

`In[]:= Remove["Global`*"]`

checking answer to pb 2

`In[]:= sol1 = DSolve[{y'[x] - y[x] == 2 x * Exp[2 x]}, y[x], x]`

`Out[]:=` $\left\{ \left\{ y[x] \rightarrow 2 e^{2x} (-1 + x) + e^x c_1 \right\} \right\}$

`In[]:= sol = DSolve[{y'[x] - y[x] == 2 x * Exp[2 x], y[0] == 1}, y[x], x]`

`Out[]:=` $\left\{ \left\{ y[x] \rightarrow e^x (3 - 2 e^x + 2 e^x x) \right\} \right\}$

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`y[x] /. sol[[1]]`

`Out[]:=` $\left\{ \left\{ y[x] \rightarrow e^x (3 - 2 e^x + 2 e^x x) \right\} \right\}$

`Out[]:=` $e^x (3 - 2 e^x + 2 e^x x)$

Pb 4 check

`In[]:= sol4 = DSolve[x^2 (y1''[x]) + 2 x (y1'[x]) - 1 == 0, y1[x], x]`

`Out[]:=` $\left\{ \left\{ y1[x] \rightarrow -\frac{c_1}{x} + c_2 + \text{Log}[x] \right\} \right\}$

`In[]:= y1[x] /. sol4[[1]]`

`Out[]:=` $-\frac{c_1}{x} + c_2 + \text{Log}[x]$

Pb 5

`In[]:= usol1 = DSolve[y2''[x] + y2'[x] - 2 y2[x] == 2 x, y2[x], x]`

`Out[]:=` $\left\{ \left\{ y2[x] \rightarrow \frac{1}{2} (-1 - 2x) + e^{-2x} c_1 + e^x c_2 \right\} \right\}$

`In[]:= usol = DSolve[{y2''[x] + y2'[x] - 2 y2[x] == 2 x, y2[0] == 0, y2'[0] == 1}, y2[x], x]`

`Out[]:=` $\left\{ \left\{ y2[x] \rightarrow \frac{1}{2} e^{-2x} (-1 - e^{2x} + 2 e^{3x} - 2 e^{2x} x) \right\} \right\}$

test

`In[]:= Exp[-2 Log[x]]`

`Out[]:=` $\frac{1}{x^2}$