\% \text{ of } 7432 &= 743.2 \\ 1\% \text{ of } 7432 &= 74.32 \\ 50\% \text{ of } 7432 &= 3716 \end{aligned}$$

When the no is increased by 20% of itself, the result is 480.
Find the number.

Sol:

$$\begin{array}{lcl} 120\% & \longrightarrow & 480 \\ 100\% & \longrightarrow & ? \end{array}$$

x4

400

If 40% of a number is 20 more than 30% of a number, find the number?

$$\begin{array}{l} \text{Diff b/w } 40\% \text{ \& } 30\% \longrightarrow 20 \\ 40\% - 30\% \Rightarrow 10\% \xrightarrow{\times 2} 20 \\ \text{Number} = \frac{20}{10\%} \xrightarrow{\times 10} 200 \end{array}$$

'A' won the election by a majority of 150 votes. If only two candidates contested, & 'A' secured 60% of total votes, find the total no of votes?

Sol :

A	→	60%
- B	→	40%
<hr/>		
Majority	→	20% — 150 votes
Total	→	100% — <u>750</u> votes

$\frac{150 \times 5}{20} = 750$

Price of Sugar first increased by 30% & then decreased by 30%. Find the original price if present price is Rs 273.

100%	91%	↓
+ 30 (30% of 100)	10%	1%
130%	20%	4%
- 39 (30% of 130)	30%	9%
91%	40%	16%
→ × 3	50%	25%
273	100%	
→ × 3		
819		

Original Price = $\frac{273 \times 100}{91} = 300$

Dec & Inc
Inc & Dec

↓↑ / ↑↓
10%

20%

30%

40%

50%

15%

12%

5%

Dec

↓

1%

4%

9%

16%

25%

2.25%

1.44%

0.25%

$(1.0)^2$

↑↑

10%.

20%.

30%.

↑

21%.

44%.

69%.

$$\rightarrow 10+10+1$$

$$\rightarrow 20+20+4$$

$$\rightarrow 30+30+9$$

$$10+10+(1.0)^2$$

$$20+20+(2.0)^2$$

$$30+30+(3.0)^2$$

$$40\% \rightarrow 40+40+4.0^2 = 40+40+16 = 96\%$$

$$14\% \rightarrow 14+14+(1.4)^2 = 14+14+1.96 = 29.96\%$$

$$12\% \rightarrow 12+12+1.2^2 = 25.44\%$$

$$5\% \rightarrow 5+5+0.5^2 = 10.25\%$$

$$3\% \rightarrow 3+3+0.3^2 = 6.09\%$$

$$\begin{array}{r} 0.3 \\ \times 0.3 \\ \hline 0.09 \end{array}$$

$$\begin{array}{lcl}
 \downarrow & \downarrow & \rightarrow 10+10-(1.0) \\
 10\% & 19\% & - 20+20-(2.0)^2 \\
 20\% & 36\% & \rightarrow 30+30-(3.0)^2 \\
 30\% & 51\% & - 5+5-(0.5)^2 \\
 5\% & 7.75\% & - 12+12-(1.2)^2 \\
 12\% & 22.56\% &
 \end{array}$$

$$\begin{array}{r}
 100 \\
 - 10 \\
 \hline
 90 \\
 - 9 \\
 \hline
 81
 \end{array}
 \rightarrow 19\%$$

Percentages

If the area of a square becomes 3380 sq units after the side of the square increases by 30%. Find the Original Area ? (100%) — ?

Side $\rightarrow 30\% \uparrow$

Area $\rightarrow 30+30+9 \rightarrow 30+30+9 = 69\% \uparrow$

Old Area — 100%

Area incre — 69%

New Arc — 169%

$$\begin{array}{rcl}
 & \times 20 & \\
 169\% & \rightarrow & 3380 \\
 100\% & \rightarrow & ? (2000) \text{ sq units} \\
 & \times 2 &
 \end{array}$$

Percentages

$R = 5\% \uparrow$
 N.A \rightarrow 441 Sav units
 O.A \rightarrow ? 400 Sav

$A \uparrow \rightarrow 5 + 5 + 0.25$
 $\rightarrow 5 + 5 + 0.25$

$\rightarrow 10.25\%$
 N.A $\rightarrow 100 + 10.25 = 110.25\%$

Information
 N.A $\rightarrow 110.25\%$ — 441
 O.A $\rightarrow 100\%$ — ?
 Question

$$\frac{441 \times 100}{110.25} \times \frac{100}{100} = \frac{441 \times 100 \times 100}{110.25 \times 100} = \frac{441 \times 100}{110.25} = 400$$

$\Rightarrow 400 \text{ Sav units}$

8. Surya spends 60% of his salary on food. 20% of Remaining on Petrol. 10% of the remaining on Entertainment & saves the remaining amount. If he saves Rs 288, find his Salary?

Sol:

Salary — 100% — ?
 Food — 60% (60% of 100) — Food
 Rem — 40%
 Petrol — 8% (20% of 40) — Petrol
 Rem — 32%
 Ent — 3.2% (10% of 32) — Ent
 Sav — 28.8% — 288/-

$$\text{Sav} = 28.8\% = 288$$

$$\text{Sal} = 100\% = ?$$

$$\frac{10}{288 \times 100} \times \frac{100}{100} = \frac{1000}{288} = 1000/-$$

Percentages

8. In a Library, 40% of books are in English. 20% of remaining are in Hindi. 60% of the remaining are in Telugu & the remaining 7200 books are in other languages. Find the total no. of books in the Library?

Sol:

Total — 100%
 Eng — 40% (40% of 100)
 Rem — 60%
 Hindi — 12% (20% of 60)
 Rem — 48%
 Tel — 28.8% (60% of 48)
 Rem — 19.2% — other lang

other lang. 19.2% — 7200

$$\text{Total} = 100\% = ?$$

$$\frac{7200 \times 100}{19.2} \times \frac{10}{10} = \frac{7200 \times 100 \times 10}{19.2 \times 10} = \frac{7200 \times 100}{19.2} = 37500$$

Total — 37500

Percentages

- Q In a Library, ~~40%~~ of books are in English 20% of remaining are in Hindi. ~~60%~~ of the remaining are in Telugu & the remaining 7200 books are in other languages. Find the total no. of books in the Library? Big No \rightarrow Small No.

Sol: ~~11111~~

Sequence is Not imp
* $5 \div 5 = 0.5^2$
 $40\% \div 40 = 4^2$
 $20\% \div 20 = 2^2$
 $30\% \div 30 = 3^2$
 $13\% \div 13 = 1.3^2$

$$\begin{array}{r} 100 \\ - 60 \text{ (60\% of 100)} \\ \hline 40 \\ - 16 \text{ (40\% of 40)} \\ \hline 24 \\ - 4.8 \text{ (20\% of 24)} \\ \hline 19.2\% \end{array}$$

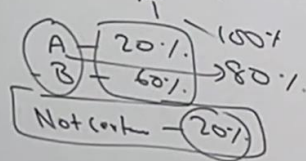
other lang. 19.2% 7200

Total $100\% = ?$

$$\frac{7200 \times 100}{19.2} \times \frac{10}{10} = \frac{30025 \times 7200 \times 100}{192}$$

Total $= \frac{75000}{2} = 37500$

- Q In a market survey, 20% opted for product A whereas 60% opted for Product B. The remaining individuals were not certain. If the difference b/w those who opted for product B & those who were not certain was 720, how many individuals were covered in the survey? (100%)



B - 60%
N.C - 20%

$$\begin{array}{r} \text{Diff} - 40\% - 720 \\ \hline 100\% = ? \end{array}$$

40% 720

100% = ?

$$\frac{180}{720 \times 100} \times 720 = 1800$$

Percentages

In a competitive Exam in state A, 6% got selected for appointment. State B had equal no. of candidates appeared as 7% got selected with 80 more candidates got selected than A. What was the no. of candidates appeared for each state?

$$\begin{array}{rcl} 7\% - 6\% & \rightarrow & 1\% \quad \times 80 \\ 100\% & \times 80 & \underline{\underline{8000}} \end{array}$$

Percentages

Q In an election b/w two candidates, one got 55% of total valid votes. 20% of the votes were invalid. Total no. of votes were 7500. The no. of valid votes that the other candidate got?

$$\begin{array}{l} A - 55\% \quad \times \\ B - 45\% \text{ of valid votes } 80\% \end{array}$$

$$B \rightarrow 45\% \text{ of } 80 \rightarrow 36\% \text{ of } 7500 = 2700$$

$$\begin{array}{r} 40\% - 3000 \\ - 4\% - 300 \\ \hline 36\% - 2700 \end{array}$$

- ① A is what % of B
A is 75% of B

$$\frac{A}{B} \times 100$$

$$\frac{360}{480} \times 100 = 75\%$$

- ② B is what % of A
B is 133.33% of A

$$\frac{B}{A} \times 100$$

$$\frac{480}{360} \times 100 = \frac{4}{3} \times 100 = 100\% + 33.33\%$$

$$\Rightarrow 133.33\%$$

- ③ A is how much % less than B

Sol A is 25% less than B

$$\frac{\text{Diff}}{B} \times 100 = \frac{80-60}{80} \times 100$$

$$= \frac{20}{80} \times 100$$

$$= 25\%$$

(4) B is how much % more than A
 B is 33.33% more than A

$$\frac{Dif}{A} \times 100 = \frac{80-60}{60} \times 100 = \frac{20}{60} \times 100 = 33.33\%$$

$$= \frac{20}{480} \times 100 = 25\%$$

A's salary is 80% more than B
 B's salary is ?% less than A

Sol

$$\frac{80}{100+80} \times 100 = \frac{80}{180} \times 100 = 44.44\%$$

$\Rightarrow 44\frac{4}{9}\%$ less

Salary of A increased by 20%. By what % should the salary get decreased so that his salary would come back to the original salary.

100 \rightarrow 120 \rightarrow 100

$$\frac{20}{120} \times 100 = 16.66\%$$

(or)
 $16\frac{2}{3}\%$

Salary of A decreased by 40%. By what % should the salary get increased so that his salary would come back to the original salary.

$100 \rightarrow 60 \rightarrow 100$

$$\frac{40}{60} \times 100 = 66.66\%$$

or

$$\underline{\underline{66\frac{2}{3}\%}}$$

$$\frac{\overset{2}{40}}{\underset{3}{60}} \times 100 = 66.66\% \text{ or } \underline{\underline{66\frac{2}{3}\%}}$$

Price of Sugar increased by 40%. By what % should the family reduce the consumption of Sugar so that the expenditure on Sugar remains same.

$A = L \times B$
 $R = P \times S$

$E = P \times C$

$100 - 140 - 100$

240×100
 7142

$= 28.57\%$

$E = 100 \times 100 = 10000$

$140 \times ? = 10000$

$x = \frac{10000}{140} = \frac{5}{7} \times 100 = 71.42\%$

$100 - 71.42 = 28.58$

$$E = P \times C$$

28.581

$$\begin{array}{r} 100.00 \\ 71.42 \\ \hline 28.58 \end{array}$$

$$x = \frac{500}{1400} = \frac{5}{14} \times 100 = 71.42\%$$

$$= 28.57\%$$

Present population of a town is 62500. Due to migration to big cities, it decreases every year by 4%. Find the population of town after 2 years.

1 st year	$\begin{array}{r} 62500 \\ - 2500 \\ \hline 60000 \end{array}$	(4% of 62500)
2 nd year	$\begin{array}{r} 60000 \\ - 2400 \\ \hline 57600 \end{array}$	(4% of 60000)
	<u>57600</u>	

$$\begin{array}{r} 62500 \\ 1^{\text{st}} \text{ year} \quad - 2500 \quad (4\% \text{ of } 62500) \\ \hline 60000 \\ 2^{\text{nd}} \text{ year} \quad - 2400 \quad (4\% \text{ of } 60000) \\ \hline 57600 \\ \hline \end{array}$$

A student has to score 33% marks to pass. He got 90 but failed by 9 marks. Find Max marks.

Pass % = 33%
 Pass marks = 90 + 9

	→ ×3
33% — 99 marks	
100% — ? <u>300 marks</u>	
	×3

$\longrightarrow x^3$

100% _____ ? 300 marks
_____ $\times 3$

In an exam, it is required to get 55% to pass. A student got 520 marks & declared as failed by 5%.

Find max marks. (100%)

Sol:

$$\begin{array}{rcl} 50\% & \longrightarrow & 520 \\ 100\% & \longrightarrow & ? \end{array} \quad \begin{array}{l} \times 2 \\ \times 2 \end{array}$$

max \longrightarrow 1040

Abhinav got 38% & failed by 14 marks.
Ravi got 43%, which is 21 marks more than pass mark.

Find pass % & max marks.

$$\begin{array}{rcl} (43\% - 38\%) & \longrightarrow & 5\% \\ 5\% & \longrightarrow & 35 \text{ marks} \\ 100\% & \longrightarrow & 700 \text{ marks} \end{array} \quad \begin{array}{l} \% \text{ dif} \\ \times 7 \\ \times 7 \end{array}$$

$$21 - (-14) = 21 + 14 = 35 \text{ marks}$$

100 marks

$$\begin{array}{rcl} (21 - (-14)) & \text{You} & 86 \\ & \text{Me} & 121 \end{array}$$

$$\text{Diff} = 35$$

$$\text{Abhinav} \rightarrow 38\% + 14 \text{ marks} \rightarrow \text{Pass \%}$$

$$\rightarrow 38\% + 2\% \rightarrow 40\%$$

$$\text{Ravi} \rightarrow 43\% - 21 \text{ marks} \rightarrow \text{Pass \%}$$

$$43\% - 3\% \rightarrow 40\%$$

$$\begin{array}{rcl} 700 - 100\% & & 146 \times 2 \\ 14 & \longrightarrow & ? 2\% \\ 21 & \longrightarrow & ? \end{array} \quad \begin{array}{l} 146 \times 2 \\ 700 \\ 168 \times 2 \\ 700 \end{array}$$

Y. Pathan Scored 120 Runs which included 3 Fours & 8 Sixes.
Find the (%) of Runs he scored by running b/w the wickets.

$$3 \times 4 = 12$$

$$8 \times 6 = 48$$

$$\text{Total} = 120 = 60 \text{ (Batsman)}$$

$$= \frac{60}{120} \times 100 = \underline{50\%}$$

If Numerator is increased by 20% & denominator decreased by 10% the resultant fraction is $\frac{16}{21}$. Find original fraction.

$$\frac{4 \cancel{12} \times \cancel{8} x}{3 \cancel{9} \times \cancel{6} y} = \frac{16}{21}$$

$$\frac{4x}{3y} = \frac{16}{21} \Rightarrow \frac{x}{y} = \frac{4 \times 3}{21 \times 4} = \frac{4}{7}$$

(Percentages)

** A man ^{G.P} Spends 75% of his income. His income increased by 20% & he increased his expenditure by 10%. Find the % change in his savings.

Sol :

$$\begin{array}{rcl} I - E & = & S \\ \text{original} \rightarrow 100 - 75 & = & 25 \\ \text{New} \rightarrow 120 - 82.5 & = & 37.5 \end{array}$$

$$10\% \text{ of } 75 = 7.5$$

$$\begin{array}{r} \text{Exp} \rightarrow 75 \\ 7.5 \quad (10\% \text{ of } 75) \\ \hline \text{NE} = 82.5\% \end{array}$$

$$\begin{array}{r} \text{Diff} \\ \hline \text{Org Sav} \end{array} \times 100 = \frac{12.5}{25} \times 100 = 50\%$$

A man ^{Exp} spends 60% of his income. His income increased by 40% & he increased his expenditure by 50%. Find the % change in his savings.

	Inc	-	Exp	=	Sav	
Original	100	-	60	=	40	
New	140	-	90	=	50	

$$\frac{10}{40} \times 100 = 25\%$$

$$\begin{array}{r} 0.76 \\ \text{Inc} \quad 60 \\ + 30 \text{ (50\% of 60)} \\ \hline \text{New} \quad 90\% \end{array}$$

Percentages

In an exam, there were 2000 candidates out of which 900 were boys. If 32% of the boys passed & 38% of girls passed. Find the % of failed candidates.

	Boys	900	Fail	68% of 900 → 612
	Girls	1100		62% of 1100 → 682
			Failed	→ 1294

$$\begin{array}{r} 647 \\ + 297 \\ \hline 944 \\ \times 100 \\ \hline 10 \end{array}$$

$$= 64.7\%$$

Two numbers are 20% & 30% of third number. How much % of first number is second number.

A	B	C
20	30	100

$$\frac{30}{20} \times 100 = 150\%$$

There are three numbers of which first no is 40% more than second no. & second no is 20% more than third. How much % of the third no is the first.

A	B	C
168	120	100

$$\frac{168}{100} \times 100 = 168\%$$

$$\begin{array}{r} C \quad 100 \\ + 20 \text{ (20\% of 100)} \\ \hline B \quad 120 \\ + 48 \text{ (40\% of 120)} \\ \hline A \quad 168 \end{array}$$

Of the three numbers, the first no is 25% less than second no & the second no is 60% more than the third. By how much % is the first no more or less than the third no.

C —	100	
	+ 60 (60% of 100)	
B —	160	
	- 40 (25% of 160)	
A —	120	

A
120

B
160

C
100

$$\frac{20}{100} \times 100$$

+ 20% more

The production of a company is decreased by 10% & then increased by 30%. Find the % change.

17%
inc

$$\begin{array}{r} 100\% \\ - 10 \text{ (10\% of 100)} \\ \hline 90 \\ + 27 \text{ (30\% of 90)} \\ \hline 117\% \end{array}$$

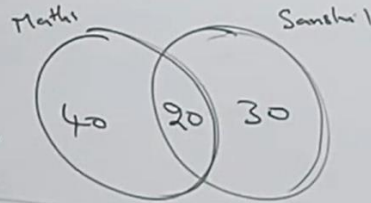
Length increased by 60%. Breadth decreased by 20%. Find % change in Area.

28% inc

$$\begin{array}{r} 100\% \\ + 60 \text{ (60\% of 100)} \\ \hline 160 \\ - 32 \text{ (20\% of 160)} \\ \hline 128\% \end{array}$$

In a college, 40% of students pass in mathematics.
 50% of students pass in Sanskrit. But 20% fail in both.
 Find % of students passed in both.

Fail
 only M - 40
 only S - 30
 Both - 20
 100 - 90

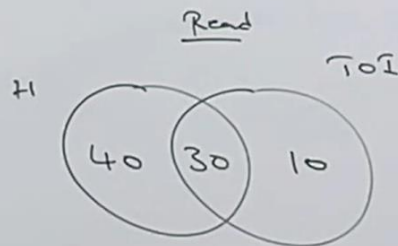


	P	F
M	40%	60%
S	50%	50%

\Rightarrow 10% passed in both

Percentages

In a town, 70% of citizens read Hindu. 40% read TOI
 & 30% read both. Find % of citizens who read neither.

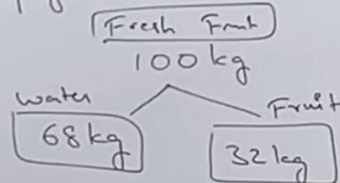


H B TOI
 40 + 30 + 10
 = 80%

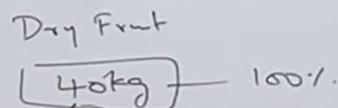
100 - 80% = 20%
 neither

Percentages

Fresh fruit contains 68% water & dry fruit contains 20% water.
 How much dry fruit can be obtained from 100 kg of fresh fruit.



80% — 32 kg
 100% — ?



$$\frac{4}{32 \times 100} = 40 \text{ kg}$$