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SUBJECT	Design and Analysis of Algorithms
EXPERIMENT No.	7
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AIM:	Backtracking (To implement N Queens problem using backtracking.)
Program 1	
PROBLEM STATEMENT :	Implement the N queen problem for 4x4 chess board.
ALGORITHM/ THEORY:	<p>Step 1 - Place the queen row-wise, starting from the left-most cell.</p> <p>Step 2 - If all queens are placed then return true and print the solution matrix.</p> <p>Step 3 - Else try all columns in the current row.</p> <ul style="list-style-type: none"> • Condition 1 - Check if the queen can be placed safely in this column then mark the current cell [Row, Column] in the solution matrix as 1 and try to check the rest of the problem recursively by placing the queen here leads to a solution or not. • Condition 2 - If placing the queen [Row, Column] can lead to the solution return true and print the solution for each queen's position. • Condition 3 - If placing the queen cannot lead to the solution then unmark this [row, column] in the solution matrix as 0, BACKTRACK, and go back to condition 1 to try other rows. <p>Step 4 - If all the rows have been tried and nothing worked, return false to trigger backtracking.</p>

PROGRAM:

```
#define N 4
#include <stdbool.h>
#include <stdio.h>

/* A utility function to print solution */
void printSolution(int board[N][N])
{
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++)
        {
            //printf(" %d ", board[i][j]);
            if(board[i][j] == 1)
            {
                printf(" Q ");
            }
            else
                printf(" %d ", board[i][j]);

        }
        printf("\n");
    }
}

bool isSafe(int board[N][N], int row, int col)
{
    int i, j;

    /* Check this row on left side */
    for (i = 0; i < col; i++)
        if (board[row][i])
            return false;

    /* Check upper diagonal on left side */
    for (i = row, j = col; i >= 0 && j >= 0; i--, j--)
        if (board[i][j])
            return false;

    /* Check lower diagonal on left side */
    for (i = row, j = col; j >= 0 && i < N; i++, j--)
        if (board[i][j])
            return false;

    return true;
}

/* A recursive utility function to solve N
Queen problem */
```

```

bool solveNQUtil(int board[N][N], int col)
{
    if (col >= N)
        return true;

    for (int i = 0; i < N; i++) {
        /* Check if the queen can be placed on
        board[i][col] */
        if (isSafe(board, i, col)) {
            /* Place this queen in board[i][col] */
            board[i][col] = 1;

            /* recur to place rest of the queens */
            if (solveNQUtil(board, col + 1))
                return true;

            board[i][col] = 0; // BACKTRACK
        }
    }

    return false;
}

bool solveNQ()
{
    int board[N][N] = { { 0, 0, 0, 0 },
                        { 0, 0, 0, 0 },
                        { 0, 0, 0, 0 },
                        { 0, 0, 0, 0 } };

    if (solveNQUtil(board, 0) == false) {
        printf("Solution does not exist");
        return false;
    }

    printSolution(board);
    return true;
}

// driver program to test above function
int main()
{
    solveNQ();
    return 0;
}

```

RESULT:

```
PS C:\Users\smsa\Desktop\SEM 4\DAA\Practicals\Exp7\output> & .\Nqueen.exe  
0 0 Q 0  
Q 0 0 0  
0 0 0 Q  
0 Q 0 0  
PS C:\Users\smsa\Desktop\SEM 4\DAA\Practicals\Exp7\output> █
```

CONCLUSION :

- N Queen problem is a classical puzzle that beautifully develops the concept of *Backtracking*.
- The time complexity of the brute force backtracking algorithm is $O(N \times N!)$. However, using *bitmasking* the time complexity can be optimized to $O(N!)O(N!)$.
- The space complexity irrespective of the approach is $O(N^2)$ because we need to print a 2-dimensional array as the answer.