1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad x^6 - 2\,x^5 + x^4 + -3\,x^4 - x^3 + -x^4 + 4\,x^3 + 2\,x = x^6 - 2\,x^5 - 3\,x^4 + 3\,x^3 + 2\,x \\ [2] \quad 2\,x^5 + 4\,x^3 + 3\,x^2 + x^6 - 4\,x^4 - x^2 + 2\,x^4 - 3\,x^3 + x = x^6 + 2\,x^5 - 2\,x^4 + x^3 + 2\,x^2 + x \\ [3] \quad 4\,x^6 + x^2 + -x^2 - x + -2\,x^6 + 6\,x^3 = 2\,x^6 + 6\,x^3 - x \\ [4] \quad 4\,x^6 + 2\,x^4 - x^3 + 5\,x^3 + 3\,x^2 + -2\,x^6 + x^3 - 4\,x = 2\,x^6 + 2\,x^4 + 5\,x^3 + 3\,x^2 - 4\,x \\ [5] \quad 2\,x^5 + 4\,x^4 - 3\,x + -x^4 - 2\,x^3 - x + -3\,x^5 + 3\,x^3 - 3\,x^2 = -x^5 + 3\,x^4 + x^3 - 3\,x^2 - 4\,x \\ [6] \quad 2\,x^5 - 3\,x^2 + -4\,x^6 - 3\,x^4 + x^2 + -3\,x^4 + 5\,x = -4\,x^6 + 2\,x^5 - 6\,x^4 - 2\,x^2 + 5\,x \\ [7] \quad 3\,x^6 - x^2 + 2\,x + -x^6 - x^4 + 3\,x^3 + (-3\,x^6 - 4\,x^4 + 4\,x^3) = -x^6 - 5\,x^4 + 7\,x^3 - x^2 + 2\,x \\ [8] \quad 5\,x^5 + x^2 + 2\,x^4 + 4\,x^3 - x^2 + 4\,x^6 - x^4 + 3\,x^2 = 4\,x^6 + 5\,x^5 + x^4 + 4\,x^3 + 3\,x^2 \\ [9] \quad x^5 + 3\,x^4 - x + -x^4 - 2\,x^2 - 3\,x + 3\,x^6 + 3\,x^3 = 3\,x^6 + x^5 + 2\,x^4 + 3\,x^3 - 2\,x^2 - 4\,x \\ [10] \quad -3\,x^5 + x^4 + x^2 + (-x^3 - 2\,x^2 + 4\,x) + (-x^6 - 3\,x^2 - x) = -x^6 - 3\,x^5 + x^4 - x^4 - x^3 - 4\,x^2 + 3\,x \\ [10] \quad -3\,x^5 + x^4 + x^2 + (-x^3 - 2\,x^2 + 4\,x) + (-x^6 - 3\,x^2 - x) = -x^6 - 3\,x^5 + x^4 - x^4 -$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 2x^2y^2-2x^2y+-x^2y^2+4x^2y-xy^2+(-4x^2y^2+xy^2+3xy)=-3x^2y^2+2x^2y+3xy \\ [3] \quad 4xy+16x^2y^2-8xy^2-12xy+-4x^2y^2-8x^2y-8xy^2=12x^2y^2-8x^2y-16xy^2-8xy \\ [4] \quad 24x^2y^2+-27x^2y+36xy^2+3xy+(-9x^2y^2-27x^2y+3xy^2)=15x^2y^2-54x^2y+39xy^2+3xy \\ [5] \quad 12x^2y+64xy^2-16xy+-44x^2y+-48x^2y+96xy^2=-80x^2y+160xy^2-16xy \\ [6] \quad 10x^2y-10xy^2-15xy+-30x^2y+50xy^2+(-5x^2y^2-85x^2y)=-5x^2y^2-105x^2y+40xy^2-15xy \\ [7] \quad 144x^2y+18xy^2+-6x^2y^2+30xy+-180x^2y+18xy^2=-6x^2y^2-36x^2y+36xy^2+30xy \\ [8] \quad 84x^2y^2+21xy^2+7x^2y^2+98x^2y+21xy^2+7x^2y+14xy^2-49xy=91x^2y^2+105x^2y+56xy^2-49xy \\ [9] \quad 128x^2y^2-32x^2y-16xy+-64x^2y-120xy^2+-128x^2y^2-8x^2y-24xy^2=-104x^2y-144xy^2-16xy \\ [10] \quad 162x^2y^2-324x^2y-36xy^2+-9x^2y^2-18xy^2+81xy+-162x^2y+63xy^2=153x^2y^2-486x^2y+9xy^2+81xy \\ [10] \quad 122x^2y^2-324x^2y-36xy^2+12xy^2+1$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad x^2y^2 + xy^2 + -2\,xy - (x^2y^2 - 4\,xy^2 - 4\,xy) = 5\,xy^2 + 2\,xy \\ &[3] \quad 2\,x^2y^2 - 6\,x^2y + -4\,x^2y + 8\,xy^2 + 16\,xy - (24\,x^2y^2) = -22\,x^2y^2 - 10\,x^2y + 8\,xy^2 + 16\,xy \\ &[4] \quad 9\,x^2y + 6\,xy^2 + 18\,xy - (-36\,x^2y - 9\,xy^2 - 6\,xy) + (3\,x^2y^2 + 9\,x^2y + 3\,xy) = 3\,x^2y^2 + 54\,x^2y + 15\,xy^2 + 27\,xy \end{aligned}$$

$$[5] \quad 44\,x^2y^2 + 8\,xy^2 + 16\,x^2y^2 - (-12\,xy^2) = 60\,x^2y^2 + 20\,xy^2$$

$$[6] \quad -20\,x^2y^2 - 35\,xy + 35\,xy^2 - 10\,xy - (-15\,x^2y^2 + 30\,x^2y) = -5\,x^2y^2 - 30\,x^2y + 35\,xy^2 - 45\,xy$$

$$[7] \quad -12\,x^2y^2 + 108\,x^2y - 36\,xy - (114\,x^2y^2 - 72\,x^2y) + (-108\,x^2y^2 + 48\,x^2y) = -234\,x^2y^2 + 228\,x^2y - 36\,xy$$

$$[8] \quad 7\,x^2y^2 - 28\,xy^2 - 14\,xy + 196\,x^2y^2 - (-7\,xy^2 - 245\,xy) = 203\,x^2y^2 - 21\,xy^2 + 231\,xy$$

$$[9] \quad 40\,x^2y + 24\,xy + -64\,x^2y^2 - 8\,x^2y - (-32\,x^2y^2 + 192\,x^2y - 192\,xy^2) = -32\,x^2y^2 - 160\,x^2y + 192\,xy^2 + 24\,xy$$

$$[10] \quad -315\,x^2y^2 - 324\,xy - (-27\,x^2y - 279\,xy^2) + (81\,x^2y^2 + 81\,x^2y - 9\,xy^2) = -234\,x^2y^2 + 108\,x^2y + 270\,xy^2 - 324\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-4 \, bx^2 yz^2) \cdot (3 \, b^3 xy^2 z^3) = -12 \, b^4 x^3 y^3 z^5 \\ &[3] \quad (8 \, b^3 x^3 y^3 z^2) \cdot (12 \, bx y^2 z) = 96 \, b^4 x^4 y^5 z^3 \\ &[4] \quad (-6 \, bx^2 yz^2) \cdot (3 \, b^2 xy^2 z^2) = -18 \, b^3 x^3 y^3 z^4 \\ &[5] \quad (32 \, b^2 x^2 yz^2) \cdot (48 \, b^3 x^3 y^2 z) = 1536 \, b^5 x^5 y^3 z^3 \\ &[6] \quad (-20 \, bx^2 yz) \cdot (20 \, b^3 x^2 y^3 z) = -400 \, b^4 x^4 y^4 z^2 \\ &[7] \quad (108 \, bx^3 yz^2) \cdot (216 \, b^3 x^3 y^3 z^2) = 23328 \, b^4 x^6 y^4 z^4 \\ &[8] \quad (-98 \, b^2 x^2 y^2 z) \cdot (7 \, b^3 x^2 y^3 z^3) = -686 \, b^5 x^4 y^5 z^4 \\ &[9] \quad (-32 \, bx y^2 z) \cdot (512 \, b^2 xy^2 z^2) = -16384 \, b^3 x^2 y^4 z^3 \\ &[10] \quad (18 \, bx^2 y^3 z^2) \cdot (2187 \, b^2 x^2 yz^2) = 39366 \, b^3 x^4 y^4 z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (3\,x^2)\cdot(4\,x^2+3\,x) = 12\,x^4+9\,x^3 \\ &[2] \quad (-2\,x)\cdot(-4\,x^2+x) = 8\,x^3-2\,x^2 \\ &[3] \quad (-4\,x)\cdot(-6\,x^2+7\,x) = 24\,x^3-28\,x^2 \\ &[4] \quad (-x)\cdot(-7\,x^2-2\,x) = 7\,x^3+2\,x^2 \\ &[5] \quad (-3\,x)\cdot(5\,x^2-3\,x) = -15\,x^3+9\,x^2 \\ &[6] \quad (-3\,x)\cdot(3\,x^2-8\,x) = -9\,x^3+24\,x^2 \\ &[7] \quad (x)\cdot(-x^2-3\,x) = -x^3-3\,x^2 \\ &[8] \quad (-2\,x^2)\cdot(-6\,x^2) = 12\,x^4 \\ &[9] \quad (3\,x)\cdot(-2\,x^2-8\,x) = -6\,x^3-24\,x^2 \\ &[10] \quad (3\,x^2)\cdot(-x^2-4\,x) = -3\,x^4-12\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x^2 + 3x) \cdot (-4x^2 + x) = -8x^4 - 10x^3 + 3x^2$$

[2] $(7x) \cdot (-2x^2) = -14x^3$
[3] $(3x^2 - 3x) \cdot (-3x^2) = -9x^4 + 9x^3$
[4] $(-x^2 - 4x) \cdot (-2x) = 2x^3 + 8x^2$
[5] $(-x^2) \cdot (-2x) = 2x^3$

[6]
$$(-3x^2 + x) \cdot (x^2 - x) = -3x^4 + 4x^3 - x^2$$

[7] $(-4x) \cdot (x^2 + 3x) = -4x^3 - 12x^2$

[8]
$$(-4x^2 - 4x) \cdot (3x^2 + 3x) = -12x^4 - 24x^3 - 12x^2$$

[9]
$$(2x^2 - 2x) \cdot (-2x^2 - 6x) = -4x^4 - 8x^3 + 12x^2$$

[10]
$$(3x) \cdot (-3x^2 - x) = -9x^3 - 3x^2$$

[11]
$$(4x^2 + x) \cdot (-3x^2 - 4x) = -12x^4 - 19x^3 - 4x^2$$

[12]
$$(-2x) \cdot (-3x^2 - x) = 6x^3 + 2x^2$$

[13]
$$(-5x) \cdot (-4x^2 + 3x) = 20x^3 - 15x^2$$

[14]
$$(2x) \cdot (3x^2) = 6x^3$$

[15]
$$(-6x^2) \cdot (-3x) = 18x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^3 + 4x^2) \cdot (x) = -x^4 + 4x^3$$

[2]
$$(3x^2 + 4x) \cdot (4x^3 + 3x^2 - x) = 12x^5 + 25x^4 + 9x^3 - 4x^2$$

[3]
$$(-3x^3 - 2x) \cdot (-x^2 - 2x) = 3x^5 + 6x^4 + 2x^3 + 4x^2$$

[4]
$$(-x^2 + x) \cdot (-5x^2 + 3x) = 5x^4 - 8x^3 + 3x^2$$

[5]
$$(-2x^3 + 3x^2) \cdot (-x) = 2x^4 - 3x^3$$

[6]
$$(2x^3 - x^2) \cdot (-4x^3 - 5x) = -8x^6 + 4x^5 - 10x^4 + 5x^3$$

[7]
$$(-3x^2) \cdot (-4x^3 + 4x^2) = 12x^5 - 12x^4$$

[8]
$$(-3x^3 - 4x) \cdot (-x^3 + x) = 3x^6 + x^4 - 4x^2$$

[9]
$$(-3x^2 - 4x) \cdot (-4x^3 + 4x^2 - 3x) = 12x^5 + 4x^4 - 7x^3 + 12x^2$$

[10]
$$(4x^2) \cdot (-2x^3 + x) = -8x^5 + 4x^3$$

[11]
$$(2x^2 - x) \cdot (-4x^3 + 2x^2 + 3x) = -8x^5 + 8x^4 + 4x^3 - 3x^2$$

[12]
$$(-2x^3) \cdot (4x^3 - 2x) = -8x^6 + 4x^4$$

[13]
$$(3x^3 - x) \cdot (x^3 + x^2) = 3x^6 + 3x^5 - x^4 - x^3$$

[14]
$$(6x^3) \cdot (-7x^3 - 4x^2 - 4x) = -42x^6 - 24x^5 - 24x^4$$

[15]
$$(-x^2 + x) \cdot (x^2 + 5x) = -x^4 - 4x^3 + 5x^2$$

[16]
$$(-7x^2 - 4x) \cdot (-4x^2 + 2x) = 28x^4 + 2x^3 - 8x^2$$

[17]
$$(-3x^3 + 2x) \cdot (x^2 - 3x) = -3x^5 + 9x^4 + 2x^3 - 6x^2$$

[18]
$$(3x^3 + 2x^2) \cdot (x^3 - 4x) = 3x^6 + 2x^5 - 12x^4 - 8x^3$$

[19]
$$(2x^3 - 3x^2) \cdot (-x^3 + 2x) = -2x^6 + 3x^5 + 4x^4 - 6x^3$$

[20]
$$(3x^3 + 4x) \cdot (2x^3 - 5x) = 6x^6 - 7x^4 - 20x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2y^2) \cdot (2x^2y^2 + xy^2 + 2xy) = 2x^4y^4 + x^3y^4 + 2x^3y^3$$

[2]
$$(0) \cdot (3x^2y^2 + xy^2) = 0$$

[3]
$$(-3x^2y^2 + 4x^2y) \cdot (2x^2y - 5xy^2) = -6x^4y^3 + 15x^3y^4 + 8x^4y^2 - 20x^3y^3$$

[4]
$$(-3x^2y^2 - 2xy) \cdot (-3x^2y^2 - 4x^2y - 3xy^2) = 9x^4y^4 + 12x^4y^3 + 9x^3y^4 + 6x^3y^3 + 8x^3y^2 + 6x^2y^3$$

[5]
$$(-4x^2y^2 + 2x^2y) \cdot (-xy^2) = 4x^3y^4 - 2x^3y^3$$

[6]
$$(-4x^2y^2 + xy^2) \cdot (-3x^2y^2 - 4xy^2) = 12x^4y^4 + 13x^3y^4 - 4x^2y^4$$

[7]
$$(4x^2y - 4xy^2) \cdot (4x^2y^2 - 3x^2y - xy^2) = 16x^4y^3 - 16x^3y^4 - 12x^4y^2 + 8x^3y^3 + 4x^2y^4$$