1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$2x^6 + -5x^5 + 2x + 2x^6 - 4x^3 - 3x^2 = 4x^6 - 5x^5 - 4x^3 - 3x^2 + 2x$$

[2] $3x^5 + 4x^3 - x^2 + -7x^6 - 3x + 2x^2 = -7x^6 + 3x^5 + 4x^3 + x^2 - 3x$
[3] $x^6 + 3x^3 - 3x^2 + -2x^6 + 2x^4 + 4x^2 + -x^4 + 3x^3 + x = -x^6 + x^4 + 6x^3 + x^2 + x$
[4] $2x^2 - 5x + -2x^6 - 3x^2 - 4x + -2x^2 - 7x = -2x^6 - 3x^2 - 16x$
[5] $-x^5 + 7x^4 + (-2x^6 - 5x^3) + (-x^5 - 4x^4 + 4x) = -2x^6 - 2x^5 + 3x^4 - 5x^3 + 4x$
[6] $x^5 - 4x^4 + x^3 + -x^6 - 5x + -3x^6 + 2x^2 + 4x = -4x^6 + x^5 - 4x^4 + x^3 + 2x^2 - x$
[7] $x^4 + x^4 - 3x^3 + 2x^2 + 4x^6 - 4x^4 + 4x^2 = 4x^6 - 2x^4 - 3x^3 + 6x^2$
[8] $3x^6 + 2x^5 + 2x^2 + -4x^6 + 3x^5 + 4x^4 + 4x^6 + x^5 = 3x^6 + 6x^5 + 4x^4 + 2x^2$
[9] $5x^4 - x^2 + -x^3 - 4x^2 + 4x^2 + 3x = 5x^4 - x^3 - x^2 + 3x$
[10] $3x^6 + 2x^2 + 3x + -x^5 - 3x^2 + -x^3 + 4x = 3x^6 - x^5 - x^3 - x^2 + 7x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0$$

$$[2] \quad 4x^2y-5xy+4xy^2-2xy+2x^2y^2+xy^2=2x^2y^2+4x^2y+5xy^2-7xy$$

$$[3] \quad 6xy^2+12xy+18xy^2+-8x^2y^2-2xy^2-4xy=-8x^2y^2+22xy^2+8xy$$

$$[4] \quad 9x^2y^2+12x^2y+27xy^2+-12x^2y^2+9x^2y-27xy^2+12x^2y-18xy=-3x^2y^2+33x^2y-18xy$$

$$[5] \quad 76x^2y+96x^2y^2+16x^2y-16xy^2+48xy=96x^2y^2+92x^2y-16xy^2+48xy$$

$$[6] \quad 95x^2y-15xy^2+25x^2y^2+75xy^2-10xy+10x^2y^2-10x^2y-50xy^2=35x^2y^2+85x^2y+10xy^2-10xy$$

$$[7] \quad 144xy^2+12x^2y^2+6xy+-72x^2y-12xy^2+144xy=12x^2y^2-72x^2y+132xy^2+150xy$$

$$[8] \quad 49x^2y^2+98xy^2-14xy+-49x^2y^2+147x^2y-49xy^2+-14x^2y+210xy^2=133x^2y+259xy^2-14xy$$

$$[9] \quad 128x^2y^2+32x^2y+64xy+-448x^2y^2+192x^2y+(-128x^2y)=-320x^2y^2+96x^2y+64xy$$

$$[10] \quad 324x^2y+9xy^2-27xy+-324x^2y^2+9x^2y+-180xy=-324x^2y^2+333x^2y+9xy^2-207xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 3\,x^2y^2 - 2\,x^2y + -2\,x^2y^2 + 4\,x^2y - (x^2y + xy) = x^2y^2 + x^2y - xy \\ &[3] \quad 2\,x^2y^2 - 12\,xy + -14\,x^2y^2 - (8\,x^2y^2 - 6\,xy) = -20\,x^2y^2 - 6\,xy \\ &[4] \quad 9\,x^2y^2 - 48\,x^2y - (27\,x^2y^2 + 12\,xy^2 - 9\,xy) + (-3\,x^2y^2 - 12\,x^2y - 9\,xy) = -21\,x^2y^2 - 60\,x^2y - 12\,xy^2 \\ &[5] \quad -4\,x^2y - 48\,xy^2 + 48\,xy + -8\,xy^2 + 48\,xy - (-8\,x^2y^2 + 64\,xy^2 - 32\,xy) = 8\,x^2y^2 - 4\,x^2y - 120\,xy^2 + 128\,xy \\ &[6] \quad -15\,x^2y^2 + 5\,x^2y^2 + 20\,xy^2 - 50\,xy - (-100\,xy^2 + 35\,xy) = -10\,x^2y^2 + 120\,xy^2 - 85\,xy \end{aligned}$$

$$\begin{array}{ll} [7] & 108\,x^2y^2 + 18\,xy^2 - 108\,xy - (162\,x^2y + 36\,xy) + (-72\,xy^2 + 18\,xy) = 108\,x^2y^2 - \\ 162\,x^2y - 54\,xy^2 - 126\,xy \\ [8] & 294\,x^2y - 98\,xy + 147\,x^2y^2 - 14\,x^2y + 98\,xy - (35\,x^2y - 196\,xy) = 147\,x^2y^2 + \\ 245\,x^2y + 196\,xy \\ [9] & 32\,x^2y^2 - 8\,xy^2 - 24\,xy + -96\,x^2y^2 - 192\,xy - (-24\,x^2y^2 + 8\,xy^2) = -40\,x^2y^2 - \\ 16\,xy^2 - 216\,xy \\ [10] & -243\,x^2y^2 - 27\,xy^2 - 81\,xy - (45\,x^2y - 81\,xy^2) + (-324\,x^2y + 207\,xy) = \\ \end{array}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

 $-243 x^2 y^2 - 369 x^2 y + 54 x y^2 + 126 x y$

[1]
$$(0) \cdot (0) = 0$$

[2] $(2bx^2yz^2) \cdot (-3b^3x^3y^2z) = -6b^4x^5y^3z^3$
[3] $(-8bxyz^3) \cdot (-24bx^2y^3z^2) = 192b^2x^3y^4z^5$
[4] $(36bxyz^2) \cdot (36b^2xy^2z) = 1296b^3x^2y^3z^3$
[5] $(-48b^2x^3y^3z) \cdot (-48bx^3y^2z) = 2304b^3x^6y^5z^2$
[6] $(15bx^2y^2z^2) \cdot (375b^2xyz^3) = 5625b^3x^3y^3z^5$
[7] $(-72b^2xyz^3) \cdot (-648bx^3y^3z^3) = 46656b^3x^4y^4z^6$
[8] $(1029b^3xy^3z^2) \cdot (-147bxy^3z^3) = -151263b^4x^2y^6z^5$
[9] $(-8b^2x^3y^3z) \cdot (24bx^2y^3z^2) = -192b^3x^5y^6z^3$
[10] $(81b^3xy^2z) \cdot (27bx^3yz^3) = 2187b^4x^4y^3z^4$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (3\,x^2)\cdot(-2\,x) = -6\,x^3 \\ &[2] \quad (-3\,x^2)\cdot(3\,x^2+4\,x) = -9\,x^4-12\,x^3 \\ &[3] \quad (-3\,x^2)\cdot(-x) = 3\,x^3 \\ &[4] \quad (-2\,x^2)\cdot(-3\,x^2-x) = 6\,x^4+2\,x^3 \\ &[5] \quad (-4\,x^2)\cdot(3\,x^2) = -12\,x^4 \\ &[6] \quad (-4\,x)\cdot(3\,x) = -12\,x^2 \\ &[7] \quad (x^2)\cdot(7\,x^2-2\,x) = 7\,x^4-2\,x^3 \\ &[8] \quad (3\,x^2)\cdot(-x^2+3\,x) = -3\,x^4+9\,x^3 \\ &[9] \quad (-x)\cdot(x^2-2\,x) = -x^3+2\,x^2 \\ &[10] \quad (x^2)\cdot(-2\,x^2+6\,x) = -2\,x^4+6\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-7x^2) \cdot (-3x) = 21x^3$$

[2] $(2x^2 + 2x) \cdot (3x^2 - x) = 6x^4 + 4x^3 - 2x^2$
[3] $(2x) \cdot (x^2 - 7x) = 2x^3 - 14x^2$
[4] $(0) \cdot (x^2 + 4x) = 0$
[5] $(7x^2) \cdot (-4x^2 - 5x) = -28x^4 - 35x^3$
[6] $(2x^2 - x) \cdot (-3x^2 + x) = -6x^4 + 5x^3 - x^2$
[7] $(-2x) \cdot (x^2 - 7x) = -2x^3 + 14x^2$
[8] $(-3x) \cdot (x) = -3x^2$

[9]
$$(0) \cdot (2x^2 + 2x) = 0$$

[10]
$$(2x) \cdot (-2x^2 + 4x) = -4x^3 + 8x^2$$

[11]
$$(x^2 + x) \cdot (-4x^2) = -4x^4 - 4x^3$$

[12]
$$(-2x^2) \cdot (x^2 + 2x) = -2x^4 - 4x^3$$

[13]
$$(-5x) \cdot (-x^2 - x) = 5x^3 + 5x^2$$

[14]
$$(-x^2) \cdot (-6x^2 + 2x) = 6x^4 - 2x^3$$

[15]
$$(x^2 + 3x) \cdot (-x^2 - 2x) = -x^4 - 5x^3 - 6x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(5x^2 + x) \cdot (x^2) = 5x^4 + x^3$$

[2]
$$(0) \cdot (-x^3 - 2x^2 - 4x) = 0$$

[3]
$$(2x) \cdot (-x^3 + 2x^2 + 2x) = -2x^4 + 4x^3 + 4x^2$$

[4]
$$(3x^3 - 5x^2) \cdot (4x^3 - x) = 12x^6 - 20x^5 - 3x^4 + 5x^3$$

[5]
$$(4x^3 - 4x) \cdot (4x^3 - 6x^2) = 16x^6 - 24x^5 - 16x^4 + 24x^3$$

[6]
$$(-3x^2 - 4x) \cdot (x^3 - 3x^2 + 4x) = -3x^5 + 5x^4 - 16x^2$$

[7]
$$(-5x^2 - x) \cdot (-2x^3) = 10x^5 + 2x^4$$

[8]
$$(-3x^3+x)\cdot(-5x^3-x)=15x^6-2x^4-x^2$$

[9]
$$(-3x^3 + 3x) \cdot (4x^3 + 4x) = -12x^6 + 12x^2$$

[10]
$$(-4x^2 + 4x) \cdot (2x^3 - 3x^2) = -8x^5 + 20x^4 - 12x^3$$

[11]
$$(-2x) \cdot (-4x^3 - x^2 - 4x) = 8x^4 + 2x^3 + 8x^2$$

[12]
$$(-2x^2 - 4x) \cdot (-3x^3) = 6x^5 + 12x^4$$

[13]
$$(3x^3 + 3x) \cdot (x^3 + 3x) = 3x^6 + 12x^4 + 9x^2$$

[14]
$$(-2x^3 - 3x^2) \cdot (x) = -2x^4 - 3x^3$$

[15]
$$(6x^3) \cdot (-3x^3 - 3x^2 - 6x) = -18x^6 - 18x^5 - 36x^4$$

[16]
$$(2x^3 - 4x^2 - 2x) \cdot (x^3 - 4x^2 - x) = 2x^6 - 12x^5 + 12x^4 + 12x^3 + 2x^2$$

[17]
$$(4x^2) \cdot (3x^3 + 2x^2 - x) = 12x^5 + 8x^4 - 4x^3$$

[18]
$$(x) \cdot (-9x^2) = -9x^3$$

[19]
$$(x^2 + x) \cdot (2x^3 - 4x^2 + 3x) = 2x^5 - 2x^4 - x^3 + 3x^2$$

[20]
$$(-2x^2 + 3x) \cdot (-3x^3 + 10x^2) = 6x^5 - 29x^4 + 30x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2y + xy) \cdot (2x^2y^2 - 7x^2y) = -4x^4y^3 + 14x^4y^2 + 2x^3y^3 - 7x^3y^2$$

[2]
$$(-6x^2y) \cdot (2x^2y^2 + 2x^2y - 2xy^2) = -12x^4y^3 - 12x^4y^2 + 12x^3y^3$$

[3]
$$(7x^2y^2) \cdot (4x^2y + xy) = 28x^4y^3 + 7x^3y^3$$

[4]
$$(-3x^2y + xy^2) \cdot (-2x^2y^2 - 2x^2y) = 6x^4y^3 - 2x^3y^4 + 6x^4y^2 - 2x^3y^3$$

[5]
$$(-3xy^2) \cdot (-2xy^2 - 3xy) = 6x^2y^4 + 9x^2y^3$$

[6]
$$(8xy^2) \cdot (-4x^2y - 3xy^2 - 3xy) = -32x^3y^3 - 24x^2y^4 - 24x^2y^3$$

[7]
$$(2x^2y - 2xy) \cdot (2x^2y + 5xy) = 4x^4y^2 + 6x^3y^2 - 10x^2y^2$$