1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$x^5 + x^4 - 3x^2 + -2x^6 - x^3 + 2x^6 - 3x^4 - 4x = x^5 - 2x^4 - x^3 - 3x^2 - 4x$$

[2] $4x^4 + 5x^3 + 3x^5 + 2x^3 + 4x^2 + 4x^2 = 3x^5 + 4x^4 + 7x^3 + 8x^2$
[3] $4x^5 + 6x^2 + -4x^6 + 5x^5 + -4x^6 + x^4 - 4x^2 = -8x^6 + 9x^5 + x^4 + 2x^2$
[4] $-4x^6 + 3x^2 - 4x + (-3x^6 - x^2 + 2x) + (-3x^4 + 2x^2) = -7x^6 - 3x^4 + 4x^2 - 2x$
[5] $3x^6 - 3x^2 + 2x + -4x^6 + 2x^2 - 2x + -3x^4 + x^3 + 3x^2 = -x^6 - 3x^4 + x^3 + 2x^2$
[6] $2x^6 + 4x^3 + 4x + 2x^6 - x^4 = 4x^6 - x^4 + 4x^3 + 4x$
[7] $x^4 - 7x + -4x^6 - 2x + -x = -4x^6 + x^4 - 10x$
[8] $-x^4 - 4x^3 - x^2 + (-3x^6 - 2x^4 - 3x^2) + (-4x^6 + 4x^3 + 4x^2) = -7x^6 - 3x^4$
[9] $3x^6 + 2x^4 - 3x + -x^5 + 3x^2 + 6x^4 - 3x = 3x^6 - x^5 + 8x^4 + 3x^2 - 6x$
[10] $2x^5 + x^2 + -x^5 + (-x^5 - 3x) = x^2 - 3x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad x^2y + 4\,xy + -3\,x^2y^2 - 2\,x^2y + 3\,xy^2 - (-4\,x^2y^2 - xy^2 + 3\,xy) = x^2y^2 - x^2y + 4\,xy^2 + xy \\ &[3] \quad -8\,x^2y + -4\,xy^2 - (24\,x^2y) = -32\,x^2y - 4\,xy^2 \\ &[4] \quad 9\,x^2y + 6\,xy - (-3\,xy^2 - 36\,xy) + (6\,xy^2 - 9\,xy) = 9\,x^2y + 9\,xy^2 + 33\,xy \\ &[5] \quad -4\,x^2y^2 + 16\,xy^2 + -112\,x^2y^2 + 64\,xy - (-48\,x^2y - 96\,xy^2) = -116\,x^2y^2 + 48\,x^2y + 112\,xy^2 + 64\,xy \end{aligned}$$

$$[6] \quad -125\,x^2y + 25\,xy^2 + 65\,x^2y - 75\,xy - (-15\,x^2y^2) = 15\,x^2y^2 - 60\,x^2y + 25\,xy^2 - 75\,xy$$

$$[7] \quad 18\,x^2y^2 - 132\,x^2y - (-12\,xy) + (-108\,x^2y - 162\,xy) = 18\,x^2y^2 - 240\,x^2y - 150\,xy$$

$$[8] \quad -7\,xy^2 + 49\,xy + 7\,x^2y^2 + 35\,x^2y - (196\,xy^2 - 70\,xy) = 7\,x^2y^2 + 35\,x^2y - 203\,xy^2 + 119\,xy$$

$$[9] \quad -8\,x^2y^2 - 8\,x^2y - 8\,xy^2 + 8\,x^2y + 32\,xy^2 - (-192\,x^2y^2 + 40\,xy) = 184\,x^2y^2 + 24\,xy^2 - 40\,xy$$

$$[10] \quad 81\,x^2y^2 + 243\,x^2y + 9\,xy^2 - (324\,x^2y^2 + 81\,x^2y - 18\,xy) + (-81\,x^2y - 81\,xy^2 + 24\,xy^2 + 81\,x^2y - 18\,xy) + (-81\,x^2y - 81\,xy^2 + 81\,x^2y - 18\,xy^2 + 81\,x^2y - 18\,xy^2$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

 $36 xy = -243 x^2 y^2 + 81 x^2 y - 72 xy^2 + 54 xy$

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (3\,b^3x^2y^3z^2) \cdot (-3\,b^3x^3y^3z^3) = -9\,b^6x^5y^6z^5 \\ &[3] \quad (-16\,bxy^3z) \cdot (6\,bx^3yz^3) = -96\,b^2x^4y^4z^4 \\ &[4] \quad (-9\,bx^2y^2z) \cdot (-12\,b^2xy^3z^2) = 108\,b^3x^3y^5z^3 \\ &[5] \quad (64\,b^3xy^2z^3) \cdot (-64\,b^3xy^2z^2) = -4096\,b^6x^2y^4z^5 \\ &[6] \quad (500\,b^2x^2y^2z) \cdot (-75\,b^2x^2y^2z^2) = -37500\,b^4x^4y^4z^3 \\ &[7] \quad (-24\,b^3xyz^2) \cdot (144\,bx^2yz) = -3456\,b^4x^3y^2z^3 \\ &[8] \quad (-196\,bx^3yz) \cdot (14\,bxyz^2) = -2744\,b^2x^4y^2z^3 \\ &[9] \quad (-2048\,bxy^3z^3) \cdot (16\,b^3xy^2z^2) = -32768\,b^4x^2y^5z^5 \\ &[10] \quad (-18\,b^3x^2yz^3) \cdot (18\,b^3xyz^2) = -324\,b^6x^3y^2z^5 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2) \cdot (-4x^2 - 3x) = -4x^4 - 3x^3$$

[2] $(-4x) \cdot (-7x^2 - 4x) = 28x^3 + 16x^2$
[3] $(-3x^2) \cdot (x^2 - 2x) = -3x^4 + 6x^3$
[4] $(-2x) \cdot (-4x^2 - 2x) = 8x^3 + 4x^2$
[5] $(-2x) \cdot (7x^2) = -14x^3$
[6] $(-3x^2) \cdot (5x^2 - 2x) = -15x^4 + 6x^3$
[7] $(4x) \cdot (-4x) = -16x^2$
[8] $(-2x) \cdot (5x^2 + 4x) = -10x^3 - 8x^2$
[9] $(-4x^2) \cdot (-11x^2 + 3x) = 44x^4 - 12x^3$
[10] $(-3x) \cdot (4x^2 + 2x) = -12x^3 - 6x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(5x) \cdot (-7x^2 - 2x) = -35x^3 - 10x^2$$

[2] $(-x^2) \cdot (4x) = -4x^3$
[3] $(-x^2 + 3x) \cdot (-4x) = 4x^3 - 12x^2$
[4] $(2x^2) \cdot (4x^2) = 8x^4$
[5] $(2x^2 + 3x) \cdot (-6x^2 - 2x) = -12x^4 - 22x^3 - 6x^2$
[6] $(0) \cdot (6x) = 0$
[7] $(-x^2 - 3x) \cdot (-2x^2 - 4x) = 2x^4 + 10x^3 + 12x^2$

[8]
$$(3x^2 + 3x) \cdot (-x^2 - 5x) = -3x^4 - 18x^3 - 15x^2$$

[9]
$$(4x^2 + 2x) \cdot (-4x^2) = -16x^4 - 8x^3$$

[10]
$$(2x) \cdot (x^2 - 5x) = 2x^3 - 10x^2$$

[11]
$$(-3x) \cdot (-2x^2 - 4x) = 6x^3 + 12x^2$$

[12]
$$(-x^2) \cdot (2x) = -2x^3$$

[13]
$$(-7x^2) \cdot (-10x) = 70x^3$$

[14]
$$(x^2 - x) \cdot (x^2 + 2x) = x^4 + x^3 - 2x^2$$

[15]
$$(-5x^2) \cdot (-3x^2 + 6x) = 15x^4 - 30x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-6x^2 + 2x) \cdot (-5x^2 - 4x) = 30x^4 + 14x^3 - 8x^2$$

[2]
$$(3x^3 + x^2) \cdot (-3x^2) = -9x^5 - 3x^4$$

[3]
$$(2x^2 + x) \cdot (-3x^3 + 3x) = -6x^5 - 3x^4 + 6x^3 + 3x^2$$

[4]
$$(3x^3 - 3x) \cdot (-x^3) = -3x^6 + 3x^4$$

[5]
$$(2x^3 - 2x) \cdot (-x^2 - 11x) = -2x^5 - 22x^4 + 2x^3 + 22x^2$$

[6]
$$(-4x^3 + x) \cdot (-x^3 + 2x^2 - 4x) = 4x^6 - 8x^5 + 15x^4 + 2x^3 - 4x^2$$

[7]
$$(-x^3 - x) \cdot (-6x^3 + 4x) = 6x^6 + 2x^4 - 4x^2$$

[8]
$$(x^3) \cdot (2x^3 - 3x^2 - 5x) = 2x^6 - 3x^5 - 5x^4$$

[9]
$$(2x^3 - 2x) \cdot (5x^3 + 3x^2 - 3x) = 10x^6 + 6x^5 - 16x^4 - 6x^3 + 6x^2$$

[10]
$$(-3x^2 + x) \cdot (4x^3) = -12x^5 + 4x^4$$

[11]
$$(-3x^3 + 4x^2) \cdot (x^3 - 4x) = -3x^6 + 4x^5 + 12x^4 - 16x^3$$

[12]
$$(4x^3) \cdot (-x^3) = -4x^6$$

[13]
$$(7x^3 - 3x^2) \cdot (-x^3 - 5x) = -7x^6 + 3x^5 - 35x^4 + 15x^3$$

[14]
$$(0) \cdot (-2x^3 + 2x^2) = 0$$

[15]
$$(3x^3 + 4x^2) \cdot (2x^3 + 3x^2 + 2x) = 6x^6 + 17x^5 + 18x^4 + 8x^3$$

[16]
$$(2x^3 + 2x^2 - x) \cdot (-4x^3 - 2x^2) = -8x^6 - 12x^5 + 2x^3$$

[17]
$$(3x^3) \cdot (-5x^3 - x) = -15x^6 - 3x^4$$

[18]
$$(-3x^3 - 4x^2) \cdot (4x^2 - 2x) = -12x^5 - 10x^4 + 8x^3$$

[19]
$$(2x^3 - 2x) \cdot (-3x^3 + 2x^2) = -6x^6 + 4x^5 + 6x^4 - 4x^3$$

[20]
$$(x^3) \cdot (x) = x^4$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(6x^2y) \cdot (6x^2y^2 + 4xy) = 36x^4y^3 + 24x^3y^2$$

[2]
$$(-x^2y^2 - x^2y) \cdot (x^2y^2 - 5xy^2) = -x^4y^4 - x^4y^3 + 5x^3y^4 + 5x^3y^3$$

[3]
$$(3x^2y - 4xy^2) \cdot (-xy^2 - 4xy) = -3x^3y^3 + 4x^2y^4 - 12x^3y^2 + 16x^2y^3$$

[4]
$$(7x^2y) \cdot (-x^2y^2 + 2xy) = -7x^4y^3 + 14x^3y^2$$

[5]
$$(2xy^2 - 4xy) \cdot (2x^2y^2 - 3x^2y - xy^2) = 4x^3y^4 - 14x^3y^3 - 2x^2y^4 + 12x^3y^2 + 4x^2y^3$$

[6]
$$(-x^2y - 2xy^2) \cdot (4xy^2 - 2xy) = -4x^3y^3 - 8x^2y^4 + 2x^3y^2 + 4x^2y^3$$

[7]
$$(-5x^2y) \cdot (x^2y^2 + 2x^2y) = -5x^4y^3 - 10x^4y^2$$