

Course Reminders

- Guest Lecture Thursday
- A3 due Friday (11:59 PM)
- Project Proposal [Feedback](#) Available
 - Median: 8.8/10; Mean: 8.5/10
 - Regrades: Piazza *proposal-regrade*; all handled by Prof Ellis
- Updates:
 - Piazza - separate folders for each assignment (i.e. A3 = *a3* folder/tag)
 - Sam's OH: Fri 11 AM-12 PM

Project Proposal: General Themes (cont'd)

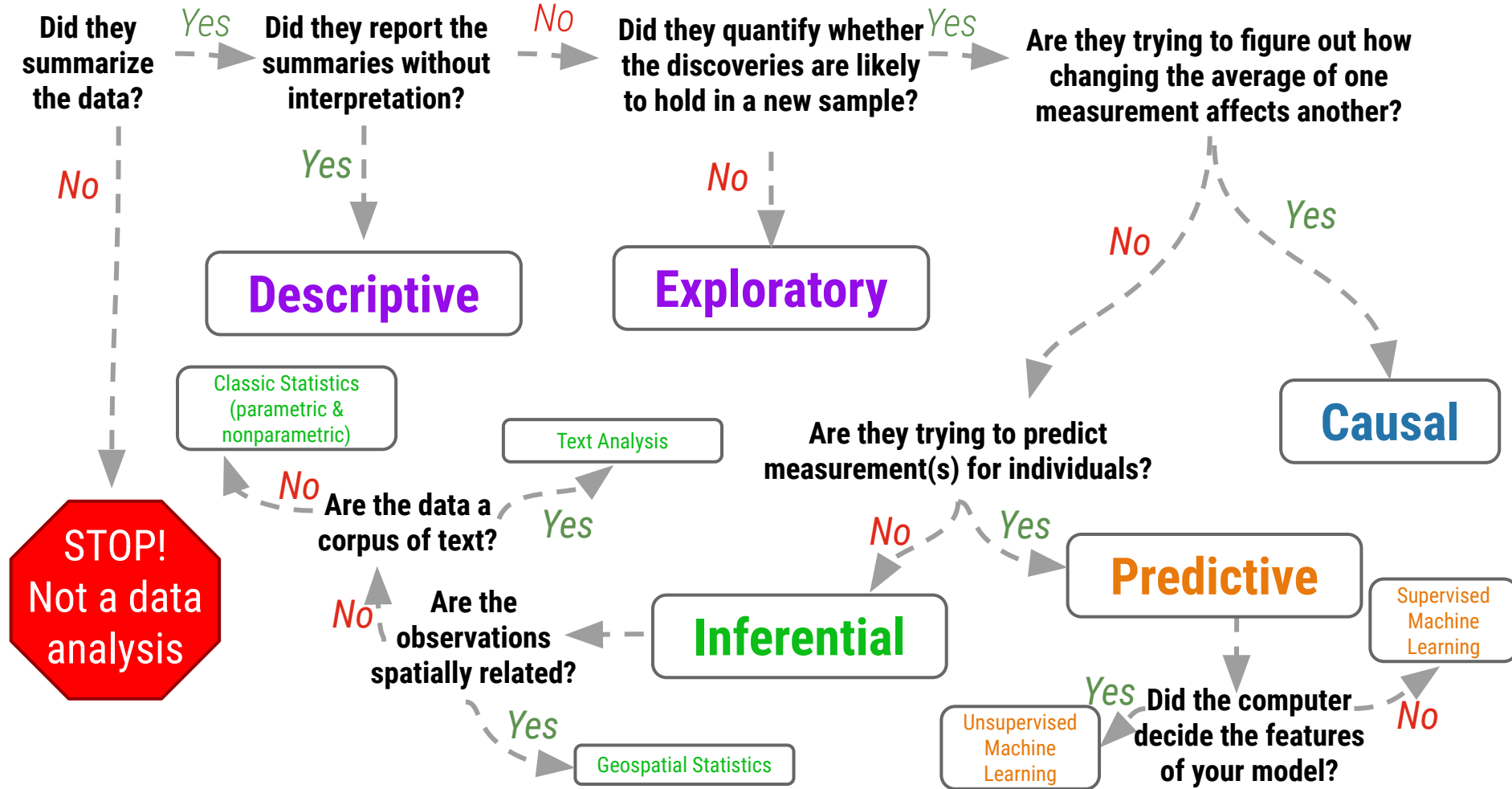
- Overall:
 - Excellent proposal but research question seems overly simple — you could feasibly answer your question with a single correlation table. How will your project go beyond this?
- Data:
 - For each dataset chosen, the proposal should describe the observations (what each row means). This proposal only describes the variables for each dataset. The proposal is also missing the number of observations within each dataset needed for this analysis.
 - It's unclear how {extra_columns} are related to your research question and hypotheses.
- Background:
 - Missing introduction to topic
 - Missing why this question is of interest to your group
 - Missing how the sources cited lead to the hypotheses of this proposal.
- Ethics:
 - How might potential sources of bias affect the analysis?

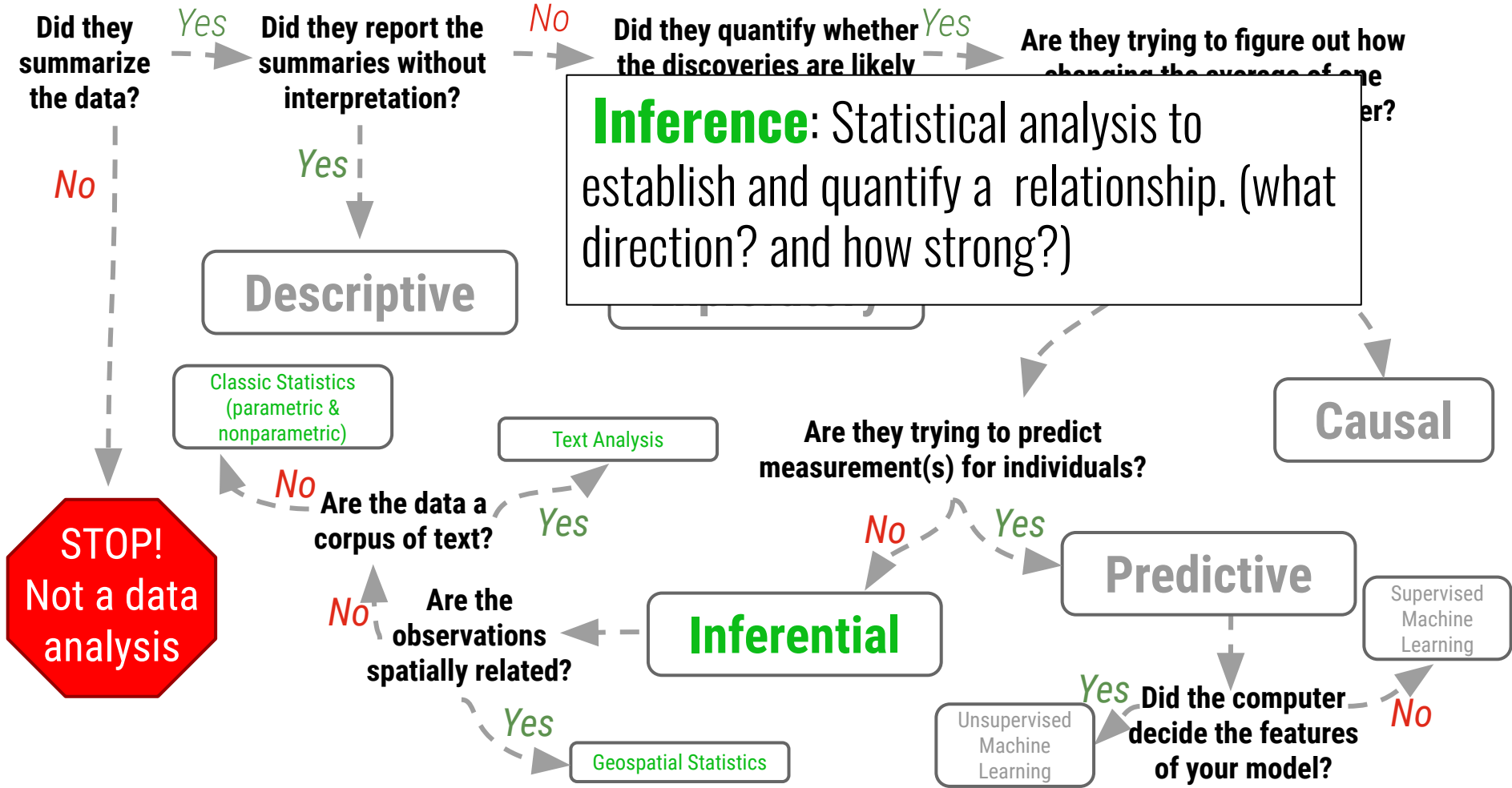
Inferential Analysis

Shannon E. Ellis, Ph.D
UC San Diego



Department of Cognitive Science
sellis@ucsd.edu





- **Problem:** Does Sesame Street affect kids brain development?
- **Data science question:** What is the relationship between watching Sesame Street and test scores among children?
- **Type of analysis:** Inferential analysis



Sesame Street
viewership

??

Test scores

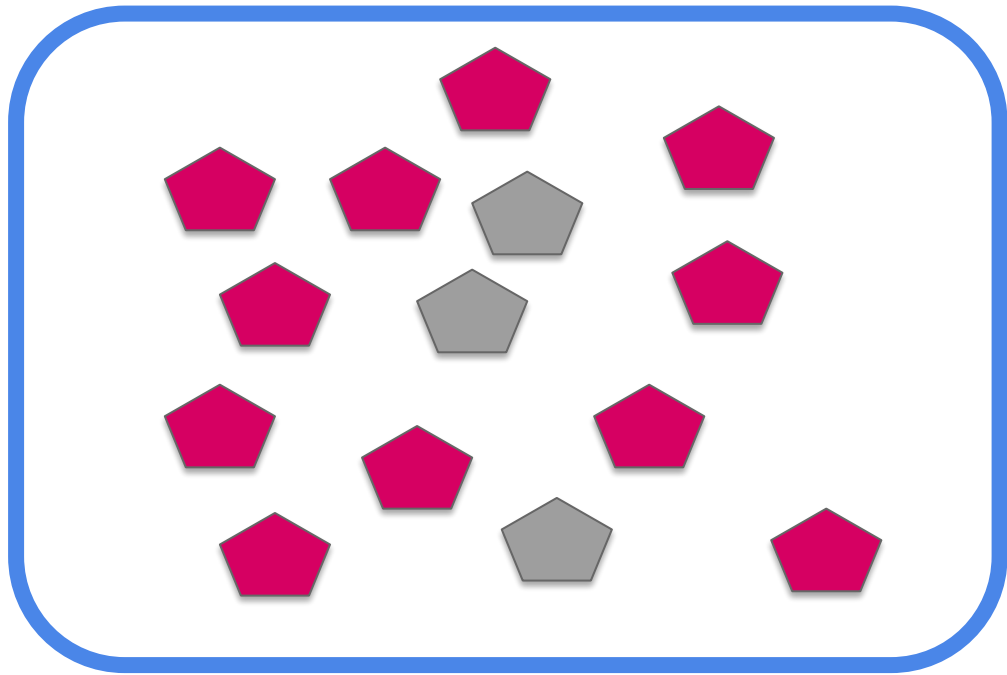
Establishing & Stating Your Null and Alternative Hypotheses Helps Guide Your Analysis

Null Hypothesis:

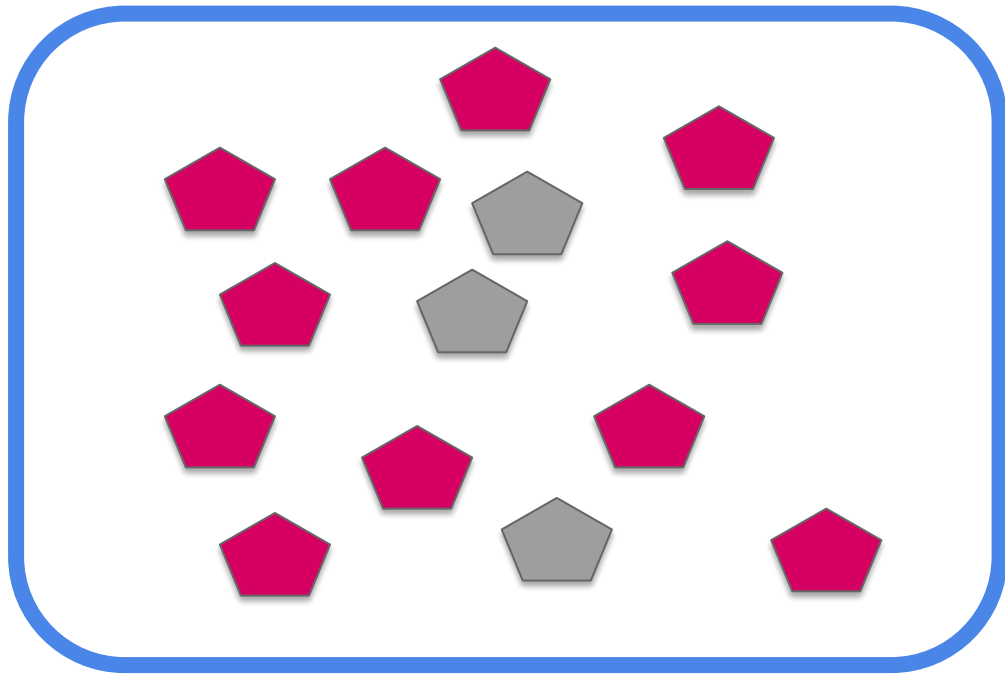
H_0 : Sesame Street has *no effect* on kids brain development

Alternative Hypothesis:

H_a : Watching Sesame Street *has an effect* on kids' brain development



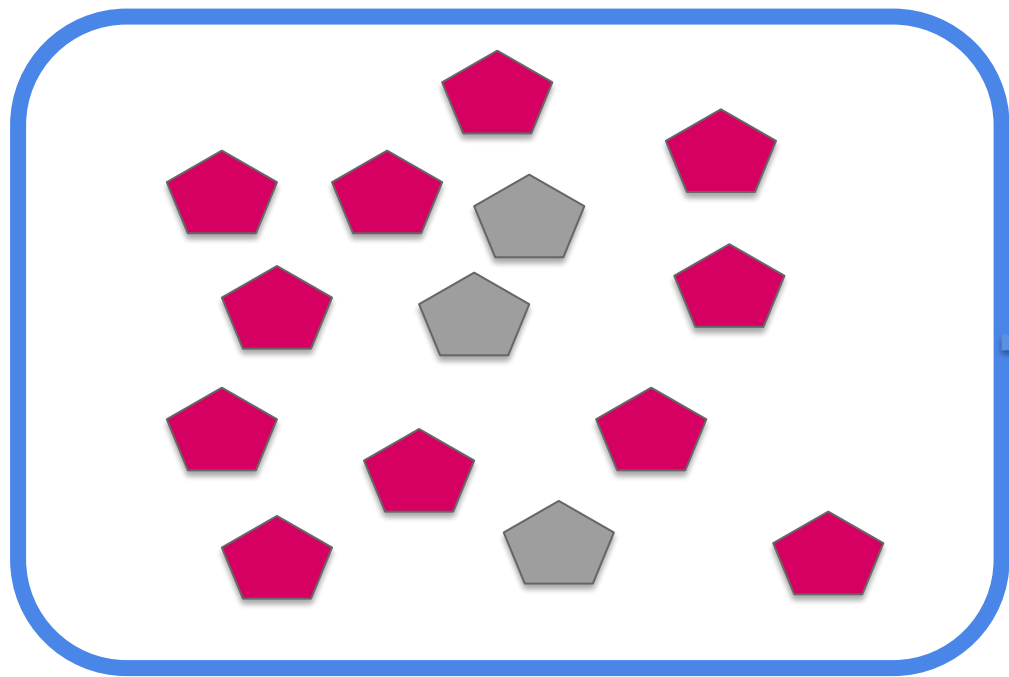
Population



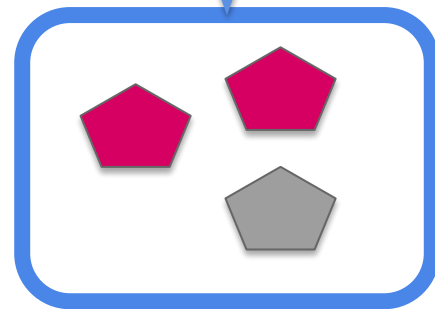
Population



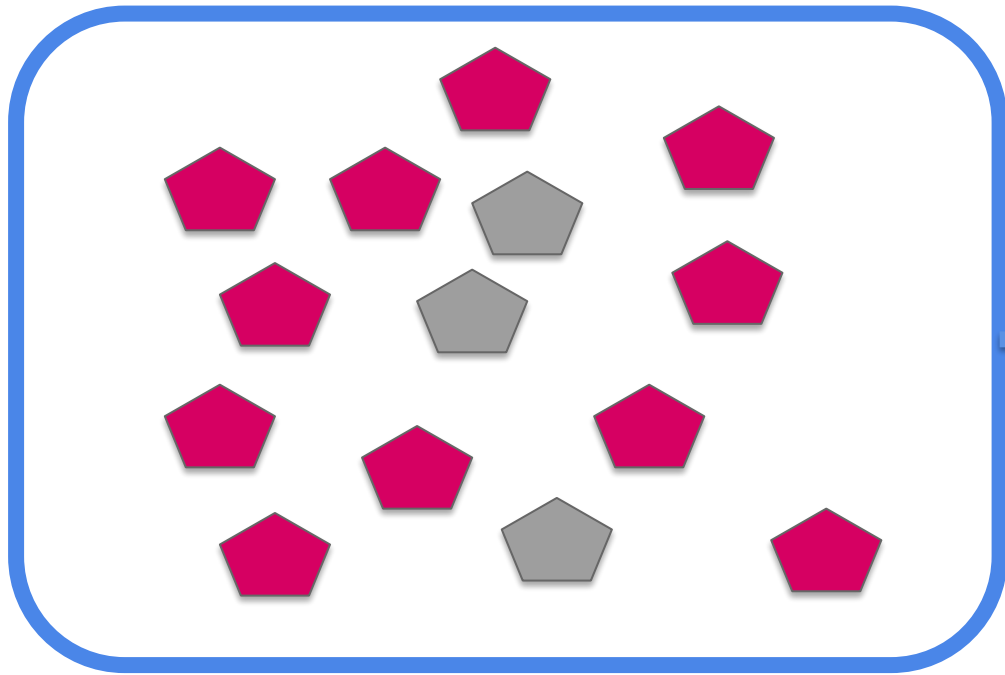
In our Sesame street
example, the population
would be all children



Population



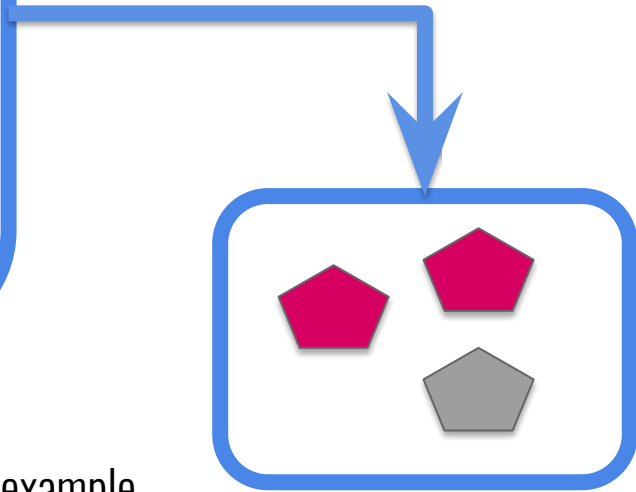
Sample



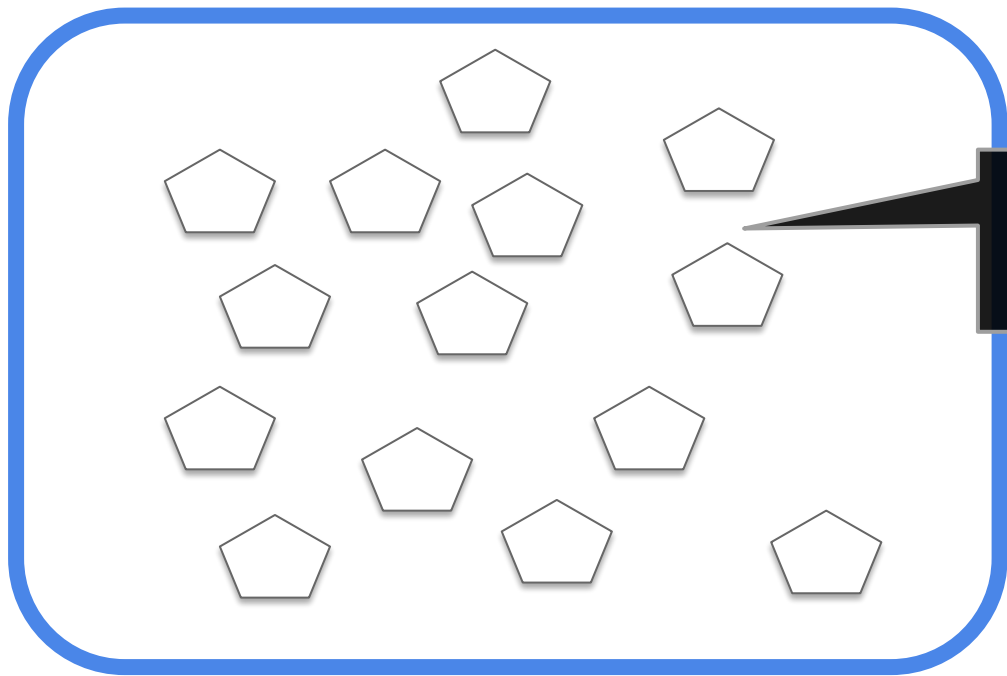
Population



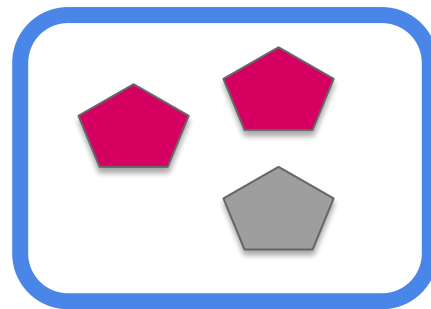
In our Sesame street example,
the sample would be the
children included in the study



Sample



Population

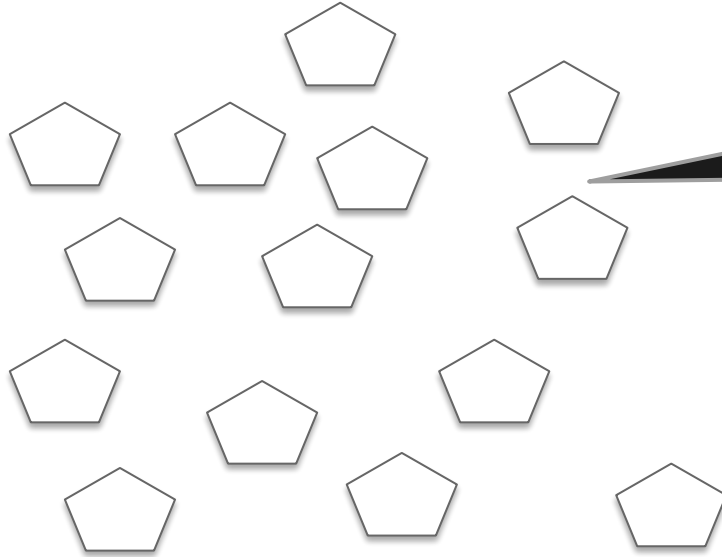


Sample

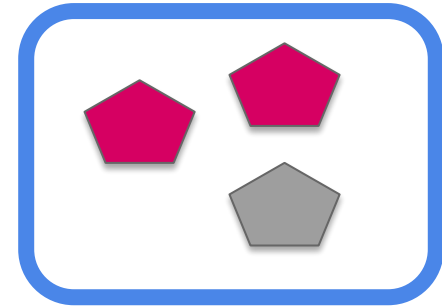


We don't know how much
Sesame street was watched by
or the tests scores of all kids

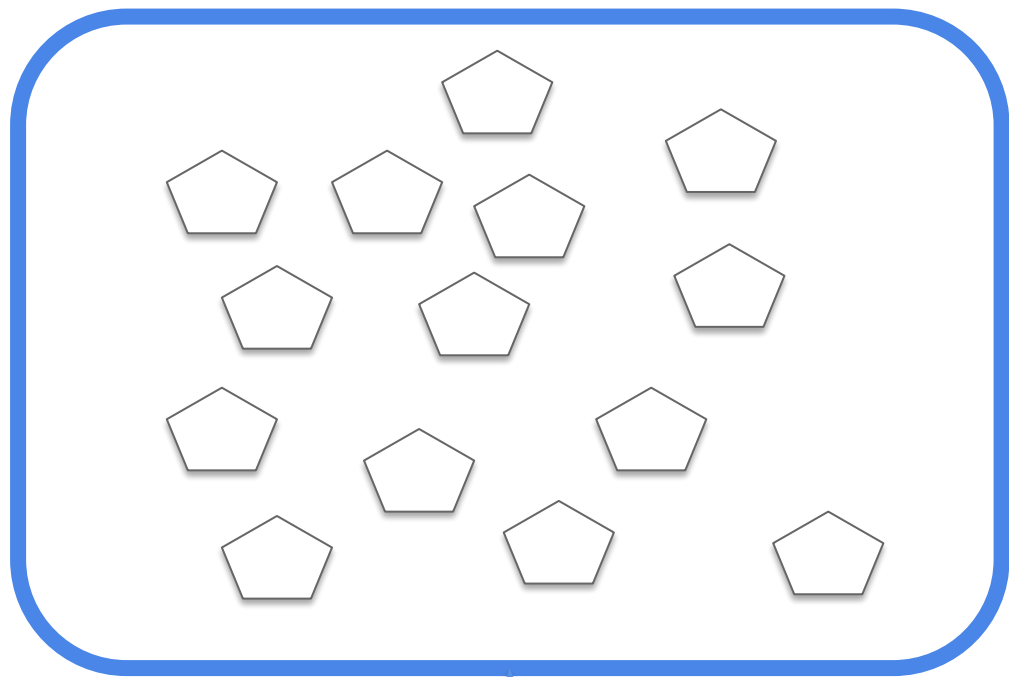
— _ (ツ) _ / —



Population



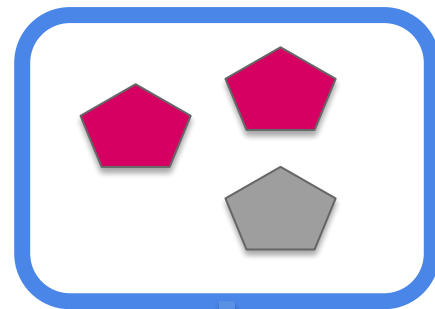
Sample



Population

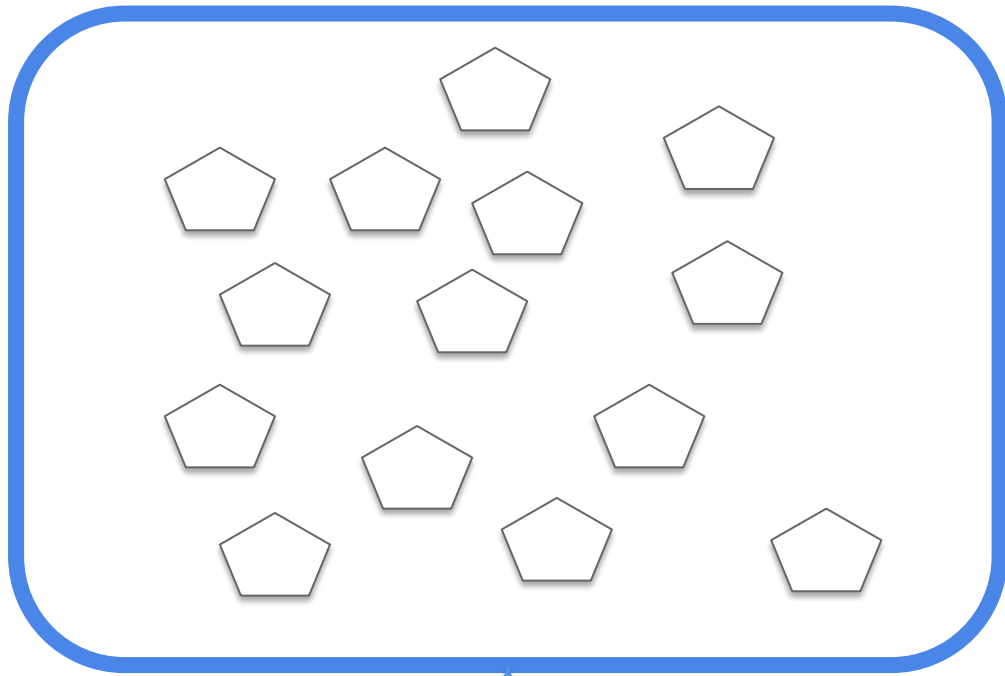


Inference!



Sample

Based on the relationship we see in our sample, we can infer the answer to our question in our population



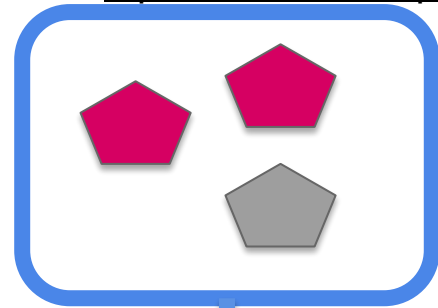
Population



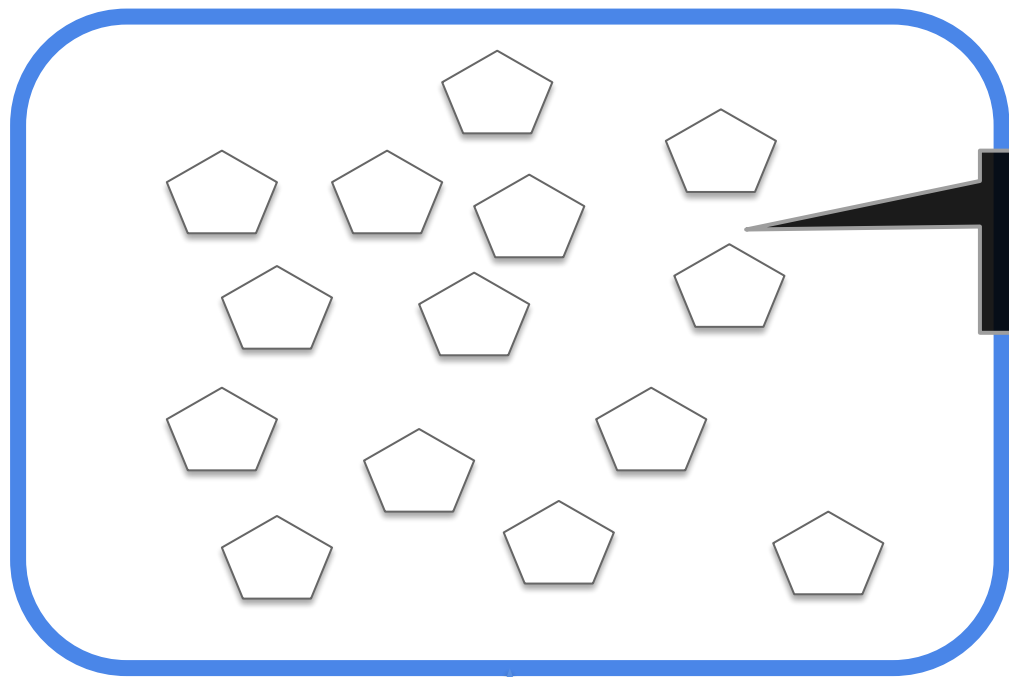
Inference!



So we look at Sesame street
viewing and test scores in a
representative sample of kids



Sample

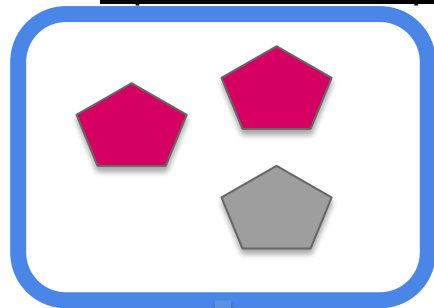


Population

Best guess

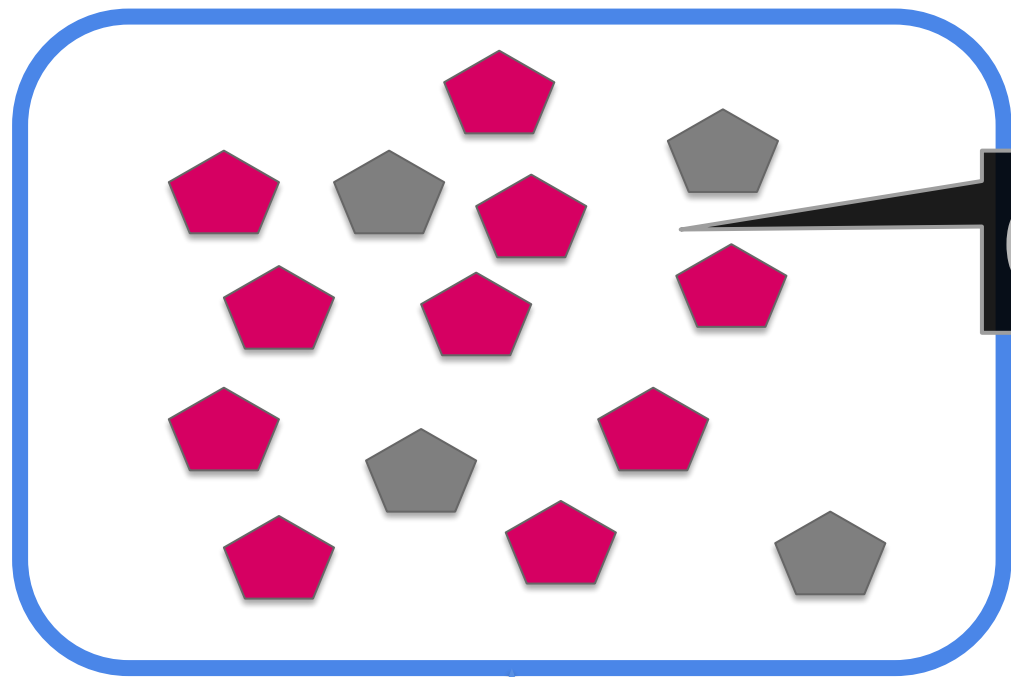


So we look at Sesame street viewing and test scores in a representative sample of kids



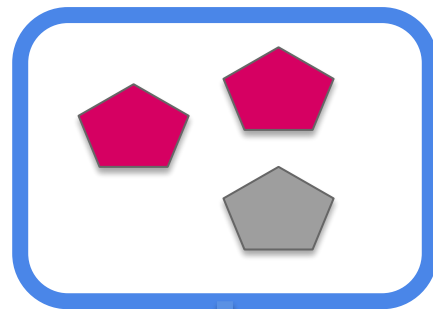
Sample

Inference!



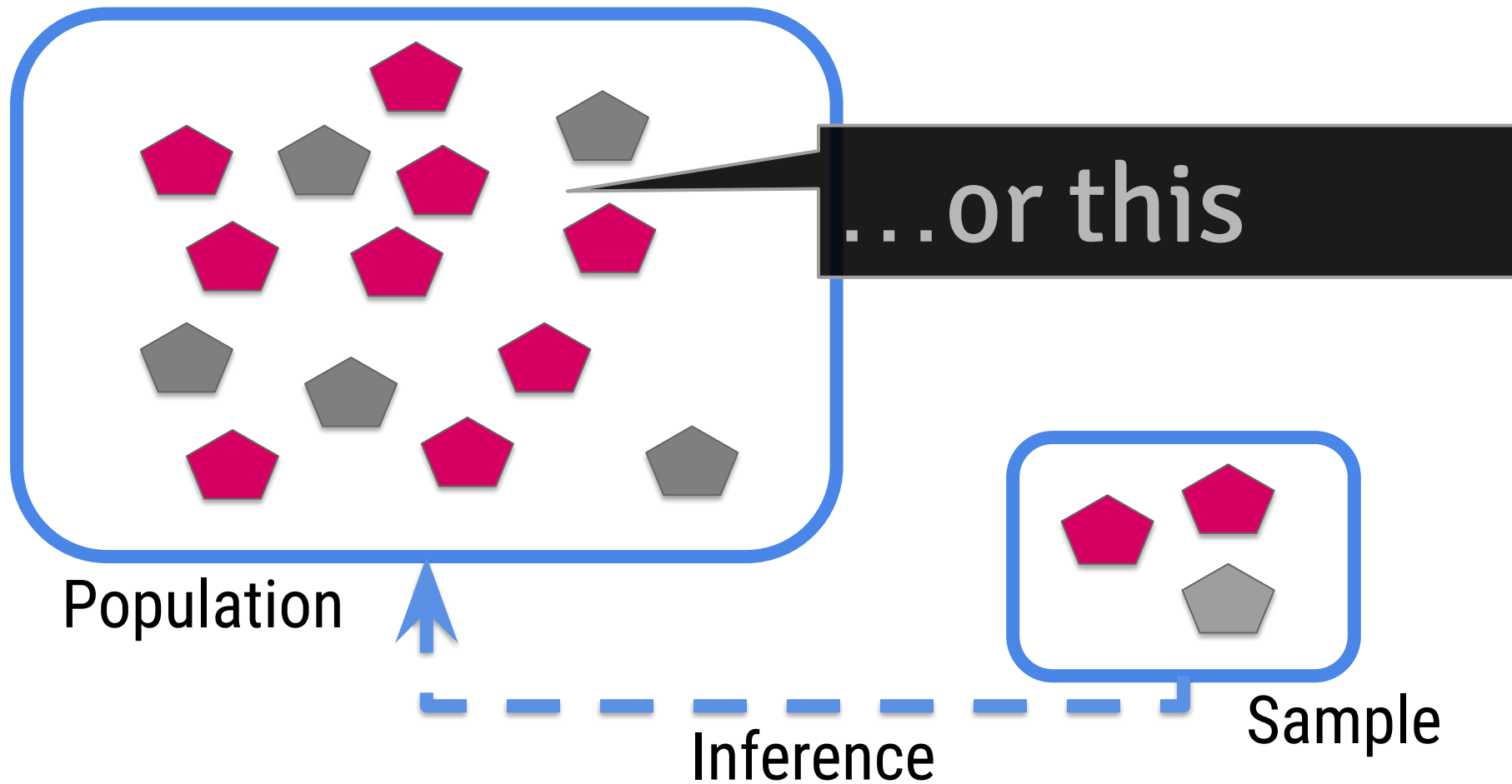
Population

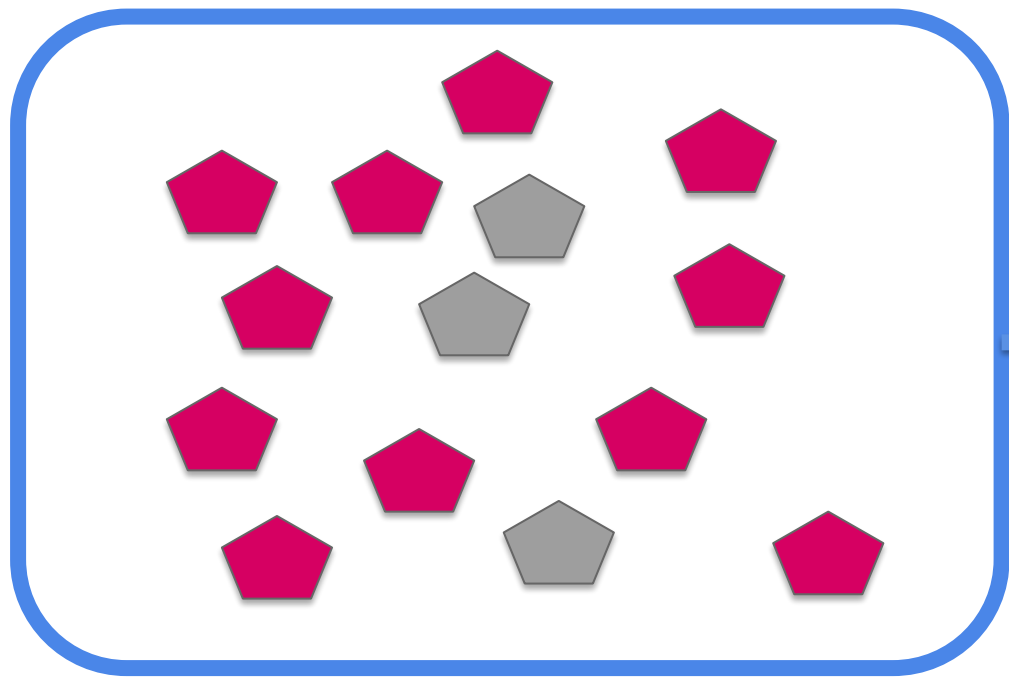
Could be this



Sample

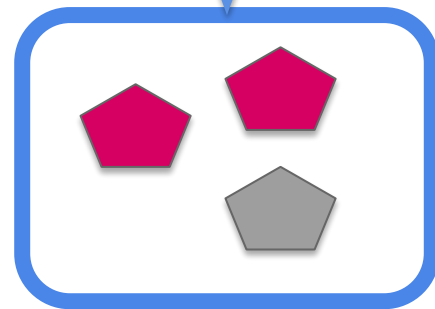
Inference



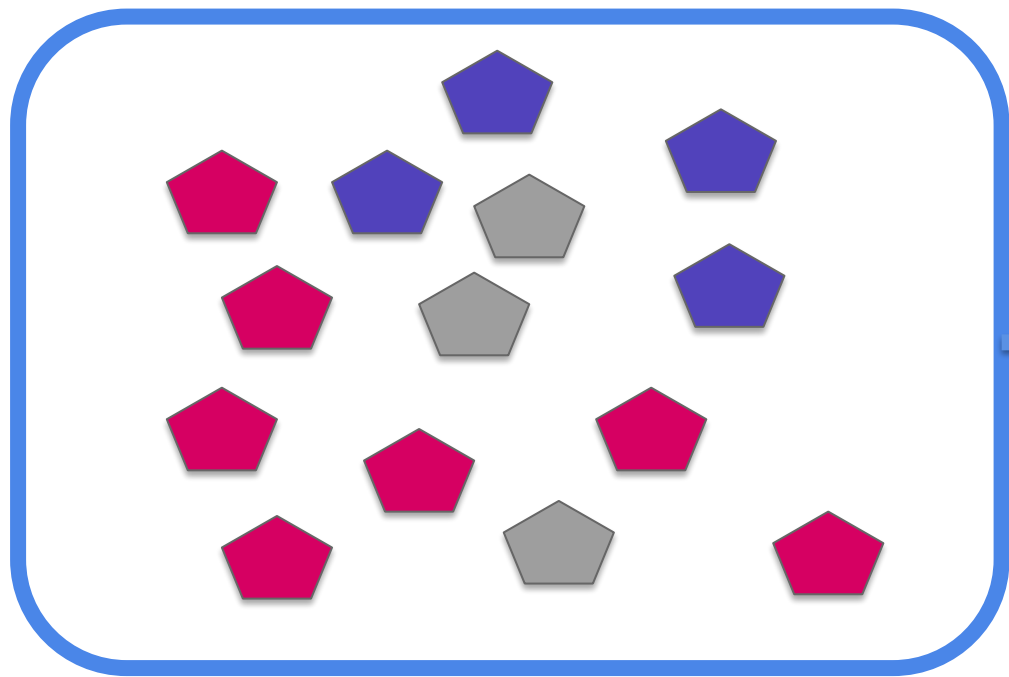


Population

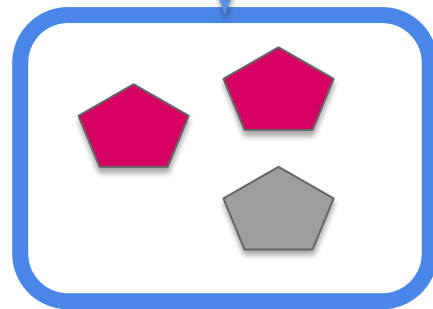
Probability



Sample

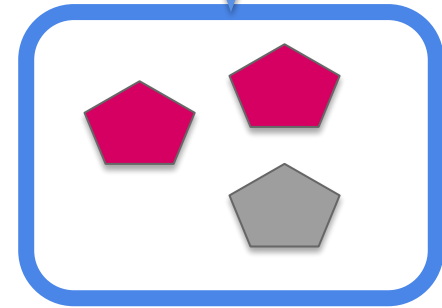
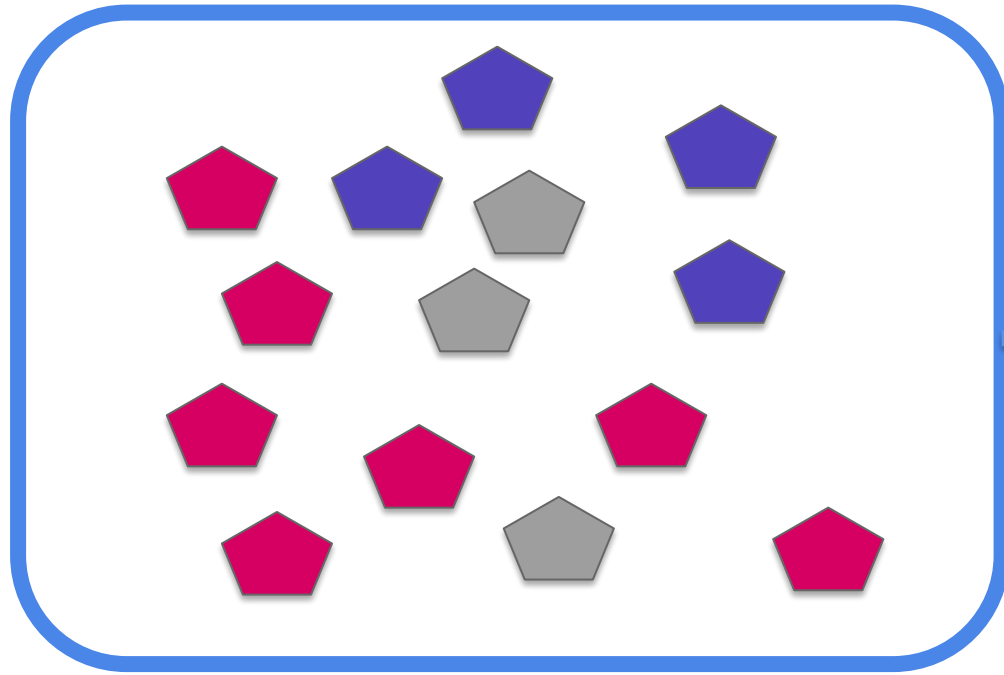


Population



Sample

If your sample is *not* representative of your population, you can not do inferential analysis.



Population

Inference

Sample

Approaches to Inference

CORRELATION

ASSOCIATION BETWEEN VARIABLES

i.e. Pearson Correlation,
Spearman Correlation,
chi-square test

COMPARISON OF MEANS

DIFFERENCE IN MEANS BETWEEN VARIABLES

i.e. t-test, ANOVA

REGRESSION

DOES CHANGE IN ONE VARIABLE MEAN CHANGE IN ANOTHER?

i.e. simple regression,
multiple regression

NON-PARAMETRIC TESTS

FOR WHEN ASSUMPTIONS IN THESE OTHER 3 CATEGORIES ARE NOT MET

i.e. Wilcoxon rank-sum
test, Wilcoxon sign-rank
test, sign test

CORRELATION

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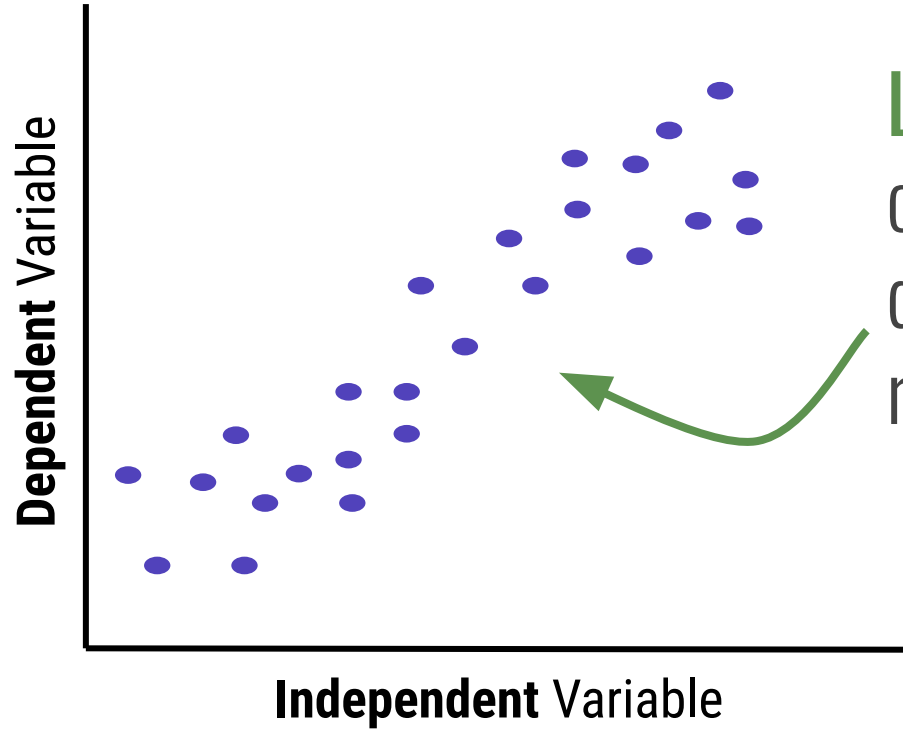
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i.e. simple regression,
multiple regression

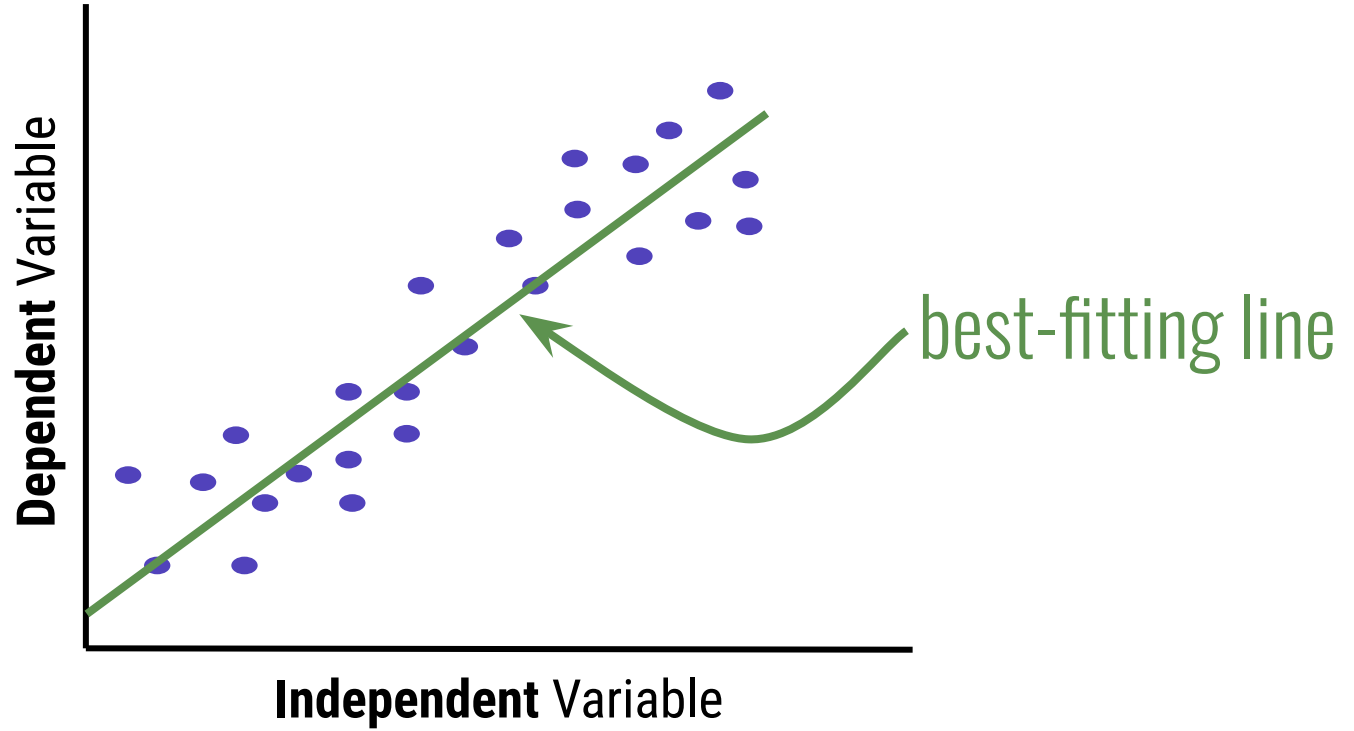
NON-PARAMETRIC TESTS

FOR WHEN ASSUMPTIONS IN THESE OTHER 3 CATEGORIES ARE NOT MET

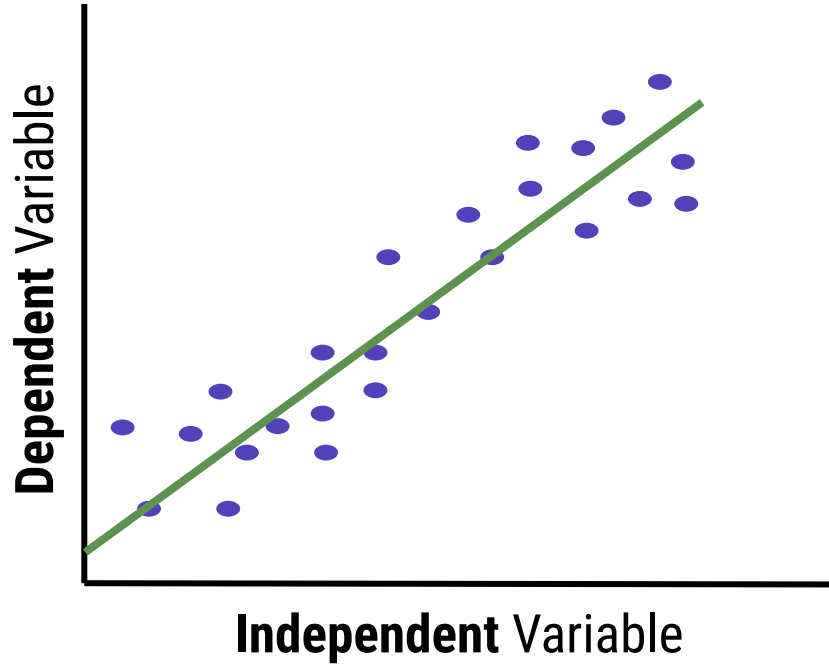
i.e. Wilcoxon rank-sum
test, Wilcoxon sign-rank
test, sign test



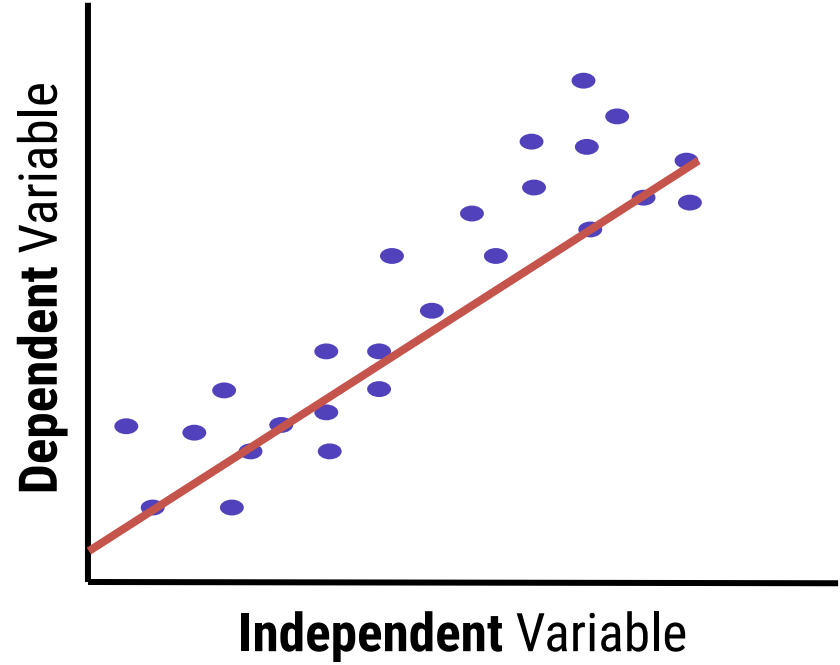
Linear regression
can be used to
describe this
relationship

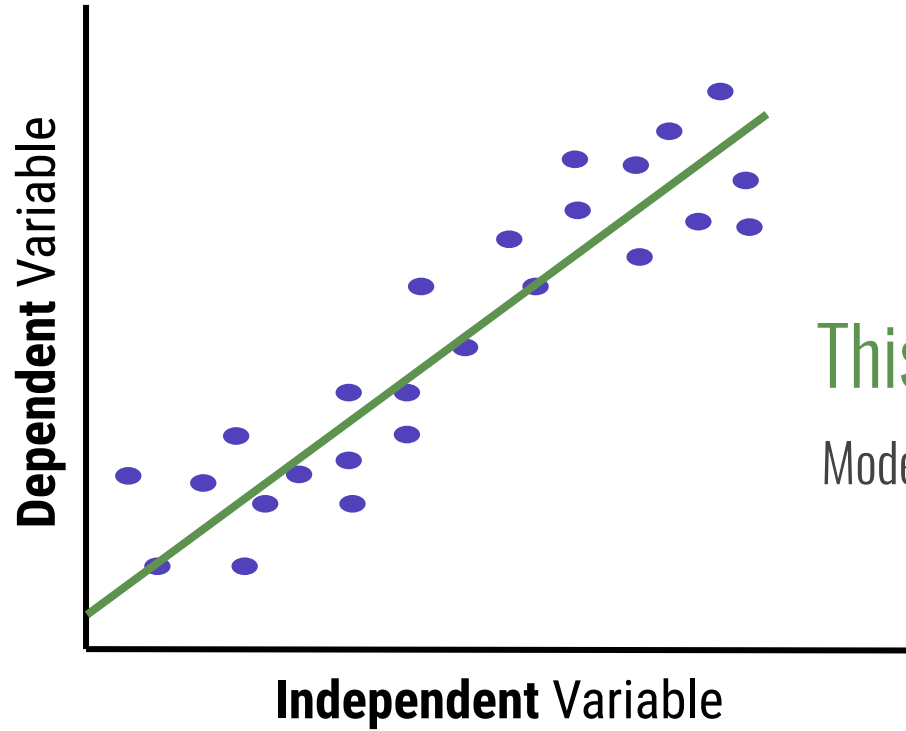


Best-fitting line



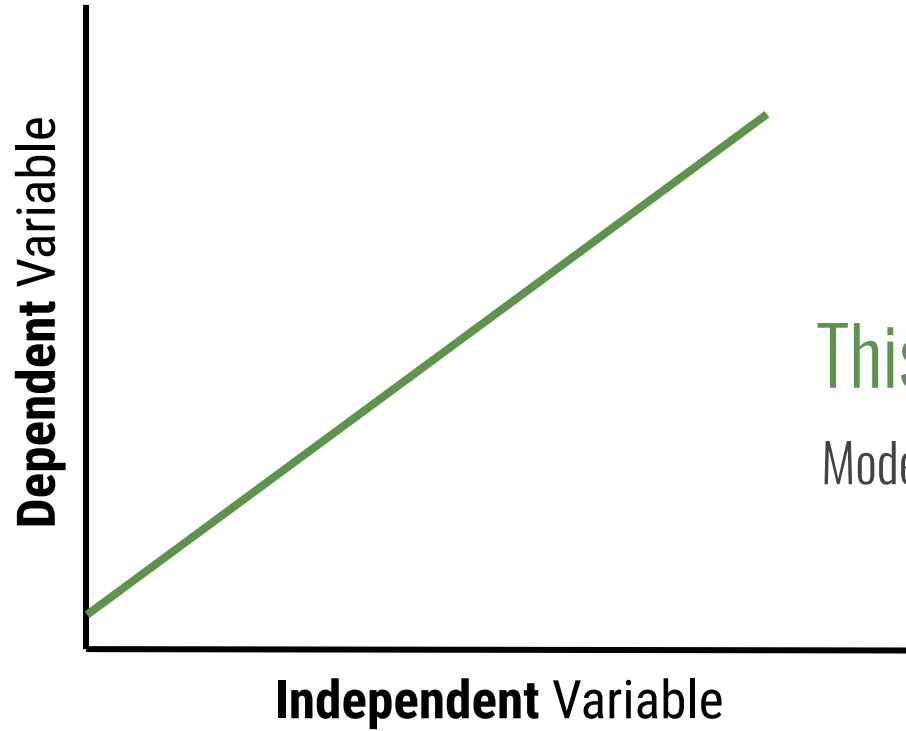
NOT a best-fitting line





This line is a **model** of the data

Models are mathematical equations generated to *represent* the real life situation

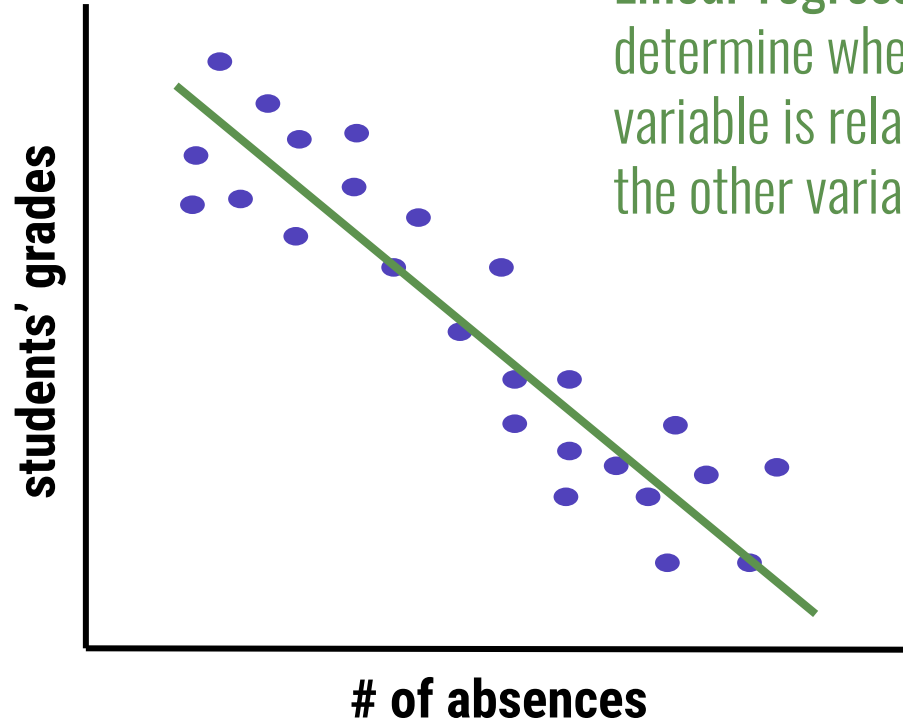


This line is a **model** of the data

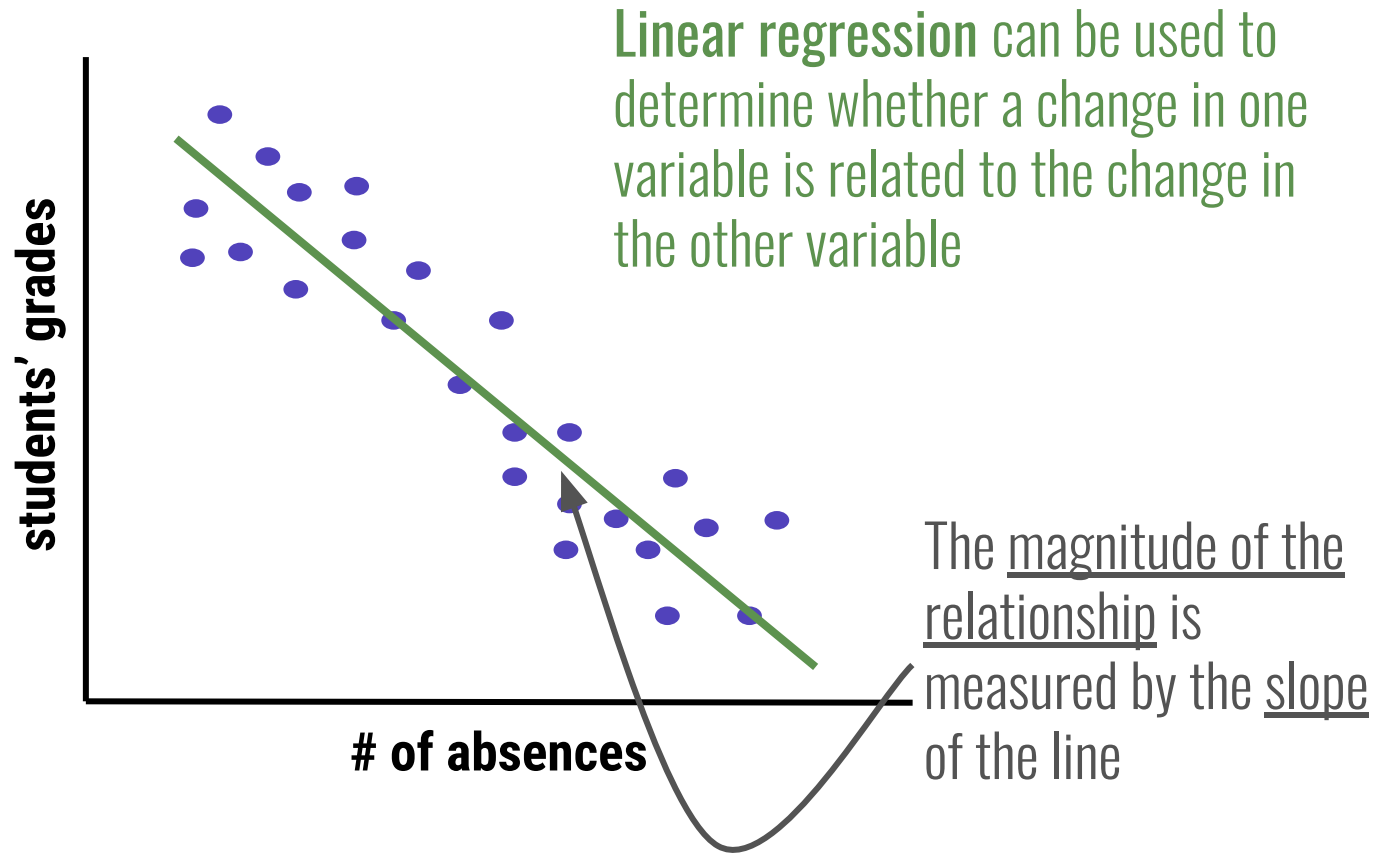
Models are mathematical equations generated to *represent* the real life situation

“All models are wrong, but some are useful”

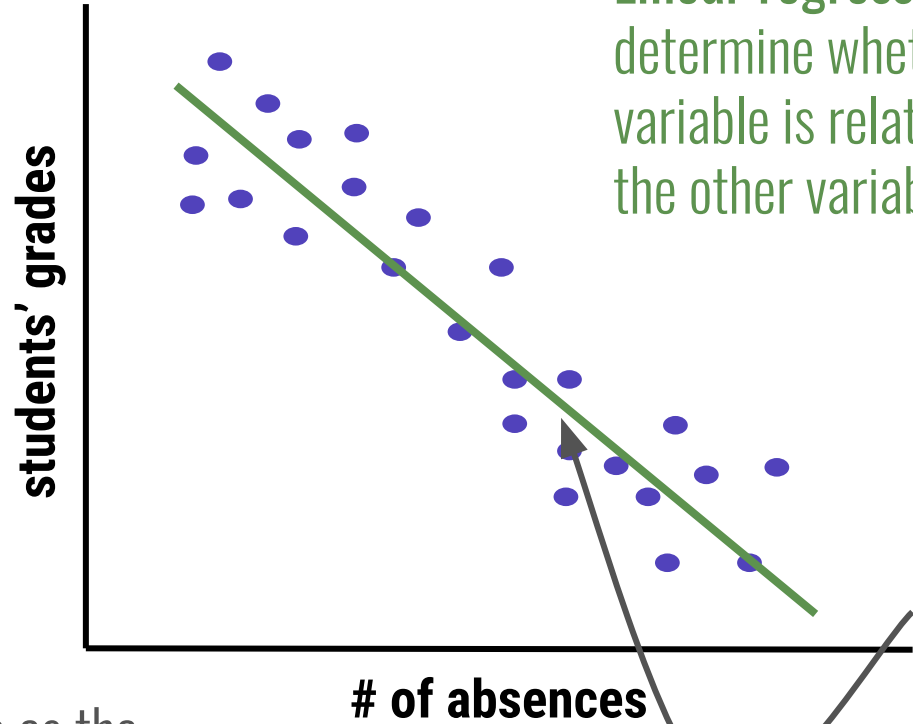
-George Box (British Statistician, *JASA* 1976)



Linear regression can be used to determine whether a change in one variable is related to the change in the other variable



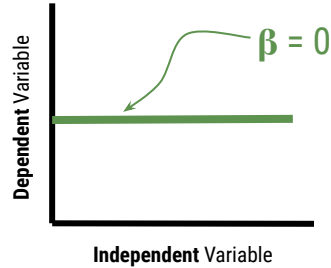
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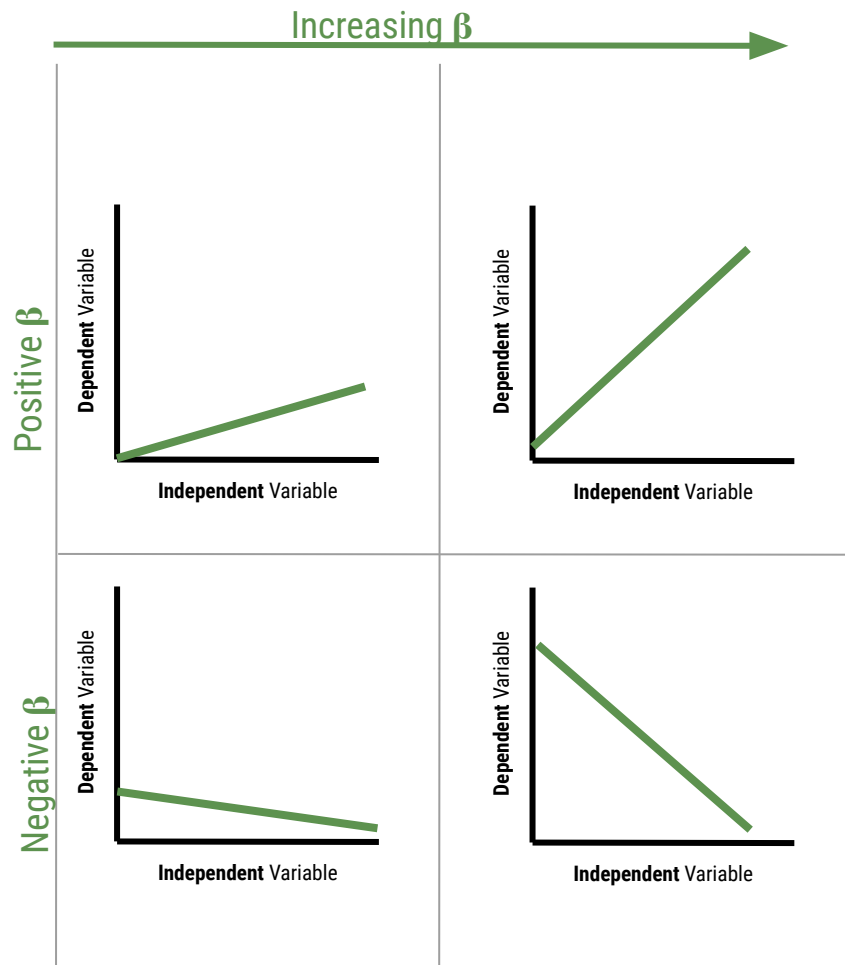
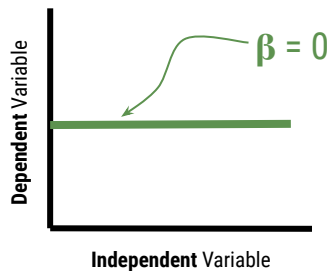
The magnitude of the relationship is measured by the slope of the line

This is also referred to as the model's effect size (β)

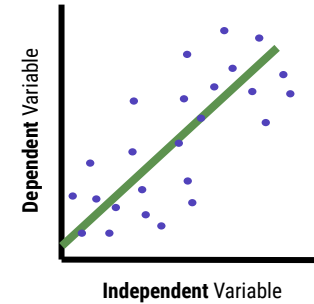
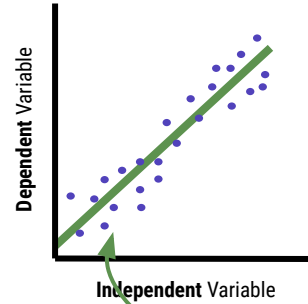
Effect size (β) can be estimated using the slope of the line



Effect size (β) can be estimated using the slope of the line



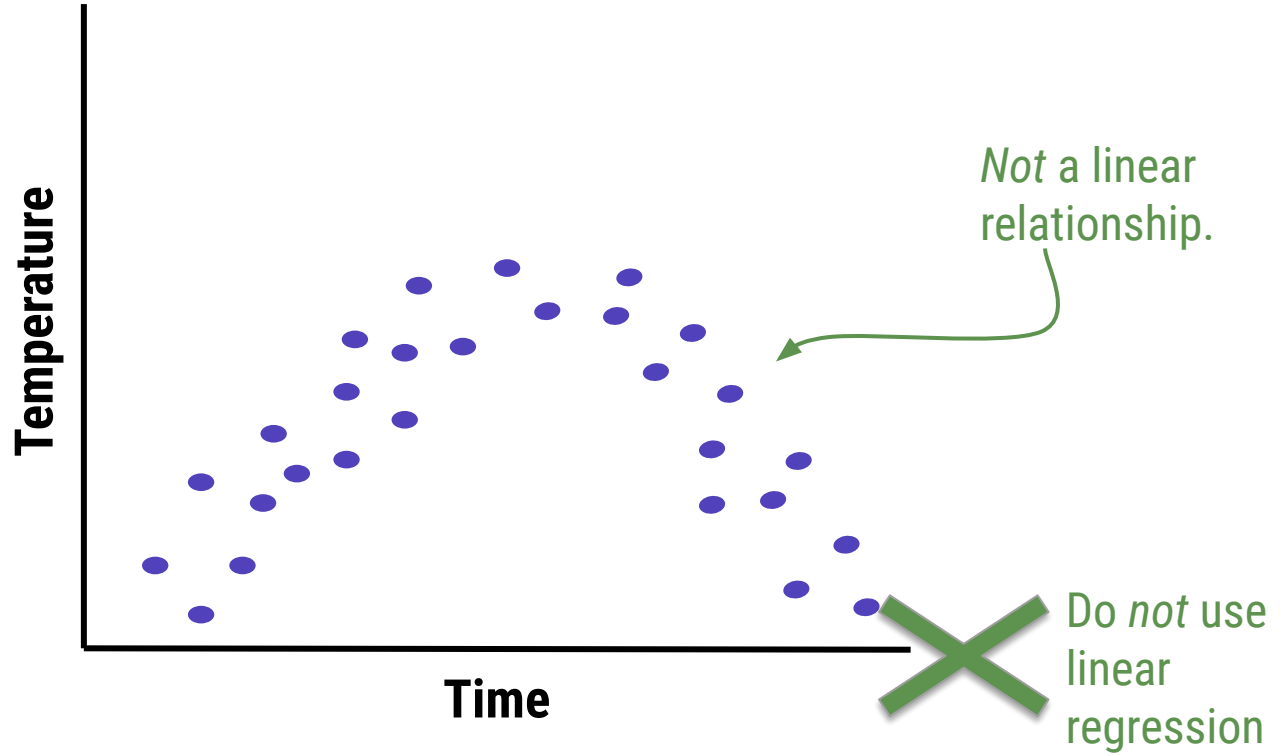
increasing standard error (SE) →



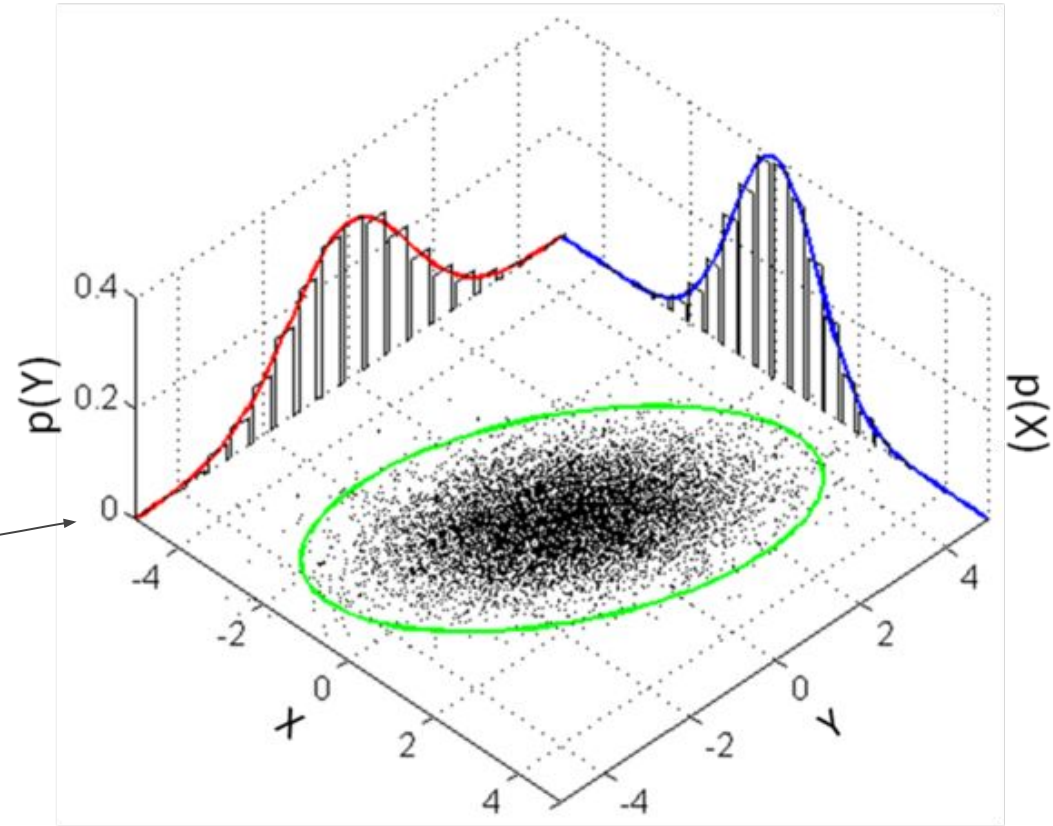
The *closer* the points
are to the regression
line, the *less uncertain*
we are in our estimate

Assumptions of linear regression

1. Linear relationship
2. Multivariate normality
3. No multicollinearity
4. No auto-correlation
5. Homoscedasticity



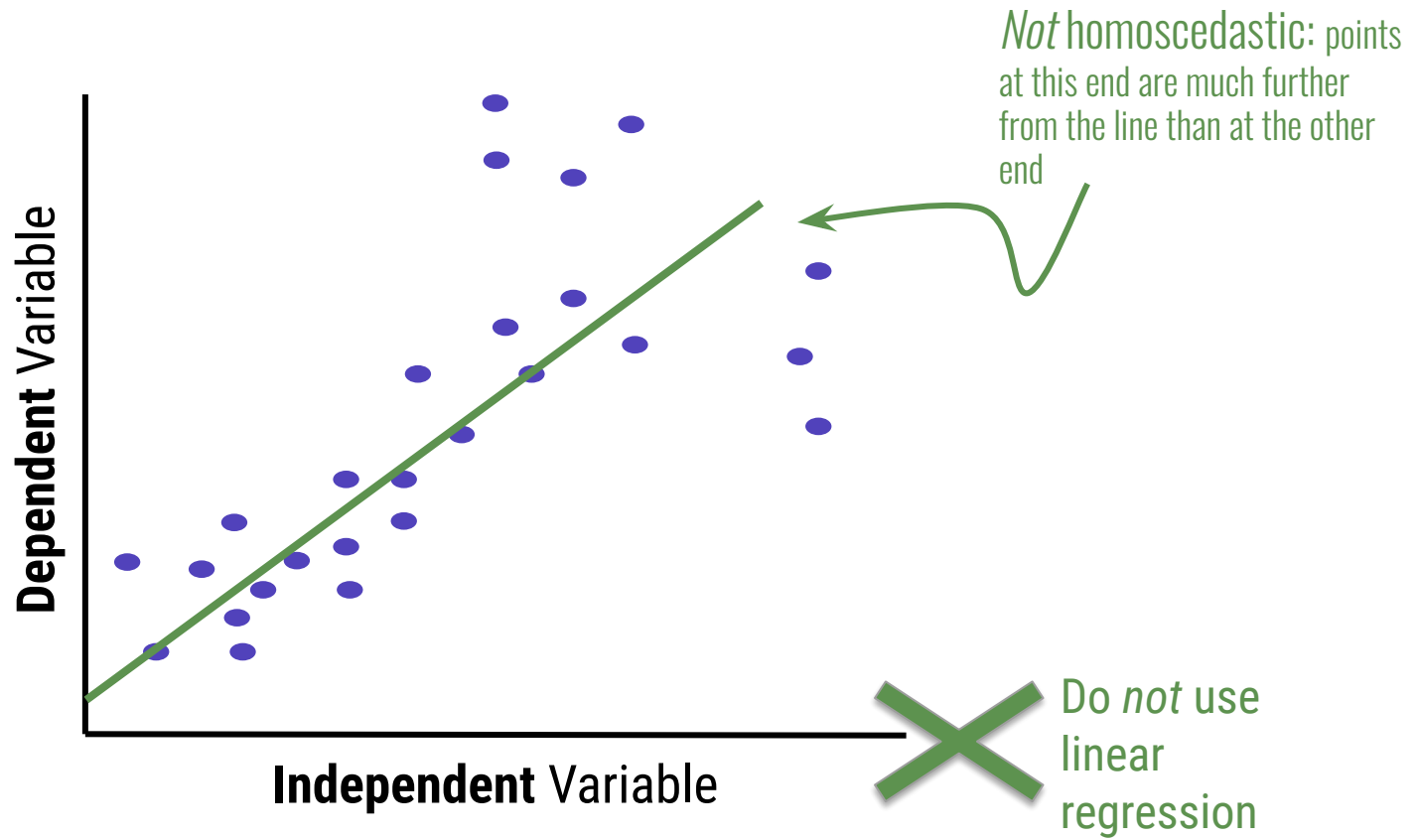
A multivariate normal
probability distribution
(joint normal)



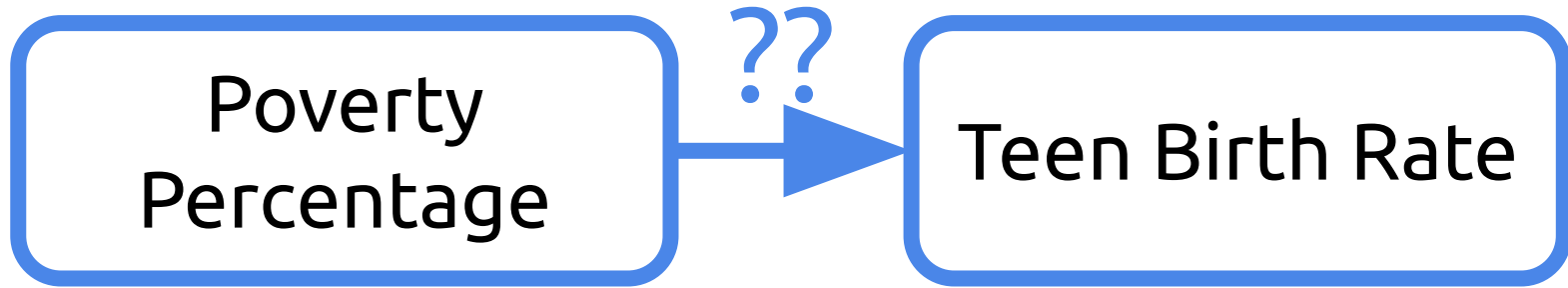
Linear regression assumes no multicollinearity. **Multicollinearity** occurs when the independent variables (in multiple linear regression) are too highly correlated with each other.

Autocorrelation occurs
when the observations are
not independent of one
another (i.e. stock prices)





Does Poverty Percentage
affect Teen Birth Rate?



Null Hypothesis:

H_0 : Poverty Rate does not affect Teen Birth Rate ($\beta=0$)

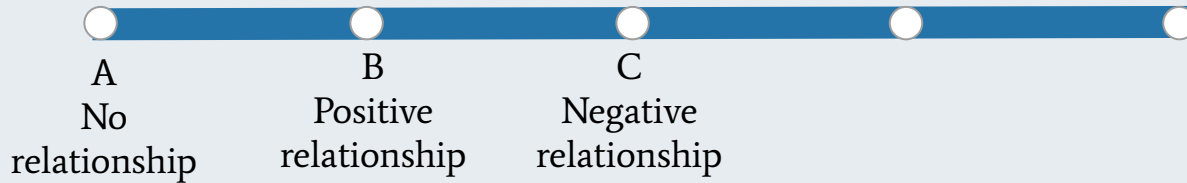
Alternative Hypothesis:

H_a : Poverty Rate affects Teen Birth Rate ($\beta \neq 0$)



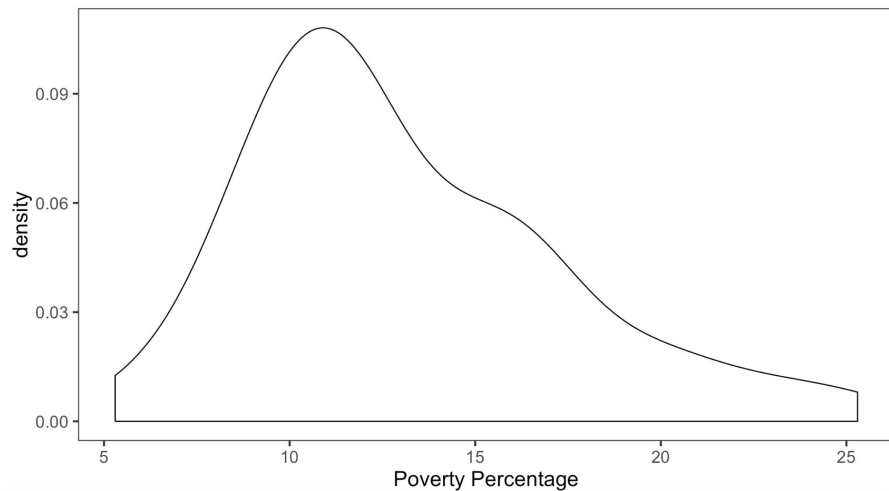
What is the relationship between Poverty Percentage & Teen Birth Rate?

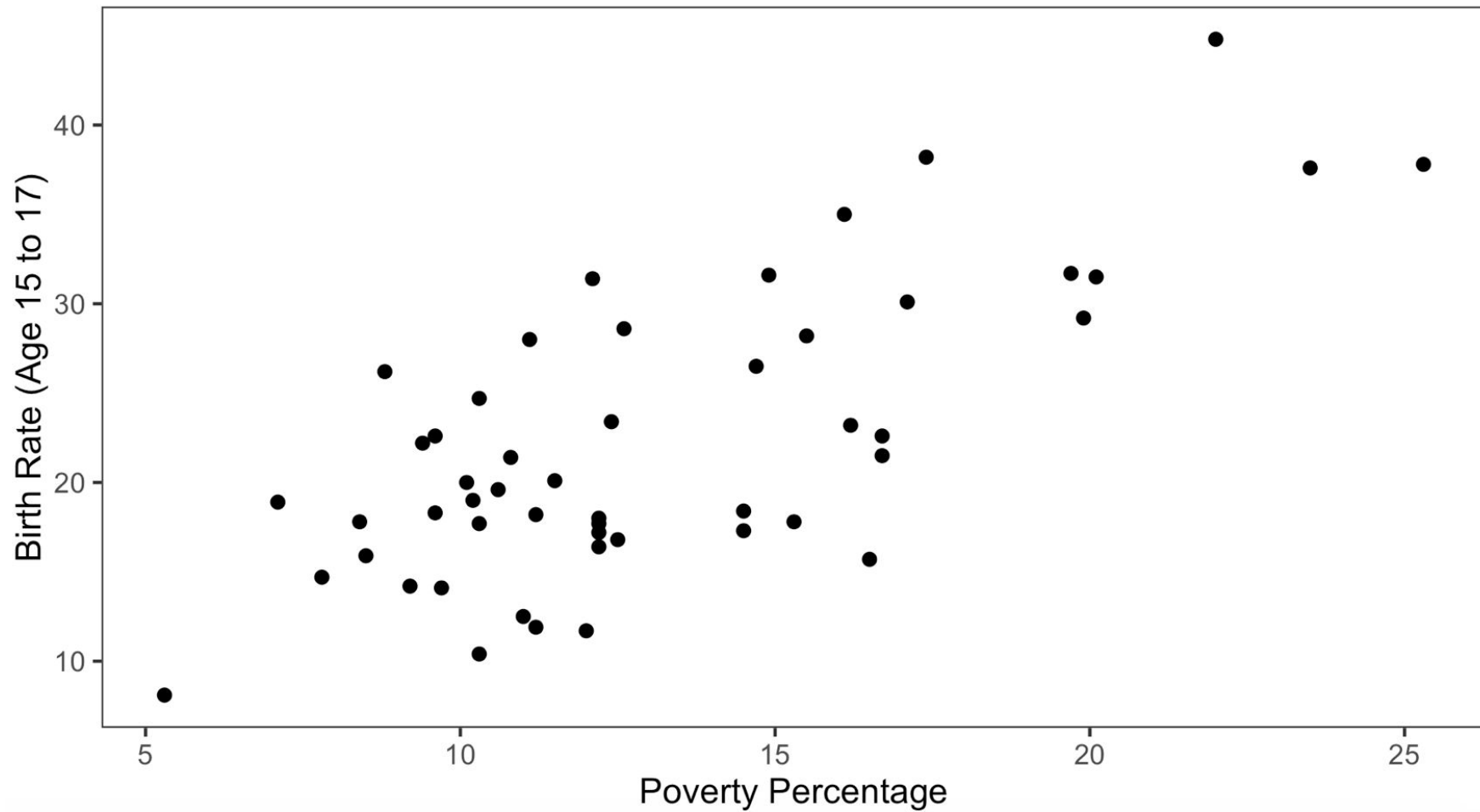
What's your hypothesis?

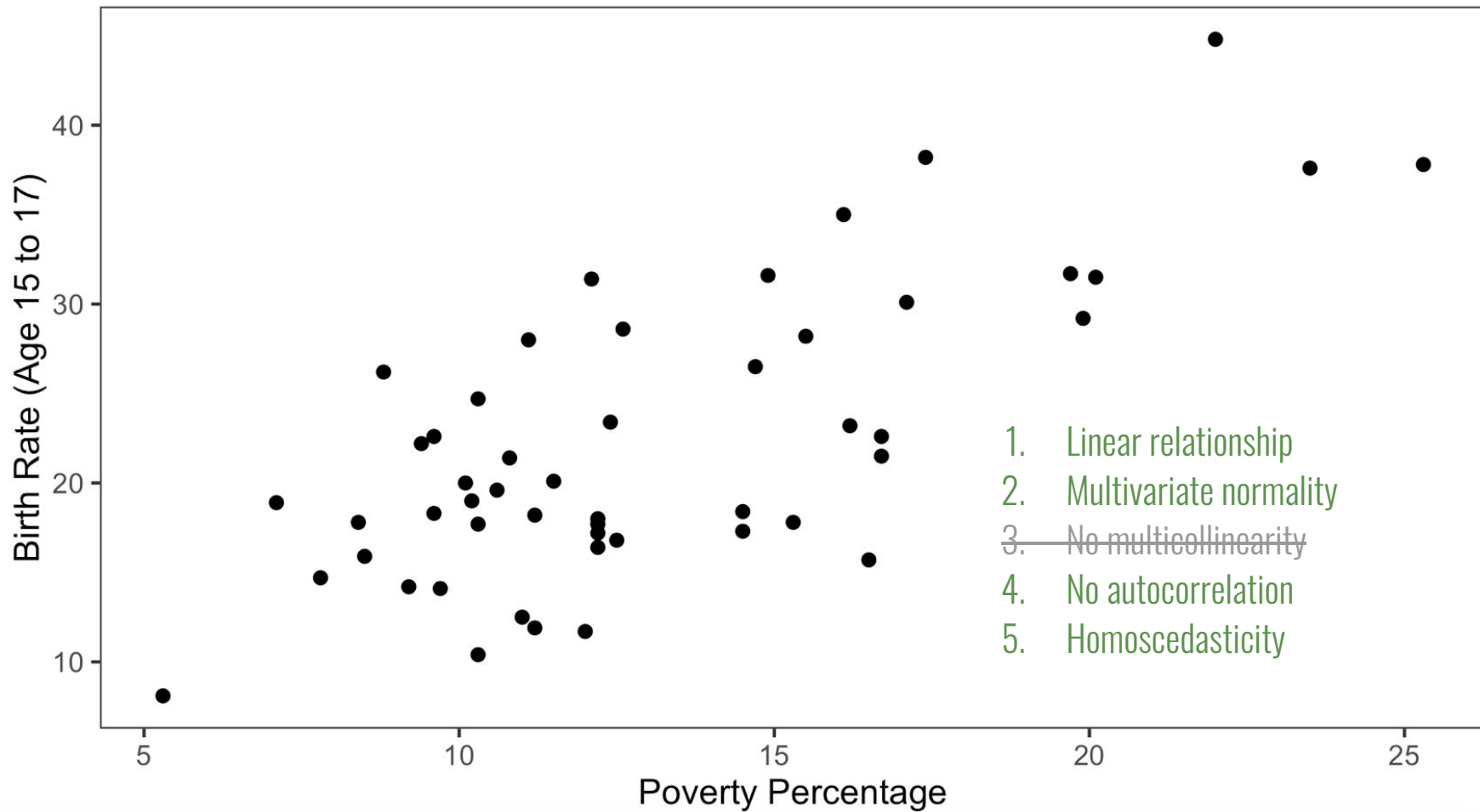


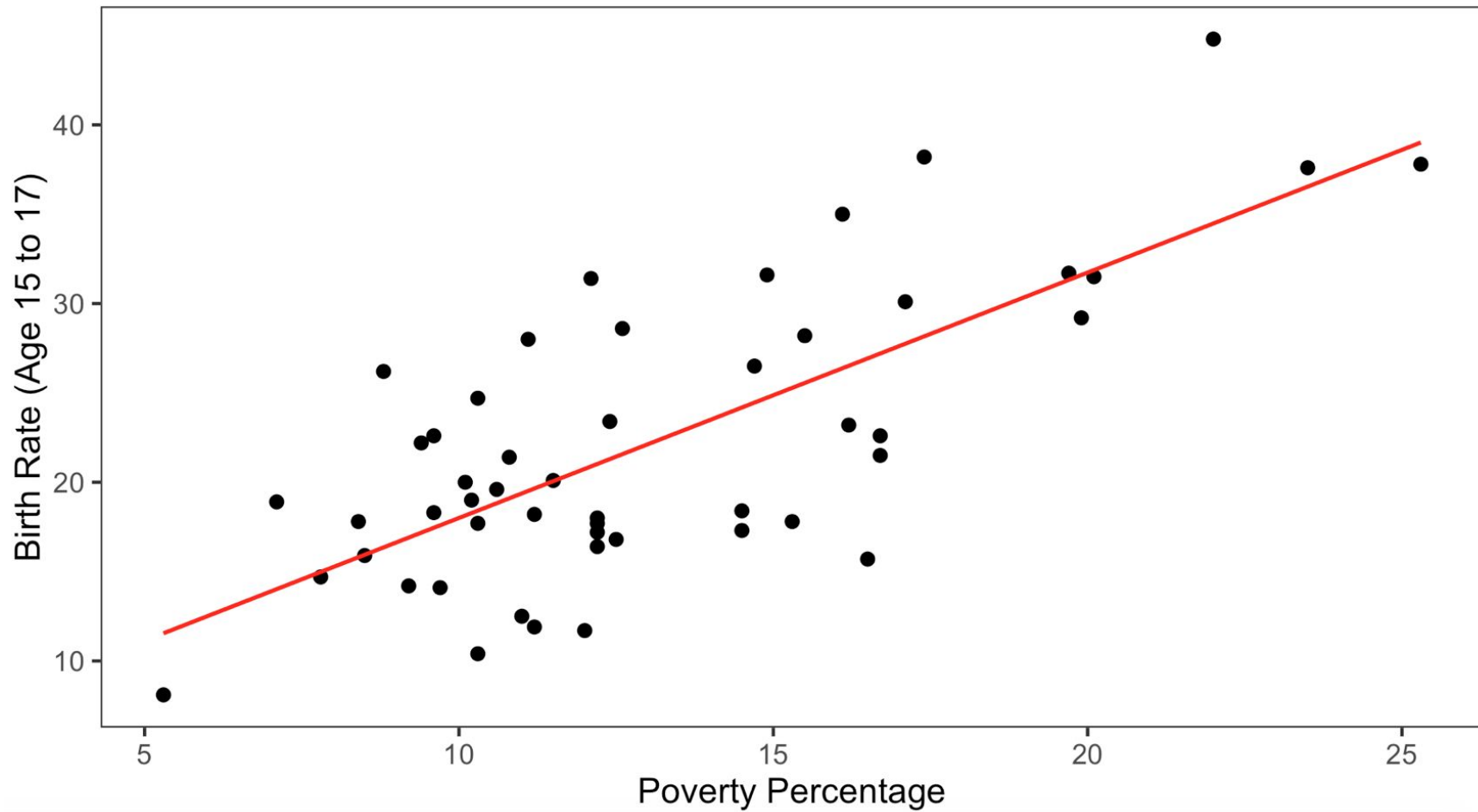
| | Location | PovPct | Brth15to17 | Brth18to19 | ViolCrime | TeenBrth |
|----|----------------------|--------|------------|------------|-----------|----------|
| 1 | Alabama | 20.1 | 31.5 | 88.7 | 11.2 | 54.5 |
| 2 | Alaska | 7.1 | 18.9 | 73.7 | 9.1 | 39.5 |
| 3 | Arizona | 16.1 | 35.0 | 102.5 | 10.4 | 61.2 |
| 4 | Arkansas | 14.9 | 31.6 | 101.7 | 10.4 | 59.9 |
| 5 | California | 16.7 | 22.6 | 69.1 | 11.2 | 41.1 |
| 6 | Colorado | 8.8 | 26.2 | 79.1 | 5.8 | 47.0 |
| 7 | Connecticut | 9.7 | 14.1 | 45.1 | 4.6 | 25.8 |
| 8 | Delaware | 10.3 | 24.7 | 77.8 | 3.5 | 46.3 |
| 9 | District_of_Columbia | 22.0 | 44.8 | 101.5 | 65.0 | 69.1 |
| 10 | Florida | 16.2 | 23.2 | 78.4 | 7.3 | 44.5 |
| 11 | Georgia | 12.1 | 31.4 | 92.8 | 9.5 | 55.7 |
| 12 | Hawaii | 10.3 | 17.7 | 66.4 | 4.7 | 38.2 |
| 13 | Idaho | 14.5 | 18.4 | 69.1 | 4.1 | 39.1 |
| 14 | Illinois | 12.4 | 23.4 | 70.5 | 10.3 | 42.2 |
| 15 | Indiana | 9.6 | 22.6 | 78.5 | 8.0 | 44.6 |
| 16 | Iowa | 12.2 | 16.4 | 55.4 | 1.8 | 32.5 |
| 17 | Kansas | 10.8 | 21.4 | 74.2 | 6.2 | 43.0 |

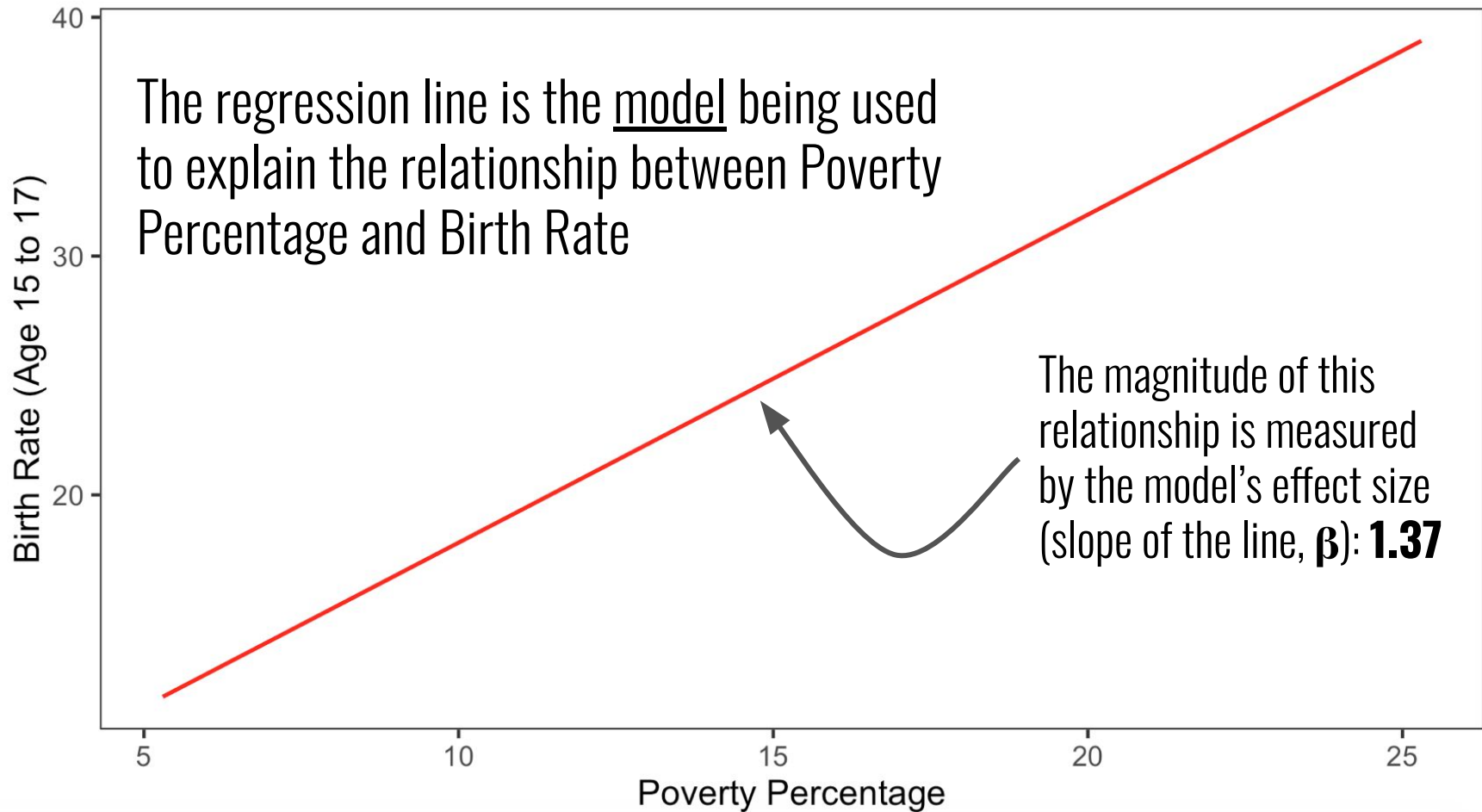
Normal(ish) distributions

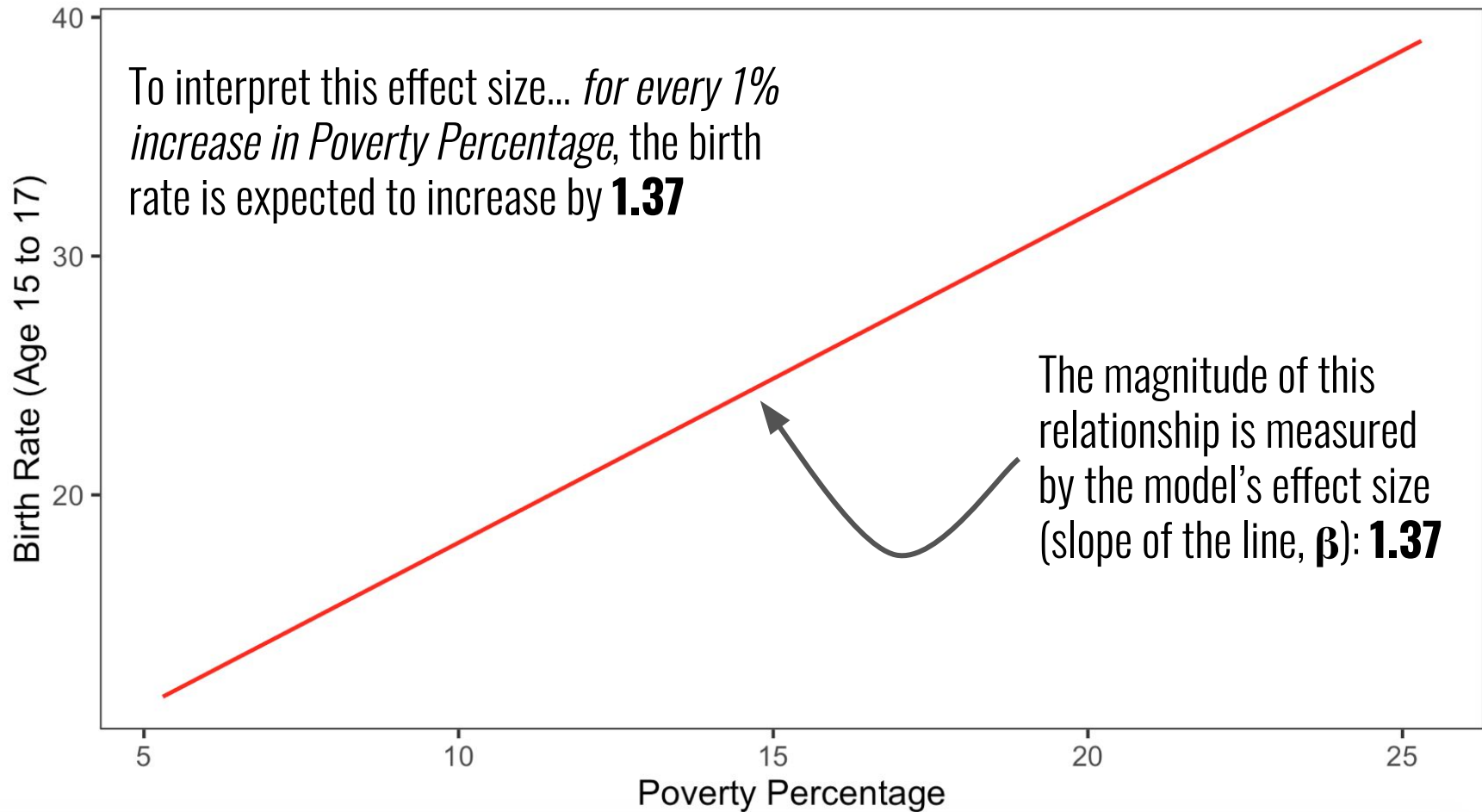




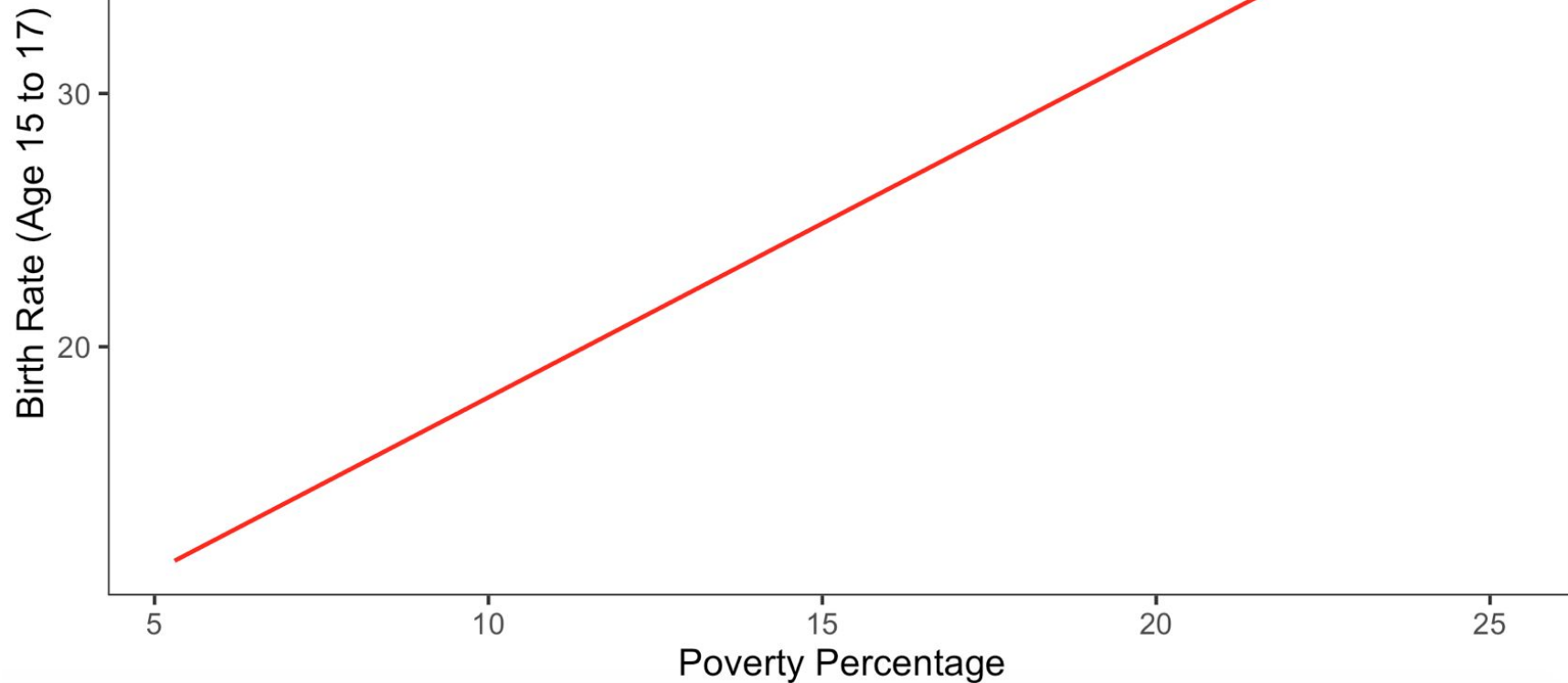








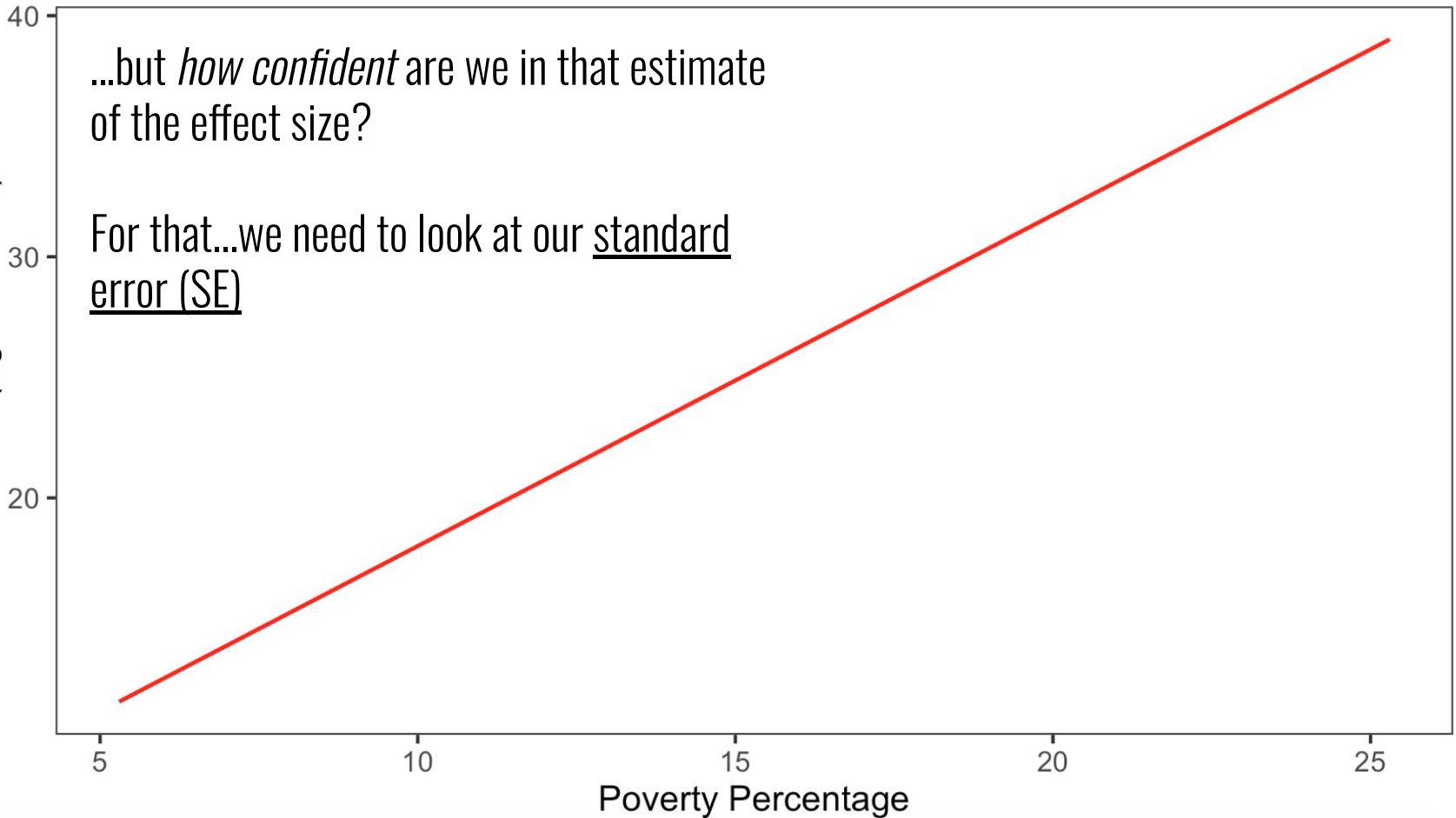
...but *how confident* are we in that estimate of the effect size?

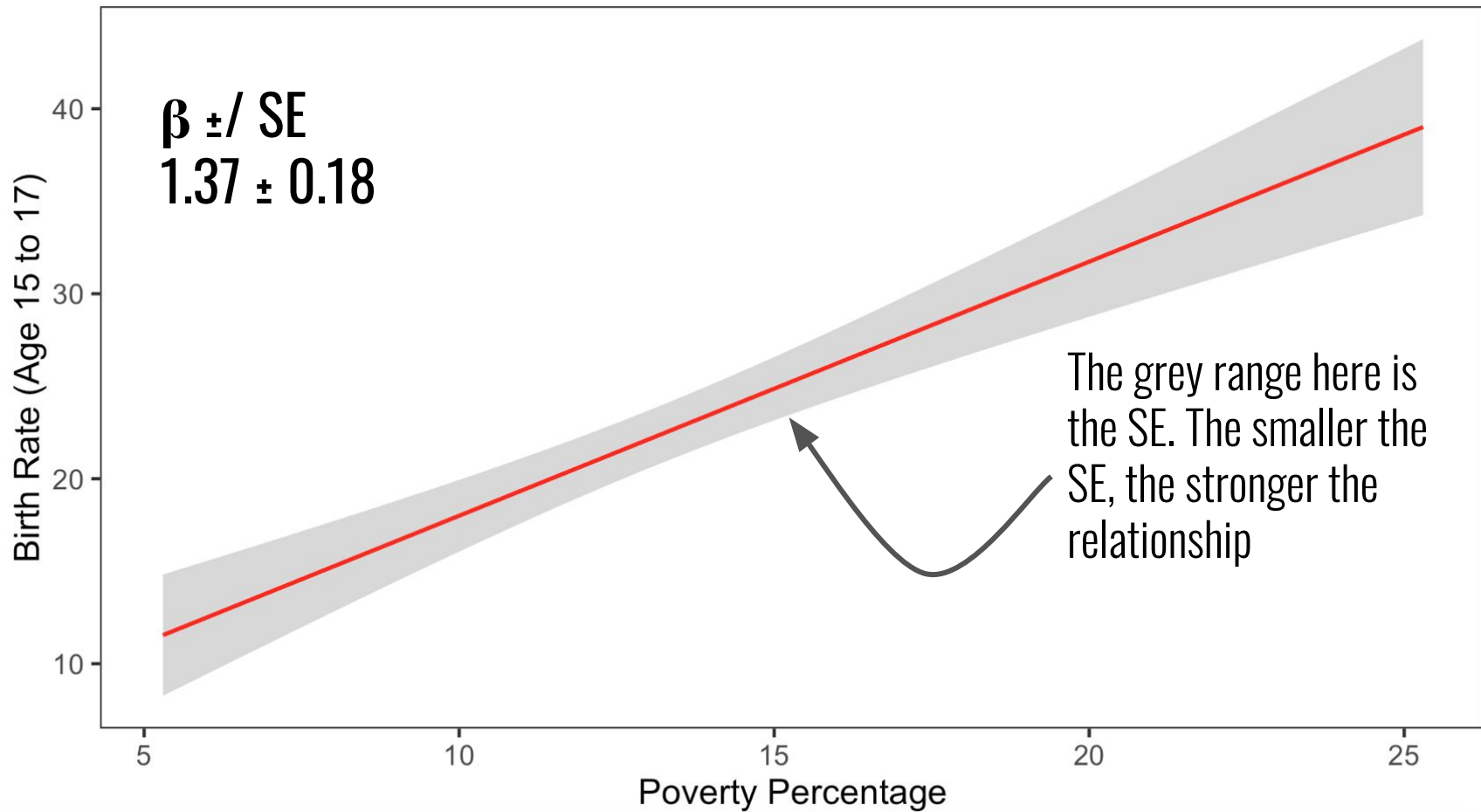


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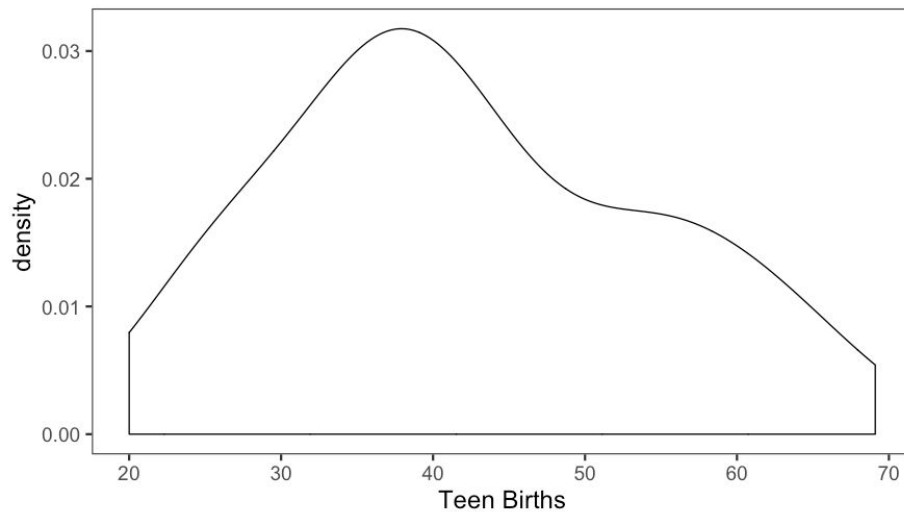
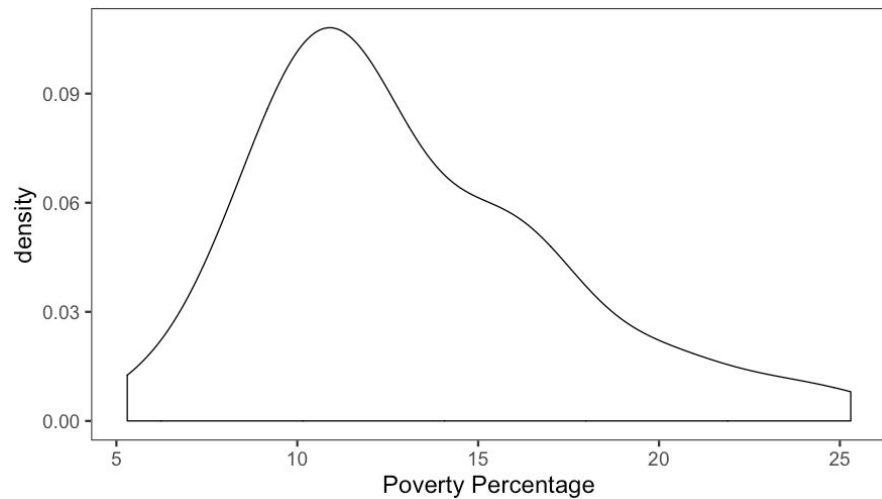
For that...we need to look at our standard error (SE)

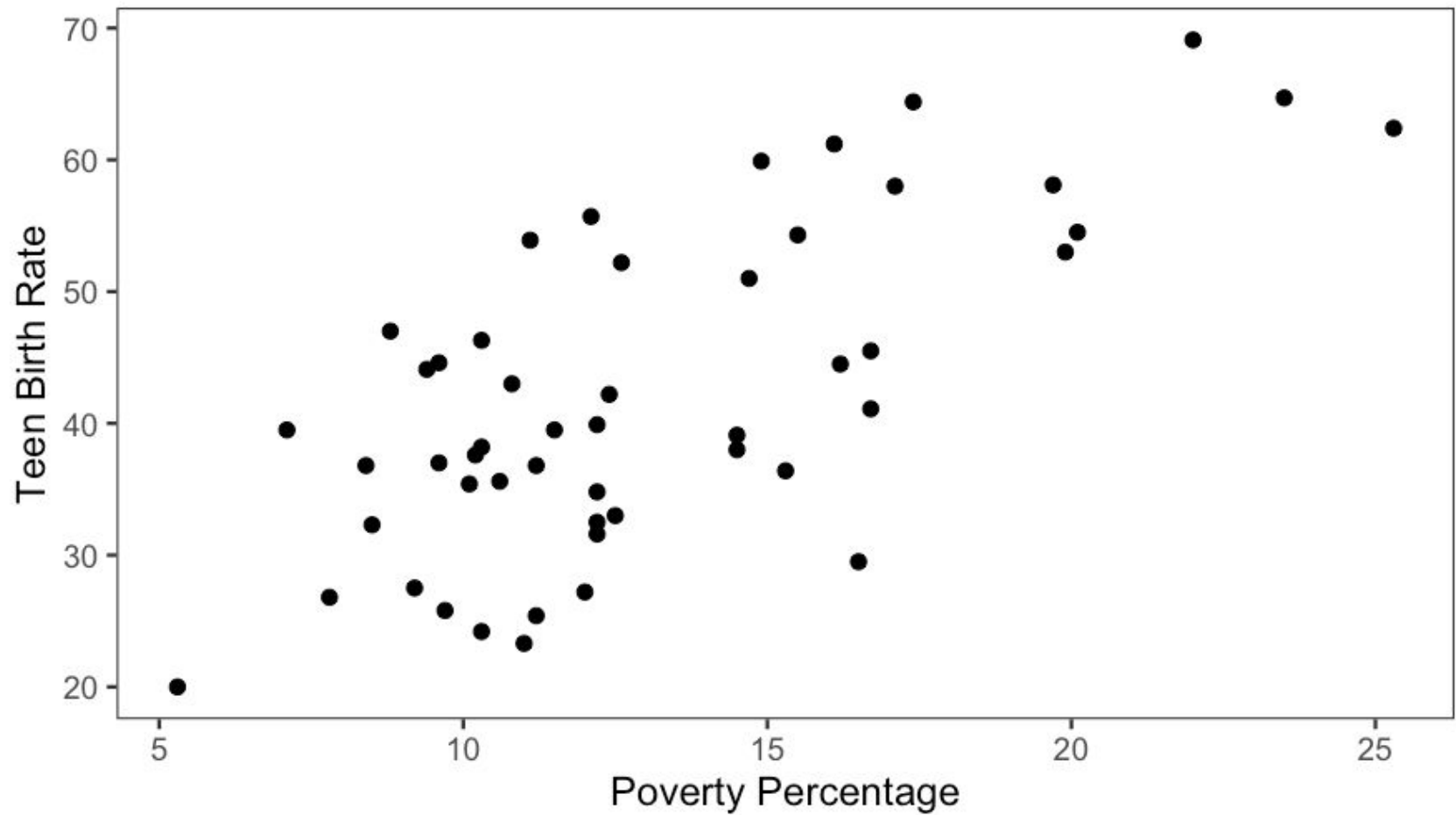
Birth Rate (Age 15 to 17)

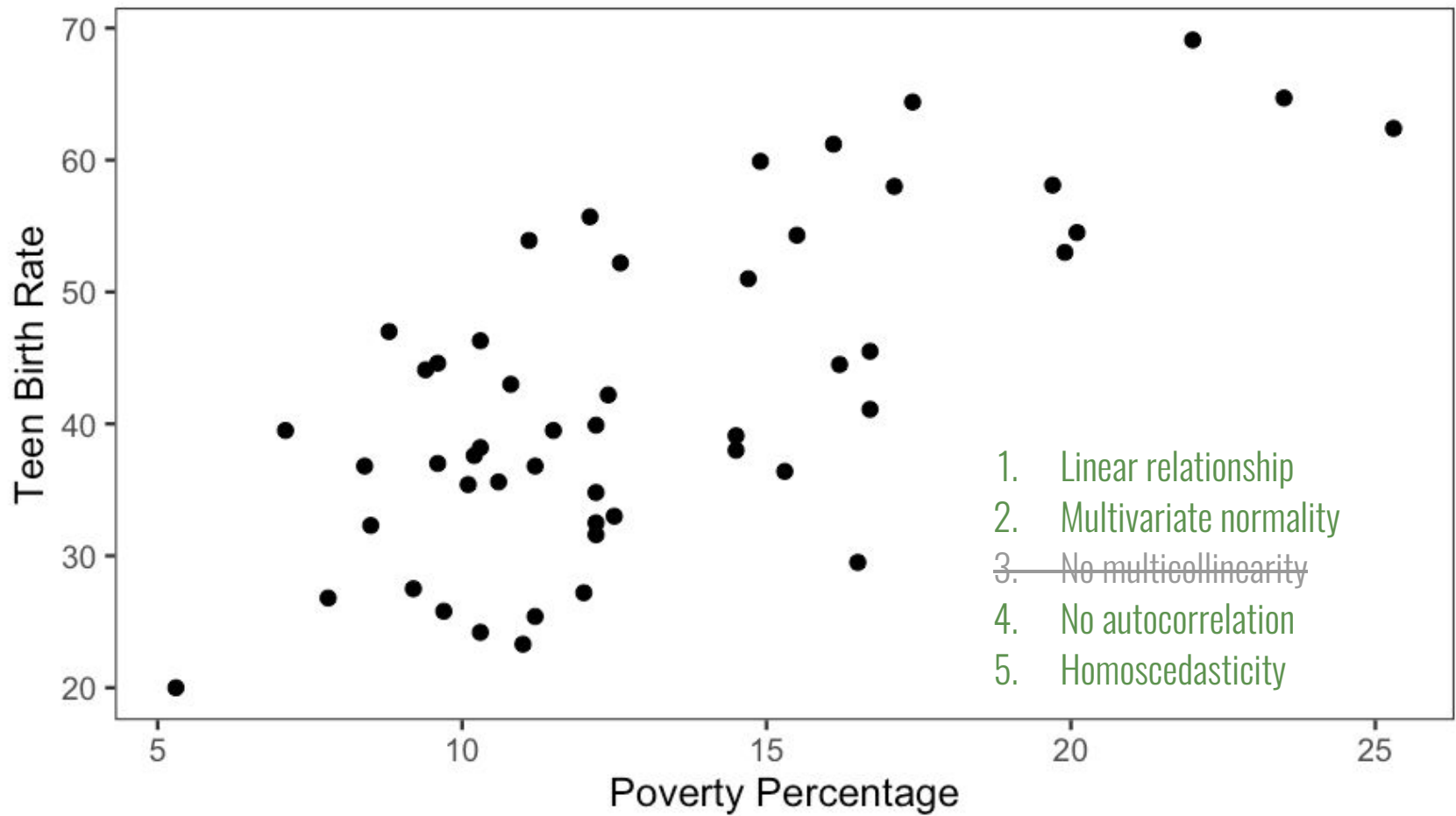


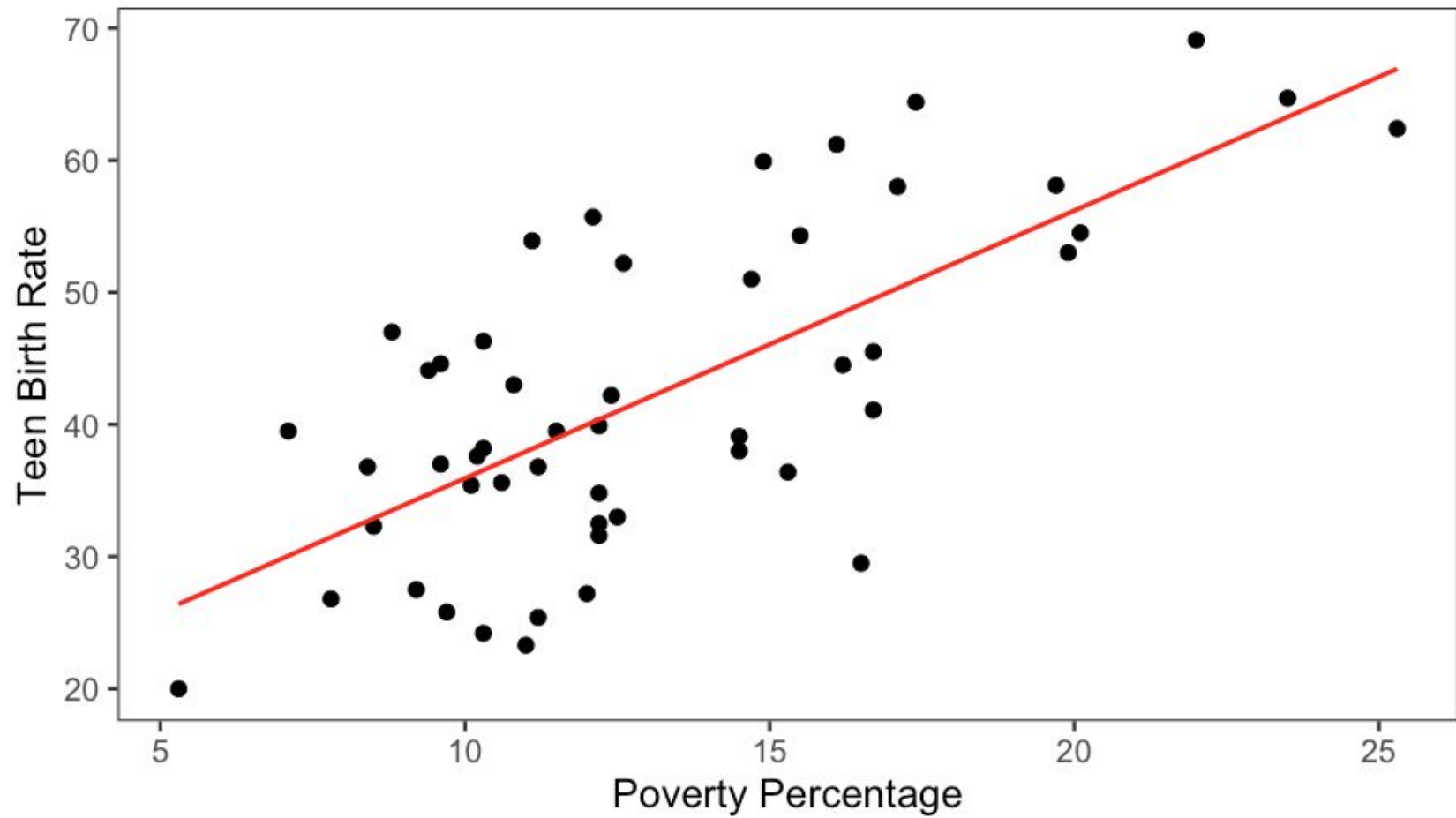


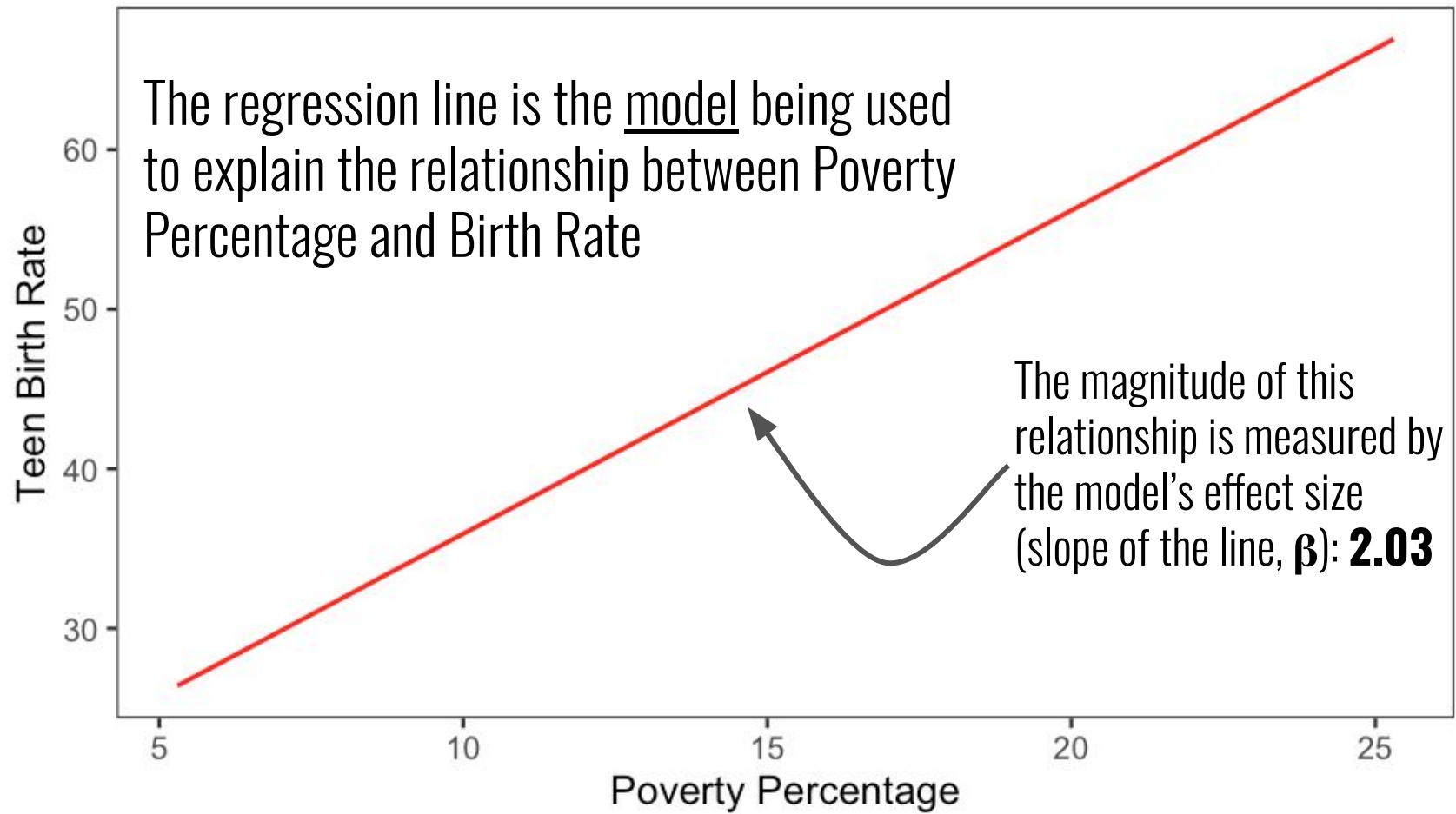
Normal(ish) distributions

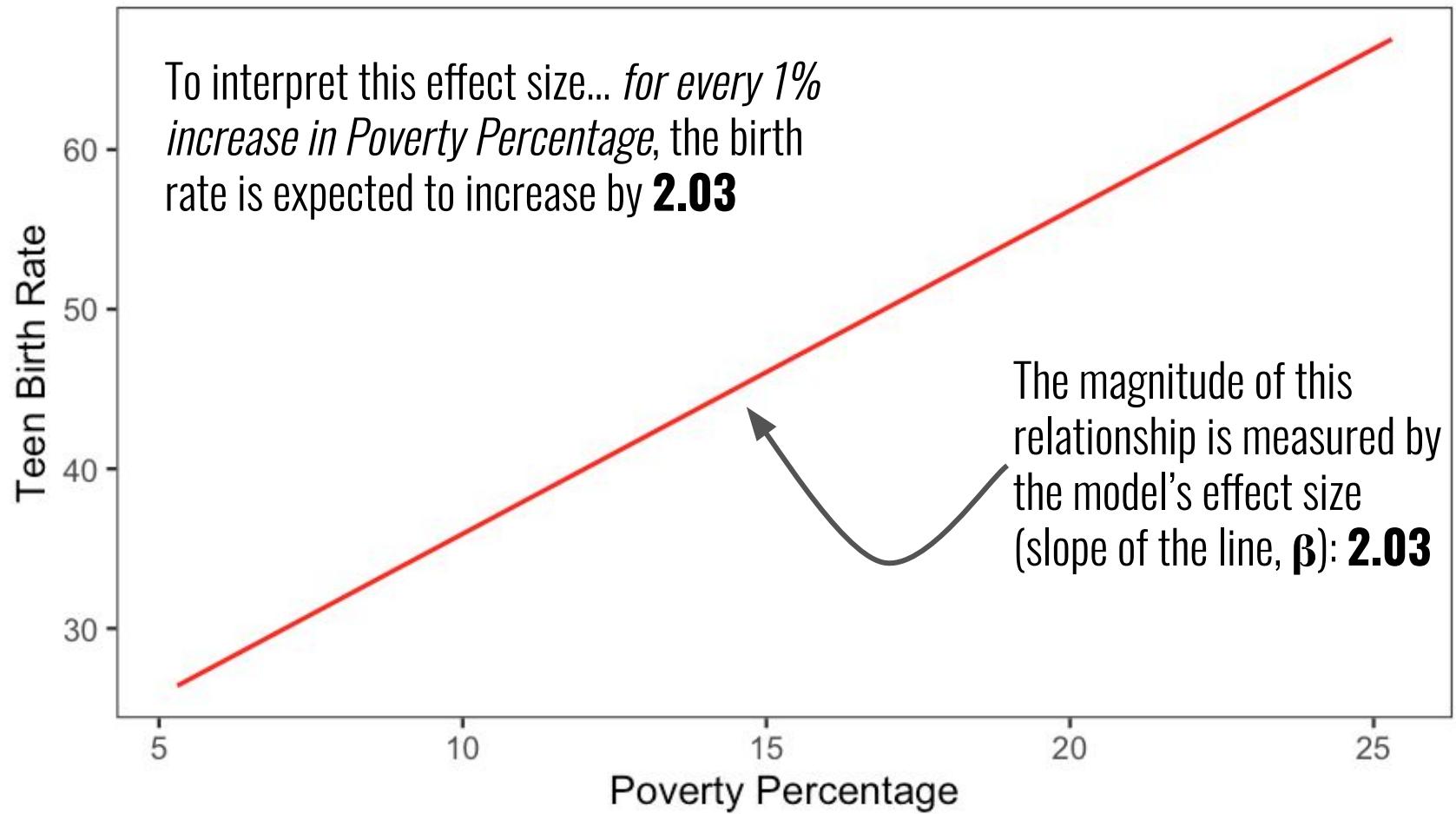












...but *how confident* are we in that estimate of the effect size?

For that...we need to look at our standard error (SE)

Teen Birth Rate

60

50

40

30

5

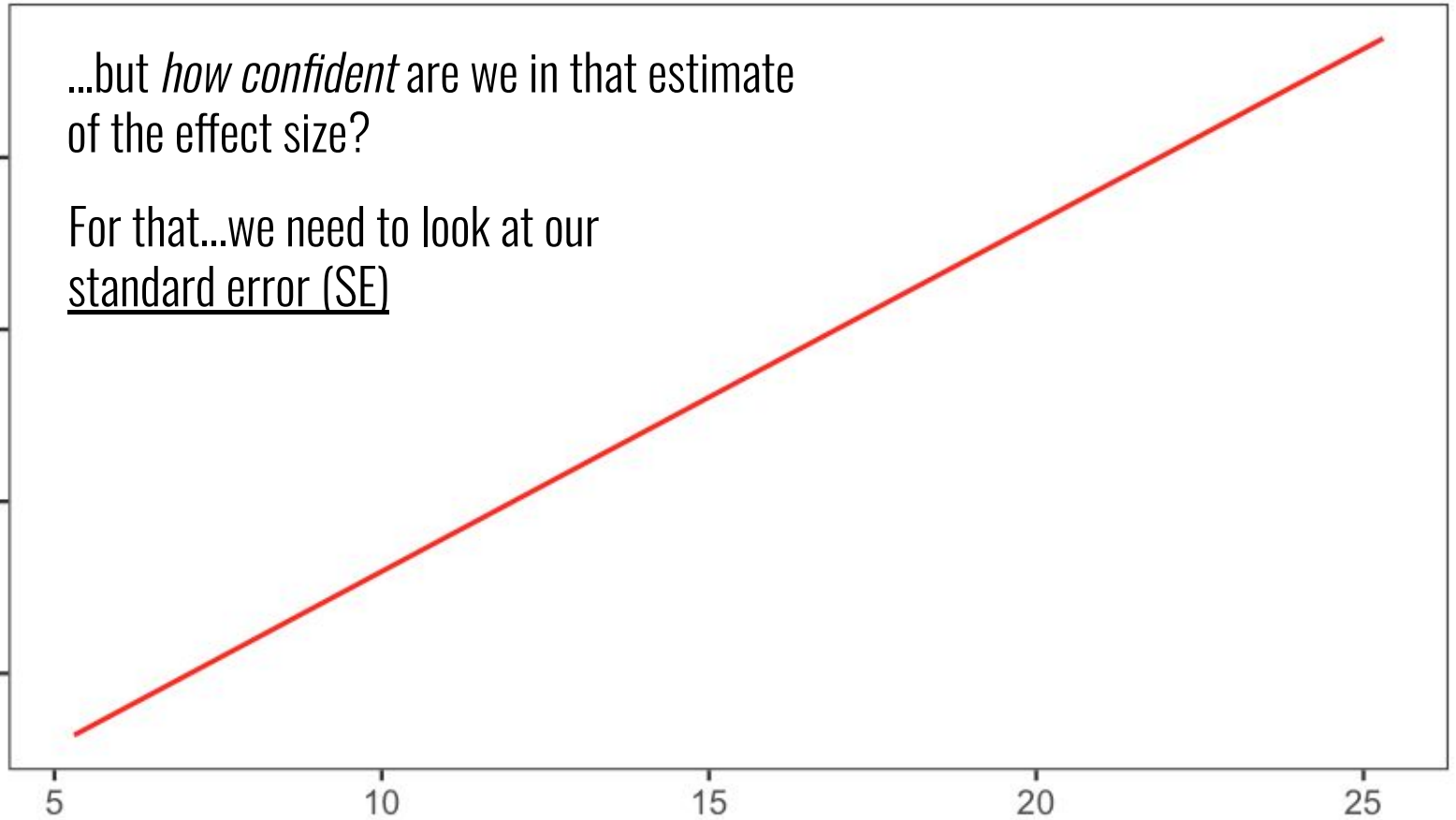
10

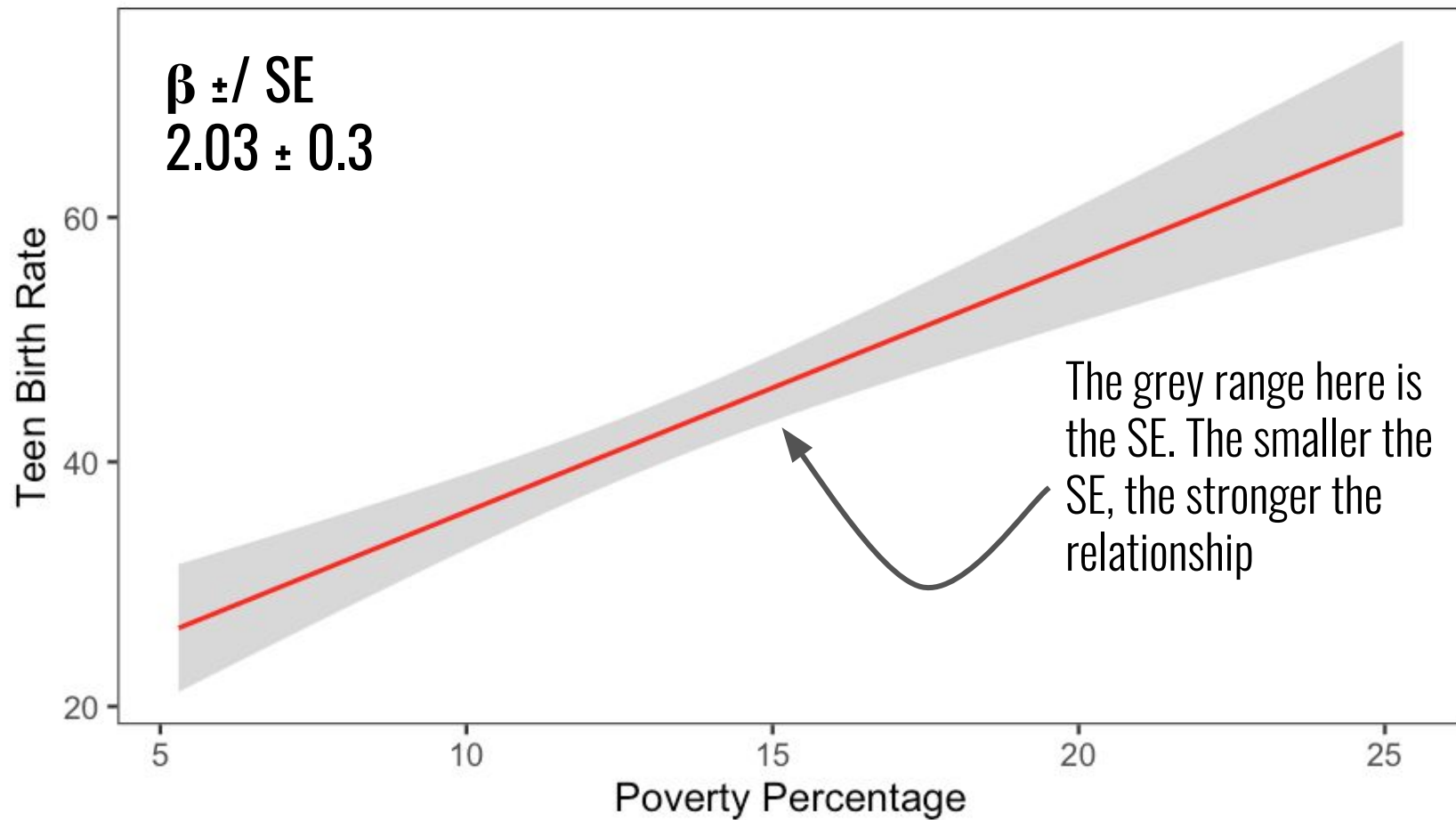
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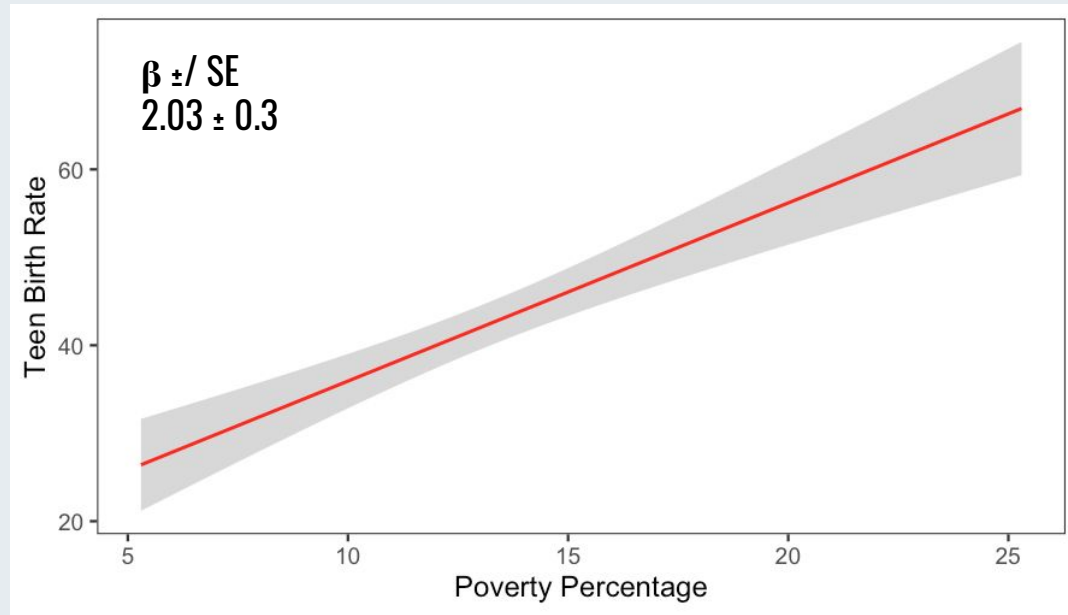
20

25

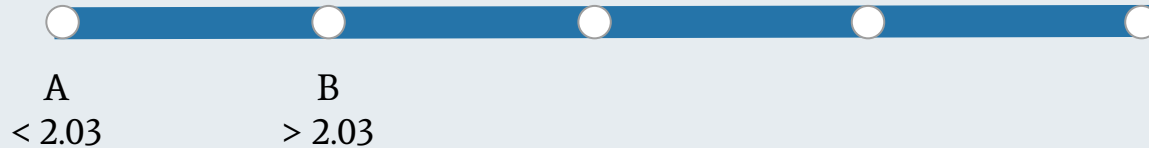
Poverty Percentage

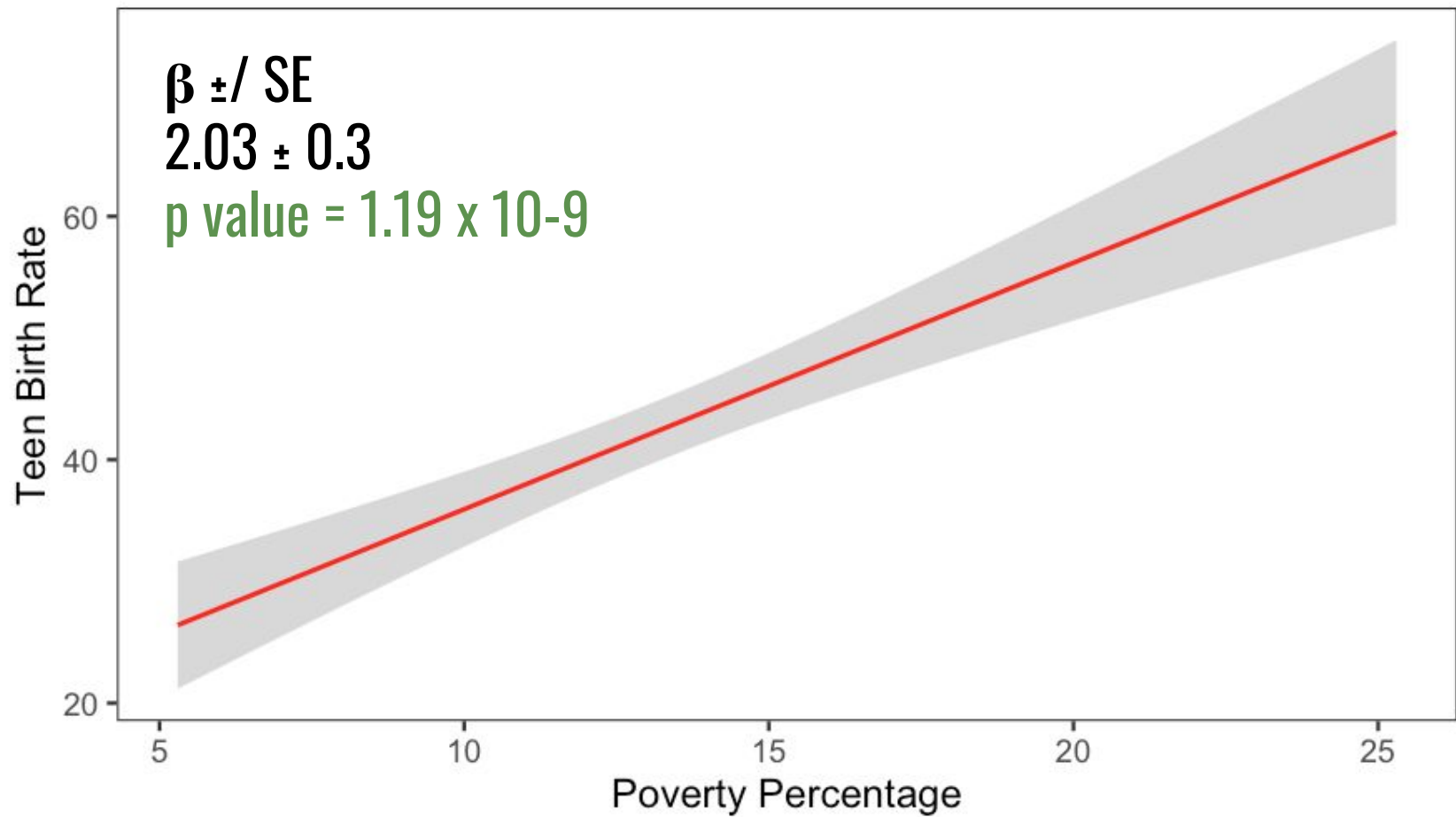




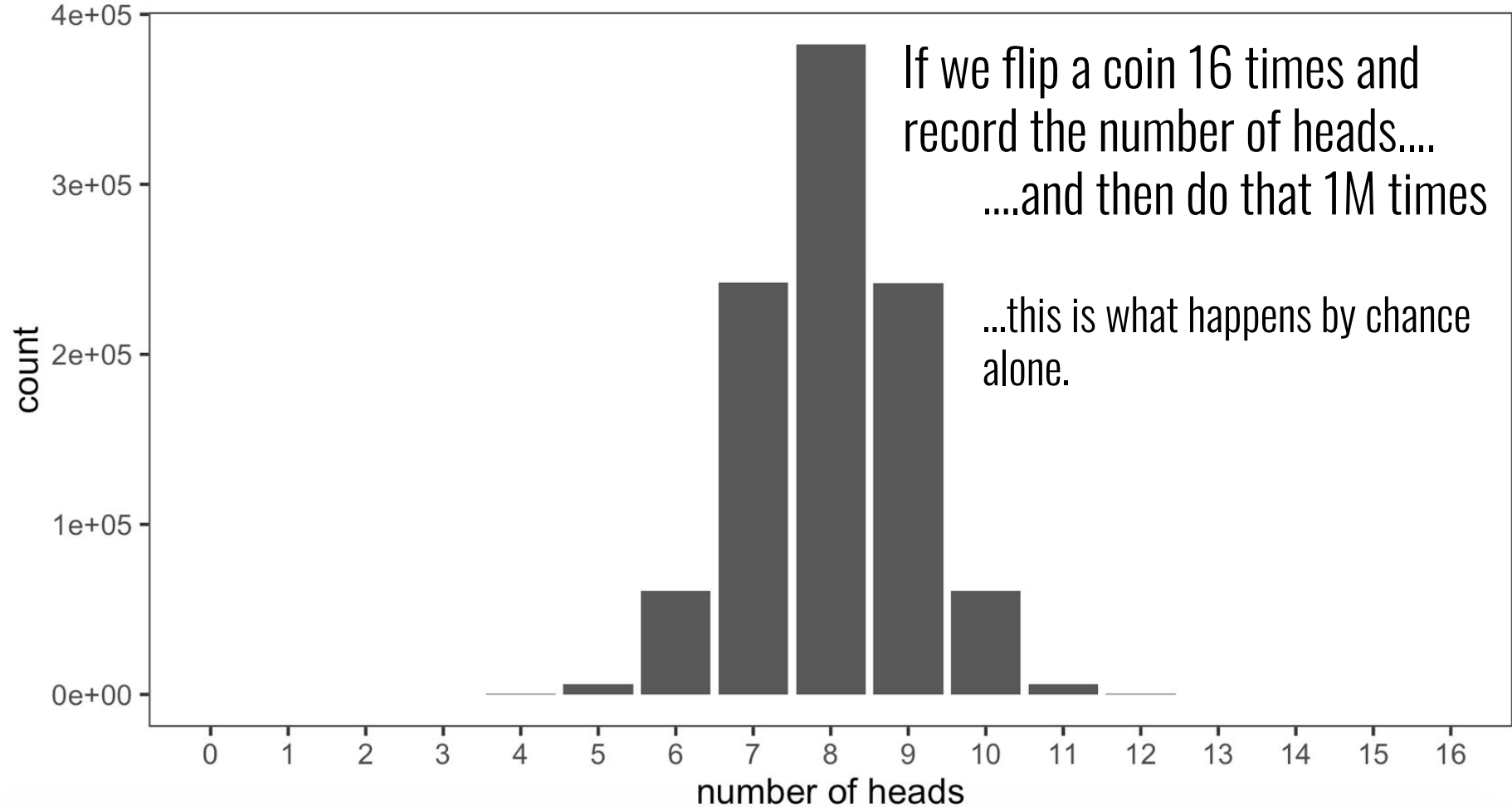


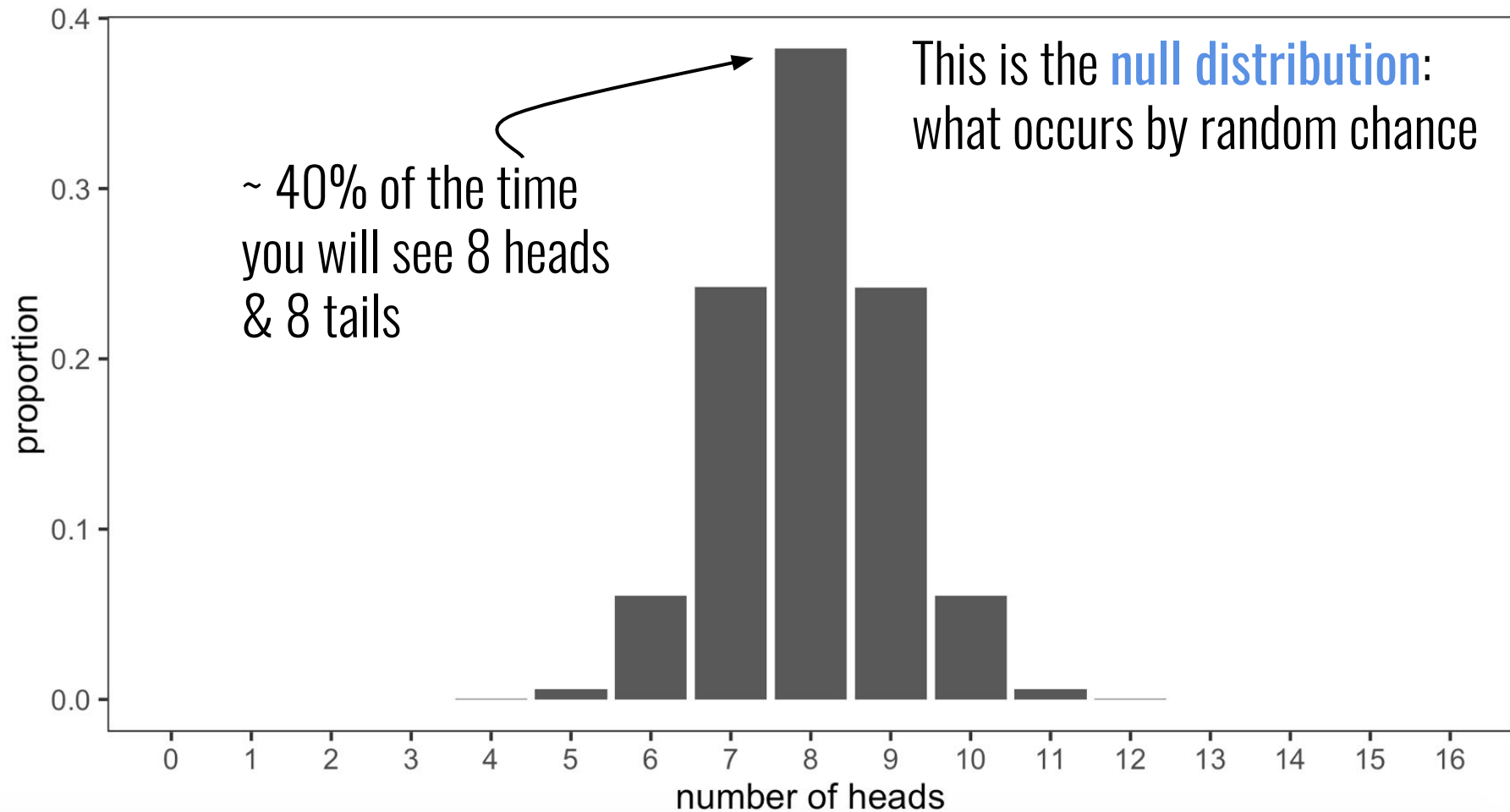
If there were a stronger effect of Poverty on Birth rate, what would β be?

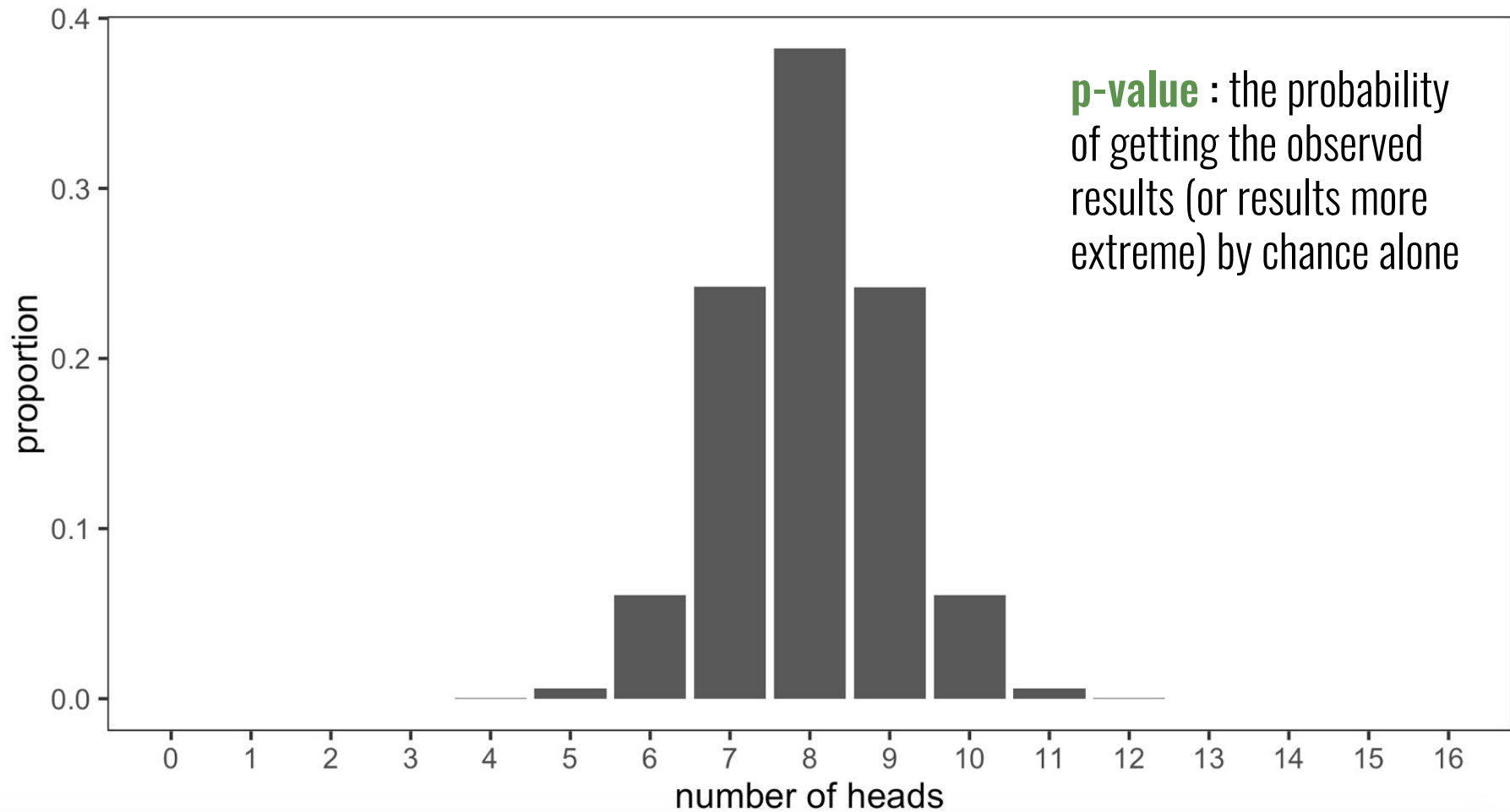




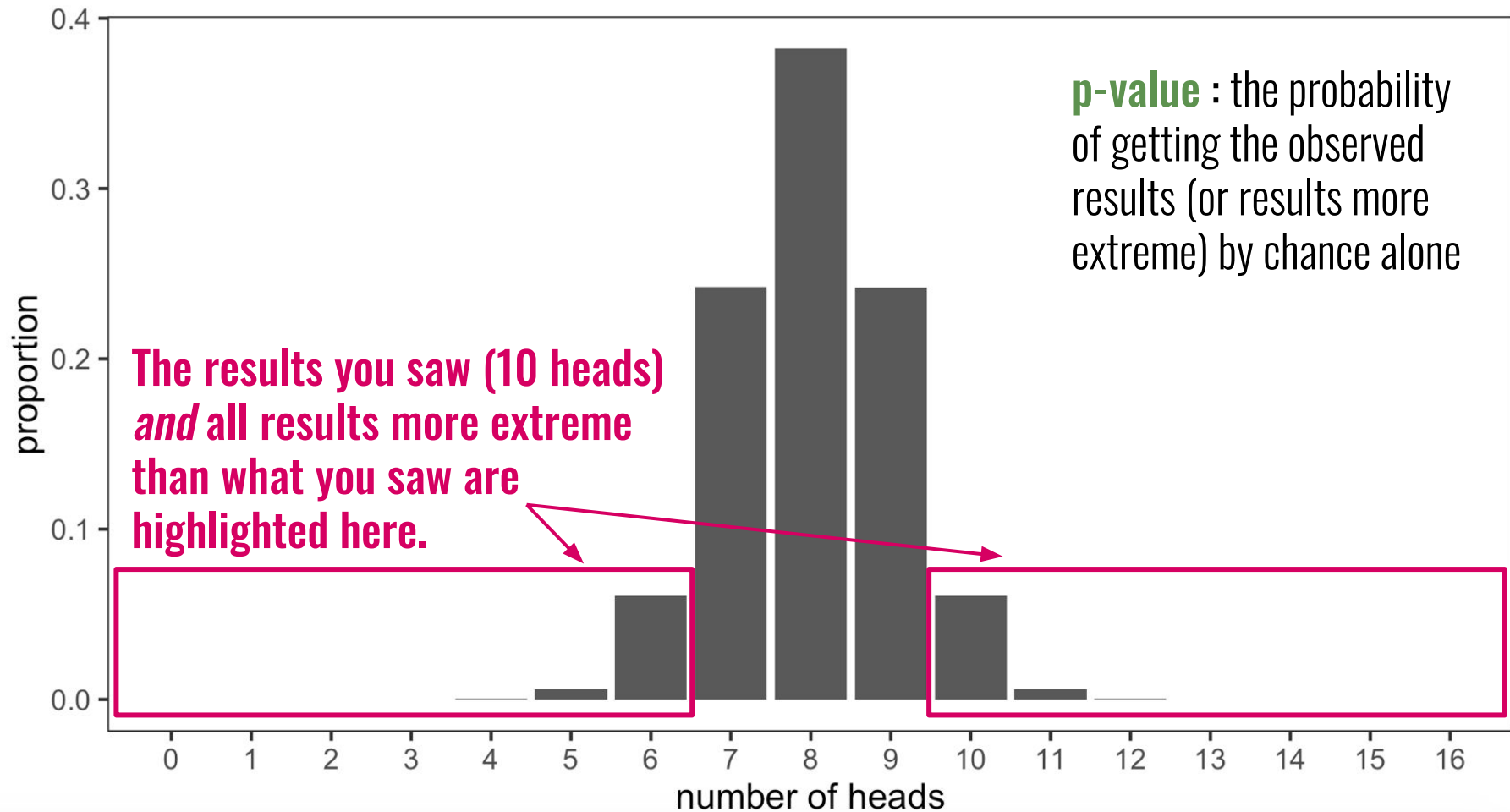
p-value : the probability of getting the observed results (or results more extreme) by chance alone

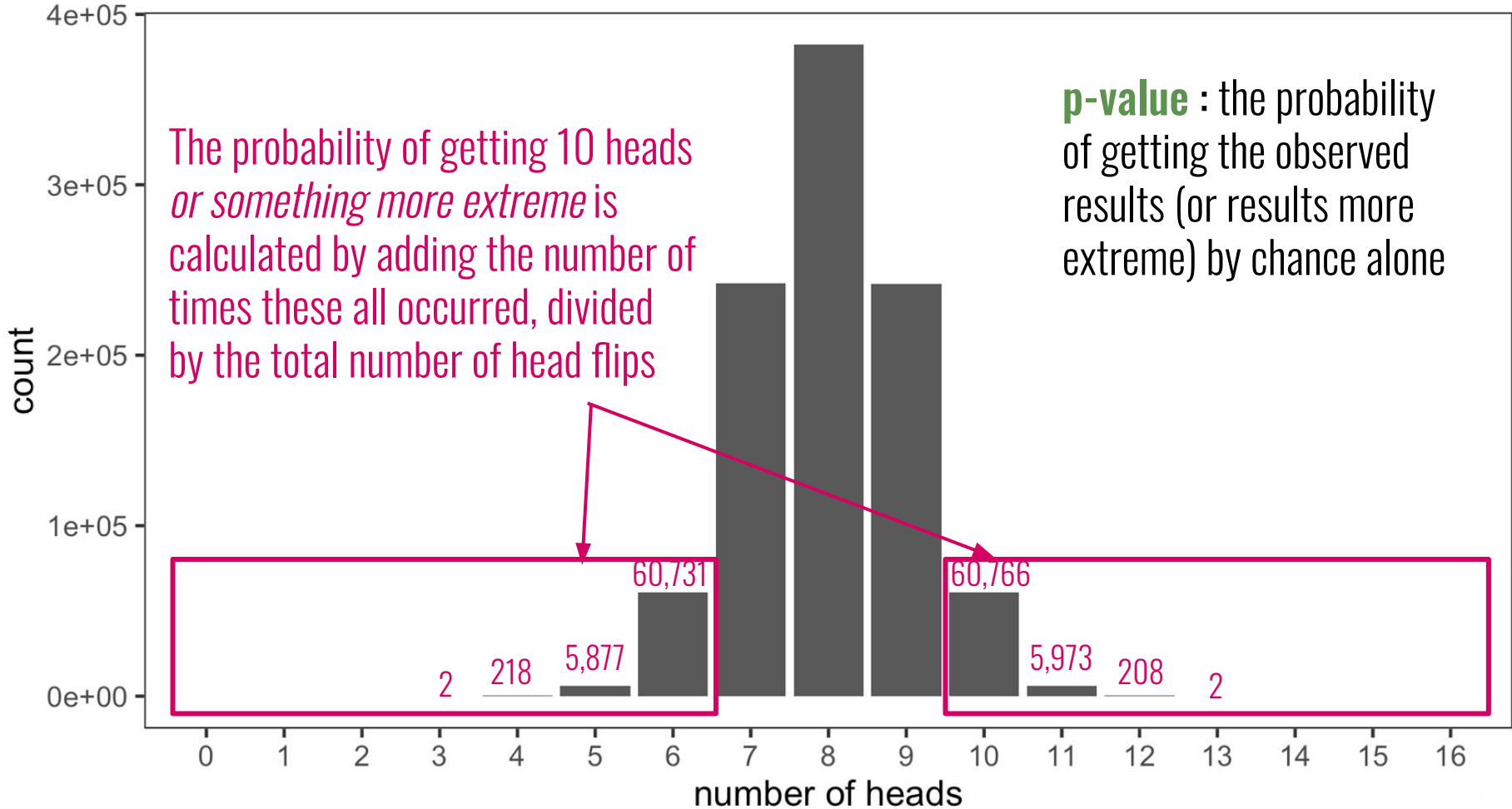


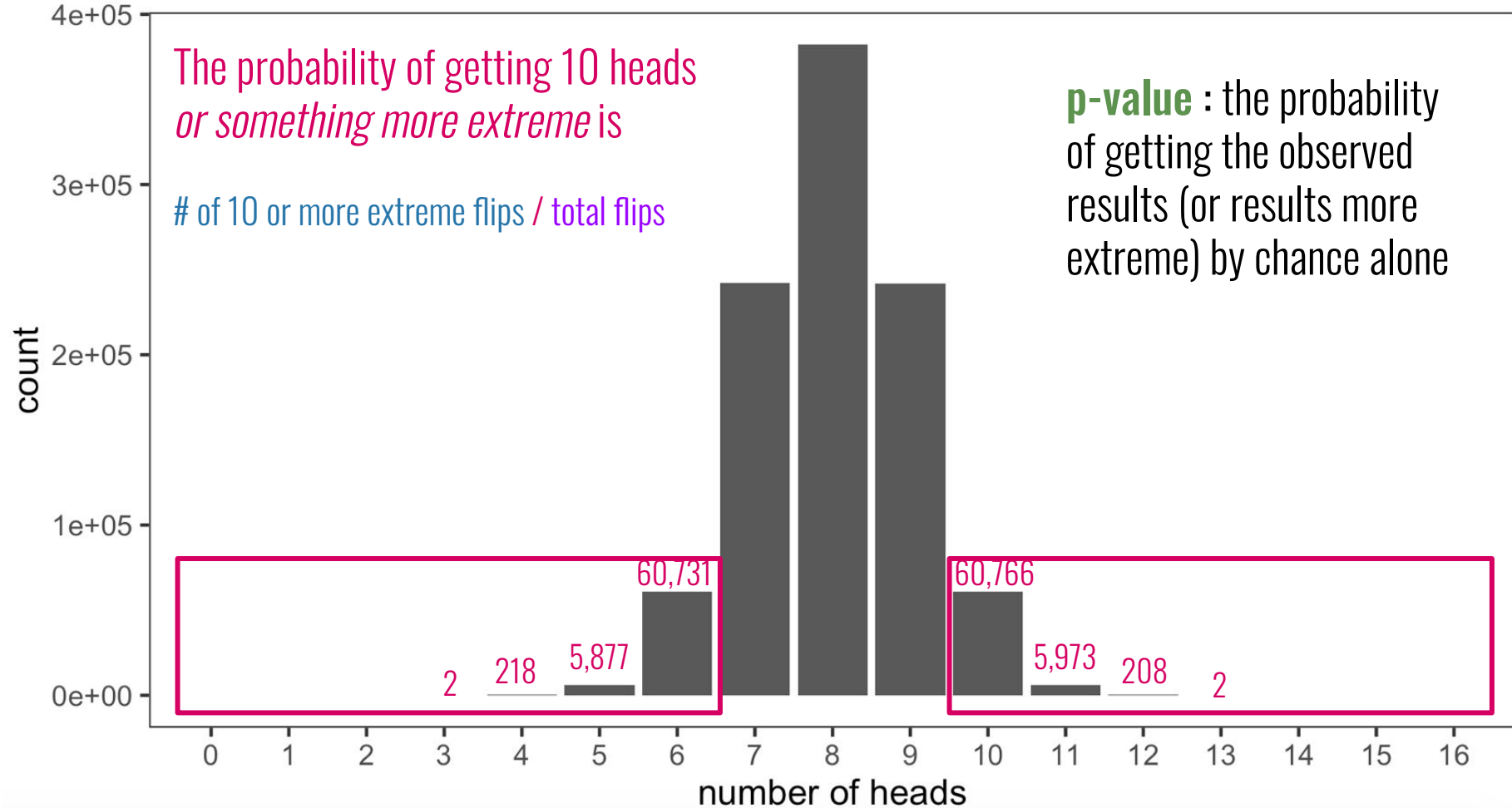


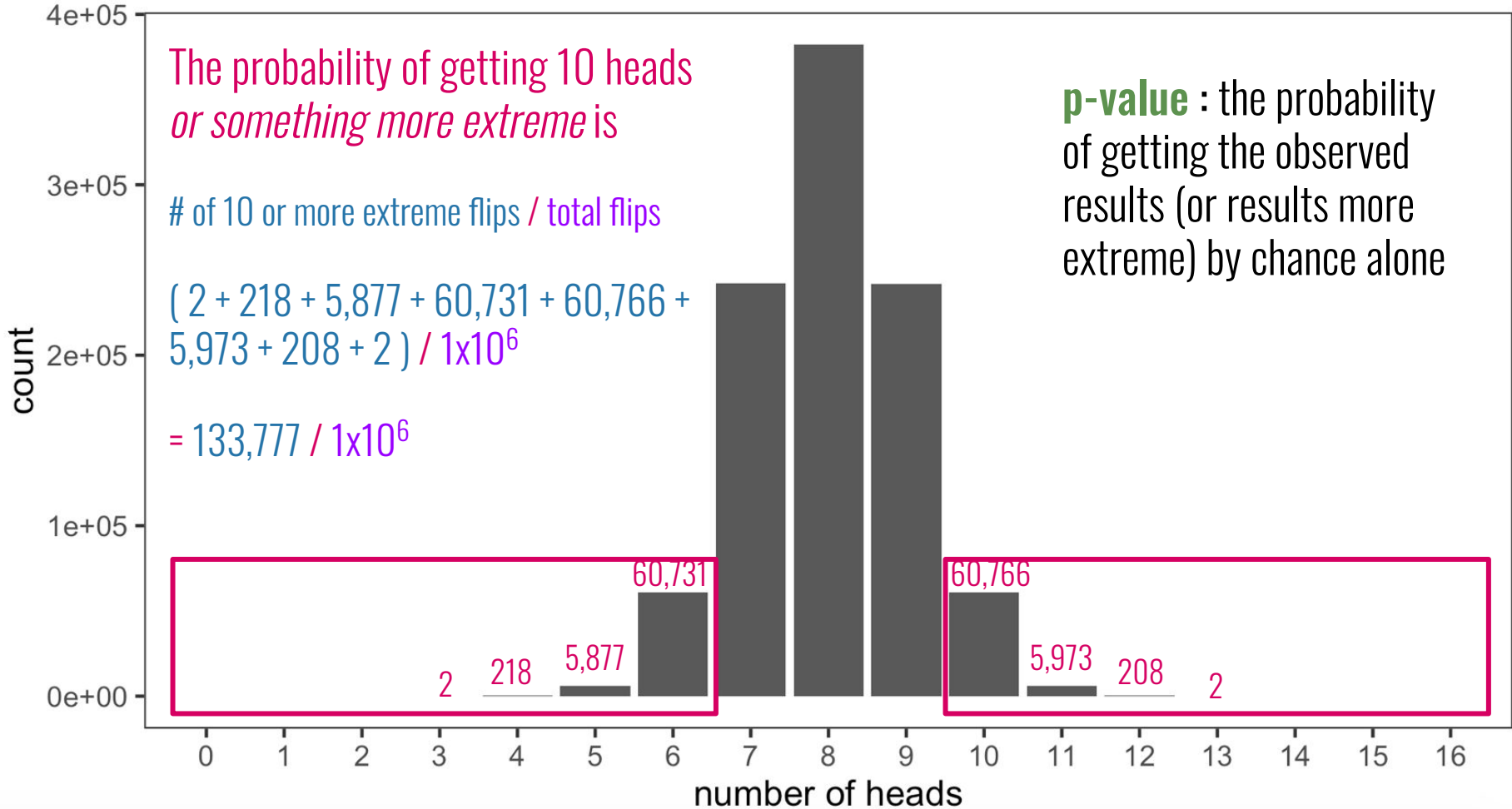


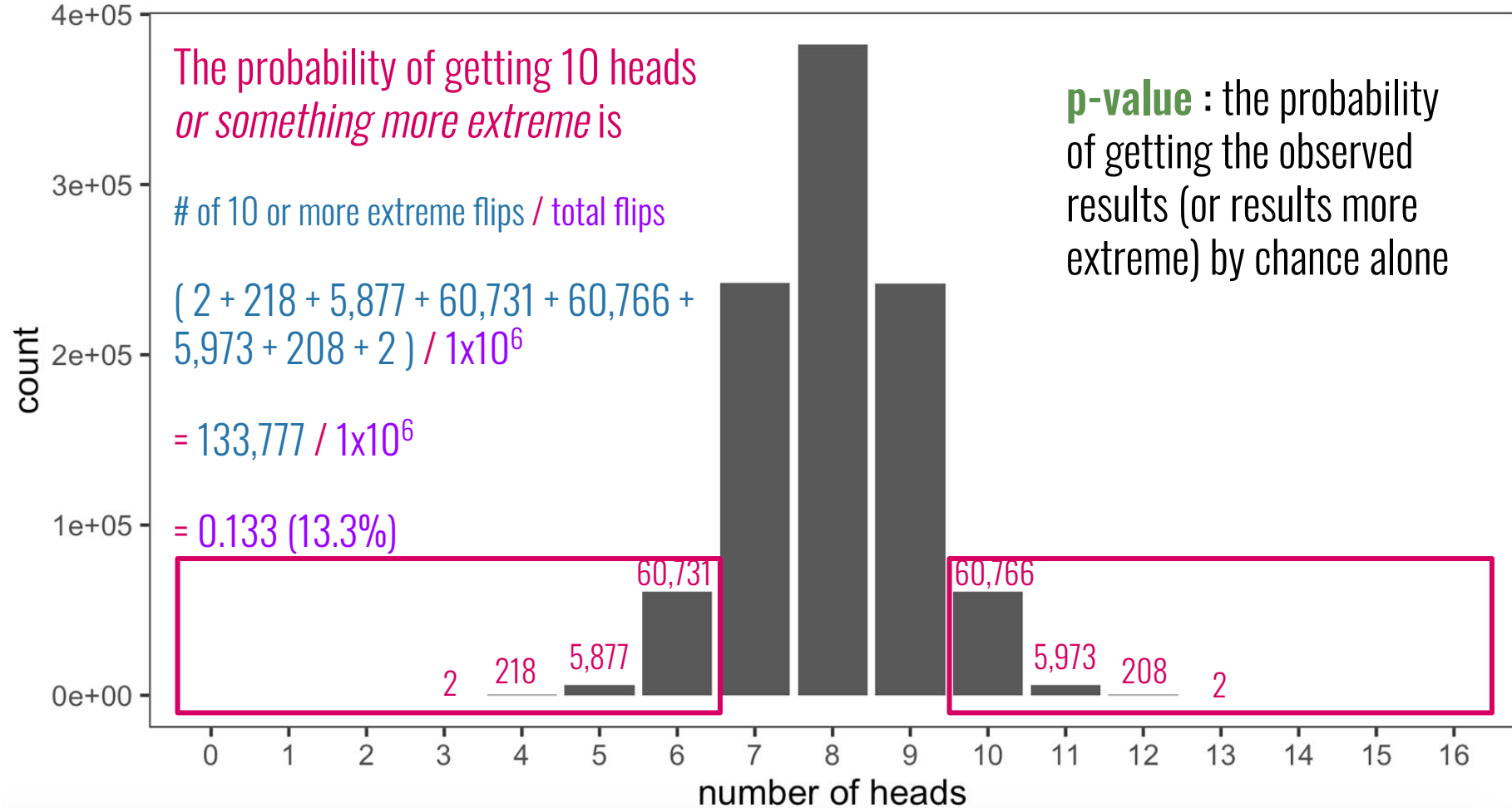


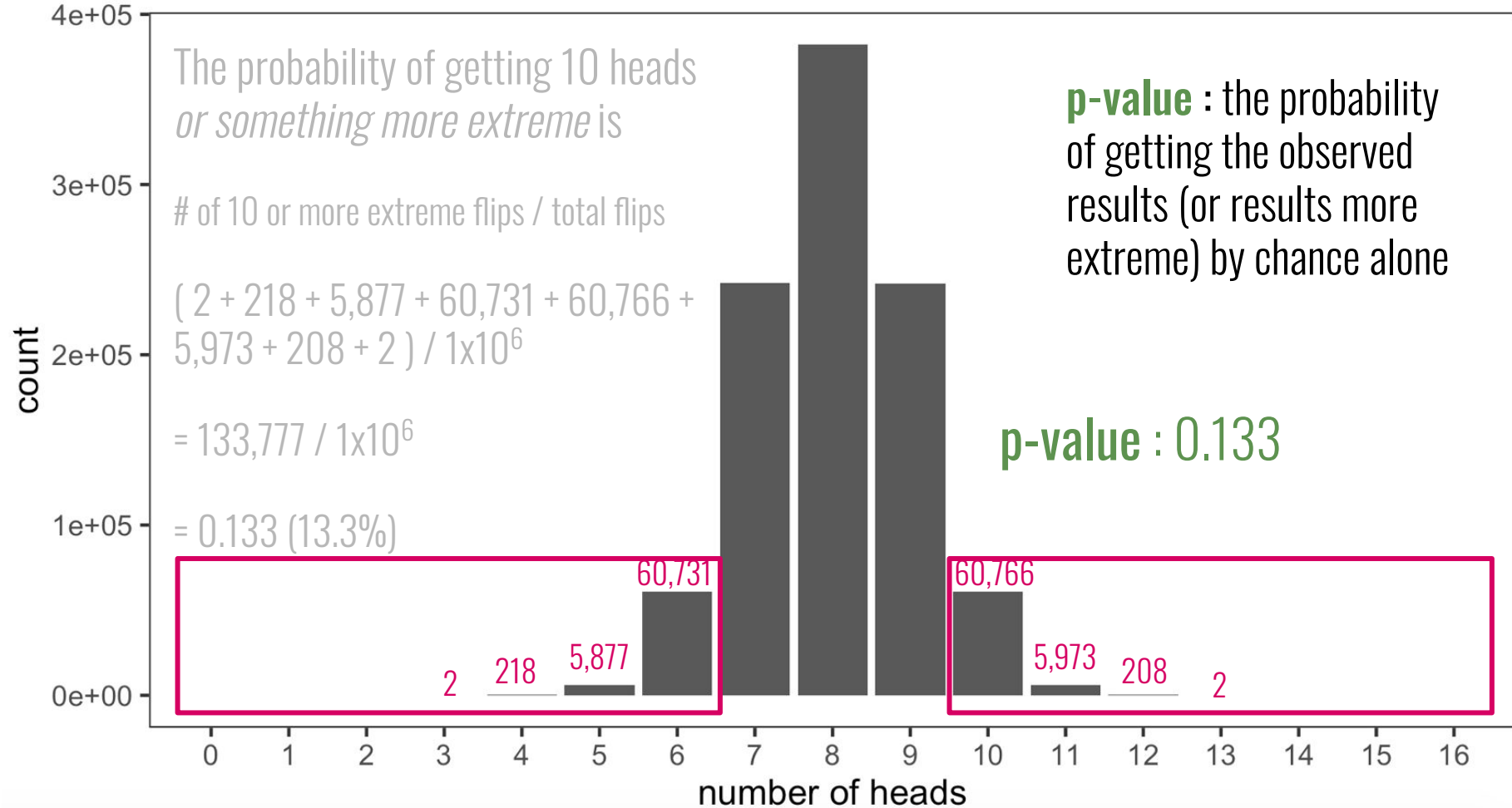


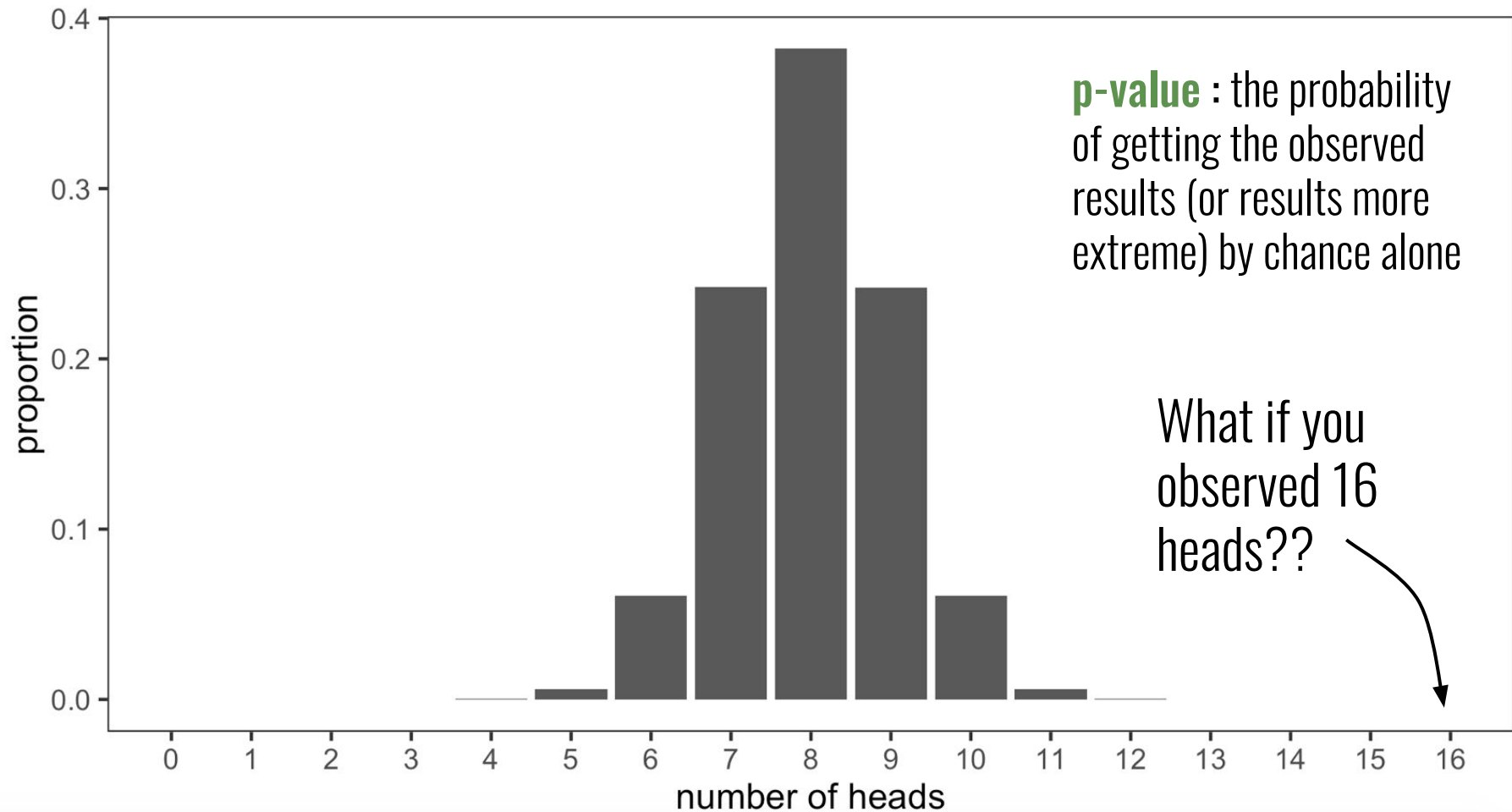


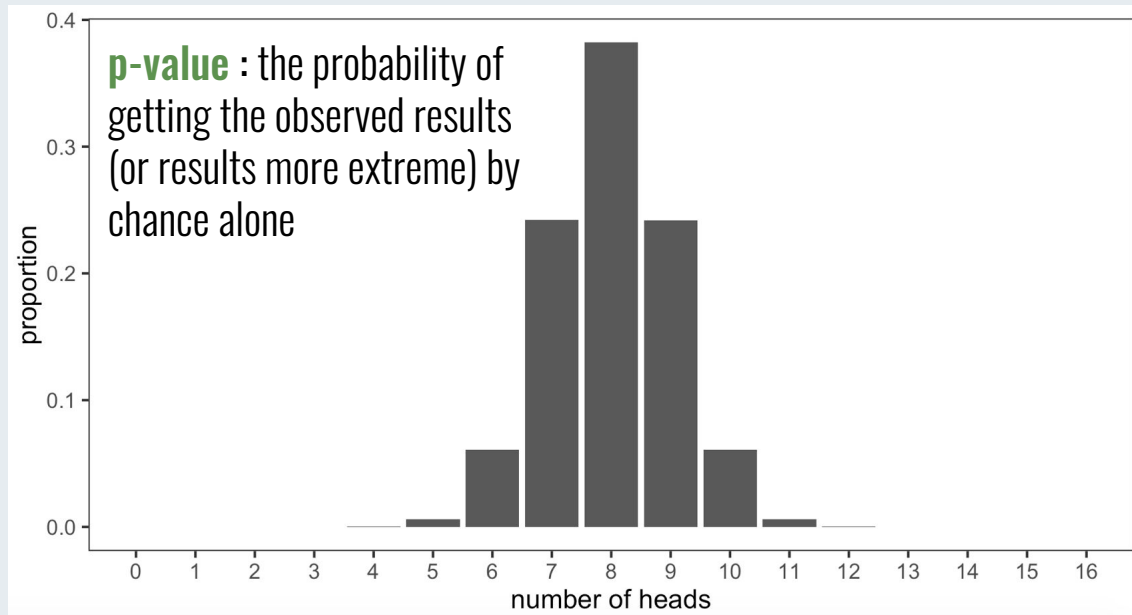




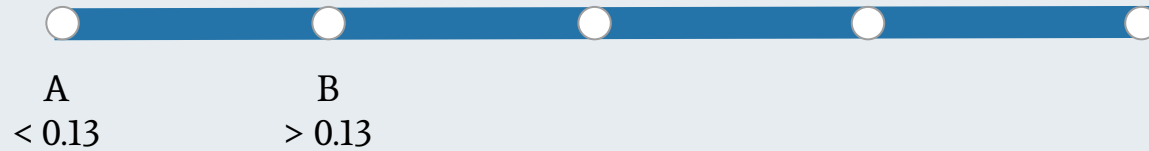


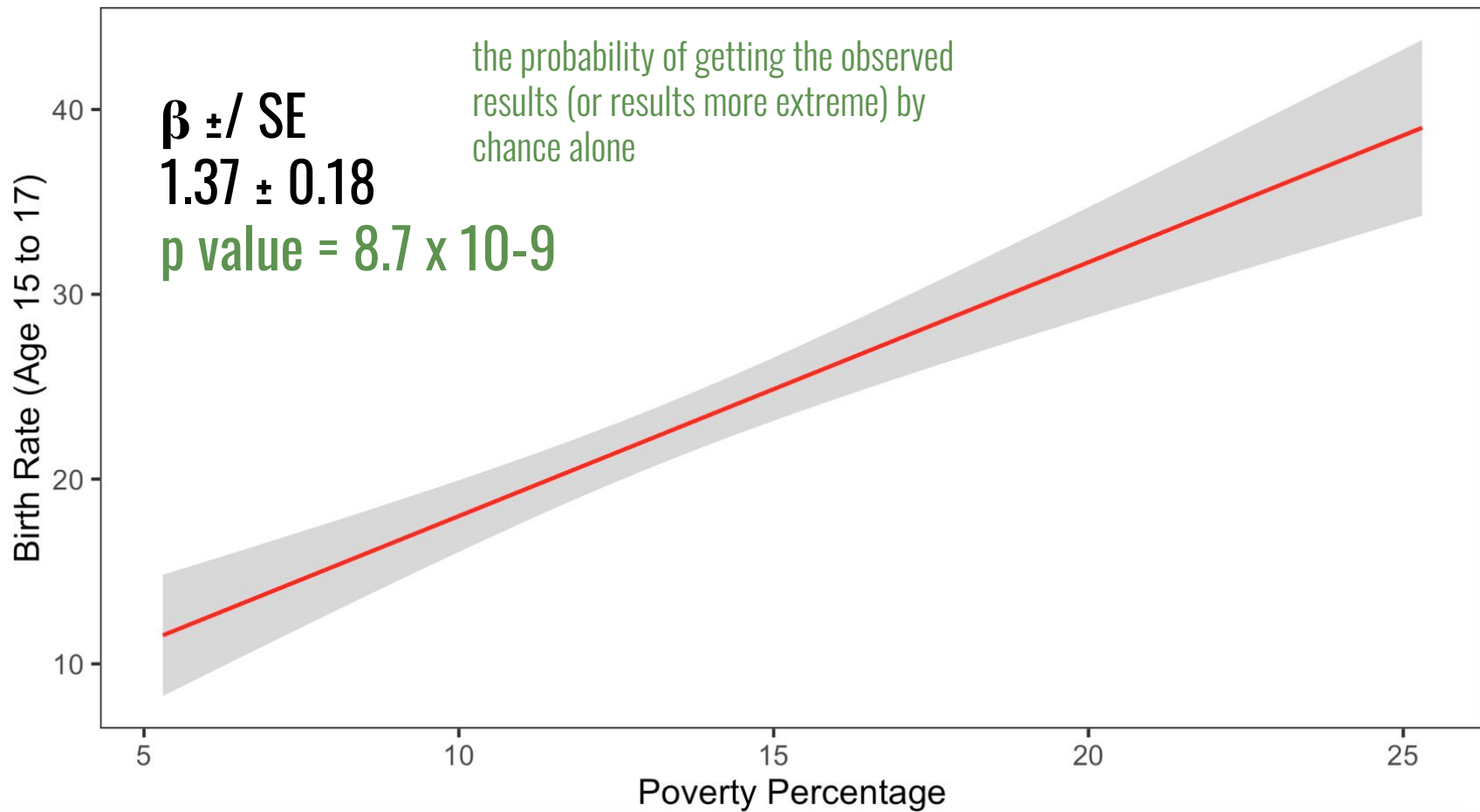




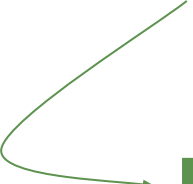


What would be the p-value of you flipping 16 heads?






Takes into account the
effect size (β) and the SE



p-value : the probability of getting the
observed results (or results more
extreme) by chance alone

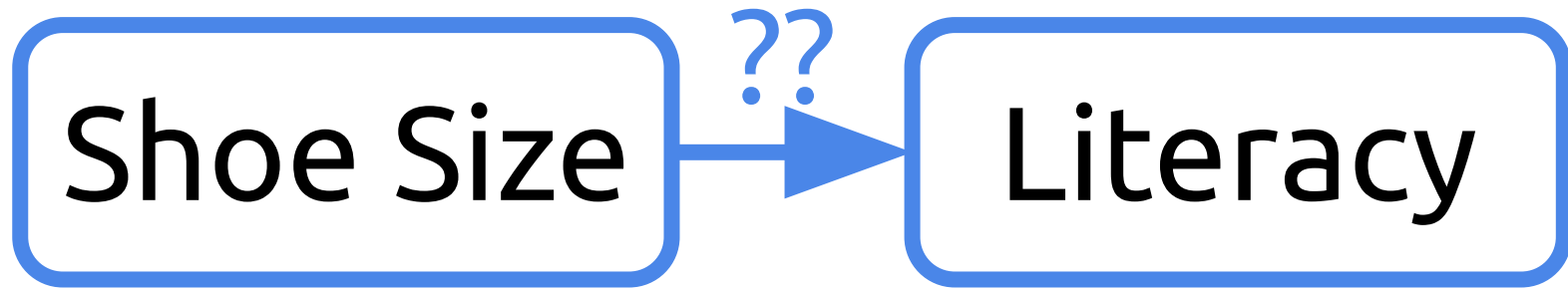
Confounding





Small shoes
Not literate

Big shoes
Literate





Small shoes
Not literate
Child

Big shoes
Literate
Adult

Shoe Size

Literacy

Age

```
graph TD; A[Shoe Size] --> C[Age]; B[Literacy] --> C;
```

The diagram illustrates a relationship where 'Shoe Size' and 'Literacy' are solid variables that point to a dashed variable 'Age'. The boxes for 'Shoe Size' and 'Literacy' are solid blue, while the box for 'Age' is dashed blue. Two blue arrows originate from the bottom of the 'Shoe Size' and 'Literacy' boxes and converge at the top of the 'Age' box.

Variable1

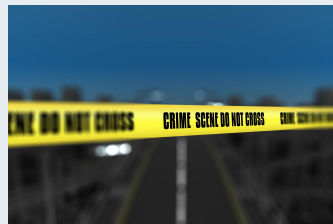
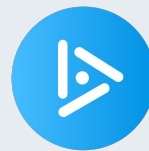
Variable2

Confounder

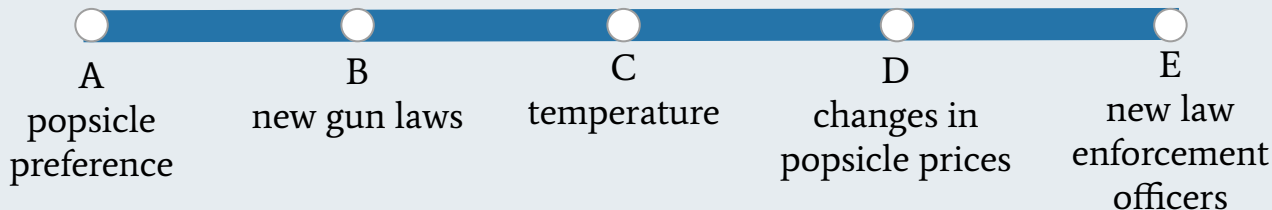
```
graph TD; V1[Variable1] --> C[Confounder]; V2[Variable2] --> C;
```

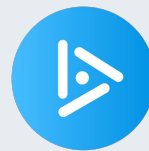
The diagram illustrates a causal relationship where two variables, Variable1 and Variable2, are influenced by a common factor, the Confounder. Variable1 and Variable2 are represented by solid blue boxes with rounded corners, while the Confounder is represented by a dashed blue box with rounded corners. Two blue arrows point from the bottom of Variable1 and Variable2 to the top of the Confounder box, indicating that the confounder is the common cause of both variables.

Confounding

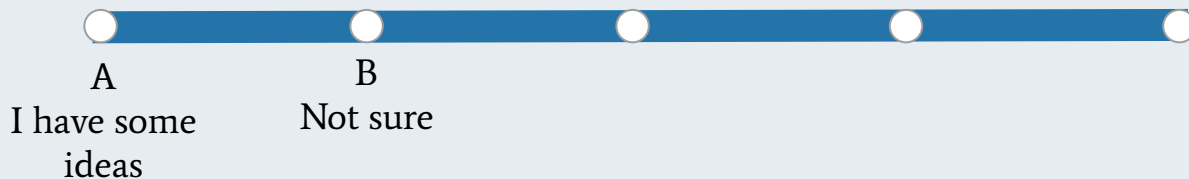


Your analysis sees an increase in crime rate whenever popsicle sales increase. What could confound this analysis?

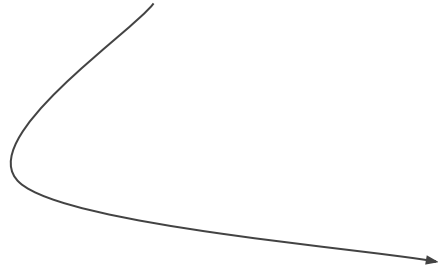




What are possible confounders for our analysis of the effect of poverty on teen birth rate?



We'll discuss additional approaches of how to account for confounding in your analysis in the next lecture.



Ignoring confounders will lead you to draw incorrect conclusions from your analyses

Spine Surgery Results

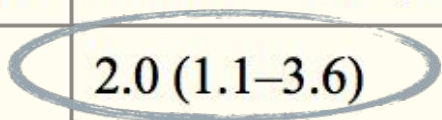
Sample: 400 patients with index vertebral fractures

| Vertebroplasty | Conservative care | Relative risk (95% confidence interval) |
|----------------|-------------------|---|
| 30/200 (15%) | 15/200 (7.5%) | 2.0 (1.1–3.6) |

subsequent fractures



Eek....looks like vertebroplasty was way worse for patients!



But wait...at time of initial fracture...

| | Vertebroplasty N = 200 | Conservative care N = 200 |
|---------------------------|---|--|
| Age, y, mean \pm SD | 78.2 \pm 4.1 | 79.0 \pm 5.2 |
| Weight, kg, mean \pm SD | 54.4 \pm 2.3 | 53.9 \pm 2.1 |
| Smoking status, No. (%) | 110 (55) | 16 (8) |

Age and weight are similar between groups. **Smoking Status** differs vastly.

So...let's stratify those results real quick

| Smoke | | | No smoke | | |
|----------------|--------------|------------------------------|----------------|--------------|------------------------------|
| Vertebroplasty | Conservative | RR (95% confidence interval) | Vertebroplasty | Conservative | RR (95% confidence interval) |
| 23/110 (21%) | 3/16 (19%) | 1.1 (0.4, 3.3) | 7/90 (8%) | 12/184(7%) | 1.2 (0.5, 2.9) |

Risk of re-fracture is now similar within group