

(1)、

```
Please input the initial value of x:
0.5
Please input the value of eps1:
0.000001
Please input the value of eps2:
0.0001
Please input n:
10
The zeros of the function is 0.567143164965
```

(2)、

```
Please input the initial value of x:
0.5
Please input the value of eps1:
0.000001
Please input the value of eps2:
0.0001
Please input n:
20
The zeros of the function is 0.566605664800
```

问题 3、程序的执行结果如下：

(1)、

$$P_2(x) = (3 * x^2) / 2 - 1 / 2$$

$$P_3(x) = (5 * x^3) / 2 - (3 * x) / 2$$

$$P_4(x) = (35 * x^4) / 8 - (15 * x^2) / 4 + 3 / 8$$

$$P_5(x) = (63 * x^5) / 8 - (35 * x^3) / 4 + (15 * x) / 8$$

$$P_6(x) = (231 * x^6) / 16 - (315 * x^4) / 16 + (105 * x^2) / 16 - 5 / 16$$

```
Please input the initial value of x:
0.9
Please input the value of eps1:
0.000001
Please input the value of eps2:
0.0001
Please input n:
10
The zeros of the function is 0.932469514337
```

```
Please input the initial value of x:
0.6
Please input the value of eps1:
0.000001
Please input the value of eps2:
```

0.0001
Please input n:
10
The zeros of the function is 0.661209398938

Please input the initial value of x:
0.2
Please input the value of eps1:
0.000001
Please input the value of eps2:
0.0001
Please input n:
10
The zeros of the function is 0.238619535162

Please input the initial value of x:
-0.9
Please input the value of eps1:
0.000001
Please input the value of eps2:
0.0001
Please input n:
10
The zeros of the function is -0.932469514341

Please input the initial value of x:
-0.66
Please input the value of eps1:
0.000001
Please input the value of eps2:
0.0001
Please input n:
10
The zeros of the function is -0.661209386469

Please input the initial value of x:
-0.2
Please input the value of eps1:
0.000001
Please input the value of eps2:
0.0001
Please input n:
10

The zeros of the function is -0.238619535148

同样，(2)、(3)、(4) 可以求出函数零点，这里直接给出程序执行的结果：

$$T_2(x) = 2 * x^2 - 1$$

$$T_3(x) = 4 * x^3 - 3 * x$$

$$T_4(x) = 8 * x^4 - 8 * x^2 + 1$$

$$T_5(x) = 16 * x^5 - 20 * x^3 + 5 * x$$

$$T_6(x) = 32 * x^6 - 48 * x^4 + 18 * x^2 - 1$$

$T_6(x) = 0$ 利用牛顿迭代法求出的结果为：

初始值	-1	-0.8	-0.4	0.4	0.8	1
计算结果	-0.96592583	-0.70710678	-0.25881905	0.25881905	0.70710678	0.96592583

$$L_2(x) = x^2 - 4 * x + 2$$

$$L_3(x) = -x^3 + 9 * x^2 - 18 * x + 6$$

$$L_4(x) = x^4 - 16 * x^3 + 72 * x^2 - 96 * x + 24$$

$$L_5(x) = -x^5 + 25 * x^4 - 200 * x^3 + 600 * x^2 - 600 * x + 120$$

$L_6(x) = 0$ 利用牛顿迭代法求出的结果为：

初始值	0.2	1.4	3.5	7	12
计算结果	0.26356032	1.41340306	3.59642577	7.08581001	12.64080084

$$H_2(x) = 4 * x^2 - 2$$

$$H_3(x) = 8 * x^3 - 12 * x$$

$$H_4(x) = 16 * x^4 - 48 * x^2 + 12$$

$$H_5(x) = 32 * x^5 - 160 * x^3 + 120 * x$$

$$H_6(x) = 64 * x^6 - 480 * x^4 + 720 * x^2 - 120$$

$H_6(x) = 0$ 利用牛顿迭代法求出的结果为：

初始值	-2.3	-1.3	-0.4	2.3	1.3	0.4
计算结果	-2.35060497	-1.33584907	-0.43607741	2.35060497	1.33584907	0.43607741

通过与材料中提供的零点的精确值比较可知，运用本程序可以准确地求解出满足精度要求的解。