

Движение тела, брошенного под углом к горизонту с учётом сопротивления воздуха



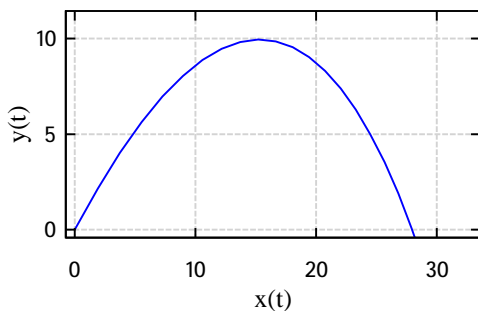
$k := 0.2 \quad \alpha := 50^\circ \quad steps := 20$

$v_0 := 20 \quad m := 1 \quad g := 9.8 \quad appVersion(3) = "1.2.9018"$

Вариант 1

$$D(t, u) := \text{stack} \left(u_3, u_4, -k \cdot \frac{u_3^2}{m}, -g - k \cdot \frac{u_4^2}{m} \right)$$

$$u_0 := \text{stack} \left(0, 0, v_0 \cdot \cos(\alpha), v_0 \cdot \sin(\alpha) \right)$$

$$u := \text{rkfixed}(u_0, 0, 3, steps, D)$$


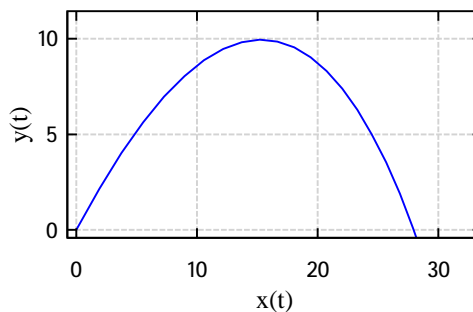
$\text{rkfixed}(" ? ") = \begin{array}{l} \text{"rkfixed(cmd)} \\ \text{rkfixed(ode, y(x), xmax)} \\ \text{rkfixed(ode, y(x), xmax, steps)} \\ \text{rkfixed(ics, xmin, xmax, steps, D(x, y))} \end{array}$

$u \left[1..rows(u) \right] \left[\begin{array}{c} 2 \\ 3 \end{array} \right]$

Вариант 2

$\text{Clear}(t, u, x(t), y(t), vx(t), vy(t)) = 1$

$t := \text{col}(u, 1)$

$$\left\{ \begin{array}{l} x(0) = 0 \quad y(0) = 0 \\ vx(0) = v_0 \cdot \cos(\alpha) \\ vy(0) = v_0 \cdot \sin(\alpha) \\ x'(t) = vx(t) \\ y'(t) = vy(t) \\ vx'(t) = -k \cdot \frac{vx(t)^2}{m} \\ vy'(t) = -g - k \cdot \frac{vy(t)^2}{m} \end{array} \right.$$


$\begin{bmatrix} x(t) \\ y(t) \end{bmatrix}$

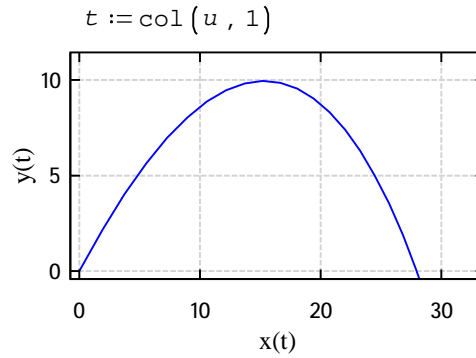
$u := \text{rkfixed} \left(\begin{bmatrix} x(t) \\ y(t) \\ vx(t) \\ vy(t) \end{bmatrix}, 3, steps \right)$

$\text{var2str} \left(\begin{bmatrix} x(t) \\ y(t) \end{bmatrix} \right) = \text{"mat(x(~t), y(~t), 2, 1)"}$

Вариант 3 `Clear(t, u, x(t), y(t), vx(t), vy(t)) = 1`

$$\left\{ \begin{array}{l} x(0) = 0 \quad y(0) = 0 \\ x'(0) = v_0 \cdot \cos(\alpha) \\ y'(0) = v_0 \cdot \sin(\alpha) \\ x''(t) = -k \cdot \frac{x'(t)}{m} \\ y''(t) = -g - k \cdot \frac{y'(t)}{m} \end{array} \right.$$

$$u := \text{rkfixed} \left(\left\{ \begin{array}{l} x(t) \\ y(t) \end{array} \right\}, 3, \text{steps} \right)$$



$$\begin{bmatrix} x(t) \\ y(t) \end{bmatrix}$$

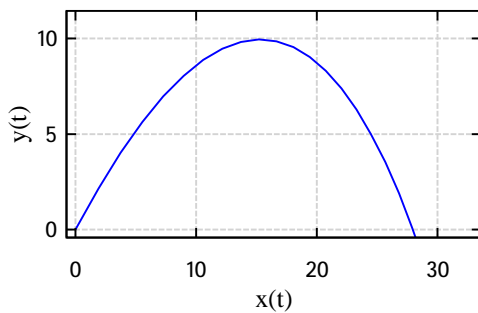
`var2str(⎣⎡ x(t) ⎤⎦) = "mat(x(~t), y(~t), 2, 1)"`

Вариант 4 `Clear(t, u, x(t), y(t), vx(t), vy(t)) = 1`

$$\text{ode} := \left\{ \begin{array}{l} x(0) = 0 \\ y(0) = 0 \\ x'(0) = v_0 \cdot \cos(\alpha) \\ y'(0) = v_0 \cdot \sin(\alpha) \\ x''(t) = -\frac{k \cdot x'(t)}{m} \\ y''(t) = -\frac{g \cdot m + k \cdot y'(t)}{m} \end{array} \right.$$

$$u := \text{rkfixed} \left(\text{ode}, \left\{ \begin{array}{l} x(t) \\ y(t) \end{array} \right\}, 3, \text{steps} \right)$$

$$t := \text{col}(u, 1)$$



$$\begin{bmatrix} x(t) \\ y(t) \end{bmatrix}$$

`var2str(⎣⎡ x(t) ⎤⎦) = "mat(x(~t), y(~t), 2, 1)"`