

Lab 4 Report

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Purpose

Visualize the process of solving the **Baguenaudier puzzle** with recursion algorithm of the lc3 assembly language.

Principles

1. In order to pretend from losing the corresponding return addresses amongst the recursion operations, a **stack** starting from x4000 is used to load the addresses. R5 is the stack pointer.

```

15  BAGUE_R
16  ✓ ; ***PUSH THE RETURN ADDRESS***
17      ADD R5, R5, #1
18      STR R7, R5, #0
19  ✓ ; ***R(i - 2)***
20      ADD R4, R0, #-2
21      BRnz SKIPI      ; if(n>2) B_R(n-2)
22      ADD R0, R0, #-2
23      JSR BAGUE_R
24      ADD R0, R0, #2
25  SKIPI
26  ✓ ; ***r(i)***
27      JSR REMOVE_ONE
28  ✓ ; ***P(i - 2)***
29      ADD R4, R0, #-2
30      BRnz SKIPII
31      ADD R0, R0, #-2
32      JSR BAGUE_P
33      ADD R0, R0, #2
34  SKIPII
35  ✓ ; ***R(i - 1)***
36      ADD R4, R0, #-1
37      BRnz SKIPIII
38      ADD R0, R0, #-1
39      JSR BAGUE_R
40      ADD R0, R0, #1
41  SKIPIII
42  ✓ ; ***POP THE RETURN ADDRESS***
43      LDR R7, R5, #0
44      ADD R5, R5, #-1
45      RET

```

2. In order to update the state of the baguenaudier, first locate the bit at the correct digit. If the operation is to remove the ring, then ADD the bit code to the current state code; if the operation is to put the ring, then NOT the bit code then AND it to the current state code.

3. In order to maintain the value of the number of the rings, at the both sides of the recursion instruction, which is the JSR instruction, subtract 1 or 2, which depends on the recursion function given inside the lab file, then add it back.

```

19  ✓ ; ***R(i - 2)***
20      ADD R4, R0, #-2
21      BRnz SKIPI      ; if(n>2) B_R(n-2)
22      ADD R0, R0, #-2
23      JSR BAGUE_R
24      ADD R0, R0, #2
25      SKIPI

```

4. According to the lab file, $P(i)$ is the inverse of $R(i)$. We can figure out that:

$R(0)$ = nothing to do; $R(1)$ = remove the 1st ring; $R(i) = R(i - 2) + \text{remove the } i\text{-th ring} + P(i - 2) + R(i - 2)$, $i \geq 2$;

$P(0)$ = nothing to do; $P(1)$ = put the 1st ring; **$P(i) = P(i - 1) + R(i - 2) + \text{put the } i\text{-th ring} + P(i - 2)$** , $i \geq 2$;

Procedure

1. Figure out the principle of how the recursion works in lc3 assembly language. Every time a JSR or a JSRR instruction is executed, the return address, i.e the PC incremented, is loaded into R7. The RET instruction at the end of the a sub-function will steer the program back to the correct address.
2. Encode a C language version to help figure out how the program goes.

Result

example 1

- $n = 3$

output

Memory				
!	▶	x3100	x0003	3
!	▶	x3101	x0001	1
!	▶	x3102	x0005	5
!	▶	x3103	x0004	4
!	▶	x3104	x0006	6
!	▶	x3105	x0007	7
!	▶	x3106	x0000	0
!	▶	x3107	x0000	0

example 2

- n = 12

output

memory				
!	▶	x3100	x000C	12
!	▶	x3101	x0002	2
!	▶	x3102	x0003	3
!	▶	x3103	x000B	11
!	▶	x3104	x000A	10
!	▶	x3105	x0008	8
!	▶	x3106	x0009	9
!	▶	x3107	x000D	13
!	▶	x3108	x000C	12
!	▶	x3109	x000E	14
!	▶	x310A	x000F	15
!	▶	x310B	x002F	47
!	▶	x310C	x002E	46
!	▶	x310D	x002C	44
!	▶	x310E	x002D	45
!	▶	x310F	x0029	41
!	▶	x3110	x0028	40
!	▶	x3111	x002A	42
!	▶	x3112	x002B	43
!	▶	x3113	x0023	35
!	▶	x3114	x0022	34
!	▶	x3115	x0020	32
!	▶	x3116	x0021	33

- over 2000 items **omitted**

Memory				
!	▶	x3B9A	x0FE7	4071
!	▶	x3B9B	x0FF7	4087
!	▶	x3B9C	x0FF6	4086
!	▶	x3B9D	x0FF4	4084
!	▶	x3B9E	x0FF5	4085
!	▶	x3B9F	x0FF1	4081
!	▶	x3BA0	x0FF0	4080
!	▶	x3BA1	x0FF2	4082
!	▶	x3BA2	x0FF3	4083
!	▶	x3BA3	x0FFB	4091
!	▶	x3BA4	x0FFA	4090
!	▶	x3BA5	x0FF8	4088
!	▶	x3BA6	x0FF9	4089
!	▶	x3BA7	x0FFD	4093
!	▶	x3BA8	x0FFC	4092
!	▶	x3BA9	x0FFE	4094
!	▶	x3BAA	x0FFF	4095
!	▶	x3BAB	x0000	0
!	▶	x3BAC	x0000	0
!	▶	x3BAD	x0000	0
!	▶	x3BAE	x0000	0