

Astrometric Observations of the Main Uranian satellites at the Pulkovo Observatory in 2007 – 2016

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Abstract

The results of observations of Uranian satellites obtained with the Pulkovo Observatory 26-inch refractor in 2007 – 2016 were presented. Almost 7000 CCD frames were analyzed and reduced using the UCAC4 catalog. Coordinates of Uranus were determined indirectly with the satellite positions and their ephemeris relative to the planet. The O-C differences were calculated for each object using the INPOP13c planetary theory and Lainey’s theory of the satellites’ motion. The mean values of the standard errors of (O-C) are within 0.02 to 0.07 arcsec. (O-C) absolute values are less than 0.5 arcsec. It is in a good agreement with ephemeris.

1 Introduction

High-precision theories of motion of the major planets and their satellites are necessary for researches of the Solar System formation and evolution, and for providing the ephemeridae for the future space missions. Construction of the theories requires an extensive observational material (Emel’yanov, 2010).

In the twentieth century photographic observations of Uranus were performed at the Pulkovo Observatory (Kiseleva, Khrutskaya, 2007). Only two of four Uranian satellites were accessible for photographic method. Also coordinates of the planet were determined with respect to the reference stars directly.

CCD-observations of Uranus have been started in 2007. The CCD-images of four main Uranian satellites (Ariel, Umbriel, Titania and Oberon) are available for robust determination of positions. Final astrometric accuracy of the satellites’ observations is similar to the positional precision presented in several recent investigations (Camargo et al., 2015, Khovrichiev, 2009). The fifth main satellite of Uranus (Miranda) is usually located within small angular distant from the planet (within bright part of scattered-light halo caused by Uranus). Therefore its images could not be correctly approximated.

The first results of observations of Uranian satellites with CCD-camera and 26-inch refractor in Pulkovo were published in 2013 (Roschina et al., 2015). Published observations covered period 2007 – 2011. UCAC2 (Zacharias et al., 2004) was used as a reference catalog. Volume of observational data in current paper is significantly bigger. The resulted data sample contains satellite positions taken from August 2007 to January 2016. The astrometric calibrations were performed with UCAC4 (Zacharias et al., 2013). This catalog provides significantly more stars in the field of view than UCAC2. It allows us to reach improvement of accuracy.

2 Observations and measurements

Current observations of Uranus are performed at the Pulkovo with the 26-inch refractor every year from the end of August to the beginning of January. The telescope is located at $59^{\circ}46'15''$ north latitude, $30^{\circ}19'23''$ east longitude, altitude above the sea level is about 85 m. Aperture diameter of the telescope is 65 cm, focal length is 1041.3 cm, focal plane scale is $19''.80/\text{mm}$ in the center of image. The CCD camera FLI Pro Line 09000 is used. Size of the CCD matrix is 3056×3056 px, each of $12 \mu\text{m}$. The field of view is $12' \times 12'$, the scale on the CCD frames is $0''.24/\text{px}$.

We obtained one normal position of each satellite per night in the case of availability of the satellite for observations. Each normal position was calculated on the basis of five individual positions measured independently. Exposure times were within the range from 3 s to 20 s. We stacked separate CCD-images to achieve optimal quality for approximation. The number of frames in stack procedure varies from 4 to

Table 1: Halo subtracting efficiency

	$(O - C)_\alpha$	$(O - C)_\delta$	SEM α	SEM δ	RMS α	RMS δ
Ariel	-0.035	-0.015	0.026	0.042	0.059	0.094
Umbriel	0.016	-0.002	0.027	0.099	0.061	0.221
Titania	-0.003	0.008	0.005	0.007	0.010	0.016
Oberon	0.009	0.009	0.003	0.012	0.006	0.027
Ariel	1.888	-1.099	1.596	0.309	3.568	0.692
Umbriel	-2.024	-0.442	1.736	0.446	3.882	0.998
Titania	0.006	0.064	0.005	0.010	0.012	0.023
Oberon	0.081	-0.045	0.006	0.011	0.012	0.026

25. Satellites' motion on the celestial sphere during observation was approximated linearly, so the average moment of time for whole series and the normal position at this moment were determined.

Observations processing and coordinates measurement were performed with the IZMCCD software package (www.izmccd.puldb.ru, Izmailov et al., 1998). In case of distortion of the satellite image by planet halo the procedure of approximation and subtraction of the halo signals was applied.

Firstly the certain area A with the image distorted by planet halo was selected. In that area the uniform grid with 4 nodes on a vertical and horizontal was allocated. For each node the system of equations (1) was formed and solved relatively a , b , c and d by the least square method.

$$I(r_i) = a + \frac{b}{r_i} + \frac{c}{r_i^2} + \frac{d}{r_i^3}, \quad (1)$$

where

$r_i = \sqrt{(x_i - x_0)^2 + (y_i - y_0)^2}$,
 (x_0, y_0) – coordinates of the node,
 i – the number of equation,
 (x_i, y_i) – coordinates of the corresponding pixel in the area A,
 $I(r_i)$ – a value of brightness in the pixel.

After such system was solved for each node we looked at the residual vectors and chose node to which the minimal residuals corresponded. Then we formed the A area of cells adjacent to the node and repeated the previous steps recurrently until the cells were size of 1 pixel. Lately we last time chose the node with the minimal vector of residuals and approximated the brightness distribution on formula (1) with the chosen pixel as (x_0, y_0) .

We determined the photocenters of satellites and reference stars images using approximation of image profile with the Lorenz function.

$$I(x, y) = \frac{C}{(1 + AR)^\alpha} + D, \quad (2)$$

where

$R = \sqrt{(x - x_0)^2 + (1 + B)(y - y_0)^2 + E(x - x_0)(y - y_0)}$,
 $I(x, y)$ – brightness in the pixel which coordinates are (x, y)
 (x_0, y_0) – coordinates of the photocenter
 α – determine the form of the curve, in our case $\alpha = 1.4$
 A, B, C, D, E – parameters of model

The Lorenz function parameters were obtained by solving an excess system of equations by the non-linear least squares method. Astrometric reduction was performed with the six-constant linear model. We taken into account the differential refraction effect of the first order. The UCAC4 (Zacharias et al., 2013) was adopted as a reference catalog. At least of 8 stars of the UCAC4 were located within field of view. The majority of frames were identified with more than 10 stars.

Errors of measurements were estimated on standard formulae.

$$\sigma_x = \sqrt{\frac{\sum_{k=1}^N (x_k - x_{mean})^2}{N-1}}; \varepsilon_x = \sigma_x / \sqrt{N},$$

Table 2: Numbers of the normal and the individual positions

	2007	2008	2009	2010	2011	2012	2013	2014	2015
Ariel	0(0)	0(0)	3(15)	0 (0)	0(0)	2 (10)	2 (10)	2 (10)	7 (35)
Umbriel	0(0)	2 (10)	4 (20)	4 (20)	4 (20)	4 (20)	14 (70)	8 (40)	11(55)
Titania	3 (13)	5 (25)	11 (55)	5 (25)	15 (75)	12 (60)	19 (91)	15 (74)	21 (105)
Oberon	4 (21)	7 (35)	11 (55)	5 (25)	18 (90)	13 (65)	18 (88)	19 (94)	21 (105)

 Table 3: Mean O-C differences of RA (α) and DEC (δ) and errors

	$(O - C)_\alpha$	$(O - C)_\delta$	SEM α	SEM δ	RMS α	RMS δ
Ariel	0.043	-0.074	0.06	0.06	0.11	0.11
Umbriel	0.025	-0.069	0.05	0.07	0.09	0.11
Titania	-0.009	-0.014	0.02	0.02	0.03	0.03
Oberon	-0.001	-0.019	0.02	0.02	0.03	0.04
Uranus	0.001	-0.021				

where x_k are measured coordinates, N is the number of individual measurements, x_{mean} is the mean coordinate.

We discarded data in the case of individual error of position was greater than critical value. This value was 0."3 in the case of Ariel and Umbriel and 0."1 in case of Titania and Oberon.

3 Results and comparison with theory

Almost 7000 CCD images of Uranus and its satellites were collected from 2007 to 2016. Table 2 contains the numbers of observational nights for each satellite. It corresponds to the number of normal positions obtained during the year. The quantities of the individual positions are shown in the parentheses.

Obtained normal positions are not evenly distributed over the period of observations. An increasing number of obtained positions is seen from 2007 to 2016. This effect was noticed in earlier work (Camargo et al., 2015). It is explained by change of the angle between the equatorial plane of Uranus and the tangent plane. In the beginning of observational span the equatorial plane of the planet (and also the satellites' orbital planes), was very close to perpendicular to the tangent plane. Therefore Uranian satellites spent most of the time behind the planet or right in front of it, so their coordinates could not be determined with CCD observations. This angle decreased at the end of observational period. As a result the satellites' images became more available for CCD astrometric observations.

We show this effect by calculating the K coefficient. Let K be a ratio of the number of normal positions obtained during an observational season to the number of nights in this season. The observational season is a period of time from the end of August to the beginning of January. Figure (1) illustrates increasing of this ratio.

We compared the positions of Uranus and its satellites with their theoretical computed positions given by INPOP13c planetary ephemeris (Fienga et al. 2014) and Lainey's satellite ephemerides (Lainey, 2008). The ephemerides were provided by the MULTI-SAT service (Emel'yanov and Arlot, 2008). We used the Lainey 2015 ephemeris available on the MULTI-SAT. This is an updated version of Lainey's theory.

Also positions of Uranus were determined with the positions of its satellites and ephemeris distances between them and the planet. Series of the O-C differences for each satellite and for the planet are shown on plots. The mean O-C differences of RA and DEC are in the Table 3. Also the standart error of the mean (SEM) and the root mean square (RMS) for each difference are shown. Observations show a good agreement with theory.

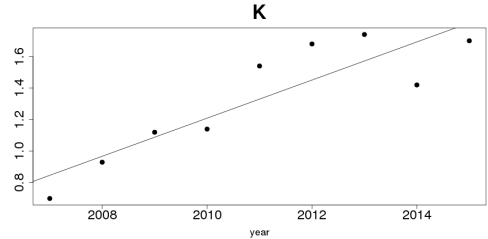
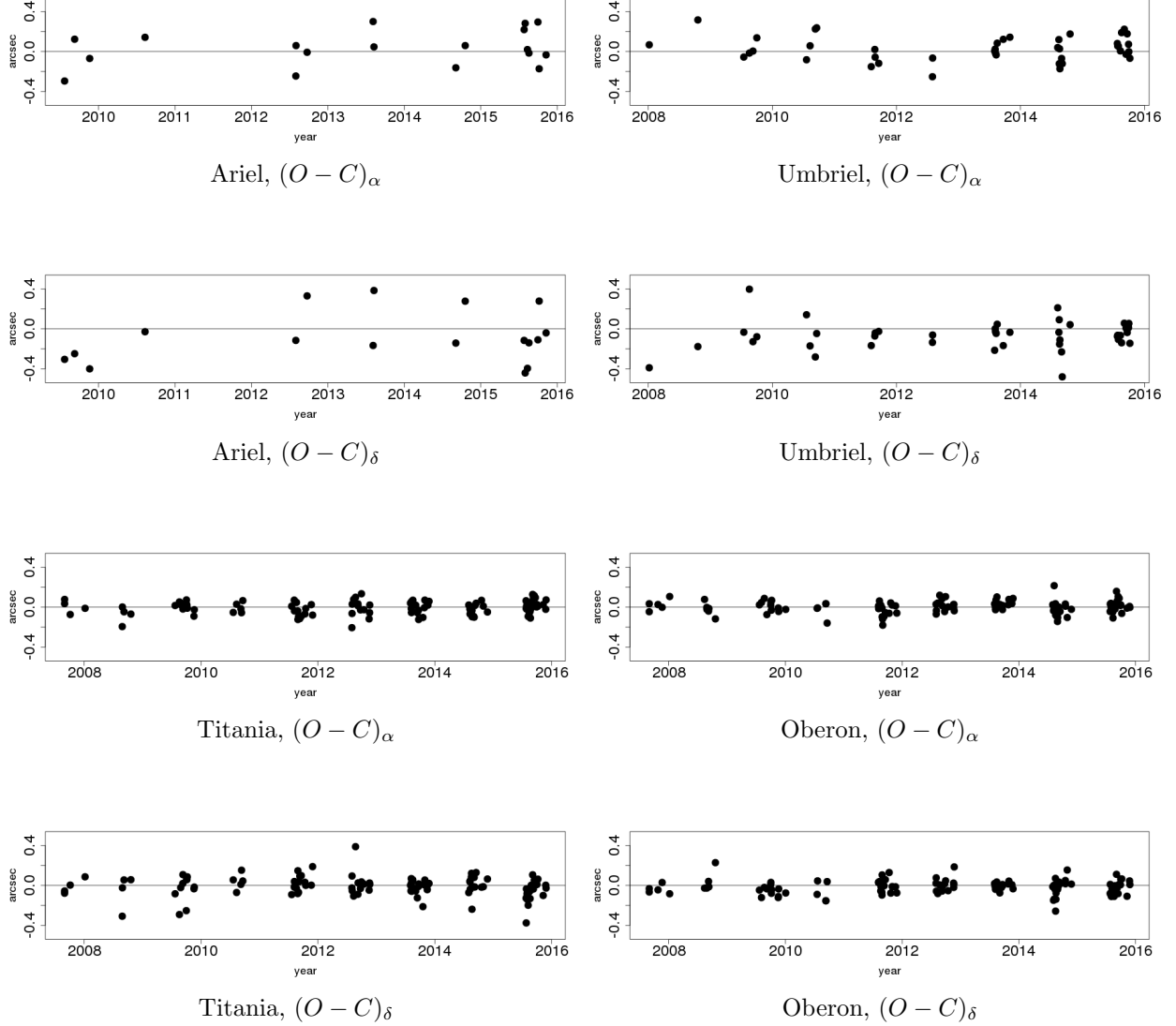


Figure 1: Ratio of the number of normal positions obtained during a season to the number of observational nights



4 Conclusion

This paper has reported the results of Uranian satellites' CCD observations performed at the Pulkovo Observatory with the 26-inch refractor in 2007 – 2016. Results' analysis has demonstrated high-quality and the suitability of methods applied in this work. In particular the method of halo subtracting is useful for obtaining coordinates of inner satellites of Solar System planets and other small celestial bodies approaching bright objects in tangent plane. Observed positions of the main Uranian satellites are usually close to ephemeris positions. The obtained normal positions are available in the Pulkovo database and in the CDS database.

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