

Mark Scheme (Results)

June 2011

GCE Further Pure FP1 (6667) Paper 1

Edexcel is one of the leading examining and awarding bodies in the UK and throughout the world. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers.

Through a network of UK and overseas offices, Edexcel's centres receive the support they need to help them deliver their education and training programmes to learners.

For further information, please call our GCE line on 0844 576 0025 or visit our website at <a href="https://www.edexcel.com">www.edexcel.com</a>.

If you have any subject specific questions about the content of this Mark Scheme that require the help of a subject specialist, you may find our **Ask The Expert** email service helpful.

Ask The Expert can be accessed online at the following link: <a href="http://www.edexcel.com/Aboutus/contact-us/">http://www.edexcel.com/Aboutus/contact-us/</a>

June 2011
Publications Code UA027965
All the material in this publication is copyright
© Edexcel Ltd 2011



### **EDEXCEL GCE MATHEMATICS**

## **General Instructions for Marking**

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
  - M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - B marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.

#### Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- The second mark is dependent on gaining the first mark



## June 2011 6667 Further Pure Mathematics FP1 Mark Scheme

Question Number	Scheme	Notes	Marks
1.	$f(x) = 3^x + 3x - 7$		
(a)	f(1) = -1 $f(2) = 8$	Either any one of $f(1) = -1$ or $f(2) = 8$ .	M1
	Sign change (positive, negative) (and $f(x)$ is continuous) therefore (a root) $\alpha$ is between $x = 1$ and $x = 2$ .	Both values correct, sign change and conclusion	A1
			(2)
(b)	$f(1.5) = 2.696152423 $ { $\Rightarrow 1,, \alpha,, 1.5$ }	f(1.5) = awrt 2.7 (or truncated to 2.6)	B1
		Attempt to find f(1.25).	M1
	$f(1.25) = 0.698222038$ $\Rightarrow 1,, \alpha, 1.25$	f(1.25) = awrt  0.7  with 1,, $\alpha$ ,, 1.25 or $1 < \alpha < 1.25$ or $[1, 1.25]$ or $(1, 1.25)$ . or equivalent in words.	A1
	In (b) there is no credit for lin correct answer with no wor	near interpolation and a	(3)
	correct answer with no wor	mig scores no maras.	5



Question Number	Scheme	Notes	Marks
<b>2.</b> (a)	$ z_1  = \sqrt{(-2)^2 + 1^2} = \sqrt{5} = 2.236$	$\sqrt{5}$ or awrt 2.24	B1 (1)
(b)	$\arg z = \pi - \tan^{-1}\left(\frac{1}{2}\right)$	$\tan^{-1}\left(\frac{1}{2}\right) \text{ or } \tan^{-1}\left(\frac{2}{1}\right) \text{ or } \cos^{-1}\left(\frac{2}{\sqrt{5}}\right) \text{ or } \sin^{-1}\left(\frac{1}{\sqrt{5}}\right) \text{ or } \sin^{-1}\left(\frac{1}{\sqrt{5}}\right) \text{ or } \cos^{-1}\left(\frac{1}{\sqrt{5}}\right)$	M1
	= 2.677945045 = 2.68 (2 c	lp) awrt 2.68	A1 oe
		s for the method mark (arg $z = 153.4349488^{\circ}$ )	(2)
	arg z =	$\tan^{-1}\left(\frac{1}{-2}\right) = -0.46$ on its own is M0	
	but $\pi+1$	$\tan^{-1}\left(\frac{1}{2}\right) = 2.68 \text{ scores } M1A1$	
		$(\frac{1}{2})$ = is M0 as is $\pi$ -tan $(\frac{1}{2})$ (2.60)	
(c)	$z^2 - 10z + 28 = 0$	(-2)	_
	$z = \frac{10 \pm \sqrt{100 - 4(1)(28)}}{2(1)}$ $= \frac{10 \pm \sqrt{100 - 112}}{2}$	An attempt to use the quadratic formula (usual rules)	M1
	$=\frac{10\pm\sqrt{-12}}{2}$ $=\frac{10\pm2\sqrt{3}i}{2}$	Attempt to simplify their $\sqrt{-12}$ in terms	M1
	2	of i. E.g. i $\sqrt{12}$ or i $\sqrt{3} \times 4$	=
		>0 then only the first M1 is available.	-
	So, $z = 5 \pm \sqrt{3}i$ . $\{p = 5, q\}$		4
		ers with no working scores full marks. ternative solution by completing the square	(3)
(d)	y <b>↑</b>	Note that the points are $(-2, 1)$ , $(5, \sqrt{3})$ and $(5, -\sqrt{3})$ .	
	•	The point $(-2, 1)$ plotted correctly on the Argand diagram with/without label.	B1
		The distinct points $z_2$ and $z_3$ plotted correctly and symmetrically about the x-axis on the Argand diagram with/without label.	B1√
	awarding the marks	placed relative to each other. If you are in doubt about then consult your team leader or use review.  depends on having obtained complex numbers in (c)	(2)
	- : : : : : : : : : : : : : : : :	(4)	8



Question Number	Scheme	Notes	Ma	rks
3. (a)	$\mathbf{A} = \begin{pmatrix} 1 & \ddot{O} \ 2 \\ \ddot{O} \ 2 & -1 \end{pmatrix}$			
(i)	$\mathbf{A}^2 = \begin{pmatrix} 1 & \ddot{O} \ 2 \\ \ddot{O} \ 2 & -1 \end{pmatrix} \begin{pmatrix} 1 & \ddot{O} \ 2 \\ \ddot{O} \ 2 & -1 \end{pmatrix}$			
	$= \begin{pmatrix} 1+2 & \ddot{O} \ 2-\ddot{O} \ 2 \\ \ddot{O} \ 2-\ddot{O} \ 2 & 2+1 \end{pmatrix}$	A correct method to multiply out two matrices. Can be implied by two out of four correct elements.	M1	
	$= \begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$	Correct answer	A1	
				(2)
(ii)	<b>Enlargement</b> ; scale factor 3, centre (0, 0).	Enlargement; scale factor 3, centre (0, 0)	B1; B1	
	Allow 'from' or 'about' for centre and '0	O' or 'origin' for (0, 0)		
				(2)
(b)	$\mathbf{B} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$			
	Reflection; in the line $y = -x$ .	Reflection; y = -x	B1; B1	
	Allow 'in the axis' 'about the lin	y = -x etc.	Di	
	The question does not specify a <u>single</u> transformation combinations that are correct e.g. Anticlockwise rotates	_ v		(2)
	by a reflection in the x-axis is acceptable. In cases lil completely correct and scored as B2 (no part mark Leader.	ke these, the combination has to be		
(c)	$\mathbf{C} = \begin{pmatrix} k+1 & 12 \\ k & 9 \end{pmatrix}, \ k \text{ is a constant.}$			
	<b>C</b> is singular $\Rightarrow$ det <b>C</b> = 0. (Can be implied)	$\det \mathbf{C} = 0$	B1	
	<b>Special Case</b> $\frac{1}{9(k+1)-12k} = 0$ <b>B</b>	(implied)M0A0		
	$9(k+1) - 12k \left(=0\right)$	Applies $9(k+1) - 12k$	M1	
	9k + 9 = 12k	-		
	9 = 3k			
	k = 3	k = 3	A1	
	k = 3 with no working can scor	e full marks		(3)
				9



Question Number	Scheme	Notes	Marks
4.	$f(x) = x^2 + \frac{5}{2x} - 3x - 1,  x \neq 0$		
(a)	$f(x) = x^2 + \frac{5}{2}x^{-1} - 3x - 1$		
	$f'(x) = 2x - \frac{5}{2}x^{-2} - 3\{+0\}$	At least two of the four terms differentiated correctly.  Correct differentiation. (Allow any	M1
	$f'(x) = 2x - \frac{5}{2x^2} - 3$	correct unsimplified form)	A1 (2)
(b)	$f(0.8) = 0.8^{2} + \frac{5}{2(0.8)} - 3(0.8) - 1(=0.365) \left(=\frac{73}{200}\right)$	A correct numerical expression for f(0.8)	B1
	$f'(0.8) = -5.30625 \left( = \frac{-849}{160} \right)$	Attempt to insert $x = 0.8$ into their $f'(x)$ . Does not require an evaluation. (If $f'(0.8)$ is incorrect for their derivative and there is no working score M0)	M1
	$\alpha_2 = 0.8 - \left(\frac{"0.365"}{"-5.30625"}\right)$	Correct application of Newton-Raphson using their values. Does not require an evaluation.	M1
	= 0868786808		
	= 0.869 (3 dp)	0.869	A1 cao
	A correct answer only with no working sco Ignore any further appl		(4)
	A derivative of $2x - 5(2x)^{-2} - 3$ is quite common	and leads to $f'(0.8) = -3.353125$ and a final	
	answer of 0.909. This would normally s		
	Similarly for a derivative of $2x - 10x^{-2} - 3$		
	f'(0.8) = -17.025 and a	answer 0.821	_
			6



Question Number	Scheme	Notes	Marks
5.	$\mathbf{A} = \begin{pmatrix} -4 & a \\ b & -2 \end{pmatrix}, \text{ where } a \text{ and } b \text{ are constants.}$		
(a)	$\mathbf{A} \begin{pmatrix} 4 \\ 6 \end{pmatrix} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$		
	Therefore, $\begin{pmatrix} -4 & a \\ b & -2 \end{pmatrix} \begin{pmatrix} 4 \\ 6 \end{pmatrix} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$	Using the information in the question to form the matrix equation. Can be implied by both correct equations below.	M1
	Do not allow this mark for other incorrect statements e.g. $\binom{4}{6}\binom{-4}{b}\binom{-4}{-2} = \binom{2}{-8}$ would be M0 unless follows:		
	So, $-16 + 6a = 2$ and $4b - 12 = -8$ Allow $\begin{pmatrix} -16 + 6a \\ 4b - 12 \end{pmatrix} = \begin{pmatrix} 2 \\ -8 \end{pmatrix}$	Any one correct equation.  Any correct horizontal line	M1
	giving $a = 3$ and $b = 1$ .	Any one of $a = 3$ or $b = 1$ .	A1
		Both $a = 3$ and $b = 1$ .	A1 (4)
(b)	$\det \mathbf{A} = 8 - (3)(1) = 5$	Finds determinant by applying $8$ – their $ab$ . $\det \mathbf{A} = 5$	M1 A1
	Special case: The equations $-16 + 6b = 2$ and 4 from incorrect matrix multiplication. This will in (b).		
	Note that $\det \mathbf{A} = \frac{1}{8 - ab}$ scores M0 here but the	ne following 2 marks are available. However,	
	beware det $\mathbf{A} = \frac{1}{8 - ab} = \frac{1}{5} \Rightarrow area S = \frac{30}{\frac{1}{5}} = 150$		
	This scores M0A0 M1A0 Area $S = (\det \mathbf{A})(\text{Area } R)$		
	Area $S = 5 \times 30 = 150 \text{ (units)}^2$	$\frac{30}{\text{their det }\mathbf{A}}$ or $30\times(\text{their det }\mathbf{A})$	M1
	If their dat A < 0 than allow	150 or ft answer	A1 $\sqrt{}$
	If their det $A < 0$ then allow In (b) Candidates may take a more laborious routhe unit square, for example, after the transforcomplete method to score any marks. Correctly answer 5 A1. Then mark as original scheme.	the for the area scale factor and find the area of rmation represented by A. This needs to be a	(4)
			8



Question Number	Scheme	Notes	Marks
6.	$z + 3iz^* = -1 + 13i$		
	(x+iy)+3i(x-iy)	$z^* = x - i y$ Substituting $z = x + i y$ and their $z^*$ into $z + 3i z^*$	B1 M1
	x + iy + 3ix + 3y = -1 + 13i	Correct equation in x and y with $i^2 = -1$ . Can be implied.	A1
	(x+3y)+i(y+3x)=-1+13i		
	Re part: $x + 3y = -1$ Im part: $y + 3x = 13$	An attempt to equate real <b>and</b> imaginary parts.  Correct equations.	M1 A1
	3x + 9y = -3 $3x + y = 13$		
	$8y = -16 \implies y = -2$	Attempt to solve simultaneous equations to find one of x or y. At least one of the equations must contain both x and y terms.	M1
	$x + 3y = -1 \implies x - 6 = -1 \implies x = 5$	Both $x = 5$ and $y = -2$ .	A1 (7)
	$\left\{ z = 5 - 2i \right\}$		7



Question Number	Scheme	Notes	Mar	ks
7.	$\{S_n = \} \sum_{r=1}^n (2r-1)^2$			
(a)	$= \sum_{r=1}^{n} 4r^2 - 4r + 1$	Multiplying out brackets and an attempt to use at least one of the two standard formulae correctly.	M1	
	$= 4.\frac{1}{6}n(n+1)(2n+1) - 4.\frac{1}{2}n(n+1) + n$	First two terms correct. + n	A1 B1	
	$= \frac{2}{3}n(n+1)(2n+1) - 2n(n+1) + n$			
	$= \frac{1}{3}n\{2(n+1)(2n+1) - 6(n+1) + 3\}$	Attempt to factorise out $\frac{1}{3}n$ Correct expression with $\frac{1}{3}n$ factorised out with no errors seen.	M1 A1	
	$= \frac{1}{3}n\left\{2(2n^2+3n+1) - 6(n+1) + 3\right\}$			
	$= \frac{1}{3}n\{4n^2+6n+2-6n-6+3\}$			
	$= \frac{1}{3}n(4n^2-1)$			
	$= \frac{1}{3}n(2n+1)(2n-1)$	Correct proof. No errors seen.	A1 *	(6)
	Note that there are no marks	for proof by induction.	-	(6)
(b)	$\sum_{r=n+1}^{3n} (2r-1)^2 = S_{3n} - S_n$			
	$= \frac{1}{3} \cdot 3n(6n+1)(6n-1) - \frac{1}{3}n(2n+1)(2n-1)$	Use of $S_{3n} - S_n$ or $S_{3n} - S_{n+1}$ with the result from (a) used at least once.  Correct unsimplified expression.  E.g. Allow $2(3n)$ for $6n$ .	M1 A1	
	Note that (b) says <b>hence</b> so they have $= n(36n^2 - 1) - \frac{1}{3}n(4n^2 - 1)$		-	
	$= \frac{1}{3}n(108n^2 - 3 - 4n^2 + 1)$	Factorising out $\frac{1}{3}n$ (or $\frac{2}{3}n$ )	dM1	
	$= \frac{1}{3}n(104n^2 - 2)$			
	$= \frac{2}{3}n(52n^2 - 1)$	$\frac{2}{3}n(52n^2-1)$	<b>A</b> 1	
	${a = 52, b = -1}$			(4)
				10



Question Number	Scheme	Notes	Ма	arks
8.	$C: y^2 = 48x$ with general point $P(12t^2, 24t)$ .			
(a)	$y^2 = 4ax \implies a = \frac{48}{4} = 12$	Using $y^2 = 4ax$ to find a.	M1	
	So, directrix has the equation $x + 12 = 0$	x + 12 = 0	A1 (	oe
	Correct answer with no work	ing allow full marks		(2)
(b)	$y = \sqrt{48} x^{\frac{1}{2}} \implies \frac{dy}{dx} = \frac{1}{2} \sqrt{48} x^{-\frac{1}{2}} \left( = 2\sqrt{3} x^{-\frac{1}{2}} \right)$ or (implicitly) $y^2 = 48x \implies 2y \frac{dy}{dx} = 48$	$\frac{dy}{dx} = \pm k x^{-\frac{1}{2}}$ $ky \frac{dy}{dx} = c$	M1	
	or (chain rule) $\frac{dy}{dx} = \frac{dy}{dt} \times \frac{dt}{dx} = 24 \times \frac{1}{24t}$	their $\frac{dy}{dt} \times \left( \frac{1}{\text{their } \frac{dx}{dt}} \right)$	-	
	When $x = 12t^2$ , $\frac{dy}{dx} = \frac{\sqrt{48}}{2\sqrt{12t^2}} = \frac{\sqrt{4}}{2t} = \frac{1}{t}$ or $\frac{dy}{dx} = \frac{48}{2y} = \frac{48}{48t} = \frac{1}{t}$	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{t}$	A1	
	<b>T</b> : $y - 24t = \frac{1}{t}(x - 12t^2)$	Applies $y - 24t = \text{their } m_T (x - 12t^2)$ or $y = (\text{their } m_T)x + c$ using $x = 12t^2$ and $y = 24t$ in an attempt to find c. Their $m_T$ must be a function of $t$ .	M1	
	$T: ty - 24t^2 = x - 12t^2$			
	<b>T</b> : $x - ty + 12t^2 = 0$	Correct solution.	A1 c	
(a)	Special case: If the gradient is quoted as Compare $P(12t^2, 24t)$ with $(3, 12)$ gives $t = \frac{1}{2}$ .	1/t, this can score M0A0M1A1 $t = \frac{1}{2}$	D1	(4)
(c)	NB $x - ty + 12t^2 = 0$ with $x = 3$ and $y = 12$ gives $4$	2	B1	
	$t = \frac{1}{2}$ into <b>T</b> gives $x - \frac{1}{2}y + 3 = 0$	Substitutes their $t$ into $\mathbf{T}$ .	M1	
	See Appendix for an alternative ap			
	At $X$ , $x = -12 \Rightarrow -12 - \frac{1}{2}y + 3 = 0$	Substitutes their $x$ from (a) into $T$ .	M1	
	So, $-9 = \frac{1}{2}y \implies y = -18$			
	So the coordinates of <i>X</i> are $(-12, -18)$ .	(-12, -18)	A1	
	The coordinates must be together at the end for the	, ,	1	(4)
				10



Question Number	Scheme	Notes	Marks
<b>9.</b> (a)	$n = 1;  \text{LHS} = \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^{1} = \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}$ $RHS = \begin{pmatrix} 3^{1} & 0 \\ 3(3^{1} - 1) & 1 \end{pmatrix} = \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}$ As LHS = RHS, the matrix result is true for $n = 1$ .	Check to see that the result is true for $n = 1$ .	B1
	Assume that the matrix equation is true for $n = k$ , i.e. $\begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^k = \begin{pmatrix} 3^k & 0 \\ 3(3^k - 1) & 1 \end{pmatrix}$		
	With $n = k+1$ the matrix equation becomes $ \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^{k+1} = \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^{k} \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix} $ $ = \begin{pmatrix} 3^{k} & 0 \\ 3(3^{k}-1) & 1 \end{pmatrix} \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix} \text{or} \begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix} \begin{pmatrix} 3^{k} & 0 \\ 3(3^{k}-1) & 1 \end{pmatrix} $	$\begin{pmatrix} 3^k & 0 \\ 0 & by \begin{pmatrix} 3 & 0 \\ 0 & 1 \end{pmatrix}$	M1
	$= \begin{pmatrix} 3^{k+1} + 0 & 0 + 0 \\ 9(3^k - 1) + 6 & 0 + 1 \end{pmatrix} \text{or} \begin{pmatrix} 3^{k+1} + 0 & 0 + 0 \\ 6.3^k + 3(3^k - 1) & 0 + 1 \end{pmatrix}$	Correct unsimplified matrix with no errors seen.	A1
	$= \begin{pmatrix} 9(3^{k}) - 3 & 1 \end{pmatrix}$ $= \begin{pmatrix} 3^{k+1} & 0 \\ 3(3(3^{k}) - 1) & 1 \end{pmatrix}$		
	$= \begin{pmatrix} 3^{k+1} & 0 \\ 3(3^{k+1} - 1) & 1 \end{pmatrix}$ If the result is true for $n = k$ , (1) then it is now true for	Manipulates so that $k \rightarrow k+1$ on at least one term. Correct result with no errors seen with some working between this and the previous A1	dM1
	n = k + 1. (2) As the result has shown to be true for $n = 1$ , (3) then the result is true for all $n$ . (4) <b>All 4</b> aspects need to be mentioned at some point for the last <b>A1</b> .	Correct conclusion with all previous marks earned	A1 cso (6)
			(0)



Question Number	Scheme	Notes	Marks
<b>9.</b> (b)	f(1) = $7^{2-1} + 5 = 7 + 5 = 12$ , {which is divisible by 12}. { : f (n) is divisible by 12 when $n = 1$ .}	Shows that $f(1) = 12$ .	B1
	Assume that for $n = k$ , $f(k) = 7^{2k-1} + 5$ is divisible by 12 for $k \in \mathcal{C}^+$ .		
	So, $f(k + 1) = 7^{2(k+1)-1} + 5$	Correct unsimplified expression for $f(k + 1)$ .	B1
	giving, $f(k+1) = 7^{2k+1} + 5$		
	$\therefore f(k+1) - f(k) = (7^{2k+1} + 5) - (7^{2k-1} + 5)$	Applies $f(k+1) - f(k)$ . No simplification is necessary and condone missing brackets.	M1
	$=7^{2k+1}-7^{2k-1}$		
	$=7^{2k-1}(7^2-1)$	Attempting to isolate 7 <sup>2k-1</sup>	M1
	$=48\left(7^{2k-1}\right)$	$48(7^{2k-1})$	A1cso
	.: $f(k+1) = f(k) + 48(7^{2k-1})$ , which is divisible by 12 as both $f(k)$ and $48(7^{2k-1})$ are both divisible by 12.(1) If the result is true for $n = k$ , (2) then it is now true for $n = k+1$ . (3) As the result has shown to be true for $n = 1$ ,(4) then the result is true for all $n$ . (5). All 5 aspects need to be mentioned at some point for the last A1.	Correct conclusion with no incorrect work. Don't condone missing brackets.	A1 cso
	There are other ways of proving this by induction. S If you are in any doubt consult your team leader a		(6)



# Appendix

Question Number	Scheme	Notes	Marks
Aliter 2. (c) Way 2	$z^2 - 10z + 28 = 0$		
,, u, z	$(z-5)^2 - 25 + 28 = 0$	$(z\pm 5)^2 \pm 25 + 28 = 0$	M1
	$\left(z-5\right)^2 = -3$		
	$z - 5 = \sqrt{-3}$		
	$z - 5 = \sqrt{3}i$	Attempt to express their $\sqrt{-3}$ in terms of i.	M1
	So, $z = 5 \pm \sqrt{3}i$ . $\{p = 5, q = 3\}$	$5 \pm \sqrt{3}i$	A1 oe
			(3)

Question Number	Scheme		Mar	ks
<b>Aliter 2.</b> (c)	$z^2 - 10z + 28 = 0$			
Way 3	$\left(z - \left(p + i\sqrt{q}\right)\right)\left(z - \left(p - i\sqrt{q}\right)\right) = z^2 - 2pz + p^2 + q$			
	$2p = \pm 10$ and $p^2 \pm q = 28$	Uses sum and product of roots	M1	
	$2p = \pm 10 \implies p = 5$ $p = 5  and  q = 3$	Attempt to solve for $p(\text{or } q)$	M1 A1	
				(3)



Question Number	Scheme	Notes	Marks
Aliter			
<b>8.</b> (c)	$\frac{dy}{dx} = 2\sqrt{3} x^{-\frac{1}{2}} = \frac{2\sqrt{3}}{\sqrt{3}} = 2$		B1
Way 2	w vs		
·	Gives $y - 12 = 2(x - 3)$	Uses (3, 12) and their "2" to find the equation of the tangent.	M1
	$x = -12 \Rightarrow y - 12 = 2(-12 - 3)$	Substitutes their <i>x</i> from (a) into their tangent	M1
	y = -18		
	So the coordinates of <i>X</i> are $(-12, -18)$ .		A1
			(4

Question Number	Scheme	Notes	Marks
Aliter			
<b>9.</b> (b)	$f(1) = 7^{2-1} + 5 = 7 + 5 = 12,$	Shows that $f(1) = 12$ .	B1
Way 2	{which is divisible by 12}. {:. $f(n)$ is divisible by 12 when $n = 1$ .}		
	Assume that for $n = k$ ,		
	$f(k) = 7^{2k-1} + 5$ is divisible by 12 for $k \in \mathfrak{C}^+$ .		
	So, $f(k+1) = 7^{2(k+1)-1} + 5$	Correct expression for $f(k + 1)$ .	B1
	giving, $f(k+1) = 7^{2k+1} + 5$		
	$7^{2k+1} + 5 = 49 \times 7^{2k-1} + 5$	Attempt to isolate 7 <sup>2k-1</sup>	M1
	$=49\times \left(7^{2k-1}+5\right)-240$	M1 Attempt to isolate $7^{2k-1} + 5$	M1
	$f(k+1) = 49 \times f(k) - 240$	Correct expression in terms of $f(k)$	A1
	As both $f(k)$ and 240 are divisible by 12 then so is $f(k + 1)$ . If the result is true for $n = k$ , then it		
	is now true for $n = k+1$ . As the result has	Correct conclusion	A1
	shown to be true for $n = 1$ , then the result is true		
	for all <i>n</i> .		
			(



Question Number	Scheme	Notes	Marks
Aliter			
<b>9.</b> (b)	$f(1) = 7^{2-1} + 5 = 7 + 5 = 12,$	Shows that $f(1) = 12$ .	B1
Way 3	{which is divisible by 12}.	. ,	
	$\{ :: f(n) \text{ is divisible by } 12 \text{ when } n = 1. \}$		
	Assume that for $n = k$ , $f(k)$ is divisible by 12		
	$so f(k) = 7^{2k-1} + 5 = 12m$		
	G 0/1 4) =2(k+1)=1 5		
	So, $f(k+1) = 7^{2(k+1)-1} + 5$	Correct expression for $f(k + 1)$ .	B1
	giving, $f(k+1) = 7^{2k+1} + 5$		
	$7^{2k+1} + 5 = 7^2 \cdot 7^{2k-1} + 5 = 49 \times 7^{2k-1} + 5$	Attempt to isolate 7 <sup>2k-1</sup>	M1
	$=49\times(12m-5)+5$	Substitute for <i>m</i>	M1
	$f(k+1) = 49 \times 12m - 240$	Correct expression in terms of <i>m</i>	A1
	As both $49 \times 12m$ and 240 are divisible by 12		
	then so is $f(k + 1)$ . If the result is true for $n = k$ ,		
	then it is now true for $n = k+1$ . As the result	Correct conclusion	A1
	has shown to be true for $n = 1$ , then the result is		
	true for all <i>n</i> .		
			(6)



Question Number	Scheme	Notes	Marks
Aliter			
<b>9.</b> (b)	$f(1) = 7^{2-1} + 5 = 7 + 5 = 12,$	Shows that $f(1) = 12$ .	B1
Way 4	{which is divisible by 12}. { $\therefore$ f (n) is divisible by 12 when $n = 1$ .}		
	Assume that for $n = k$ ,		-
	$f(k) = 7^{2k-1} + 5$ is divisible by 12 for $k \in \mathcal{C}^+$ .		-
	$f(k+1) + 35f(k) = 7^{2(k+1)-1} + 5 + 35(7^{2k-1} + 5)$	Correct expression for $f(k + 1)$ .	B1
	$f(k+1) + 35f(k) = 7^{2k+1} + 5 + 35(7^{2k-1} + 5)$	Add appropriate multiple of $f(k)$ For $7^{2k}$ this is likely to be 35 (119, 203,.) For $7^{2k-1}$ 11 (23, 35, 47,)	M1
	giving, $7.7^{2k} + 5 + 5.7^{2k} + 175$	Attempt to isolate 7 <sup>2k</sup>	M1
	$=180+12\times 7^{2k}=12(15+7^{2k})$	Correct expression	A1
	:. $f(k+1) = 12(7^{2k} + 15) - 35f(k)$ . As both $f(k)$		
	and $12(7^{2k} + 15)$ are divisible by 12 then so is		
	f(k + 1). If the result is true for $n = k$ , then it is now true for $n = k+1$ . As the result has shown	Correct conclusion	A1
	to be true for $n = 1$ , then the result is true for all $n$ .		(6)

Further copies of this publication are available from Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN

Telephone 01623 467467
Fax 01623 450481
Email <u>publication.orders@edexcel.com</u>
Order Code UA027965 June 2011

For more information on Edexcel qualifications, please visit  $\underline{www.edexcel.com/quals}$ 

Pearson Education Limited. Registered company number 872828 with its registered office at Edinburgh Gate, Harlow, Essex CM20 2JE





