1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 2\,x^6 + 3\,x^3 - x + 3\,x^6 + 4\,x^5 - 4\,x^2 + 4\,x^4 + x^2 - 2\,x = 5\,x^6 + 4\,x^5 + 4\,x^4 + 3\,x^3 - 3\,x^2 - 3\,x$$

$$[2] \quad x^6 - x^4 - 2\,x^3 + -x^6 - 4\,x^3 + x^6 + 5\,x^5 = x^6 + 5\,x^5 - x^4 - 6\,x^3$$

$$[3] \quad 4\,x^4 - 6\,x^3 + 2\,x^6 - 7\,x^2 + -2\,x^3 - 4\,x^2 + x = 2\,x^6 + 4\,x^4 - 8\,x^3 - 11\,x^2 + x$$

$$[4] \quad x^4 + -3\,x + 4\,x^3 - x = x^4 + 4\,x^3 - 4\,x$$

$$[5] \quad 4\,x^4 - x^2 + -2\,x^6 + x^4 - 2\,x^2 + -2\,x^6 + 3\,x^4 - 4\,x = -4\,x^6 + 8\,x^4 - 3\,x^2 - 4\,x$$

$$[6] \quad 2\,x^5 - 6\,x^4 + 2\,x^6 - 2\,x^2 + 0 = 2\,x^6 + 2\,x^5 - 6\,x^4 - 2\,x^2$$

$$[7] \quad 4\,x^5 - x^3 + 4\,x^3 + 2\,x^2 + 3\,x + 6\,x^2 - 3\,x = 4\,x^5 + 3\,x^3 + 8\,x^2$$

$$[8] \quad -3\,x^4 - x^3 + 4\,x + (-8\,x^2) + (-4\,x^6) = -4\,x^6 - 3\,x^4 - x^3 - 8\,x^2 + 4\,x$$

$$[9] \quad x^4 - x^3 + x^6 + 3\,x^5 - 3\,x^2 + -3\,x^4 - 2\,x^3 - x^2 = x^6 + 3\,x^5 - 2\,x^4 - 3\,x^3 - 4\,x^2$$

$$[10] \quad 2\,x^6 + 2\,x^3 + 2\,x + -x^4 - 4\,x^2 - x + -x^6 - 8\,x = x^6 - x^4 + 2\,x^3 - 4\,x^2 - 7\,x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 2x^2y^2+xy^2-3\,xy+-6\,xy+2\,x^2y^2-3\,x^2y-xy=4\,x^2y^2-3\,x^2y+xy^2-10\,xy \\ [3] \quad 8\,x^2y^2-4\,x^2y-8\,xy+-12\,x^2y^2-16\,x^2y+4\,xy^2+-6\,x^2y+4\,xy=-4\,x^2y^2-26\,x^2y+4\,xy^2-4\,xy \\ [4] \quad 6\,x^2y^2-36\,xy+6\,x^2y^2+9\,x^2y+6\,xy^2+36\,x^2y^2-9\,x^2y+27\,xy^2=48\,x^2y^2+33\,xy^2-36\,xy \\ [5] \quad 16\,xy+-16\,x^2y^2+16\,x^2y-8\,xy+-48\,x^2y^2+8\,xy^2-16\,xy=-64\,x^2y^2+16\,x^2y+8\,xy^2-8\,xy \\ [6] \quad 15\,x^2y^2-50\,xy^2+-25\,x^2y^2+5\,xy^2-25\,xy+-5\,x^2y-20\,xy=-10\,x^2y^2-5\,x^2y-45\,xy^2-45\,xy \\ [7] \quad 24\,x^2y^2+150\,xy^2+-108\,x^2y^2-36\,x^2y-72\,xy+(-108\,x^2y^2+72\,xy^2)=-192\,x^2y^2-36\,x^2y+222\,xy^2-72\,xy \\ [8] \quad -21\,x^2y+49\,xy+(-98\,x^2y^2+63\,xy^2)+(-49\,x^2y^2-14\,xy^2-147\,xy)=-147\,x^2y^2-21\,x^2y+49\,xy^2-98\,xy \\ [9] \quad 16\,x^2y+280\,xy^2+-80\,x^2y^2+192\,x^2y+-128\,x^2y^2+32\,x^2y+192\,xy^2=-208\,x^2y^2+240\,x^2y+472\,xy^2 \\ [10] \quad 63\,x^2y^2+81\,xy+-81\,x^2y^2-27\,xy^2+-297\,x^2y^2+324\,xy^2=-315\,x^2y^2+297\,xy^2+81\,xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -5\,x^2y^2 + 3\,xy^2 + -2\,x^2y^2 + 4\,x^2y + 2\,xy^2 - (-x^2y^2 + 4\,x^2y) = -6\,x^2y^2 + 5\,xy^2 \\ &[3] \quad -8\,x^2y^2 - 4\,x^2y + -20\,x^2y^2 + 16\,x^2y - (-4\,x^2y^2 + 12\,xy^2 - 16\,xy) = -24\,x^2y^2 + 12\,x^2y - 12\,xy^2 + 16\,xy \\ &[4] \quad -3\,x^2y^2 + 12\,xy^2 - (9\,xy^2 + 6\,xy) + (27\,x^2y^2 + 18\,x^2y - 36\,xy) = 24\,x^2y^2 + 18\,x^2y + 3\,xy^2 - 42\,xy \end{aligned}$$

$$[5] \quad 8\,x^2y^2 - 56\,xy^2 + -32\,x^2y^2 - 8\,xy - (32\,x^2y + 16\,xy) = -24\,x^2y^2 - 32\,x^2y - 56\,xy^2 - 24\,xy \\ [6] \quad -30\,x^2y^2 - 100\,xy + 10\,x^2y^2 - 20\,xy^2 - (-100\,x^2y + 75\,xy) = -20\,x^2y^2 + 100\,x^2y - 20\,xy^2 - 175\,xy \\ [7] \quad 6\,x^2y^2 - 18\,x^2y + 36\,xy^2 - (96\,x^2y - 24\,xy^2) + (18\,x^2y^2 + 6\,x^2y) = 24\,x^2y^2 - 108\,x^2y + 60\,xy^2 \\ [8] \quad 21\,xy^2 + 210\,xy + 49\,x^2y^2 - 196\,x^2y - 196\,xy^2 - (98\,x^2y) = 49\,x^2y^2 - 294\,x^2y - 175\,xy^2 + 210\,xy \\ \end{cases}$$

[9]
$$224 x^2 y^2 + -256 x^2 y^2 + 24 x^2 y + 128 xy - (16 x^2 y + 24 xy^2 + 256 xy) = -32 x^2 y^2 + 8 x^2 y - 24 xy^2 - 128 xy$$

[10]
$$-18x^2y + 27xy - (-36x^2y^2 + 81xy^2) + (0) = 36x^2y^2 - 18x^2y - 81xy^2 + 27xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

[1]
$$(0) \cdot (0) = 0$$

[2]
$$(b^3x^3y^2z) \cdot (-4b^2x^2yz^2) = -4b^5x^5y^3z^3$$

[3]
$$(-16bx^2y^2z^2) \cdot (32b^3xy^2z^3) = -512b^4x^3y^4z^5$$

[4]
$$(6b^2x^3yz^2) \cdot (27b^3xy^3z) = 162b^5x^4y^4z^3$$

[5]
$$(192bx^2y^2z) \cdot (-48b^2x^2y^2z^2) = -9216b^3x^4y^4z^3$$

[6]
$$(125b^2x^2y^2z) \cdot (-10b^3xyz^2) = -1250b^5x^3y^3z^3$$

[7]
$$(216b^3xy^3z^3) \cdot (72b^3xyz) = 15552b^6x^2y^4z^4$$

[8]
$$(-196 bxy^3z^3) \cdot (-98 b^3x^2yz) = 19208 b^4x^3y^4z^4$$

[9]
$$(-1024 b^2 x y z^3) \cdot (-128 b^3 x^3 y^2 z) = 131072 b^5 x^4 y^3 z^4$$

[10]
$$(-81 bx^2y^2z^3) \cdot (-729 b^3x^2y^2z^2) = 59049 b^4x^4y^4z^5$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2) \cdot (3x^2) = 3x^4$$

[2]
$$(2x^2) \cdot (7x^2 - 4x) = 14x^4 - 8x^3$$

[3]
$$(2x^2) \cdot (x^2 - x) = 2x^4 - 2x^3$$

[4]
$$(3x^2) \cdot (5x^2 + 6x) = 15x^4 + 18x^3$$

[5]
$$(-3x) \cdot (3x^2) = -9x^3$$

[6]
$$(3x) \cdot (x^2) = 3x^3$$

[7]
$$(3x) \cdot (5x^2 + 2x) = 15x^3 + 6x^2$$

[8]
$$(-3x^2) \cdot (-3x^2 - x) = 9x^4 + 3x^3$$

[9]
$$(4x^2) \cdot (5x^2 - 2x) = 20x^4 - 8x^3$$

[10]
$$(-x) \cdot (-4x^2 - 2x) = 4x^3 + 2x^2$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(3x^2 + 4x) \cdot (-3x^2 + 3x) = -9x^4 - 3x^3 + 12x^2$$

[2]
$$(2x^2 - 4x) \cdot (-3x^2 + 6x) = -6x^4 + 24x^3 - 24x^2$$

[3]
$$(0) \cdot (5x^2 - 3x) = 0$$

[4]
$$(-5x^2) \cdot (-3x^2) = 15x^4$$

[5]
$$(x^2 - 2x) \cdot (2x^2) = 2x^4 - 4x^3$$

[6]
$$(-3x^2 + 3x) \cdot (-2x^2 - 3x) = 6x^4 + 3x^3 - 9x^2$$

[7] $(-2x^2 - 2x) \cdot (2x^2 - 6x) = -4x^4 + 8x^3 + 12x^2$

[8]
$$(-5x) \cdot (-3x) = 15x^2$$

[9]
$$(-2x^2) \cdot (-4x^2) = 8x^4$$

[10]
$$(2x^2 + x) \cdot (2x^2 + 2x) = 4x^4 + 6x^3 + 2x^2$$

[11]
$$(4x^2 - 4x) \cdot (0) = 0$$

[12]
$$(2x) \cdot (-3x^2 + 4x) = -6x^3 + 8x^2$$

[13]
$$(-7x) \cdot (-x^2 + 2x) = 7x^3 - 14x^2$$

[14]
$$(-4x^2 - 2x) \cdot (4x^2 + 4x) = -16x^4 - 24x^3 - 8x^2$$

[15]
$$(-4x^2 - x) \cdot (-3x) = 12x^3 + 3x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (4\,x^3) \cdot (-x^2) = -4\,x^5 \\ & [2] \quad (-4\,x^3 - 2\,x^2) \cdot (-2\,x^3 - 2\,x) = 8\,x^6 + 4\,x^5 + 8\,x^4 + 4\,x^3 \\ & [3] \quad (-6\,x^3) \cdot (2\,x^3 + 5\,x^2 + 3\,x) = -12\,x^6 - 30\,x^5 - 18\,x^4 \\ & [4] \quad (-3\,x^3 - 3\,x) \cdot (-6\,x^2) = 18\,x^5 + 18\,x^3 \\ & [5] \quad (4\,x^2 - 4\,x) \cdot (-4\,x^3 + x^2 + x) = -16\,x^5 + 20\,x^4 - 4\,x^2 \\ & [6] \quad (3\,x^3 + x^2) \cdot (-x^3 - 2\,x^2 + 3\,x) = -3\,x^6 - 7\,x^5 + 7\,x^4 + 3\,x^3 \\ & [7] \quad (-2\,x^3 + x^2 - 3\,x) \cdot (-6\,x^3) = 12\,x^6 - 6\,x^5 + 18\,x^4 \\ & [8] \quad (x) \cdot (2\,x^3 - 3\,x^2 + 2\,x) = 2\,x^4 - 3\,x^3 + 2\,x^2 \\ & [9] \quad (3\,x^3 + 2\,x^2) \cdot (2\,x^3 - 3\,x^2 - 3\,x) = 6\,x^6 - 5\,x^5 - 15\,x^4 - 6\,x^3 \\ & [10] \quad (4\,x) \cdot (-x^3 - 4\,x^2 - 4\,x) = -4\,x^4 - 16\,x^3 - 16\,x^2 \\ & [11] \quad (-x^3 - x^2) \cdot (4\,x^2) = -4\,x^5 - 4\,x^4 \\ & [12] \quad (-x^3) \cdot (4\,x^3 - 3\,x) = -4\,x^6 + 3\,x^4 \\ & [13] \quad (2\,x^2 - 6\,x) \cdot (-2\,x^2) = -4\,x^4 + 12\,x^3 \\ & [14] \quad (3\,x^3 - 4\,x^2) \cdot (-2\,x^3 - 7\,x) = -6\,x^6 + 8\,x^5 - 21\,x^4 + 28\,x^3 \\ & [15] \quad (4\,x^3 - x^2) \cdot (3\,x^3 - 3\,x^2) = -3\,x^5 + 6\,x^4 - 4\,x^3 - 8\,x^2 \\ & [17] \quad (-x^2 + x) \cdot (3\,x^3 - 3\,x^2) = -3\,x^5 + 6\,x^4 - 3\,x^3 \\ & [18] \quad (-4\,x^2 + 3\,x) \cdot (-6\,x^3 - 4\,x) = 24\,x^5 - 18\,x^4 + 16\,x^3 - 12\,x^2 \\ & [19] \quad (-2\,x^3 - 4\,x^2) \cdot (x^3 + 2\,x^2 - 2\,x) = -2\,x^6 - 8\,x^5 - 4\,x^4 + 8\,x^3 \\ & [20] \quad (-x^3 + 4\,x) \cdot (-3\,x^3 + x) = 3\,x^6 - 13\,x^4 + 4\,x^2 \end{aligned}$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x^2y^2-2\,xy)\cdot(-3\,xy^2+3\,xy) = -12\,x^3y^4+12\,x^3y^3+6\,x^2y^3-6\,x^2y^2 \\ &[2] \quad (-xy)\cdot(-2\,x^2y^2-x^2y+2\,xy) = 2\,x^3y^3+x^3y^2-2\,x^2y^2 \\ &[3] \quad (-4\,x^2y^2+2\,x^2y)\cdot(xy^2) = -4\,x^3y^4+2\,x^3y^3 \\ &[4] \quad (4\,xy^2+3\,xy)\cdot(2\,xy^2+xy) = 8\,x^2y^4+10\,x^2y^3+3\,x^2y^2 \\ &[5] \quad (-3\,xy^2-xy)\cdot(-2\,x^2y+2\,xy^2+xy) = 6\,x^3y^3-6\,x^2y^4+2\,x^3y^2-5\,x^2y^3-x^2y^2 \\ &[6] \quad (2\,x^2y^2-2\,xy)\cdot(-4\,x^2y+2\,xy^2-2\,xy) = -8\,x^4y^3+4\,x^3y^4-4\,x^3y^3+8\,x^3y^2-4\,x^2y^3+4\,x^2y^2 \\ &[7] \quad (x^2y^2+2\,xy^2)\cdot(x^2y^2+3\,xy) = x^4y^4+2\,x^3y^4+3\,x^3y^3+6\,x^2y^3 \end{aligned}$$