1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad x^4 + 3 \, x^3 + 2 \, x^2 + -x^5 - 4 \, x^3 + 4 \, x + (-2 \, x^5 - 4 \, x^4 + 4 \, x^2) = -3 \, x^5 - 3 \, x^4 - x^3 + 6 \, x^2 + 4 \, x$$

$$[2] \quad x^6 - 2 \, x^2 + 3 \, x + -6 \, x^4 + 2 \, x + (-x^3 + 2 \, x) = x^6 - 6 \, x^4 - x^3 - 2 \, x^2 + 7 \, x$$

$$[3] \quad 3 \, x^3 - 2 \, x + x^6 - 2 \, x^4 + x^5 - 2 \, x^4 + 4 \, x^2 = x^6 + x^5 - 4 \, x^4 + 3 \, x^3 + 4 \, x^2 - 2 \, x$$

$$[4] \quad x^5 - 7 \, x + -5 \, x^6 + 2 \, x^3 + -3 \, x^4 - x^2 + x = -5 \, x^6 + x^5 - 3 \, x^4 + 2 \, x^3 - x^2 - 6 \, x$$

$$[5] \quad 3 \, x^5 + x^4 - x + -2 \, x^6 - x^2 + x + -3 \, x^6 + x^2 - 2 \, x = -5 \, x^6 + 3 \, x^5 + x^4 - 2 \, x$$

$$[6] \quad 4 \, x^6 + x^4 + 3 \, x^3 + -2 \, x^6 - 5 \, x^4 + 3 \, x^6 + 3 \, x^5 + 2 \, x = 5 \, x^6 + 3 \, x^5 - 4 \, x^4 + 3 \, x^3 + 2 \, x$$

$$[7] \quad 7 \, x^5 - 4 \, x^3 + -4 \, x^5 - 4 \, x^3 - 3 \, x^2 + (-x^6 + x^5 - 4 \, x^3) = -x^6 + 4 \, x^5 - 12 \, x^3 - 3 \, x^2$$

$$[8] \quad x^4 + x^3 - 3 \, x + -2 \, x^6 + 3 \, x^3 + 3 \, x^2 + (-2 \, x^6 - 7 \, x^3) = -4 \, x^6 + x^4 - 3 \, x^3 + 3 \, x^2 - 3 \, x$$

$$[9] \quad 3 \, x^3 + 6 \, x + 4 \, x^4 - 5 \, x^3 + 4 \, x^5 + 6 \, x^2 = 4 \, x^5 + 4 \, x^4 - 2 \, x^3 + 6 \, x^2 + 6 \, x$$

$$[10] \quad 4 \, x^6 + 3 \, x^5 + x^2 + -4 \, x^5 + 2 \, x^4 - x^2 + -4 \, x^5 + 2 \, x^3 = 4 \, x^6 - 5 \, x^5 + 2 \, x^4 + 2 \, x^3 + 2 \, x^4 + 2 \, x^3 + 2 \, x^4 + 2 \, x^3 + 2 \, x^4 + 2$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 3x^2y-4xy^2-3xy+2x^2y^2+4x^2y^2-xy^2=6x^2y^2+3x^2y-5xy^2-3xy \\ [3] \quad -4x^2y^2-4x^2y+12xy+(-12x^2y^2+4xy^2)+(-4x^2y-6xy^2)=-16x^2y^2-8x^2y-2xy^2+12xy \\ [4] \quad 9x^2y+9xy^2+3xy+45x^2y^2+36xy+3x^2y+33xy=45x^2y^2+12x^2y+9xy^2+72xy \\ [5] \quad 16x^2y^2-8xy+64x^2y^2-20xy+8x^2y^2-64x^2y+4xy=88x^2y^2-64x^2y-24xy \\ [6] \quad 40xy^2-50xy+-60x^2y^2+50xy^2+(-70x^2y^2)=-130x^2y^2+90xy^2-50xy \\ [7] \quad 144x^2y-18xy^2-144xy+-12x^2y^2-144xy^2+36xy+(-60x^2y^2+72xy^2)=-72x^2y^2+144x^2y-90xy^2-108xy \\ [8] \quad -175x^2y^2+147xy^2+(-49x^2y^2+196x^2y+147xy^2)+(-7x^2y^2+21x^2y+49xy^2)=-231x^2y^2+217x^2y+343xy^2 \\ [9] \quad 8x^2y^2+48xy+-64x^2y^2-16x^2y-192xy+-128xy^2-256xy=-56x^2y^2-16x^2y-128xy^2-400xy \\ [10] \quad 9x^2y^2-162x^2y+81xy^2+243x^2y^2+198xy^2+-243xy^2=252x^2y^2-162x^2y+36xy^2 \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 4\,x^2y + 4\,xy + 2\,x^2y^2 + 2\,x^2y - (4\,x^2y - 2\,xy^2) = 2\,x^2y^2 + 2\,x^2y + 2\,xy^2 + 4\,xy \\ &[3] \quad -16\,x^2y + 2\,xy^2 - 4\,xy + 4\,x^2y^2 - 16\,xy - (14\,x^2y^2 - 8\,x^2y) = -10\,x^2y^2 - 8\,x^2y + 2\,xy^2 - 20\,xy \\ &[4] \quad -9\,x^2y + 18\,xy^2 - (-9\,x^2y^2 + 6\,x^2y) + (27\,x^2y - 18\,xy^2) = 9\,x^2y^2 + 12\,x^2y \\ &[5] \quad -16\,x^2y^2 + 32\,x^2y + 8\,x^2y^2 + 56\,xy^2 - (32\,xy^2 + 56\,xy) = -8\,x^2y^2 + 32\,x^2y + 24\,xy^2 - 56\,xy \end{aligned}$$

$$[6] \quad 50 \, x^2 y^2 - 10 \, x^2 y - 75 \, xy + -15 \, x^2 y + 10 \, xy^2 - 10 \, xy - (-75 \, x^2 y + 20 \, xy^2 + 5 \, xy) = \\ 50 \, x^2 y^2 + 50 \, x^2 y - 10 \, xy^2 - 90 \, xy \\ [7] \quad 144 \, x^2 y^2 + 48 \, x^2 y - (168 \, x^2 y^2 - 12 \, xy^2) + (12 \, x^2 y + 12 \, xy) = -24 \, x^2 y^2 + \\ 60 \, x^2 y + 12 \, xy^2 + 12 \, xy \\ [8] \quad 14 \, x^2 y^2 - 196 \, x^2 y - 98 \, xy^2 + 28 \, x^2 y - (-28 \, x^2 y + 343 \, xy) = 14 \, x^2 y^2 - 140 \, x^2 y - \\ 98 \, xy^2 - 343 \, xy \\ [9] \quad 24 \, x^2 y^2 - 200 \, xy + -8 \, x^2 y^2 - 256 \, xy^2 + 64 \, xy - (32 \, x^2 y^2 + 16 \, x^2 y + 24 \, xy^2) = \\ -16 \, x^2 y^2 - 16 \, x^2 y - 280 \, xy^2 - 136 \, xy \\ [10] \quad -81 \, x^2 y + 162 \, xy^2 + 27 \, xy - (9 \, x^2 y^2 - 81 \, x^2 y) + (189 \, x^2 y + 162 \, xy^2) = \\ -9 \, x^2 y^2 + 189 \, x^2 y + 324 \, xy^2 + 27 \, xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (2\,b^2x^3y^2z^2) \cdot (-4\,b^2x^2yz^2) = -8\,b^4x^5y^3z^4 \\ &[3] \quad (-6\,b^2x^2yz^2) \cdot (-8\,b^2x^3y^3z) = 48\,b^4x^5y^4z^3 \\ &[4] \quad (-81\,b^2x^2yz^3) \cdot (27\,b^3x^3y^2z) = -2187\,b^5x^5y^3z^4 \\ &[5] \quad (64\,bx^3yz^2) \cdot (16\,b^3x^2y^2z) = 1024\,b^4x^5y^3z^3 \\ &[6] \quad (-20\,b^3x^3y^3z) \cdot (-25\,b^3x^3yz) = 500\,b^6x^6y^4z^2 \\ &[7] \quad (-144\,b^3x^3y^2z^2) \cdot (-24\,b^2x^2yz^3) = 3456\,b^5x^5y^3z^5 \\ &[8] \quad (343\,b^2xy^3z) \cdot (-686\,b^3x^3y^3z^2) = -235298\,b^5x^4y^6z^3 \\ &[9] \quad (8\,b^3x^2yz^2) \cdot (-128\,b^2x^2y^3z^2) = -1024\,b^5x^4y^4z^4 \\ &[10] \quad (81\,b^3xy^2z) \cdot (-18\,b^2x^3y^2z^3) = -1458\,b^5x^4y^4z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (-3\,x^2) \cdot (-4\,x^2 - 2\,x) = 12\,x^4 + 6\,x^3 \\ & [2] \quad (-2\,x^2) \cdot (x^2 + 5\,x) = -2\,x^4 - 10\,x^3 \\ & [3] \quad (3\,x^2) \cdot (-8\,x^2 + 5\,x) = -24\,x^4 + 15\,x^3 \\ & [4] \quad (-2\,x^2) \cdot (-3\,x^2 - x) = 6\,x^4 + 2\,x^3 \\ & [5] \quad (-x^2) \cdot (-2\,x^2 + x) = 2\,x^4 - x^3 \\ & [6] \quad (3\,x^2) \cdot (-x^2 + x) = -3\,x^4 + 3\,x^3 \\ & [7] \quad (-2\,x^2) \cdot (-3\,x^2 + 3\,x) = 6\,x^4 - 6\,x^3 \\ & [8] \quad (x) \cdot (-3\,x^2 - x) = -3\,x^3 - x^2 \\ & [9] \quad (4\,x^2) \cdot (-6\,x^2 - 8\,x) = -24\,x^4 - 32\,x^3 \\ & [10] \quad (4\,x) \cdot (5\,x) = 20\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x) \cdot (-7\,x^2 + 3\,x) = 7\,x^3 - 3\,x^2 \\ &[2] \quad (-4\,x^2 - 2\,x) \cdot (-3\,x^2 + x) = 12\,x^4 + 2\,x^3 - 2\,x^2 \\ &[3] \quad (x^2 + 3\,x) \cdot (5\,x^2 - 2\,x) = 5\,x^4 + 13\,x^3 - 6\,x^2 \\ &[4] \quad (3\,x^2 + 4\,x) \cdot (3\,x^2) = 9\,x^4 + 12\,x^3 \\ &[5] \quad (-x^2 - 3\,x) \cdot (3\,x^2 + 5\,x) = -3\,x^4 - 14\,x^3 - 15\,x^2 \\ &[6] \quad (-x) \cdot (x^2 + 2\,x) = -x^3 - 2\,x^2 \end{aligned}$$

[7]
$$(0) \cdot (-8x^2 - x) = 0$$

[8]
$$(0) \cdot (2x^2) = 0$$

[9]
$$(2x^2 + 2x) \cdot (-x^2) = -2x^4 - 2x^3$$

[10]
$$(3x^2 - 3x) \cdot (-3x^2) = -9x^4 + 9x^3$$

[11]
$$(3x^2) \cdot (-4x^2 + x) = -12x^4 + 3x^3$$

[12]
$$(-4x^2 + 3x) \cdot (-6x^2 - 4x) = 24x^4 - 2x^3 - 12x^2$$

[13]
$$(3x^2) \cdot (-x^2 + 4x) = -3x^4 + 12x^3$$

[14]
$$(-x^2 - 4x) \cdot (-x^2 - 3x) = x^4 + 7x^3 + 12x^2$$

[15]
$$(-4x^2 + 3x) \cdot (3x^2) = -12x^4 + 9x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x) \cdot (x^3 - 2x^2) = x^4 - 2x^3$$

[2]
$$(-4x^3) \cdot (-3x^2 + 4x) = 12x^5 - 16x^4$$

[3]
$$(x^2 + 3x) \cdot (-9x) = -9x^3 - 27x^2$$

[4]
$$(4x^3 + 6x^2) \cdot (3x^2 - 2x) = 12x^5 + 10x^4 - 12x^3$$

[5]
$$(-x^3 - 4x^2) \cdot (-x^3 - 2x^2 - 2x) = x^6 + 6x^5 + 10x^4 + 8x^3$$

[6]
$$(2x) \cdot (-6x^3 - 4x^2 + 3x) = -12x^4 - 8x^3 + 6x^2$$

[7]
$$(-2x^3 + 3x) \cdot (-4x^2 - 2x) = 8x^5 + 4x^4 - 12x^3 - 6x^2$$

[8]
$$(-3x) \cdot (-3x^3 + 7x^2) = 9x^4 - 21x^3$$

[9]
$$(3x^3 - 2x) \cdot (-5x^2) = -15x^5 + 10x^3$$

[10]
$$(-3x^3 - x^2 + x) \cdot (x^3 + 8x^2) = -3x^6 - 25x^5 - 7x^4 + 8x^3$$

[11]
$$(2x^2 - 3x) \cdot (-4x^3 - 4x^2) = -8x^5 + 4x^4 + 12x^3$$

[12]
$$(-2x^3) \cdot (-3x) = 6x^4$$

[13]
$$(5x^3 + 4x^2) \cdot (-x^3 - x^2) = -5x^6 - 9x^5 - 4x^4$$

[14]
$$(-2x^2) \cdot (3x^3 - 5x^2) = -6x^5 + 10x^4$$

[15]
$$(-3x^3 + x^2) \cdot (x^3 - 3x) = -3x^6 + x^5 + 9x^4 - 3x^3$$

[16]
$$(-2x^3 - 2x^2 - 3x) \cdot (-3x^3 - 7x) = 6x^6 + 6x^5 + 23x^4 + 14x^3 + 21x^2$$

[17]
$$(3x^2 + 4x) \cdot (-3x^3 - x) = -9x^5 - 12x^4 - 3x^3 - 4x^2$$

[18]
$$(4x^3 + x) \cdot (-x^3) = -4x^6 - x^4$$

[19]
$$(-2x^3 - 3x^2 - x) \cdot (-4x) = 8x^4 + 12x^3 + 4x^2$$

[20]
$$(0) \cdot (5x^2 + x) = 0$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^2y + 2xy^2) \cdot (4x^2y^2 + 4x^2y + 3xy) = -12x^4y^3 + 8x^3y^4 - 12x^4y^2 + 8x^3y^3 - 9x^3y^2 + 6x^2y^3$$

[2]
$$(3x^2y^2 - xy^2) \cdot (x^2y^2 + 2x^2y) = 3x^4y^4 + 6x^4y^3 - x^3y^4 - 2x^3y^3$$

[3]
$$(-4x^2y - 4xy) \cdot (-2x^2y^2 - 3x^2y - 3xy^2) = 8x^4y^3 + 12x^4y^2 + 20x^3y^3 + 12x^3y^2 + 12x^2y^3$$

[4]
$$(-6x^2y) \cdot (-2x^2y + xy^2 + 3xy) = 12x^4y^2 - 6x^3y^3 - 18x^3y^2$$

$$[5] \quad (-2\,x^2y^2 + 3\,x^2y) \cdot (-2\,x^2y^2 + 3\,x^2y - xy) = 4\,x^4y^4 - 12\,x^4y^3 + 9\,x^4y^2 + 2\,x^3y^3 - 3\,x^3y^2$$

$$[6] \quad (4\,x^2y + 4\,xy) \cdot (-2\,x^2y^2 - 3\,x^2y + 4\,xy) = -8\,x^4y^3 - 12\,x^4y^2 - 8\,x^3y^3 + 4\,x^3y^2 + 16\,x^2y^2$$

$$[7] \quad (x^2y^2 + 2\,x^2y) \cdot (3\,x^2y - 4\,xy^2 + 2\,xy) = 3\,x^4y^3 - 4\,x^3y^4 + 6\,x^4y^2 - 6\,x^3y^3 + 4\,x^3y^2$$