1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0+0+0=0 \\ & [2] \quad 4\,x^2y+4\,xy^2+3\,xy+x^2y^2+4\,xy^2+-x^2y^2=4\,x^2y+8\,xy^2+3\,xy \\ & [3] \quad 26\,x^2y+-6\,x^2y-4\,xy+(-20\,x^2y^2)=-20\,x^2y^2+20\,x^2y-4\,xy \\ & [4] \quad 6\,x^2y^2+6\,x^2y-9\,xy^2+-9\,x^2y^2-54\,xy+9\,x^2y-21\,xy=-3\,x^2y^2+15\,x^2y-9\,xy^2-75\,xy \\ & [5] \quad 64\,x^2y^2-64\,xy^2+32\,xy+-16\,x^2y^2+8\,x^2y-8\,xy^2+12\,xy=48\,x^2y^2+8\,x^2y-72\,xy^2+44\,xy \\ & [6] \quad 75\,x^2y^2-25\,x^2y-75\,xy^2+-25\,x^2y^2-10\,x^2y+-20\,x^2y^2+35\,x^2y=30\,x^2y^2-75\,xy^2 \\ & [7] \quad 18\,x^2y+6\,xy^2+120\,x^2y^2+108\,xy+-18\,x^2y^2=102\,x^2y^2+18\,x^2y+6\,xy^2+108\,xy \\ & [8] \quad 98\,x^2y^2+147\,xy^2-147\,xy+196\,x^2y^2+14\,xy^2+28\,x^2y^2+49\,xy^2=322\,x^2y^2+210\,x^2y^2-147\,xy \\ & [9] \quad -256\,x^2y-128\,xy^2+16\,xy+(-8\,x^2y+16\,xy)+(-184\,x^2y+16\,xy)=-448\,x^2y-128\,xy^2+48\,xy \\ & [10] \quad 405\,x^2y^2+9\,x^2y+9\,xy^2+306\,xy+-18\,x^2y^2-81\,x^2y-81\,xy=387\,x^2y^2-72\,x^2y+9\,xy^2+225\,xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -4\,x^2y^2 - 3\,x^2y - xy + 4\,xy^2 - xy - (-x^2y^2 - 3\,x^2y) = -3\,x^2y^2 + 4\,xy^2 - 2\,xy \\ &[3] \quad 16\,x^2y^2 + 8\,x^2y + 6\,xy + 16\,x^2y^2 - 4\,x^2y - (10\,x^2y^2 + 8\,x^2y) = 22\,x^2y^2 - 4\,x^2y + 6\,xy \\ &[4] \quad 21\,x^2y^2 - 27\,xy^2 - (3\,x^2y^2 - 18\,xy^2 - 18\,xy) + (-15\,x^2y^2 + 9\,xy^2) = 3\,x^2y^2 + 18\,xy \\ &[5] \quad 20\,x^2y + 32\,xy + 48\,x^2y^2 - 32\,x^2y - 48\,xy^2 - (16\,x^2y^2 - 32\,xy) = 32\,x^2y^2 - 12\,x^2y - 48\,xy^2 + 64\,xy \end{aligned}$$

$$\begin{aligned} & [6] \quad -100\,x^2y^2 + 100\,x^2y - 20\,xy^2 + -20\,x^2y^2 - 10\,x^2y - 25\,xy^2 - (-10\,x^2y) = \\ & -120\,x^2y^2 + 100\,x^2y - 45\,xy^2 \\ & [7] \quad 72\,x^2y + 12\,xy^2 - (-138\,x^2y + 72\,xy^2) + (12\,xy^2 - 78\,xy) = 210\,x^2y - 48\,xy^2 - \\ & 78\,xy \\ & [8] \quad 147\,x^2y^2 - 49\,x^2y + 28\,x^2y^2 + 7\,xy^2 + 14\,xy - (-28\,x^2y^2 + 49\,xy^2 - 98\,xy) = \\ & 203\,x^2y^2 - 49\,x^2y - 42\,xy^2 + 112\,xy \\ & [9] \quad 192\,x^2y + 96\,xy^2 + -24\,x^2y^2 + 280\,xy^2 - (-8\,x^2y - 24\,xy^2 - 8\,xy) = -24\,x^2y^2 + \\ & 200\,x^2y + 400\,xy^2 + 8\,xy \\ & [10] \quad 108\,x^2y^2 - 243\,xy^2 - (-27\,x^2y^2 - 243\,xy^2 - 9\,xy) + (-18\,x^2y^2 - 324\,x^2y + 162\,xy) = 117\,x^2y^2 - 324\,x^2y + 171\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-bx^3y^2z^3) \cdot (4\,bx^2y^2z) = -4\,b^2x^5y^4z^4 \\ &[3] \quad (-16\,b^2x^3y^2z) \cdot (-4\,b^3x^3y^2z) = 64\,b^5x^6y^4z^2 \\ &[4] \quad (54\,b^3x^3y^2z^2) \cdot (12\,bx^2y^2z) = 648\,b^4x^5y^4z^3 \\ &[5] \quad (64\,b^3x^3y^3z) \cdot (8\,b^2xy^2z^3) = 512\,b^5x^4y^5z^4 \\ &[6] \quad (-125\,bx^2y^3z^3) \cdot (-20\,b^3xyz^2) = 2500\,b^4x^3y^4z^5 \\ &[7] \quad (-216\,b^2x^2yz) \cdot (-6\,b^2x^2yz^2) = 1296\,b^4x^4y^2z^3 \\ &[8] \quad (7\,bx^3yz) \cdot (343\,b^2x^2y^2z^2) = 2401\,b^3x^5y^3z^3 \\ &[9] \quad (-1536\,bx^2y^2z) \cdot (2048\,bxy^3z) = -3145728\,b^2x^3y^5z^2 \\ &[10] \quad (18\,b^3xy^2z) \cdot (9\,bx^2y^2z^2) = 162\,b^4x^3y^4z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x^2) \cdot (-5x^2) = -10x^4$$

[2] $(-2x) \cdot (-x^2 - 6x) = 2x^3 + 12x^2$
[3] $(3x^2) \cdot (-2x^2 + x) = -6x^4 + 3x^3$
[4] $(-3x) \cdot (8x^2 + x) = -24x^3 - 3x^2$
[5] $(x^2) \cdot (-x^2 - 2x) = -x^4 - 2x^3$
[6] $(-x^2) \cdot (8x^2 + 4x) = -8x^4 - 4x^3$
[7] $(2x) \cdot (x^2 + 4x) = 2x^3 + 8x^2$
[8] $(4x^2) \cdot (-2x) = -8x^3$
[9] $(-2x^2) \cdot (-3x^2 + 5x) = 6x^4 - 10x^3$
[10] $(x) \cdot (2x^2 + 4x) = 2x^3 + 4x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-4x^2 - x) \cdot (x^2) = -4x^4 - x^3$$

[2] $(7x) \cdot (-6x^2) = -42x^3$
[3] $(-8x^2) \cdot (x^2 - 4x) = -8x^4 + 32x^3$
[4] $(x) \cdot (x^2 + 4x) = x^3 + 4x^2$
[5] $(0) \cdot (-5x^2 + 4x) = 0$
[6] $(4x^2 + 3x) \cdot (4x^2 - 5x) = 16x^4 - 8x^3 - 15x^2$

[7]
$$(0) \cdot (-x^2 - 3x) = 0$$

[8]
$$(-4x^2 + x) \cdot (-4x^2 - 8x) = 16x^4 + 28x^3 - 8x^2$$

[9]
$$(3x^2) \cdot (4x^2 + x) = 12x^4 + 3x^3$$

[10]
$$(x^2) \cdot (6x^2 - 4x) = 6x^4 - 4x^3$$

[11]
$$(-4x^2 - 2x) \cdot (-x) = 4x^3 + 2x^2$$

[12]
$$(2x^2) \cdot (-2x) = -4x^3$$

[13]
$$(x^2 + x) \cdot (-2x^2 - 2x) = -2x^4 - 4x^3 - 2x^2$$

[14]
$$(-6x^2) \cdot (-2x^2 + x) = 12x^4 - 6x^3$$

[15]
$$(-5x) \cdot (2x^2 + x) = -10x^3 - 5x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-4x^3) \cdot (-5x^3 - 2x) = 20x^6 + 8x^4$$

[2]
$$(2x^3 - 4x^2) \cdot (-x^3 + 2x^2) = -2x^6 + 8x^5 - 8x^4$$

[3]
$$(4x^2 - 4x) \cdot (-3x^3 - 3x) = -12x^5 + 12x^4 - 12x^3 + 12x^2$$

[4]
$$(-4x^3 - x) \cdot (5x^2 + x) = -20x^5 - 4x^4 - 5x^3 - x^2$$

[5]
$$(8x) \cdot (5x^3 - 6x^2) = 40x^4 - 48x^3$$

[6]
$$(2x^3 - x) \cdot (-4x^3 - 5x) = -8x^6 - 6x^4 + 5x^2$$

[7]
$$(4x^3) \cdot (-x^2 - 4x) = -4x^5 - 16x^4$$

[8]
$$(5x^3) \cdot (3x^3 - 3x^2 - 6x) = 15x^6 - 15x^5 - 30x^4$$

[9]
$$(3x^3 - 2x) \cdot (-6x^3 - 4x^2 + 3x) = -18x^6 - 12x^5 + 21x^4 + 8x^3 - 6x^2$$

[10]
$$(-4x^2 - 3x) \cdot (-x^2 + 3x) = 4x^4 - 9x^3 - 9x^2$$

[11]
$$(4x^3) \cdot (x^2 - 4x) = 4x^5 - 16x^4$$

[12]
$$(3x^2 - 3x) \cdot (2x^3 + 4x^2) = 6x^5 + 6x^4 - 12x^3$$

[13]
$$(3x^3 - 4x^2 - 3x) \cdot (2x^3 + 6x^2) = 6x^6 + 10x^5 - 30x^4 - 18x^3$$

[14]
$$(-4x^2 - 4x) \cdot (-5x^2 + x) = 20x^4 + 16x^3 - 4x^2$$

[15]
$$(-4x^3 - 2x) \cdot (-4x^3 - 2x) = 16x^6 + 16x^4 + 4x^2$$

[16]
$$(4x) \cdot (-4x^2 + 4x) = -16x^3 + 16x^2$$

[17]
$$(4x^3 + x^2) \cdot (4x^3 + 2x) = 16x^6 + 4x^5 + 8x^4 + 2x^3$$

[18]
$$(0) \cdot (4x^3 - 4x^2 + 2x) = 0$$

[19]
$$(-4x^2 - 5x) \cdot (x^3 - 5x) = -4x^5 - 5x^4 + 20x^3 + 25x^2$$

[20]
$$(-4x^2 + x) \cdot (-x^3 + x^2 + 3x) = 4x^5 - 5x^4 - 11x^3 + 3x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2y^2 + xy) \cdot (-2x^2y^2 + 6x^2y) = -2x^4y^4 + 6x^4y^3 - 2x^3y^3 + 6x^3y^2$$

[2]
$$(-3x^2y + 3xy^2) \cdot (0) = 0$$

[3]
$$(xy^2 - 4xy) \cdot (-x^2y + 6xy^2) = -x^3y^3 + 6x^2y^4 + 4x^3y^2 - 24x^2y^3$$

[4]
$$(-4x^2y^2 + 4xy^2) \cdot (-x^2y) = 4x^4y^3 - 4x^3y^3$$

[5]
$$(2x^2y^2) \cdot (x^2y^2 + 3x^2y) = 2x^4y^4 + 6x^4y^3$$

[6]
$$(-x^2y^2 + xy^2) \cdot (4x^2y + xy^2 - 2xy) = -4x^4y^3 - x^3y^4 + 6x^3y^3 + x^2y^4 - 2x^2y^3$$

[7]
$$(6x^2y^2) \cdot (2xy^2 + xy) = 12x^3y^4 + 6x^3y^3$$