## 1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad x^6 + 3 \, x^2 + -x^4 - 3 \, x^3 - x^2 + -3 \, x^6 - 2 \, x^5 + 4 \, x^3 = -2 \, x^6 - 2 \, x^5 - x^4 + x^3 + 2 \, x^2$$

$$[2] \quad 4 \, x^5 + x^4 + -2 \, x^6 + 2 \, x^5 + 4 \, x^3 + -2 \, x^6 + 3 \, x^5 + 2 \, x^4 = -4 \, x^6 + 9 \, x^5 + 3 \, x^4 + 4 \, x^3$$

$$[3] \quad 4 \, x^6 - 2 \, x^3 - 3 \, x + 3 \, x^4 - 3 \, x^3 + 4 \, x^2 + -x^6 - 4 \, x^2 - 2 \, x = 3 \, x^6 + 3 \, x^4 - 5 \, x^3 - 5 \, x$$

$$[4] \quad x^6 - 4 \, x^3 + -4 \, x^3 + 2 \, x^5 + 2 \, x^3 = x^6 + 2 \, x^5 - 6 \, x^3$$

$$[5] \quad 2 \, x^6 - 2 \, x^4 - x^2 + -x^6 - x^5 + 3 \, x^4 + (-3 \, x^3 + 2 \, x^2) = x^6 - x^5 + x^4 - 3 \, x^3 + x^2$$

$$[6] \quad x^5 - x^3 + 4 \, x^2 + -x^4 - x^2 - 3 \, x + 3 \, x^5 + x^3 - 3 \, x = 4 \, x^5 - x^4 + 3 \, x^2 - 6 \, x$$

$$[7] \quad 2 \, x^5 + 3 \, x^4 - 3 \, x^2 + 4 \, x^6 + 2 \, x^2 - x + 3 \, x^6 - x^3 + x^2 = 7 \, x^6 + 2 \, x^5 + 3 \, x^4 - x^3 - x$$

$$[8] \quad 5 \, x^6 + x^5 + -4 \, x^6 - 4 \, x^5 - 2 \, x^3 + 2 \, x^6 + 4 \, x^4 - 2 \, x = 3 \, x^6 - 3 \, x^5 + 4 \, x^4 - 2 \, x^3 - 2 \, x$$

$$[9] \quad 2 \, x^3 - 8 \, x^2 + 4 \, x$$

$$[9] \quad 2 \, x^3 - 8 \, x^2 + -3 \, x^5 + 4 \, x^4 + 3 \, x^3 + -2 \, x^6 + 2 \, x^5 + 4 \, x = -2 \, x^6 - x^5 + 4 \, x^4 + 5 \, x^3 - 8 \, x^2 + 4 \, x$$

$$[10] \quad -2 \, x^5 - 7 \, x^3 + (-4 \, x^4 - 7 \, x^2) + (-x^6 + 3 \, x^5) = -x^6 + x^5 - 4 \, x^4 - 7 \, x^3 - 7 \, x^2$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{array}{lll} [1] & 0+0+0=0 \\ [2] & 2\,x^2y^2+-4\,x^2y^2+2\,xy^2+-3\,x^2y^2-3\,x^2y+3\,xy^2=-5\,x^2y^2-3\,x^2y+5\,xy^2 \\ [3] & 4\,x^2y+6\,xy^2+-4\,x^2y^2+12\,xy^2+6\,xy+4\,x^2y^2-24\,xy=4\,x^2y+18\,xy^2-18\,xy \\ [4] & 9\,x^2y+9\,xy^2+-9\,x^2y+3\,xy^2-27\,xy+-9\,x^2y^2+9\,x^2y+9\,xy^2=-9\,x^2y^2+9\,x^2y+21\,xy^2-27\,xy \\ [5] & 4\,x^2y-8\,xy+-16\,x^2y+80\,xy^2+64\,x^2y-12\,xy=52\,x^2y+80\,xy^2-20\,xy \\ [6] & 15\,x^2y+20\,xy^2+-20\,x^2y-95\,xy^2+(-65\,x^2y^2+75\,x^2y)=-65\,x^2y^2+70\,x^2y-75\,xy^2 \\ [7] & 180\,x^2y^2-6\,x^2y+-6\,x^2y^2-36\,x^2y-18\,xy^2+-18\,x^2y^2+108\,xy^2+12\,xy=156\,x^2y^2-42\,x^2y+90\,xy^2+12\,xy \\ [8] & 21\,x^2y^2-147\,xy^2-7\,xy+-7\,xy+-7\,x^2y^2+7\,x^2y=14\,x^2y^2+7\,x^2y-147\,xy^2-14\,xy \\ [9] & 184\,x^2y+192\,xy^2+-248\,x^2y+-384\,x^2y^2-32\,xy^2=-384\,x^2y^2-64\,x^2y+160\,xy^2 \\ [10] & 225\,x^2y^2+324\,x^2y+9\,x^2y-162\,xy^2+324\,xy \\ [10] & 225\,x^2y^2+324\,x^2y+9\,x^2y-162\,xy^2+324\,xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 2\,x^2y^2 - 5\,xy + 4\,x^2y - 2\,xy^2 - xy - (-4\,x^2y + 5\,xy^2) = 2\,x^2y^2 + 8\,x^2y - 7\,xy^2 - 6\,xy \\ &[3] \quad -4\,x^2y^2 + -8\,x^2y + 10\,xy^2 - (4\,x^2y^2 - 8\,xy^2 + 8\,xy) = -8\,x^2y^2 - 8\,x^2y + 18\,xy^2 - 8\,xy \\ &[4] \quad -9\,x^2y^2 - 9\,x^2y + 36\,xy^2 - (-9\,x^2y - 18\,xy^2 - 3\,xy) + (36\,x^2y^2 + 9\,x^2y) = 27\,x^2y^2 + 9\,x^2y + 54\,xy^2 + 3\,xy \\ &[5] \quad -4\,xy^2 + 20\,xy + 12\,x^2y^2 + 80\,xy - (-16\,x^2y^2 + 52\,xy) = 28\,x^2y^2 - 4\,xy^2 + 48\,xy \\ &[6] \quad 75\,x^2y - 5\,xy^2 + 75\,x^2y + 25\,xy - (85\,x^2y + 25\,xy) = 65\,x^2y - 5\,xy^2 \\ &[7] \quad 24\,xy^2 + 96\,xy - (72\,x^2y - 72\,xy^2 + 144\,xy) + (-12\,xy) = -72\,x^2y + 96\,xy^2 - 60\,xy \end{aligned}$$

$$[8] \quad 196\,xy^2 - 21\,xy + -140\,xy^2 + 98\,xy - (-28\,x^2y^2 + 147\,xy^2 - 28\,xy) = 28\,x^2y^2 - 91\,xy^2 + 105\,xy$$
 
$$[9] \quad 8\,x^2y + 160\,xy^2 + -208\,xy^2 + 8\,xy - (-16\,x^2y - 64\,xy^2) = 24\,x^2y + 16\,xy^2 + 8\,xy$$
 
$$[10] \quad 153\,x^2y^2 - 36\,x^2y - (-81\,x^2y^2) + (-486\,x^2y^2 - 81\,xy) = -252\,x^2y^2 - 36\,x^2y - 81\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$[1] \quad (0) \cdot (0) = 0$$

$$[2] \quad (-2\,b^3x^3yz^3) \cdot (-3\,b^2x^3y^2z^3) = 6\,b^5x^6y^3z^6$$

$$[3] \quad (6\,b^2xyz^3) \cdot (-24\,bx^3yz^3) = -144\,b^3x^4y^2z^6$$

$$[4] \quad (9\,b^3xy^2z^3) \cdot (-18\,bxy^3z^3) = -162\,b^4x^2y^5z^6$$

$$[5] \quad (16\,b^2x^3y^3z^2) \cdot (16\,b^2x^2yz^2) = 256\,b^4x^5y^4z^4$$

$$[6] \quad (-20\,bx^3y^2z^2) \cdot (-100\,bxyz^2) = 2000\,b^2x^4y^3z^4$$

$$[7] \quad (216\,b^3x^3y^2z^2) \cdot (-216\,bx^2y^3z^2) = -46656\,b^4x^5y^5z^4$$

$$[8] \quad (1029\,bx^2y^2z^2) \cdot (-14\,b^3xy^2z) = -14406\,b^4x^3y^4z^3$$

$$[9] \quad (8\,bxy^3z^3) \cdot (1536\,bx^2y^2z^2) = 12288\,b^2x^3y^5z^5$$

$$[10] \quad (-2916\,bx^3yz) \cdot (-2916\,b^2xyz^3) = 8503056\,b^3x^4y^2z^4$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (3\,x^2) \cdot (-7\,x^2 - 3\,x) = -21\,x^4 - 9\,x^3 \\ &[2] \quad (-2\,x) \cdot (5\,x^2 + 3\,x) = -10\,x^3 - 6\,x^2 \\ &[3] \quad (4\,x) \cdot (-4\,x^2 + 7\,x) = -16\,x^3 + 28\,x^2 \\ &[4] \quad (4\,x) \cdot (x^2 + 5\,x) = 4\,x^3 + 20\,x^2 \\ &[5] \quad (2\,x^2) \cdot (3\,x^2 + 5\,x) = 6\,x^4 + 10\,x^3 \\ &[6] \quad (2\,x^2) \cdot (-3\,x^2 - 3\,x) = -6\,x^4 - 6\,x^3 \\ &[7] \quad (-4\,x) \cdot (-2\,x^2 + 8\,x) = 8\,x^3 - 32\,x^2 \\ &[8] \quad (-2\,x) \cdot (-x^2 - 2\,x) = 2\,x^3 + 4\,x^2 \\ &[9] \quad (-4\,x) \cdot (-4\,x^2 + 2\,x) = 16\,x^3 - 8\,x^2 \\ &[10] \quad (3\,x^2) \cdot (-x) = -3\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-3\,x)\cdot(-3\,x^2+2\,x) = 9\,x^3-6\,x^2 \\ &[2] \quad (-3\,x^2+2\,x)\cdot(x^2-8\,x) = -3\,x^4+26\,x^3-16\,x^2 \\ &[3] \quad (-3\,x^2+x)\cdot(-4\,x^2-2\,x) = 12\,x^4+2\,x^3-2\,x^2 \\ &[4] \quad (3\,x^2)\cdot(-2\,x^2+3\,x) = -6\,x^4+9\,x^3 \\ &[5] \quad (4\,x)\cdot(-4\,x^2+x) = -16\,x^3+4\,x^2 \\ &[6] \quad (-x^2+3\,x)\cdot(2\,x^2+4\,x) = -2\,x^4+2\,x^3+12\,x^2 \\ &[7] \quad (6\,x^2)\cdot(2\,x^2+2\,x) = 12\,x^4+12\,x^3 \\ &[8] \quad (8\,x^2)\cdot(-x^2+7\,x) = -8\,x^4+56\,x^3 \\ &[9] \quad (-x^2+3\,x)\cdot(2\,x) = -2\,x^3+6\,x^2 \\ &[10] \quad (4\,x^2-3\,x)\cdot(-5\,x^2+2\,x) = -20\,x^4+23\,x^3-6\,x^2 \end{aligned}$$

[11] 
$$(0) \cdot (2x^2 - 4x) = 0$$

[12] 
$$(-4x^2 - 4x) \cdot (-4x^2 + 4x) = 16x^4 - 16x^2$$

[13] 
$$(-2x^2 + 4x) \cdot (-2x^2 + x) = 4x^4 - 10x^3 + 4x^2$$

[14] 
$$(2x^2 + 4x) \cdot (3x^2 + 3x) = 6x^4 + 18x^3 + 12x^2$$

[15] 
$$(x^2 + x) \cdot (8x^2 - x) = 8x^4 + 7x^3 - x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(2x^3 - 6x^2) \cdot (-x^2 - 5x) = -2x^5 - 4x^4 + 30x^3$$

[2] 
$$(5x) \cdot (3x^2 + 4x) = 15x^3 + 20x^2$$

[3] 
$$(2x^3 + x^2) \cdot (-2x^2 - 5x) = -4x^5 - 12x^4 - 5x^3$$

[4] 
$$(3x^3 + x^2) \cdot (-x^3 - 4x^2 - 3x) = -3x^6 - 13x^5 - 13x^4 - 3x^3$$

[5] 
$$(6x^3) \cdot (2x^3 + 2x^2 + 5x) = 12x^6 + 12x^5 + 30x^4$$

[6] 
$$(-x^2) \cdot (7x^2) = -7x^4$$

[7] 
$$(-4x^3 - 6x^2) \cdot (-x^3 - 2x^2 - x) = 4x^6 + 14x^5 + 16x^4 + 6x^3$$

[8] 
$$(3x^2 + 2x) \cdot (-3x^3 + x^2) = -9x^5 - 3x^4 + 2x^3$$

[9] 
$$(x^2) \cdot (8x^3 + 2x^2) = 8x^5 + 2x^4$$

[10] 
$$(x^3) \cdot (-4x^3 - 4x) = -4x^6 - 4x^4$$

[11] 
$$(2x^3 + 2x^2) \cdot (-6x^3 - 2x^2 - x) = -12x^6 - 16x^5 - 6x^4 - 2x^3$$

[12] 
$$(-2x^3 - 3x^2) \cdot (-4x^2) = 8x^5 + 12x^4$$

[13] 
$$(-x^3) \cdot (-2x^2) = 2x^5$$

[14] 
$$(-2x^3 - x) \cdot (7x) = -14x^4 - 7x^2$$

[15] 
$$(6x^3) \cdot (-8x^2) = -48x^5$$

[16] 
$$(4x^3 - 3x^2) \cdot (-3x^3 + 2x) = -12x^6 + 9x^5 + 8x^4 - 6x^3$$

[17] 
$$(2x) \cdot (-4x^2 - 8x) = -8x^3 - 16x^2$$

[18] 
$$(3x^3 - 2x^2) \cdot (-4x^3 - x^2 + x) = -12x^6 + 5x^5 + 5x^4 - 2x^3$$

[19] 
$$(-2x^3 - 2x) \cdot (3x^3) = -6x^6 - 6x^4$$

[20] 
$$(4x^3 - 3x^2) \cdot (x^3 + 3x^2 + x) = 4x^6 + 9x^5 - 5x^4 - 3x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(4x^2y - 3xy) \cdot (-2x^2y^2 + xy^2) = -8x^4y^3 + 10x^3y^3 - 3x^2y^3$$

[2] 
$$(4x^2y + 3xy^2) \cdot (-x^2y) = -4x^4y^2 - 3x^3y^3$$

[3] 
$$(-x^2y^2 + 3xy) \cdot (-3x^2y - 4xy^2 + 3xy) = 3x^4y^3 + 4x^3y^4 - 3x^3y^3 - 9x^3y^2 - 12x^2y^3 + 9x^2y^2$$

[4] 
$$(5x^2y) \cdot (x^2y^2 + 3x^2y) = 5x^4y^3 + 15x^4y^2$$

[5] 
$$(3xy^2 + 2xy) \cdot (-3x^2y - 2xy) = -9x^3y^3 - 6x^3y^2 - 6x^2y^3 - 4x^2y^2$$

[6] 
$$(0) \cdot (3x^2y^2) = 0$$

[7] 
$$(-4x^2y - 4xy^2) \cdot (-4x^2y^2 + 3xy^2) = 16x^4y^3 + 16x^3y^4 - 12x^3y^3 - 12x^2y^4$$