

## Course of Study Bachelor Computer Science

# Exercises Statistics WS 2022/23

### **Sheet IX - Solutions**

### Two Samples Tests

1. Two machines produce screw-nuts. The diameters of the screw-nuts from machine 1 resp. 1 are normally distributed with standard deviation  $\sigma_1 = 0.5$  resp.  $\sigma_2 = 0.6$  and unknown means  $\mu_1$  resp  $\mu_2$ . Two sample are drawn:

M1: 5.46, 5.34, 4.34, 4.82, 4.4, 5.12, 5.69, 5.53, 4.77, 5.82

M2: 5.45, 5.31, 4.11, 4.69, 4.18, 5.05, 5.72, 5.54, 4.62, 5.89, 5.6, 5.19, 3.31, 4.43, 5.3, 4.09

Test the hypotheses  $\mu_1 \geq \mu_2$  at level  $\alpha = 0.05$ 

**Answer:** 2 sample Gauss test: no rejection since p-value = 0.152

2. To test two training methods A and B for javelin throw, 60 untrained physical education students were randomly divided into two groups of m=25 and n=35 students, respectively. Before the start of the training phase First, a performance test was conducted and for each student the distance of the best of two throws was noted. After completion of the training phase, during which the students in group 1 were method A and the students of group 2 were trained according to method B, was trained, a corresponding performance test was performed. The



following results were obtained for the differences between the values obtained in the second and the first performance test:

- Group 1: 7.06, 11.84, 9.28, 7.92, 13.5, 3.98, 3.82, 7.34, 8.7, 9.24, 4.86, 3.32, 12.78, 12, 5.24, 11.4, 6.56, 9.04, 7.72, 9.26, 7.88, 8.6, 9.3, 8.42, 8.54
- Group 2: 8.68, 6, 6.3, 10.24, 10.88, 5.36, 7.82, 4.7, 9.02, 9.78, 6.9, 5.8, 13.56, 10.32, 13.3, 11.38, 7.94, 10.74, 13.68, 14.92, 7.42, 10.36, 10.54, 5.22, 13.74, 12.98, 10.34, 10.02, 17.8, 13.04, 5.2, 9.4, 11.18, 12.68, 12.36

Which hypothesis do you have to test if you want to show that the Method B is better than Method A? Perform an corresponding test at the level  $\alpha = 0.05$ . Assume that the values obtained are a realization of independent in the group i  $N(\mu_i, \sigma_i^2)$ -distributed random variables (i=1,2).

**Answer:** 2 unpaired sample t-test resp Welsh test: reject  $H_0$ 

```
# Exercise: 2 sample t-test, Welsh-test
                                 infstat_2samples_testing_javelin_throw.R
  # 2 independent random variable with unknown but equal resp. not equal variances
# Aufgabensammlung Lehn: Nr. 128
# To test two training methods A and B for javelin throw, 60
# untrained physical education students were randomly divided into
# two groups of m=25 and n=35 students, respectively. Before the
# start of the training phase First, a performance test was conducted
# and for each student the distance of the best of two throws was
# noted. After completion of the training phase, during which the
# students in group 1 were method A and the students of group 2 were
# trained according to method B, was trained, a corresponding
# performance test was performed. The following results were obtained
# for the differences between the values obtained in the second and
# the first performance test:
x <- c(7.06.11.84 9.28 7.02 12.5 2.00 2.00 7.01
  # Aufgabensammlung Lehn: Nr. 128
  # for the differences between the values obtained in the second and # the first performance test: x \leftarrow c \ (7.06\,,11.84\,,9.28\,,7.92\,,13.5\,,3.98\,,3.82\,,7.34\,,8.7\,,9.24\,,4.86\,,3.32\,,\\ 12.78\,,12\,,5.24\,,11.4\,,6.56\,,9.04\,,7.72\,,9.26\,,7.88\,,8.6\,,9.3\,,8.42\,,8.54) y \leftarrow c \ (8.68\,,6\,,6\,,3\,,10.24\,,10.88\,,5.36\,,7.82\,,4.7\,,9.02\,,9.78\,,6.9\,,\\ 5.8\,,13.56\,,10.32\,,13.3\,,11.38\,,7.94\,,10.74\,,13.68\,,14.92\,,7.42\,,10.36\,,\\ 10.54\,,5.22\,,13.74\,,12.98\,,10.34\,,10.02\,,17.8\,,13.04\,,5.2\,,9.4\,,11.18\,,\\ 12.68\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.26\,,12.2
                                12.68,12.36)
  \# Which hypothesis do you have to test if you want to show that the \# Method B is better than Method A? Perform an corresponding test at \# the level alpha = 0.05.
  \# H0: mu.x >= mu.y, H1: mu.x < mu.y
  # case: equal
alpha <- 0.05
   t.test(x,y,alternative="less",mu=0,paired=FALSE,var.equal=TRUE,conf.level=1-alpha)
  # reject H0, since p-value = 0.0181
```



3. A (hypothetical) experiment is conducted on the effect of alcohol on perceptual motor ability. Ten subjects are each tested twice, once after having two drinks and once after having two glasses of water. The two tests were on two different days to give the alcohol a chance to wear off. Half of the subjects were given alcohol first and half were given water first. The scores of the 10 subjects are shown below. The first number for each subject is their performance in the "water" condition. Higher scores reflect better performance. Test to see if alcohol had a significant effect. Report the t and p values.

person	1, 2, 3, 4, 5, 6, 7, 8, 9, 10
water	16, 15, 11, 20, 19, 14, 13, 15, 14, 16
alcohol	13, 13, 10, 18, 17, 11, 10, 15, 11, 16

Assume that the values obtained are a realization of independent in the group i  $N(\mu_i, \sigma_i^2)$ -distributed random variables (i=1,2).

**Answer:** two paired sample t-test: reject H0

4. A company manager is considering whether to purchase a new type B scale on the market. A new acquisition should be made only if the type B scale is better than the type A scale used up to now. For the evaluation of the quality of a scale, the scatter of weighing results should be used. In weight measurements for one and the same weight the following results were obtained the following measured values for the individual scales:



Under suitable nomal distribution assumptions, check with a test with  $\alpha = 0.05$  to determine whether a new acquisition makes sense.

**Answer:** F-test: rejection of  $H_0: \sigma_A \leq \sigma_B$ 

5. On one farm, 10 cattle were fed (group 1) were fed concentrates of composition A, and the remaining 10 cattle (group 2) were fed the conventional conventional feed of composition B. After a certain time weight gain was noted in both groups:

- (a) Assuming that weight gain can be described by independent random variables that are identically normally distributed in both cases, use an appropriate test at level  $\alpha=0.1$  to test whether to reject the assumption that weight gain from administration of composition A concentrate has the same dispersion as weight gain from administration of the conventional composition B diet.
- (b) Assuming that weight gain can be described by independent random variables with equal variance, identically normally distributed in each of the two cases, use an appropriate test at the level  $\alpha=0.025$  to test whether the hypothesis that weight gain with administration of concentrate of composition A is not greater than weight gain with administration of the conventional diet of composition B is correct.

**Answer:** a) F-test: no rejection of  $H_0: \sigma_1 = \sigma_2$ , b) two unpaired sample t-test: rejection of  $H_0: \mu_1 \leq \mu_2$ 



```
Exercise: 2 unpaired sample t-test and F-test
# file: infstat_2samples_testing_cattle_feed.R
# Aufgabensammlung Lehn, Wegmann Aufgabe 130

# On one farm, 10 cattle were fed (group 1) were fed concentrates of

# composition A, and the remaining 10 cattle (group 2) were fed the

# conventional conventional feed of composition B. After a certain
# time weight gain was noted in both groups:
  \begin{array}{l} < < - \text{ c } (\,7.\,2\,,4.\,1\,,5.\,5\,,4.\,5\,,5.\,7\,,3.\,8\,,4.\,6\,,6.\,0\,,5.\,2\,,5.\,4) \\ < - \text{ c } (\,5.\,3\,,4.\,4\,,5.\,0\,,3.\,5\,,3.\,9\,,4.\,9\,,5.\,6\,,2.\,5\,,4.\,0\,,3.\,6) \end{array}
\# Assuming that weight gain can be described by independent \# random variables that are identically normally distributed in \# both cases, use an appropriate test at level alpha=0.1 to
# test whether to reject the assumption that weight gain from # administration of composition A concentrate has the same # dispersion as weight gain from administration of the # conventional composition B diet.
mean(x); var(x)
mean(y); var(y)
alpha <- 0.1
var.test(x,y,alternative="two.sided",conf.level=1-alpha)</pre>
# do not reject H0, that the variances are equal
# Assuming that weight gain can be described by independent # random variables with equal variance, identically normall
# random variables with equal variance, identically normally # distributed in each of the two cases, use an appropriate test at # the level alpha=0.05 to test whether the hypothesis that
# weight gain with administration of concentrate of composition A # is not greater than weight gain with administration of the # conventional diet of composition B is correct.
alpha <- 0.025
t.test(x,y,alternative="greater",paired=FALSE,var.equal=TRUE,conf.level=1-alpha)
# reject H0, that the mu.x < mu.y since p-value = 0.0181
```

#### 6. Heumann, Schoemaker Aufgabe 10.5

A company producing clothing often finds deficient T-shirts among its production.

- (a) The company's controlling department decides that the production is no longer profitable when there are more than 10% deficient T-shirts. A sample of 230 shirts yield 32 shirts which contain deficiencies. Use the approximate binomial test and the exact binomial test to decide whether the shirt production is profitable or not ( $\alpha = 0.05$ ).
- (b) The company is offered a new cutting machine. To test whether the change of machine helps to improve the production quality, 115 sample T-shirts are evaluated, 7 of which have deficiencies. Use the 2 sample binomial test to decide whether the new machine yields improvement or not ( $\alpha = 0.5$ )

**Answer:** one sample binomial test and its approximation two sample tests on p: Fisher's exact test and its approximation



```
# file: infstat_2samples_testing_tshirts.R
 <del>Ä</del>
 # Heumann, Schoemaker Aufgabe 10.5
\# A company producing clothing often finds deficient T-shirts among \# its production. \# The company's controlling department decides that the production is no longer \# profitable when there are more than 10% deficient T-shirts. A sample of 230 \# shirts yield 35 shirts which contain deficiencies. Use the approximate \# binomial test and the exact binomial test to decide whether the shirt \# production is profitable or not (alpha=0.05). n < -230; def < -31
# H0: p \le 0.1, H1: p > 0.1

p0 < -0.1; r < -def/n

# one sample test for p: normal approximation

# test statistics

t.x < -(r-p0)/sqrt(p0*(1-p0)/n)
 # decision: reject H0, if t.x > 1-alpha quantile of the N(0,1)-distr. alpha <- 0.05 t.x > quantile of the N(0,1)-distr. # rejection of M2
  # rejection of HO
\# one sample test for p: exact binomial test binom.test(x = def, n = n, p = p0, alternative = "greater", conf.level = 1-alpha) qbinom(1-alpha, size = n, prob = p0) \# 95% quantile of B(n,p0) is 31 \# no rejection of H0, since p-value = 0.05414 \# Since the exact binomial test is more precise than the approximate binomial \# test , we follow the result of the exact binomial test.
\# The company is offered a new cutting machine. To test whether the change of \# machine helps to improve the production quality, 115 sample T-shirts are \# evaluated, 7 of which have deficiencies. Use the 2 sample binomial test to \# decide whether the new machine yields improvement or not (alpha =0.5)
 phat <- (def1+def2)/(n1+n2)
 \# H0: p2 >= p1, H1: p2 < p1
 # two sample test for p: normal approximation
# two sample very the sample with the sample very the very the
 # two sample test for p: fisher's exact test
# contingency table: machine2 machine1
# def 7 31
                                                                                                                                \frac{7}{109}
                                                                                                                                                          199
                                                                                          ok
  , conf.level = 1-alpha)
 \# rejection of H0, since p-value = 0.02465
```

7. In 380 randomly selected families with four children each it is investigated how many of them are girls. The result is the following findings:

Number of girls	families
0	25
1	95
2	150
3	80
4	30

Does this finding correspond to the hypothesis that the variable "number of girls in families with four children each" follows a Binomial dis-



tribution with n = 4 and p = 0.5? Test this hypothesis at a significance level of 0.1!

**Answer:**  $\chi^2$  goodness of fit test: do not reject Ho

8. The hypothesis is to be tested that the height of adult of adult German men is normally distributed (significance level 10%). For this purpose, a random sample is collected, which leads to the following findings:

class	frequency
150 to 155	20
155  to  160	30
160  to  165	55
165  to  170	60
170  to  175	85
175  to  180	80
180 to 185	50
185 to 190	40
190 to 195	30
195  to  200	15
200  to  205	10

What is the test decision?

**Answer:**  $\chi^2$  goodness of fit test: rejection



```
mid = 0.5*(from+to)
)
results
# estimation of mean and sd
est.mean <- mean(rep(x=results$mid,times=results$no))
est.sd <- sd(rep(x=results$mid,times=results$no))

# expected number of observation
est.p <- pnorm(results$from, mean = est.mean, sd = est.sd) -
pnorm(results$from, mean = est.mean, sd = est.sd)
est.no <- est.p * sum(results$no)

# H0: no normally distributed
chi2 <- sum((results$no-est.no)^2/est.no)
# decision: reject H0, if chi^2 (1-alpha) quantile of chi^2
# distribution with k = number of classes - 2 -1
chi2 > qchisq(1-0.1, df = length(results$from)-2-1)
1-pchisq(chi2, df = length(results$from)-2-1)
# reject H0, since p-value = 0.0598
```

9. Some parents of the West Bay little leaguers think that they are noticing a pattern. There seems to be a relationship between the number on the kids' jerseys and their position. These parents decide to record what they see. The hypothetical data appear below. Conduct a Chi Square test to determine if the parents' suspicion that there is a relationship between jersey number and position is right.

	Infield	Outfield	Pitcher	Total
0-9	12	5	5	22
10-19	5	10	2	17
20+	4	4	7	15
Total	21	19	14	54

**Answer:**  $\chi^2$  test: association two qualitative variables, reject at the 5% level



```
\# decision: reject H0, if chi^2 > (1-alpha) quantile of chi^2 \# distribution with k=(3-1)(3-1)=4 res%statistic > qchisq (0.95, df=4) \# reject H0, since p-value = 0.03679 1-pchisq (10.22573, df=4)
```

10. Two therapies for a specific febrile illness are to be be compared. For this purpose, 4 and 6 randomly selected randomly selected patients and the duration of treatment in hours required for the patient to be necessary for the patient to be free of fever.

Therapie 1	Therapie 2		
X	Y		
89,75	89		
94,5	91		
98,75	94		
101,5	96,75		
	99,5		
	101,25		

It is assumed that the given measured values are a realization of of independent random variables  $X_1, ..., X_4, Y_1, ..., Y_6$  and these random variables and these random variables have the continuous distribution function F and G, respectively. Test the hypothesis  $H_0: F = G$  at the level  $\alpha = 0.05$  by applying an appropriate nonparametric test.

#### Answer: Wilcoxon-Mann-Whitney U Test: no rejection



- 11. **Heumann, Schoemaker Aufgabe 10.3** Christian decide to purchase the new CD Bruce Springsteen. His first thought is to buy it online, via an online auction. He discovers that he can also buy the CD, without bidding at an auction, from the same online store. He also looks at the price at an internet book staore which was recommended to him by a friend. He notes down the following prices in Euro.
  - Internet book store: 16.95
  - Online store, no auction:
    18.19, 16.98, 19.97, 16.98, 18.19, 15.99, 13.79, 15.90, 15.90, 15.90, 15.90, 17.72
  - Online store, auction:
    10.50, 12.00, 9.54, 10.55, 11.99, 9.30, 10.59, 10.50, 10.01, 11.89,
    11.03, 9.52, 15.49, 11.02
  - (a) Calculate and interpret the arithmetic mean, variance, standard deviation and the coefficient of variation for the online, both for the auction and non-auction.
  - (b) Test the hypothesis that the mean price at the online store (no auction) is unequal 16.95 Euro ( $\alpha = 0.05$ ).
  - (c) Calculate a confidence interval for the mean price at the online store (no auction) and interpret your findings in the light of the hypothesis in b).
  - (d) Test the hypothesis that the mean price at the online store (auction) is less than 16.95 Euro ( $\alpha = 0.05$ ).
  - (e) Test the hypothesis that the mean non-auction price is higher than the mean auction price. Assume (i) that the variances are equal in both samples and (ii) that the varainces are unequal.
  - (f) Test the hypothesis that the variance of the non auction-price is unequal to the variance of the auction price ( $\alpha = 0.05$ ).



(g) Use the Wilcoxon-Mann-Whitney U-test to compare the location of the auction and non-auction prices.

**Answer:** 1 sample t-test, 2 sample t-test, Welsh test, F-test, Wilcoxon-Mann-Whitney U-test

```
1 sample t-test , 2 sample t-test , Welsh test , F-test Wilcoxon-Mann-Whitney U-test
      Exercise:
                         infstat_2samples_testing_bookstore.R
 library (tidyverse)
 # Heumann, Schoemaker Aufgabe 10.3
# Heumann, Schoemaker Aufgabe 10.3
# Christian decide to purchase the new CD Bruce Springstee. His
# first thought is to buy it online, via an online auction. He
# discovers that he can also buy the CD, without bidding at an
# auction, from the same online store. He also looks at the price at
# an internet book staore which was recommended to him by a
# friend. He notes down the following prices in Euro.
 \begin{array}{l} ibs < & -16.95 \\ os < & -tibble\,(noa = c\,(18.19\,,\ 16.98\,,\ 19.97\,,\ 16.98\,,\ 18.19\,,\ 15.99\,,\ 13.79\,,\ NA, \\ & & 15.90\,,\ 15.90\,,\ 15.90\,,\ 15.90\,,\ 19.97\,,\ 17.72\,)\,, \\ auc = c\,(10.50\,,\ 12.00\,,\ 9.54\,,\ 10.55\,,\ 11.99\,,\ 9.30\,,\ 10.59\,,\ 10.50 \\ & & 10.01\,,\ 11.89\,,\ 11.03\,,\ 9.52\,,\ 15.49\,,\ 11.02\,) \\ \end{array} 
                                                                                                                                                                                                        10.59, 10.50,
 # Calculate and interpret the the arithmetic mean, variance,
# standard deviation and the coefficient of variation for the the
 # online, both for the auction and non-auction os %% summarise(
os %% summarise(
mean.noa = mean(noa, na.rm = TRUE), mean.auc = mean(auc, na.rm = TRUE),
var.noa = var(noa, na.rm = TRUE), var.auc = var(auc, na.rm = TRUE),
sd.noa = sd(noa, na.rm = TRUE), sd.auc = sd(auc, na.rm = TRUE),
var.coeff.noa = sd.noa/mean.noa, var.coeff.auc = sd.auc/mean.auc)
# It seems to be evident, that the mean auction prices are lower than mean non-
# auction prices. But the auction prices show a higher variability to the mean
# for the auction prices
 \# Test the hypothesis that the mean price at the online store \# (no auction) is unequal 16.95 Euro (alpha = 0.05).
  alpha <- 0.05
 # One Sample t-\text{test}: t=0.16237, t=0
 # Calculate a confidence interval for the mean price at the # online store (no auction) and interpret your findings in the # light of the hypothesis in b).
 # 95 percent confidence interval:
                                                                                                                  15.96603 18.09243
\# Test the hypothesis that the mean price at the online store \# (auction) is less than 16.95 Euro (alpha=0.05). t.test(x = os$auc, alternative = "less", mu = ibs, conf.level = 1-alpha) \# One Sample t-test: t = -14.203, df = 13, p-value = 1.352e-09 \# conclusion: the mean auction prices are lower than the price from the
  # book store
 # Test the hypothesis that the mean non-auction price is
# higher than the mean auction price. Assume (i) that the
# variances are equal in both samples and (ii) that the varainces
 # are unequal.
# 1) not equal variances

t.test(x = os$noa, y = os$auc, alternative = "greater", paired = FALSE,
var.equal = FALSE, conf.level = 1-alpha)

# Welch Two Sample t-test: 9.3792, df = 24.123, p-value = 8.066e-10
 # conclusion: same as before
 # Test the hypothesis that the variance of the non
 # auction-price is unequal to the variance of the auction price # (alpha=0.05).
 # (alpha=0.05). var.test(x = os$noa, y = os$auc, alternative = "two.sided", conf.level = 1-alpha) # F test to compare two variances: F = 1.2577, num df = 12, denom df = 13, p-value = 0.6856
```



```
\# conclusion: no evidence, that the variances are different; this justifies the \# use of 2 sample t.test with equal variances. In practice, it is best to use the \# Welsh-test rather than the t-test \# Use the Wilcoxon-Mann-Whitney U-test to compare the location \# of the auction and non-auction prices. wilcox.test(x = os$noa, y = os$auc, conf.level = 1-alpha) \# Wilcoxon rank sum test with continuity correction: W = 181, p-value = 1.347e-05 \# conclusion: the locations are shifted
```

#### 12. Heumann, Schoemaker Aufgabe 10.6

Two friends play a computer game and each of them repeats the same level 10 times. The score obtained are:

	1	2	3	4	5	6	7	8	9	10
Player 1	91	101	112	99	108	88	99	105	111	104
Player 2	261	47	40	29	64	6	87	47	98	351

- (a) Player 2 insists that he is a better player and suggests to compare their performance. Use an appropriate test ( $\alpha=0.05$ ) to test this hypothesis.
- (b) Player 1 insists that he is a better player. He propose to not focus on the mean and to use the Wlicoxon-Mann-Whitney Utest for comparison ( $\alpha = 00.5$ ). What are the advantages and disadvantages of using this test compared with a)?

#### **Answer:** Welsh test, Wilcoxon-Mann-Whitney U-test



```
# not met, it makes no sense to use a t-test. Moreover, because the # distribution is skewed the mean may not be a sensible measure of # comparison. A drawback of the U-test is that it uses only the ranks and # not the raw data: it thus uses less informaton than the t-test, # which would be preferred when comparing means of a reasonably sized sample.
```

#### 13. Heumann, Schoemaker Aufgabe 10.8

The passengers rescued from the titanic depending on the travel classes is given in the following table

	1. Class	2. Class	3. Class	Staff	Total
Rescued	202	125	180	211	718
Not rescued	135	160	541	674	1510

Check with an appropriate test whether the "rescue status" and the "travel class" are independent and whether the conditional probabilities of "rescue status" given "travel class" differ by "travel class".

#### **Answer:** $\chi^2$ homogeneity and independence test