A. Artifact Appendix

A.1 Abstract

This appendix describes how to reproduce the results described in the paper 'The CORA Tensor Compiler: Compilation for Ragged Tensors With Minimal Padding'. The experiments in the paper evaluate CORA on an Nvidia V100 GPU, an 8-core, 16-thread Intel CascadeLake CPU, an 8-core ARM Neoverse N1 CPU and a 64-core ARM Neoverse N1 CPU. Below, we provide instructions to set up and execute CORA as well as other frameworks used in the evaluation on each of these platforms. As we start with publicly available Docker containers in all cases, one a few GPU-related dependencies (such as cuDNN) as well as CORA's dependencies (such as the Z3 SMT solver, LLVM and Open-BLAS) need to be installed. We provide instructions for each of these below. In each case, 100 GB of disk space should be more than enough for the evaluation.

A.2 Artifact check-list (meta-information)

- Compilation: We reply on the publicly available compilers nvcc, the CUDA compiler to compile CUDA code generated by CORA, gcc to build CORA and other dependencies and LLVM to facilitate code generation for CPUs.
- Data set: We use sequence lengths for 8 different commonly used NLP datasets, all of which are included in the repositories described below.
- **Run-time environment:** The artifact has been tested on Ubuntu 20.04 and with the following versions of different dependencies.
- Hardware: We use an Nvidia V100 GPU for the GPU evaluation, and an 8-core, 16-thread Intel CascadeLake CPU, an 8-core ARM Neoverse N1 CPU and a 64-core ARM Neoverse N1 CPU for evaluation CORA on CPUs.
- Metrics: We use execution time as the primary execution metric of evaluation.
- Output: We generate CSV files, and also provide Python scripts to generate plots from the raw data.
- Experiments: Python/bash scripts are provided to replicate the results.
- Disk space required: 100 GB on each backend.
- Time needed to prepare workflow: A few hours on each backend.
- Time needed to complete experiments: Running all experiments on a backend takes several hours. The experiments on the ARM CPUs are particularly slow, taking 2-3 days to complete.
- **Publicly availability:** Yes, in the form of GitHub repositories (linked later) as well as on Zenodo at the url https://doi.org/10.5281/zenodo.6326455.

A.3 Description

A.3.1 Software dependencies

GPU: Below, we describe the environment we use across the different hardware backends we evaluate CORA on. On all of the backends, we use Ubuntu 20.04. Some of the frameworks below are already installed as part of the Docker images we start with (described below), while some need to be manually or installed. This is described below in §A.4.

Dependencies Common across Backends: CORA requires the following frameworks on all platforms: Z3 4.8.8, LLVM 9.0.0, cmake \geq 3.5 and g++ \geq 5.0.

Nvidia GPU: CUDA 11.1 (V11.1.105), cuDNN 8.2.1, Py-Torch 1.9.0+cu111, FasterTransformer (modified on top of FasterTransformer v4.0 (commit dd4c071) and provided as part of the cora_benchmarks repository). Make sure that nvcc is on the PATH.

ARM CPUs: OpenBLAS 0.3.10, PyTorch 1.10.0 with ARM Compute Library 21.12, TensorFlow 2.6.0 with ARM Compute Library 21.09

Intel CPU: Intel oneAPI MKL v2021.3

A.3.2 Data sets

All datasets are included in the cora_benchmarks repository.

A.4 Installation

Below, we provide installation instructions for setting up the environment as described above in §A.3.1 and building CORA on all the hardware backends.

A.4.1 Nvidia GPU:

Setting up the environment:

- Start from docker container: nvcr.io/nvidia/tenso rflow:20.12-tf1-py3.
- 2. Install Z3 4.8.8 available at https://github.com/Z 3Prover/z3/releases. Download the file z3-4.8.8 -x64-ubuntu-16.04.zip and move the contents of lib/ and include/ in this download to /usr/lib and /usr/include accordingly.
- 3. Install cuDNN 8.2.1 (for CUDA 11.x) by using the tar file installation method described on https://docs.n vidia.com/deeplearning/cudnn/install-guide/index.html\#installlinux-tar.
- 4. Install libtinfo-dev and libxml2-dev by running apt install libtinfo-dev libxml2-dev.
- Download pre-built LLVM 9.0.0 for Ubuntu 19.04 from the LLVM download page (https://releases.llvm. org/download.html). Let the path to the root of the downloaded LLVM distribution be LLVM_PATH.

Building CORA:

1. Clone the CORA repo as follows:

```
git clone --recurse-submodules -j8
    https://github.com/pratikfegade/cora
```

Make sure you're on the ragged_tensors branch Let the root of CORAbe CORA_ROOT.

- 2. In the file cora/config.cmake.gpu, set the variable USE_LLVM to <LLVM_PATH>/bin/llvm-config.
- 3. Build CoRAlike so:

```
mkdir build
cp config.cmake.gpu build/config.cmake
cd build
cmake ..
make -j8 tvm
```

- 4. Finally, the compiled shared library libtvm.so should be present in the build directory
- 5. Make sure that your PYTHONPATH contains \${CORA_ROO T}/python before moving on to the experiments

Installing PyTorch:

```
Install PyTorch 1.9.0+cu111 like so:
pip3 install torch==1.9.0+cu111 \\
    torchvision==0.10.0+cu111 \\
    torchaudio==0.9.0 \\
    -f https://download.pytorch.org/whl/torch_stable.html
```

Building FasterTransformer:

- Clone the cora_benchmarks repository available at ht tps://github.com/pratikfegade/cora_benchmarks.
- 2. Build FasterTransformer like so:

```
cd cora_benchmarks/bert_layer/faster_transformer
mkdir build
cd build
cmake -DSM=70 -DCMAKE_BUILD_TYPE=Release ..
make -j8
```

A.4.2 ARM CPUs

Setting up the environment for PyTorch and CORA:

- 1. Start from docker container armswdev/pytorch-arm-n eoverse-n1:r21.12-torch-1.10.0-onednn-acl
- 2. Download source for Z3 4.8.0 from https://github.com/Z3Prover/z3/releases. Build and install Z3 as follows:

```
cd z3-4.8.0.0
mkdir build
cd build
cmake -G "Unix Makefiles" ../
sudo make -j8 install
```

3. Build and install OpenBLAS as follows:

```
git clone https://github.com/xianyi/OpenBLAS
git checkout \\
    ee823b6ed98b2c9f8d72d9cdac195c64a6386a92
make TARGET=NEOVERSEN1 -j8
sudo make PREFIX=/usr/local/ install
```

4. Download pre-built LLVM 9.0.0 for Aarch64 from the LLVM download page (https://releases.llvm.org/down

- load.html). Let the path to the root of the downloaded LLVM distribution be LLVM_PATH.
- 5. Install libtinfo-dev, libtinfo5-dev and libxml2-dev by running apt install libtinfo-dev libxml2-dev libtinfo-dev.

Building CORA:

Just as on the GPU backend, clone the CORA repository. Checkout the arm branch. Run the following commands in the root of the repository. Ensure that the variable USE_LLVM points to the <LLVM_PATH>/bin/llvm-config before executing the commands.

```
mkdir build
cp config.cmake.arm build/config.cmake
cd build
cmake ..
make -j8 tvm
```

Make sure that your PYTHONPATH contains \${CORA_ROO T}/python before moving on to the experiments.

TensorFlow: We use the publicly available container arms wdev/tensorflow-arm-neoverse-n1:r21.09-tf-2.6.0-onednn-acl in order to exexcute TensorFlow on the ARM machines. No additional environment set up needs to be done for this.

A.4.3 Intel CPU

Setting up the environment:

- 1. Start from docker container ubuntu: 20.04
- 2. Install Z3 4.8.8 available at https://github.com/Z 3Prover/z3/releases. Download the file z3-4.8.8 -x64-ubuntu-16.04.zip and move the contents of lib/ and include/ in this download to /usr/lib and /usr/include accordingly.
- 3. Install Intel oneAPI Math Kernel Library from https: //www.intel.com/content/www/us/en/develo per/tools/oneapi/onemkl.html. The exact version (v2021.3) we used for our evaluation no longer seems to be available for download. Therefore the performance results for MKL runs may differ.
- 4. Install libtinfo-dev and libxml2-dev by running apt install libtinfo-dev libxml2-dev.
- Download pre-built LLVM 9.0.0 for Ubuntu 19.04 from the LLVM download page (https://releases.llvm. org/download.html). Let the path to the root of the downloaded LLVM distribution be LLVM_PATH.
- Install libtinfo-dev, libtinfo5-dev and libxml2-dev by running apt install libtinfo-dev libxml2-dev libtinfo-dev.

Building CORA:

Just as on the GPU backend, clone the CORA repository. Checkout the arm branch. Run the following commands in the root of the repository. Ensure that the variable USE_LLVM

points to the <LLVM_PATH>/bin/llvm-config before executing the commands.

```
mkdir build
cp config.cmake.arm build/config.cmake
cd build
cmake ..
make -j8 tvm
```

Make sure that your PYTHONPATH contains \${CORA_ROO T}/python before moving on to the experiments.

A.5 Experiment workflow

CORA is a tensor compiler. It takes an input a description of a tensor operator and generates LLVM or CUDA code for the kernel depending on whether the target is a CPU or a GPU. For evaluating individual kernels, such as trmm, vgemm or any of the 9 kernels that make up the transformer layer (illustrated in Figure3 of the paper), merely executing the python script implementing the kernel will compile the kernel, generate the code and execute it. For evaluating the entire transformer layer, or parts of it (such the self-attention or the MHA modules), we separate the steps of code generation and execution. We first generate compiled code for each of the operators in the form of shared libraries, which are then loaded and executed to form the layer to benchmark layer performance. The scripts provided automate all of these steps.

A.6 General Evaluation Notes and Instructions

We provide instructions to replicate the results in the paper on the three hardware backends below in §A.7, §A.7.6 and §A.7.7. We provide scripts to generate plots from the raw data when applicable, and a draft of the paper (cora_ben chmarks/expected_results_plotting_script/cora_paper_draft.pdf) as a way to provide expected results unless otherwise mentioned.

- 1. All paths below are relative to the root of the cora_ben chmarks repository
- 2. The section, figure and table numbers in the titles refer to the section, table and figure numbers in the provided draft of the paper.
- The starred measurements are primary performance measurements, while the rest cvan be thought of as analysis of the primary performance measurements.

The script cora_benchmarks/expected_results_plo tting_script/make_plots.py can be used to generate plots from the raw data when applicable. It can be executed as follows:

where CSV_DIR should to the path to a folder that contains all the csv files generated from all the evaluation across the three backends. The script will generate the plots in FIG_DIR.

A.7 Nvidia GPU Evaluation

Checkout the gpu branch in the cora_benchmarks repository.

A.7.1 Section 7.1: Matrix Multiplication

Variable-Sized Batched GEMM (vgemm)*:

- 1. Compile vbatch_gemm/cbt, vbatch_gemm/gemm_cub las by running make in those directories
- 2. Run

```
python3 scripts/vbatch_gemm_eval.py \\
    --target cuda --max-batches 50 \\
    --out-dir results
```

Output will be generated in results/vbatch_gemm_r esults_cuda.csv.

By default, the above script only runs a subset of the configurations evaluated in the paper as a way to demonstrate that the artifact is functional. In order to run the full evaluation as in the paper, pass the --full-evaluation option to the script.

3. Batch size 512 may need to run separately with CORAas it sometimes OOMs. This can be like so:

```
python3 ./vbatch_gemm/tvm/vbatch_gemm.py \\
    --target cuda --batch-sizes 512 \\
    --max-batches 10 \\
    --data-file ./vbatch_gemm/data.txt \\
```

Triangular Matrix Multiplication GEMM (trmm)*:

- Compile trmm/cublas by running make in those directories
- 2. Run

```
python3 scripts/trmm_eval.py --target cuda \\
    --out-dir results
```

By default, the above script only runs a subset of the configurations evaluated in the paper as a way to demonstrate that the artifact is functional. In order to run the full evaluation as in the paper, pass the --full-evaluation option to the script. Output will be generated in results/trmm_results_cuda.csv.

A.7.2 Section 7.2: The Transformer Model

Table 4: Transformer encoder forward execution latencies on Nvidia V100*

- Ensure that the line #define OP_TIMES 1 (line 3) of the file bert_layer/faster_transformer/fastert ransformer/time_map.h is commented out.
- 2. Build bert_layer/fastertransformer by running cmake -DSM=70 -DCMAKE_BUILD_TYPE=Release .. make

in the folder bert_layer/fastertransformer/build.

3. Run

```
python3 scripts/bert_layer_eval.py \\
```

```
--out-dir results \\
--max-batches 50 \\
--target cuda
```

By default, the above script only runs a subset of the configurations evaluated in the paper as a way to demonstrate that the artifact is functional. In order to run the full evaluation as in the paper, pass the --full-evaluation option to the script. Output will be generated in results/bert_layer_results_cuda.csv.

This will execute the model and generate execution latencies for a single encoder layer of the transformer model. During execution, CORAincurs some overheads (referred to as prelude overheads) which, in a multi-layered model would be amortized across execution of multiple layers. In the paper, we report the execution latencies for a layer assuming a 6-layer model. In order to compute these execution latencies, we separately measure the prelude overheads and subtract 5/6th these prelude costs from the execution latencies measured above. The prelude overheads can be measured by running

```
python3 scripts/bert_layer_eval.py \\
    --target cuda --out-dir results \\
    --max-batches 50 --prelude-overhead
```

Output will be generated in results/bert_layer_pre lude_results_cuda.csv.

Figures 13 and A.10: Per-operator execution time breakdown for RACE dataset at batch size 128 (Figure 13) and COLA dataset at batch size 32 (Figure A.10 in Section D.8) on the V100 GPU

- 1. Ensure that the line #define OP_TIMES 1 (line 3) of the file bert_layer/faster_transformer/fastert ransformer/time_map.h is not commented.
- Build bert_layer/fastertransformer by running cmake -DSM=70 -DCMAKE_BUILD_TYPE=Release ... make

in the folder bert_layer/fastertransformer/build.

3. Run

```
python3 scripts/op_times_eval.py \\
    --target cuda --out-dir results \\
    --max-batches 50 --gen-libs
```

Output will be generated in results/per_op_times_r esults_cuda.csv.

Just like above, we separately measure per-operator prelude overheads and subtract the appropriate amount from the per-operator ltencies measured above. These per-operator prelude overheads can be measured by running

```
python3 scripts/op_times_eval.py \\
    --target cuda --out-dir results \\
    --max-batches 50 --gen-libs \\
    --prelude-overhead
```

Output will be generated in results/per_op_times_p relude_results_cuda.csv.

Figure 11: MHA with and without layout change op fusion for the RACE dataset

Run

```
python3 scripts/pad_fusion_eval.py \\
    --target cuda --out-dir results \\
    --max-batches 50
```

Output will be generated in results/pad_fusion_results_cuda.csv.

Figure A.4: Masked Scaled Dot-Product Attention with and without padding for the attention matrix for the RACE and MNLI datasets (more discussion in Section D.3)

Run

```
python3 scripts/pad_fusion_eval.py \\
    --target cuda --max-batches 50 \\
    --out-dir results
```

Output will be generated in results/bert_layer_mmh a_results_cuda.csv.

Figure A.5: Memory consumption (more discussion in Section D.5)*

Run

```
python3 scripts/bert_layer_eval.py \\
    --target cuda --out-dir results \\
    --max-batches 50 --mem
```

Output will be generated in results/bert_layer_mem _results_cuda.csv.

A.7.3 Sections 7.3 and D.6: Operation Splitting and Horizontal Fusion (AttnV in Section 7.3 and QKt in Section D.6)

Run

```
python3 scripts/bin_packed_eval.py \\
    --target cuda --out-dir results \\
    --max-batches 50
```

Output will be generated in results/bin_packed_res ults_cuda.csv.

A.7.4 Section 7.4: CoRAOverheads

Prelude overheads

Rıın

```
python3 scripts/prelude_overheads_eval.py \\
    --out-dir results --max-batches 50
```

Output will be generated in results/prelude_overh eads_breakdown_results_cuda.csv.

Partial padding overheads (Figure A.8)

Run

```
python3 intro_study/flops.py \\
    --max-batches 50 \\
    --out-file results/intro_flops.csv
```

Ragged tensor overheads and load hoisting (Figure A.9) Run

```
python3 scripts/ragged_overheads_eval.py \\
    --target cuda --out-dir results \\
    --max-batches 50
```

Output will be generated in results/ragged_overhea ds_results_cuda.csv.

A.7.5 Sections 7.5 and D.4: Evaluation Against Sparse Tensor Compilers*

- Compile taco/taco_bcsr_trmm, taco/taco_bcsr_t rmul, taco/taco_csr_trmm, taco/taco_csr_trmul, taco/taco_csr_tradd by running make in taco/
- 2. Run

```
python3 scripts/taco_tr_eval.py \\
    --target cuda \\
    --out-dir results
```

By default, the above script only runs a subset of the configurations evaluated in the paper as a way to demonstrate that the artifact is functional. In order to run the full evaluation as in the paper, pass the --full-evaluation option to the script. Output will be generated in results/taco_results_cuda.csv.

A.8 Intel CPU Evaluation

Checkout the intel branch in the cora_benchmarks repository.

Variable-Sized Batched GEMM (vgemm)*:

- Compile vbatch_gemm/mkl, by running make in those directories
- 2. Run

```
python3 scripts/vbatch_gemm_eval.py \\
    --target cpu --max-batches 50 \\
    --out-dir results
```

By default, the above script only runs a subset of the configurations evaluated in the paper as a way to demonstrate that the artifact is functional. In order to run the full evaluation as in the paper, pass the --full-evaluation option to the script. Output will be generated in results/vbatch_gemm_results_cpu.csv.

A.9 8- and 64-core ARM CPU Evaluation

On the ARM CPU, we use one Docker image to evaluate PyTorch and CORA, and a second one to evaluate Tensor-Flow. Therefore, one needs to separately invoke the evaluation scripts in both the containers and then manually merge the generated CSV files. Checkout the arm_8 or the arm_64 branch in the cora_benchmarks repository depending on

whether the 8-core or the 64-core ARM CPU is used.

Table 5: MHA evaluation on ARM CPU for PyTorch and CORA*

In the container where we set up PyTorch and CORA, run the following command from the root of the cora_benchmarks repository:

```
python3 scripts/bert_layer_eval.py \\
    --out-dir results \\
    --max-batches 50 \\
    --target cpu --pt-cora
```

Output will be generated in the file results/bert_layer _results_cpu.csv.

Table 5: MHA evaluation on ARM CPU for TensorFlow

In the TensorFlow container, run the following command from the root of the cora_benchmarks repository:

```
python3 scripts/bert_layer_eval.py \\
    --out-dir results \\
    --max-batches 50 \\
    --target cpu --tf
```

The open --append can be used if the results are to be appended to the same CSV file as the one with the results for PyTorch and CoRA. In any case, the output will be generated in/appended to the file results/bert_layer_results_cpu.csv.

By default in both the cases above, the script only runs a subset of the configurations evaluated in the paper as a way to demonstrate that the artifact is functional. In order to run the full evaluation as in the paper, pass the --full-evaluation option to the script.

We had to re-run these experiments after the reviews and the provided paper draft does not contain the revised results. The revised expected results can be found in the two provided CSV files named cora_benchmarks/expected_results_plotting_script/arm_mha_8_core_results.csv and cora_benchmarks/expected_results_plotting_script/arm_mha_64_core_results.csv. The files contain the results for the 8- and 64-core ARM CPUs respectively.

A.10 Experiment customization

- 1. **GPU Evaluation:** The GPU evaluation has been tested on GPUs with compute capability 70. While the evaluation may run on other GPUs as well, we have not yet tested it thoroughly.
- 2. Intel CPU Evaluation: The Intel CPU evaluation should work for other CPUs beyond the CascadeLake CPUs we have tested it on. However, given that our schedules have been tuned for the 8-core CascadeLake CPU, the performance might not be optimal. Further, when running on other Intel CPUs, the LLVM target triple would need to be changed (in the file cora_benchmarks/scripts/common.py on line 10).

3. ARM CPU Evaluation: The ARM CPU evaluation should work for other CPUs beyond the Neoverse N1 CPUs we have tested it on. However, given that our schedules have been tuned for the Neoverse N1 CPU, the performance might not be optimal. Further, when running on other Intel CPUs, the LLVM target triple would need to be changed (in the file cora_benchmarks/run_utils.py on line 39). The number of threads would also be need to be changed for PyTorch evaluation in the files cora_benchmarks/bert_layer/pytorch/layer_cpu_micro_batch.py and cora_benchmarks/bert_layer/pytorch/layer_cpu.py.