

# EDEXCEL - LONDON EXAMINATIONS

Stewart House 32 Russell Square London WC1B 5DN

June 2001

Advanced Supplementary/Advanced Level

General Certificate of Education

Subject MECHANICS 6679

Paper No. M3

Question number	Scheme	Marks
1. (a)	$v = \int \frac{1}{2} e^{-\frac{1}{6}t} dt$ $= -3e^{-\frac{1}{6}t} (+c)$ <p>use of limits or <math>t=0, v=10</math></p> $v = 13 - 3e^{-\frac{1}{6}t}$	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\rightarrow M1 \leftarrow</math>  A1  M1  A1 </div> (4)
(b)	$t=3, v = 11.2 \text{ ms}^{-1}$	M1 A1 (2)
(c)	13 (ft. if $v = a \pm be^{-\frac{1}{6}t}$ )	B1 + (1) (7)
2. (a)	$\cos \theta = \frac{3}{4}, 0.75, 6/8$	B1 (1)
(b)	$mg \cos \theta (-R) = \frac{mv^2}{0.8}$ $v^2 = 5.88 \text{ m}^2 \text{ s}^{-2}$	M1 A1 A1 (3)
(c)	$\frac{1}{2} m \cdot 5.88 - \frac{1}{2} mu^2 = mg \times 0.2$ $u = 1.4$	M1 A1 A1 (3) (7)
3. (a)	$\frac{1}{2} \times 1.5 v^2 = \frac{52 \times 0.05^2}{2 \times 0.25}$ $v = 0.589 \text{ ms}^{-1} \text{ (3SF)}$	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\rightarrow M1 \leftarrow</math> A1 A1  M1 A1 </div> (5)
(b)	$F = 0.6 \times 1.5g$ $\frac{52x}{0.25} \text{ or } \frac{52x}{25}$ $T=F \Rightarrow x = 0.0424 \text{ m or } 4.24 \text{ cm}$ $\text{Min distance} = 0.208 \text{ m or } 20.8 \text{ cm}$	M1 B1 M1 A1 A1 V (5) (10)

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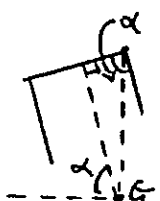
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A.(a)	$g = k/R^2 \Rightarrow k = R^2 g$ $a = -\frac{k}{x^2}$ $v \frac{dv}{dx} = -\frac{R^2 g}{x^2}$	B1 $\rightarrow$ M1 M1 A1 c.s.o. (4)
b)	$\int v dv = -\int \frac{R^2 g}{x^2} dx$ $\frac{v^2}{2} = \frac{R^2 g}{x} (+ c)$ <p style="text-align: center;"><i>correct</i></p> $x=R, v=u \text{ or } \text{use of limits}$ $\frac{v^2}{2} = \frac{R^2 g}{x} + \frac{u^2}{2} - Rg$ <p style="text-align: center;"><i>use of v=0</i></p> $X = \frac{2gR^2}{2gR - u^2}$	$\rightarrow$ M1 A1 $\rightarrow$ M1 A1 M1 A1 (6) (10)
S(a)	$\frac{\pi r^2 h}{6} \quad \frac{1}{6} \pi r^2 h \quad \frac{5}{6} \pi r^2 h$ <p style="text-align: center;">(6) (1) (5)</p> $\frac{1}{2}h \quad \frac{7h}{8} \quad \bar{x}$ $6 \cdot \frac{1}{2}h - \frac{7h}{8} = 5\bar{x}$ $\bar{x} = \frac{17h}{40}$	B2 -1 e.e.o.o. B2 -1 e.e.o.o. M1 A1 A1 (7)
(b)	 $\tan \alpha = \frac{h - \bar{x}}{r}$ <p style="text-align: center;"><i>use of h=4r to obtain expression in h or only</i></p> $\alpha = 66.5^\circ \text{ (1DP)}$	$\rightarrow$ M1 A1 M1 A1 (4) (11)

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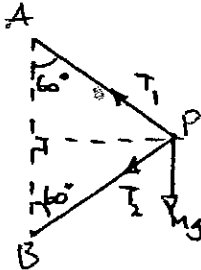
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6. (a)	$r = \frac{1}{2}h \tan 60^\circ = \frac{\sqrt{3}h}{2} *$	M1 A1 (2)
(b)	 <p> <math>R(1), T_1 \cos 60^\circ - T_2 \cos 60^\circ = mg</math>  <math>R(1), T_1 \sin 60^\circ + T_2 \sin 60^\circ = m \frac{\sqrt{3}}{2} h \omega^2</math>              Use of <math>\cos 60^\circ = \frac{1}{2}</math> and <math>\sin 60^\circ = \frac{\sqrt{3}}{2}</math>              Solving for <math>T_1</math> or <math>T_2</math>  <math>T_1 = \frac{1}{2}m(h\omega^2 + 2g); T_2 = \frac{1}{2}m(h\omega^2 - 2g)</math> </p>	<p> <math>\rightarrow</math> M1 A1  <math>\rightarrow</math> M1 A1                      B1                      M1                      A1; A1 = (8)                 </p>
(c)	$T_2 > 0 \Rightarrow \omega > \sqrt{\frac{2g}{h}}$ $T = \frac{2\pi}{T} \Rightarrow T < 2\pi \sqrt{\frac{h}{2g}} = \frac{\pi\sqrt{2h}}{g} *$	<p>                     M1 A1 ✓                      M1 A1 c.s.c. (4)                      (14)                 </p>
7. (a)	In equlib, $T = mg \sin 30^\circ$ $\lambda \frac{1}{8}a = mg \sin 30^\circ \Rightarrow \lambda = 4mg *$	<p>                     B1                      M1 A1 (3)                 </p>
(b)	$m\ddot{x} = mg \sin 30^\circ - \frac{4mg}{a}(\frac{1}{8}a + x)$ $\ddot{x} = -\frac{4g}{a}x \Rightarrow \text{SHM}$ $\text{Period} = 2\pi \sqrt{\frac{a}{4g}} = \frac{\pi\sqrt{a}}{\sqrt{g}} *$	<p> <math>\rightarrow</math> M1 A2  <math>\rightarrow</math> M1 A1                      A1 (6)                 </p>
(c)	Max accel = $\omega^2 a = \frac{4g}{a} \cdot \frac{a}{4} = g$	M1 A1 (2)
(d)	$x = \frac{a}{4} \sin \omega t; \frac{a}{8} = \frac{a}{4} \sin \omega t$ $\omega t = \sin^{-1} \frac{1}{2} = \pi/6$ $t = \frac{\pi}{2\omega} \sqrt{\frac{a}{g}}$	<p> <math>\rightarrow</math> M1 A1  <math>\rightarrow</math> M1 A1                      A1 ✓ (5)                 </p>
OR:	Circle approach: $\theta = \frac{\pi}{2} - \cos^{-1} \frac{1}{2} = \frac{\pi}{2} - \frac{\pi}{3} = \frac{\pi}{6}$ $\omega t = \pi/6$ $t = \frac{\pi}{2\omega} \sqrt{\frac{a}{g}}$	<p>                     OR <math>\rightarrow</math> M1 A1  <math>\rightarrow</math> M1 A1                      A1 ✓ (5)                 </p>
OR:	$\cos^{-1}(-\frac{1}{2}) - \cos^{-1}(0) = \frac{2\pi}{3} - \frac{\pi}{2} = \frac{\pi}{6}$ $\omega t = \pi/6$ $t = \frac{\pi}{2\omega} \sqrt{\frac{a}{g}}$	<p>                     OR <math>\rightarrow</math> M1 A1  <math>\rightarrow</math> M1 A1                      A1 ✓ (5)                 </p>
		(16)

Question	Solution	Markscheme
7.(d)	$\theta = \frac{\pi}{2} - \cos^{-1} \frac{1}{2} = \frac{\pi}{6}$ $\omega t = \frac{\pi}{6}$ $t = \frac{\pi}{6} \sqrt{\frac{a}{4g}} = \frac{\pi}{12} \sqrt{\frac{a}{g}}$	$\left[ \begin{array}{l} M1 A1 \\ M1 A1 \end{array} \right]$ <p>A1 f.t.</p>
<u>OR:</u>	$\cos^{-1}(-\frac{1}{2}) - \cos^{-1}(0) = \frac{2\pi}{3} - \frac{\pi}{2} = \frac{\pi}{6}$ $\omega t = \frac{\pi}{6}$ $t = \frac{\pi}{6} \sqrt{\frac{a}{4g}} = \frac{\pi}{12} \sqrt{\frac{a}{g}}$	$\left[ \begin{array}{l} M1 A1 \\ M1 A1 \end{array} \right]$ <p>A1 f.t.</p>