Assignment 4 - Naive Machine Translation and LSH

You will now implement your first machine translation system and then you will see how locality sensitive hashing works. Let's get started by importing the required functions!

If you are running this notebook in your local computer, don't forget to download the twitter samples and stopwords from nltk.

```
nltk.download('stopwords')
nltk.download('twitter_samples')
```

Important Note on Submission to the AutoGrader

Before submitting your assignment to the AutoGrader, please make sure you are not doing the following:

- 1. You have not added any extra print statement(s) in the assignment.
- 2. You have not added any extra code cell(s) in the assignment.
- 3. You have not changed any of the function parameters.
- 4. You are not using any global variables inside your graded exercises. Unless specifically instructed to do so, please refrain from it and use the local variables instead.
- 5. You are not changing the assignment code where it is not required, like creating *extra* variables.

If you do any of the following, you will get something like, Grader Error: Grader feedback not found (or similarly unexpected) error upon submitting your assignment. Before asking for help/debugging the errors in your assignment, check for these first. If this is the case, and you don't remember the changes you have made, you can get a fresh copy of the assignment by following these instructions (<a href="https://www.coursera.org/learn/classification-vector-spaces-in-nlp/supplement/YLuAg/h-ow-to-refresh-your-workspace).

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```
In [85]: # add folder, tmp2, from our local workspace containing pre-downloaded corpora
filePath = f"{getcwd()}/tmp2/"
nltk.data.path.append(filePath)
```

1. The Word Embeddings Data for English and French Words

Write a program that translates English to French.

The Data

The full dataset for English embeddings is about 3.64 gigabytes, and the French embeddings are about 629 megabytes. To prevent the Coursera workspace from crashing, we've extracted a subset of the embeddings for the words that you'll use in this assignment.

The subset of data

To do the assignment on the Coursera workspace, we'll use the subset of word embeddings.

```
In [86]: en_embeddings_subset = pickle.load(open("./data/en_embeddings.p", "rb"))
fr_embeddings_subset = pickle.load(open("./data/fr_embeddings.p", "rb"))
```

Look at the data

• en_embeddings_subset: the key is an English word, and the value is a 300 dimensional array, which is the embedding for that word.

```
'the': array([ 0.08007812, 0.10498047, 0.04980469, 0.0534668, -0.06738281, ....
```

• fr_embeddings_subset: the key is a French word, and the value is a 300 dimensional array, which is the embedding for that word.

```
'la': array([-6.18250e-03, -9.43867e-04, -8.82648e-03, 3.24623e-02,...
```

Load two dictionaries mapping the English to French words

- A training dictionary
- · and a testing dictionary.

```
In [35]: # loading the english to french dictionaries
    en_fr_train = get_dict('./data/en-fr.train.txt')
    print('The length of the English to French training dictionary is', len(en_fr_en_fr_test = get_dict('./data/en-fr.test.txt')
    print('The length of the English to French test dictionary is', len(en_fr_test)
```

The length of the English to French training dictionary is 5000 The length of the English to French test dictionary is 1500

Looking at the English French dictionary

• en_fr_train is a dictionary where the key is the English word and the value is the French translation of that English word.

```
{'the': 'la',
'and': 'et',
'was': 'était',
'for': 'pour',
```

• en_fr_test is similar to en_fr_train, but is a test set. We won't look at it until we get to testing.

1.1 Generate Embedding and Transform Matrices

Exercise 1 - get_matrices

Translating English dictionary to French by using embeddings.

You will now implement a function <code>get_matrices</code> , which takes the loaded data and returns matrices X and Y.

Inputs:

- en_fr : English to French dictionary
- en embeddings : English to embeddings dictionary
- fr_embeddings : French to embeddings dictionary

Returns:

• Matrix X and matrix Y, where each row in X is the word embedding for an english word, and the same row in Y is the word embedding for the French version of that English word.

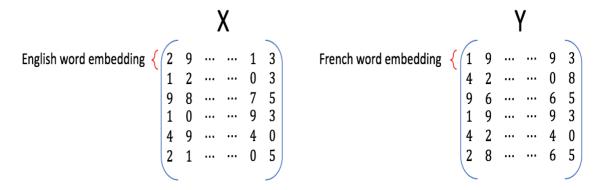


Figure 1

Use the en_fr dictionary to ensure that the ith row in the X matrix corresponds to the ith row in the Y matrix.

Instructions: Complete the function get_matrices() :

- Iterate over English words in en_fr dictionary.
- · Check if the word have both English and French embedding.

Hints

```
In [36]: # UNO C1 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def get_matrices(en_fr, french_vecs, english_vecs):
             Creates matrices of word embeddings for English and French words that are
             Inputs:
                 en_fr: Dictionary mapping English words to French words.
                 french_vecs: Dictionary of French word embeddings.
                 english_vecs: Dictionary of English word embeddings.
             Outputs:
                 X: Matrix with each row being the embedding of an English word. Shape
                 Y: Matrix with each row being the embedding of the corresponding Frend
             Note:
                 This function does not compute or return a projection matrix.
             ### START CODE HERE ###
             # X_l and Y_l are lists of the english and french word embeddings
             X l = list()
             Y_1 = list()
             # get the english words (the keys in the dictionary) and store in a set()
             english_set = set(english_vecs.keys())
             # get the french words (keys in the dictionary) and store in a set()
             french_set = set(french_vecs.keys())
             # store the french words that are part of the english-french dictionary (t
             french_words = set(en_fr.values())
             # loop through all english, french word pairs in the english french diction
             for en_word, fr_word in en_fr.items():
                 # check that the french word has an embedding and that the english wor
                 if fr_word in french_set and en_word in english_set:
                     # get the english embedding
                     en_vec = english_vecs[en_word]
                     # get the french embedding
                     fr_vec = french_vecs[fr_word]
                     # add the english embedding to the list
                     X_1.append(en_vec)
                     # add the french embedding to the list
                     Y_1.append(fr_vec)
             # stack the vectors of X_l into a matrix X
             X = np.vstack(X_1)
             # stack the vectors of Y L into a matrix Y
             Y = np.vstack(Y 1)
             ### END CODE HERE ###
```

Now we will use function <code>get_matrices()</code> to obtain sets <code>X_train</code> and <code>Y_train</code> of English and French word embeddings into the corresponding vector space models.

```
In [38]: # Test your function
w4_unittest.test_get_matrices(get_matrices)
```

All tests passed

2 - Translations



Figure 2

Write a program that translates English words to French words using word embeddings and vector space models.

2.1 - Translation as Linear Transformation of Embeddings

Given dictionaries of English and French word embeddings you will create a transformation matrix R

- Given an English word embedding, ${f e}$, you can multiply ${f e}{f R}$ to get a new word embedding ${f f}$.
 - Both e and f are <u>row vectors</u> (<u>https://en.wikipedia.org/wiki/Row_and_column_vectors</u>).
- You can then compute the nearest neighbors to f in the french embeddings and recommend the word that is most similar to the transformed word embedding.

Describing translation as the minimization problem

Find a matrix R that minimizes the following equation.

$$\arg\min_{\mathbf{R}} \|\mathbf{X}\mathbf{R} - \mathbf{Y}\|_F \tag{1}$$

Frobenius norm

The Frobenius norm of a matrix A (assuming it is of dimension m, n) is defined as the square root of the sum of the absolute squares of its elements:

$$\|\mathbf{A}\|_{F} \equiv \sqrt{\sum_{i=1}^{m} \sum_{j=1}^{n} |a_{ij}|^{2}}$$
 (2)

Actual loss function

In the real world applications, the Frobenius norm loss:

$$\|\mathbf{X}\mathbf{R} - \mathbf{Y}\|_F$$

is often replaced by it's squared value divided by m:

$$\frac{1}{m}\|\mathbf{X}\mathbf{R}-\mathbf{Y}\|_F^2$$

where m is the number of examples (rows in \mathbf{X}).

- The same R is found when using this loss function versus the original Frobenius norm.
- The reason for taking the square is that it's easier to compute the gradient of the squared Frobenius.
- The reason for dividing by *m* is that we're more interested in the average loss per embedding than the loss for the entire training set.
 - The loss for all training set increases with more words (training examples), so taking the average helps us to track the average loss regardless of the size of the training set.

[Optional] Detailed explanation why we use norm squared instead of the norm: Click for optional details

Implementing translation mechanism described in this section.

Exercise 2 - compute loss

Step 1: Computing the loss

- The loss function will be squared Frobenius norm of the difference between matrix and its approximation, divided by the number of training examples *m*.
- Its formula is:

$$L(X, Y, R) = \frac{1}{m} \sum_{i=1}^{m} \sum_{j=1}^{n} (a_{ij})^{2}$$

where a_{ij} is value in *i*th row and *j*th column of the matrix $\mathbf{XR} - \mathbf{Y}$.

Instructions: complete the compute_loss() function

Compute the approximation of Y by matrix multiplying X and R

- Compute difference XR Y
- Compute the squared Frobenius norm of the difference and divide it by *m*.

Hints

```
In [39]:
         # UNQ_C3 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def compute_loss(X, Y, R):
             1.1.1
             Inputs:
                 X: a matrix of dimension (m,n) where the columns are the English embed
                 Y: a matrix of dimension (m,n) where the columns correspong to the Fre
                 R: a matrix of dimension (n,n) - transformation matrix from English to
             Outputs:
                 L: a matrix of dimension (m,n) - the value of the loss function for gi
             ### START CODE HERE ###
             # m is the number of rows in X
             m = X.shape[0]
             # diff is XR - Y
             diff = X @ R - Y
             # diff_squared is the element-wise square of the difference
             diff_squared = diff ** 2
             # sum_diff_squared is the sum of the squared elements
             sum_diff_squared = np.sum(diff_squared)
             # loss i is the sum_diff_squared divided by the number of examples (m)
             loss = sum_diff_squared / m
             ### END CODE HERE ###
             return loss
```

Expected loss for an experiment with random matrices: 8.1866

Expected output:

Expected loss for an experiment with random matrices: 8.1866

```
In [41]: # Test your function
w4_unittest.test_compute_loss(compute_loss)
```

All tests passed

Exercise 3 - compute_gradient

Step 2: Computing the gradient of loss with respect to transform matrix R

- · Calculate the gradient of the loss with respect to transform matrix R.
- The gradient is a matrix that encodes how much a small change in R affect the change in the loss function.
- The gradient gives us the direction in which we should decrease R to minimize the loss.
- *m* is the number of training examples (number of rows in *X*).
- The formula for the gradient of the loss function L(X, Y, R) is:

$$\frac{d}{dR}L(X,Y,R) = \frac{d}{dR}\left(\frac{1}{m}\|XR - Y\|_F^2\right) = \frac{2}{m}X^T(XR - Y)$$

Instructions: Complete the compute gradient function below.

Hints

```
In [42]:
         # UNO C4 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def compute_gradient(X, Y, R):
             Inputs:
                 X: a matrix of dimension (m,n) where the columns are the English embed
                 Y: a matrix of dimension (m,n) where the columns correspong to the Fre
                 R: a matrix of dimension (n,n) - transformation matrix from English to
             Outputs:
                 g: a scalar value - gradient of the loss function L for given X, Y and
             ### START CODE HERE ###
             # m is the number of rows in X
             m = X.shape[0]
             # gradient is X^T(XR - Y) * 2/m
             gradient = (2 / m) * X.T @ (X @ R - Y)
             ### END CODE HERE ###
             return gradient
```

Expected output:

In [44]: # Test your function
 w4_unittest.test_compute_gradient(compute_gradient)

All tests passed

Step 3: Finding the optimal R with Gradient Descent Algorithm

Gradient Descent

<u>Gradient descent (https://ml-cheatsheet.readthedocs.io/en/latest/gradient_descent.html)</u> is an iterative algorithm which is used in searching for the optimum of the function.

- Earlier, we've mentioned that the gradient of the loss with respect to the matrix encodes how much a tiny change in some coordinate of that matrix affect the change of loss function.
- Gradient descent uses that information to iteratively change matrix R until we reach a point where the loss is minimized.

Training with a fixed number of iterations

Most of the time we iterate for a fixed number of training steps rather than iterating until the loss falls below a threshold.

OPTIONAL: explanation for fixed number of iterations click here for detailed discussion

Pseudocode:

- 1. Calculate gradient g of the loss with respect to the matrix R.
- 2. Update R with the formula:

$$R_{\text{new}} = R_{\text{old}} - \alpha g$$

Where α is the learning rate, which is a scalar.

Learning Rate

- The learning rate or "step size" α is a coefficient which decides how much we want to change R in each step.
- If we change R too much, we could skip the optimum by taking too large of a step.
- If we make only small changes to R, we will need many steps to reach the optimum.
- Learning rate α is used to control those changes.
- Values of α are chosen depending on the problem, and we'll use <code>learning_rate</code> = 0.0003 as the default value for our algorithm.

Exercise 4 - align_embeddings

Implement align_embeddings()

```
In [45]:
         # UNQ_C5 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def align_embeddings(X, Y, train_steps=100, learning_rate=0.0003, verbose=True
             Inputs:
                 X: a matrix of dimension (m,n) where the columns are the English embed
                 Y: a matrix of dimension (m,n) where the columns correspong to the Fre
                 train_steps: positive int - describes how many steps will gradient des
                 learning_rate: positive float - describes how big steps will gradient
             Outputs:
                 R: a matrix of dimension (n,n) - the projection matrix that minimizes
             np.random.seed(129)
             # the number of columns in X is the number of dimensions for a word vector
             # R is a square matrix with length equal to the number of dimensions in th
             R = np.random.rand(X.shape[1], X.shape[1])
             for i in range(train_steps):
                 if verbose and i % 25 == 0:
                     print(f"loss at iteration {i} is: {compute_loss(X, Y, R):.4f}")
                 ### START CODE HERE ###
                 # use the function that you defined to compute the gradient
                 gradient = compute_gradient(X, Y, R)
                 # update R by subtracting the Learning rate times gradient
                 R -= learning_rate * gradient
                 ### END CODE HERE ###
             return R
        # UNQ_C6 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
In [46]:
         # You do not have to input any code in this cell, but it is relevant to grading
         # Testing your implementation.
         np.random.seed(129)
         m = 10
         n = 5
         X = np.random.rand(m, n)
         Y = np.random.rand(m, n) * .1
         R = align\_embeddings(X, Y)
         loss at iteration 0 is: 3.7242
         loss at iteration 25 is: 3.6283
         loss at iteration 50 is: 3.5350
         loss at iteration 75 is: 3.4442
         Expected Output:
             loss at iteration 0 is: 3.7242
             loss at iteration 25 is: 3.6283
             loss at iteration 50 is: 3.5350
             loss at iteration 75 is: 3.4442
```

```
In [47]: # Test your function
w4_unittest.test_align_embeddings(align_embeddings)
```

All tests passed

Calculate Transformation matrix R

Using just the training set, find the transformation matrix ${\bf R}$ by calling the function align_embeddings() .

NOTE: The code cell below will take a few minutes to fully execute (~3 mins)

```
In [48]: # UNQ_C7 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
# You do not have to input any code in this cell, but it is relevant to gradin
R_train = align_embeddings(X_train, Y_train, train_steps=400, learning_rate=0.
```

```
loss at iteration 0 is: 963.0146
loss at iteration 25 is: 97.8292
loss at iteration 50 is: 26.8329
loss at iteration 75 is: 9.7893
loss at iteration 100 is: 4.3776
loss at iteration 125 is: 2.3281
loss at iteration 150 is: 1.4480
loss at iteration 175 is: 1.0338
loss at iteration 200 is: 0.8251
loss at iteration 225 is: 0.7145
loss at iteration 250 is: 0.6534
loss at iteration 275 is: 0.6185
loss at iteration 300 is: 0.5981
loss at iteration 325 is: 0.5858
loss at iteration 350 is: 0.5782
loss at iteration 375 is: 0.5735
```

Expected Output

```
loss at iteration 0 is: 963.0146
loss at iteration 25 is: 97.8292
loss at iteration 50 is: 26.8329
loss at iteration 75 is: 9.7893
loss at iteration 100 is: 4.3776
loss at iteration 125 is: 2.3281
loss at iteration 150 is: 1.4480
loss at iteration 175 is: 1.0338
loss at iteration 200 is: 0.8251
loss at iteration 225 is: 0.7145
loss at iteration 250 is: 0.6534
loss at iteration 275 is: 0.6185
loss at iteration 300 is: 0.5981
loss at iteration 325 is: 0.5858
loss at iteration 350 is: 0.5782
loss at iteration 375 is: 0.5735
```

2.2 - Testing the Translation

k-Nearest Neighbors Algorithm

k-Nearest neighbors algorithm (https://en.wikipedia.org/wiki/K-nearest_neighbors_algorithm)

- k-NN is a method which takes a vector as input and finds the other vectors in the dataset that are closest to it.
- The 'k' is the number of "nearest neighbors" to find (e.g. k=2 finds the closest two neighbors).

Searching for the Translation Embedding

Since we're approximating the translation function from English to French embeddings by a linear transformation matrix \mathbf{R} , most of the time we won't get the exact embedding of a French word when we transform embedding \mathbf{e} of some particular English word into the French embedding space.

• This is where k-NN becomes really useful! By using 1-NN with \mathbf{eR} as input, we can search for an embedding \mathbf{f} (as a row) in the matrix \mathbf{Y} which is the closest to the transformed vector \mathbf{eR}

Cosine Similarity

Cosine similarity between vectors u and v calculated as the cosine of the angle between them. The formula is

$$\cos(u, v) = \frac{u \cdot v}{\|u\| \|v\|}$$

- cos(u, v) = 1 when u and v lie on the same line and have the same direction.
- cos(u, v) is -1 when they have exactly opposite directions.
- cos(u, v) is 0 when the vectors are orthogonal (perpendicular) to each other.

Note: Distance and similarity are pretty much opposite things.

- We can obtain distance metric from cosine similarity, but the cosine similarity can't be used directly as the distance metric.
- When the cosine similarity increases (towards 1), the "distance" between the two vectors decreases (towards 0).
- We can define the cosine distance between u and v as

$$d_{\cos}(u, v) = 1 - \cos(u, v)$$

Exercise 5 - nearest_neighbor

Complete the function nearest_neighbor()

Inputs:

- Vector v ,
- A set of possible nearest neighbors candidates

- · k nearest neighbors to find.
- The distance metric should be based on cosine similarity.
- cosine_similarity function is already implemented and imported for you. It's
 arguments are two vectors and it returns the cosine of the angle between them.
- Iterate over rows in candidates, and save the result of similarities between current row and vector v in a python list. Take care that similarities are in the same order as row vectors of candidates.
- Now you can use <u>numpy argsort</u>
 (https://docs.scipy.org/doc/numpy/reference/generated/numpy.argsort.html#numpy.argsort)
 to sort the indices for the rows of candidates.

Hints

```
In [49]:
         # UNQ_C8 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def nearest_neighbor(v, candidates, k=1, cosine_similarity=cosine_similarity):
             Input:
               - v, the vector you are going find the nearest neighbor for
               - candidates: a set of vectors where we will find the neighbors
               - k: top k nearest neighbors to find
             Output:
               - k_idx: the indices of the top k closest vectors in sorted form
             ### START CODE HERE ###
             similarity_l = []
             # for each candidate vector...
             for row in candidates:
                 # get the cosine similarity
                 cos_similarity = cosine_similarity(v, row)
                 # append the similarity to the list
                 similarity_l.append(cos_similarity)
             # sort the similarity list and get the indices of the sorted list
             sorted_ids = np.argsort(similarity_1)
             # Reverse the order of the sorted_ids array
             sorted_ids = sorted_ids[::-1]
             # get the indices of the k most similar candidate vectors
             k idx = sorted ids[:k]
             ### END CODE HERE ###
             return k idx
```

```
In [50]: # UNQ_C9 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
# You do not have to input any code in this cell, but it is relevant to gradin
# Test your implementation:
v = np.array([1, 0, 1])
candidates = np.array([[1, 0, 5], [-2, 5, 3], [2, 0, 1], [6, -9, 5], [9, 9, 9]
print(candidates[nearest_neighbor(v, candidates, 3)])
```

```
[[2 0 1]
[1 0 5]
[9 9 9]]
```

Expected Output:

```
[[2 0 1]
[1 0 5]
[9 9 9]]
```

```
In [51]: # Test your function
w4_unittest.test_nearest_neighbor(nearest_neighbor)
```

All tests passed

Test your Translation and Compute its Accuracy

Exercise 6 - test_vocabulary

Complete the function $test_vocabulary$ which takes in English embedding matrix X, French embedding matrix Y and the R matrix and returns the accuracy of translations from X to Y by R.

- Iterate over transformed English word embeddings and check if the closest French word vector belongs to French word that is the actual translation.
- Obtain an index of the closest French embedding by using nearest_neighbor (with argument k=1), and compare it to the index of the English embedding you have just transformed.
- Keep track of the number of times you get the correct translation.
- Calculate accuracy as

 $accuracy = \frac{\#(correct predictions)}{\#(total predictions)}$

```
# UNO C10 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
def test_vocabulary(X, Y, R, nearest_neighbor=nearest_neighbor):
    Input:
        X: a matrix where the columns are the English embeddings.
        Y: a matrix where the columns correspong to the French embeddings.
        R: the transform matrix which translates word embeddings from
        English to French word vector space.
    Output:
        accuracy: for the English to French capitals
    ### START CODE HERE ###
    # The prediction is X times R
    pred = np.dot(X, R)
    # initialize the number correct to zero
    num correct = 0
    # Loop through each row in pred (each transformed embedding)
    for i in range(len(pred)):
        # get the index of the nearest neighbor of pred at row 'i'; also pass
        pred_idx = nearest_neighbor(pred[i], Y, k=1)[0]
        # if the index of the nearest neighbor equals the row of i... \
        if pred_idx == i:
            # increment the number correct by 1.
            num_correct += 1
    # accuracy is the number correct divided by the number of rows in 'pred' (
    accuracy = num_correct / len(pred)
    ### END CODE HERE ###
    return accuracy
```

Let's see how is your translation mechanism working on the unseen data:

```
In [53]: X_val, Y_val = get_matrices(en_fr_test, fr_embeddings_subset, en_embeddings_subset)
In [54]: # UNQ_C11 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
# You do not have to input any code in this cell, but it is relevant to gradin
acc = test_vocabulary(X_val, Y_val, R_train) # this might take a minute or tw
print(f"accuracy on test set is {acc:.3f}")
accuracy on test set is 0.557
```

Expected Output:

0.557

You managed to translate words from one language to another language without ever seing them with almost 56% accuracy by using some basic linear algebra and learning a mapping of words from one language to another!

```
In [55]: # Test your function
w4_unittest_test_vocabulary(test_vocabulary)
```

All tests passed

3 - LSH and Document Search

In this part of the assignment, you will implement a more efficient version of k-nearest neighbors using locality sensitive hashing. You will then apply this to document search.

- Process the tweets and represent each tweet as a vector (represent a document with a vector embedding).
- Use locality sensitive hashing and k nearest neighbors to find tweets that are similar to a
 given tweet.

```
In [56]: # get the positive and negative tweets
all_positive_tweets = twitter_samples.strings('positive_tweets.json')
all_negative_tweets = twitter_samples.strings('negative_tweets.json')
all_tweets = all_positive_tweets + all_negative_tweets
```

3.1 - Getting the Document Embeddings

Bag-of-words (BOW) Document Models

Text documents are sequences of words.

- The ordering of words makes a difference. For example, sentences "Apple pie is better than pepperoni pizza." and "Pepperoni pizza is better than apple pie" have opposite meanings due to the word ordering.
- However, for some applications, ignoring the order of words can allow us to train an efficient and still effective model.
- This approach is called Bag-of-words document model.

Document Embeddings

- Document embedding is created by summing up the embeddings of all words in the document.
- If we don't know the embedding of some word, we can ignore that word.

Exercise 7 - get_document_embedding

Complete the get_document_embedding() function.

- The function get_document_embedding() encodes entire document as a "document" embedding.
- It takes in a document (as a string) and a dictionary, en_embeddings
- It processes the document, and looks up the corresponding embedding of each word.
- It then sums them up and returns the sum of all word vectors of that processed tweet.

```
In [59]:
         # UNO C12 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def get_document_embedding(tweet, en_embeddings, process_tweet=process_tweet):
             Input:
                 - tweet: a string
                 en_embeddings: a dictionary of word embeddings
             Output:
                 - doc_embedding:
                 sum of all word embeddings in the tweet
             doc_embedding = np.zeros(300)
             ### START CODE HERE ###
             # process the document into a list of words (process the tweet)
             processed_doc = process_tweet(tweet)
             for word in processed doc:
                 # add the word embedding to the running total for the document embeddi
                 if word in en_embeddings:
                     doc_embedding += en_embeddings[word]
             ### END CODE HERE ###
             return doc_embedding
In [60]: # UNO C13 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         # You do not have to input any code in this cell, but it is relevant to gradin
         # testing your function
         custom_tweet = "RT @Twitter @chapagain Hello There! Have a great day. :) #good
         tweet_embedding = get_document_embedding(custom_tweet, en_embeddings_subset)
         tweet_embedding[-5:]
Out[60]: array([-0.00268555, -0.15378189, -0.55761719, -0.07216644, -0.32263184])
         Expected output:
             array([-0.00268555, -0.15378189, -0.55761719, -0.07216644, -0.3226318
             41)
In [61]: # Test your function
         w4_unittest.test_get_document_embedding(get_document_embedding)
          All tests passed
```

Exercise 8 - get_document_vecs

Store all document vectors into a dictionary

Now, let's store all the tweet embeddings into a dictionary. Implement get_document_vecs()

```
# UNO C14 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def get_document_vecs(all_docs, en_embeddings, get_document_embedding=get_docu
             Input:
                 - all_docs: list of strings - all tweets in our dataset.
                 - en_embeddings: dictionary with words as the keys and their embedding
             Output:
                 - document_vec_matrix: matrix of tweet embeddings.
                 - ind2Doc_dict: dictionary with indices of tweets in vecs as keys and
             # the dictionary's key is an index (integer) that identifies a specific tw
             # the value is the document embedding for that document
             ind2Doc_dict = {}
             # this is list that will store the document vectors
             document_vec_1 = []
             for i, doc in enumerate(all_docs):
                 ### START CODE HERE ###
                 # get the document embedding of the tweet
                 doc_embedding = get_document_embedding(doc, en_embeddings)
                 # save the document embedding into the ind2Tweet dictionary at index i
                 ind2Doc_dict[i] = doc_embedding
                 # append the document embedding to the list of document vectors
                 document_vec_l.append(doc_embedding)
                 ### END CODE HERE ###
             # convert the list of document vectors into a 2D array (each row is a docu
             document_vec_matrix = np.vstack(document_vec_1)
             return document_vec_matrix, ind2Doc_dict
         document_vecs, ind2Tweet = get_document_vecs(all_tweets, en_embeddings_subset)
In [63]:
         # UNQ C15 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
In [65]:
         # You do not have to input any code in this cell, but it is relevant to gradin
         print(f"length of dictionary {len(ind2Tweet)}")
         print(f"shape of document_vecs {document_vecs.shape}")
         length of dictionary 10000
         shape of document_vecs (10000, 300)
```

Expected Output

length of dictionary 10000
shape of document_vecs (10000, 300)

```
In [66]: # Test your function. This cell may take some seconds to run.
w4_unittest.test_get_document_vecs(get_document_vecs)
```

All tests passed

3.2 - Looking up the Tweets

Now you have a vector of dimension (m,d) where m is the number of tweets (10,000) and d is the dimension of the embeddings (300). Now you will input a tweet, and use cosine similarity to see which tweet in our corpus is similar to your tweet.

```
In [67]: my_tweet = 'i am sad'
    process_tweet(my_tweet)
    tweet_embedding = get_document_embedding(my_tweet, en_embeddings_subset)

In [68]: # UNQ_C16 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
    # You do not have to input any code in this cell, but it is relevant to gradin
    # this gives you a similar tweet as your input.
    # this implementation is vectorized...
    idx = np.argmax(cosine_similarity(document_vecs, tweet_embedding))
    print(all_tweets[idx])

@hanbined sad pray for me :(((
Expected Output
```

3.3 - Finding the most Similar Tweets with LSH

You will now implement locality sensitive hashing (LSH) to identify the most similar tweet.

• Instead of looking at all 10,000 vectors, you can just search a subset to find its nearest neighbors.

Let's say your data points are plotted like this:

@hanbined sad pray for me :(((

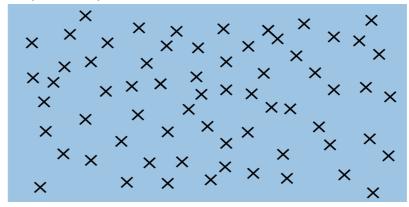
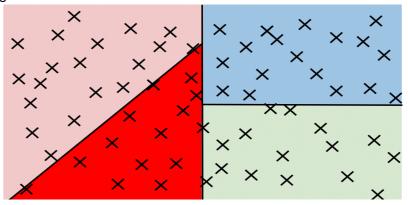


Figure 3

You can divide the vector space into regions and search within one region for nearest neighbors of a given vector.



```
In [69]: N_VECS = len(all_tweets)  # This many vectors.
N_DIMS = len(ind2Tweet[1])  # Vector dimensionality.
print(f"Number of vectors is {N_VECS} and each has {N_DIMS} dimensions.")
```

Number of vectors is 10000 and each has 300 dimensions.

Choosing the number of planes

- Each plane divides the space to 2 parts.
- So n planes divide the space into 2^n hash buckets.
- We want to organize 10,000 document vectors into buckets so that every bucket has about 16 vectors.
- For that we need $\frac{10000}{16} = 625$ buckets.
- We're interested in n, number of planes, so that $2^n = 625$. Now, we can calculate $n = \log_2 625 = 9.29 \approx 10$.

```
In [70]: # The number of planes. We use log2(625) to have ~16 vectors/bucket.
N_PLANES = 10
# Number of times to repeat the hashing to improve the search.
N_UNIVERSES = 25
```

3.4 - Getting the Hash Number for a Vector

For each vector, we need to get a unique number associated to that vector in order to assign it to a "hash bucket".

Hyperplanes in Vector Spaces

- In 3-dimensional vector space, the hyperplane is a regular plane. In 2 dimensional vector space, the hyperplane is a line.
- Generally, the hyperplane is subspace which has dimension 1 lower than the original vector space has.
- A hyperplane is uniquely defined by its normal vector.
- Normal vector n of the plane π is the vector to which all vectors in the plane π are orthogonal (perpendicular in 3 dimensional case).

Using Hyperplanes to Split the Vector Space

We can use a hyperplane to split the vector space into 2 parts.

- All vectors whose dot product with a plane's normal vector is positive are on one side of the plane.
- All vectors whose dot product with the plane's normal vector is negative are on the other side of the plane.

Encoding Hash Buckets

- For a vector, we can take its dot product with all the planes, then encode this information to assign the vector to a single hash bucket.
- When the vector is pointing to the opposite side of the hyperplane than normal, encode it by 0.
- Otherwise, if the vector is on the same side as the normal vector, encode it by 1.
- If you calculate the dot product with each plane in the same order for every vector, you've encoded each vector's unique hash ID as a binary number, like [0, 1, 1, ... 0].

Exercise 9 - hash_value_of_vector

We've initialized hash table hashes for you. It is list of N_UNIVERSES matrices, each describes its own hash table. Each matrix has N_DIMS rows and N_PLANES columns. Every column of that matrix is a N_DIMS -dimensional normal vector for each of N_PLANES hyperplanes which are used for creating buckets of the particular hash table.

Exercise: Your task is to complete the function hash_value_of_vector which places vector v in the correct hash bucket.

- First multiply your vector v , with a corresponding plane. This will give you a vector of dimension (1, N_planes).
- You will then convert every element in that vector to 0 or 1.
- You create a hash vector by doing the following: if the element is negative, it becomes a 0, otherwise you change it to a 1.
- You then compute the unique number for the vector by iterating over N PLANES
- Then you multiply 2^i times the corresponding bit (0 or 1).
- You will then store that sum in the variable hash value.

Intructions: Create a hash for the vector in the function below. Use this formula:

$$hash = \sum_{i=0}^{N-1} \left(2^i \times h_i \right)$$

Create the sets of planes

- Create multiple (25) sets of planes (the planes that divide up the region).
- You can think of these as 25 separate ways of dividing up the vector space with a different set of planes.
- Each element of this list contains a matrix with 300 rows (the word vector have 300 dimensions), and 10 columns (there are 10 planes in each "universe").

Hints

```
In [72]: # UNQ_C17 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def hash_value_of_vector(v, planes):
             """Create a hash for a vector; hash_id says which random hash to use.
             Input:
                 - v: vector of tweet. It's dimension is (1, N_DIMS)
                 - planes: matrix of dimension (N_DIMS, N_PLANES) - the set of planes t
                 - res: a number which is used as a hash for your vector
             .....
             ### START CODE HERE ###
             # for the set of planes,
             # calculate the dot product between the vector and the matrix containing t
             # remember that planes has shape (300, 10)
             # The dot product will have the shape (1,10)
             dot_product = np.dot(v, planes)
             # get the sign of the dot product (1,10) shaped vector
             sign_of_dot_product = np.sign(dot_product)
             # set h to be false (eqivalent to 0 when used in operations) if the sign i
             # and true (equivalent to 1) if the sign is positive (1,10) shaped vector
             # if the sign is 0, i.e. the vector is in the plane, consider the sign to
             h = sign_of_dot_product >= 0
             # remove extra un-used dimensions (convert this from a 2D to a 1D array)
             h = h.astype(int).flatten()
             # initialize the hash value to 0
             hash value = 0
             n_planes = h.shape[0]
             for i in range(n_planes):
                 # increment the hash value by 2^i * h_i
                 hash_value += (2 ** i) * h[i]
             ### END CODE HERE ###
             # cast hash_value as an integer
             hash_value = int(hash_value)
             return hash value
```

The hash value for this vector, and the set of planes at index 0, is 768

Expected Output

The hash value for this vector, and the set of planes at index 0, is 768

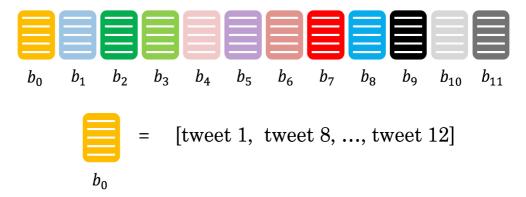
```
In [74]: # Test your function
w4_unittest.test_hash_value_of_vector(hash_value_of_vector)

All tests passed
```

3.5 - Creating a Hash Table

Exercise 10 - make_hash_table

Given that you have a unique number for each vector (or tweet), You now want to create a hash table. You need a hash table, so that given a hash_id, you can quickly look up the corresponding vectors. This allows you to reduce your search by a significant amount of time.



We have given you the <code>make_hash_table</code> function, which maps the tweet vectors to a bucket and stores the vector there. It returns the <code>hash_table</code> and the <code>id_table</code>. The <code>id_table</code> allows you know which vector in a certain bucket corresponds to what tweet.

Hints

```
In [75]: # UNO C19 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         # This is the code used to create a hash table:
         # This function is already implemented for you. Feel free to read over it.
         ### YOU CANNOT EDIT THIS CELL
         def make_hash_table(vecs, planes, hash_value_of_vector=hash_value_of_vector):
             Input:
                 - vecs: list of vectors to be hashed.
                 - planes: the matrix of planes in a single "universe", with shape (emb
             Output:
                 - hash_table: dictionary - keys are hashes, values are lists of vector
                 - id_table: dictionary - keys are hashes, values are list of vectors i
                                     (it's used to know which tweet corresponds to the
             # number of planes is the number of columns in the planes matrix
             num_of_planes = planes.shape[1]
             # number of buckets is 2^(number of planes)
             # ALTERNATIVE SOLUTION COMMENT:
             \# num buckets = pow(2, num of planes)
             num_buckets = 2**num_of_planes
             # create the hash table as a dictionary.
             # Keys are integers (0,1,2.. number of buckets)
             # Values are empty lists
             hash_table = {i: [] for i in range(num_buckets)}
             # create the id table as a dictionary.
             # Keys are integers (0,1,2... number of buckets)
             # Values are empty lists
             id_table = {i: [] for i in range(num_buckets)}
             # for each vector in 'vecs'
             for i, v in enumerate(vecs):
                 # calculate the hash value for the vector
                 h = hash_value_of_vector(v, planes)
                 # store the vector into hash table at key h,
                 # by appending the vector v to the list at key h
                 hash_table[h].append(v) # @REPLACE None
                 # store the vector's index 'i' (each document is given a unique intege
                 # the key is the h, and the 'i' is appended to the list at key h
                 id table[h].append(i) # @REPLACE None
             return hash_table, id_table
```

In [76]: # UNQ_C20 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
You do not have to input any code in this cell, but it is relevant to gradin
planes = planes_l[0] # get one 'universe' of planes to test the function
tmp_hash_table, tmp_id_table = make_hash_table(document_vecs, planes)

print(f"The hash table at key 0 has {len(tmp_hash_table[0])} document vectors'
print(f"The id table at key 0 has {len(tmp_id_table[0])} document indices")
print(f"The first 5 document indices stored at key 0 of id table are {tmp_id_t

The hash table at key 0 has 3 document vectors
The id table at key 0 has 3 document indices
The first 5 document indices stored at key 0 of id table are [3276, 3281, 3282]

Expected output

The hash table at key 0 has 3 document vectors
The id table at key 0 has 3 document indices
The first 5 document indices stored at key 0 of id table are [3276, 3 281, 3282]

```
In [77]: # Test your function
w4_unittest.test_make_hash_table(make_hash_table)
```

All tests passed

3.6 - Creating all Hash Tables

You can now hash your vectors and store them in a hash table that would allow you to quickly look up and search for similar vectors. Run the cell below to create the hashes. By doing so, you end up having several tables which have all the vectors. Given a vector, you then identify the buckets in all the tables. You can then iterate over the buckets and consider much fewer vectors. The more tables you use, the more accurate your lookup will be, but also the longer it will take.

```
In [78]: # Creating the hashtables
def create_hash_id_tables(n_universes):
    hash_tables = []
    id_tables = []
    for universe_id in range(n_universes): # there are 25 hashes
        print('working on hash universe #:', universe_id)
        planes = planes_l[universe_id]
        hash_table, id_table = make_hash_table(document_vecs, planes)
        hash_tables.append(hash_table)
        id_tables.append(id_table)

    return hash_tables, id_tables

hash_tables, id_tables = create_hash_id_tables(N_UNIVERSES)
```

```
working on hash universe #: 0
working on hash universe #: 1
working on hash universe #: 2
working on hash universe #: 3
working on hash universe #: 4
working on hash universe #: 5
working on hash universe #: 6
working on hash universe #: 7
working on hash universe #: 8
working on hash universe #: 9
working on hash universe #: 10
working on hash universe #: 11
working on hash universe #: 12
working on hash universe #: 13
working on hash universe #: 14
working on hash universe #: 15
working on hash universe #: 16
working on hash universe #: 17
working on hash universe #: 18
working on hash universe #: 19
working on hash universe #: 20
working on hash universe #: 21
working on hash universe #: 22
working on hash universe #: 23
working on hash universe #: 24
```

Approximate K-NN

Exercise 11 - approximate_knn

Implement approximate K nearest neighbors using locality sensitive hashing, to search for documents that are similar to a given document at the index doc id.

Inputs

- doc_id is the index into the document list all_tweets.
- v is the document vector for the tweet in all_tweets at index doc_id.
- planes_1 is the list of planes (the global variable created earlier).
- k is the number of nearest neighbors to search for.
- num_universes_to_use: to save time, we can use fewer than the total number of available universes. By default, it's set to N_UNIVERSES, which is 25 for this assignment.

- hash_tables: list with hash tables for each universe.
- id_tables: list with id tables for each universe.

The approximate_knn function finds a subset of candidate vectors that are in the same "hash bucket" as the input vector 'v'. Then it performs the usual k-nearest neighbors search on this subset (instead of correlate through all 40,000 truests).

Hints

```
In [ ]: # UNQ_C21 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
        # This is the code used to do the fast nearest neighbor search. Feel free to q
        def approximate_knn(doc_id, v, planes_l, hash_tables, id_tables, k=1, num_univ
            """Search for k-NN using hashes."""
            #assert num_universes_to_use <= N_UNIVERSES</pre>
            # Vectors that will be checked as possible nearest neighbor
            vecs_to_consider_l = list()
            # list of document IDs
            ids_to_consider_l = list()
            # create a set for ids to consider, for faster checking if a document ID d
            ids_to_consider_set = set()
            # loop through the universes of planes
            for universe_id in range(num_universes_to_use):
                # get the set of planes from the planes_l list, for this particular un
                planes = planes_l[universe_id]
                # get the hash value of the vector for this set of planes
                hash_value = hash_value_of_vector(v, planes)
                # get the hash table for this particular universe_id
                hash_table = hash_tables[universe_id]
                # get the list of document vectors for this hash table, where the key
                document_vectors_l = hash_table[hash_value]
                # get the id_table for this particular universe_id
                id_table = id_tables[universe_id]
                # get the subset of documents to consider as nearest neighbors from th
                new_ids_to_consider = id_table[hash_value]
                ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
                # Loop through the subset of document vectors to consider
                for i, new_id in enumerate(new_ids_to_consider):
                    if doc_id == new_id:
                        continue
                    # if the document ID is not yet in the set ids_to_consider...
                    if new_id not in ids_to_consider_set:
                        # access document_vectors_l list at index i to get the embeddi
                        # then append it to the list of vectors to consider as possibl
                        document_vector_at_i = document_vectors_l[i]
                        vecs_to_consider_l.append(document_vector_at_i)
                        # append the new_id (the index for the document) to the list of
                        ids_to_consider_l.append(new_id)
                        # also add the new id to the set of ids to consider
                        # (use this to check if new_id is not already in the IDs to co
                        None
                ### END CODE HERE ###
            # Now run k-NN on the smaller set of vecs-to-consider.
```

```
print("Fast considering %d vecs" % len(vecs_to_consider_1))
            # convert the vecs to consider set to a list, then to a numpy array
            vecs_to_consider_arr = np.array(vecs_to_consider_1)
            # call nearest neighbors on the reduced list of candidate vectors
            nearest_neighbor_idx_l = nearest_neighbor(v, vecs_to_consider_arr, k=k)
            # Use the nearest neighbor index list as indices into the ids to consider
            # create a list of nearest neighbors by the document ids
            nearest_neighbor_ids = [ids_to_consider_l[idx]
                                    for idx in nearest_neighbor_idx_1]
            return nearest_neighbor_ids
In [ ]: #document_vecs, ind2Tweet
        doc_id = 0
        doc_to_search = all_tweets[doc_id]
        vec_to_search = document_vecs[doc_id]
In [ ]: # UNQ_C22 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
        # You do not have to input any code in this cell, but it is relevant to gradin
        # Sample
        nearest_neighbor_ids = approximate_knn(
            doc_id, vec_to_search, planes_1, hash_tables, id_tables, k=3, num_universe
In [ ]: | print(f"Nearest neighbors for document {doc_id}")
        print(f"Document contents: {doc_to_search}")
        print("")
        for neighbor_id in nearest_neighbor_ids:
            print(f"Nearest neighbor at document id {neighbor id}")
            print(f"document contents: {all_tweets[neighbor_id]}")
        w4 unittest.test approximate knn(approximate knn, hash tables, id tables)
```

```
In [ ]: # Test your function
```

4 Conclusion

Congratulations - Now you can look up vectors that are similar to the encoding of your tweet using LSH!