1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad x^6 - 3x^5 + -x^6 + 2x^2 + 2x^5 + 3x^4 + 2x^2 = -x^5 + 3x^4 + 4x^2 \\ [2] \quad 3x^5 + 2x^3 + x^2 + x^5 + 4x^4 - x + -3x^6 = -3x^6 + 4x^5 + 4x^4 + 2x^3 + x^2 - x \\ [3] \quad x^6 + x^5 + 4x^2 + -3x^6 + -6x^5 + 2x^3 = -2x^6 - 5x^5 + 2x^3 + 4x^2 \\ [4] \quad -3x^4 - x^3 + x + (-4x^6 - 4x^4 - 2x) + (-3x^3 + 4x) = -4x^6 - 7x^4 - 4x^3 + 3x \\ [5] \quad 2x^5 - x^3 - 3x^2 + -3x^6 + 4x^4 + 2x^2 + -3x^6 + x^4 + 3x^3 = -6x^6 + 2x^5 + 5x^4 + 2x^3 - x^2 \\ [6] \quad 2x^3 - 6x^2 + -4x^4 - 2x + (-7x^6 + 3x) = -7x^6 - 4x^4 + 2x^3 - 6x^2 + x \\ [7] \quad 3x^5 + x^4 - 2x^2 + x^4 - x^2 + 2x + -4x^5 - 3x^4 - 3x^3 = -x^5 - x^4 - 3x^3 - 3x^2 + 2x \\ [8] \quad 3x^6 + 3x^5 + 4x^3 + -2x^6 - 3x^5 - 4x^4 + -3x^5 + 2x^4 - x^2 = x^6 - 3x^5 - 2x^4 + 4x^3 - x^2 \\ [9] \quad x^4 + 3x^3 + x^2 + x^5 + 4x^3 - x + 2x^6 - 3x^2 - 4x = 2x^6 + x^5 + x^4 + 7x^3 - 2x^2 - 5x \\ [10] \quad 3x^5 - 4x^4 - x^2 + -3x^6 - x^3 + 3x + -4x^3 - x^2 + 2x = -3x^6 + 3x^5 - 4x^4 - 5x^3 - 2x^2 + 5x \\ \end{cases}$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0+0+0=0 \\ & [2] \quad x^2y^2-2\,xy^2-4\,xy+-x^2y^2+4\,x^2y+2\,x^2y^2-3\,xy^2-4\,xy=2\,x^2y^2+4\,x^2y-5\,xy^2-8\,xy \\ & [3] \quad 10\,x^2y^2-6\,xy^2+8\,x^2y^2+8\,xy^2+4\,xy+-14\,x^2y^2-6\,xy^2=4\,x^2y^2-4\,xy^2+4\,xy \\ & [4] \quad 3\,x^2y^2+24\,xy+-9\,xy^2-18\,xy+-9\,x^2y-6\,xy^2-27\,xy=3\,x^2y^2-9\,x^2y-15\,xy^2-21\,xy \\ & [5] \quad 4\,x^2y^2-16\,xy^2+-40\,x^2y^2+4\,xy+64\,xy^2+8\,xy=-36\,x^2y^2+48\,xy^2+12\,xy \\ & [6] \quad 20\,x^2y^2-10\,x^2y-100\,xy^2+-15\,x^2y^2-75\,x^2y-5\,xy^2+-100\,x^2y^2-75\,xy^2=-95\,x^2y^2-85\,x^2y-180\,xy^2 \\ & [7] \quad 84\,x^2y^2+36\,xy^2+-18\,x^2y^2+72\,xy^2+(-18\,x^2y^2-144\,x^2y)=48\,x^2y^2-144\,x^2y+108\,xy^2 \\ & [8] \quad 196\,x^2y+7\,xy^2-28\,xy+-147\,x^2y^2+-21\,x^2y^2-28\,xy^2-21\,xy=-168\,x^2y^2+196\,x^2y-21\,xy^2-49\,xy \\ & [9] \quad 32\,x^2y^2-384\,xy^2+-24\,x^2y-40\,xy^2+24\,x^2y^2+16\,x^2y-24\,xy^2=56\,x^2y^2-8\,x^2y-448\,xy^2 \\ & [10] \quad 9\,x^2y^2+171\,xy^2+-18\,x^2y^2+18\,xy^2-27\,xy+99\,x^2y^2-81\,x^2y=90\,x^2y^2-81\,x^2y+189\,xy^2-27\,xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y^2 - x^2y + xy + -2\,x^2y + 5\,xy - (-2\,x^2y - 3\,xy^2) = -2\,x^2y^2 - x^2y + 3\,xy^2 + 6\,xy \\ &[3] \quad -2\,x^2y^2 + 8\,xy^2 + -4\,x^2y^2 - 4\,xy^2 - (-4\,xy^2 - 32\,xy) = -6\,x^2y^2 + 8\,xy^2 + 32\,xy \\ &[4] \quad -9\,x^2y^2 + 9\,xy - (18\,x^2y - 18\,xy^2 - 12\,xy) + (-12\,x^2y + 9\,xy^2 + 18\,xy) = -9\,x^2y^2 - 30\,x^2y + 27\,xy^2 + 39\,xy \end{aligned}$$

$$[5] \quad 64\,x^2y^2 + 68\,x^2y + -48\,x^2y + 112\,xy - (4\,x^2y^2 - 40\,x^2y) = 60\,x^2y^2 + 60\,x^2y + 112\,xy \\ [6] \quad 50\,x^2y^2 + 25\,xy + 10\,x^2y + 30\,xy^2 - (150\,x^2y^2 - 75\,x^2y) = -100\,x^2y^2 + 85\,x^2y + 30\,xy^2 + 25\,xy \\ [7] \quad 12\,x^2y^2 + 18\,xy^2 - (18\,x^2y^2 + 36\,x^2y) + (24\,x^2y^2 - 144\,xy^2) = 18\,x^2y^2 - 36\,x^2y - 126\,xy^2 \\ [8] \quad -28\,xy^2 + 245\,xy + 126\,x^2y^2 - 49\,xy - (-147\,x^2y - 28\,xy^2 - 7\,xy) = 126\,x^2y^2 + 147\,x^2y + 203\,xy \\ [9] \quad -32\,x^2y^2 - 88\,x^2y + 96\,x^2y^2 + 64\,xy^2 - (-8\,x^2y^2 + 264\,xy) = 72\,x^2y^2 - 88\,x^2y + 64\,xy^2 - 264\,xy \\ [10] \quad 261\,x^2y - (81\,x^2y - 27\,xy^2) + (-81\,x^2y^2 - 324\,xy^2) = -81\,x^2y^2 + 180\,x^2y - 297\,xy^2 \\ \end{cases}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-bx^3y^2z^3) \cdot (2\,bxyz^2) = -2\,b^2x^4y^3z^5 \\ &[3] \quad (-16\,b^3x^2y^3z) \cdot (24\,b^3x^2y^2z) = -384\,b^6x^4y^5z^2 \\ &[4] \quad (9\,b^3x^2y^3z^3) \cdot (27\,b^2x^2y^2z^2) = 243\,b^5x^4y^5z^5 \\ &[5] \quad (12\,b^2x^3y^2z^2) \cdot (-64\,bx^2yz^2) = -768\,b^3x^5y^3z^4 \\ &[6] \quad (-75\,b^2xy^2z^2) \cdot (50\,b^2x^3y^3z^2) = -3750\,b^4x^4y^5z^4 \\ &[7] \quad (216\,b^3xy^2z) \cdot (24\,b^3x^2y^2z) = 5184\,b^6x^3y^4z^2 \\ &[8] \quad (343\,bx^2y^2z^2) \cdot (-343\,b^2x^2y^3z^3) = -117649\,b^3x^4y^5z^5 \\ &[9] \quad (-16\,b^3xy^3z^2) \cdot (192\,b^3xyz^2) = -3072\,b^6x^2y^4z^4 \\ &[10] \quad (-1458\,b^2x^3y^2z^2) \cdot (2187\,bxy^3z) = -3188646\,b^3x^4y^5z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (3\,x^2)\cdot(-5\,x) = -15\,x^3 \\ & [2] \quad (-4\,x)\cdot(-5\,x^2) = 20\,x^3 \\ & [3] \quad (-3\,x^2)\cdot(-x^2-3\,x) = 3\,x^4+9\,x^3 \\ & [4] \quad (2\,x^2)\cdot(2\,x^2-x) = 4\,x^4-2\,x^3 \\ & [5] \quad (-3\,x)\cdot(x) = -3\,x^2 \\ & [6] \quad (-4\,x)\cdot(2\,x^2+4\,x) = -8\,x^3-16\,x^2 \\ & [7] \quad (x)\cdot(3\,x^2-7\,x) = 3\,x^3-7\,x^2 \\ & [8] \quad (-x)\cdot(-7\,x^2) = 7\,x^3 \\ & [9] \quad (-x)\cdot(2\,x) = -2\,x^2 \\ & [10] \quad (-4\,x)\cdot(3\,x^2-x) = -12\,x^3+4\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2) \cdot (4x^2 + 3x) = 4x^4 + 3x^3$$

[2] $(-4x^2) \cdot (-x^2 - 2x) = 4x^4 + 8x^3$
[3] $(-3x^2 + 2x) \cdot (2x^2 - 3x) = -6x^4 + 13x^3 - 6x^2$
[4] $(0) \cdot (5x^2 - 4x) = 0$

[5]
$$(-2x^2 + 3x) \cdot (-2x^2 + x) = 4x^4 - 8x^3 + 3x^2$$

[6] $(-3x^2 + 4x) \cdot (5x) = -15x^3 + 20x^2$

[7]
$$(-3x^2 - 4x) \cdot (x^2 + x) = -3x^4 - 7x^3 - 4x^2$$

[8]
$$(-4x^2 + 4x) \cdot (-x^2) = 4x^4 - 4x^3$$

[9]
$$(x^2 + x) \cdot (2x^2 + x) = 2x^4 + 3x^3 + x^2$$

[10]
$$(-2x^2 + 2x) \cdot (-2x^2 - 4x) = 4x^4 + 4x^3 - 8x^2$$

[11]
$$(2x^2 - 3x) \cdot (-x^2 + x) = -2x^4 + 5x^3 - 3x^2$$

[12]
$$(3x^2 - x) \cdot (-2x^2 + 2x) = -6x^4 + 8x^3 - 2x^2$$

[13]
$$(2x^2 + 2x) \cdot (-x^2) = -2x^4 - 2x^3$$

[14]
$$(4x^2 + 4x) \cdot (-8x^2) = -32x^4 - 32x^3$$

[15]
$$(4x^2 + x) \cdot (8x^2 - 4x) = 32x^4 - 8x^3 - 4x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^3 + 4x^2 + 3x) \cdot (x^2 + 4x) = -3x^5 - 8x^4 + 19x^3 + 12x^2$$

[2]
$$(x^3) \cdot (-2x^3 - x) = -2x^6 - x^4$$

[3]
$$(-x) \cdot (-6x^3 - 2x^2 - 4x) = 6x^4 + 2x^3 + 4x^2$$

[4]
$$(-2x^3 - 3x^2) \cdot (2x^3 - 4x) = -4x^6 - 6x^5 + 8x^4 + 12x^3$$

[5]
$$(-2x^2) \cdot (-4x^2 - 3x) = 8x^4 + 6x^3$$

[6]
$$(2x^3 + 4x^2) \cdot (9x^2) = 18x^5 + 36x^4$$

[7]
$$(3x^3 - 3x^2 + 3x) \cdot (-x^3 + x^2) = -3x^6 + 6x^5 - 6x^4 + 3x^3$$

[8]
$$(2x^3) \cdot (-7x^3 - 4x^2) = -14x^6 - 8x^5$$

[9]
$$(2x^3 - 4x^2) \cdot (-4x^3 - 5x^2) = -8x^6 + 6x^5 + 20x^4$$

[10]
$$(8x^2) \cdot (-7x^3) = -56x^5$$

[11]
$$(x^3 - 2x) \cdot (-5x^3 + x) = -5x^6 + 11x^4 - 2x^2$$

[12]
$$(3x^3 + 2x) \cdot (2x^2 - x) = 6x^5 - 3x^4 + 4x^3 - 2x^2$$

[13]
$$(-x^3 + 3x^2) \cdot (3x^3 - 3x^2) = -3x^6 + 12x^5 - 9x^4$$

[14]
$$(-4x^3 - 3x) \cdot (-7x^3 - x) = 28x^6 + 25x^4 + 3x^2$$

[15]
$$(-6x) \cdot (8x^2 - 8x) = -48x^3 + 48x^2$$

[16]
$$(-x^3 + 3x^2) \cdot (x^2 - 6x) = -x^5 + 9x^4 - 18x^3$$

[17]
$$(-5x^2) \cdot (x^3 - 3x^2 + 3x) = -5x^5 + 15x^4 - 15x^3$$

[18]
$$(0) \cdot (2x^3 - 2x^2 - 2x) = 0$$

[19]
$$(-4x^2 + 3x) \cdot (x^2 - 7x) = -4x^4 + 31x^3 - 21x^2$$

[20]
$$(3x^2 + 4x) \cdot (6x) = 18x^3 + 24x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^2y + 2xy) \cdot (2x^2y^2 - 4x^2y) = -2x^4y^3 + 4x^4y^2 + 4x^3y^3 - 8x^3y^2$$

[2]
$$(-4x^2y^2 - 3xy) \cdot (4x^2y + xy) = -16x^4y^3 - 4x^3y^3 - 12x^3y^2 - 3x^2y^2$$

[3]
$$(-3xy^2 - 2xy) \cdot (-4x^2y - 4xy^2 + 3xy) = 12x^3y^3 + 12x^2y^4 + 8x^3y^2 - x^2y^3 - 6x^2y^2$$

[4]
$$(-2xy^2) \cdot (-4x^2y) = 8x^3y^3$$

$$\begin{aligned} & [5] \quad (4\,x^2y^2 + 3\,xy^2) \cdot (-2\,x^2y + 4\,xy^2 - 2\,xy) = -8\,x^4y^3 + 16\,x^3y^4 - 14\,x^3y^3 + \\ & 12\,x^2y^4 - 6\,x^2y^3 \\ & [6] \quad (2\,x^2y) \cdot (2\,x^2y^2 - 8\,xy^2) = 4\,x^4y^3 - 16\,x^3y^3 \\ & [7] \quad (3\,xy^2 - 3\,xy) \cdot (-3\,x^2y + xy^2 - 4\,xy) = -9\,x^3y^3 + 3\,x^2y^4 + 9\,x^3y^2 - 15\,x^2y^3 + \\ & 12\,x^2y^2 \end{aligned}$$