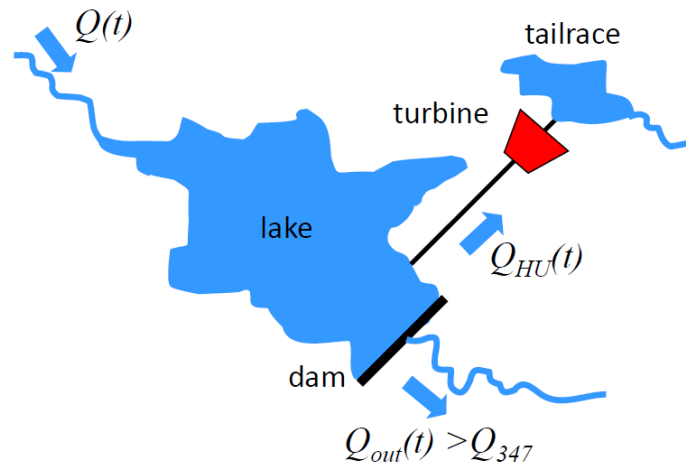


Assignment: Management of a multipurpose reservoir

Deadline for submission: 31st December



Synopsis

Evaluate the feasibility of improving the flood control operations of an existing reservoir of a hydropower plant. A larger fraction of the storage needs to be reserved for flood control and cannot be used for hydroelectric generation. The downstream part of the river should be protected from floods larger than $Q_{lim} = 150 \text{ m}^3/\text{s}$. The larger the volume for hydroelectric use, the higher the energy production. The larger the volume for flood control, the more efficiently floods can be attenuated. The two uses (hydroelectric and flood control) are therefore in competition. The goal of the assignment is to estimate the trade-off between energy production and probability that the released flow Q_{out} exceeds Q_{lim} , as a function of the volume reserved for flood control. Note that the discharge used for hydropower generation is then released into a different river system.

Tasks

1. Develop a continuous lumped hydrological model for the drainage basin of the reservoir to transform rainfall into discharge (inflow in the reservoir).
2. Fit the hydrological model using as training set the available time series of precipitation and discharge.
3. By using a Poisson pulse model, generate a 100-year-long rainfall time series with the same statistical properties as the observed rainfall.
4. Transform generated rainfall into a generated time series of discharge by means of the fitted hydrological model.
5. Simulate the reservoir routing and the flood control operations for different maximum levels for hydroelectric use.
6. Evaluate the average annual energy produced and the flooding probability.

7. (*facultative*) Repeat the simulations of point 5 by using seasonally varying maximum levels for hydroelectric use and different values of the discharge for hydroelectric use Q_{HU} . Find the subset of non-dominated solutions and analyse their properties.

Input data

- Six-year-long series of measured rainfall and discharge (files `P.txt`, `Q_obs.txt`);
- Monthly mean series of temperature and crop factor (files `temperature.txt` and `kc.txt`);
- Parameters for the hydrological model: wilting point s_w , soil moisture for maximum plant transpiration s_1 , porosity n , base flow Q_b , mean superficial residence time (t_{sup}), area of the basin A and latitude (see Table 2);
- Relation between area of reservoir lake and level of the reservoir (file `area_rating-curve.txt`);
- Reservoir parameters: discharge coefficients for sluice gate and spillway ($C_{q,sl}$, $C_{q,sp}$) spillway length and height (L , p) (see Table 2);
- The design discharge of the turbine Q_T (see Table 2);
- Power plant parameters: pipe diameter, length and sand equivalent roughness (D , L_p , k_s), turbine efficiency η , altitude gap between the bottom of the reservoir and the tailrace Δh , minimum level for hydropower production (see Table 2).

Procedure

Hydrological model. Implement the hydrological model on the 6-year-long series of precipitation and discharge.

1. Compute the potential evapotranspiration ET_0 via the Thornthwaite method.
2. Attribute arbitrary values to the parameters K_{sat} , c , t_{sub} , z .
3. Use an Euler explicit scheme to integrate the system of equations at hourly scale (see Table 3).
4. Test the mass balance of your system in order to ensure a correct implementation.
5. Evaluate the goodness of fit of the chosen parameter set by calculating the Nash-Sutcliffe index NS .

$$NS = 1 - \frac{\sum_{t=t_0}^{t_{end}} [Q_{obs}(t) - Q_{mod}(t)]^2}{\sum_{t=t_0}^{t_{end}} [Q_{obs}(t) - \overline{Q_{obs}}]^2};$$

where Q_{obs} and Q_{mod} are the measured and modelled discharges, respectively. $\overline{Q_{obs}}$ is the average measured discharge.

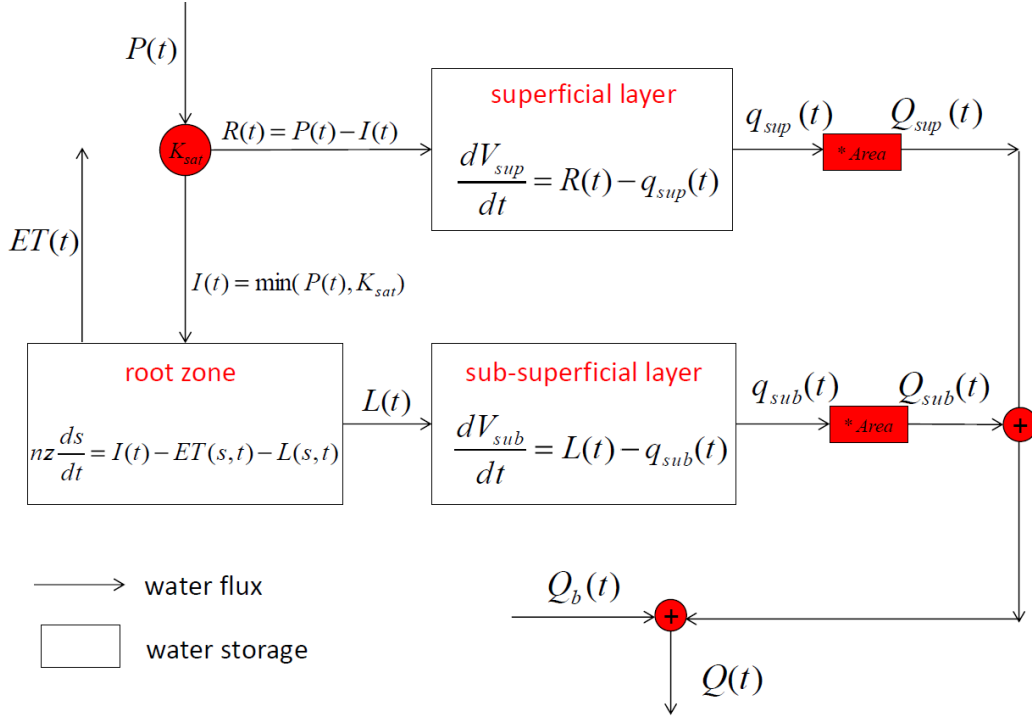


Figure 1: Scheme of the hydrological model. Boxes indicate water storages, arrows indicate water fluxes.

Model calibration. Find the set of parameters $\{K_{sat}, c, t_{sub}, z\}$ that maximizes the Nash-Sutcliffe index. Use a simulated annealing strategy in order to find the parameter set that maximizes NS .

1. Define a functional form for the temperature

$$T_{SA}(i) = \exp(-c_r \cdot i)$$

where i counts the iterations of the calibration procedure, while c_r is a cooling rate (see Table 2).

2. Attribute arbitrary values to the parameters K_{sat}, c, t_{sub}, z . Run the hydrological model and evaluate NS_{old} .
3. Select a new parameter set by drawing from a truncated normal distribution centered in the previous parameter set (use function `TruncNormRnd.m`).
4. Run the hydrological model with the new parameter set and evaluate NS_{new} .
5. If $NS_{new} > NS_{old}$, accept the new parameter set.
6. Otherwise, accept the new parameter set with probability

$$\exp\left(\frac{NS_{new} - NS_{old}}{T_{SA}(i)}\right)$$

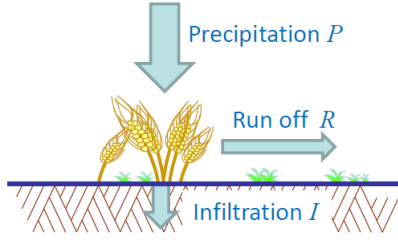
7. Repeat from 3 until convergence. A good fitting should achieve $NS \geq 0.87$.

Variable	Symbol	Unit
Precipitation	P	[LT ⁻¹]
Infiltration	I	[LT ⁻¹]
Runoff	R	[LT ⁻¹]
Soil moisture	s	[-]
Evapotranspiration	ET	[LT ⁻¹]
Leaching	L	[LT ⁻¹]
Superficial storage	V_{sup}	[L]
Superficial specific discharge	q_{sup}	[LT ⁻¹]
Superficial discharge	Q_{sup}	[L ³ T ⁻¹]
Sub-superficial storage	V_{sub}	[L]
Sub-superficial specific discharge	q_{sub}	[LT ⁻¹]
Sub-superficial discharge	Q_{sub}	[L ³ T ⁻¹]

Table 1: List of variables for the hydrological model

Parameter	Symbol	Value	Unit
<i>Hydrological model: to be calibrated</i>			
Hydraulic conductivity for saturated soil	K_{sat}	-	[LT ⁻¹]
Exponent for power-law relation $L(s)$	c	-	[-]
Root zone depth	z	-	[L]
Mean sub-superficial residence time	t_{sub}	-	[T]
<i>Hydrological model: other</i>			
Wilting point	s_w	0.25	-
Soil moisture stress threshold	s_1	0.4	-
Porosity	n	0.3	-
Baseflow	Q_b	7	m ³ /s
Mean superficial residence time	t_{sup}	22	h
Catchment area	\mathcal{A}	4000	km ²
Latitude	ϕ	38	°
<i>Calibration of the hydrological model</i>			
Cooling rate	c_r	1/1200	-
<i>Reservoir</i>			
Discharge coefficient for sluice gate	$C_{q,sl}$	0.6	-
Discharge coefficient for spillway	$C_{q,sp}$	0.5	-
Length of the spillway	L	100	m
Level of the spillway crest	p	18	m
<i>Power plant</i>			
Discharge to the turbine	Q_T	55	m ³ /s
Pipe diameter	D	3	m
Pipe length	L_p	1000	m
Sand equivalent roughness	k_s	0.5	mm
Turbine efficiency	η	0.80	-
Altitude gap between the bottom of the reservoir and the tailrace	Δh	70	m
Minimum level for hydroelectric production	$l_{min,HU}$	2	m

Table 2: List of parameters

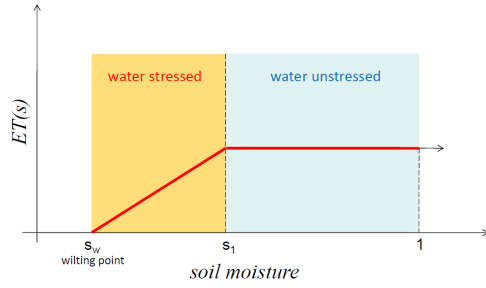


Runoff generation (Horton mechanism):

$$P(t) = R(t) + I(t);$$

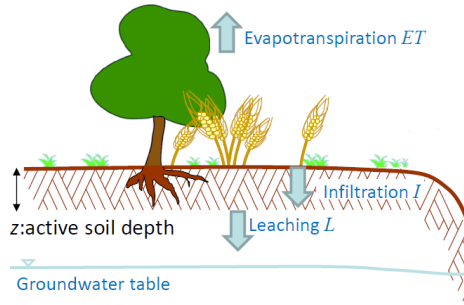
$$I(t) = \min(P(t), K_{sat});$$

$$R(t) = P(t) - I(t);$$



Evapotranspiration computation:

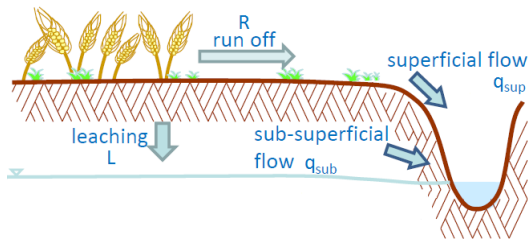
$$ET(t) = \begin{cases} 0, & \text{if } 0 \leq s(t) \leq s_w, \\ k_c ET_0 \cdot \frac{s(t) - s_w}{s_1 - s_w}, & \text{if } s_w < s(t) \leq s_1. \\ k_c ET_0, & \text{if } s_1 < s(t) \leq 1. \end{cases}$$



Soil moisture dynamics:

$$nz \frac{ds}{dt} = I(t) - ET(s, t) - L(s, t);$$

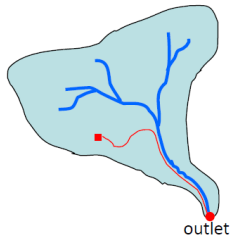
$$L(t) = K(s) = K_{sat} \cdot s(t)^c;$$



Linear reservoir scheme:

$$\frac{dV_{sup}}{dt} = R(t) - q_{sup}(t); \quad q_{sup}(t) = t_{sup}^{-1} V_{sup}(t);$$

$$\frac{dV_{sub}}{dt} = L(t) - q_{sub}(t); \quad q_{sub}(t) = t_{sub}^{-1} V_{sub}(t).$$



Discharge computation:

$$Q_{sup}(t) = \mathcal{A} \cdot q_{sup}(t);$$

$$Q_{sub}(t) = \mathcal{A} \cdot q_{sub}(t);$$

$$Q(t) = Q_{sup}(t) + Q_{sub}(t) + Q_b.$$

Table 3: System of equations constituting the hydrological model.

Simulated rainfall sequence. Generate 100 years of rainfall (at daily timescale) with the parameters (mean daily rainfall depth α and rainfall frequency λ) estimated from the observed precipitation.

1. Up-scale the given hourly rainfall series to average daily rainfall. The resulting time series should have one value for each day with mm/day as unit.
2. Evaluate the parameters α (mean precipitation intensity) and λ (frequency of rainfall events). Account for seasonality by computing different values of the parameters for each month.
3. Generate the 100-year-long rainfall series. For any generic day of month m :
 - a rainfall event occurs with probability $\lambda(m)\Delta t$, where $\Delta t = 1$ day.
 - If a rainfall event occurs, the rainfall depth is extracted from an exponential distribution with mean $\alpha(m)$. Use the inverse transformation method to generate exponentially distributed random variables.

Points 2 and 3 are repeated for all the days and months of the generation period.

4. Use the function `downscaling.m` to down-scale the daily generated rainfall to hourly rainfall.

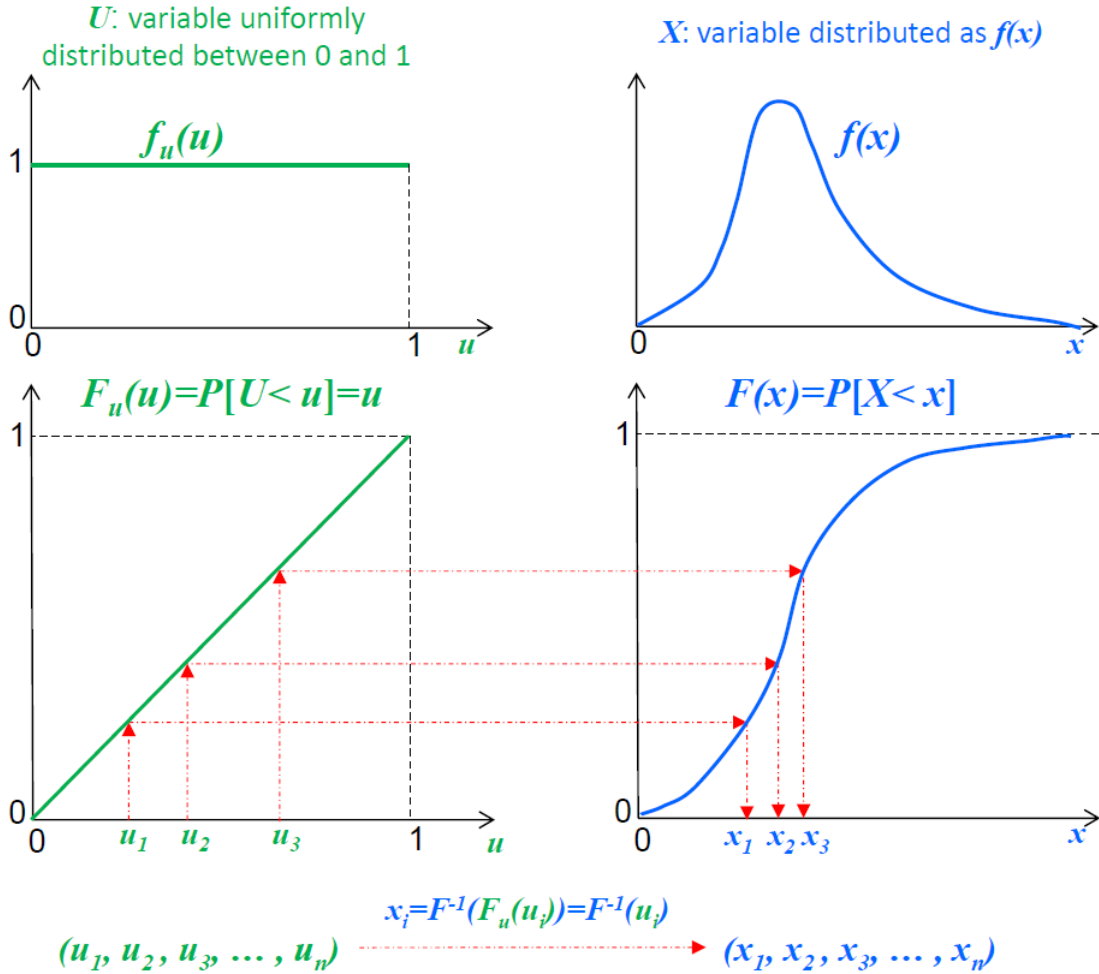


Figure 2: Inverse transformation method.

Simulated discharge sequence. Run the calibrated hydrological model forced by the generated rainfall and obtain the discharge time series that will constitute the input of the reservoir.

Flood control. Implement the flood control practice and the reservoir routing. Assume that the power plant works only during peak hours (from 11:00 to 18:00, 7 hours). If at the beginning of the day (midnight) the level in the reservoir is above the minimum level for hydroelectrical use, the plant will work during that day, otherwise it will not. When the turbine is working, Q_{HU} is always equal to the turbine design discharge Q_T . To compute the net head of the turbine, account for frictional head losses along the pipe, entrance head loss (half of the kinematic term) and exit head loss (one kinematic term). The efficiency of the turbine η can be assumed as constant.

1. Compute the minimum flow target Q_{347} (discharge that is exceeded 95% of the time) from the 100-year-long generated input discharge time series.
2. Starting from the area rating curve, compute the volume rating curve (use trapezoidal approximation).
3. Assume a value for the maximum level for hydroelectric use (e.g. 15 m) and compute the corresponding volume.
4. For each time step of integration ($\Delta t = 1$ hour):
 - Evaluate the level of the reservoir (use the function `level_volume.m` which is faster than `interp1`).
 - Compute the discharge Q_{HU} routed to the power plant. $Q_{HU} = Q_T$ during peak hours if the power plant is working in that particular day, otherwise $Q_{HU} = 0$.
 - Compute the sluice opening area A . The opening of the sluice gate is operated so that:
 - the discharge through the gate $Q_g(t)$ is larger than the minimum flow Q_{347} and lower than Q_{lim} ;
 - the level is kept, if possible (i.e. if the gate discharge is within the aforementioned limits), at the maximum level for hydroelectrical use;
 - if during floods the maximum level for hydroelectrical use is exceeded, the reservoir is emptied as quick as possible.

The above practice can be implemented as follows. At each time step, the opening of the sluice gate is computed so that volume at the end of the time step equals (if possible, i.e. if the gate discharge is within the aforementioned limits) the volume corresponding to the maximum level for hydroelectrical use ($V_{max,HU}$).

$$Q_g(t) = \max \begin{cases} Q_{347} \\ \min \left\{ \frac{V(t) + [Q(t) - Q_{HU}(t)] \cdot \Delta t - V_{max,HU}}{\Delta t}, Q_{lim} \right\} \end{cases}$$

where V is the volume stored in the reservoir.

- Compute the total output discharge Q_{out} :

$$Q_{out} = \begin{cases} C_{q,sl} A \sqrt{2gl} & \text{if } l \leq p, \\ C_{q,sl} A \sqrt{2gl} + C_{q,sp} L \sqrt{2g(l-p)^3}, & \text{if } l > p. \end{cases}$$

where l is the level in the reservoir (with respect to the empty pool), p and L are the level of the spillway crest and the spillway length, respectively; $C_{q,sl}$ and $C_{q,sp}$ are the discharge coefficients for sluice gate and spillway, respectively; g is the gravity acceleration.

- Integrate the storage equation:

$$\frac{dV(t)}{dt} = Q(t) - Q_{out}(l(V(t))) - Q_{HU}(t),$$

via an Euler explicit scheme. Other fluxes (e.g. evaporation from the lake, input of rainfall into the lake, deep percolation) are negligible.

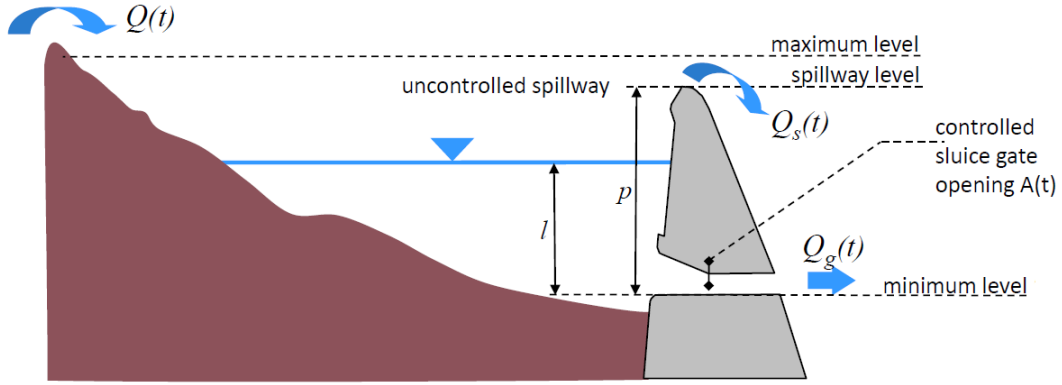


Figure 3: Cross-section of the reservoir

Energy production and flooding probability. Repeat the flood control practice and the routing of the reservoir for different values (from 10 to 18 m, with step size of 1 m) of maximum level for hydroelectrical use $l_{max,HU}$. Compute the average annual energy production in [GWh] and the probability that the released discharge Q_{out} is larger than $Q_{lim} = 150 \text{ m}^3/\text{s}$ (for numerical reasons, the condition should read: $Q_{out} > 151 \text{ m}^3/\text{s}$) as a function of $l_{max,HU}$. Use the same sequence of generated discharge (100-year-long) to simulate the reservoir routing for different values of $l_{max,HU}$.

Facultative: Multi-criteria optimization In a separate script (Lastname_MultiCriteria.m), modify the previous reservoir routing by accounting for seasonally varying maximum levels for hydroelectric use. Moreover, consider different values for the design discharge to the turbine Q_T . Using as input a discharge time series of shorter length, run the reservoir routing and plot flooding probability against average annual energy production for all possible combinations of seasonal $l_{max,HU}$ and Q_T . Identify all non-dominated solutions. The template for this file is not given.

Suggested settings:

- Length of the discharge time series: 30 years at least.

- Use one value of $l_{max,HU}$ from April to October and a second one from November to March.
- For both seasons, $l_{max,HU}$ ranges from 13 m to 18 m with a step size of 0.5 m.
- Q_T ranges from 50 m³/s to 70 m³/s, with a step size of 5 m³/s.
- Suppose that the turbine efficiency η does not change as a function of Q_T .

Warning: with the suggested settings, it might take around one hour to run the code! It is suggested to start by running the script with a reduced set of decision variables.

Report

1. Report the best fit parameters for the hydrological model.
2. Plot the time series of observed discharge and of the discharge as simulated by the hydrological model with the best fit parameters (Figure 101 of the template `Lastname_Calibrate_HM.m`).
3. Plot Markov chains of the calibrated parameters and sequences of values of NS and T_{SA} as a function of the number of iterations (Figure 102 of the template `Lastname_Calibrate_HM.m`).
4. Plot the comparison between the statistics of the observed and generated precipitation (Figure 1 of the template `Lastname_Main.m`).
5. Plot the time series (100-year-long) of generated precipitation in [mm/h], run off in [mm/h], infiltration in [mm/h], soil moisture, leakage in [mm/h] and evapotranspiration in [mm/h] (as Figure 103 of the template `Lastname_Calibrate_HM.m` but for the calibrated hydrological model forced by the generated precipitation).
6. Plot the area and the volume rating curves (Figure 1001 of the template `Lastname_Main.m`).
7. Report the minimum flow (discharge that is equalled or exceeded 95% of the time) of the generated discharge.
8. For a maximum level for hydroelectric use of 15 m, plot the time series (100 years long) of input discharge, output discharge, volume within the reservoir and level (Figure 1002 of the template `Lastname_Main.m`).
9. Plot the average annual energy production in [GWh] and the probability that Q_{out} exceeds 150 m³/s for different values of the maximum level for hydroelectrical use (see Figure 4).
10. (facultative) For each combination of $l_{max,HU}$ (in summer and winter) and Q_T , plot the average annual energy production against the flooding probability (1 point for each combination). Highlight all non-dominated solutions.
11. (facultative) Elaborate on the influence of decision variables on the determination of non-dominated solutions. Do not exceed 400 words. Figures are allowed.

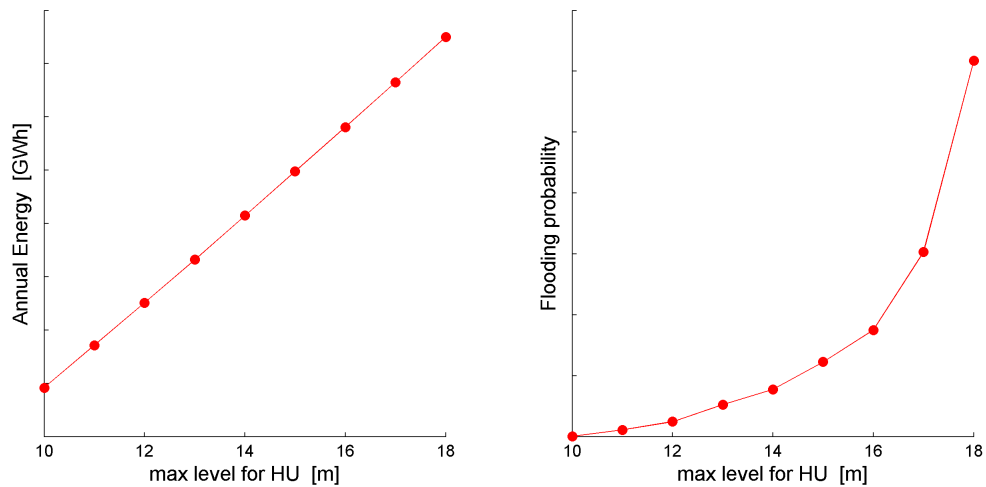


Figure 4: Annual average energy production and flooding probability as a function of $l_{max,HU}$.

Required files

- `Lastname_HydroModel.m`: function that executes the hydrological model.
- `Lastname_Calibrate_HM.m`: calibration of the hydrological model.
- `Lastname_Main.m`: generation of rainfall; calibrated hydrological model forced by the generated rainfall; implementation of the flood control practice and reservoir routing; computation of the annual energy production and flooding probability for different values of the maximum level for hydroelectrical use.
- (facultative) `Lastname_MultiCriteria.m`: modification of `Lastname_Main.m` that accounts for different levels $l_{max,HU}$ in summer and winter and different values for Q_T ; plot of all possible combinations in an energy vs. flooding probability graph; algorithm for identification of non-dominated solutions; graphs used for the answer to question 11.
- `Lastname_Report.pdf`: report providing the answers to the previous questions and contains the figures described above (no description nor discussion, except for question 11).

Notes

- The facultative part may let you gain up to 15 points. The maximum grade for the assignment is 100.
- Everyone must submit her/his own files through Moodle.
- Do not upload the input files nor the auxiliary functions (`level_volume.m`, `down-scaling.m`, `TruncNormRnd.m`).
- Do not upload compressed files.
- Scripts must work without errors and produce the same figures that are shown in the report. Commented parts of the scripts will not be read.
- Please report the unit of measure in all the figures' axes and in all the answers.