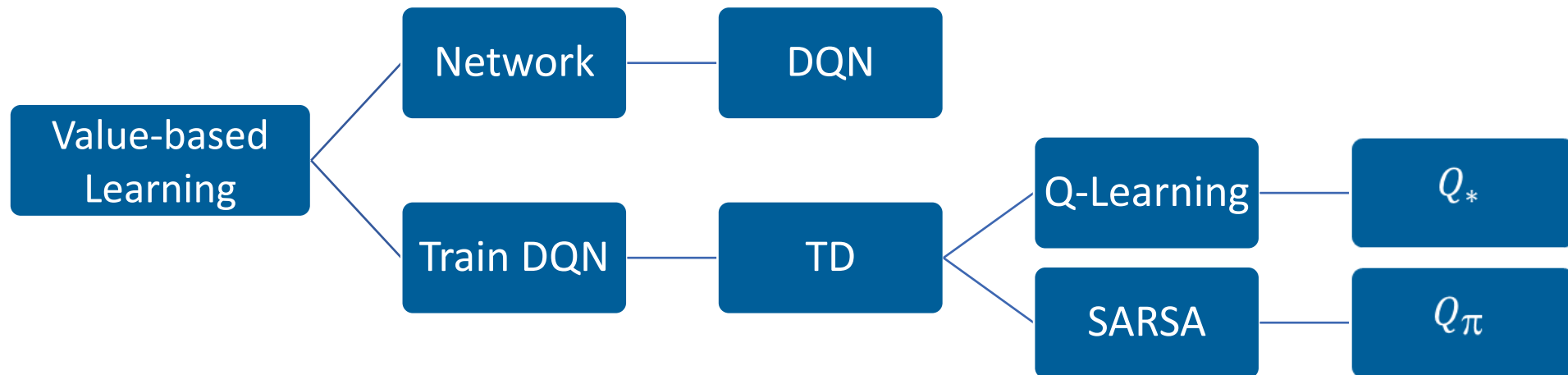


Reinforcement Learning

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Contents



Background

Goal of RL: Maximize sum of rewards.

How: Take the best **action**, basing on $Q^*(s,a)$.

$$a_t = \operatorname{argmax}_a Q(s_t, a, \mathbf{w})$$

Problem: Get to know $Q^*(s,a)$.



DQN

DQN: Neural network named Deep Q Network, denoted as $Q(s,a;\mathbf{w})$.

Goal: Use $Q(s,a;\mathbf{w})$ to approximate $Q^*(s,a)$.



DQN

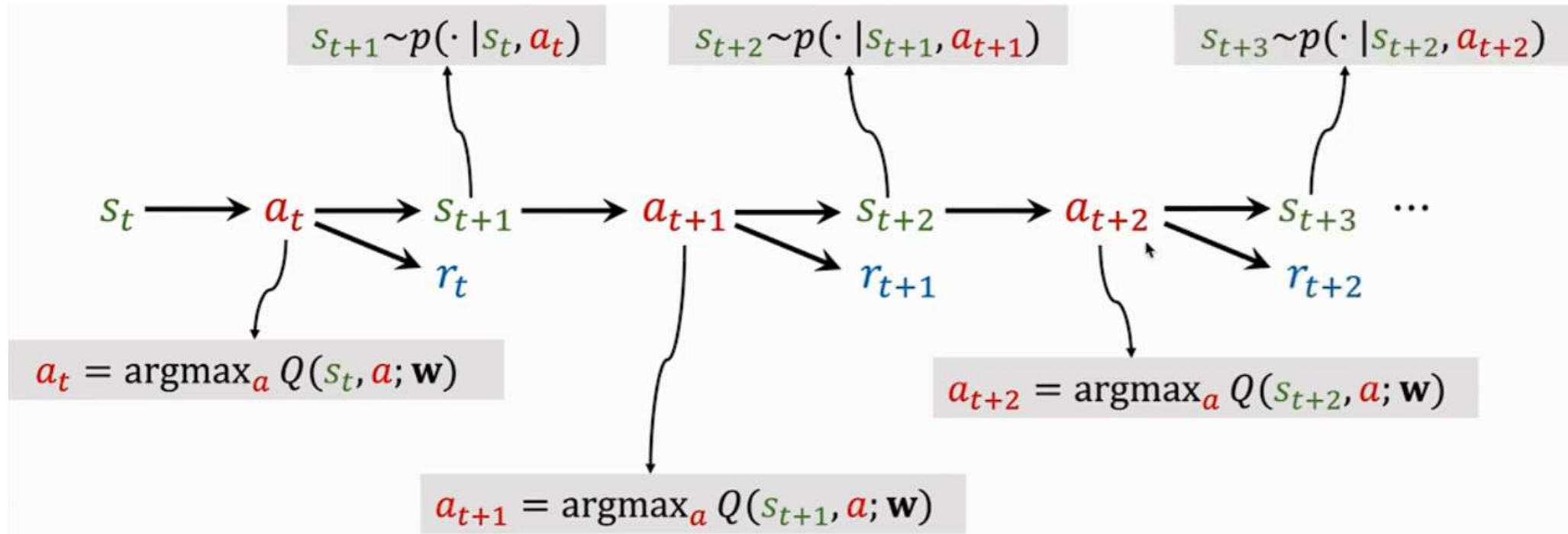


Example: If action space is {"left", "up", "right"}, then **Q** is a

3-dimensional vector $\begin{pmatrix} Q(s_t, "left"; \mathbf{w}_t) \\ Q(s_t, "up"; \mathbf{w}_t) \\ Q(s_t, "right"; \mathbf{w}_t) \end{pmatrix}$

DQN

Apply DQN in a game



TD – Q-Learning

TD: Temporal difference, used to **train DQN**, including Q-Learning & SARSA.

Q-Learning aims to approximate Q^* , while **SARSA** aims to approximate Q_π .



TD – Q-Learning

Observe transition: (s_t, a_t, r_t, s_{t+1})

$$\hat{q} = Q(s_t, a_t; \mathbf{w})$$

TD target: $y_t = r_t + \gamma * \max_a Q(s_{t+1}, a; \mathbf{w}) \rightarrow \text{Bellman Optimality Equation}$

TD error: $\delta_t = Q(s_t, a_t; \mathbf{w}) - y_t$

Loss: $\delta_t^2 / 2$

Gradient: $\frac{\partial \delta_t^2 / 2}{\partial \mathbf{w}} = \delta_t * \frac{\partial Q(s_t, a_t; \mathbf{w})}{\partial \mathbf{w}}$

Update: $\mathbf{w} \leftarrow \mathbf{w} - \alpha * \delta_t * \frac{\partial Q(s_t, a_t; \mathbf{w})}{\partial \mathbf{w}}$



TD – SARSA

SARSA: **S**tate**A**ction**R**eward**S**tate**A**ction

$$(s_t, a_t, r_t, s_{t+1}, a_{t+1})$$

SARSA is used to approximate Q_π .



TD – SARSA

Observe transition: $(s_t, a_t, r_t, s_{t+1}, a_{t+1})$

$$\hat{q} = q(s_t, a_t; \mathbf{w})$$

TD target: $y_t = r_t + \gamma * q(s_{t+1}, a_{t+1}; \mathbf{w})$

TD error: $\delta_t = q(s_t, a_t; \mathbf{w}) - y_t$

Loss: $\delta_t^2 / 2$

Gradient: $\frac{\partial \delta_t^2 / 2}{\partial \mathbf{w}} = \delta_t * \frac{\partial q(s_t, a_t; \mathbf{w})}{\partial \mathbf{w}}$

Update: $\mathbf{w} \leftarrow \mathbf{w} - \alpha * \delta_t * \frac{\partial q(s_t, a_t; \mathbf{w})}{\partial \mathbf{w}}$



On-policy & off-policy

On-policy: Behavior policy is the same with target policy.

Off-policy: Behavior policy is **not** the same with target policy.

Behavior policy: Used to control agent and gain experience.

Target policy: A certain policy that RL aims to find.

For example, Q-Learning is off-policy while SARSA is on-policy.



Experience replay

Meaning: Save interaction records (experience) into arrays and reuse them later to train the agent.

Advantages: Elimination of relevance and faster convergence speed.

Only applies to **off-policy** solutions.

Thank you.

