

**2.15** Sean  $f_i: B^3 \rightarrow B$  las funciones booleanas de tres variables con  $i = 63, 82, 103, 104, 116, 126, 143, 172, 188, 217$  y  $231$ . Halla:

- Sus formas canónicas disyuntivas y conjuntivas
- Sus implicantes primos mediante Quine, consensos, FCC y Karnaugh.
- Sus formas canónicas disyuntivas reducidas.
- Sus formas no simplificables mediante Karnaugh y Petrick.

|                  |                  |                  |
|------------------|------------------|------------------|
| $63 = 00111111$  | $116 = 01110100$ | $188 = 10111100$ |
| $82 = 01010010$  | $126 = 01111110$ | $217 = 11011001$ |
| $103 = 01100111$ | $143 = 10001111$ | $231 = 11100111$ |
| $104 = 01101000$ | $172 = 10101100$ |                  |

→ Formas canónicas disyuntivas (suma minterm).

$$\begin{aligned}
 f_{63} &= m_2 + m_3 + m_4 + m_5 + m_6 + m_7 = \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}\bar{z} + x\bar{y}z + xy\bar{z} + xyz \\
 f_{82} &= m_1 + m_3 + m_6 = \bar{x}\bar{y}z + \bar{x}yz + xy\bar{z} \\
 f_{103} &= m_1 + m_2 + m_5 + m_6 + m_7 = \bar{x}\bar{y}z + \bar{x}y\bar{z} + x\bar{y}z + xy\bar{z} + xyz \\
 f_{104} &= m_1 + m_2 + m_4 = \bar{x}\bar{y}z + \bar{x}y\bar{z} + x\bar{y}\bar{z} \\
 f_{116} &= m_1 + m_2 + m_3 + m_5 = \bar{x}\bar{y}z + \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}\bar{z} \\
 f_{126} &= m_1 + m_2 + m_3 + m_4 + m_5 + m_6 = \bar{x}\bar{y}z + \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}\bar{z} + x\bar{y}z + xyz \\
 f_{143} &= m_0 + m_4 + m_5 + m_6 + m_7 = \bar{x}\bar{y}\bar{z} + x\bar{y}\bar{z} + x\bar{y}z + xy\bar{z} + xyz \\
 f_{172} &= m_0 + m_2 + m_4 + m_5 = \bar{x}\bar{y}\bar{z} + \bar{x}y\bar{z} + x\bar{y}\bar{z} + x\bar{y}z \\
 f_{188} &= m_0 + m_2 + m_3 + m_4 + m_5 = \bar{x}\bar{y}\bar{z} + \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}\bar{z} + x\bar{y}z \\
 f_{217} &= m_0 + m_1 + m_3 + m_4 + m_7 = \bar{x}\bar{y}\bar{z} + \bar{x}\bar{y}z + \bar{x}yz + x\bar{y}\bar{z} + xyz \\
 f_{231} &= m_0 + m_1 + m_2 + m_5 + m_6 + m_7 = \bar{x}\bar{y}\bar{z} + \bar{x}\bar{y}z + \bar{x}yz + x\bar{y}\bar{z} + xy\bar{z} + xyz
 \end{aligned}$$



→ Formas canónicas conjuntivas (prod. max term).

$$f_{63} = M_0 \cdot M_1 = (x+y+z) \cdot (x+y+\bar{z})$$

$$f_{82} = M_0 \cdot M_2 \cdot M_4 \cdot M_5 \cdot M_7 = (x+y+z) \cdot (x+\bar{y}+z) \cdot (\bar{x}+y+z) \cdot (\bar{x}+y+\bar{z}) \cdot (\bar{x}+\bar{y}+\bar{z})$$

$$f_{103} = M_0 \cdot M_3 \cdot M_4 = (x+y+z) \cdot (x+\bar{y}+\bar{z}) \cdot (\bar{x}+y+z)$$

$$f_{104} = M_0 \cdot M_3 \cdot M_5 \cdot M_6 \cdot M_7 = (x+y+z) \cdot (x+\bar{y}+\bar{z}) \cdot (\bar{x}+y+\bar{z}) \cdot (\bar{x}+\bar{y}+z) \cdot (\bar{x}+\bar{y}+\bar{z})$$

$$f_{116} = M_0 \cdot M_4 \cdot M_6 \cdot M_7 = (x+y+z) \cdot (\bar{x}+y+z) \cdot (\bar{x}+\bar{y}+z) \cdot (\bar{x}+\bar{y}+\bar{z})$$

$$f_{126} = M_0 \cdot M_7 = (x+y+z) \cdot (\bar{x}+\bar{y}+\bar{z})$$

$$f_{143} = M_1 \cdot M_2 \cdot M_3 = (x+y+\bar{z}) \cdot (x+\bar{y}+z) \cdot (x+\bar{y}+\bar{z})$$

$$f_{172} = M_1 \cdot M_3 \cdot M_6 \cdot M_7 = (x+y+\bar{z}) \cdot (x+\bar{y}+\bar{z}) \cdot (\bar{x}+\bar{y}+z) \cdot (\bar{x}+\bar{y}+\bar{z})$$

$$f_{188} = M_1 \cdot M_6 \cdot M_7 = (x+y+\bar{z}) \cdot (\bar{x}+\bar{y}+z) \cdot (\bar{x}+\bar{y}+\bar{z})$$

$$f_{217} = M_2 \cdot M_5 \cdot M_6 = (x+\bar{y}+z) \cdot (\bar{x}+y+\bar{z}) \cdot (\bar{x}+\bar{y}+z)$$

$$f_{231} = M_3 \cdot M_4 = (x+\bar{y}+\bar{z}) \cdot (\bar{x}+y+z)$$

→ Implicantes primos. → Para que el ejercicio no sea demasiado extenso y se vea por entendido el procedimiento haremos cada una de ellas con un método.

Quine:

$$f_{63}) \begin{array}{c|cc|c} x y z & 111X & 11-X \\ \hline x y \bar{z} & 110X & 1-1X \\ x \bar{y} z & 101X & -11X \\ \hline \bar{x} y z & 011X & 1-0X \\ \hline x \bar{y} \bar{z} & 100X & -10X \\ \bar{x} y \bar{z} & 010X & 10-X \\ & & 01-X \end{array} \quad \begin{array}{c} 1-- \\ -1- \end{array} \Rightarrow f_{63}(x,y,z) = x+y$$

Implicantes primos =  $\{x, y\}$ .

$$f_{82}) \begin{array}{c|cc|c} \bar{x} y z & 011X & 0-1 \\ \hline x y \bar{z} & 110 & \\ \hline \bar{x} \bar{y} z & 001X & \end{array} \quad \Rightarrow f_{82}(x,y,z) = x y \bar{z} + \bar{x} z$$

Implicantes. Primos =  $\{x y \bar{z}, \bar{x} z\}$

§103)

|                   |       |     |
|-------------------|-------|-----|
| $xyz$             | 111 X | 11- |
| $xy\bar{z}$       | 110 X | 1-1 |
| $x\bar{y}z$       | 101 X | -01 |
| $\bar{x}y\bar{z}$ | 010 X | -10 |
| $\bar{x}\bar{y}z$ | 001 X |     |

$\Rightarrow \S_{103}(x,y,z) = xy + xz + \bar{y}z + y\bar{z}$

I.P. =  $\{xy, xz, \bar{y}z, y\bar{z}\}$

FCC:

§126) =  $M_0 \cdot M_7 = (x+y+z) \cdot (\bar{x}+\bar{y}+\bar{z}) = \cancel{\bar{x}x} + \cancel{\bar{x}y} + \cancel{\bar{x}z} +$   
 $= \cancel{\bar{x}x} + \bar{x}y + \bar{x}z + \bar{y}x + \bar{y}y + \bar{y}z + \bar{z}x + \bar{z}y + \bar{z}z =$   
 $= \bar{x}y + \bar{x}z + \bar{y}x + \bar{y}z + \bar{z}x + \bar{z}y =$

§217)  $(x,y,z) = M_2 \cdot M_5 \cdot M_6 = (x+\bar{y}+\bar{z}) \cdot (\bar{x}+y+\bar{z}) \cdot (\bar{x}+\bar{y}+z) =$   
 $(\cancel{\bar{x}x} + \bar{x}\bar{y} + \bar{x}\bar{z} + x\bar{y} + \cancel{\bar{y}y} + \bar{y}z + x\bar{z} + \bar{y}\bar{z} + \cancel{\bar{z}z}) (\bar{x}+\bar{y}+z) =$   
 $= (\bar{x}\bar{y} + \bar{x}\bar{z} + x\bar{y} + \bar{y}z + x\bar{z} + \bar{y}\bar{z}) (\bar{x}+\bar{y}+z) =$   
 $= (\bar{x}\bar{y} + \bar{x}\bar{z} + \cancel{\bar{x}y} + \cancel{\bar{x}\bar{y}} + \cancel{\bar{x}z} + \cancel{\bar{x}\bar{z}} + \cancel{xy} + \cancel{y\bar{z}} + \cancel{yz} + \cancel{y\bar{z}} + \cancel{z\bar{x}} + \cancel{z\bar{y}} + \cancel{z\bar{z}} + \bar{y}\bar{z}) =$   
 $= \bar{x}\bar{y} + \bar{x}\bar{z} + \bar{y}z + x\bar{z} + \bar{y}\bar{z} =$   
 $= \bar{x}\bar{y} + \bar{x}\bar{z} + \bar{y}z + x\bar{z} + \bar{y}\bar{z} =$   
 $= \bar{x}\bar{z} + x\bar{z} + \bar{y}$

§231)  $(x,y,z) = M_3 \cdot M_4 = (x+\bar{y}+\bar{z}) \cdot (\bar{x}+y+z) =$   
 $= \cancel{x\bar{x}} + \cancel{\bar{x}y} + \bar{x}\bar{z} + xy + \cancel{\bar{y}y} + \bar{y}z + \cancel{xz} + \cancel{\bar{y}z} + \cancel{\bar{z}z} =$   
 $= xy + \bar{x}\bar{y} + xz + \bar{x}\bar{z} + yz + \bar{y}z.$



## Consensos

$$f_{104}) = m_1 + m_2 + m_4 = \bar{x}\bar{y}z + \bar{x}y\bar{z} + x\bar{y}\bar{z} =$$

$$= \bar{x}\bar{y}z + \bar{x}y\bar{z} + x\bar{y}\bar{z}. \quad (\text{No consigo simplificar}).$$

Aplico karnaugh

| xy \ z | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0      |    | 1  |    | 1  |
| 1      | 1  |    |    |    |

→ efectivamente ya está en forma reducida.

$$f_{116}) = m_1 + m_2 + m_3 + m_5 = \bar{x}\bar{y}z + \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}z =$$

$$= \bar{x}\bar{y}z + \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}z + \bar{x}y =$$

$$= \bar{x}\bar{y}z + x\bar{y}z + \bar{x}y = \bar{x}\bar{y}z + x\bar{y}z + \bar{x}y + \bar{x}z =$$

$$= x\bar{y}z + \bar{x}y + \bar{x}z = x\bar{y}z + \bar{x}y + \bar{x}z + \bar{y}z =$$

$$= \bar{x}y + \bar{x}z + \bar{y}z$$

## karnaugh

$$f_{143}(x,y,z) = m_0 + m_4 + m_5 + m_6 + m_7 = \bar{x}\bar{y}\bar{z} + x\bar{y}\bar{z} + x\bar{y}z + x\bar{y}\bar{z} + x\bar{y}z =$$

| xy \ z | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0      | 1  |    | 1  | 1  |
| 1      |    |    | 1  | 1  |

$$\Rightarrow f_{143}(x,y,z) = x + \bar{y}\bar{z} \quad \neq \text{reducida}$$

$$f_{188}(x,y,z) = \bar{x}\bar{y}\bar{z} + \bar{x}y\bar{z} + \bar{x}yz + x\bar{y}\bar{z} + x\bar{y}z =$$

| xy \ z | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0      | 1  | 1  |    | 1  |
| 1      |    | 1  |    | 1  |

$$\Rightarrow f_{188}(x,y,z) = \bar{x}\bar{z} + \bar{x}y + x\bar{y} \quad \neq \text{reducida}$$

$$f_{188}(x,y,z) = \bar{x}\bar{z} + \bar{x}y + x\bar{y} + \bar{y}z$$

$$f_{172}) = \bar{x}\bar{y}\bar{z} + x\bar{y}\bar{z} + x\bar{y}z + x\bar{y}z$$

| xy \ z | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0      | 1  | 1  |    | 1  |
| 1      |    |    |    | 1  |

$$\Rightarrow f_{172}(x,y,z) = \bar{x}\bar{z} + x\bar{y} \quad \text{form. reducida}$$

$$f_{172}(x,y,z) = \bar{x}\bar{z} + x\bar{y} + \bar{y}\bar{z} \quad (\text{S.P.})$$

→ Sus formas canónicas disyuntivas reducidas las acabamos de obtener en este apartado anterior.

→ Formas no simplificables { Karnaugh Petrick.

Mediante Karnaugh ya hemos obtenido las de  $f_{104})$ ,  $f_{143})$ ,  $f_{188})$  y  $f_{172})$ . Hagamos también así  $f_{126})$ ,  $f_{217})$ ,  $f_{231})$  y  $f_{116})$ :

$$f_{126})$$

| xy \ z | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0      |    | 1  | 1  | 1  |
| 1      | 1  | 1  |    | 1  |

$$\Rightarrow f_{126}(x,y,z) = \bar{x}z + y\bar{z} + x\bar{y}$$

$$f_{116})$$

| xy \ z | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0      |    | 1  |    |    |
| 1      | 1  | 1  |    | 1  |

$$\Rightarrow f_{116}(x,y,z) = \bar{x}y + \bar{y}z$$

$$f_{217})$$

| xy \ z | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0      | 1  |    |    | 1  |
| 1      | 1  | 1  | 1  |    |

$$\Rightarrow f_{217}(x,y,z) = \bar{y}\bar{z} + yz + \bar{x}\bar{y}$$



f<sub>231</sub>)

|        |    |    |    |    |
|--------|----|----|----|----|
| xy \ z | 00 | 01 | 11 | 10 |
| 0      | 1  | 1  | 1  |    |
| 1      | 1  |    | 1  | 1  |

$$\Rightarrow f_{231}(x,y,z) = \bar{x}\bar{y} + y\bar{z} + xz$$

→ Calculamos las formas no simplificables de f<sub>63</sub>, f<sub>82</sub> y f<sub>83</sub> por petrick y Quine.

f<sub>63</sub>).

|   |                                     |                               |                                     |                               |                               |                         |
|---|-------------------------------------|-------------------------------|-------------------------------------|-------------------------------|-------------------------------|-------------------------|
|   | m <sub>2</sub><br>$\bar{x}y\bar{z}$ | m <sub>3</sub><br>$\bar{x}yz$ | m <sub>4</sub><br>$x\bar{y}\bar{z}$ | m <sub>5</sub><br>$x\bar{y}z$ | m <sub>6</sub><br>$xy\bar{z}$ | m <sub>7</sub><br>$xyz$ |
| x |                                     |                               | X                                   | X                             | X                             | X                       |
| y | X                                   | X                             |                                     |                               | X                             | X                       |

Tanto x como y son monomios o fundamentales para la exp. de f. → ~~pr~~ implicantes primos esenciales.

→ f<sub>63</sub>) (x,y,z) = x+y.

f<sub>82</sub>)

|   |                                     |                               |                               |
|---|-------------------------------------|-------------------------------|-------------------------------|
|   | m <sub>1</sub><br>$\bar{x}\bar{y}z$ | m <sub>3</sub><br>$\bar{x}yz$ | m <sub>6</sub><br>$xy\bar{z}$ |
| A | $xy\bar{z}$                         |                               | X                             |
| B | $\bar{x}z$                          | X                             | X                             |

Ambos i. primos esenciales.

$$\begin{matrix} m_1 \equiv B \\ m_2 \equiv B \\ m_3 \equiv A \end{matrix} \left\{ \Rightarrow A \cdot B \Rightarrow A+B \right.$$

AB    ↑

f<sub>82</sub>) (x,y,z) =  $xy\bar{z} + \bar{x}z$ .

f<sub>103</sub>) (x,y,z) =

|             |                                     |                                     |                               |                               |                         |
|-------------|-------------------------------------|-------------------------------------|-------------------------------|-------------------------------|-------------------------|
|             | m <sub>1</sub><br>$\bar{x}\bar{y}z$ | m <sub>2</sub><br>$\bar{x}y\bar{z}$ | m <sub>5</sub><br>$x\bar{y}z$ | m <sub>6</sub><br>$xy\bar{z}$ | m <sub>7</sub><br>$xyz$ |
| xy          |                                     |                                     |                               | X                             | X                       |
| xz          |                                     |                                     | X                             |                               | X                       |
| $\bar{y}z$  | X                                   |                                     | X                             |                               |                         |
| y $\bar{z}$ |                                     | X                                   |                               | X                             |                         |

$\bar{y}z$   
 $y\bar{z}$  } i. primos esenciales

elegir entre  $\begin{cases} xy \\ xz \end{cases}$ .

Formas óptimas

$$\left\{ \begin{array}{l} \rightarrow f_{103}(x,y,z) = xy + y\bar{z} + \bar{y}z \\ \rightarrow f_{103}(x,y,z) = xz + y\bar{z} + \bar{y}z. \end{array} \right.$$

2.16 Sean  $f_i : B^4 \rightarrow B$  las funciones booleanas de 4 variables con  $i = 13244, 43944$  y  $62640$ . Halla:

a)  $\rightarrow$  sus formas canónicas disyuntivas y conjuntivas

b)  $\rightarrow$  sus implicantes primos.

c)  $\rightarrow$  sus formas canónicas disyuntivas reducidas.

d)  $\rightarrow$  sus formas no simplificables.

$$\textcircled{1} = 13244 = 0011001110111100$$

$$\textcircled{2} = 43944 = 1010101110101000$$

$$\textcircled{3} = 62640 = 1111010010110000$$

a) FORMAS CANÓNICAS DISYUNTIVAS:

$$\begin{aligned} f_1(x,y,z,t) &= m_2 + m_3 + m_6 + m_7 + m_8 + m_{10} + m_{11} + m_{12} + m_{13} = \\ &= \bar{x}\bar{y}z\bar{t} + \bar{x}\bar{y}zt + \bar{x}y\bar{z}\bar{t} + \bar{x}y\bar{z}t + x\bar{y}\bar{z}\bar{t} + x\bar{y}\bar{z}t + x\bar{y}z\bar{t} + xy\bar{z}\bar{t} + xy\bar{z}t. \end{aligned}$$

$$\begin{aligned} f_2(x,y,z,t) &= m_0 + m_2 + m_4 + m_6 + m_7 + m_8 + m_{10} + m_{12} = \\ &= \bar{x}\bar{y}\bar{z}\bar{t} + \bar{x}\bar{y}\bar{z}t + \bar{x}\bar{y}z\bar{t} + \bar{x}\bar{y}zt + \bar{x}y\bar{z}\bar{t} + \bar{x}y\bar{z}t + x\bar{y}\bar{z}\bar{t} + x\bar{y}\bar{z}t. \end{aligned}$$

$$\begin{aligned} f_3(x,y,z,t) &= m_0 + m_1 + m_2 + m_3 + m_5 + m_8 + m_{10} + m_{11} = \\ &= \bar{x}\bar{y}\bar{z}\bar{t} + \bar{x}\bar{y}\bar{z}t + \bar{x}\bar{y}z\bar{t} + \bar{x}\bar{y}zt + \bar{x}y\bar{z}\bar{t} + x\bar{y}\bar{z}\bar{t} + x\bar{y}\bar{z}t + x\bar{y}z\bar{t}. \end{aligned}$$

F.C. CONJUNTIVAS:

$$\begin{aligned} f_1(x,y,z,t) &= M_0 \cdot M_1 \cdot M_4 \cdot M_5 \cdot M_9 \cdot M_{14} \cdot M_{15} = \\ &= (x+y+z+t)(x+y+z+\bar{t})(x+\bar{y}+z+t)(x+\bar{y}+z+\bar{t})(\bar{x}+y+z+\bar{t})(\bar{x}+\bar{y}+z+t)(\bar{x}+\bar{y}+\bar{z}+\bar{t}) \end{aligned}$$

$$\begin{aligned} f_2(x,y,z,t) &= M_1 \cdot M_3 \cdot M_5 \cdot M_9 \cdot M_{11} \cdot M_{13} \cdot M_{14} \cdot M_{15} = \\ &= (x+y+z+\bar{t})(x+y+\bar{z}+\bar{t})(x+\bar{y}+z+\bar{t})(\bar{x}+y+z+\bar{t})(\bar{x}+\bar{y}+\bar{z}+\bar{t})(\bar{x}+\bar{y}+z+t)(\bar{x}+\bar{y}+\bar{z}+t) \end{aligned}$$

$$\begin{aligned} f_3(x,y,z,t) &= M_4 \cdot M_6 \cdot M_7 \cdot M_9 \cdot M_{12} \cdot M_{13} \cdot M_{14} \cdot M_{15} = \\ &= (x+\bar{y}+z+t)(x+\bar{y}+\bar{z}+t)(x+\bar{y}+\bar{z}+\bar{t})(\bar{x}+y+z+\bar{t})(\bar{x}+\bar{y}+z+t)(\bar{x}+\bar{y}+z+\bar{t})(\bar{x}+\bar{y}+\bar{z}+t)(\bar{x}+\bar{y}+\bar{z}+\bar{t}) \end{aligned}$$



b) IMPLICANTES PRIMOS  $\rightarrow$  Aplicamos Quine

81:

|                     |           |         |
|---------------------|-----------|---------|
| $xy\bar{z}t$        | 1 1 0 1 X | 1 1 0 - |
| $\bar{x}yzt$        | 0 1 1 1 X | 0 - 1 1 |
| $x\bar{y}zt$        | 1 0 1 1 X | 0 1 1 - |
| $\bar{x}\bar{y}zt$  | 0 0 1 1 X | 1 0 1 - |
| $\bar{x}yzt\bar{t}$ | 0 1 1 0 X | 0 - 1 1 |
| $x\bar{y}zt\bar{t}$ | 1 0 1 0 X | 0 1 1 - |
| $xy\bar{z}\bar{t}$  | 1 1 0 0 X | - 0 1 1 |
| $\bar{x}yzt$        | 0 1 1 1 X | 1 0 1 - |
| $x\bar{y}zt$        | 1 0 1 1 X |         |

|                           |           |           |         |
|---------------------------|-----------|-----------|---------|
| $\bar{x}yzt$              | 0 1 1 1 X | 0 - 1 1 X | 0 - 1 - |
| $x\bar{y}zt$              | 1 0 1 1 X | 0 1 1 - X | - 0 1 - |
| $xy\bar{z}t$              | 1 1 0 1 X | 1 0 1 - X |         |
| $\bar{x}\bar{y}zt$        | 0 0 1 1 X | 1 1 0 -   |         |
| $\bar{x}yzt\bar{t}$       | 0 1 1 0 X | 0 0 1 - X |         |
| $x\bar{y}zt\bar{t}$       | 1 0 1 0 X | 0 - 1 0 X |         |
| $xy\bar{z}\bar{t}$        | 1 1 0 0 X | 1 0 1 0   |         |
| $\bar{x}yzt\bar{t}$       | 1 1 0 0 X | 1 0 - 0   |         |
| $\bar{x}\bar{y}zt\bar{t}$ | 0 0 1 0 X | 1 - 0 0   |         |
| $x\bar{y}zt\bar{t}$       | 1 0 0 0 X |           |         |

$$= xy\bar{z} + \bar{y}z\bar{t} + x\bar{y}\bar{t} + x\bar{z}\bar{t} + \bar{x}z + \bar{y}z.$$

FORMA CANÓNICA REDUCIDA.

e  
IMPLICANTES PRIMOS.

82:

|                           |           |           |         |
|---------------------------|-----------|-----------|---------|
| $\bar{x}yzt$              | 0 1 1 1 X | 0 1 1 -   | 0 - - 0 |
| $\bar{x}yzt\bar{t}$       | 0 1 1 0 X | 0 - 1 0 X | - 0 - 0 |
| $x\bar{y}zt$              | 1 0 1 0 X | 0 1 - 0 X | - - 0 0 |
| $x\bar{y}zt\bar{t}$       | 1 1 0 0 X | - 0 1 0 X |         |
| $\bar{x}\bar{y}zt\bar{t}$ | 0 0 1 0 X | 1 0 - 0 X |         |
| $\bar{x}yzt\bar{t}$       | 0 1 0 0 X | - 1 0 0 X |         |
| $x\bar{y}zt\bar{t}$       | 1 0 0 0 X | 1 - 0 0 X |         |
| $\bar{x}\bar{y}zt\bar{t}$ | 0 0 0 0 X | 0 0 - 0 X |         |
|                           |           | 0 - 0 0 X |         |
|                           |           | - 0 0 0 X |         |

$$= \bar{x}yz + \bar{x}\bar{t} + \bar{y}\bar{t} + \bar{z}\bar{t}$$

Forma Canónica Reducida

e  
Implicantes primos.



③:

|   |    |    |    |    |    |
|---|----|----|----|----|----|
|   |    | y  |    | x  |    |
|   |    | 00 | 01 | 11 | 10 |
| z | t  | 00 | 1  |    | 1  |
|   | 01 | 1  | 1  |    |    |
|   | 11 | 1  |    |    | 1  |
|   | 10 | 1  |    |    | 1  |

$$\Rightarrow f_3 = \bar{x}\bar{y} + \bar{y}\bar{z}\bar{t} + \bar{x}\bar{z}t + x\bar{y}z$$

↑  
FORMA REDUCIDA (CANÓNICA)

↑  
e  
Implicantes primos.

↑  
Forma no simplificable.

c) → Ya hemos hallado en el paso anterior las formas canónicas disyuntivas reducidas.

d) →

④:

|                   | m <sub>2</sub><br>$\bar{x}\bar{y}z\bar{t}$ | m <sub>3</sub><br>$\bar{x}\bar{y}zt$ | m <sub>6</sub><br>$\bar{x}yz\bar{t}$ | m <sub>7</sub><br>$\bar{x}yzt$ | m <sub>8</sub><br>$x\bar{y}\bar{z}\bar{t}$ | m <sub>10</sub><br>$x\bar{y}z\bar{t}$ | m <sub>11</sub><br>$x\bar{y}zt$ | m <sub>12</sub><br>$xy\bar{z}\bar{t}$ | m <sub>13</sub><br>$xy\bar{z}t$ |
|-------------------|--|--------------------------------------|--------------------------------------|--------------------------------|--|---------------------------------------|---------------------------------|---------------------------------------|---------------------------------|
| $x\bar{y}\bar{z}$ |  |                                      |                                      |                                |  |                                       |                                 | X                                     | X                               |
| $x\bar{y}t$       |  |                                      |                                      |                                | X  | X                                     |                                 |                                       |                                 |
| $x\bar{z}\bar{t}$ |  |                                      |                                      |                                | X  |                                       |                                 | X                                     |                                 |
| $\bar{y}z\bar{t}$ | X  |                                      |                                      |                                |  | X                                     |                                 |                                       |                                 |
| $\bar{x}z$        | X  | X                                    | X                                    | X                              |  |                                       |                                 |                                       |                                 |
| $\bar{y}z$        | X  | X                                    |                                      |                                |  | X                                     | X                               |                                       |                                 |

Vemos que son implic. primos esenciales:  $\bar{x}z$ ,  $\bar{y}z$ ,  $x\bar{y}\bar{z}$

El único minterm que no queda representado por alguno de estos términos anteriores es, m<sub>8</sub>. Luego la forma no simplificable de ④ queda:

$$f_4(x, y, z, t) = \begin{cases} \bar{x}z + \bar{y}z + x\bar{y}\bar{z} + x\bar{y}t \\ \bar{x}z + \bar{y}z + x\bar{y}\bar{z} + x\bar{z}\bar{t} \end{cases} \quad (2 \text{ posibles F.N.S.})$$

f2:

|   |                  | m <sub>0</sub>                 | m <sub>2</sub>           | m <sub>4</sub>           | m <sub>6</sub>     | m <sub>7</sub> | m <sub>8</sub>           | m <sub>10</sub>    | m <sub>12</sub> |
|---|------------------|--------------------------------|--------------------------|--------------------------|--------------------|----------------|--------------------------|--------------------|-----------------|
|   |                  | $\bar{x}\bar{y}\bar{z}\bar{t}$ | $\bar{x}\bar{y}z\bar{t}$ | $\bar{x}y\bar{z}\bar{t}$ | $\bar{x}yz\bar{t}$ | $\bar{x}yzt$   | $x\bar{y}\bar{z}\bar{t}$ | $x\bar{y}z\bar{t}$ | $xyz\bar{t}$    |
| A | $\bar{x}yz$      |                                |                          |                          | x                  | x              |                          |                    |                 |
| B | $\bar{x}\bar{t}$ | x                              | x                        | x                        | x                  |                |                          |                    |                 |
| C | $\bar{y}\bar{t}$ | x                              | x                        |                          |                    |                | x                        | x                  |                 |
| D | $\bar{z}\bar{t}$ | x                              |                          | x                        |                    |                | x                        |                    | x               |

→ I. Primos esenciales =  $\bar{x}yz$ ,  $\bar{y}\bar{t}$ ,  $\bar{z}\bar{t}$ .

Todos los minterms ~~est~~ contienen al menos alguno de estos términos (I.P.E.) luego la forma no simplif. queda:

f2(x,y,z,t) =  $\bar{x}yz + \bar{y}\bar{t} + \bar{z}\bar{t}$ .

Comprobamos con Petrick:

$$\left. \begin{array}{lll} m_0 = B+C+D & m_6 = A+B & m_{10} = C \\ m_2 = B+C & m_7 = A & m_{12} = D \\ m_4 = B+D & m_8 = C+D & \end{array} \right\} f = A+C+D.$$

$\left. \begin{array}{l} m_0 \checkmark \\ m_2 \checkmark \\ m_4 \checkmark \\ m_6 \checkmark \\ m_7 \checkmark \\ m_8 \checkmark \\ m_{10} \checkmark \\ m_{12} \checkmark \end{array} \right\}$

f3: (comprobación).

|                         | m <sub>0</sub>                 | m <sub>1</sub>           | m <sub>2</sub>           | m <sub>3</sub>     | m <sub>5</sub> | m <sub>8</sub>           | m <sub>10</sub>    | m <sub>11</sub> |
|-------------------------|--------------------------------|--------------------------|--------------------------|--------------------|----------------|--------------------------|--------------------|-----------------|
|                         | $\bar{x}\bar{y}\bar{z}\bar{t}$ | $\bar{x}y\bar{z}\bar{t}$ | $\bar{x}\bar{y}z\bar{t}$ | $\bar{x}yz\bar{t}$ | $\bar{x}yzt$   | $x\bar{y}\bar{z}\bar{t}$ | $x\bar{y}z\bar{t}$ | $x\bar{y}zt$    |
| $x\bar{y}z$             |                                |                          |                          |                    |                |                          | x                  | x               |
| $\bar{x}\bar{z}\bar{t}$ |                                | x                        |                          |                    | x              |                          |                    |                 |
| $\bar{y}\bar{z}\bar{t}$ | x                              |                          |                          |                    |                | x                        |                    |                 |
| $\bar{x}\bar{y}$        | x                              | x                        | x                        | x                  |                |                          |                    |                 |

→ I. Primos esenciales =  $x\bar{y}z$ ,  $\bar{x}\bar{z}\bar{t}$ ,  $\bar{y}\bar{z}\bar{t}$ ,  $\bar{x}\bar{y}$ .

Efectivamente, la forma no simplificable de f3 es:

f3(x,y,z,t) =  $x\bar{y}z + \bar{x}\bar{z}\bar{t} + \bar{y}\bar{z}\bar{t} + \bar{x}\bar{y}$