

# Introduction to Image Processing

Lecture 1  
16<sup>th</sup> Sept. 2015

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## ① Human Vision

Human eye

Image formation in the eye

Brightness adaptation & discrimination

## ② Digital Image

Formation

Sampling & quantisation

## ③ Pixel Relationships

Neighbours

Adjacency

Path

Subset & region

Distance measures



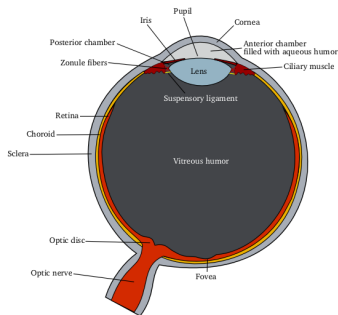
## Human Vision

### Human eye

## From the eye to a camera

### Choroid

- ▶ Composed of blood vessels serving as source of nutrition
- ▶ Avoid the entrance of external light or backscatter
- ▶ See relation with physics experiments





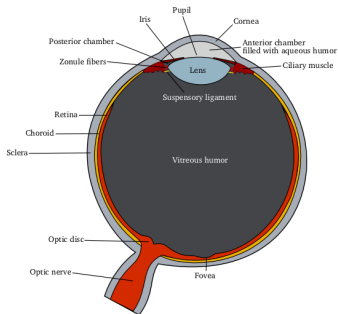
## Human Vision

### Human eye

## From the eye to a camera

### Ciliary body & iris

- ▶ Control the amount of light (2 mm to 8 mm)
- ▶ Relation with the camera aperture





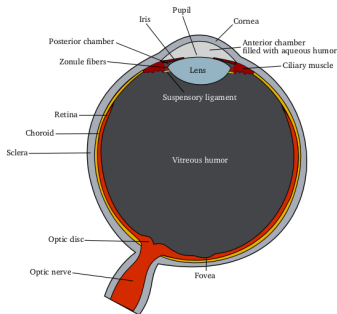
## Human Vision

### Human eye

## From the eye to a camera

### Lens

- ▶ Made of fibrous cells and attached to ciliary body
- ▶ Absorb 8 % of visible light and all the IR and UV
- ▶ Cataract diseases
- ▶ Idem to an optical lens





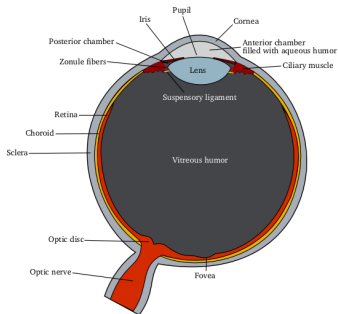
## Human Vision

### Human eye

## From the eye to a camera

### Retina

- ▶ Contains 2 types of discrete light receptors: the cones and the rods
- ▶ Myopia & hyperopia





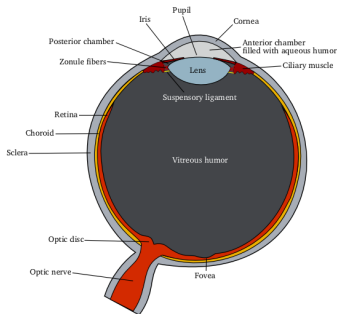
## Human Vision

### Human eye

## From the eye to a camera

### Cones

- ▶ Account for about 6 to 7 million per eye
- ▶ Are sensitive to color and details
- ▶ Each one connected to a single nerve end
- ▶ Cone vision is called *photopic* and is sensitive to high levels of illumination
- ▶ Similar to a high frequency receptor





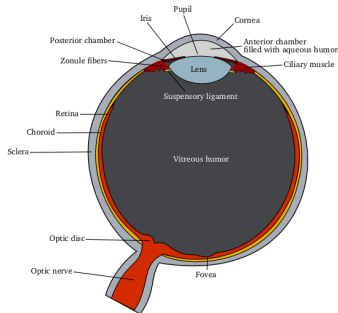
# Human Vision

## Human eye

### From the eye to a camera

#### Rods

- ▶ Account for 75 to 150 millions per eye
- ▶ Not involved in color
- ▶ Give a general and overall picture of the FOV
- ▶ Several rods connected to a single nerve end
- ▶ Sensitive to low levels of illuminations: *scotopic*
- ▶ Similar to a low frequency receptor







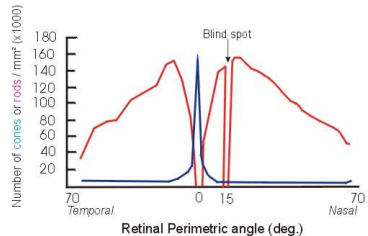
## Human Vision

### Human eye

## From the eye to a camera

### Cones & Rods

- ▶ Symmetrically distributed
- ▶ Note the presence of the blind spot



Adapted after Østerberg, 1935



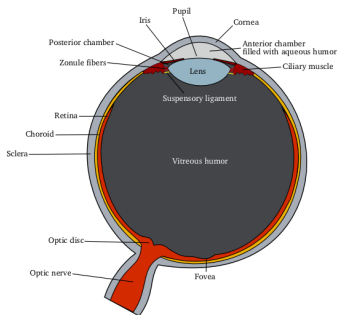
## Human Vision

### Human eye

## From the eye to a camera

### Fovea

- ▶ Localisation of the cones in this area
- ▶  $1.5 \text{ mm} \times 1.5 \text{ mm}$
- ▶ 150,000 elts/ $\text{mm}^2$  to 337,000 elts/ $\text{mm}^2$
- ▶ CCD imaging ship would need a  $5 \text{ mm} \times 5 \text{ mm}$  to achieve similar density

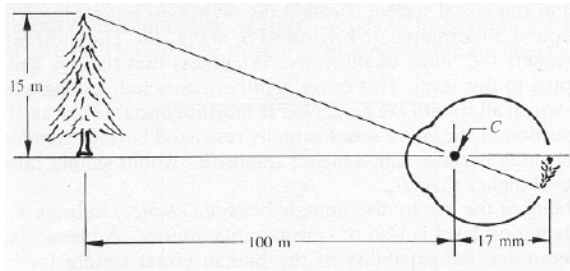




## Human Vision

### Image formation in the eye

#### Example



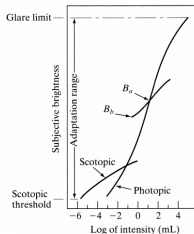
- ▶ Focal length varies from 17 mm to 14 mm
- ▶ Perception takes place by the relative excitation of light receptors.
- ▶ The receptors transform this energy to electrical impulses



## Human Vision Brightness adaptation & discrimination

### Human visual system

- ▶ The human vision system (HVS) can adapt to  $10^{10}$  light intensity levels
- ▶ Subjective brightness is a logarithmic function of the light intensity incident on the eye



- ▶ The HVS cannot operate over such a range simultaneously
- ▶ For a given set of conditions, the current sensitivity level is called *brightness adaptation level*



## Human Vision

### Brightness adaptation & discrimination

#### Human visual system

- ▶ The eye also discriminates between changes in brightness at any specific adaption level
- ▶ This is characterised by the Weber ratio

$$\frac{\Delta I_c}{I}, \quad (1)$$

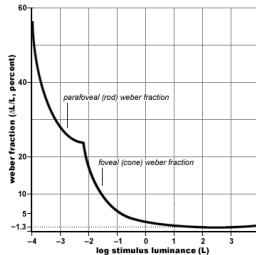
where  $\Delta I_c$  is the increment of illumination discriminable 50 % of the time and  $I$  is the background illumination



## Human Vision

### Brightness adaptation & discrimination

## Human visual system



- ▶ Small values of Weber ratio mean good brightness discrimination and vice versa
- ▶ At low levels of illumination brightness discrimination is poor (rods)
- ▶ It improves significantly as background illumination increases (cones)
- ▶ The typical observer can discern one to two dozen different intensity changes



## Human Vision

### Brightness adaptation & discrimination

#### Human visual system

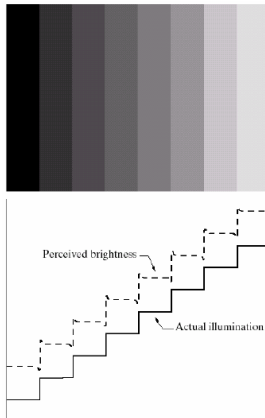
- ▶ Overall intensity discrimination is broad due to different set of incremental changes to be detected at each new adaptation level
- ▶ Perceived brightness is not a simple function of intensity: Mach band effect, simultaneously contrast, and optical effect



## Human Vision

### Brightness adaptation & discrimination

#### Mach band effect







## Human Vision

### Brightness adaptation & discrimination

#### Simultaneously contrast

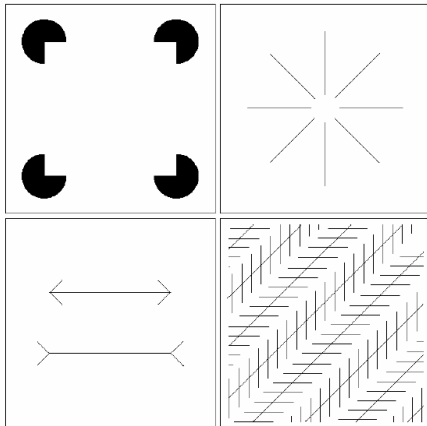




## Human Vision

### Brightness adaptation & discrimination

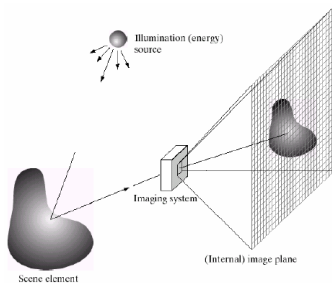
#### Optical effect





## Digital Image

### Digital image formation

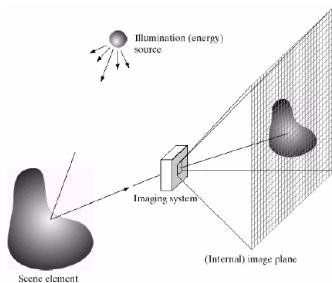


- ▶  $f(x, y)$ : intensity or brightness of a pixel at a position  $(x, y)$
- ▶  $0 < f(x, y) < +\infty$



## Digital Image

### Digital image formation

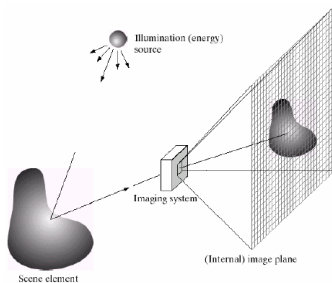


- $r(x, y)$ : illumination —  $[0, +\infty[$



## Digital Image

### Digital image formation

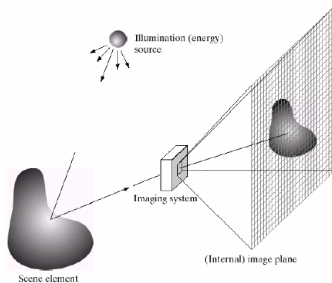


- ▶  $r(x, y)$ : illumination —  $[0, +\infty[$
- ▶  $i(x, y)$ : reflectance —  $[0, 1]$



## Digital Image

### Digital image formation



- ▶  $r(x, y)$ : illumination —  $[0, +\infty[$
- ▶  $i(x, y)$ : reflectance —  $[0, 1]$
- ▶  $f(x, y) = r(x, y)i(x, y)$



## Digital Image

### Example of reflectance

- ▶ Black velvet: 0.01
- ▶ Snow: 0.93

### Example of illumination

- ▶ Sunny day: 9000 foot-candles
- ▶ Cloudy day: 1000 foot-candles
- ▶ Full moon: 0.01 foot-candles



## Digital Image

### In practise

- ▶  $i(x, y)$  and  $r(x, y)$  are bounded

$$i_{\min}(x_0, y_0) r_{\min}(x_0, y_0) < f(x_0, y_0) < i_{\max}(x_0, y_0) r_{\max}(x_0, y_0) , \quad (2)$$

$$L_{\min} < f(x_0, y_0) < L_{\max} . \quad (3)$$

- ▶  $[L_{\min}, L_{\max}] \approx [10, 1000]$  — Shifted in  $[0, L - 1]$





## Digital Image

### In practise

- ▶  $i(x, y)$  and  $r(x, y)$  are bounded

$$i_{\min}(x_0, y_0) r_{\min}(x_0, y_0) < f(x_0, y_0) < i_{\max}(x_0, y_0) r_{\max}(x_0, y_0) , \quad (2)$$

$$L_{\min} < f(x_0, y_0) < L_{\max} . \quad (3)$$

- ▶  $[L_{\min}, L_{\max}] \approx [10, 1000]$  — Shifted in  $[0, L - 1]$

→ What is the value for true white and black colors in an image?



## Digital Image

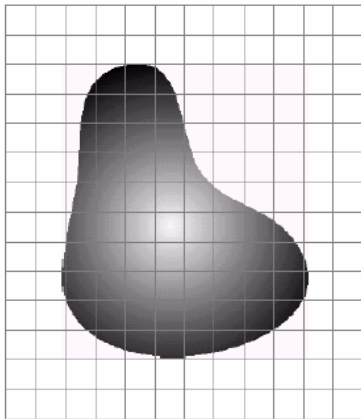
### Conversion from continuous to digital

- ▶  $f(x, y)$  is a continuous function with regarding the coordinates and the amplitude
- ▶ Image sampling to refer to spatial coordinates
- ▶ Signal quantisation to digitise the amplitude



## Digital Image

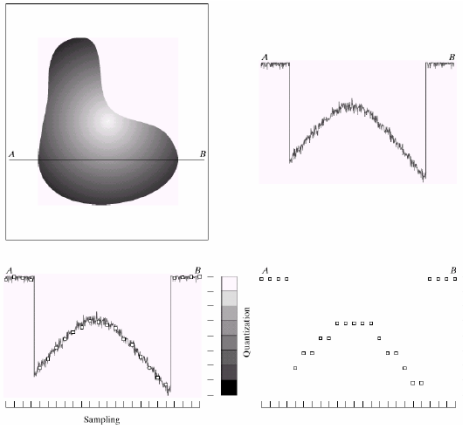
### Sampling





## Digital Image

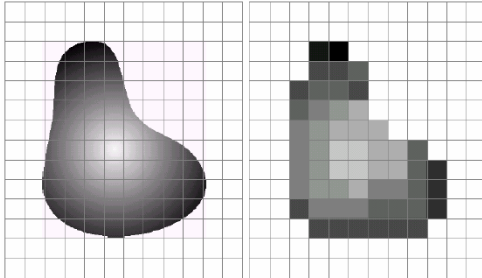
### Quantisation





## Digital Image

### Digital image

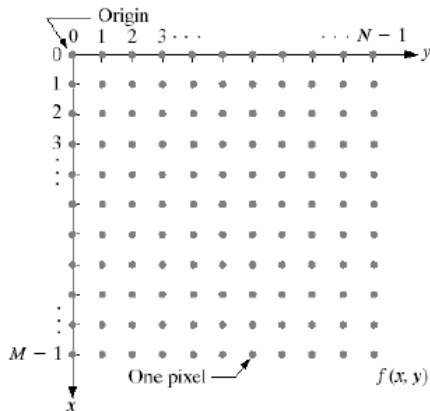


► Check the appendix notebook



## Digital Image

### Coordinate system convention





## Digital Image

### Digitisation requirements

- ▶ Set an height:  $M$
- ▶ Set an width:  $N$
- ▶ Set an intensity level:  $L = 2^k$  and equally spaced
- ▶ *Dynamic range* :  $\frac{L_{\min}}{L_{\max}}$





## Digital Image

### Parameter variations

$N/k$	1 ( $L = 2$ )	2 ( $L = 4$ )	3 ( $L = 8$ )	4 ( $L = 16$ )	5 ( $L = 32$ )	6 ( $L = 64$ )	7 ( $L = 128$ )	8 ( $L = 256$ )
32	1,024	2,048	3,072	4,096	5,120	6,144	7,168	8,192
64	4,096	8,192	12,288	16,384	20,480	24,576	28,672	32,768
128	16,384	32,768	49,152	65,536	81,920	98,304	114,688	131,072
256	65,536	131,072	196,608	262,144	327,680	393,216	458,752	524,288
512	262,144	524,288	786,432	1,048,576	1,310,720	1,572,864	1,835,008	2,097,152
1024	1,048,576	2,097,152	3,145,728	4,194,304	5,242,880	6,291,456	7,340,032	8,388,608
2048	4,194,304	8,388,608	12,582,912	16,777,216	20,971,520	25,165,824	29,369,128	33,554,432
4096	16,777,216	33,554,432	50,331,648	67,108,864	83,886,080	100,663,296	117,440,512	134,217,728
8192	67,108,864	134,217,728	201,326,592	268,435,456	335,544,320	402,653,184	469,762,048	536,870,912

→ What is the best values regarding the resolution and dynamic range parameters?

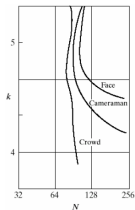
- ▶ Larger is better ...
- ▶ ... storage and processing could be a problem





## Digital Image

### Isopreference curves





## Digital Image

Non-uniform sampling and quantisation



## Digital Image

### Non-uniform sampling and quantisation

- ▶ Fine sampling in details region — coarse sampling in smooth region



## Digital Image

### Non-uniform sampling and quantisation

- ▶ Fine sampling in details region — coarse sampling in smooth region
- ▶ Few gray levels in details regions — more in smooth region



## Pixel Relationships

### Neighbours

*4-neighbours* —  $N_4$ -p

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*D-neighbours* —  $N_D$ -p

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*8-neighbours* —  $N_8$ -p

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1



## Pixel Relationships

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1	0	1	1	0
0	1	1	0	1





## Pixel Relationships

### Adjacency

Let denotes  $V = \{1\}$  defining the adjacency

*4-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*8-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*m-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
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0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
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*m-adjacency*

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0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*m-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

$q \in N_4(p)$



## Pixel Relationships

### Adjacency

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0	1	0	0	1
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1	0	1	1	0
0	1	1	0	1

*8-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*m-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

$q \in N_D(p)$



# Pixel Relationships

## Adjacency

Let denotes  $V = \{1\}$  defining the adjacency

*4-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*8-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*m-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

$q \in N_D(p)$  AND  
 $N_4(p) \cap N_4(q) \notin V$



## Pixel Relationships

### Adjacency

Let  $V = \{1\}$  defining the adjacency

*4-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*8-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1

*m-adjacency*

0	1	1	1	0
0	1	0	0	1
0	0	1	0	0
1	0	1	1	0
0	1	1	0	1



## Pixel Relationships

Path

0	1	1	1	0
0	1	0	0	1
0	1	1	0	0
1	0	1	1	0
0	1	1	1	1





## Pixel Relationships

### Path

4-path

0	1	1	1	0
0	1	0	0	1
0	1	1	0	0
1	0	1	1	0
0	1	1	1	1



## Pixel Relationships

### Path

8-path

0	1	1	1	0
0	1	0	0	1
0	1	1	0	0
1	0	1	1	0
0	1	1	1	1



## Pixel Relationships

### Path

m-path

0	1	1	1	0
0	1	0	0	1
0	1	1	0	0
1	0	1	1	0
0	1	1	1	1

- ▶ if  $(x_{init}, y_{init}) = (x_{end}, y_{end}) \rightarrow$  closed path



## Pixel Relationships

### Subset

- ▶  $p$  and  $q$  are *connected* in the subset  $S$  if there is a path in with all the pixels belonging to  $S$
- ▶ For any pixel  $p$  in  $S$ , the set of pixels in  $S$  that are connected to  $p$  is a *connected component* of  $S$
- ▶ If  $S$  has only one connected component then  $S$  is called a *connected set*

### Region

- ▶  $R$  is a subset of pixels:  $R$  is a region if  $R$  is a connected set
- ▶ Region can be *adjacent* or *disjoint*



## Pixel Relationships

### Distance measures

#### Definition

For pixels  $p, q, z$  with coordinates  $(x, y), (s, t), (u, v)$ ,  $D$  is a distance function or metric if:

- ▶  $D(p, q) \geq 0$  ( $D(p, q) = 0$  iff  $p = q$ )
- ▶  $D(p, q) = D(q, p)$  and
- ▶  $D(p, z) \leq D(p, q) + D(q, z)$



## Pixel Relationships

### Distance measures

#### Euclidean distance

For pixels  $p, q, z$  with coordinates  $(x, y)$ ,  $(s, t)$ ,  $(u, v)$ :

$$\blacktriangleright D_e(p, q) = \sqrt{(x - s)^2 + (y - t)^2}$$

#### $D_4$ distance

$$\blacktriangleright D_4(p, q) = |x - s| + |y - t|$$

#### $D_8$ distance

$$\blacktriangleright D_8(p, q) = \max(|x - s|, |y - t|)$$

#### $D_m$ distance

$\blacktriangleright$  Shortest  $m$ -path considering the  $m$ -adjacency