Write your name here Surname	Other nan	nes
Pearson	Centre Number	Candidate Number
Edexcel GCE		
Further P Mathema Advanced/Advance	atics FP3	
Monday 26 June 2017 – A	Afternoon	Paper Reference
Time: 1 hour 30 minute		6669/01

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for each question are shown in brackets
 use this as a quide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶



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$dv = \operatorname{sech}^2 x$	
$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{sech}^2 x}{\sqrt{1 + \tanh^2 x}}$	(5
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Question 1 continued		olan
	Q1	1
	(Total 5 marks)	



2. The ellipse E has equation

$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$

The line *l* is the normal to *E* at the point *P* (6 cos θ , 5 sin θ), where $0 < \theta < \frac{\pi}{2}$

(a) Use calculus to show that an equation of l is

$$6x\sin\theta - 5y\cos\theta = 11\sin\theta\cos\theta$$

(5)

The line l meets the x-axis at the point Q.

The point R is the foot of the perpendicular from P to the x-axis.

(b) Show that $\frac{OQ}{OR} = e^2$, where e is the eccentricity of the ellipse E.

(4)

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Question 2 continued	
Question 2 continued	
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Question 2 continued		

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3.	(a) Using the definition for cosh x in terms of exponentials, show th	at
	$\cosh 2x \equiv 2\cosh^2 x - 1$	(3)
	(b) Find the exact values of x for which	(-)
	(b) Find the exact values of x for which	
	$29\cosh x - 3\cosh 2x = 38$	
	giving your answers in terms of natural logarithms.	
		(6)

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Question 3 continued	



Question 3 continue	d		

Question 3 continued	
-	23
(Total 9 marks)	



Use the substitution $x + 2 = u^2$, where u > 0, to show that

$$\int_{-1}^{7} \frac{(x+2)^{\frac{1}{2}}}{x+5} \, \mathrm{d}x = a + b\pi\sqrt{3}$$

where a	and h	are	rational	numbers	to b	e found	1

where a and b are rational numbers to be found.	(9)

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Question 4 continued		

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Question 4 continued		
		Q4
	(Total 9 marks)	



5.	The plane Π_1 has equation $x - 2y - 3z = 5$ and the plane Π_2 has equation $6x + y - 4z = 7$
	(a) Find, to the nearest degree, the acute angle between Π_1 and Π_2
	(a) Find, to the hearest degree, the acute angle between H_1 and H_2
	The point P has coordinates $(2, 3, -1)$. The line l is perpendicular to Π_1 and passes through the point P . The line l intersects Π_2 at the point Q .
	(b) Find the coordinates of Q .
	(4)
	The plane Π_3 passes through the point Q and is perpendicular to Π_1 and Π_2
	(c) Find an equation of the plane Π_3 in the form $\mathbf{r} \cdot \mathbf{n} = p$
	(4)

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Question 5 contin	ued		

Question 5 continued		Leave blank
		Q5
	(Total 11 marks)	



6. The matrix \mathbf{M} is given by

$$\mathbf{M} = \begin{pmatrix} 1 & k & 0 \\ 2 & -2 & 1 \\ -4 & 1 & -1 \end{pmatrix}, k \in \mathbb{R}, k \neq \frac{1}{2}$$

(a) Show that det $\mathbf{M} = 1 - 2k$.

(2)

(b) Find \mathbf{M}^{-1} in terms of k.

(4)

The straight line l_1 is mapped onto the straight line l_2 by the transformation represented by the matrix

$$\begin{pmatrix}
1 & 0 & 0 \\
2 & -2 & 1 \\
-4 & 1 & -1
\end{pmatrix}$$

Given that l_2 has cartesian equation

$$\frac{x-1}{5} = \frac{y+2}{2} = \frac{z-3}{1}$$

(c) find a cartesian equation of the line l_1

(6)

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Question 6 continued	



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		Q6
	(Total 12 marks)	



7.

$$I_n = \int_0^{\ln 2} \cosh^n x \, dx, \quad n \geqslant 0$$

(a) Show that, for $n \ge 2$,

$$I_n = \frac{3a^{n-1}}{nb^n} + \frac{n-1}{n}I_{n-2}$$

where a and b are integers to be found.

(6)

(b) Hence, or otherwise, find the exact value of

$$\int_0^{\ln 2} \cosh^4 x \, dx$$

(4)

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	(Total 10 marks)	



8. The curve C has equation

$$y = \ln\left(\frac{e^x + 1}{e^x - 1}\right), \quad \ln 2 \leqslant x \leqslant \ln 3$$

(a) Show that

$$\frac{\mathrm{d}y}{\mathrm{d}x} = -\frac{2\mathrm{e}^x}{\mathrm{e}^{2x} - 1}$$

(b) Find the length of the curve C, giving your answer in the form $\ln a$, where a is a rational number.

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TOTAL FOR PAPER: 75 MARKS	
(Total 10 marks)	
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