Lecture Speech and Audio Signal Processing



Lecture 5: Noise reduction & Dereverberation



Content

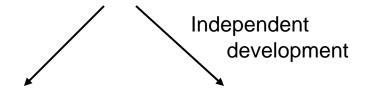


- Wiener filter
- Realization in the frequency domain
- Extensions of the basic approach
- Modified noise reduction procedure
- Dereverberation

Setup



Design of filters by means of minimizing the squared error (according to Gauß)



1941: A. Kolmogoroff: Interpolation und Extrapolation von stationären zufälligen Folgen, Izv. Akad. Nauk SSSR Ser. Mat. 5, pp. 3 – 14, 1941 (in Russian)

1942: N. Wiener: The Extrapolation, Interpolation, and Smoothing of Stationary Time Series with Engineering Applications, J. Wiley, New York, USA, 1949 (originally published in 1942 as MIT Radiation Laboratory Report)

Assumptions & Design criteria:

- ☐ One Wiener filter application: Separate a desired signal from an additive noise.
- ☐ The desired signal (typically speech) and noise are modeled as random processes.
- ☐ The filter is designed based on statistical properties up to the second order for speech and noise.

Literature



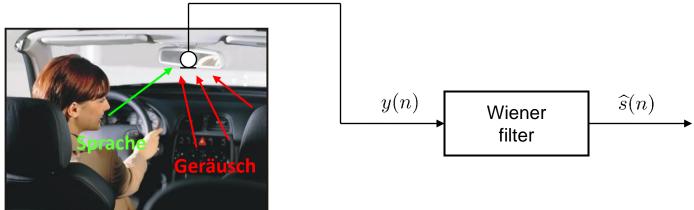
Basics of the Wiener filter:

- E. Hänsler / G. Schmidt: Acoustic Echo and Noise Control Kapitel 5 (Wiener Filter), Wiley, 2004
- E. Hänsler: Statistische Signale: Grundlagen und Anwendungen Kapitel 8 (Optimalfilter nach Wiener und Kolmogoroff), Springer, 2001
- M. S.Hayes: Statistical Digital Signal Processing and Modeling Kapitel 7 (Wiener Filtering), Wiley, 1996
- S. Haykin: Adaptive Filter Theory − Kapitel 2 (Wiener Filters), Prentice Hall, 2002

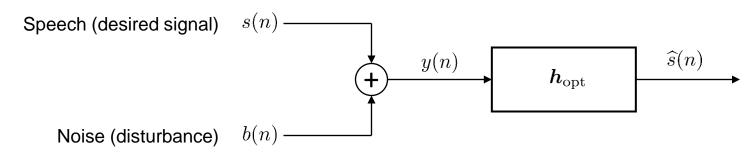
The Wiener filter – a noise reduction application example



Application:

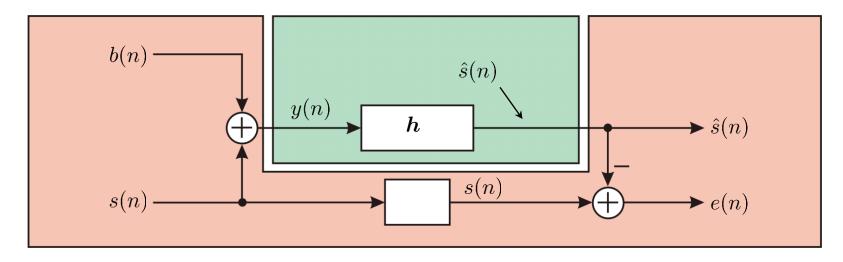


Model:





Structure in the time domain:



FIR filter structure:

$$\hat{s}(n) = \sum_{i=0}^{N-1} h_i y(n-i)$$

Optimization criterion:

$$E\{e^2(n)\} \xrightarrow[h_i=h_{i,\text{opt}}]{} \min$$



Further assumptions:

 $lue{}$ The target signal s(n) and the noise b(n) are zero-mean and uncorrelated, i.e. orthogonal:

$$m_s = m_b = 0, \ r_{sb}(l) = m_s \cdot m_b = 0$$

Calculation of the optimum filter coefficients:

$$\mathrm{E}\{e^2(n)\} \underset{h_i = h_{i,\mathrm{opt}}}{\longrightarrow} \min$$

$$\left. \frac{\partial}{\partial h_i} \mathbf{E} \left\{ e^2(n) \right\} \right|_{h_i = h_{i, \text{opt}}} = 0$$

$$\frac{\partial}{\partial h_i} \mathbf{E} \left\{ e^2(n) \right\} \Big|_{h_i = h_{i,\text{opt}}} = 0$$

$$2 \mathbf{E} \left\{ e(n) \frac{\partial}{\partial h_i} e(n) \right\} \Big|_{h_i = h_{i,\text{opt}}} = 0$$



Calculation of the optimum filter coefficients:

$$2\operatorname{E}\!\left\{e(n)\,\frac{\partial}{\partial h_i}e(n)\right\}\bigg|_{h_i=h_{i,\mathrm{opt}}}=0$$
 Take the error signal:
$$e(n)=s(n)-\sum_{i=0}^{N-1}h_i\,y(n-i)$$

$$2\operatorname{E}\!\left\{\left(s(n)-\sum_{j=0}^{N-1}h_j\,y(n-j)\right)y(n-i)\right\}\bigg|_{h_i=h_{i,\mathrm{opt}}}=0$$

$$r_{sy}(i)-\sum_{i=0}^{N-1}h_{j,\mathrm{opt}}\,r_{yy}(i-j)=0$$

Target signal and noise are orthogonal: $r_{sy}(l) = r_{ss}(l) + \underbrace{r_{sb}(l)}_{=0} = r_{ss}(l)$

$$r_{ss}(i) - \sum_{j=0}^{N-1} h_{j,\text{opt}} r_{yy}(i-j) = 0 \quad \forall i \in [0, \dots, N-1]$$



Calculation of the optimum filter coefficients:

$$\begin{bmatrix} r_{yy}(0) & r_{yy}(1) & \dots & r_{yy}(N-1) \\ r_{yy}(1) & r_{yy}(0) & \dots & r_{yy}(N-2) \\ \vdots & \vdots & \ddots & \vdots \\ r_{yy}(N-1) & r_{yy}(N-2) & \dots & r_{yy}(0) \end{bmatrix} \begin{bmatrix} h_{0,\text{opt}} \\ h_{1,\text{opt}} \\ \vdots \\ h_{N-1,\text{opt}} \end{bmatrix} = \begin{bmatrix} r_{ss}(0) \\ r_{ss}(1) \\ \vdots \\ r_{ss}(N-1) \end{bmatrix}$$

Difficulties:

□ The autocorrelation function of the speech signal cannot simply be measured.

Solution: $r_{ss}(l) = r_{yy}(l) - r_{bb}(l)$ with a noise autocorrelation function to be measured in speech pauses.

□ The inverse of the autocorrelation matrix does not necessarily exist since the matrix is only non-negative definite.

Solution: Calculation in the frequency domain.

□ The solution of the above matrix equation system is computational complex (and has to be redone every approx. 20 msec).

Solution: Calculation in the frequency domain.



Time domain solution:

$$r_{ss}(i) - \sum_{j=0}^{N-1} h_{j,\text{opt}} r_{yy}(i-j) = 0$$

Frequency domain solution:

$$S_{ss}(\Omega) - H_{\text{opt}}(e^{j\Omega}) S_{yy}(\Omega) = 0$$

$$H_{\text{opt}}(e^{j\Omega}) = \frac{S_{ss}(\Omega)}{S_{yy}(\Omega)}$$

Orthogonality of speech and noise: $S_{ss}(\Omega) = S_{yy}(\Omega) - S_{bb}(\Omega)$

$$H_{\text{opt}}(e^{j\Omega}) = 1 - \frac{S_{bb}(\Omega)}{S_{yy}(\Omega)}$$



Frequency domain solution:

$$H_{\rm opt}(e^{j\Omega}) = 1 - \frac{S_{bb}(\Omega)}{S_{yy}(\Omega)}$$

Approximation with short-term estimates:

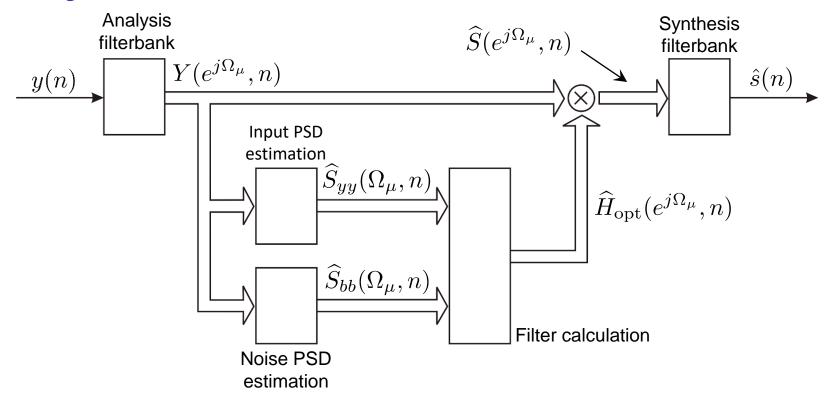
$$\widehat{H}_{\text{opt}}(e^{j\Omega}, n) = \max \left\{ 0, 1 - \frac{\widehat{S}_{bb}(\Omega, n)}{\widehat{S}_{yy}(\Omega, n)} \right\}$$

Typical solution:

- □ Realization with a filter bank system (Application of adaptive attenuation factors in each subband)
- □ The prototype low-pass of the filter-bank should have a length between 15 and 100 msec.
- ☐ The subsampling rate (sample time of the sub-band signals) should be between 1 and 20 msec.
- □ The basic Wiener formula will be modified in order to be suitable for practical applications: Over-estimation, Limitation of the attenuation, etc.



Processing structure:



PSD = power spectral density

M sub-bands with a discrete frequency index:

$$\Omega_{\mu}$$
 with: $0 \le \mu \le M$



Power spectral density estimation for the input signal:

$$\widehat{S}_{yy}(\Omega_{\mu}, n) = \left| Y(e^{j\Omega_{\mu}}, n) \right|^2$$

Theory behind: Estimation of PSDs with "periodograms"

Power spectral density estimation for the noise:



Estimation schemes using voice activity detection (VAD)

Tracking of minima of short-term power estimations



Two alternatives:

1) Schemes with voice activity detection:

$$\widehat{S}_{bb}(\Omega_{\mu}, n) = \begin{cases} \beta \, \widehat{S}_{bb}(\Omega_{\mu}, n - 1) + (1 - \beta) \, \widehat{S}_{yy}(\Omega_{\mu}, n), & \text{during speech pauses,} \\ \widehat{S}_{bb}(\Omega_{\mu}, n - 1), & \text{else.} \end{cases}$$

- 2) Tracking of minima of the short-term power (s. lecture 1, p.45):
 - 1) Smoothing:

$$\overline{S_{yy}(\Omega_{\mu}, n)} = \beta \overline{S_{yy}(\Omega_{\mu}, n - 1)} + (1 - \beta) \widehat{S}_{yy}(\Omega_{\mu}, n)$$

2) Minimum value, with a slight increase to avoid a freezing of the estimate:

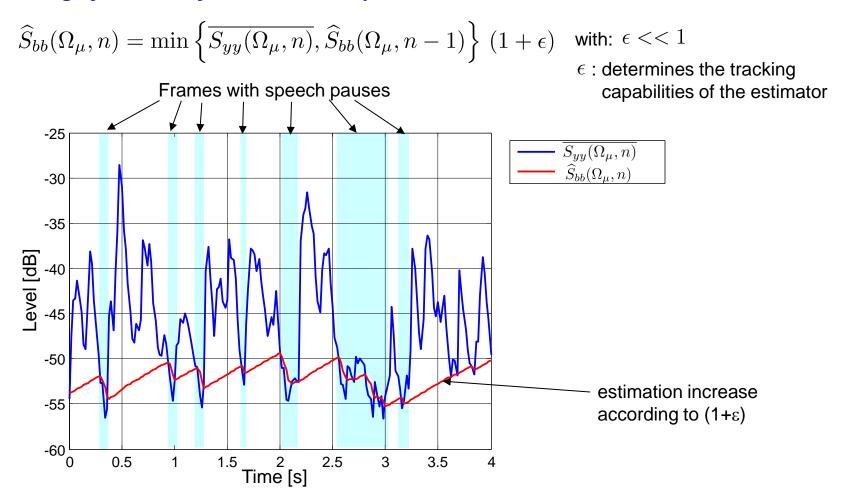
$$\widehat{S}_{bb}(\Omega_{\mu},n) = \min\left\{\overline{S_{yy}(\Omega_{\mu},n)}, \widehat{S}_{bb}(\Omega_{\mu},n-1)\right\} \, (1+\epsilon) \, \text{with: } \epsilon << 1$$

 ϵ : determines the tracking capabilities of the estimator

Noise power spectral density estimation

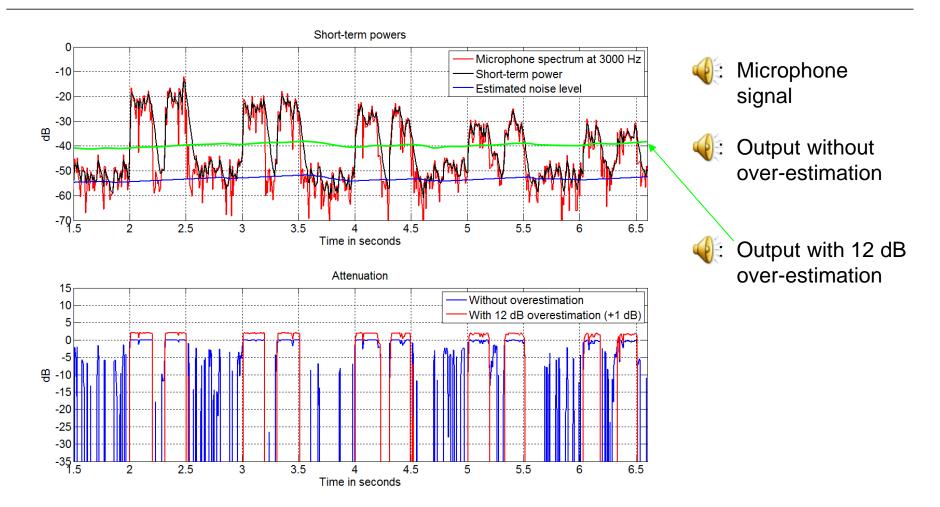


2) Tracking of minima of the short-term power:



Noise reduction





Noise reduction



Limiting the maximum attenuation:

□ For several application the original shape of the noise should be preserved (the noise should only be attenuated but not completely removed). This could be achieved by inserting a maximum attenuation:

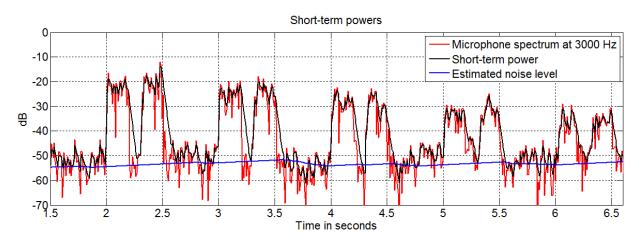
$$H_{\min}(e^{j\Omega_{\mu}}, n) = H_{\min}.$$

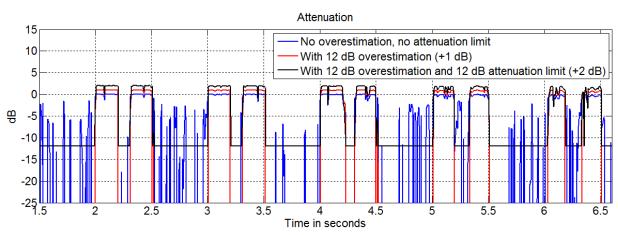
$$\widehat{H}_{\text{opt}}(e^{j\Omega}, n) = \max \left\{ 1 - K_{\text{over}} \frac{\widehat{S}_{bb}(\Omega, n)}{\widehat{S}_{yy}(\Omega, n)}, H_{\text{min}} \right\}$$

□ In addition, this attenuation limits can be varied slowly over time (slightly more attenuation during speech pauses, less attenuation during speech activity).

Noise reduction



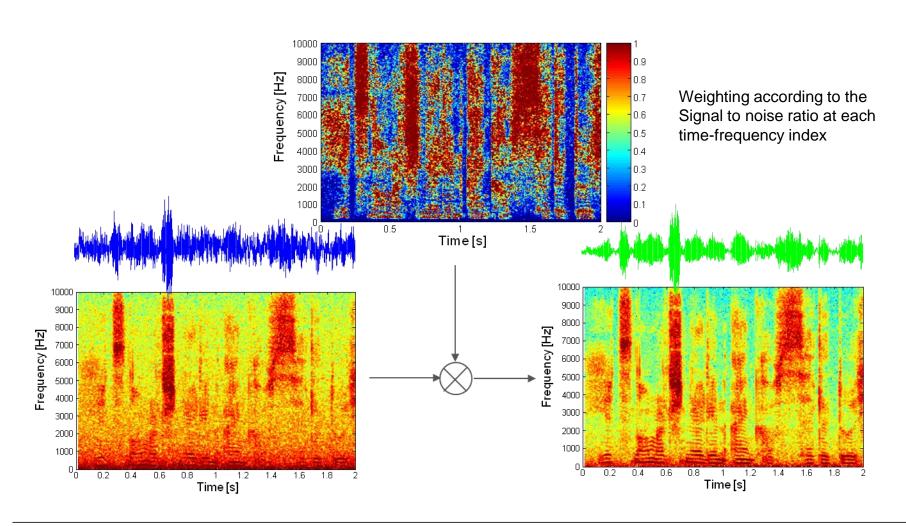




- Microphone signal
- Output without attenuation limit
- Output with attenuation limit

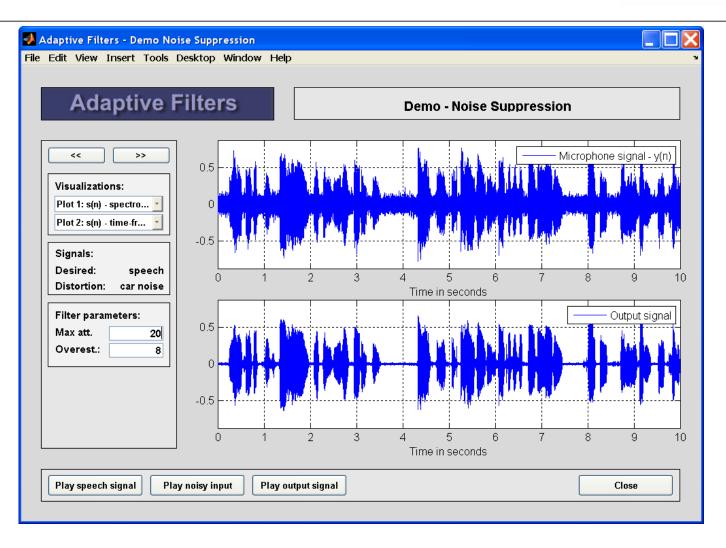
Noise reduction: Spectrogram view





Noise reduction: Matlab-Demo



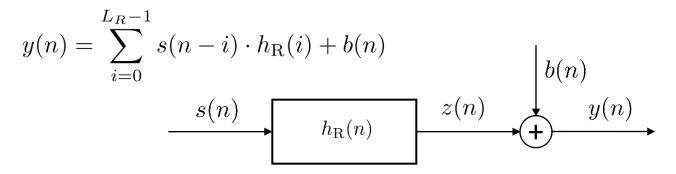


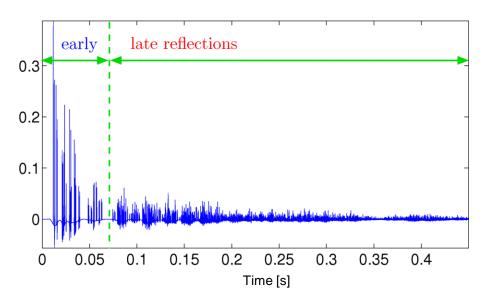


- □ Speech recordings in large rooms sound reverberant, and this the larger the distance is between the signal source and the recording microphone.
- □ This provokes the following effects:
 - The recorded sound quality is perceived as low.
 - □ For large reverberation even the speech intelligibility may be reduced. Here, first hearing impaired people are concerned (=> demands for dereverberation techniques in hearing aids)
 - Automatic speech recognition systems tend to fail in reverberant environments.
- □ Reverberation may also contribute to a good and natural speech quality.
 Early reflections (~ 30 50 ms) are typically desired.
- □ Ideally the room impulse response is known and an inverse filtering is applied. This approach, however, has mainly a theoretical importance.
- □ The procedure sketched here tries to apply a Wiener filter approach comparable to the noise reduction.



□ Convolution with room impulse response + additive noise

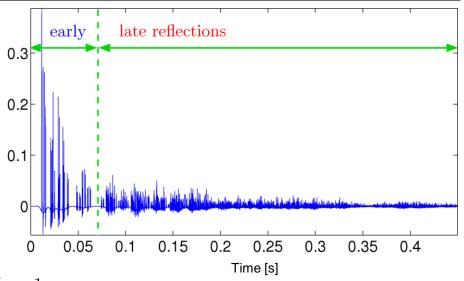




- Early reverberant components are desired and contribute to a natural sound and even to a good speech intelligibility.
- Late reverberant components should be cancelled

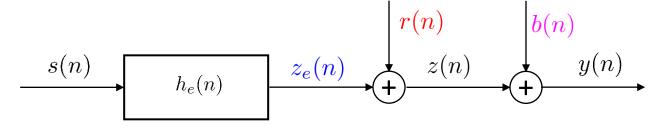


Model late reflections as additive noise component



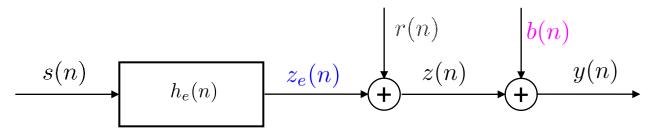
$$y(n) = \sum_{i=0}^{L_e-1} s(n-i) \cdot h_e(i) + \sum_{i=L_e}^{L_R-1} s(n-i) \cdot h_l(i) + b(n)$$

 $z_e(n)$: early reverberant speech r(n): late reverberant speech noi





□ Model late reflections as additive noise component:



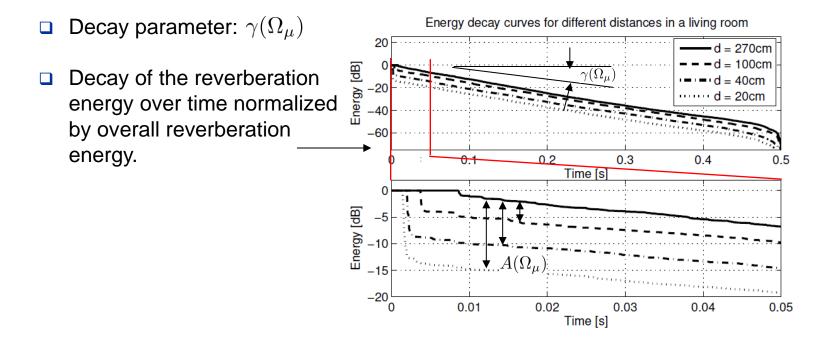
□ Incorporation in the Wiener formula:

$$\widehat{S}_{bb}(\Omega_{\mu}, n) \longrightarrow \widehat{S}_{bb}(\Omega_{\mu}, n) + \widehat{S}_{rr}(\Omega_{\mu}, n)$$

$$\widehat{H}_{opt}(e^{j\Omega_{\mu}}, n) = \max \left\{ H_{min}, 1 - \frac{K_{bb, over} \widehat{S}_{bb}(\Omega_{\mu}, n) + K_{rr, over} \widehat{S}_{rr}(\Omega_{\mu}, n)}{\widehat{S}_{yy}(\Omega_{\mu}, n)} \right\}.$$



- □ Estimation of the PSD of the reverberant signal.
- Two main properties which determine the reverberant signal:
 - Direct-to-reverberant ratio which depends on the distance d between the audio source and the audio sink:





- □ Estimation of the PSD of the reverberant signal.
 - Disturbing reverberation after L_e samples considering the attenuation of the direct path $A(\Omega_{\mu})$ and the decay parameter $\gamma(\Omega_{\mu})$:

$$S_{rr}(\Omega_{\mu}, n) \approx \sum_{k=L_e}^{\infty} S_{ss}(\Omega_{\mu}, n-k) A(\Omega_{\mu}) e^{-\gamma(\Omega_{\mu}) k}$$

- □ Typically, the clean speech is not available
 - => take the noisy spectrum

$$\widehat{S}_{ss}(\Omega_{\mu}, n) \approx |Y(e^{j\Omega_{\mu}}, n)|^2$$

- => leads to an overestimation of the reverberation in noisy environments.
- Summed estimation:

$$\widehat{S}_{rr}(\Omega_{\mu}, n) = \sum_{k=L_e}^{\infty} |Y(e^{j\Omega_{\mu}}, n-k)|^2 A(\Omega_{\mu}) e^{-\gamma(\Omega_{\mu}) k}$$

Recursive estimation:

$$\widehat{S}_{rr}(\Omega_{\mu}, n) = \widehat{S}_{rr}(\Omega_{\mu}, n - 1) e^{-\gamma(\Omega_{\mu})} + |Y(e^{j\Omega_{\mu}}, n - L_e)|^2 A(\Omega_{\mu}) e^{-\gamma(\Omega_{\mu}) L_e}$$



- □ Estimation of the of the direct-to-reverberant ratio and the decay parameter:
 - Rather complicated procedures.
 - A simple approach is sketched in [2]: [2]: M. Buck, A. Wolf: Model Based Dereverberation for Speech Recognition: ITG-Fachtagung Sprachkommunikation, Aachen, Oct. 2008
 - 1) Determine decay rate (assumption: T_60 or T_40 etc. time is known, s. next slide for its definition):

$$10 \log_{10} \left(e^{-\gamma(\Omega_{\mu}) T_{60} f_s} \right) = -60 \, dB \qquad \Longrightarrow \qquad \gamma(\Omega_{\mu}) = \frac{6 \ln(10)}{T_{60} f_s}$$

2) Determine the direct-to-reverberant ratio:

$$\tilde{S}_{rr}(\Omega_{\mu}, n) = \tilde{S}_{rr}(\Omega_{\mu}, n - 1) e^{-\gamma(\Omega_{\mu})} + |Y(e^{j\Omega_{\mu}}, n - L_{e})|^{2} e^{-\gamma(\Omega_{\mu}) L_{e}}$$

$$\hat{Q}_{A}(\Omega_{\mu}, n) = \frac{|Y(e^{j\Omega_{\mu}}, n)|^{2}}{\tilde{S}_{rr}(\Omega_{\mu}, n)}$$

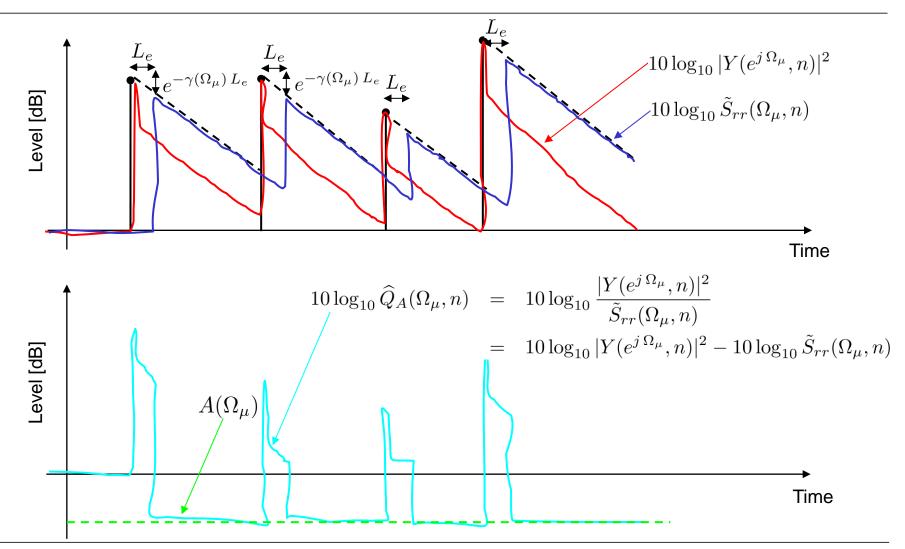
Minimum search in speech pauses:

$$\widehat{A}(\Omega_{\mu}, n) = \min \left\{ (1 + \epsilon) \, \widehat{A}(\Omega_{\mu}, n - 1), \, \widehat{Q}_{A}(\Omega_{\mu}, n) \right\}$$

$$\Rightarrow \ \widehat{S}_{rr}(\Omega_{\mu},n) = \widehat{A}(\Omega_{\mu},n) \, \widetilde{S}_{rr}(\Omega_{\mu},n)$$

Example with impulses as excitation





Repetition (Lecture 1, page 23):



\square Reverberation after a time $t = N^*Ts$

$$att_{max} = \frac{\sigma_e^2(N)}{\sigma_y^2} = \frac{\sum_{v=N}^{\infty} h_v^2}{\sum_{v=0}^{\infty} h_v^2}$$

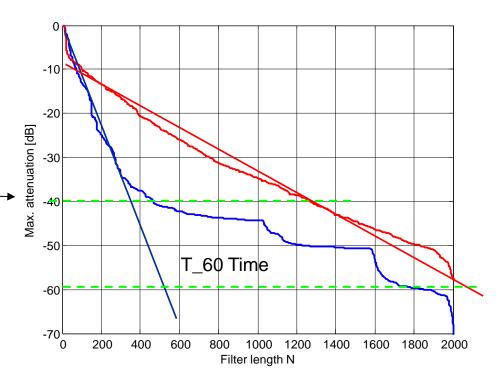
40 dB attenuation: -

N = 450 for a car cabin (example)

N = 1250 for an office room (example)

- □ Determine reverberation time:
 T_60 is a value which typically characterizes the reverberation:
 - Set att_max to 60 dB and calculate corresponding N, or t.

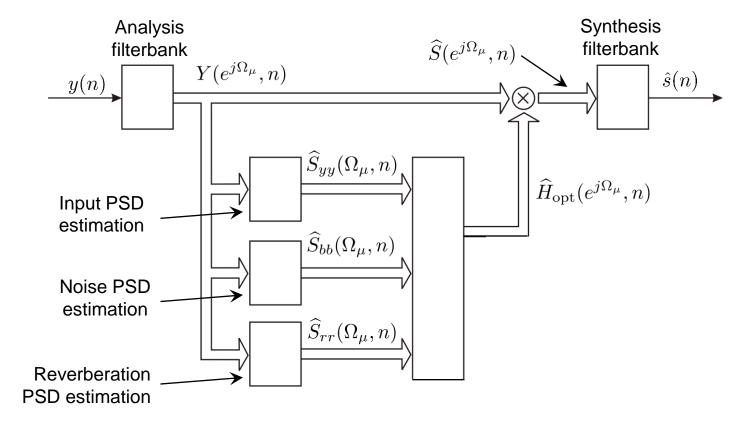
Attenuation in dependence of N



red: office room blue: car cabin

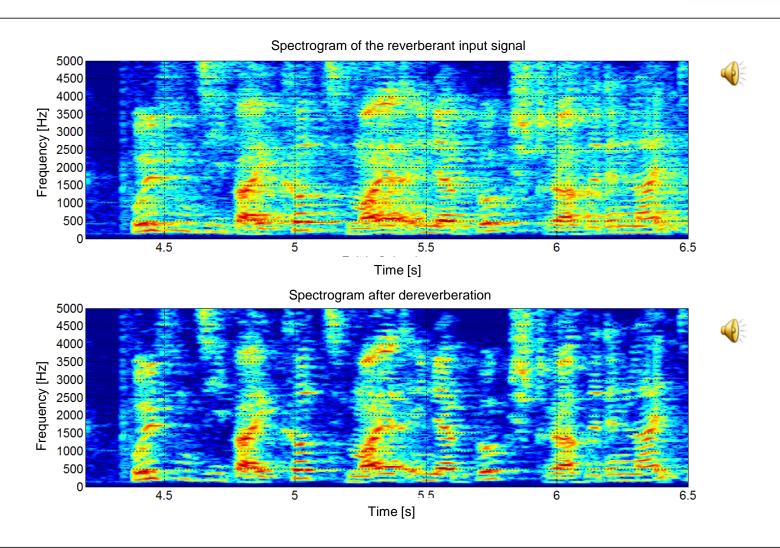


Combined noise reduction and dereverberation:



PSD = power spectral density

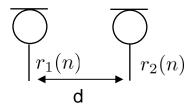




Two microphone based dereverberation



☐ The late reflections are modeled as diffuse noise



☐ Definition of the coherence function:

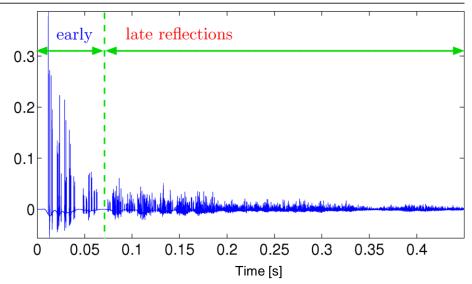
$$\gamma_{r_1 r_2}(\Omega) = \frac{S_{r_1 r_2}(\Omega)}{\sqrt{S_{r_1 r_1}(\Omega) S_{r_2 r_2}(\Omega)}}$$

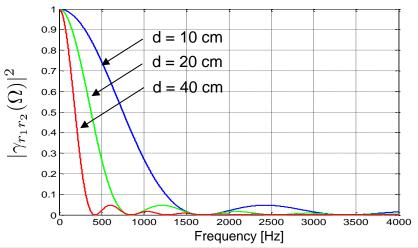
☐ For diffuse noise fields one obtains:

$$|\gamma_{r_1 r_2}(\Omega)|^2 = \frac{\sin^2(\Omega f_s d/c)}{(\Omega f_s d/c)^2}$$

 f_s : sampling rate

c: sound propagation speed





Two microphone based dereverberation

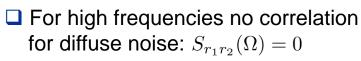


■ Target signal + reverberation:

$$\begin{array}{c|c} \hline \\ \hline \\ x_1(n) \\ \hline \end{array} \begin{array}{c} x_1(n) = s(n) + r_1(n) \\ \hline \\ x_2(n) & x_2(n) = s(n) + r_2(n) \\ \hline \end{array}$$

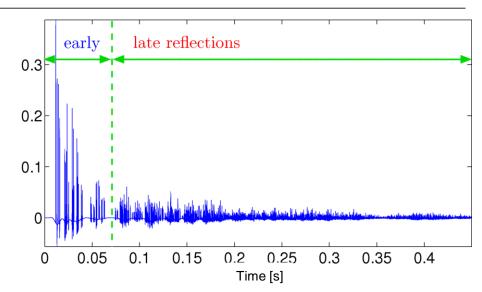
$$\gamma_{x_1x_2}(\Omega) = \frac{S_{x_1x_2}(\Omega)}{\sqrt{S_{x_1x_1}(\Omega) S_{x_2x_2}(\Omega)}}$$
$$= \frac{S_{ss}(\Omega) + S_{r_1r_2}(\Omega)}{S_{ss}(\Omega) + S_{rr}(\Omega)}$$

with:
$$S_{rr}(\Omega) = S_{r_1r_1}(\Omega) = S_{r_2r_2}(\Omega)$$



$$= \gamma_{x_1 x_2}(\Omega) = \frac{S_{ss}(\Omega)}{S_{ss}(\Omega) + S_{rr}(\Omega)} = \frac{S_{ss}(\Omega)}{S_{xx}(\Omega)}$$

identical to the Wiener filter.

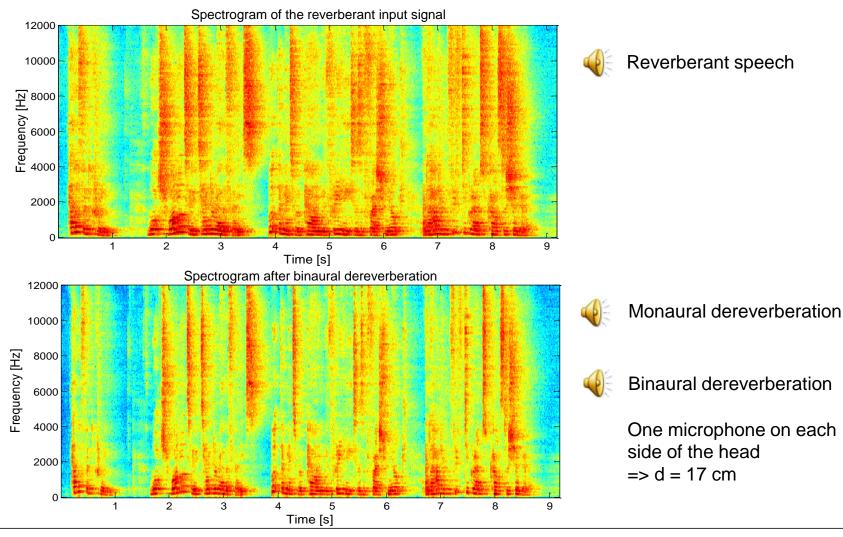


$$\Rightarrow$$
 $\widehat{H}_{\mathrm{opt}}(e^{j\Omega_{\mu}}, n) = \gamma_{x_1x_2}(\Omega_{\mu}, n)$

Coherence function allows filter design for the reverberation reduction. For low frequencies the diffuse coherence has to be considered.

Two microphone based dereverberation





Summary & Outlook



Summary

- Wiener filter
- ☐ Realization in the frequency domain
- Modified basic filter approach
- Modified noise reduction approaches
- Dereverberation methods

Outlook to next week:

Beamforming