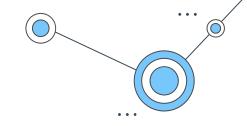


CZ2001 Lab Project 1-Searching Algorithms

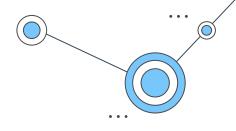


Objectives

- To propose algorithms that solve string searching problems on genome sequences
- The algorithms should return **positions** of occurrences of a query sequence in the source sequence and the **number of** occurrences



Table of Contents



Brute Force Algorithm

- Design and Execution
- Complexity Analysis

BMH Algorithm

- Design and Execution
- Complexity Analysis

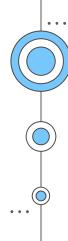
KMP Algorithm (modified)

- Design and Execution
- Complexity Analysis

Comparison 2 Conclusion

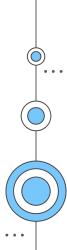






O1Brute Force

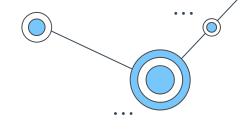
Naive String Searching Algorithm





 Walk through the source sequence from the beginning till the end

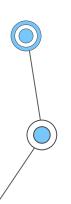
Check at each position
 if the resulting substring
 equals the query
 sequence



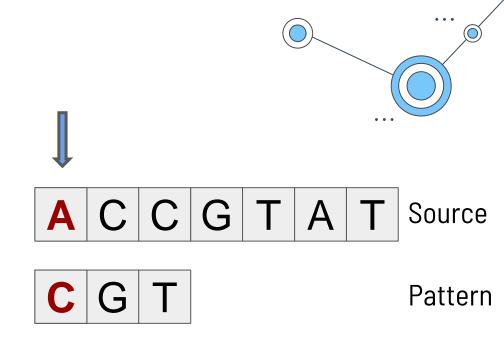
A C C G T A T Source

CGT

Pattern

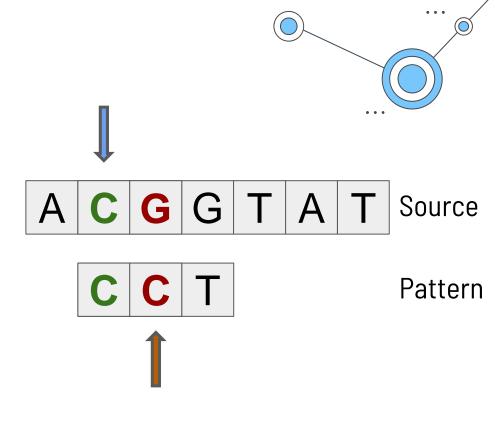


- Walk through the source sequence from the beginning till the end
- Check at each position if the resulting substring equals the query sequence



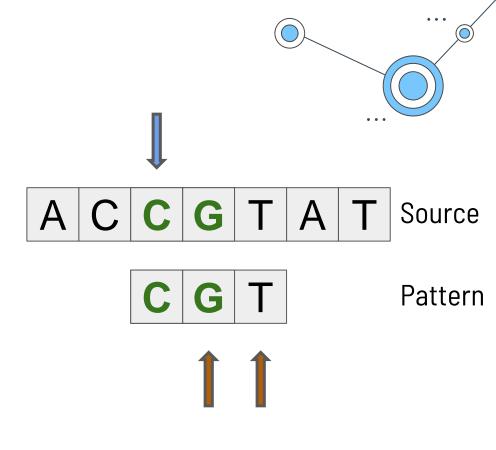


- Walk through the source sequence from the beginning till the end
- Check at each position if the resulting substring equals the query sequence



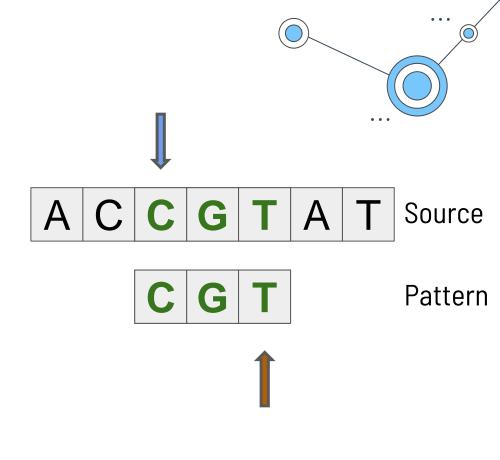


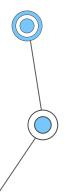
- Walk through the source sequence from the beginning till the end
- Check at each position if the resulting substring equals the query sequence



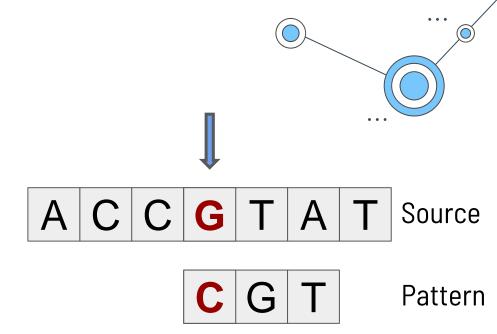


- Walk through the source sequence from the beginning till the end
- Check at each position if the resulting substring equals the query sequence



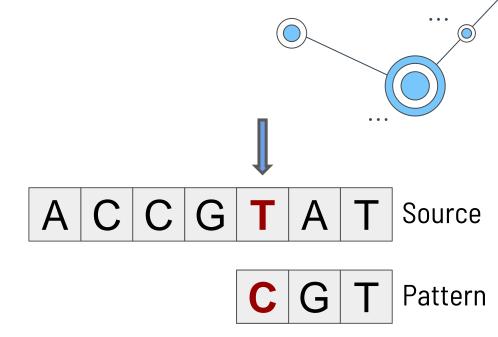


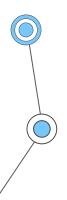
- Walk through the source sequence from the beginning till the end
- Check at each position if the resulting substring equals the query sequence





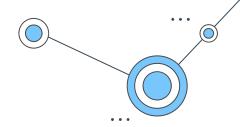
- Walk through the source sequence from the beginning till the end
- Check at each position if the resulting substring equals the query sequence





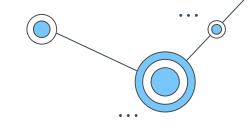


- Nested for-loop
 - Outer loop: check along all possible substrings
 - Inner loop: compare characters between the substring and the query sequence



```
# create an empt
occurrences =
<u># s1: querv sequence: s2: source gen</u>
for i in range (len(s2)-len(s1)+1):
    for j in range (len(s1)):
                    != s1[j]:
                               # misma
            match = False
            break
    # match found
    if match:
                     # append the pos-
        occurrences.append(i+1)
```

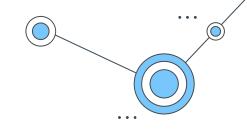




Time Complexity

- let n denote the length of the source genome sequence, and m be the length of the query sequence, where (n>>m)
- To analyze the time complexity of brute force algorithm, we will be looking at the **number of character comparisons**





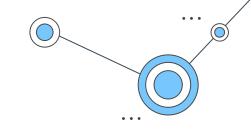
Time Complexity - Best Case Scenario

- Every first-character comparison between possible substring and query sequence results in a mismatch
- The total number of comparisons is only determined by the number of outer-loop iterations, which is (n-m+1), or O(n)

Text: ACTGGTTCATGACCT

Pattern: BATGTC



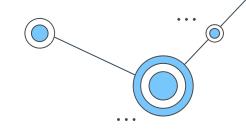


Time Complexity - Worst Case Scenario

 The total number of comparisons is the **product** of the number of outer-loop comparisons and inner-loop comparisons, which is m(n-m+1), or O(mn)

Text: TTTTTTTTT Text: TTTTTTTT

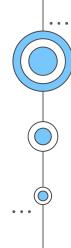
Pattern: TTTT Pattern: TTTA



Time Complexity - Average Case Scenario

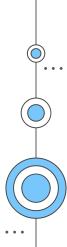
- Outer loop: it will always be executed (n-m+1) times
- Inner loop: assume each number of comparisons (from 1 to m) is equally likely, expected number of comparisons = (1+m)/2
- The average number of comparisons = (n-m+1)[(1+m)/2] = O(mn)

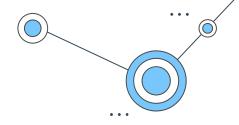




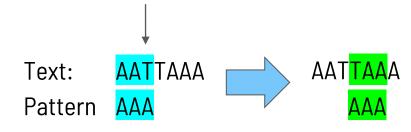
02 BMH

Boyer Moore Horspool Algorithm

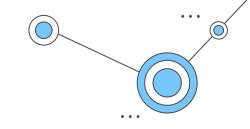




- Reduce searching time by comparing pattern with text sequences from end to start of pattern
- Comparisons between first few characters can be skipped when there is a mismatch in the last few characters

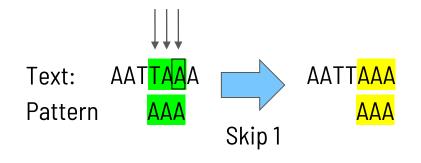






Searching in BMH

 Bad Match Table: Records number skips to do after mismatch with respect to the rightmost character compared in the text

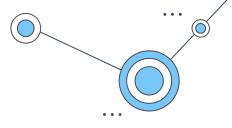


Δ	A C G						
7			•				
	3	3	3				
1							

Bad Match Table

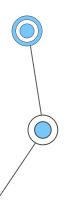






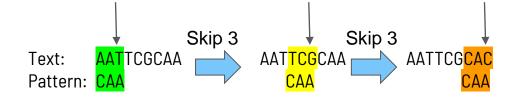
n: Length of text m: Length of pattern σ: Number of alphabets

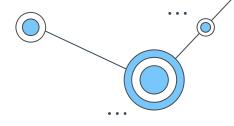
- Counting the number of character comparisons.
- For all cases: $O(m+\sigma)$
 - \circ Assign position to alphabet in Bad Match Table (σ)
 - Calculate number of skips (m)



Time Complexity: Searching

- Best Case Scenario: O(n/m)
 - When the first compared character is always not found in the pattern
 - 1 Comparison and m skips per outer loop





n: Length of text

m: Length of pattern

 $\sigma\hbox{: Number of alphabets}$

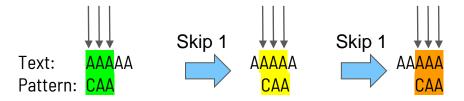
: Comparison

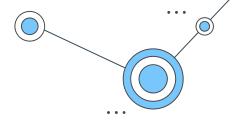
Α	С	G	Т
1	2	3	3





- Worst Case Scenario: O(nm)
 - When all characters in the pattern matches or when all but the last match
 - m comparisons and 1 skips per outer loop





n: Length of text

m: Length of pattern

 $\sigma \hbox{: } \text{Number of alphabets}$

: Comparison

Α	С	G	T
1	2	3	3

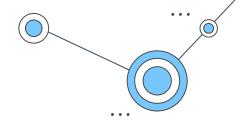


Time Complexity: Searching

Average Case Scenario: O(n)

E (Number of comparisons)

- = E(Times outer loop executed) * E(Comparisons per outer loop)
- = n/E(Skips per outer loop) * E(Comparisons per outer loop)
- = n = O(n)
- Assume each skip (from 1 to m) is equally likely
 - \circ E(Skips per outer loop) = (1+m)/2
- Assume each number of comparisons (from 1 to m) is equally likely
 - \circ E(Comparisons per outer loop) = (1+m)/2

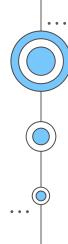


n: Length of text

m: Length of pattern

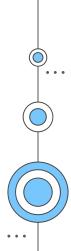
 $\sigma\hbox{: Number of alphabets}$

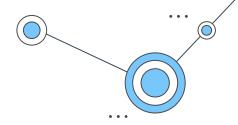




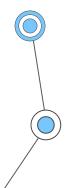
03 Modi-KMP

Modified Knuth-Morris-Pratt algorithm





- Uses two preprocessing techniques to reduce comparisons:
 Bad match table(BMT) & Longest Prefix-Suffix array(LPS)
- Implements bad character heuristic within KMP algorithm, which initially use only lps array.



Bad Match Table

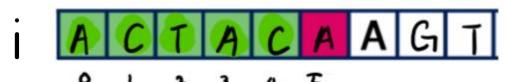
Α	С	G	Т
1	3	3	3

Pattern: ACTACG

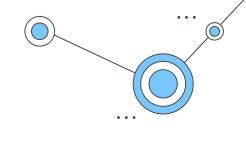
lps	arrary
-----	--------

Α	С	Т	Α	С	G
0	0	0	1	2	0

Lps array

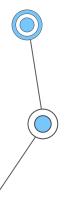


Pattern: ACTACG

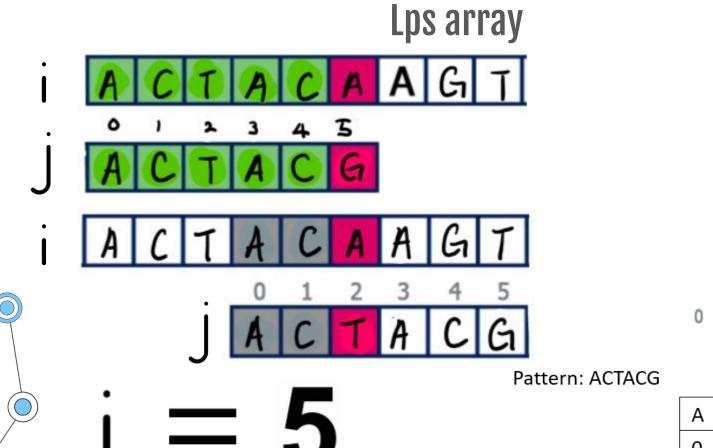


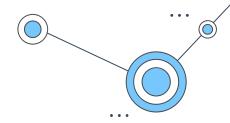
lps arrary

Α	O	Т	Α	O	G
0	0	0	1	2	0



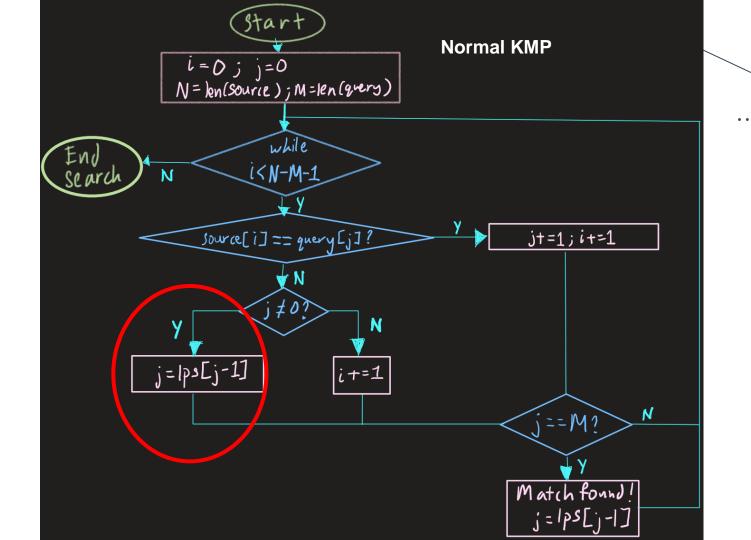
i = 5

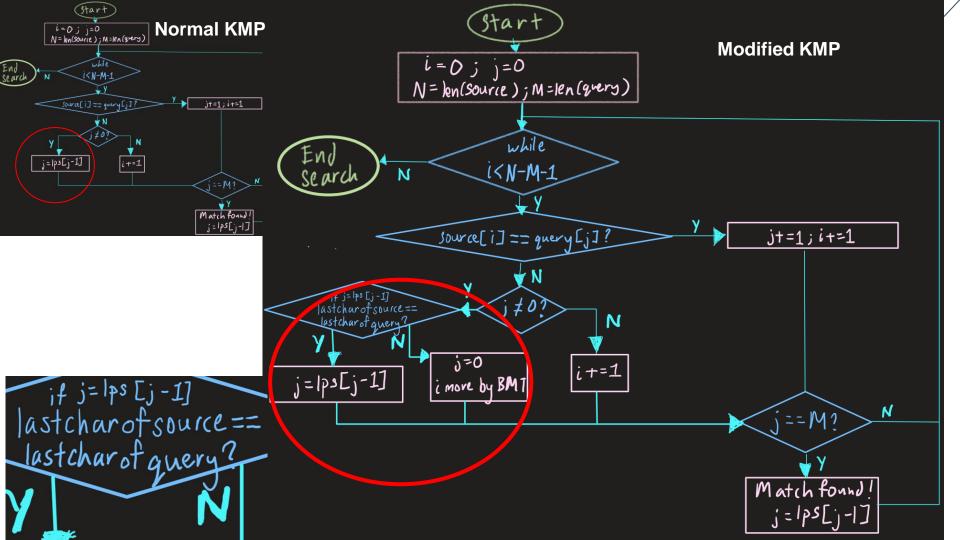




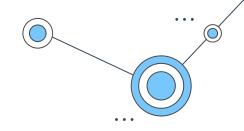


Α	С	Т	Α	С	G
0	0	0	1	2	0





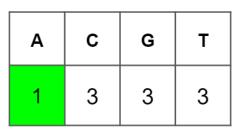
Time Complexity: Preprocessing



n is length of Source DNA, m is length of query pattern

- Bad Match Table: For all cases: approx. O(m)
- LPS: For all cases 0(m)

Bad Match Table



Pattern: ACTACG

lps arrary

Α	C	Т	Α	C	G
0	0	0	1	2	0

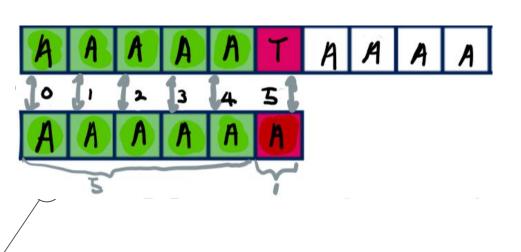
Time Complexity:

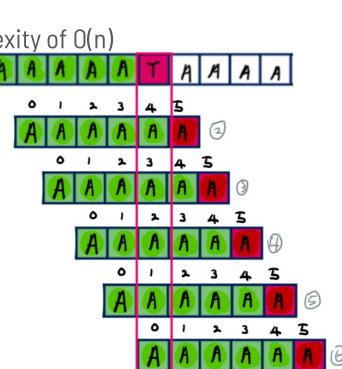
- Best Case Scenario: O(n/m)
 - Occurs when if-else allows BMT⇒ causing algorithm to run like Boyer-Moore
 - Pointer i signifying pattern moving along source code increments by m each time, causing only n/m comparisons



Time Complexity:

- Worst Case Scenario: O(n)
 - Text=AAAAATAAAATAAAATAAAA...
 - Pattern=AAAAAA, length of pattern = 6
 - Compares approx. 2n times: has complexity of O(n)





Time Complexity:

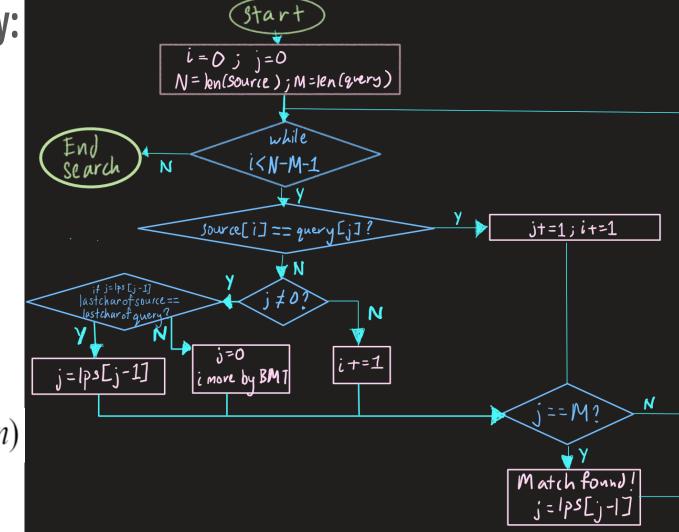
Average Case Scenario: O(n)

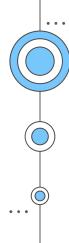
Expected i shifts per iteration:

$$\frac{1}{4} + \frac{15 + 9m^2}{32m}$$

Expected number of comparisons:

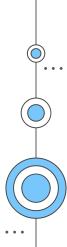
$$n/(\frac{15+8m+9m^2}{32m}) = O(n)$$





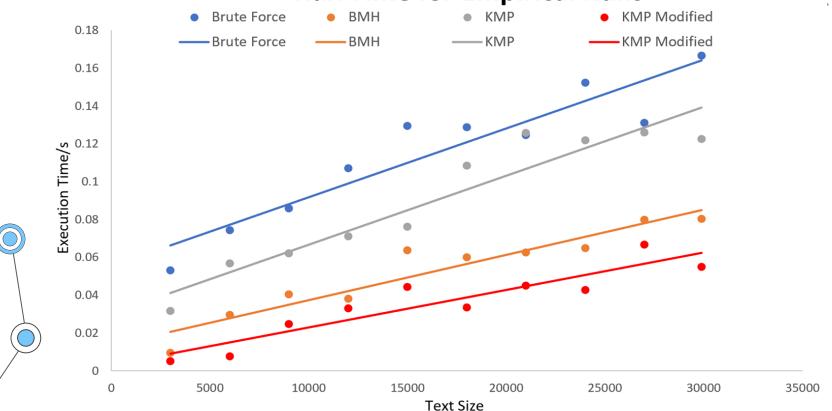
04 Conclusion

Comparison between algorithms



Comparison for empirical runs



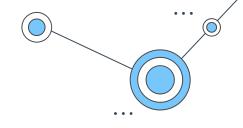


Theoretical Complexity

* n: Length of text, m: Length of pattern, σ : Number of alphabets

Algorithms	Preprocessing complexit		Best Case Time Complexity	Worst Case Time Complexity	Average Case Time Complexity	Preprocessing Space Complexity	Overall Space Complexity
Brute Force			O(n)	O(mn)	O(mn)	-	O(1)
вмн	O(m+σ) for bad cl table	haracter	O($\frac{n}{m}$)	O(mn)	O(n)	O(1) for building bad character table	O(1)
KMP	O(m) for lps a	rray	O(n)	O(n)	O(n)	O(m) for lps Table	O(m)
Modified KMP	O(m+σ) for bad character table	O(m) for lps array	O(½)	O(n)	O(n)	O(m) for lps Table & O(1) for building bad character table	O(m)





Thank You:)

