

# LE-128/715

## Segona prova

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# Continguts

1. Historial acadèmic i professional
2. Pla de treball
3. Lliçó

# Historial acadèmic i professional

# Educació

- 2008 - 2011    Diplomatura d'estadística  
UPC
- 2011 - 2013    Màster en estadística i IO (MEIO)  
UPC-UB
- 2013 - 2018    MS, PhD in Statistical Science  
Duke University  
Advisor: James O. Berger

# Trajectòria professional

2018 - 2022   Assistant Professor in Statistics  
Zicklin School of Business  
The City University of New York

2022 - present   Becari María Zambrano  
UPC

# Transferència de coneixement

- ▶ Consultoria: Takata (amb David Banks a Duke), SYMYB (amb Xavier Tort-Martorell)
- ▶ Formació a empreses: ORICA (amb Xavier Tort-Martorell i Lluís Marco)

# Pla de treball

# Docència

- ▶ Més de 8 anys d'experiència entre doctorat, assistant professor i becari
- ▶ Estudiantat divers: des d'estudiants d'escola de negocis fins a CFIS, des d'estudiants de primer de grau fins a doctorat
- ▶ Assignatures diverses: estadística bàsica, multivariant, R, bayesiana, disseny, modelització, inferència, etc.
- ▶ Docència en anglès i català



# Recerca

**Especialitat:** teoria i mètodes bayesians

- ▶ Proves d'hipòtesi i selecció de variables
- ▶ Mètodes no paramètrics bayesians
- ▶ Sèries temporals
- ▶ Disseny i anàlisi d'experiments
- ▶ Altres: privacitat, optimització, computació i fonaments

# Proves d'hipòtesi i selecció de variables

- ▶ Peña, V. & Barrientos, A.F. Differentially private methods for managing model uncertainty in linear regression models. **JMLR**.
- ▶ Peña, V. & Barrientos, A.F. (2023) Differentially Private Hypothesis Testing with the Subsampled and Aggregated Randomized Response Mechanism. **Statistica Sinica**.
- ▶ Mulder, J., Berger, J. O., Peña, V., & Bayarri, M. J. (2021). On the prevalence of information inconsistency in normal linear models. **TEST**.
- ▶ Peña, V. & Berger J.O. (2020). Restricted type II maximum likelihood priors on regression coefficients. **Bayesian Analysis**.

# Mètodes no paramètrics bayesians

- ▶ Jauch, M., Barrientos, A. F., Peña, V. & Matteson, D. Mixture representations and Bayesian nonparametric inference for likelihood ratio ordered distributions. **Submitted to Bayesian Analysis.**
- ▶ Barrientos, A. F. & Peña, V. (2020). Bayesian bootstraps for massive datasets. **Bayesian Analysis.**

# Sèries temporals

- ▶ Peña, V., & Irie, K. (2022). On the Relationship between Uhlig Extended and beta-Bartlett Processes. **Journal of Time Series Analysis**.
- ▶ Investigació concurrent i futura amb Kaoru Irie (Universitat de Tokyo): models dinàmics multivariants per a matrius de covariàncies

# Disseny i anàlisi d'experiments

- ▶ Attolini, C. S. O., Peña, V., & Rossell, D. (2015). Designing alternative splicing RNA-seq studies. Beyond generic guidelines. **Bioinformatics**.
- ▶ Investigació concurrent i futura amb Gonzalo García-Donato (Universidad de Castilla y la Mancha): anàlisi de dissenys factorials fraccionals

# Altres

- ▶ Guo, Q., Barrientos, A.F. & Peña, V. Differentially Private Methods for Compositional Data. **Submitted to JCGS.**
- ▶ Jauch, M. & Peña, V. (2016). Bayesian optimization with shape constraints. **NIPS Workshop on Bayesian Optimization.**
- ▶ Peña, V. & Berger, J. O. A note on recent criticisms to Birnbaum's theorem. *arXiv:1711.08093*.
- ▶ Investigació sobre mètodes computacionals per a la distribució GIG i estimació amb SURE amb Michael Jauch (FSU)

# Finançament

- ▶ A CUNY: finançament intern pels estius i un projecte de recerca.
- ▶ Projecte del ministeri: “Métodos Bayesianos para la selección de variables en problemas de alta dimensionalidad y con datos perdidos” amb Gonzalo García-Donato (UCLM), Maria Eugenia Castellanos (URJC), Alicia Quirós (León), Stefano Cabras (UC3M) i Anabel Forte (UV)
- ▶ Presentarem proposta per la nova convocatòria de l'AEI (gener 2024)

Lliçó



## $p$ -values vs $P(H_0 \mid \text{data})$

- ▶ In introductory statistics classes, you learned that the  $p$ -value is not  $P(H_0 \mid \text{data})$ .
- ▶ In Bayesian statistics, we can compute  $P(H_0 \mid \text{data})$ .

### Question

How similar is  $P(H_0 \mid \text{data})$  to the  $p$ -value?

# Testing a point null: normal mean

- ▶ We observe  $X_i \stackrel{\text{iid}}{\sim} N(\mu, \sigma^2)$  for  $i \in \{1, 2, \dots, n\}$  with  $\sigma^2$  known.
- ▶ We want to do the hypothesis test

$$H_0 : \mu = \mu_0 \qquad H_1 : \mu \neq \mu_0$$

for a fixed  $\mu_0$ .

# Non-Bayesian solution: $z$ -test

- ▶ From a non-Bayesian perspective, we can do a  $z$ -test.
- ▶ If  $\Phi$  is the cdf of the  $N(0, 1)$  distribution and  $z = \sqrt{n}(\sum_{i=1}^n x_i/n - \mu_0)/\sigma$ , the  $p$ -value is

$$2[1 - \Phi(|z|)] = 2[1 - \text{pnorm}(\text{abs}(z))].$$

- ▶ If we reject  $H_0$  whenever the  $p$ -value is less than  $\alpha$ , then

$$P_{H_0}(\text{reject } H_0) = \alpha.$$

# Bayesian solution

- ▶ All unknowns have probability distributions.
- ▶ Need to specify  $P(H_0)$  and  $P(H_1)$ .
- ▶ Under  $H_0$ , we know that  $\mu = \mu_0$ .
- ▶ Under  $H_1$ , we know that  $\mu \neq \mu_0$ , but we don't know the value of  $\mu$  exactly: we need to specify a prior  $f(\mu \mid H_1)$ .

# Bayes theorem

Applying Bayes theorem, we can find

$$P(H_0 \mid x_{1:n}) = \frac{P(H_0)f(x_{1:n} \mid H_0)}{P(H_0)f(x_{1:n} \mid H_0) + P(H_1)f(x_{1:n} \mid H_1)}$$

$$f(x_{1:n} \mid H_0) = \prod_{i=1}^n N(x_i \mid \mu_0, \sigma^2)$$

$$f(x_{1:n} \mid H_1) = \underbrace{\int_{\mathbb{R}} \prod_{i=1}^n N(x_i \mid \mu, \sigma^2) f(\mu \mid H_1) \, d\mu}_{f(x_{1:n}, \mu \mid H_1)}$$

# How to choose priors?

- ▶ How to choose  $P(H_0)$  and  $P(H_1)$ ?
  - ▶ In the absence of prior information, we can choose  $P(H_0) = P(H_1) = 1/2$ .

- ▶ How to choose  $f(\mu | H_1)$ ?

- ▶ Use a default prior: for example,

$$\mu | H_1 \sim N(\mu_0, \sigma^2) \quad (\text{unit information prior})$$

- ▶ We can also consider robust Bayes.

# Robust Bayes

- ▶ Instead of considering one prior, consider a class of priors  $\Gamma$ .
- ▶ Find  $\min_{\Gamma} P(H_0 \mid x_{1:n})$ : worst case for  $H_0$ .
- ▶ Following Berger and Sellke (1987), we will consider:

$$\Gamma_A = \{\text{all distributions}\}$$

$$\Gamma_S = \{\text{all distributions symmetric about } \mu_0\}.$$

$p$ -values are not  $P(H_0 \mid x_{1:n})$

- ▶ Robust Bayes is *aggressive* against  $H_0$ : we're picking the worst possible case over a class of priors.
- ▶ However, we'll see that

$$\min_{\Gamma} P(H_0 \mid x_{1:n}) \geq p\text{-value}.$$

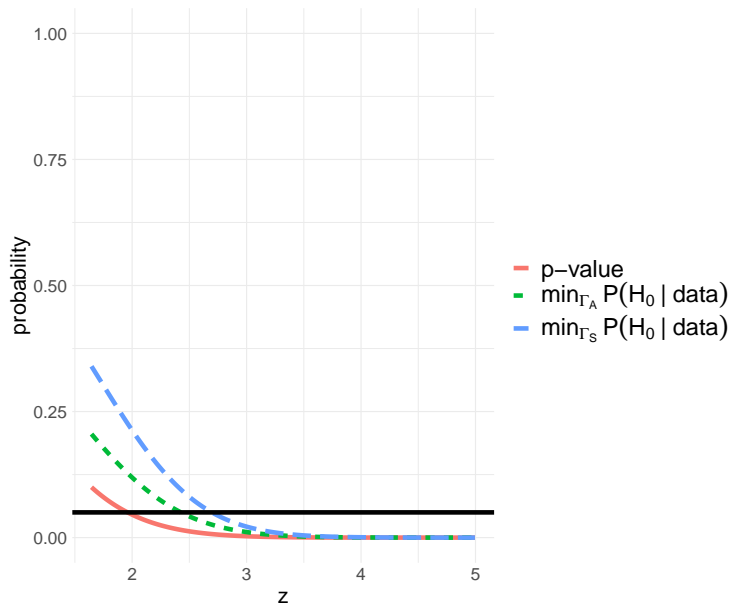
- ▶ Interpreting a  $p$ -value as  $P(H_0 \mid x_{1:n})$  overestimates evidence against  $H_0$ .



# Results: Table

$z$	$p$ -value	$\min \Gamma_A$	$\min \Gamma_S$
1.645	0.100	0.205	0.340
1.960	0.050	0.128	0.227
2.576	0.010	0.035	0.068
3.291	0.001	0.004	0.009

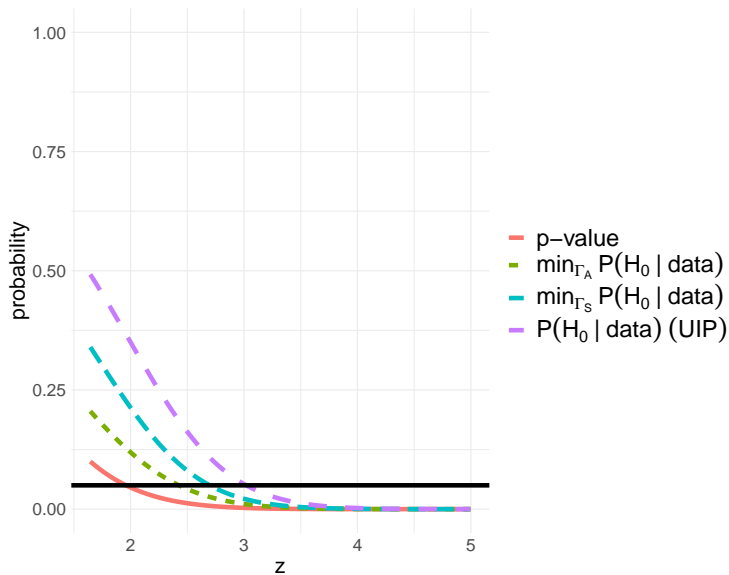
# Results: Plot



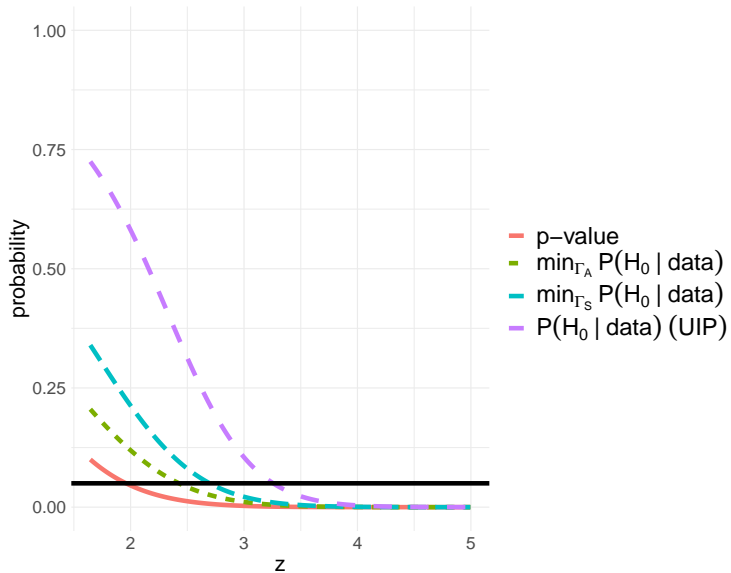
# Comparison with unit information prior

- ▶ How far are robust Bayesian answers to what we would obtain with a default prior?
- ▶ Add in the results for the unit information prior.
- ▶ Results depend on  $z$  and  $n$ .
- ▶ The higher  $n$  is, the bigger the difference with  $p$ -values and robust Bayes.
- ▶ Similar results with other default priors: e.g., Cauchy or hyper- $g$ .

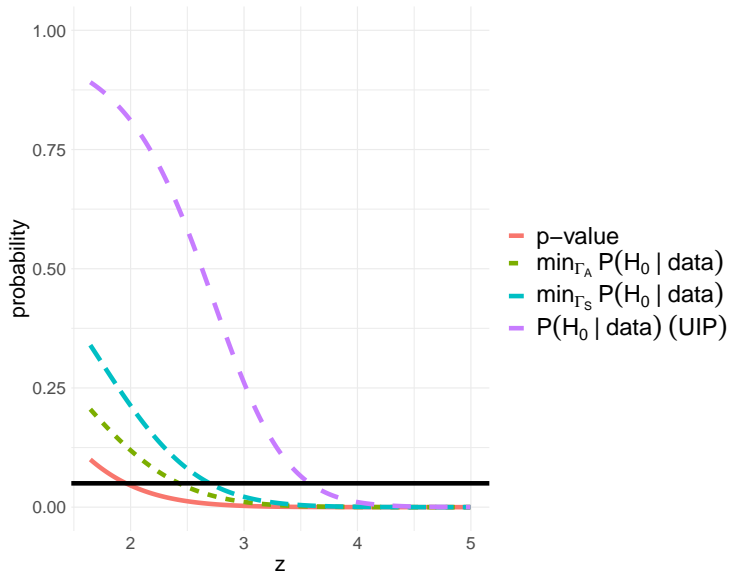
$n = 10$



$n = 100$



$n = 1000$



# Conclusions

- ▶  $P(H_0 \mid x_{1:n})$  can be pretty different to  $p$ -values.
- ▶ In point null hypothesis testing of normal means,
$$P(H_0 \mid x_{1:n}) \geq p\text{-value}.$$

- ▶ Robust Bayes can be far from proper Bayes for large  $n$ .

# Reference

Berger, J. O., & Sellke, T. (1987). Testing a point null hypothesis: The irreconcilability of  $p$ -values and evidence. *Journal of the American Statistical Association*, 82(397), 112-122.