## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad -x^5 - 2x^2 + 4x + (-2x^4 + 3x^2 - 4x) + (-x^4 - 2x) = -x^5 - 3x^4 + x^2 - 2x$$

$$[2] \quad 2x^6 - x^4 + x^2 + x + -x^6 - 2x^3 + 3x^2 = x^6 - x^4 - 2x^3 + 4x^2 + x$$

$$[3] \quad 7x^2 + -4x^5 - 3x^3 + 2x^2 + 2x^6 - 3x^4 = 2x^6 - 4x^5 - 3x^4 - 3x^3 + 9x^2$$

$$[4] \quad 4x^3 + -x^4 + 3x + 3x^6 - 4x^2 = 3x^6 - x^4 + 4x^3 - 4x^2 + 3x$$

$$[5] \quad 3x^4 + 3x^3 + 3x^2 + -4x^6 - 4x^4 + x + -x^4 - 6x^3 = -4x^6 - 2x^4 - 3x^3 + 3x^2 + x$$

$$[6] \quad x^5 - 2x^4 + 2x^2 + 2x^6 - 4x^5 + 4x + -2x^6 - 4x = -3x^5 - 2x^4 + 2x^2$$

$$[7] \quad x^5 + 3x^2 - 4x + -x^6 + 2x^4 - x^3 + -x^6 - 6x^4 = -2x^6 + x^5 - 4x^4 - x^3 + 3x^2 - 4x$$

$$[8] \quad -4x^3 - 2x^2 + 3x + (-3x^5 - 2x^3) + (-x^5 + x^4 + 4x^3) = -4x^5 + x^4 - 2x^3 - 2x^2 + 3x$$

$$[9] \quad 4x^6 + x^5 + 2x^6 - 3x^5 + -2x^4 - x^3 + 3x = 6x^6 - 2x^5 - 2x^4 - x^3 + 3x$$

[10]  $3x^6 + 2x^4 - 3x^2 + -2x^4 + 2x^2 - 3x + (-3x^6 + x^4) = x^4 - x^2 - 3x$ 

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0 + 0 + 0 = 0 \\ & [2] \quad -2 \, x^2 y + x y^2 + (-8 \, x^2 y^2 - 3 \, x^2 y) + (-2 \, x^2 y + 3 \, x y^2 - x y) = -8 \, x^2 y^2 - 7 \, x^2 y + 4 \, x y^2 - x y \\ & [3] \quad 4 \, x^2 y^2 - 8 \, x y^2 + 4 \, x y + -8 \, x^2 y - 16 \, x y^2 - 2 \, x y + 6 \, x^2 y = 4 \, x^2 y^2 - 2 \, x^2 y - 24 \, x y^2 + 2 \, x y \\ & [4] \quad 36 \, x^2 y - 9 \, x y^2 + 36 \, x y + -15 \, x y^2 + 27 \, x^2 y^2 - 9 \, x^2 y + 9 \, x y^2 = 27 \, x^2 y^2 + 27 \, x^2 y - 15 \, x y^2 + 36 \, x y \\ & [5] \quad 36 \, x y^2 + 12 \, x y + 48 \, x^2 y^2 - 16 \, x^2 y + 48 \, x^2 y^2 - 8 \, x^2 y - 64 \, x y^2 = 96 \, x^2 y^2 - 24 \, x^2 y - 28 \, x y^2 + 12 \, x y \\ & [6] \quad 90 \, x y + 100 \, x^2 y^2 + 10 \, x y + -30 \, x y^2 - 75 \, x y = 100 \, x^2 y^2 - 30 \, x y^2 + 25 \, x y \\ & [7] \quad 72 \, x^2 y^2 + 72 \, x^2 y + 18 \, x y + -12 \, x^2 y + 6 \, x y^2 + 36 \, x y + -72 \, x^2 y^2 + 72 \, x^2 y + 24 \, x y^2 = 132 \, x^2 y + 30 \, x y^2 + 54 \, x y \\ & [8] \quad 91 \, x^2 y - 196 \, x y^2 + -14 \, x^2 y - 21 \, x y + 49 \, x^2 y + 7 \, x y = 126 \, x^2 y - 196 \, x y^2 - 14 \, x y \\ & [9] \quad 272 \, x^2 y^2 + 256 \, x^2 y + -128 \, x y + -40 \, x^2 y - 128 \, x y = 272 \, x^2 y^2 + 216 \, x^2 y - 256 \, x y \\ & [10] \quad 153 \, x^2 y^2 + 243 \, x^2 y + -36 \, x^2 y^2 + 162 \, x^2 y - 27 \, x y^2 + -153 \, x^2 y - 243 \, x y^2 = 117 \, x^2 y^2 + 252 \, x^2 y - 270 \, x y^2 \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 3\,x^2y + xy^2 + 4\,xy + -x^2y^2 - 3\,x^2y + 3\,xy^2 - (-3\,x^2y - 4\,xy^2) = -x^2y^2 + 3\,x^2y + 8\,xy^2 + 4\,xy \\ &[3] \quad -8\,x^2y^2 + 4\,x^2y + 4\,xy + -4\,x^2y^2 - 20\,xy - (4\,x^2y^2 + 8\,xy^2 - 16\,xy) = -16\,x^2y^2 + 4\,x^2y - 8\,xy^2 \\ &[4] \quad -6\,x^2y + 9\,xy^2 - (6\,x^2y^2 - 18\,x^2y + 36\,xy) + (12\,x^2y^2 - 3\,xy) = 6\,x^2y^2 + 12\,x^2y + 9\,xy^2 - 39\,xy \\ &[5] \quad -32\,x^2y^2 - 64\,xy^2 + -48\,x^2y^2 + 12\,xy^2 - 8\,xy - (-52\,x^2y - 4\,xy) = -80\,x^2y^2 + 52\,x^2y - 52\,xy^2 - 4\,xy \end{aligned}$$

$$\begin{aligned} & [6] \quad 25\,x^2y + 60\,xy + -5\,x^2y^2 - 15\,xy^2 + 75\,xy - \left(-50\,xy^2 - 5\,xy\right) = -5\,x^2y^2 + \\ & 25\,x^2y + 35\,xy^2 + 140\,xy \\ & [7] \quad 18\,x^2y^2 + 138\,x^2y - \left(-18\,x^2y^2 + 6\,x^2y + 24\,xy\right) + \left(18\,x^2y + 66\,xy\right) = 36\,x^2y^2 + \\ & 150\,x^2y + 42\,xy \\ & [8] \quad 196\,x^2y^2 - 112\,x^2y + 343\,x^2y - 49\,xy - \left(-147\,x^2y^2 - 147\,xy^2 + 147\,xy\right) = \\ & 343\,x^2y^2 + 231\,x^2y + 147\,xy^2 - 196\,xy \\ & [9] \quad 24\,x^2y + 128\,xy - \left(296\,xy\right) = 24\,x^2y - 168\,xy \\ & [10] \quad 243\,x^2y^2 + 279\,xy^2 - \left(-243\,x^2y + 36\,xy^2 + 162\,xy\right) + \left(162\,x^2y^2 - 216\,xy^2\right) = \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

 $405 x^2 y^2 + 243 x^2 y + 27 x y^2 - 162 x y$ 

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-2\,b^3x^3y^2z^3) \cdot (-2\,b^2xy^3z) = 4\,b^5x^4y^5z^4 \\ &[3] \quad (-16\,b^2x^2y^3z) \cdot (-2\,b^3x^2y^2z) = 32\,b^5x^4y^5z^2 \\ &[4] \quad (-54\,bx^3y^2z^2) \cdot (108\,b^2x^3yz^3) = -5832\,b^3x^6y^3z^5 \\ &[5] \quad (-12\,b^3x^2y^2z^3) \cdot (-64\,bx^2y^3z^2) = 768\,b^4x^4y^5z^5 \\ &[6] \quad (-10\,b^3x^2yz) \cdot (-15\,bx^3yz^3) = 150\,b^4x^5y^2z^4 \\ &[7] \quad (-6\,b^2x^2yz^2) \cdot (18\,bxyz) = -108\,b^3x^3y^2z^3 \\ &[8] \quad (1372\,b^2x^2y^3z) \cdot (-147\,b^2x^2y^3z^2) = -201684\,b^4x^4y^6z^3 \\ &[9] \quad (-24\,b^3xy^3z) \cdot (24\,b^3x^3yz^2) = -576\,b^6x^4y^4z^3 \\ &[10] \quad (-18\,b^2x^3y^3z^3) \cdot (2916\,bxyz^3) = -52488\,b^3x^4y^4z^6 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x)\cdot(-2\,x^2-4\,x) = -8\,x^3-16\,x^2 \\ &[2] \quad (-2\,x)\cdot(4\,x^2+x) = -8\,x^3-2\,x^2 \\ &[3] \quad (x^2)\cdot(-2\,x^2+3\,x) = -2\,x^4+3\,x^3 \\ &[4] \quad (-4\,x)\cdot(6\,x^2+4\,x) = -24\,x^3-16\,x^2 \\ &[5] \quad (-4\,x)\cdot(-4\,x^2-2\,x) = 16\,x^3+8\,x^2 \\ &[6] \quad (2\,x)\cdot(3\,x) = 6\,x^2 \\ &[7] \quad (-3\,x^2)\cdot(4\,x^2+3\,x) = -12\,x^4-9\,x^3 \\ &[8] \quad (-2\,x)\cdot(-3\,x^2-4\,x) = 6\,x^3+8\,x^2 \\ &[9] \quad (x)\cdot(-x^2+2\,x) = -x^3+2\,x^2 \\ &[10] \quad (-x)\cdot(-x^2+6\,x) = x^3-6\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(x^2) \cdot (-7x) = -7x^3$$
  
[2]  $(5x) \cdot (-6x^2 + 4x) = -30x^3 + 20x^2$   
[3]  $(x^2) \cdot (4x^2 - 2x) = 4x^4 - 2x^3$   
[4]  $(-2x^2 + x) \cdot (-2x^2 - 5x) = 4x^4 + 8x^3 - 5x^2$   
[5]  $(x^2) \cdot (-x^2 - 3x) = -x^4 - 3x^3$   
[6]  $(-2x) \cdot (3x^2 - 4x) = -6x^3 + 8x^2$   
[7]  $(-4x^2 + 4x) \cdot (-4x^2) = 16x^4 - 16x^3$ 

[8] 
$$(2x^2 + 2x) \cdot (-4x) = -8x^3 - 8x^2$$

[9] 
$$(3x^2) \cdot (-x) = -3x^3$$

[10] 
$$(-4x^2 + x) \cdot (2x) = -8x^3 + 2x^2$$

[11] 
$$(5x) \cdot (-2x^2 - x) = -10x^3 - 5x^2$$

[12] 
$$(5x^2) \cdot (-x^2) = -5x^4$$

[13] 
$$(3x^2) \cdot (-3x^2 + 3x) = -9x^4 + 9x^3$$

[14] 
$$(-4x) \cdot (-2x^2 + 4x) = 8x^3 - 16x^2$$

[15] 
$$(0) \cdot (-3x^2 + x) = 0$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(2x^2) \cdot (-3x) = -6x^3$$

[2] 
$$(-2x^2) \cdot (-5x^2 - x) = 10x^4 + 2x^3$$

[3] 
$$(5x) \cdot (x^3 + 4x) = 5x^4 + 20x^2$$

[4] 
$$(-2x^3 + 5x^2) \cdot (-x^3 - 3x) = 2x^6 - 5x^5 + 6x^4 - 15x^3$$

[5] 
$$(3x) \cdot (-2x^3 + x) = -6x^4 + 3x^2$$

[6] 
$$(-2x^3 - 4x) \cdot (2x^3 + 2x^2) = -4x^6 - 4x^5 - 8x^4 - 8x^3$$

[7] 
$$(-3x^3 - 3x^2) \cdot (-8x^3 + x) = 24x^6 + 24x^5 - 3x^4 - 3x^3$$

[8] 
$$(x^3 - x^2) \cdot (-5x^3 + 4x^2) = -5x^6 + 9x^5 - 4x^4$$

[9] 
$$(0) \cdot (4x^3 - x) = 0$$

[10] 
$$(-x^2 + 4x) \cdot (5x) = -5x^3 + 20x^2$$

[11] 
$$(2x^3 + 4x^2) \cdot (-x^2 - 8x) = -2x^5 - 20x^4 - 32x^3$$

[12] 
$$(-3x^2 + x) \cdot (2x^3 + x^2 + 3x) = -6x^5 - x^4 - 8x^3 + 3x^2$$

[13] 
$$(x) \cdot (4x^3 + x) = 4x^4 + x^2$$

[14] 
$$(4x^3 + x) \cdot (-2x^3 - x^2 + 2x) = -8x^6 - 4x^5 + 6x^4 - x^3 + 2x^2$$

[15] 
$$(-3x^3 + 3x) \cdot (-3x^3 - 4x^2 + 3x) = 9x^6 + 12x^5 - 18x^4 - 12x^3 + 9x^2$$

[16] 
$$(2x^3) \cdot (2x^3 + 5x^2) = 4x^6 + 10x^5$$

[17] 
$$(-x^3 + x) \cdot (3x^3 + x) = -3x^6 + 2x^4 + x^2$$

[18] 
$$(4x^3 - x) \cdot (-4x^3 - 3x^2) = -16x^6 - 12x^5 + 4x^4 + 3x^3$$

[19] 
$$(8x) \cdot (2x^3 + x^2 - 3x) = 16x^4 + 8x^3 - 24x^2$$

[20] 
$$(3x) \cdot (4x^3 + x^2 - 2x) = 12x^4 + 3x^3 - 6x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(2x^2y - 4xy) \cdot (xy^2 - 4xy) = 2x^3y^3 - 8x^3y^2 - 4x^2y^3 + 16x^2y^2$$

[2] 
$$(-4x^2y^2 - x^2y) \cdot (-4x^2y^2 - 3x^2y - 4xy^2) = 16x^4y^4 + 16x^4y^3 + 16x^3y^4 + 3x^4y^2 + 4x^3y^3$$

[3] 
$$(x^2y^2 + 2xy) \cdot (2x^2y - xy^2) = 2x^4y^3 - x^3y^4 + 4x^3y^2 - 2x^2y^3$$

[4] 
$$(0) \cdot (3x^2y^2 - 4xy^2) = 0$$

[5] 
$$(-3xy^2) \cdot (2x^2y^2 + x^2y - xy^2) = -6x^3y^4 - 3x^3y^3 + 3x^2y^4$$

[6] 
$$(-xy) \cdot (-3x^2y - 2xy) = 3x^3y^2 + 2x^2y^2$$

[7] 
$$(2xy^2-xy)\cdot(-x^2y^2+4x^2y+3xy^2) = -2x^3y^4+9x^3y^3+6x^2y^4-4x^3y^2-3x^2y^3$$