1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 4x^4 - 2x^2 + -x^4 - 4x^3 - 2x^2 + -3x^6 - x^5 + 4x^4 = -3x^6 - x^5 + 7x^4 - 4x^3 - 4x^2 \\ [2] \quad x^4 - 3x + -2x^6 + x^3 + -4x^4 + x^2 - x = -2x^6 - 3x^4 + x^3 + x^2 - 4x \\ [3] \quad -3x^5 - x^3 + 4x^2 + (-3x^6 + 4x^4 - 4x^2) + (-3x^5 + 2x^3 + 2x) = -3x^6 - 6x^5 + 4x^4 + x^3 + 2x \\ [4] \quad 4x^3 + x^2 + 6x^4 + 4x^2 + -4x^5 - 2x^4 = -4x^5 + 4x^4 + 4x^3 + 5x^2 \\ [5] \quad 3x^6 + x^4 + 4x + -2x^5 + 3x^4 + 3x^2 + (-5x^3 + 4x) = 3x^6 - 2x^5 + 4x^4 - 5x^3 + 3x^2 + 8x \\ [6] \quad 4x^5 - x^3 - x^2 + -4x^4 + 3x^2 + 4x^3 = 4x^5 - 4x^4 + 3x^3 + 2x^2 \\ [7] \quad 2x^5 - x^4 - x + -4x^5 + x^3 - 3x + 5x^4 - 3x^2 = -2x^5 + 4x^4 + x^3 - 3x^2 - 4x \\ [8] \quad 4x^4 - 4x^3 - 2x^2 + -4x^6 + 2x^5 + 4x^4 + 3x^4 + 2x^2 = -4x^6 + 2x^5 + 11x^4 - 4x^3 \\ [9] \quad x^3 + 2x^2 - 3x + -4x^5 - 2x^4 + 2x^3 + 4x^6 + 3x^5 + x = 4x^6 - x^5 - 2x^4 + 3x^3 + 2x^2 - 2x \\ \end{cases}$$

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Ejercicio 2: Realiza las siguientes sumas de polinomios:

[10] $4x^4 + x^2 + 3x^5 - 2x^3 = 3x^5 + 4x^4 - 2x^3 + x^2$

$$[1] \quad 0+0+0=0 \\ [2] \quad 4x^2y+-3x^2y^2-3x^2y+3xy^2+(-2x^2y-7xy^2)=-3x^2y^2-x^2y-4xy^2 \\ [3] \quad 14x^2y^2-12x^2y+-4x^2y^2+4x^2y+8xy^2+-2x^2y^2+2xy^2+4xy=8x^2y^2-8x^2y+10xy^2+4xy \\ [4] \quad 6x^2y^2+6xy+36x^2y^2+6xy^2+3x^2y^2+39xy=45x^2y^2+6xy^2+45xy \\ [5] \quad 12x^2y+44xy+16xy^2-16xy+-16x^2y^2-52xy^2=-16x^2y^2+12x^2y-36xy^2+28xy \\ [6] \quad -20x^2y^2+75x^2y-20xy+(-25x^2y^2+20x^2y+20xy^2)+(-70xy^2+75xy)=-45x^2y^2+95x^2y-50xy^2+55xy \\ [7] \quad 12x^2y+72xy^2-12xy+-108x^2y^2+36x^2y-36xy^2+(-6x^2y+108xy^2+144xy)=-108x^2y^2+42x^2y+144xy^2+132xy \\ [8] \quad -112x^2y^2-147x^2y+(-28xy^2)+(-28x^2y+28xy^2)=-112x^2y^2-175x^2y-128xy \\ [9] \quad 40x^2y^2+-128x^2y^2+8x^2y-128xy+(-144x^2y^2)=-232x^2y^2+8x^2y-128xy \\ [10] \quad 162x^2y^2-27xy^2+-162x^2y+27xy^2+324xy+45x^2y+36xy=162x^2y^2-117x^2y+360xy \\ [10] \quad 162x^2y^2-27xy^2+162x^2y+27xy^2+324xy+45x^2y+36xy=162x^2y^2-117x^2y+360xy \\ [10] \quad 162x^2y^2-27xy^2+162x^2y+27xy^2+324xy+45x^2y+36xy=162x^2y^2-117x^2y+360xy \\ [10] \quad 162x^2y^2-27xy^2+162x^2y+27xy^2+324xy+45x^2y+36xy=162x^2y^2-117x^2y+360xy \\ [10] \quad 162x^2y^2-27xy^2+360xy \\ [10] \quad 162x^2y^2-27xy^2+360x^2+360x^2 \\ [10] \quad 162x^2y^2-27xy^2+360x^2 \\ [10] \quad 162x^2y^2-27xy^2+36$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y + x^2y + 4\,xy - (x^2y^2) = -x^2y^2 - x^2y + 4\,xy \\ &[3] \quad 2\,x^2y \, + \,12\,xy^2 \, + \,16\,xy \, + \,12\,x^2y^2 \, + \,6\,x^2y \, - \,(-8\,x^2y^2 \, - \,8\,xy^2 \, + \,4\,xy) \, = \\ &20\,x^2y^2 + 8\,x^2y \, + \,20\,xy^2 \, + \,12\,xy \\ &[4] \quad -9\,x^2y \, - \,27\,xy \, - \,(12\,x^2y \, + \,36\,xy^2 \, - \,27\,xy) \, + \,(-3\,x^2y^2 \, - \,9\,x^2y \, - \,18\,xy) \, = \\ &-3\,x^2y^2 \, - \,30\,x^2y \, - \,36\,xy^2 \, - \,18\,xy \end{aligned}$$

$$\begin{aligned} & [5] \quad -112\,x^2y^2 - 4\,x^2y + 16\,x^2y^2 + 96\,xy^2 - (48\,x^2y^2 - 4\,x^2y + 32\,xy) = -144\,x^2y^2 + \\ & 96\,xy^2 - 32\,xy \\ & [6] \quad -25\,x^2y^2 + 10\,x^2y - 50\,xy + -25\,x^2y^2 + 25\,x^2y - 15\,xy^2 - (15\,x^2y + 50\,xy) = \\ & -50\,x^2y^2 + 20\,x^2y - 15\,xy^2 - 100\,xy \\ & [7] \quad -144\,x^2y^2 + 6\,x^2y + 12\,xy^2 - (12\,xy^2) + (24\,x^2y^2 + 24\,x^2y + 108\,xy) = \\ & -120\,x^2y^2 + 30\,x^2y + 108\,xy \\ & [8] \quad -147\,x^2y + 7\,xy + 7\,x^2y^2 - 196\,xy^2 - 14\,xy - (21\,x^2y^2 + 147\,x^2y + 14\,xy) = \\ & -14\,x^2y^2 - 294\,x^2y - 196\,xy^2 - 21\,xy \\ & [9] \quad 16\,x^2y^2 - 64\,x^2y + 32\,xy^2 + -216\,xy^2 - (-256\,x^2y^2 + 192\,xy) = 272\,x^2y^2 - \\ & 64\,x^2y - 184\,xy^2 - 192\,xy \\ & [10] \quad 162\,x^2y + 324\,xy^2 + 18\,xy - (243\,x^2y^2 + 27\,x^2y + 324\,xy^2) + (-72\,x^2y^2 + 36\,xy^2) = -315\,x^2y^2 + 135\,x^2y + 36\,xy^2 + 18\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (bxyz) \cdot (-2\,b^3x^3y^2z^3) = -2\,b^4x^4y^3z^4 \\ &[3] \quad (4\,b^3x^2y^2z^2) \cdot (-12\,bxy^3z) = -48\,b^4x^3y^5z^3 \\ &[4] \quad (-3\,b^2x^2y^2z^3) \cdot (108\,b^3xy^3z^2) = -324\,b^5x^3y^5z^5 \\ &[5] \quad (-64\,b^3xy^2z) \cdot (64\,b^3x^2yz^3) = -4096\,b^6x^3y^3z^4 \\ &[6] \quad (-250\,b^2xy^2z) \cdot (15\,b^3x^2y^3z^2) = -3750\,b^5x^3y^5z^3 \\ &[7] \quad (6\,b^3xyz^2) \cdot (-864\,b^2xy^3z) = -5184\,b^5x^2y^4z^3 \\ &[8] \quad (-28\,bx^3y^2z^3) \cdot (-196\,b^3x^2y^3z) = 5488\,b^4x^5y^5z^4 \\ &[9] \quad (8\,b^3x^3yz) \cdot (-512\,bxyz) = -4096\,b^4x^4y^2z^2 \\ &[10] \quad (-729\,b^2xy^2z^2) \cdot (-1458\,b^3xy^2z^2) = 1062882\,b^5x^2y^4z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (x) \cdot (-3\,x^2 + 5\,x) = -3\,x^3 + 5\,x^2 \\ &[2] \quad (-2\,x^2) \cdot (-7\,x^2 - x) = 14\,x^4 + 2\,x^3 \\ &[3] \quad (3\,x^2) \cdot (3\,x^2 - 3\,x) = 9\,x^4 - 9\,x^3 \\ &[4] \quad (2\,x^2) \cdot (-2\,x) = -4\,x^3 \\ &[5] \quad (-3\,x^2) \cdot (7\,x^2 - 2\,x) = -21\,x^4 + 6\,x^3 \\ &[6] \quad (x^2) \cdot (x^2 - 3\,x) = x^4 - 3\,x^3 \\ &[7] \quad (4\,x^2) \cdot (6\,x) = 24\,x^3 \\ &[8] \quad (-3\,x^2) \cdot (-2\,x^2 - 2\,x) = 6\,x^4 + 6\,x^3 \\ &[9] \quad (x^2) \cdot (x^2 - 4\,x) = x^4 - 4\,x^3 \\ &[10] \quad (-x) \cdot (6\,x^2 - 3\,x) = -6\,x^3 + 3\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x) \cdot (4x^2) = 8x^3$$

[2] $(-2x) \cdot (4x^2 + x) = -8x^3 - 2x^2$
[3] $(x^2 + x) \cdot (-2x^2 + 4x) = -2x^4 + 2x^3 + 4x^2$
[4] $(2x^2) \cdot (-3x^2 - 5x) = -6x^4 - 10x^3$

[5]
$$(-x^2 - 3x) \cdot (-3x^2) = 3x^4 + 9x^3$$

[6]
$$(-3x) \cdot (2x^2 + 2x) = -6x^3 - 6x^2$$

[7]
$$(-8x) \cdot (-4x^2 + 4x) = 32x^3 - 32x^2$$

[8]
$$(-7x^2) \cdot (8x^2 - 2x) = -56x^4 + 14x^3$$

[9]
$$(-2x^2) \cdot (-2x^2 - 7x) = 4x^4 + 14x^3$$

[10]
$$(4x^2 + 4x) \cdot (-4x^2 + 3x) = -16x^4 - 4x^3 + 12x^2$$

[11]
$$(-4x^2) \cdot (-x^2) = 4x^4$$

[12]
$$(4x) \cdot (3x^2 + 6x) = 12x^3 + 24x^2$$

[13]
$$(-4x^2 + 3x) \cdot (5x^2 - x) = -20x^4 + 19x^3 - 3x^2$$

[14]
$$(-3x^2 + x) \cdot (3x^2 + x) = -9x^4 + x^2$$

[15]
$$(4x^2 + 4x) \cdot (7x^2 - 3x) = 28x^4 + 16x^3 - 12x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x) \cdot (5x^2 + 2x) = 5x^3 + 2x^2$$

[2]
$$(0) \cdot (x^3 - 4x^2 - 5x) = 0$$

[3]
$$(-x^2-2x)\cdot(-4x^3-x^2-2x)=4x^5+9x^4+4x^3+4x^2$$

[4]
$$(-2x^3 + x^2 - 2x) \cdot (3x^2 - 2x) = -6x^5 + 7x^4 - 8x^3 + 4x^2$$

[5]
$$(-3x^3+x)\cdot(-x^3-3x^2+x)=3x^6+9x^5-4x^4-3x^3+x^2$$

[6]
$$(2x^3 - 4x) \cdot (-3x^3 - 2x^2 - x) = -6x^6 - 4x^5 + 10x^4 + 8x^3 + 4x^2$$

[7]
$$(-4x^3 - x^2) \cdot (-8x^3 + x) = 32x^6 + 8x^5 - 4x^4 - x^3$$

[8]
$$(0) \cdot (-4x^3 + 2x^2 + 7x) = 0$$

[9]
$$(-x^2) \cdot (4x^3 + 2x^2 - 4x) = -4x^5 - 2x^4 + 4x^3$$

[10]
$$(-6x^3 - 4x^2) \cdot (3x^3 + 3x^2 - 3x) = -18x^6 - 30x^5 + 6x^4 + 12x^3$$

[11]
$$(-3x^3 - 2x) \cdot (-3x^3 - x^2 + 2x) = 9x^6 + 3x^5 + 2x^3 - 4x^2$$

[12]
$$(4x^2) \cdot (4x^3 + 4x^2 - 5x) = 16x^5 + 16x^4 - 20x^3$$

[13]
$$(-4x^3) \cdot (-2x^3 - 3x^2 - 2x) = 8x^6 + 12x^5 + 8x^4$$

[14]
$$(-3x^2 - 4x) \cdot (x^3 + 11x^2) = -3x^5 - 37x^4 - 44x^3$$

[15]
$$(2x^3) \cdot (4x^3 - 3x^2) = 8x^6 - 6x^5$$

[16]
$$(x^2 - 4x) \cdot (x^2) = x^4 - 4x^3$$

[17]
$$(-3x^3 + 4x) \cdot (4x^3 + 5x) = -12x^6 + x^4 + 20x^2$$

[18]
$$(3x^3 - 2x^2) \cdot (3x^3 + x^2 - 2x) = 9x^6 - 3x^5 - 8x^4 + 4x^3$$

[19]
$$(-2x) \cdot (7x^3 - x^2) = -14x^4 + 2x^3$$

[20]
$$(x^3 + 2x) \cdot (8x^3 + 4x^2 - 4x) = 8x^6 + 4x^5 + 12x^4 + 8x^3 - 8x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-5x^2y^2) \cdot (4x^2y^2 + x^2y - 4xy^2) = -20x^4y^4 - 5x^4y^3 + 20x^3y^4$$

[2]
$$(-4x^2y + 3xy) \cdot (x^2y^2 + 5xy^2) = -4x^4y^3 - 17x^3y^3 + 15x^2y^3$$

[3]
$$(x^2y + 3xy^2) \cdot (4x^2y^2 - xy^2 - xy) = 4x^4y^3 + 12x^3y^4 - x^3y^3 - 3x^2y^4 - x^3y^2 - 3x^2y^3$$

[4]
$$(-2xy^2 - 3xy) \cdot (4x^2y) = -8x^3y^3 - 12x^3y^2$$

[5]
$$(2xy^2 + 4xy) \cdot (-4x^2y - 2xy^2) = -8x^3y^3 - 4x^2y^4 - 16x^3y^2 - 8x^2y^3$$

$$\begin{aligned} & [6] \quad (-4\,xy^2+2\,xy)\cdot(3\,x^2y^2+2\,x^2y-xy^2) = -12\,x^3y^4-2\,x^3y^3+4\,x^2y^4+4\,x^3y^2-2\,x^2y^3 \\ & [7] \quad (-5\,xy)\cdot(x^2y^2+4\,xy) = -5\,x^3y^3-20\,x^2y^2 \end{aligned}$$