## 1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 4x^4 + 3x^2 + -3x^6 - 2x^3 - 3x + -2x^6 + x^4 + 4x^3 = -5x^6 + 5x^4 + 2x^3 + 3x^2 - 3x$$

$$[2] \quad 2x^5 - x^2 + x + -3x^3 + 5x^2 + 4x^6 + 2x^5 + 3x^4 = 4x^6 + 4x^5 + 3x^4 - 3x^3 + 4x^2 + x$$

$$[3] \quad 2x^3 - 4x^2 - 2x + -6x^6 + 2x^3 + 4x^4 - x^3 = -6x^6 + 4x^4 + 3x^3 - 4x^2 - 2x$$

$$[4] \quad 3x^4 + 2x^3 - 3x + -2x^6 + x^5 - 4x^3 + 3x^6 - x^5 + 3x = x^6 + 3x^4 - 2x^3$$

$$[5] \quad -2x^3 - x^2 + (-3x^6 + x) + (-4x^5 - 2x^4 + 4x) = -3x^6 - 4x^5 - 2x^4 - 2x^3 - x^2 + 5x$$

$$[6] \quad -3x^6 - 4x^5 + x + (-2x^6 + 3x^4 + 4x^2) + (-x^6 + 3x^5) = -6x^6 - x^5 + 3x^4 + 4x^2 + x$$

$$[7] \quad 3x^6 - 4x^4 + x^2 + -4x^2 - 4x + 8x^5 - 3x^3 = 3x^6 + 8x^5 - 4x^4 - 3x^3 - 3x^2 - 4x$$

$$[8] \quad 4x^5 + 5x^2 + -3x^4 + x^2 + (-2x^6 - 4x^5 - 2x) = -2x^6 - 3x^4 + 6x^2 - 2x$$

$$[9] \quad -2x^4 + 4x^3 - 2x + (-2x^6 + x^3 - x) + (-2x^4 - 2x^3 + 3x^2) = -2x^6 - 4x^4 + 3x^3 + 3x^2 - 3x$$

$$[10] \quad 2x^6 + x^2 + x + -3x^5 + 3x^2 + -7x^5 - 3x^2 = 2x^6 - 10x^5 + x^2 + x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad x^2y^2-xy^2+3\,xy+-4\,x^2y^2+xy^2-3\,xy=-3\,x^2y^2 \\ [3] \quad 10\,x^2y^2+8\,xy^2+-4\,x^2y+4\,xy+-8\,x^2y^2-4\,x^2y-4\,xy=2\,x^2y^2-8\,x^2y+8\,xy^2 \\ [4] \quad 9\,x^2y+45\,xy+-27\,x^2y^2+18\,xy+12\,x^2y-12\,xy^2=-27\,x^2y^2+21\,x^2y-12\,xy^2+63\,xy \\ [5] \quad 12\,x^2y-64\,xy+12\,x^2y+64\,xy^2+16\,xy+16\,x^2y^2-64\,xy^2=16\,x^2y^2+24\,x^2y-48\,xy \\ [6] \quad 15\,x^2y-5\,xy^2+-85\,xy^2+5\,xy+(-15\,x^2y^2+55\,x^2y)=-15\,x^2y^2+70\,x^2y-90\,xy^2+5\,xy \\ [7] \quad 72\,x^2y-72\,xy^2-108\,xy+24\,x^2y+144\,xy^2-12\,xy+-108\,x^2y+90\,xy=-12\,x^2y+72\,xy^2-30\,xy \\ [8] \quad 105\,xy^2+-7\,xy^2-7\,xy+(-49\,x^2y-28\,xy)=-49\,x^2y+98\,xy^2-35\,xy \\ [9] \quad 64\,x^2y^2+24\,x^2y+8\,xy+-24\,x^2y^2+192\,x^2y+-208\,x^2y^2-16\,x^2y=-168\,x^2y^2+200\,x^2y+8\,xy \\ [10] \quad 18\,x^2y^2+270\,xy+-27\,x^2y^2-81\,x^2y+162\,xy^2+-9\,x^2y^2-324\,xy^2+324\,xy=-18\,x^2y^2-81\,x^2y-162\,xy^2+594\,xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y^2 + 5\,xy + 3\,x^2y^2 - 6\,x^2y - (3\,xy^2 - 3\,xy) = x^2y^2 - 6\,x^2y - 3\,xy^2 + 8\,xy \\ &[3] \quad 16\,x^2y + 2\,xy + -14\,x^2y^2 - (28\,x^2y^2 - 16\,xy) = -42\,x^2y^2 + 16\,x^2y + 18\,xy \\ &[4] \quad -27\,x^2y^2 - 36\,xy - (27\,x^2y^2 + 36\,xy) + (-12\,xy^2 - 18\,xy) = -54\,x^2y^2 - 12\,xy^2 - 90\,xy \\ &[5] \quad -64\,x^2y^2 + 16\,x^2y + 16\,xy^2 - 32\,xy - (16\,x^2y^2 - 36\,xy^2) = -80\,x^2y^2 + 16\,x^2y + 52\,xy^2 - 32\,xy \\ &[6] \quad 15\,x^2y^2 - 15\,xy^2 - 50\,xy + -75\,xy^2 - (-25\,x^2y + 50\,xy^2 + 20\,xy) = 15\,x^2y^2 + 25\,x^2y - 140\,xy^2 - 70\,xy \end{aligned}$$

$$[7] \quad -30\,x^2y - (18\,x^2y^2 - 36\,xy) + (36\,xy^2 - 120\,xy) = -18\,x^2y^2 - 30\,x^2y + 36\,xy^2 - 84\,xy$$
 
$$[8] \quad -98\,x^2y^2 - 7\,x^2y + 196\,xy + -14\,x^2y^2 + 168\,xy^2 - (-182\,x^2y - 14\,xy) = -112\,x^2y^2 + 175\,x^2y + 168\,xy^2 + 210\,xy$$
 
$$[9] \quad 128\,x^2y - 32\,xy + 8\,xy^2 + 64\,xy - (-208\,x^2y^2 - 8\,x^2y) = 208\,x^2y^2 + 136\,x^2y + 8\,xy^2 + 32\,xy$$
 
$$[10] \quad -27\,x^2y^2 - 18\,x^2y + 36\,xy - (18\,x^2y^2 + 252\,x^2y) + (-486\,x^2y - 18\,xy^2) = -45\,x^2y^2 - 756\,x^2y - 18\,xy^2 + 36\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

[1] 
$$(0) \cdot (0) = 0$$
  
[2]  $(3bxy^2z^3) \cdot (-bx^2y^2z^2) = -3b^2x^3y^4z^5$   
[3]  $(16b^2x^2yz) \cdot (-16b^3x^3y^3z^2) = -256b^5x^5y^4z^3$   
[4]  $(-9b^3xy^3z) \cdot (27b^3x^2y^3z^3) = -243b^6x^3y^6z^4$   
[5]  $(-64bxy^3z) \cdot (-256bx^2y^2z) = 16384b^2x^3y^5z^2$   
[6]  $(-100bx^2y^3z) \cdot (-20b^2x^2yz^3) = 2000b^3x^4y^4z^4$   
[7]  $(144bx^3y^2z^3) \cdot (-72b^3xy^2z^3) = -10368b^4x^4y^4z^6$   
[8]  $(1372b^3xy^2z^2) \cdot (-7bx^2y^2z) = -9604b^4x^3y^4z^3$   
[9]  $(-8bxy^2z^2) \cdot (1024bx^2yz^2) = -8192b^2x^3y^3z^4$   
[10]  $(243b^2x^2yz^3) \cdot (2916bx^2y^2z) = 708588b^3x^4y^3z^4$ 

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x) \cdot (6\,x^2 + 3\,x) = -6\,x^3 - 3\,x^2 \\ &[2] \quad (x^2) \cdot (4\,x^2 + x) = 4\,x^4 + x^3 \\ &[3] \quad (3\,x^2) \cdot (-5\,x^2 + 6\,x) = -15\,x^4 + 18\,x^3 \\ &[4] \quad (3\,x^2) \cdot (-5\,x^2 + 4\,x) = -15\,x^4 + 12\,x^3 \\ &[5] \quad (-2\,x^2) \cdot (x^2 + 5\,x) = -2\,x^4 - 10\,x^3 \\ &[6] \quad (-3\,x^2) \cdot (x) = -3\,x^3 \\ &[7] \quad (3\,x) \cdot (-2\,x^2 - 9\,x) = -6\,x^3 - 27\,x^2 \\ &[8] \quad (-4\,x^2) \cdot (2\,x^2 + 4\,x) = -8\,x^4 - 16\,x^3 \\ &[9] \quad (-3\,x^2) \cdot (4\,x^2) = -12\,x^4 \\ &[10] \quad (-2\,x^2) \cdot (-4\,x^2 + 2\,x) = 8\,x^4 - 4\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x^2+2\,x)\cdot(-2\,x^2+3\,x) = -8\,x^4+8\,x^3+6\,x^2\\ &[2] \quad (2\,x^2-2\,x)\cdot(4\,x^2-7\,x) = 8\,x^4-22\,x^3+14\,x^2\\ &[3] \quad (x^2-4\,x)\cdot(-3\,x) = -3\,x^3+12\,x^2\\ &[4] \quad (2\,x^2-3\,x)\cdot(0) = 0\\ &[5] \quad (-5\,x^2)\cdot(-2\,x^2+x) = 10\,x^4-5\,x^3\\ &[6] \quad (4\,x^2+x)\cdot(2\,x^2+7\,x) = 8\,x^4+30\,x^3+7\,x^2\\ &[7] \quad (-5\,x)\cdot(2\,x^2-x) = -10\,x^3+5\,x^2\\ &[8] \quad (-2\,x^2)\cdot(-2\,x^2-6\,x) = 4\,x^4+12\,x^3 \end{aligned}$$

[9] 
$$(-3x^2) \cdot (-2x^2 + 4x) = 6x^4 - 12x^3$$

[10] 
$$(x) \cdot (3x^2 + 4x) = 3x^3 + 4x^2$$

[11] 
$$(4x^2 + 4x) \cdot (x^2 - 4x) = 4x^4 - 12x^3 - 16x^2$$

[12] 
$$(-x) \cdot (-4x^2 - 4x) = 4x^3 + 4x^2$$

[13] 
$$(-x^2 - 3x) \cdot (2x^2) = -2x^4 - 6x^3$$

[14] 
$$(4x) \cdot (-2x^2 - 3x) = -8x^3 - 12x^2$$

[15] 
$$(2x^2) \cdot (2x^2 - 7x) = 4x^4 - 14x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-4x^3) \cdot (-2x^2 + x) = 8x^5 - 4x^4$$

[2] 
$$(-4x^3 - 2x) \cdot (3x^3 + 3x^2) = -12x^6 - 12x^5 - 6x^4 - 6x^3$$

[3] 
$$(2x^3 - 4x) \cdot (-2x^2 - 2x) = -4x^5 - 4x^4 + 8x^3 + 8x^2$$

[4] 
$$(-4x^3 + 7x^2) \cdot (-x^3 + 3x) = 4x^6 - 7x^5 - 12x^4 + 21x^3$$

[5] 
$$(2x^3) \cdot (6x^2 - 3x) = 12x^5 - 6x^4$$

[6] 
$$(2x^3 + 4x^2) \cdot (7x^3 + x^2) = 14x^6 + 30x^5 + 4x^4$$

[7] 
$$(-x^3 + 5x) \cdot (3x^3 + x^2 + 4x) = -3x^6 - x^5 + 11x^4 + 5x^3 + 20x^2$$

[8] 
$$(-x^3 + 2x) \cdot (-4x^2 + 4x) = 4x^5 - 4x^4 - 8x^3 + 8x^2$$

[9] 
$$(3x^3 + 2x) \cdot (-3x^3 - 6x) = -9x^6 - 24x^4 - 12x^2$$

[10] 
$$(-2x^3 - 2x^2 + 2x) \cdot (3x^3 - 4x^2 + 2x) = -6x^6 + 2x^5 + 10x^4 - 12x^3 + 4x^2$$

[11] 
$$(-2x^3) \cdot (3x^3 + 4x^2 + 3x) = -6x^6 - 8x^5 - 6x^4$$

[12] 
$$(0) \cdot (-x^3 - x^2 - 3x) = 0$$

[13] 
$$(x^3 + 4x^2 - 3x) \cdot (-2x^3 - 5x) = -2x^6 - 8x^5 + x^4 - 20x^3 + 15x^2$$

[14] 
$$(-3x^2 + x) \cdot (-3x^3 + 3x^2) = 9x^5 - 12x^4 + 3x^3$$

[15] 
$$(3x^2 + 3x) \cdot (4x^3 + x^2) = 12x^5 + 15x^4 + 3x^3$$

[16] 
$$(-6x^2 - 3x) \cdot (x^3 + 4x^2 + 2x) = -6x^5 - 27x^4 - 24x^3 - 6x^2$$

[17] 
$$(x) \cdot (4x^3 + 3x) = 4x^4 + 3x^2$$

[18] 
$$(-4x^3 - 3x^2) \cdot (2x^3 - 2x^2 - 3x) = -8x^6 + 2x^5 + 18x^4 + 9x^3$$

[19] 
$$(3x^2 + 3x) \cdot (4x^3 + 3x^2 + 3x) = 12x^5 + 21x^4 + 18x^3 + 9x^2$$

[20] 
$$(2x^2 - 2x) \cdot (-2x) = -4x^3 + 4x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-4x^2y + 4xy) \cdot (7x^2y - xy^2) = -28x^4y^2 + 4x^3y^3 + 28x^3y^2 - 4x^2y^3$$

[2] 
$$(xy^2 - 4xy) \cdot (-3xy) = -3x^2y^3 + 12x^2y^2$$

[3] 
$$(x^2y^2-2xy^2)\cdot(-4x^2y+xy^2-4xy) = -4x^4y^3+x^3y^4+4x^3y^3-2x^2y^4+8x^2y^3$$

[4] 
$$(5xy) \cdot (-2x^2y - 4xy) = -10x^3y^2 - 20x^2y^2$$

[5] 
$$(3x^2y^2 + 2xy) \cdot (x^2y^2 + 3x^2y + 3xy^2) = 3x^4y^4 + 9x^4y^3 + 9x^3y^4 + 2x^3y^3 + 6x^3y^2 + 6x^2y^3$$

[6] 
$$(-2x^2y - xy) \cdot (xy^2) = -2x^3y^3 - x^2y^3$$

[7] 
$$(2x^2y^2 - 4xy) \cdot (-5xy^2 + xy) = -10x^3y^4 + 2x^3y^3 + 20x^2y^3 - 4x^2y^2$$