Centre No.					Pape	er Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	9	/	0	1	Signature	

Paper Reference(s)

6669/01

Edexcel GCE

Further Pure Mathematics FP3 Advanced/Advanced Subsidiary

Monday 28 June 2010 – Afternoon

Time: 1 hour 30 minutes

Materials required for examination	Items included with question papers
Mathematical Formulae (Pink)	Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 8 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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Turn over

Total



1. The	e line $x = 8$	is a	directrix	of the	ellipse	with equation
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$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, \quad a > 0, \ b > 0,$$

Find the value of a and the value of b .					



	Use calculus to find the exact value of $\int_{-2}^{1} \frac{1}{x^2 + 4x + 13} dx$.	(5)

3.	(a)	Starting from the definitions of $\sinh x$ and $\cosh x$ in terms of exponentials, prothat $\cosh 2x = 1 + 2\sinh^2 x$	ove
			(3)
	(b)	Solve the equation	
	(0)	$\cosh 2x - 3\sinh x = 15,$	
		giving your answers as exact logarithms.	
			(5)

- **4.** $I_n = \int_0^a (a-x)^n \cos x \, dx, \quad a > 0, \quad n \geqslant 0$
 - (a) Show that, for $n \ge 2$,

$$I_n = na^{n-1} - n(n-1)I_{n-2}$$

(5)

(b) Hence evaluate $\int_{0}^{\frac{\pi}{2}} \left(\frac{\pi}{2} - x\right)^{2} \cos x \, dx.$

(3)

estion 4 continued		



5. Given that $y = (\operatorname{arcosh} 3x)^2$, where 3x > 1, show that

(a)	$(9x^2 - 1)\left(\frac{\mathrm{d}y}{\mathrm{d}x}\right)^2 = 36$	iy,	
	(ax)		(5)

(b)
$$(9x^2 - 1)\frac{d^2y}{dx^2} + 9x\frac{dy}{dx} = 18$$
. (4)



$$\mathbf{M} = \begin{pmatrix} 1 & 0 & 3 \\ 0 & -2 & 1 \\ k & 0 & 1 \end{pmatrix}, \text{ where } k \text{ is a constant.}$$

Given that $\begin{pmatrix} 6 \\ 1 \end{pmatrix}$ is an eigenvector of **M**,

- (a) find the eigenvalue of **M** corresponding to $\begin{pmatrix} 6 \\ 1 \\ 6 \end{pmatrix}$, **(2)**
- (b) show that k = 3,

(2)

(c) show that **M** has exactly two eigenvalues.

(4)

A transformation $T: \mathbb{R}^3 \to \mathbb{R}^3$ is represented by **M**.

The transformation T maps the line l_1 , with cartesian equations $\frac{x-2}{1} = \frac{y}{-3} = \frac{z+1}{4}$, onto the line l_2 .

(d) Taking k = 3, find cartesian equations of l_2 .

(5)

uestion 6 continued	



7. The plane Π has vector equation

$$\mathbf{r} = 3\mathbf{i} + \mathbf{k} + \lambda (-4\mathbf{i} + \mathbf{j}) + \mu (6\mathbf{i} - 2\mathbf{j} + \mathbf{k})$$

(a) Find an equation of Π in the form $\mathbf{r.n} = p$, where \mathbf{n} is a vector perpendicular to Π and p is a constant.

(5)

The point P has coordinates (6, 13, 5). The line l passes through P and is perpendicular to Π . The line l intersects Π at the point N.

(b) Show that the coordinates of N are (3, 1, -1).

(4)

The point R lies on Π and has coordinates (1,0,2).

(c) Find the perpendicular distance from *N* to the line *PR*. Give your answer to 3 significant figures.

(5)



8. The hyperbola *H* has equation $\frac{x^2}{16} - \frac{y^2}{4} = 1$.

The line l_1 is the tangent to H at the point $P(4 \sec t, 2 \tan t)$.

(a) Use calculus to show that an equation of l_1 is

$$2y\sin t = x - 4\cos t$$

(5)

(8)

The line l_2 passes through the origin and is perpendicular to l_1 .

The lines l_1 and l_2 intersect at the point Q.

(b) Show that, as t varies, an equation of the locus of Q is

$$(x^2 + y^2)^2 = 16x^2 - 4y^2$$

Question 8 continued		blank
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		Q8
	(Total 13 marks)	
END	TOTAL FOR PAPER: 75 MARKS	