1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$4x^4 - 5x^3 + x^4 + 3x^2 + x + 4x^5 + 2x^4 - 2x^3 = 4x^5 + 7x^4 - 7x^3 + 3x^2 + x$$

[2] $2x^2 + 6x + -3x^6 - 2x^5 - 4x^2 + -3x^4 + x^2 = -3x^6 - 2x^5 - 3x^4 - x^2 + 6x$
[3] $x^3 + x^5 - x^4 - 2x + -3x^6 - 3x^3 + 2x^2 = -3x^6 + x^5 - x^4 - 2x^3 + 2x^2 - 2x$
[4] $2x + -2x^6 - 4x^5 - 4x^3 + 3x^6 - x^5 + 4x^3 = x^6 - 5x^5 + 2x$
[5] $3x^3 + 2x^2 - 2x + 2x^6 - x^2 - 3x + -4x^6 + x^4 = -2x^6 + x^4 + 3x^3 + x^2 - 5x$
[6] $3x^6 + x^4 + x^6 + 2x^4 - 2x^2 + 4x^6 + 2x^4 - 3x^3 = 8x^6 + 5x^4 - 3x^3 - 2x^2$
[7] $4x^5 - x + -3x^2 + (-4x^6 + 3x^5 + 4x) = -4x^6 + 7x^5 - 3x^2 + 3x$
[8] $x^5 - 3x + -x^2 + 5x + (-3x^6 - 2x^3) = -3x^6 + x^5 - 2x^3 - x^2 + 2x$
[9] $4x^6 - x^5 - 3x + -x^5 + 3x^4 + 3x + 2x^4 + x^3 + 2x^2 = 4x^6 - 2x^5 + 5x^4 + x^3 + 2x^2$
[10] $x^6 - 4x^4 + -2x^6 - x^3 - x + (-x^6 - x^5 - 2x^4) = -2x^6 - x^5 - 6x^4 - x^3 - x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0$$

$$[2] \quad 2x^2y^2+6xy^2+-3x^2y^2+2xy^2-3xy+-xy^2=-x^2y^2+7xy^2-3xy$$

$$[3] \quad 16xy^2+-8x^2y^2-4xy+-8x^2y^2-4x^2y-12xy^2=-16x^2y^2-4x^2y+4xy^2-4xy$$

$$[4] \quad -36x^2y^2+3x^2y-36xy+(-27x^2y^2+12xy^2)+(-6x^2y^2+9x^2y+27xy^2)=-69x^2y^2+12x^2y+39xy^2-36xy$$

$$[5] \quad 48x^2y-16xy+-8xy^2+68xy+48x^2y^2-12x^2y+64xy=48x^2y^2+36x^2y-8xy^2+116xy$$

$$[6] \quad 15x^2y^2+10xy^2-15xy+90x^2y^2+10x^2y+10x^2y^2-10x^2y=115x^2y^2+10xy^2-15xy$$

$$[7] \quad -108x^2y+24xy^2-24xy+(-36x^2y-12xy^2+12xy)+(-144x^2y^2)=-144x^2y^2-144x^2y+12xy^2-12xy$$

$$[8] \quad 245x^2y^2+28x^2y+-147x^2y-70xy+(-21x^2y^2-98x^2y-21xy^2)=224x^2y^2-217x^2y-21xy^2-70xy$$

$$[9] \quad 24xy^2+128xy+-40x^2y+24xy^2+80xy^2=-40x^2y+128xy^2+128xy$$

$$[10] \quad 9x^2y^2+18xy^2-9xy+-27x^2y^2-81x^2y+324xy^2+-81x^2y^2-81x^2y-9xy=-99x^2y^2-162x^2y+342xy^2-18xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 3\,xy + -3\,x^2y^2 + 4\,x^2y - xy^2 - (x^2y + 3\,xy^2 - 2\,xy) = -3\,x^2y^2 + 3\,x^2y - 4\,xy^2 + 5\,xy \\ &[3] \quad -24\,x^2y^2 + 2\,x^2y + 12\,x^2y^2 + 4\,xy^2 + 16\,xy - (-18\,x^2y^2 - 16\,xy^2) = 6\,x^2y^2 + 2\,x^2y + 20\,xy^2 + 16\,xy \\ &[4] \quad 3\,x^2y^2 - 18\,x^2y - 12\,xy^2 - (-21\,x^2y^2 + 36\,xy) + (-72\,x^2y^2 + 9\,xy) = -48\,x^2y^2 - 18\,x^2y - 12\,xy^2 - 27\,xy \\ &[5] \quad -32\,x^2y^2 + 16\,x^2y + 16\,x^2y^2 - 48\,xy - (-68\,x^2y^2 - 8\,xy^2) = 52\,x^2y^2 + 16\,x^2y + 8\,xy^2 - 48\,xy \end{aligned}$$

$$[6] \quad -50\,x^2y^2 - 10\,x^2y + -130\,xy - (-15\,x^2y^2 - 50\,xy^2 + 20\,xy) = -35\,x^2y^2 - 10\,x^2y + 50\,xy^2 - 150\,xy$$

$$[7] \quad -36\,x^2y^2 - 108\,xy^2 + 144\,xy - (-72\,x^2y^2 + 126\,x^2y) + (12\,xy^2 + 24\,xy) = 36\,x^2y^2 - 126\,x^2y - 96\,xy^2 + 168\,xy$$

$$[8] \quad 21\,x^2y^2 + 147\,xy^2 + 196\,xy + 182\,x^2y + 28\,xy^2 - (21\,xy^2 + 7\,xy) = 21\,x^2y^2 + 182\,x^2y + 154\,xy^2 + 189\,xy$$

$$[9] \quad -48\,xy^2 - 256\,xy + -96\,xy^2 + 24\,xy - (-128\,x^2y^2 + 128\,xy) = 128\,x^2y^2 - 144\,xy^2 - 360\,xy$$

$$[10] \quad 81\,x^2y^2 + 27\,xy^2 + 36\,xy - (-18\,xy^2 + 306\,xy) + (-81\,x^2y^2 - 18\,xy^2 - 9\,xy) = 27\,xy^2 - 279\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-2 \, bx^2 y^2 z^3) \cdot (3 \, bx^2 y z^2) = -6 \, b^2 x^4 y^3 z^5 \\ &[3] \quad (-4 \, b^3 x y^3 z^2) \cdot (2 \, b^3 x y^3 z^2) = -8 \, b^6 x^2 y^6 z^4 \\ &[4] \quad (-36 \, bx^2 y z) \cdot (-12 \, bx^3 y z) = 432 \, b^2 x^5 y^2 z^2 \\ &[5] \quad (-64 \, bx y^3 z) \cdot (-16 \, b^3 x y^2 z) = 1024 \, b^4 x^2 y^5 z^2 \\ &[6] \quad (375 \, b^2 x^3 y^3 z) \cdot (-15 \, b^2 x^3 y z) = -5625 \, b^4 x^6 y^4 z^2 \\ &[7] \quad (24 \, b^3 x^2 y^3 z^2) \cdot (108 \, bx^2 y^3 z^2) = 2592 \, b^4 x^4 y^6 z^4 \\ &[8] \quad (-686 \, b^3 x^3 y^2 z) \cdot (98 \, b^2 x^3 y^3 z) = -67228 \, b^5 x^6 y^5 z^2 \\ &[9] \quad (64 \, b^3 x^2 y^3 z^3) \cdot (-192 \, b^2 x^2 y^2 z) = -12288 \, b^5 x^4 y^5 z^4 \\ &[10] \quad (9 \, bx y^2 z) \cdot (-27 \, bx y^3 z^3) = -243 \, b^2 x^2 y^5 z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(3x^2) \cdot (4x^2 + 2x) = 12x^4 + 6x^3$$

[2] $(x) \cdot (-4x^2 - 3x) = -4x^3 - 3x^2$
[3] $(-3x) \cdot (-3x^2 + 6x) = 9x^3 - 18x^2$
[4] $(-3x) \cdot (-4x^2 + 7x) = 12x^3 - 21x^2$
[5] $(3x) \cdot (3x^2 - x) = 9x^3 - 3x^2$
[6] $(-4x) \cdot (-6x^2 - 4x) = 24x^3 + 16x^2$
[7] $(-3x) \cdot (-2x^2 - x) = 6x^3 + 3x^2$
[8] $(3x) \cdot (6x^2) = 18x^3$
[9] $(4x) \cdot (-5x^2 - 4x) = -20x^3 - 16x^2$
[10] $(-3x) \cdot (4x^2 - 3x) = -12x^3 + 9x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-4x^2 + 3x) \cdot (-x^2 - 3x) = 4x^4 + 9x^3 - 9x^2$$

[2] $(x^2 + 4x) \cdot (2x^2 + x) = 2x^4 + 9x^3 + 4x^2$
[3] $(-x^2 - 3x) \cdot (5x^2 - 3x) = -5x^4 - 12x^3 + 9x^2$
[4] $(x^2 - x) \cdot (-5x^2 + 3x) = -5x^4 + 8x^3 - 3x^2$
[5] $(-5x) \cdot (5x) = -25x^2$
[6] $(-2x) \cdot (-x^2 + 2x) = 2x^3 - 4x^2$

[7]
$$(-3x^2) \cdot (-2x^2 - 2x) = 6x^4 + 6x^3$$

[8]
$$(0) \cdot (2x^2 - 3x) = 0$$

[9]
$$(-2x^2 + 2x) \cdot (2x^2 + 5x) = -4x^4 - 6x^3 + 10x^2$$

[10]
$$(x^2 - 4x) \cdot (3x^2 - x) = 3x^4 - 13x^3 + 4x^2$$

[11]
$$(x^2 + 4x) \cdot (4x) = 4x^3 + 16x^2$$

[12]
$$(4x^2 - 2x) \cdot (-6x^2 + 2x) = -24x^4 + 20x^3 - 4x^2$$

[13]
$$(6x) \cdot (5x) = 30x^2$$

[14]
$$(-2x^2 - 2x) \cdot (-x) = 2x^3 + 2x^2$$

[15]
$$(3x^2 - 4x) \cdot (-x^2 + x) = -3x^4 + 7x^3 - 4x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2 + 2x) \cdot (x^2 - 4x) = -2x^4 + 10x^3 - 8x^2$$

[2]
$$(-6x^2) \cdot (-6x) = 36x^3$$

[3]
$$(x^3 + 3x^2) \cdot (-3x^3 + 3x^2) = -3x^6 - 6x^5 + 9x^4$$

[4]
$$(3x^3 + 3x^2) \cdot (-5x^3 + x^2) = -15x^6 - 12x^5 + 3x^4$$

[5]
$$(-4x^2 - 4x) \cdot (-2x^3 - 2x) = 8x^5 + 8x^4 + 8x^3 + 8x^2$$

[6]
$$(-4x^3 - x) \cdot (x^3 + 2x^2) = -4x^6 - 8x^5 - x^4 - 2x^3$$

[7]
$$(-6x^2 - 4x) \cdot (2x^3 - 3x^2 + 4x) = -12x^5 + 10x^4 - 12x^3 - 16x^2$$

[8]
$$(3x^3 + x) \cdot (3x^3 + 2x) = 9x^6 + 9x^4 + 2x^2$$

[9]
$$(7x^2) \cdot (3x^3 - 4x^2 + 3x) = 21x^5 - 28x^4 + 21x^3$$

[10]
$$(2x) \cdot (4x^3 - x^2) = 8x^4 - 2x^3$$

[11]
$$(-2x^2) \cdot (2x^3 - 4x^2 - 2x) = -4x^5 + 8x^4 + 4x^3$$

[12]
$$(2x^3 + 2x) \cdot (2x^3 + 3x^2 + 5x) = 4x^6 + 6x^5 + 14x^4 + 6x^3 + 10x^2$$

[13]
$$(2x^3 - 2x^2 - x) \cdot (2x^3 - 2x^2) = 4x^6 - 8x^5 + 2x^4 + 2x^3$$

[14]
$$(-x^3 + 2x) \cdot (-x^3 - x) = x^6 - x^4 - 2x^2$$

[15]
$$(-3x^2 - x) \cdot (x^2 - 5x) = -3x^4 + 14x^3 + 5x^2$$

[16]
$$(-x^2 - 2x) \cdot (x^3 + 5x) = -x^5 - 2x^4 - 5x^3 - 10x^2$$

[17]
$$(x^2 - 2x) \cdot (-5x^3 - 4x^2 + 4x) = -5x^5 + 6x^4 + 12x^3 - 8x^2$$

[18]
$$(4x^3 - 3x) \cdot (-2x^2 - 4x) = -8x^5 - 16x^4 + 6x^3 + 12x^2$$

[19]
$$(5x) \cdot (5x^2) = 25x^3$$

[20]
$$(-3x^3 + 4x^2) \cdot (-7x^2 - 5x) = 21x^5 - 13x^4 - 20x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2y^2) \cdot (-x^2y^2 + x^2y - 2xy^2) = -x^4y^4 + x^4y^3 - 2x^3y^4$$

[2]
$$(xy^2) \cdot (-x^2y^2 + 3x^2y) = -x^3y^4 + 3x^3y^3$$

[3]
$$(4x^2y + 4xy^2) \cdot (x^2y) = 4x^4y^2 + 4x^3y^3$$

[4]
$$(-3x^2y^2 + xy^2) \cdot (x^2y^2 + x^2y) = -3x^4y^4 - 3x^4y^3 + x^3y^4 + x^3y^3$$

[5]
$$(-4x^2y^2 + 2x^2y) \cdot (6xy^2 - 2xy) = -24x^3y^4 + 20x^3y^3 - 4x^3y^2$$

[5]
$$(-4x^2y^2 + 2x^2y) \cdot (6xy^2 - 2xy) = -24x^3y^4 + 20x^3y^3 - 4x^3y^2$$

[6] $(-3x^2y^2 + x^2y) \cdot (3x^2y^2 - 3x^2y - xy) = -9x^4y^4 + 12x^4y^3 - 3x^4y^2 + 3x^3y^3 - x^3y^2$

[7]
$$(4x^2y^2 - 2xy^2) \cdot (-4x^2y^2 + 3x^2y + 4xy) = -16x^4y^4 + 12x^4y^3 + 8x^3y^4 + 10x^3y^3 - 8x^2y^3$$