

Jaypee University of Engineering & Technology, Guna

T-1 (Even Semester 2022)

18B11MA211 – Discrete Mathematics

Maximum duration: 1 Hour

Maximum Marks: 15

Notes:

1. This question paper has four questions.
2. Write relevant answers only.
3. Do not write anything on question paper (Except your Er. No.).

Marks

[4]

Q1. (a) Using Mathematical Induction, show that for a positive integer n ; $11^{n+1} + 12^{2n-1}$ is always divisible by 133.

(b) Let A, B and C be the sets.
Prove analytically and graphically that $(B - A) \cup (C - A) = (B \cup C) - A$.

Q2. (a) Draw diagram for relation R on $A = \{1, 2, 3, 4, 5, 6, 7, 8\}$, where xRy if y is divisible by x . [4]

(b) Let $A = \{1, 2, 3, \dots, 9\}$ and let R be the relation on $A \times A$ defined by:
 $(a, b) R(c, d)$ if $a + d = b + c$
(i) Prove that R is an equivalence relation.
(ii) Find $[(2, 5)]$, i.e. the equivalence class of $(2, 5)$.

Q3. (a) A person deposits Rs1000 in an account that yields 9% interest compounded annually. [4]
(i) Set up a recurrence relation for the amount in the account at the end of n years.
(ii) Find an explicit formula for the amount in the account at the end of n years.
(iii) How much money will the account contain after 100 years?

(b) Write the domain of the following function: $f(x) = \sqrt{81 - x^2}$.

Q4. Construct the truth table of the following: [3]
 $[\sim p \wedge (\sim q \wedge r)] \vee (q \wedge r) \vee (p \wedge r)$

Write the dual of the following identity:

$$A \cup B = (A \cap B') \cup (A' \cap B) \cup (A \cap B)$$