



IOE 511/MATH 562 - Continuous Optimization Methods Project Problems - Winter 2023

Problem 1 P1_quad_10_10:

$$f(x) = \frac{1}{2}x^T Q x + q^T x$$

where $q \in \mathbb{R}^n$ and $Q \in \mathbb{R}^{n \times n}$. A randomly generated convex quadratic function. Dimension n = 10; Condition number $\kappa = 10$. Starting Point: rng(0); x_0=20*rand(10,1)=10.

(Functions provided: function, gradient, Hessian)

Problem 2 P2_quad_10_1000:

$$f(x) = \frac{1}{2}x^T Q x + q^T x$$

where $q \in \mathbb{R}^n$ and $Q \in \mathbb{R}^{n \times n}$. A randomly generated convex quadratic function. Dimension n = 10; Condition number $\kappa = 1000$. Starting Point: rng(0); x_0=20*rand(10,1)=10.

(Functions provided: function)

Problem 3 P3_quad_1000_10:

$$f(x) = \frac{1}{2}x^T Q x + q^T x$$

where $q \in \mathbb{R}^n$ and $Q \in \mathbb{R}^{n \times n}$. A randomly generated convex quadratic function. Dimension n = 1000; Condition number $\kappa = 10$. Starting Point: rng(0); x_0=20*rand(1000,1)=10.

(Functions provided: function)

Problem 4 P4_quad_1000_1000:

$$f(x) = \frac{1}{2}x^T Q x + q^T x$$

where $q \in \mathbb{R}^n$ and $Q \in \mathbb{R}^{n \times n}$. A randomly generated convex quadratic function. Dimension n = 1000; Condition number $\kappa = 1000$. Starting Point: rng(0); x_0=20*rand(1000,1)=10.

(Functions provided: function)

Problem 5 P5_quartic_1:

$$f(x) = \frac{1}{2}x^T x + \frac{\sigma}{4}(x^T Q x)^2$$

where $\sigma = 10^{-4}$ and $A \in \mathbb{R}^{n \times n}$. The dimension n = 4, and the matrix A is given by

$$Q = \begin{bmatrix} 5 & 1 & 0 & 0.5 \\ 1 & 4 & 0.5 & 0 \\ 0 & 0.5 & 3 & 0 \\ 0.5 & 0 & 0 & 2 \end{bmatrix}.$$

Starting Point: $x_0 = [\cos(70) \sin(70) \cos(70) \sin(70)]^T$.

(Functions provided: function)

Problem 6 P6_quartic_2:

$$f(x) = \frac{1}{2}x^T x + \frac{\sigma}{4}(x^T Q x)^2$$

where $\sigma = 10^4$ and $A \in \mathbb{R}^{n \times n}$. The dimension n = 4, and the matrix A is given by

$$Q = \begin{bmatrix} 5 & 1 & 0 & 0.5 \\ 1 & 4 & 0.5 & 0 \\ 0 & 0.5 & 3 & 0 \\ 0.5 & 0 & 0 & 2 \end{bmatrix}.$$

Starting Point: $x_0 = [\cos(70) \sin(70) \cos(70) \sin(70)]^T$.

(Functions provided: function)

Problem 7 Rosenbrock_2:

$$f(x) = (1 - x_{[1]})^2 + 100(x_{[2]} - x_{[1]}^2)^2$$
, where $x = [x_{[1]} \ x_{[2]}]^T \in \mathbb{R}^2$.

Dimension n = 2. Starting Point: $x_0 = [-1.2 \ 1]^T$.

(Functions provided: none-this function was studied in HW2)

Problem 8 Rosenbrock_100:

$$f(x) = \sum_{i=1}^{99} [(1 - x_{[i]})^2 + 100(x_{[i+1]} - x_{[i]}^2)^2], \text{ where } x \in \mathbb{R}^{100}.$$

Dimension n = 100. Starting Point: $x_0 = [-1.2 \ 1 \ \cdots \ 1]^T$.

(Functions provided: none)

Problem 9 DataFit_2:

$$f(x) = \sum_{i=1}^{3} (y_{[i]} - x_{[1]}(1 - x_{[2]}^{i}))^{2}$$
, where $x = [x_{[1]} \ x_{[2]}]^{T} \in \mathbb{R}^{2}$,

where $y = [1.5 \ 2.25 \ 2.625]^T$. Dimension n = 2. Starting Point: x_0=[1 1]^T.

(Functions provided: none-this function was studied in HW3)

Problem 10 Exponential_10:

$$f(x) = \frac{\exp(x_{[1]}) - 1}{\exp(x_{[1]}) + 1} + 0.1 \exp(-x_{[1]}) + \sum_{i=2}^{10} (x_{[i]} - 1)^4, \text{ where } x = [x_{[1]} \ x_{[2]} \ \cdots \ x_{[10]}]^T \in \mathbb{R}^{10}.$$

Dimension n = 10. Starting Point: $x_0 = [1 \ 0 \ \cdots \ 0]^T$.

(Functions provided: none-this function was studied in HW3)

Problem 11 Exponential_1000:

$$f(x) = \frac{\exp(x_{[1]}) - 1}{\exp(x_{[1]}) + 1} + 0.1 \exp(-x_{[1]}) + \sum_{i=2}^{100} (x_{[i]} - 1)^4, \text{ where } x = [x_{[1]} \ x_{[2]} \ \cdots \ x_{[100]}]^T \in \mathbb{R}^{100}.$$

Dimension n = 100. Starting Point: $x_0 = [1 \ 0 \ \cdots \ 0]^T$.

(Functions provided: none-this function was studied in HW3)

Problem 12 Genhumps_5:

$$f(x) = \sum_{i=1}^{4} \sin(2x_{[i]})^2 \sin(2x_{[i+1]})^2 + 0.05(x_{[i]}^2 + x_{[i+1]}^2), \text{ where } x = [x_{[1]} \ x_{[2]} \ \cdots \ x_{[5]}]^T \in \mathbb{R}^5.$$

Dimension n = 5. Starting Point: $x_0 = [-506.2 \ 506.2 \ \cdots \ 506.2]^T$.

(Functions provided: function, gradient, Hessian)