Centre No.				Paper Reference			Surname	Initial(s)			
Candidate No.			6	6	6	7	/	0	1	Signature	

Paper Reference(s)

### 6667/01

## **Edexcel GCE**

# Further Pure Mathematics FP1 Advanced/Advanced Subsidiary

Monday 30 January 2012 - Morning

Time: 1 hour 30 minutes

Materials required for examination	Items included with question paper
Mathematical Formulae (Pink)	Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.

#### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

#### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 9 questions in this question paper. The total mark for this paper is 75.

There are 24 pages in this question paper. Any blank pages are indicated.

#### **Advice to Candidates**

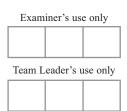
You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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Turn over

Total

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		Leave blank
1.	Given that $z_1 = 1 - i$ ,	
1.		
	(a) find $arg(z_1)$ . (2)	
	Given also that $z_2 = 3 + 4i$ , find, in the form $a + ib$ , $a, b \in \mathbb{R}$ ,	
	(b) $z_1 z_2$ ,	
	(2)	
	(c) $\frac{z_2}{z_1}$ . (3)	
	$z_1$	
	In part (b) and part (c) you must show all your working clearly.	
		1



. (:	٥)	Show that $f(x) = x^4 + x - 1$ has a real root $\alpha$ in the interval [0.5, 1.0].
• (	a)	Show that $T(x) = x + x - 1$ has a real root $\alpha$ in the interval [0.3, 1.0]. (2)
(1	b)	Starting with the interval [0.5, 1.0], use interval bisection twice to find an interval of
		width 0.125 which contains $\alpha$ .
		(3)
(	c)	Taking 0.75 as a first approximation, apply the Newton Raphson process twice to
		$f(x)$ to obtain an approximate value of $\alpha$ . Give your answer to 3 decimal places.
		(5)

(b) Show that the equation of the normal to $C$ at $P$ is $y + tx = 8t + 4t^3$ . (5)	A parabola $C$ has cartesian equation $y^2 = 16x$ . The point $P(4t^2, 8t)$ is a gen on $C$ .  (a) Write down the coordinates of the focus $F$ and the equation of the directrix	
	(b) Show that the equation of the normal to C at P is $y + tx = 8t + 4t^3$ .	



- 4. A right angled triangle *T* has vertices A(1, 1), B(2, 1) and C(2, 4). When *T* is transformed by the matrix  $\mathbf{P} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ , the image is T'.
  - (a) Find the coordinates of the vertices of T'. (2)
  - (b) Describe fully the transformation represented by **P**. (2)

The matrices  $\mathbf{Q} = \begin{pmatrix} 4 & -2 \\ 3 & -1 \end{pmatrix}$  and  $\mathbf{R} = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$  represent two transformations. When T is transformed by the matrix  $\mathbf{Q}\mathbf{R}$ , the image is T''.

(c) Find QR.

**(2)** 

(d) Find the determinant of **QR**.

**(2)** 

(e) Using your answer to part (d), find the area of T''.

(3)

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5.	The roots	of the	equation
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$$z^3 - 8z^2 + 22z - 20 = 0$$

are  $z_1$ ,  $z_2$  and  $z_3$ .

(a) Given that  $z_1 = 3 + i$ , find  $z_2$  and  $z_3$ .

**(4)** 

(b) Show, on a single Argand diagram, the points representing  $z_1$ ,  $z_2$  and  $z_3$ .

**(2)** 



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**6.** (a) Prove by induction

$$\sum_{r=1}^{n} r^3 = \frac{1}{4} n^2 (n+1)^2$$
 (5)

(b) Using the result in part (a), show that

$$\sum_{r=1}^{n} (r^3 - 2) = \frac{1}{4} n(n^3 + 2n^2 + n - 8)$$
(3)

(c) Calculate the exact value of  $\sum_{r=20}^{50} (r^3 - 2)$ . (3)

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7.	. <i>F</i>	A sequence	can be	descri	bed by	the	recurrence	formul	la
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$$u_{n+1} = 2u_n + 1,$$
  $n \ge 1, u_1 = 1$ 

(a) Find  $u_2$  and  $u_3$ .

**(2)** 

(b) Prove by induction that  $u_n = 2^n - 1$ 

(5)

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8.	$\Lambda = \begin{pmatrix} 0 \\ \end{pmatrix}$	1
0.	$\mathbf{A} = \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix}$	3

(a) Show that **A** is non-singular. (2)

(b) Find **B** such that  $\mathbf{B}\mathbf{A}^2 = \mathbf{A}$ . **(4)** 



**9.** The rectangular hyperbola H has cartesian equation xy = 9

The points  $P\left(3p, \frac{3}{p}\right)$  and  $Q\left(3q, \frac{3}{q}\right)$  lie on H, where  $p \neq \pm q$ .

(a) Show that the equation of the tangent at P is  $x + p^2y = 6p$ .

**(4)** 

(b) Write down the equation of the tangent at Q.

**(1)** 

The tangent at the point P and the tangent at the point Q intersect at R.

(c) Find, as single fractions in their simplest form, the coordinates of R in terms of p and q.

**(4)**