WS 2015/16

# Examination Statistics Prof. Dr. E. Falkenberg Course of Study: Computer Sciences 3.6.2015

Name Matricula	tion Numbe	: <b>r</b> :									
I hereby co	onfirm that l	[ am	phy	ysica	lly 1	fit to	take	the ex	amination.		
Signature student											
	Problems	1	2	3	4	5	Sum	Mark	]		
	Max. scores	16	13	11	16	11	67		]		
	Obt. scores							1			

### Authorized examinations aids:

Scientific calculator, one english-german dictionary, one book and one file folder

### Further instructions:

- 1. Do not use your own paper. Blank paper is attached to this question paper. Extra sheets will be provided on demand.
- 2. Please notice, not only the solution but the deriviation of the solution has to be given.
- 3. You will be excluded from the exam if you
  - cooperate in any form with other participants;
  - keep your mobile phone switched on;
  - use a mobile phone, a notebook or any other similar electronic device;
  - use documents which are not allowed.
- 4. Switch off all electronic devices und remove them from the table.

Good Luck! Dr. Falkenberg 1. In the following table are the results of a survey of 25 students about the number of lent books from the universities library in a term.

number of lent books	no of students
0	5
1	5
2	3
3	2
4	2
5	2
6	2
7	1
8	1
9	1
10	1

- (a) Calculate the arithmetic mean, the modus, the median, the first quartil, the third quartil, the 90%-quantil and the standard deviation.
- (b) If you compare the values of the median and the arithmetic mean what can you say about the form of the distributions of the number of lent book.
- (c) Draw a box-plot.

- 2. The company Meyer Inc. uses in their machines a special electronic device. The company A delivers 80% of these devices, the company B delivers 15% of these devices and the company C delivers the remaining devices. The delivered devices from company are defect with rate 4%. In the deliveries of company B are 6% defect and in deliveries of company C are 9% defect.
  - (a) If a device is randomly selected from all delivered devices, find the probability that it is not defect.
  - (b) If a randomly selected device is then tested and is found to be defective, find the probability that it was delivered by the company A resp. B or C.
  - (c) If devices are randomly selected from all delivered devices, what is the probability that the tenth checked device is the second defect device?

- 3. In a medival market a dealer sells homemade pancakes. The dealer puts allways one scoop of his pastry in the pan for every pancake. The volume in the scoop differs from portion to portion. The volume is uniform distributed random variable V on the interval [190,210g].
  - (a) Determine E(V) and Var(V).
  - (b) Apply the central limit theorem to find an approximation of the distribution of the cumulated volume of pastry for 200 portion of pancakes.
  - (c) What is the approximated probability that the dealers pastry store of 40,25 kg is not sufficient for 200 sold pancakes?

- 4. A machine fills washing powder in 5 kg packages. The filled volume is a normaly distributed random variable A. During the fillings of the packages the expected value of A may change. The variance of A remains constant during the fillings of the packages. A worker takes a random sample of 100 packages. The  $1-\alpha=0.95\%$  confidence interval is [4.997kg, 5.0054kg].
  - (a) Determine the mean of the sample and the standard deviation of A.
  - (b) Calculate a 99%-confidence interval for the volume of a package.
  - (c) Calculate a 95%-upper confidence bound for the volume of a package.
  - (d) How many packages should the worker sample at least to get a 95%-confidence interval of a length less than 30g?

<u>Hint:</u> If you can not solve a) please use 5.01kg as the mean of the sample and 0.03 kg as standard deviation of A.

- 5. The well known politician Allgood candidates for the presidential chair. He supposes that the majority of the voters will vote him. In a random sample with 100 voters 60 voters would vote him. Is this sufficient evidence to support the Allgood's claim?
  - (a) State the null hypothesis.
  - (b) Give the appropriate test statistic.
  - (c) Use alpha of 0.005 to determine the rejection area.
  - (d) Find the p-value for the test.
  - (e) State your conclusions, and interpret your results.

Table of the Standard Normal Distribution N(0,1)

	?,?0	?,?1	?,?2	?,?3	?,?4	?,?5	?,?6	?,?7	?,?8	?,?9
0	0.500000	0.503989	0.507978	0.511966	0.515953	0.519939	0.523922	0.527903	0.531881	0.535856
0.1	0.539828	0.543795	0.547758	0.551717	0.555670	0.559618	0.563559	0.567495	0.571424	0.575345
0.2	0.579260	0.583166	0.587064	0.590954	0.594835	0.598706	0.602568	0.606420	0.610261	0.614092
0.3	0.617911	0.621720	0.625516	0.629300	0.633072	0.636831	0.640576	0.644309	0.648027	0.651732
0.4	0.655422	0.659097	0.662757	0.666402	0.670031	0.673645	0.677242	0.680822	0.684386	0.687933
0.5	0.691462	0.694974	0.698468	0.701944	0.705401	0.708840	0.712260	0.715661	0.719043	0.722405
0.6	0.725747	0.729069	0.732371	0.735653	0.738914	0.742154	0.745373	0.748571	0.751748	0.754903
0.7	0.758036	0.761148	0.764238	0.767305	0.770350	0.773373	0.776373	0.779350	0.782305	0.785236
0.8	0.788145	0.791030	0.793892	0.796731	0.799546	0.802337	0.805105	0.807850	0.810570	0.813267
0.9	0.815940	0.818589	0.821214	0.823814	0.826391	0.828944	0.831472	0.833977	0.836457	0.838913
1	0.841345	0.843752	0.846136	0.848495	0.850830	0.853141	0.855428	0.857690	0.859929	0.862143
1.1	0.864334	0.866500	0.868643	0.870762	0.872857	0.874928	0.876976	0.879000	0.881000	0.882977
1.2	0.884930	0.886861	0.888768	0.890651	0.892512	0.894350	0.896165	0.897958	0.899727	0.901475
1.3	0.903200	0.904902	0.906582	0.908241	0.909877	0.911492	0.913085	0.914657	0.916207	0.917736
1.4	0.919243	0.920730	0.922196	0.923641	0.925066	0.926471	0.927855	0.929219	0.930563	0.931888
1.5	0.933193	0.934478	0.935745	0.936992	0.938220	0.939429	0.940620	0.941792	0.942947	0.944083
1.6	0.945201	0.946301	0.947384	0.948449	0.949497	0.950529	0.951543	0.952540	0.953521	0.954486
1.7	0.955435	0.956367	0.957284	0.958185	0.959070	0.959941	0.960796	0.961636	0.962462	0.963273
1.8	0.964070	0.964852	0.965620	0.966375	0.967116	0.967843	0.968557	0.969258	0.969946	0.970621
1.9	0.971283	0.971933	0.972571	0.973197	0.973810	0.974412	0.975002	0.975581	0.976148	0.976705
2	0.977250	0.977784	0.978308	0.978822	0.979325	0.979818	0.980301	0.980774	0.981237	0.981691
2.1	0.982136	0.982571	0.982997	0.983414	0.983823	0.984222	0.984614	0.984997	0.985371	0.985738
2.2	0.986097	0.986447	0.986791	0.987126	0.987455	0.987776	0.988089	0.988396	0.988696	0.988989
2.3	0.989276	0.989556	0.989830	0.990097	0.990358	0.990613	0.990863	0.991106	0.991344	0.991576
2.4	0.991802	0.992024	0.992240	0.992451	0.992656	0.992857	0.993053	0.993244	0.993431	0.993613
2.5	0.993790	0.993963	0.994132	0.994297	0.994457	0.994614	0.994766	0.994915	0.995060	0.995201
2.6	0.995339	0.995473	0.995604	0.995731	0.995855	0.995975	0.996093	0.996207	0.996319	0.996427
2.7	0.996533	0.996636	0.996736	0.996833	0.996928	0.997020	0.997110	0.997197	0.997282	0.997365
2.8	0.997445	0.997523	0.997599	0.997673	0.997744	0.997814	0.997882	0.997948	0.998012	0.998074
2.9	0.998134	0.998193	0.998250	0.998305	0.998359	0.998411	0.998462	0.998511	0.998559	0.998605
3	0.998650	0.998694	0.998736	0.998777	0.998817	0.998856	0.998893	0.998930	0.998965	0.998999
3.1	0.999032	0.999065	0.999096	0.999126	0.999155	0.999184	0.999211	0.999238	0.999264	0.999289
3.2	0.999313	0.999336	0.999359	0.999381	0.999402	0.999423	0.999443	0.999462	0.999481	0.999499
3.3	0.999517	0.999534	0.999550	0.999566	0.999581	0.999596	0.999610	0.999624	0.999638	0.999651
3.4	0.999663	0.999675	0.999687	0.999698	0.999709	0.999720	0.999730	0.999740	0.999749	0.999758
3.5	0.999767	0.999776	0.999784	0.999792	0.999800	0.999807	0.999815	0.999822	0.999828	0.999835
3.6	0.999841	0.999847	0.999853	0.999858	0.999864	0.999869	0.999874	0.999879	0.999883	0.999888
3.7	0.999892	0.999896	0.999900	0.999904	0.999908	0.999912	0.999915	0.999918	0.999922	0.999925
3.8	0.999928	0.999931	0.999933	0.999936	0.999938	0.999941	0.999943	0.999946	0.999948	0.999950
3.9	0.999952	0.999954	0.999956	0.999958	0.999959	0.999961	0.999963	0.999964	0.999966	0.999967
4	0.999968	0.999970	0.999971	0.999972	0.999973	0.999974	0.999975	0.999976	0.999977	0.999978

# Quantiles of the Standard Normal Distribution $N(0,1)\ u_p$

	р	X	p	X	р	X
1	0.800	0.8416212	0.950	1.6448536	0.990	2.3263479
2	0.820	0.9153651	0.955	1.6953977	0.991	2.3656181
3	0.840	0.9944579	0.960	1.7506861	0.992	2.4089155
4	0.860	1.0803193	0.965	1.8119107	0.993	2.4572634
5	0.880	1.1749868	0.970	1.8807936	0.994	2.5121443
6	0.900	1.2815516	0.975	1.9599640	0.995	2.5758293
7	0.920	1.4050716	0.980	2.0537489	0.996	2.6520698
8	0.940	1.5547736	0.985	2.1700904	0.997	2.7477814
9	0.960	1.7506861	0.990	2.3263479	0.998	2.8781617
10	0.980	2.0537489	0.995	2.5758293	0.999	3.0902323

## Quantiles of the $t_n$ -Distribution $t_{n,p}$

	p=0.6	p = 0.65	p=0.7	p = 0.75	p = 0.8	p = 0.85	p=0.9	p = 0.95	p = 0.96	p = 0.97	p=0.975	p = 0.98	p=0.985	p = 0.99	p=0.995	p=0.999	p=0.9995
1	0.3249	0.5095	0.7265	1.0000	1.3764	1.9626	3.0777	6.3138	7.9158	10.5789	12.7062	15.8945	21.2049	31.8205	63.6567	318.3088	636.6192
2	0.2887	0.4447	0.6172	0.8165	1.0607	1.3862	1.8856	2.9200	3.3198	3.8964	4.3027	4.8487	5.6428	6.9646	9.9248	22.3271	31.5991
3	0.2767	0.4242	0.5844	0.7649	0.9785	1.2498	1.6377	2.3534	2.6054	2.9505	3.1824	3.4819	3.8960	4.5407	5.8409	10.2145	12.9240
4	0.2707	0.4142	0.5686	0.7407	0.9410	1.1896	1.5332	2.1318	2.3329	2.6008	2.7764	2.9985	3.2976	3.7469	4.6041	7.1732	8.6103
5	0.2672	0.4082	0.5594	0.7267	0.9195	1.1558	1.4759	2.0150	2.1910	2.4216	2.5706	2.7565	3.0029	3.3649	4.0321	5.8934	6.8688
6	0.2648	0.4043	0.5534	0.7176	0.9057	1.1342	1.4398	1.9432	2.1043	2.3133	2.4469	2.6122	2.8289	3.1427	3.7074	5.2076	5.9588
7	0.2632	0.4015	0.5491	0.7111	0.8960	1.1192	1.4149	1.8946	2.0460	2.2409	2.3646	2.5168	2.7146	2.9980	3.4995	4.7853	5.4079
8	0.2619	0.3995	0.5459	0.7064	0.8889	1.1081	1.3968	1.8595	2.0042	2.1892	2.3060	2.4490	2.6338	2.8965	3.3554	4.5008	5.0413
9	0.2610	0.3979	0.5435	0.7027	0.8834	1.0997	1.3830	1.8331	1.9727	2.1504	2.2622	2.3984	2.5738	2.8214	3.2498	4.2968	4.7809
10	0.2602	0.3966	0.5415	0.6998	0.8791	1.0931	1.3722	1.8125	1.9481	2.1202	2.2281	2.3593	2.5275	2.7638	3.1693	4.1437	4.5869
11	0.2596	0.3956	0.5399	0.6974	0.8755	1.0877	1.3634	1.7959	1.9284	2.0961	2.2010	2.3281	2.4907	2.7181	3.1058	4.0247	4.4370
12	0.2590	0.3947	0.5386	0.6955	0.8726	1.0832	1.3562	1.7823	1.9123	2.0764	2.1788	2.3027	2.4607	2.6810	3.0545	3.9296	4.3178
13	0.2586	0.3940	0.5375	0.6938	0.8702	1.0795	1.3502	1.7709	1.8989	2.0600	2.1604	2.2816	2.4358	2.6503	3.0123	3.8520	4.2208
14	0.2582	0.3933	0.5366	0.6924	0.8681	1.0763	1.3450	1.7613	1.8875	2.0462	2.1448	2.2638	2.4149	2.6245	2.9768	3.7874	4.1405
15	0.2579	0.3928	0.5357	0.6912	0.8662	1.0735	1.3406	1.7531	1.8777	2.0343	2.1314	2.2485	2.3970	2.6025	2.9467	3.7328	4.0728
16	0.2576	0.3923	0.5350	0.6901	0.8647	1.0711	1.3368	1.7459	1.8693	2.0240	2.1199	2.2354	2.3815	2.5835	2.9208	3.6862	4.0150
17	0.2573	0.3919	0.5344	0.6892	0.8633	1.0690	1.3334	1.7396	1.8619	2.0150	2.1098	2.2238	2.3681	2.5669	2.8982	3.6458	3.9651
18	0.2571	0.3915	0.5338	0.6884	0.8620	1.0672	1.3304	1.7341	1.8553	2.0071	2.1009	2.2137	2.3562	2.5524	2.8784	3.6105	3.9216
19	0.2569	0.3912	0.5333	0.6876	0.8610	1.0655	1.3277	1.7291	1.8495	2.0000	2.0930	2.2047	2.3456	2.5395	2.8609	3.5794	3.8834
20	0.2567	0.3909	0.5329	0.6870	0.8600	1.0640	1.3253	1.7247	1.8443	1.9937	2.0860	2.1967	2.3362	2.5280	2.8453	3.5518	3.8495
21	0.2566	0.3906	0.5325	0.6864	0.8591	1.0627	1.3232	1.7207	1.8397	1.9880	2.0796	2.1894	2.3278	2.5176	2.8314	3.5272	3.8193
22	0.2564	0.3904	0.5321	0.6858	0.8583	1.0614	1.3212	1.7171	1.8354	1.9829	2.0739	2.1829	2.3202	2.5083	2.8188	3.5050	3.7921
23	0.2563	0.3902	0.5317	0.6853	0.8575	1.0603	1.3195	1.7139	1.8316	1.9782	2.0687	2.1770	2.3132	2.4999	2.8073	3.4850	3.7676
24	0.2562	0.3900	0.5314	0.6848	0.8569	1.0593	1.3178	1.7109	1.8281	1.9740	2.0639	2.1715	2.3069	2.4922	2.7969	3.4668	3.7454
25	0.2561	0.3898	0.5312	0.6844	0.8562	1.0584	1.3163	1.7081	1.8248	1.9701	2.0595	2.1666	2.3011	2.4851	2.7874	3.4502	3.7251
26	0.2560	0.3896	0.5309	0.6840	0.8557	1.0575	1.3150	1.7056	1.8219	1.9665	2.0555	2.1620	2.2958	2.4786	2.7787	3.4350	3.7066
27	0.2559	0.3894	0.5306	0.6837	0.8551	1.0567	1.3137	1.7033	1.8191	1.9632	2.0518	2.1578	2.2909	2.4727	2.7707	3.4210	3.6896
28	0.2558	0.3893	0.5304	0.6834	0.8546	1.0560	1.3125	1.7011	1.8166	1.9601	2.0484	2.1539	2.2864	2.4671	2.7633	3.4082	3.6739
29	0.2557	0.3892	0.5302	0.6830	0.8542	1.0553	1.3114	1.6991	1.8142	1.9573	2.0452	2.1503	2.2822	2.4620	2.7564	3.3962	3.6594
30	0.2556	0.3890	0.5300	0.6828	0.8538	1.0547	1.3104	1.6973	1.8120	1.9546	2.0423	2.1470	2.2783	2.4573	2.7500	3.3852	3.6460
40	0.2550	0.3881	0.5286	0.6807	0.8507	1.0500	1.3031	1.6839	1.7963	1.9357	2.0211	2.1229	2.2503	2.4233	2.7045	3.3069	3.5510
50	0.2547	0.3875	0.5278	0.6794	0.8489	1.0473	1.2987	1.6759	1.7870	1.9244	2.0086	2.1087	2.2338	2.4033	2.6778	3.2614	3.4960
60	0.2545	0.3872	0.5272	0.6786	0.8477	1.0455	1.2958	1.6706	1.7808	1.9170	2.0003	2.0994	2.2229	2.3901	2.6603	3.2317	3.4602
70	0.2543	0.3869	0.5268	0.6780	0.8468	1.0442		1.6669	1.7765	1.9118	1.9944	2.0927	2.2152	2.3808	2.6479	3.2108	3.4350
80	0.2542	0.3867	0.5265	0.6776	0.8461	1.0432			1.7732	1.9078	1.9901	2.0878	2.2095	2.3739	2.6387	3.1953	3.4163
90	0.2541	0.3866	0.5263	0.6772	0.8456	1.0424		1.6620	1.7707	1.9048	1.9867	2.0839	2.2050	2.3685	2.6316	3.1833	3.4019
100	0.2540	0.3864	0.5261	0.6770	0.8452	1.0418	1.2901	1.6602	1.7687	1.9024	1.9840	2.0809	2.2015	2.3642	2.6259	3.1737	3.3905
200	0.2537	0.3859	0.5252	0.6757	0.8434	1.0391	1.2858	1.6525	1.7596	1.8915	1.9719	2.0672	2.1857	2.3451	2.6006	3.1315	3.3398
300	0.2536	0.3857	0.5250	0.6753	0.8428	1.0382	1.2844	1.6499	1.7566	1.8879	1.9679	2.0627	2.1805	2.3388	2.5923	3.1176	3.3233
400	0.2535	0.3856	0.5248	0.6751	0.8425	1.0378	1.2837	1.6487	1.7551	1.8861	1.9659	2.0605	2.1779	2.3357	2.5882	3.1107	3.3150
500	0.2535	0.3855	0.5247	0.6750	0.8423	1.0375	1.2832	1.6479	1.7543	1.8851	1.9647	2.0591	2.1763	2.3338	2.5857	3.1066	3.3101
$\infty$	0.2533	0.3853	0.5244	0.6745	0.8416	1.0364	1.2816	1.6449	1.7507	1.8808	1.9600	2.0537	2.1701	2.3263	2.5758	3.0902	3.2905

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# Quantiles of the $\chi_n^2$ -Distribution $\chi_{n,p}$

	p=0.005	p=0.01	p=0.015	p=0.02	p=0.025	p=0.05	p=0.1	p=0.5	p = 0.9	p=0.95	p=0.975	p=0.98	p=0.985	p=0.99	p=0.995
1	0.000	0.000	0.000	0.001	0.001	0.004	0.016	0.455	2.706	3.841	5.024	5.412	5.916	6.635	7.879
2	0.010	0.020	0.030	0.040	0.051	0.103	0.211	1.386	4.605	5.991	7.378	7.824	8.399	9.210	10.597
3	0.072	0.115	0.152	0.185	0.216	0.352	0.584	2.366	6.251	7.815	9.348	9.837	10.465	11.345	12.838
4	0.207	0.297	0.368	0.429	0.484	0.711	1.064	3.357	7.779	9.488	11.143	11.668	12.339	13.277	14.860
5	0.412	0.554	0.662	0.752	0.831	1.145	1.610	4.351	9.236	11.070	12.833	13.388	14.098	15.086	16.750
6	0.676	0.872	1.016	1.134	1.237	1.635	2.204	5.348	10.645		14.449	15.033	15.777	16.812	18.548
7	0.989	1.239	1.418	1.564	1.690	2.167	2.833	6.346	12.017		16.013	16.622	17.398	18.475	20.278
8	1.344	1.646	1.860	2.032	2.180	2.733	3.490	7.344	13.362		17.535	18.168	18.974	20.090	21.955
9	1.735	2.088	2.335	2.532	2.700	3.325	4.168	8.343		16.919	19.023	19.679	20.513	21.666	23.589
10	2.156	2.558	2.837	3.059	3.247	3.940	4.865		15.987		20.483	21.161	22.021	23.209	25.188
11	2.603	3.053	3.363	3.609	3.816	4.575	5.578				21.920		23.503	24.725	26.757
12	3.074	3.571	3.910	4.178	4.404	5.226	6.304				23.337	24.054	24.963	26.217	28.300
13	3.565	4.107	4.476	4.765	5.009	5.892	7.042				24.736	25.472	26.403	27.688	29.819
14	4.075	4.660	5.057	5.368	5.629	6.571	7.790		21.064		26.119	26.873	27.827	29.141	31.319
15	4.601	5.229	5.653	5.985	6.262	7.261	8.547	14.339	22.307	24.996	27.488	28.259	29.235	30.578	32.801
16	5.142	5.812	6.263	6.614	6.908	7.962	9.312		23.542		28.845	29.633	30.629	32.000	34.267
17	5.697	6.408	6.884	7.255	7.564	8.672	10.085			27.587	30.191	30.995	32.011	33.409	35.718
18	6.265	7.015	7.516	7.906	8.231	9.390	10.865		25.989	28.869	31.526	32.346	33.382	34.805	37.156
19	6.844	7.633	8.159	8.567	8.907	10.117	11.651		27.204	30.144	32.852	33.687	34.742	36.191	38.582
20	7.434	8.260	8.810	9.237	9.591	10.851	12.443		28.412		34.170	35.020	36.093	37.566	39.997
25	10.520		12.187	12.697	13.120	14.611	16.473		34.382	37.652	40.646	41.566	42.725	44.314	46.928
30	13.787		15.719	16.306	16.791	18.493	20.599		40.256	43.773	46.979	47.962	49.199	50.892	53.672
35	17.192		19.369	20.027	20.569	22.465	24.797		46.059	49.802	53.203	54.244	55.553	57.342	60.275
40	20.707	_	23.113	23.838	24.433	26.509	29.051	39.335	51.805	55.758	59.342	60.436	61.812	63.691	66.766
45	24.311		26.933		28.366	30.612	33.350		57.505	61.656	65.410		67.994	69.957	73.166
50	27.991		30.818	31.664	32.357	34.764	37.689	49.335	63.167	67.505	71.420	72.613	74.111	76.154	79.490
60	35.534		38.744		40.482	43.188	46.459		74.397	79.082	83.298	84.580	86.188		91.952
70	43.275	45.442	46.836		48.758	51.739	55.329	69.334			95.023			100.425	104.215
80	51.172		55.061		57.153	60.391	64.278			101.879		108.069			
90	59.196		63.394	64.635	65.647	69.126	73.291				118.136				
100	67.328		71.818	73.142	74.222	77.929	82.358				129.561				
110	75.550	78.458	80.318	81.723	82.867	86.792					140.917				
120	83.852		88.886	90.367							152.211				
130	92.222	000-	97.512								163.453				
140		104.034													
150											185.800				
160		121.346													
170		130.064													
180		138.820													
190		147.610													
200	152.241	156.432	159.096	161.100	162.728	168.279	174.835	199.334	$2\frac{2}{5}6.021$	233.994	241.058	243.187	245.845	249.445	255.264