## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad x^4 - 3x^3 - 4x^2 + -5x^6 + x^2 + 4x^6 - 8x^2 = -x^6 + x^4 - 3x^3 - 11x^2$$

$$[2] \quad 2x^5 - 3x + 4x^5 - 3x^2 - x + 4x^3 - 3x^2 = 6x^5 + 4x^3 - 6x^2 - 4x$$

$$[3] \quad 3x^5 - 2x^4 - 2x + x^5 + 4x^4 + 3x^2 + -3x^6 - x^3 + x^2 = -3x^6 + 4x^5 + 2x^4 - x^3 + 4x^2 - 2x$$

$$[4] \quad 2x^5 + x^3 - 3x + -7x^4 - 4x^2 + -3x^5 + 4x^4 = -x^5 - 3x^4 + x^3 - 4x^2 - 3x$$

$$[5] \quad -x^6 - 8x^5 + (-x^6 + 3x^5 + 2x^3) + (-5x^4 - 4x^3) = -2x^6 - 5x^5 - 5x^4 - 2x^3$$

$$[6] \quad x^2 + -3x^6 + 2x^3 + -2x^5 - 4x^3 - 2x = -3x^6 - 2x^5 - 2x^3 + x^2 - 2x$$

$$[7] \quad 3x^6 - x^5 - 2x^2 + 4x^5 - 4x^3 - x + 3x^6 - 3x^5 + x^4 = 6x^6 + x^4 - 4x^3 - 2x^2 - x$$

$$[8] \quad 2x^5 - x^3 - 2x^2 + -x^5 + 3x^3 - 2x + -2x^5 + x^4 + 4x^3 = -x^5 + x^4 + 6x^3 - 2x^2 - 2x$$

$$[9] \quad 3x^6 + 4x^5 - 4x^3 + -4x^5 - x^3 + (-2x^6 + 6x^3) = x^6 + x^3$$

$$[10] \quad 2x^6 + 3x^5 + x + -5x^2 + 3x + (-3x^5 - x^2 + 3x) = 2x^6 - 6x^2 + 7x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} &[1] \quad 0+0+0=0 \\ &[2] \quad 6\,x^2y^2-xy+-xy^2-3\,xy+2\,x^2y^2+5\,xy^2=8\,x^2y^2+4\,xy^2-4\,xy \\ &[3] \quad -20\,x^2y^2-2\,xy^2+(-6\,x^2y+8\,xy^2)+(-8\,x^2y^2-4\,x^2y)=-28\,x^2y^2-10\,x^2y+\\ 6\,xy^2 \\ &[4] \quad 6\,x^2y+9\,xy+18\,x^2y^2+18\,xy+-27\,x^2y^2-9\,x^2y-3\,xy=-9\,x^2y^2-3\,x^2y+24\,xy \\ &[5] \quad 12\,x^2y^2-16\,x^2y-16\,xy^2+-32\,x^2y-60\,xy^2+-64\,x^2y^2+12\,xy^2-16\,xy=\\ -52\,x^2y^2-48\,x^2y-64\,xy^2-16\,xy \\ &[6] \quad 25\,x^2y^2+10\,xy^2+5\,xy+-150\,x^2y^2+50\,xy+120\,x^2y-50\,xy=-125\,x^2y^2+\\ 120\,x^2y+10\,xy^2+5\,xy \\ &[7] \quad 90\,x^2y-12\,xy+-18\,x^2y^2-6\,x^2y+108\,xy^2+(-24\,x^2y^2-108\,x^2y)=\\ -42\,x^2y^2-24\,x^2y+108\,xy^2-12\,xy \\ &[8] \quad 21\,x^2y+-49\,x^2y^2-98\,x^2y+49\,xy^2+49\,xy^2=-49\,x^2y^2-77\,x^2y+98\,xy^2\\ &[9] \quad 192\,x^2y^2+64\,x^2y-16\,xy^2+-72\,x^2y-24\,xy+(-24\,x^2y^2+8\,xy^2)=168\,x^2y^2-\\ 8\,x^2y-8\,xy^2-24\,xy \\ &[10] \quad -27\,x^2y^2-162\,xy^2-9\,xy+(-261\,x^2y^2+243\,x^2y)+(-243\,x^2y^2+243\,x^2y+18\,xy^2)=-531\,x^2y^2+486\,x^2y-144\,xy^2-9\,xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 2\,x^2y^2 - 2\,xy^2 + -4\,x^2y^2 + 3\,x^2y + 2\,xy - (xy^2 + xy) = -2\,x^2y^2 + 3\,x^2y - 3\,xy^2 + xy \\ &[3] \quad 6\,x^2y + 2\,xy^2 - 4\,xy + 20\,x^2y + 16\,xy - (-2\,xy^2 + 8\,xy) = 26\,x^2y + 4\,xy^2 + 4\,xy \\ &[4] \quad 9\,xy^2 + 6\,xy - (39\,xy^2) + (21\,xy^2) = -9\,xy^2 + 6\,xy \\ &[5] \quad 16\,xy + 4\,x^2y^2 + 36\,x^2y - (32\,x^2y - 64\,xy^2 + 32\,xy) = 4\,x^2y^2 + 4\,x^2y + 64\,xy^2 - 16\,xy \\ &[6] \quad -100\,x^2y^2 + 75\,xy^2 - 25\,xy + 100\,x^2y + 50\,xy^2 - (-20\,x^2y + 10\,xy^2 - 25\,xy) = -100\,x^2y^2 + 120\,x^2y + 115\,xy^2 \end{aligned}$$

$$\begin{aligned} &[7] \quad -132\,x^2y^2 + 36\,xy^2 - (-144\,x^2y^2 + 24\,x^2y + 6\,xy) + (6\,x^2y^2 - 18\,xy^2 - 12\,xy) = \\ &18\,x^2y^2 - 24\,x^2y + 18\,xy^2 - 18\,xy \\ &[8] \quad 49\,x^2y^2 + 49\,x^2y + -98\,x^2y + 28\,xy - (-14\,x^2y^2 + 56\,xy) = 63\,x^2y^2 - 49\,x^2y - \\ &28\,xy \\ &[9] \quad 88\,x^2y + 256\,xy^2 + 32\,xy^2 - 24\,xy - (24\,x^2y^2 - 24\,x^2y - 32\,xy^2) = -24\,x^2y^2 + \\ &112\,x^2y + 320\,xy^2 - 24\,xy \\ &[10] \quad 243\,x^2y - 18\,xy^2 - (162\,x^2y^2 - 243\,x^2y) + (-162\,x^2y^2 - 9\,xy^2 + 36\,xy) = \\ &-324\,x^2y^2 + 486\,x^2y - 27\,xy^2 + 36\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (4\,b^2xy^3z^2) \cdot (b^3x^2yz^2) = 4\,b^5x^3y^4z^4 \\ &[3] \quad (-4\,b^3x^3y^2z^2) \cdot (-24\,b^3x^2y^3z^2) = 96\,b^6x^5y^5z^4 \\ &[4] \quad (54\,bxyz^2) \cdot (-3\,b^2xyz) = -162\,b^3x^2y^2z^3 \\ &[5] \quad (-8\,bx^3y^3z) \cdot (16\,bx^3yz) = -128\,b^2x^6y^4z^2 \\ &[6] \quad (-25\,b^3x^2y^3z^3) \cdot (-25\,bx^2yz^3) = 625\,b^4x^4y^4z^6 \\ &[7] \quad (-108\,bx^3yz^3) \cdot (-12\,b^3x^2y^3z^3) = 1296\,b^4x^5y^4z^6 \\ &[8] \quad (147\,bxyz^2) \cdot (14\,b^3x^3yz^2) = 2058\,b^4x^4y^2z^4 \\ &[9] \quad (-24\,b^3x^3y^2z^3) \cdot (256\,b^3x^3y^3z^3) = -6144\,b^6x^6y^5z^6 \\ &[10] \quad (2187\,bx^2y^3z^3) \cdot (1458\,b^3xy^2z) = 3188646\,b^4x^3y^5z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x^2) \cdot (6\,x^2) = -6\,x^4 \\ &[2] \quad (-2\,x^2) \cdot (-2\,x^2 + 4\,x) = 4\,x^4 - 8\,x^3 \\ &[3] \quad (3\,x) \cdot (-3\,x^2 + 7\,x) = -9\,x^3 + 21\,x^2 \\ &[4] \quad (-2\,x) \cdot (-2\,x^2 + 2\,x) = 4\,x^3 - 4\,x^2 \\ &[5] \quad (3\,x) \cdot (-4\,x^2) = -12\,x^3 \\ &[6] \quad (-2\,x^2) \cdot (-2\,x^2 + x) = 4\,x^4 - 2\,x^3 \\ &[7] \quad (-4\,x^2) \cdot (7\,x^2 + 3\,x) = -28\,x^4 - 12\,x^3 \\ &[8] \quad (-4\,x^2) \cdot (-4\,x^2) = 16\,x^4 \\ &[9] \quad (-4\,x^2) \cdot (3\,x^2 + x) = -12\,x^4 - 4\,x^3 \\ &[10] \quad (4\,x^2) \cdot (5\,x^2 + 2\,x) = 20\,x^4 + 8\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (2\,x^2+4\,x)\cdot(4\,x^2)=8\,x^4+16\,x^3\\ &[2] \quad (0)\cdot(0)=0\\ &[3] \quad (8\,x)\cdot(-x^2+5\,x)=-8\,x^3+40\,x^2\\ &[4] \quad (x^2-3\,x)\cdot(x^2-5\,x)=x^4-8\,x^3+15\,x^2\\ &[5] \quad (4\,x^2+4\,x)\cdot(x^2+2\,x)=4\,x^4+12\,x^3+8\,x^2\\ &[6] \quad (-2\,x^2+2\,x)\cdot(9\,x)=-18\,x^3+18\,x^2\\ &[7] \quad (2\,x^2-4\,x)\cdot(x^2-4\,x)=2\,x^4-12\,x^3+16\,x^2\\ &[8] \quad (-5\,x)\cdot(-x^2+2\,x)=5\,x^3-10\,x^2 \end{aligned}$$

[9] 
$$(-4x^2) \cdot (-2x^2 - x) = 8x^4 + 4x^3$$

[10] 
$$(-3x) \cdot (-7x^2 - x) = 21x^3 + 3x^2$$

[11] 
$$(-3x) \cdot (2x^2 - 2x) = -6x^3 + 6x^2$$

[12] 
$$(-2x^2) \cdot (-9x) = 18x^3$$

[13] 
$$(0) \cdot (-x^2 + 3x) = 0$$

[14] 
$$(7x) \cdot (-4x^2 - 6x) = -28x^3 - 42x^2$$

[15] 
$$(6x^2) \cdot (-x^2 + x) = -6x^4 + 6x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(5x^3 - 2x^2) \cdot (-5x^3 - 3x) = -25x^6 + 10x^5 - 15x^4 + 6x^3$$

[2] 
$$(2x^2 - 2x) \cdot (-x^2 - 2x) = -2x^4 - 2x^3 + 4x^2$$

[3] 
$$(-8x) \cdot (-x^3 - 4x^2 + 7x) = 8x^4 + 32x^3 - 56x^2$$

[4] 
$$(-3x^3 - x^2 - 3x) \cdot (-2x^2) = 6x^5 + 2x^4 + 6x^3$$

[5] 
$$(-2x^3 - 3x) \cdot (-2x^3 - x^2 + 8x) = 4x^6 + 2x^5 - 10x^4 + 3x^3 - 24x^2$$

[6] 
$$(-x) \cdot (-x^3 - 5x^2) = x^4 + 5x^3$$

[7] 
$$(-2x^3 + 4x^2 + 3x) \cdot (-4x^2 - x) = 8x^5 - 14x^4 - 16x^3 - 3x^2$$

[8] 
$$(2x^3 - 4x) \cdot (-x^2 - 4x) = -2x^5 - 8x^4 + 4x^3 + 16x^2$$

[9] 
$$(-7x^3) \cdot (-4x^2 + 4x) = 28x^5 - 28x^4$$

[10] 
$$(-4x^3 + 3x) \cdot (-3x^3 - 6x^2) = 12x^6 + 24x^5 - 9x^4 - 18x^3$$

[11] 
$$(3x^2 - 2x) \cdot (3x^3 - 3x) = 9x^5 - 6x^4 - 9x^3 + 6x^2$$

[12] 
$$(-7x^3) \cdot (6x^3 + 3x^2) = -42x^6 - 21x^5$$

[13] 
$$(-3x^3 - 5x^2) \cdot (-3x^3 - 2x^2 - x) = 9x^6 + 21x^5 + 13x^4 + 5x^3$$

[14] 
$$(x^3 - 4x) \cdot (-x^3 + 2x^2 + 7x) = -x^6 + 2x^5 + 11x^4 - 8x^3 - 28x^2$$

[15] 
$$(4x^3) \cdot (x^3 - 4x) = 4x^6 - 16x^4$$

[16] 
$$(-3x^3 - 7x) \cdot (2x^3 - 5x^2) = -6x^6 + 15x^5 - 14x^4 + 35x^3$$

[17] 
$$(2x^2 + 3x) \cdot (2x^3 - x^2) = 4x^5 + 4x^4 - 3x^3$$

[18] 
$$(x) \cdot (-6x^2 - 3x) = -6x^3 - 3x^2$$

[19] 
$$(4x^3) \cdot (3x) = 12x^4$$

[20] 
$$(x^3 + 3x^2) \cdot (-2x^3 - 4x^2 - 6x) = -2x^6 - 10x^5 - 18x^4 - 18x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(4x^2y - xy^2) \cdot (2xy^2) = 8x^3y^3 - 2x^2y^4$$

[2] 
$$(3x^2y^2 + 3xy^2) \cdot (-4x^2y - 4xy^2 + 3xy) = -12x^4y^3 - 12x^3y^4 - 3x^3y^3 - 12x^2y^4 + 9x^2y^3$$

[3] 
$$(3x^2y^2 - xy) \cdot (-2x^2y - 3xy^2 - xy) = -6x^4y^3 - 9x^3y^4 - 3x^3y^3 + 2x^3y^2 + 3x^2y^3 + x^2y^2$$

[4] 
$$(-5x^2y^2) \cdot (x^2y^2) = -5x^4y^4$$

[5] 
$$(-2x^2y) \cdot (-2x^2y^2) = 4x^4y^3$$

[6] 
$$(x^2y^2 + xy) \cdot (-x^2y^2 - 2xy) = -x^4y^4 - 3x^3y^3 - 2x^2y^2$$

[7] 
$$(-x^2y^2 - 3x^2y) \cdot (3xy^2) = -3x^3y^4 - 9x^3y^3$$