

CROSS RIVER UNIVERSITY OF TECHNOLOGY, CALABAR
DEPARTMENT OF COMPUTER SCIENCE
FIRST SEMESTER EXAMINATIONS 2018/2019 SESSION

COURSE CODE: CSC 3103

COURSE TITLE: NUMERICAL METHODS

TIME: 2HRS

INSTRUCTION: Answer any 4 questions

- 1a. If 0.66266667 is the approximation to the fraction $\frac{2}{3}$, compute the absolute error, relative error and percentage error
- b. Distinguish between: (i) truncation and rounding (ii) computational and propagated errors, and (iii) sensitive and insensitive problems
- 2a. Find the next iterative value of the root of the equation $x^2 - 4 = 0$ using:
 (i) Newton-Raphson method, if the initial guess is 3,
 (ii) Secant method, if the initial guesses are 3 and 4
- b. Write a program that uses either *Secant* **OR** *Newton's* method to find the root of the equation in (a) above
- 3a. Determine the value of $f(-2.5)$ from the set of function values in the table below using finite difference interpolation scheme.

X	-3	-2	-1	0	1	2	3
F(X)	-27	-8	-1	0	1	8	27

- b. Find the best straight line fit to the following data points: (0, 1), (1, 2), (3, 3)
- 4a. Estimate: $\int_{-0.6}^{0.6} xe^x dx$ using the subdivisions -0.6, -0.4, -0.2, 0.0, 0.2, 0.4, 0.6 by:
 (i) Trapezoidal Rule (ii) Simpson's Rule
- b. Write a program to evaluate the integral in 4a above using any of the methods mentioned

- 5a. Write the matrix A below in the form [L] [U], where L is a unit lower triangular matrix and U is an upper triangular matrix:

<u>Matrix A for 5a.</u>	<u>System of equations for 5b</u>	<u>System of equations for 6a</u>
$A = \begin{pmatrix} 25 & 5 & 4 \\ 10 & 8 & 16 \\ 8 & 12 & 22 \end{pmatrix}$	$\begin{aligned} 10x_1 + x_2 + 2x_3 &= \mathbf{44} \\ 2x_1 + 10x_2 + x_3 &= \mathbf{51} \\ x_1 + 2x_2 + 10x_3 &= \mathbf{61} \end{aligned}$	$\begin{aligned} 2x_1 - x_2 &= \mathbf{2} \\ 2x_1 - 3x_2 + x_3 &= \mathbf{-2} \\ -x_1 + x_2 - 3x_3 &= \mathbf{-6} \end{aligned}$

- b. Write a program to solve the system of equations shown above using any method.
- 6a. Solve the system of equations above using:
 (i) 3 iterations of the Jacobi method, and (ii) 3 iterations of the Gauss-Seidel method
- b. What are the main differences between Jacobi iteration and Gauss-Seidel method?

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INSTRUCTION: Answer any 4 questions. Program may be written in any language of choice.

- 1a. Suppose 0.6624367 is the approximation to the fraction $\frac{2}{3}$, give the absolute error, relative error and percentage error.
- b. Distinguish clearly between: Round-off and Truncation errors.
- c. Name 5 causes of inexact measurements in numerical computation.
- 2a. Write a program to solve the equation $20x^3 - 22x^2 - 5x - 1 = 0$ to 4 decimal places given that it has a root at approximately $x=0.6$ using direct iteration technique.
- b. What is the condition for convergence of an iteration process for the numerical solution of non-linear equations?
- 3a. Use the Newton's method to find the first 3 approximations to the positive root of $f(x) = x^2 + 3x - 4$ given that $x_0 = 2$.
- b. State the Secant's formula for solving $f(x)$
- c. Use a computer program to solve 3(a) above.
- 4a. What are the uses of interpolation in real life?
- b. Determine the value of $f(2.5)$ from the set of function values using the Gregory-Newton forward difference formula.

X	1	2	3	4	5	6
f(x)	0	19	70	171	340	595

- c. Write a program to compute the solution of the problem stated in 4(b) above.
- 5a. Find the best straight line fit to the data points: (0, 1), (1, 2), (3, 3).
- b. Write the matrix A below in the form LU, where L is a unit lower triangular matrix and U is an upper triangular matrix:
$$A = \begin{pmatrix} 4 & -1 & -1 \\ -1 & 4 & -1 \\ -1 & -1 & 4 \end{pmatrix}$$
- 6a. Evaluate the integral $\int_0^2 \frac{dx}{1+x^4}$ to 3 decimal places using Simpson's Rule with five intervals.
- b. Develop an algorithm to evaluate the integral in 6(a) above.