FP2 Specimen

1.
$$\frac{x}{x-3}$$
, $\frac{1}{x-2}$ => $\frac{x(x-2)^2(x-3)^2}{x-3}$, $\frac{(x-2)^2(x-3)^2}{x-2}$

=)
$$x(x-3)(x-2)^2 - (x-2)(x-3)^2 > 0$$

=)
$$(x-2)(x-3)[x(x-2)-(x-3)]>0$$

both the when
$$x > 3$$
 $(x - \frac{3}{2})^2 + \frac{3}{4} \Rightarrow \text{always positive}$.

both the when $x > 3$ $(x > 3) \cup (x < 2)$

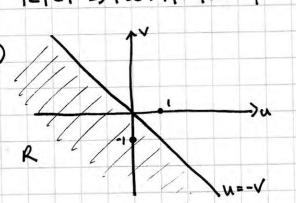
2)
$$\frac{1}{r^2} - \frac{1}{(r+1)^2} = \frac{(r+1)^2 - r^2}{r^2(r+1)^2} = \frac{2r+1}{r^2(r+1)^2}$$

5)
$$\sqrt{\frac{2r+1}{r^2(r+1)^2}} \quad r = 1 \quad \left(\frac{1}{1} - \frac{1}{4}\right) \quad + \quad r = n-1 \quad \left(\frac{1}{(p-1)^2} + \frac{1}{n^2}\right) \quad + \quad \left(\frac{1}{(p-1)^2} + \frac{1}{n^2}\right) \quad + \quad \left(\frac{1}{(p-1)^2} + \frac{1}{(p-1)^2}\right) \quad + \quad \left(\frac{1}{(p-1)^2} +$$

$$r=3\left(\frac{1}{4}-\frac{1}{16}\right)+r=n\left(\frac{1}{2}-\frac{1}{(n+1)^2}\right)$$

$$\therefore \int \frac{2r+1}{r^2(r+1)^2} = 1 - \frac{1}{(n+1)^2}$$

3)
$$\omega = \frac{z-i}{z+1}$$
 => $\omega z + \omega = z - i$ => $\omega + i = z - \omega z$



$$\frac{d}{dx} \left(\frac{d^{2}y}{dx^{2}} \right) + \frac{d}{dx} \left(y \frac{dy}{dx} \right) = \frac{d}{dx} (x)$$

$$\frac{d^{3}y}{dx^{2}} + y \frac{d^{2}y}{dx^{2}} \left(\frac{dy}{dx} \right)^{2} = 1$$

$$y''' + 0 + (2)^{2} = 1$$

$$y'' + 0 + (2)^{2} = 1$$

$$y' + 0 + (2)^{2} = 1$$

$$y'' + 0 + (2)^{2} = 1$$

$$y'' + 0 + (2)^{2}$$

y"+yy'=x

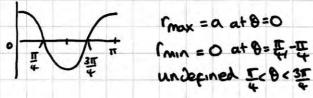
5"+0=1 => 5"=1

5)
$$\frac{dS}{dt} = 0.1S = t$$
 IF $f(x) = e^{\int -0.1 dt} = e^{-0.1 t}$

4) dry + y dy = x y=0

t=10 S=300e-200 => S= £615 million

6)
$$r^2 = a^2 \cos 2\theta$$



$$y = r Sin\theta = \alpha (\cos 2\theta)^{\frac{1}{2}} \times Sin\theta$$

$$\frac{dy}{d\theta} = \frac{1}{2} a ((0.20)^{-\frac{1}{2}} - 2 \sin 20 \times \sin \theta + a ((0.520)^{\frac{1}{2}} \times (0.50)^{\frac{1}{2}} \times (0.50)$$

$$\Gamma^2 = \alpha^2 \cos \frac{\pi}{3} \Rightarrow \Gamma^2 = \frac{1}{2}\alpha^2 \Rightarrow \Gamma = \frac{1}{\sqrt{2}}\alpha \Rightarrow \Gamma = \frac{\sqrt{2}}{2}\alpha$$

c) Area =
$$\frac{1}{2}a^{2}\int_{0}^{\pi_{4}}\cos 2\theta d\theta = \frac{1}{2}a^{2}\left[\frac{1}{2}\sin 2\theta\right]_{\frac{\pi}{4}}^{\frac{\pi}{4}}$$

= $\frac{1}{2}a^{2}\left[\left(\frac{1}{2}\right)-\left(-\frac{1}{2}\right)\right] = \frac{1}{2}a^{2}$

7)
$$x = e^{t}$$
 $\Rightarrow \frac{dx}{dt} = e^{t}$ $\frac{dt}{dx} = e^{-t}$

$$\frac{d}{dx}\left(\frac{dy}{dx}\right) = \frac{d^2y}{dx^2} = \frac{d}{dx}\left(e^{-t}\frac{dy}{dt}\right) = \left[\frac{d}{dx}\left(e^{-t}\right)\right]\frac{dy}{dt} + e^{-t}\left[\frac{d}{dx}\left(\frac{dy}{dt}\right)\right]$$

7b)
$$x^{2} \frac{dy}{dx^{2}} - 2x \frac{dy}{dx} + 2y = x^{3}$$
 $e^{2k} \left[e^{-2k} \left(\frac{d^{2}y}{dk^{2}} - \frac{dy}{dk} \right) \right] - 2e^{k} \left[e^{-k} \frac{dy}{dk^{2}} \right] + 2y = e^{3k}$
 $= \frac{d^{2}y}{dk^{2}} - 3 \frac{dy}{dk} + 2y = e^{3k}$
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 $= \frac{d^{2}y}{dk^{2}} - 3 \frac{dy}{dk} + 2y = e^$

$$y = \lambda e^{3t}$$

$$y' = 3\lambda e^{3t}$$

$$y'' = 9\lambda e^{3t}$$

$$q\lambda e^{3t} - q\lambda e^{3t} + 2\lambda e^{3t} = e^{3t}$$

$$\therefore y = Ae^{t} + Be^{2t} + \frac{1}{2}e^{3t}$$

$$= y = Ax + Bx^{2} + \frac{1}{2}x^{3}$$

$$= \frac{2l + 1}{2l} = e^{iP\theta} + e^{-iP\theta}$$

$$= \frac{(os l\theta + iSin l\theta)}{(os (-l\theta) + iSin (-l\theta))} + \frac{(os l\theta + iSin l\theta)}{(os l\theta - iSin l\theta)}$$

$$= \frac{(os l\theta + iSin (-l\theta))}{(os l\theta - iSin l\theta)}$$

$$= \frac{2(os l\theta)}{2(os l\theta)} + \frac{1}{2(os l\theta)}$$

$$= \frac{(os l\theta + iSin l\theta)}{(os l\theta - iSin l\theta)}$$

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z-P=(ei0)P=e-ipo

z = e i 0 => z = (e i 0) = e i po

 $(Z+1)^4 = Z^4 + 4Z^3(\frac{1}{2}) + 6Z^2(\frac{1}{2}) + 4Z(\frac{1}{2}) + (\frac{1}{24})$

 $= \left(\frac{Z^4 + \frac{1}{Z^4}}{Z^4} \right) + 4 \left(\frac{Z^2 + \frac{1}{Z^2}}{Z^2} \right) + 6$

8)

=)
$$16\cos^{4}\theta = 2\cos 4\theta + 8\cos 2\theta + 6$$

: $\cos^{4}\theta = \frac{1}{8}\cos 4\theta + \frac{1}{2}\cos 2\theta + \frac{3}{8}$
=) $\cos^{4}\theta = \frac{1}{8}\cos 4\theta + \frac{1}{2}\cos 2\theta + \frac{3}{8}$
c) Volume = $\pi \left(u^{2}dx = \pi \left(\cos^{4}\theta d\theta = \frac{1}{4}\pi \left(\cos 4\theta + \frac{1}{8}\cos 2\theta + 3d\theta\right)\right)\right)$

c) Volume =
$$\pi \int y^2 dx = \pi \int \cos^4\theta d\theta = \frac{1}{8}\pi \int \cos^4\theta + \frac{1}{8}\cos^2\theta + 3d\theta$$

= $\frac{1}{8}\pi \left[\frac{1}{4}\sin^4\theta + \frac{1}{8}\sin^2\theta + 3\theta \right]^{\frac{1}{2}} = \frac{1}{8}\pi \left[\frac{3\pi}{2} - \frac{3\pi}{2} \right] = \frac{3}{8}\pi^2$