

$$8.14 (a) sY(s) + 2Y(s) = X(s)$$

$$\Rightarrow H(s) = \frac{Y(s)}{X(s)} = \frac{1}{s+2} \quad \text{Re}[s] > -2$$

$$(b) h(t) = e^{-2t} u(t)$$

$$s(t) = \int_{-\infty}^t h(\tau) d\tau = u(t) \int_0^t e^{-2\tau} d\tau = \frac{1-e^{-2t}}{2} u(t)$$

$$(c) y_1(t) = \int_{-\infty}^{+\infty} x_1(\tau) h(t-\tau) d\tau = \int_{-\infty}^{+\infty} e^{-\tau} e^{-2(t-\tau)} u(t-\tau) d\tau$$

$$= \int_{-\infty}^t e^{\tau-2t} d\tau$$

$$= e^{-t}$$

$$(d) X_2(s) = \frac{1}{s+1} \quad \text{Re}[s] > -1$$

$$Y_2(s) = X_2(s)H(s) = \frac{1}{s+1} - \frac{1}{s+2} \quad \text{Re}[s] > -1$$

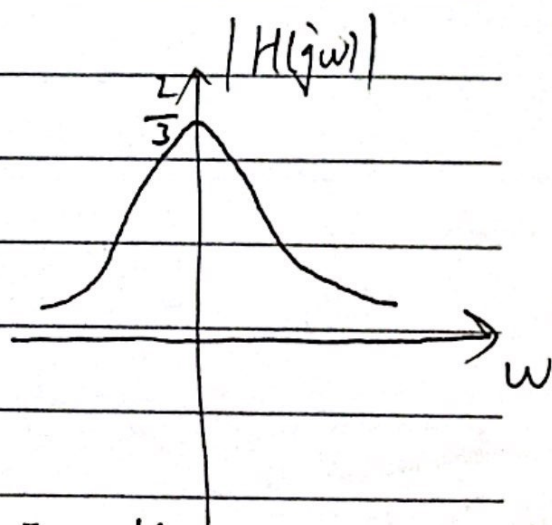
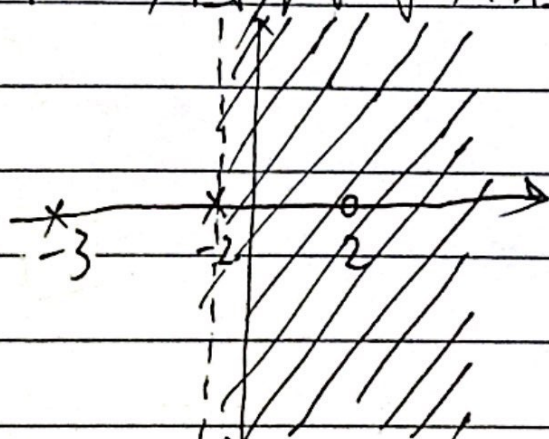
$$y_2(t) = e^{-t} u(t) - e^{-2t} u(t)$$

$$8.16 (a) 2 \frac{X(s)}{s} - 4 \frac{X(s)}{s^2} = Y(s) + 5 \frac{Y(s)}{s} + 6 \frac{Y(s)}{s^2}$$

$$\Rightarrow H(s) = \frac{Y(s)}{X(s)} = \frac{2s-4}{s^2+5s+6} \quad \text{Re}[s] > -2$$

(b) 稳定, 因为 $H(j\omega)$ 存在

(c)



$$(d) X(s) = \frac{1}{s+4} \quad \text{Re}[s] > -4$$

$$Y(s) = X(s)H(s) = \frac{10}{s+3} - \frac{6}{s+4} - \frac{4}{s+2} \quad \text{Re}[s] > -2$$

$$y(t) = 10e^{-3t} u(t) - 6e^{-4t} u(t) - 4e^{-2t} u(t)$$