1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$3x^4 + 4x^3 - 3x + 2x^3 + 4x^2 + 3x + x^6 - 3x^3 - 3x = x^6 + 3x^4 + 3x^3 + 4x^2 - 3x$$

[2] $0 + x^4 + 6x + x^5 + x^3 + 4x^2 = x^5 + x^4 + x^3 + 4x^2 + 6x$
[3] $x^5 + 2x^4 + -5x^4 - 2x + 3x^6 - 2x^4 + 2x = 3x^6 + x^5 - 5x^4$
[4] $3x^5 + x^4 + 4x + 3x^6 - 3x^3 + -4x^3 + 2x^2 = 3x^6 + 3x^5 + x^4 - 7x^3 + 2x^2 + 4x$
[5] $x^4 - 4x^3 + x + -x^6 + 4x^5 - 3x^3 + -x^6 - 2x^3 - 2x^2 = -2x^6 + 4x^5 + x^4 - 9x^3 - 2x^2 + x$
[6] $2x^5 - 4x^3 - 2x^2 + -6x^4 + 4x^2 + 4x^5 + x^4 - x = 6x^5 - 5x^4 - 4x^3 + 2x^2 - x$
[7] $x^4 - x^3 - 4x + 2x^5 + x^3 + 4x^5 + 4x^2 - 4x = 6x^5 + x^4 + 4x^2 - 8x$
[8] $x^5 + x^2 - 2x + -9x^4 + -2x^6 - 3x^4 + 3x^3 = -2x^6 + x^5 - 12x^4 + 3x^3 + x^2 - 2x$
[9] $2x^6 + 2x^3 + 4x + 2x^5 - x + 2x^6 - 2x^4 - x = 4x^6 + 2x^5 - 2x^4 + 2x^3 + 2x$

[10] $2x^6 + -4x^6 + x^2 + 2x^6 - 2x^3 - 3x^2 = -2x^3 - 2x^2$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 3x^2y^2-3x^2y-4xy^2+-xy^2+4xy+2x^2y^2=5x^2y^2-3x^2y-5xy^2+4xy \\ [3] \quad 2x^2y+12xy^2-4xy+-6x^2y+6xy^2+6xy+-2xy^2-4xy=-4x^2y+16xy^2-2xy \\ [4] \quad 9x^2y^2+27xy+-36x^2y^2-9x^2y-12xy^2+9x^2y^2-27xy^2=-18x^2y^2-9x^2y-39xy^2+27xy \\ [5] \quad 8xy^2+8x^2y^2-8xy^2-64xy+16x^2y^2+8x^2y+64xy^2=24x^2y^2+8x^2y+64xy^2-64xy \\ [6] \quad 15x^2y^2-20x^2y-5xy+-5x^2y^2+75x^2y-50xy+-75x^2y^2-75x^2y+50xy=-65x^2y^2-20x^2y-5xy \\ [7] \quad -120x^2y+144xy+(-18x^2y^2-6x^2y-12xy^2)+(-150xy^2-18xy)=-18x^2y^2-126x^2y-162xy^2+126xy \\ [8] \quad 28x^2y^2-21x^2y+28xy+196x^2y^2+28x^2y+147xy+-7x^2y=224x^2y^2+175xy \\ [9] \quad -16x^2y^2+192x^2y+64xy^2+(-32x^2y^2+128x^2y+8xy^2)+(-32x^2y+96xy)=-48x^2y^2+288x^2y+72xy^2+96xy \\ [10] \quad 81x^2y^2+324xy^2+81xy+-108x^2y^2-81xy+18xy^2-261xy=-27x^2y^2+342xy^2-261xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -4\,x^2y^2 + 4\,x^2y + 3\,xy + 6\,x^2y^2 + 2\,xy^2 - (-4\,x^2y^2 - 4\,xy^2) = 6\,x^2y^2 + 4\,x^2y + 6\,xy^2 + 3\,xy \\ &[3] \quad 8\,x^2y^2 + 10\,xy + -12\,x^2y + 2\,xy^2 - (-6\,x^2y^2 + 2\,xy^2) = 14\,x^2y^2 - 12\,x^2y + 10\,xy \\ &[4] \quad -27\,x^2y^2 + 3\,x^2y + 18\,xy^2 - (3\,x^2y^2 - 27\,xy^2 - 27\,xy) + (33\,x^2y^2) = 3\,x^2y^2 + 3\,x^2y + 45\,xy^2 + 27\,xy \end{aligned}$$

$$[5] \quad 32\,x^2y^2 - 60\,xy^2 + -44\,x^2y - \left(-16\,x^2y^2 + 64\,xy\right) = 48\,x^2y^2 - 44\,x^2y - 60\,xy^2 - 64\,xy \\ [6] \quad 10\,x^2y^2 + 70\,xy + 15\,x^2y^2 - 50\,x^2y - 20\,xy^2 - \left(-75\,x^2y\right) = 25\,x^2y^2 + 25\,x^2y - 20\,xy^2 + 70\,xy \\ [7] \quad 36\,x^2y + 48\,xy - \left(-144\,x^2y^2 + 18\,xy^2 - 12\,xy\right) + \left(168\,x^2y^2\right) = 312\,x^2y^2 + 36\,x^2y - 18\,xy^2 + 60\,xy \\ [8] \quad 133\,x^2y^2 - 147\,x^2y + -98\,x^2y^2 + 7\,xy^2 - \left(21\,xy^2 + 196\,xy\right) = 35\,x^2y^2 - 147\,x^2y - 14\,xy^2 - 196\,xy \\ [9] \quad -8\,x^2y - 72\,xy^2 + -16\,x^2y^2 - 32\,x^2y - 16\,xy^2 - \left(16\,xy^2 - 72\,xy\right) = -16\,x^2y^2 - 40\,x^2y - 104\,xy^2 + 72\,xy \\ [10] \quad 18\,x^2y^2 - 36\,x^2y + 162\,xy^2 - \left(81\,x^2y^2 - 81\,x^2y\right) + \left(27\,x^2y^2 - 81\,xy^2 - 9\,xy\right) = -36\,x^2y^2 + 45\,x^2y + 81\,xy^2 - 9\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (2\,b^2x^3y^2z^3) \cdot (3\,bxy^3z) = 6\,b^3x^4y^5z^4 \\ &[3] \quad (-2\,b^2x^2yz^2) \cdot (12\,b^2x^3y^2z) = -24\,b^4x^5y^3z^3 \\ &[4] \quad (27\,b^3x^3yz^2) \cdot (27\,b^2xy^2z) = 729\,b^5x^4y^3z^3 \\ &[5] \quad (-128\,bx^3yz^3) \cdot (16\,b^2xy^2z^2) = -2048\,b^3x^4y^3z^5 \\ &[6] \quad (-500\,b^3x^3yz^2) \cdot (5\,bxy^2z) = -2500\,b^4x^4y^3z^3 \\ &[7] \quad (-24\,b^2xyz^3) \cdot (648\,b^2x^2y^2z^3) = -15552\,b^4x^3y^3z^6 \\ &[8] \quad (-196\,bx^2yz^2) \cdot (28\,bx^3yz^3) = -5488\,b^2x^5y^2z^5 \\ &[9] \quad (-192\,b^2x^3y^2z^3) \cdot (192\,bx^3yz^3) = -36864\,b^3x^6y^3z^6 \\ &[10] \quad (-81\,b^3x^3yz^2) \cdot (36\,b^2x^3y^3z) = -2916\,b^5x^6y^4z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x^2)\cdot(7\,x^2+6\,x) = 28\,x^4+24\,x^3 \\ &[2] \quad (4\,x^2)\cdot(-4\,x^2+x) = -16\,x^4+4\,x^3 \\ &[3] \quad (4\,x^2)\cdot(-x^2+x) = -4\,x^4+4\,x^3 \\ &[4] \quad (2\,x)\cdot(2\,x^2-4\,x) = 4\,x^3-8\,x^2 \\ &[5] \quad (x)\cdot(4\,x^2-5\,x) = 4\,x^3-5\,x^2 \\ &[6] \quad (-x^2)\cdot(2\,x^2) = -2\,x^4 \\ &[7] \quad (x^2)\cdot(7\,x^2-3\,x) = 7\,x^4-3\,x^3 \\ &[8] \quad (3\,x)\cdot(5\,x^2) = 15\,x^3 \\ &[9] \quad (4\,x)\cdot(x^2+3\,x) = 4\,x^3+12\,x^2 \\ &[10] \quad (-2\,x)\cdot(4\,x^2-5\,x) = -8\,x^3+10\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(6x^2) \cdot (-7x^2) = -42x^4$$

[2] $(0) \cdot (-x^2 - 5x) = 0$
[3] $(-6x) \cdot (3x^2 - 6x) = -18x^3 + 36x^2$
[4] $(-5x) \cdot (3x) = -15x^2$

[5]
$$(-2x^2 - 2x) \cdot (x^2 + 2x) = -2x^4 - 6x^3 - 4x^2$$

[6] $(x^2 - x) \cdot (3x^2 - x) = 3x^4 - 4x^3 + x^2$

[7]
$$(-2x^2 + 2x) \cdot (-2x) = 4x^3 - 4x^2$$

[8]
$$(-3x^2 + x) \cdot (x^2 - x) = -3x^4 + 4x^3 - x^2$$

[9]
$$(4x^2 + x) \cdot (-5x^2) = -20x^4 - 5x^3$$

[10]
$$(-x) \cdot (6x^2) = -6x^3$$

[11]
$$(2x) \cdot (-6x^2 + 2x) = -12x^3 + 4x^2$$

[12]
$$(-6x) \cdot (-5x^2 - 2x) = 30x^3 + 12x^2$$

[13]
$$(-5x) \cdot (-x^2 + 4x) = 5x^3 - 20x^2$$

[14]
$$(5x) \cdot (-x^2 + 7x) = -5x^3 + 35x^2$$

[15]
$$(-7x^2) \cdot (-3x^2 - 4x) = 21x^4 + 28x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^3 - 3x^2 + 3x) \cdot (-2x^3 - 2x^2 + 2x) = 6x^6 + 12x^5 - 6x^4 - 12x^3 + 6x^2$$

[2]
$$(7x^2) \cdot (-2x^2) = -14x^4$$

[3]
$$(-x^3 - 2x) \cdot (-2x^3 - 5x^2) = 2x^6 + 5x^5 + 4x^4 + 10x^3$$

[4]
$$(6x^2 + 4x) \cdot (-3x^3 - x^2 - 2x) = -18x^5 - 18x^4 - 16x^3 - 8x^2$$

[5]
$$(-x) \cdot (-2x^2 + 3x) = 2x^3 - 3x^2$$

[6]
$$(-5x) \cdot (-8x^3 - 3x^2) = 40x^4 + 15x^3$$

[7]
$$(-3x^3 - 5x^2) \cdot (x^3 - 8x^2) = -3x^6 + 19x^5 + 40x^4$$

[8]
$$(4x^2 + 2x) \cdot (-4x^3 + 3x) = -16x^5 - 8x^4 + 12x^3 + 6x^2$$

[9]
$$(2x^3 + 4x) \cdot (3x^3 + 6x^2) = 6x^6 + 12x^5 + 12x^4 + 24x^3$$

[10]
$$(6x^3 + x) \cdot (-3x^3 - 2x) = -18x^6 - 15x^4 - 2x^2$$

[11]
$$(-2x^2 + 2x) \cdot (-6x^3 - 4x^2 - 4x) = 12x^5 - 4x^4 - 8x^2$$

[12]
$$(4x^3 - x) \cdot (4x^3 - 6x^2) = 16x^6 - 24x^5 - 4x^4 + 6x^3$$

[13]
$$(x^2) \cdot (-4x^3 - 6x^2) = -4x^5 - 6x^4$$

[14]
$$(x^3 - 4x) \cdot (-3x^3) = -3x^6 + 12x^4$$

[15]
$$(-x^3) \cdot (-3x^3 - 3x^2 - x) = 3x^6 + 3x^5 + x^4$$

[16]
$$(-3x^3 + 4x^2) \cdot (-x^3 + 6x^2) = 3x^6 - 22x^5 + 24x^4$$

[17]
$$(8x) \cdot (-3x^3 - 3x^2 - 3x) = -24x^4 - 24x^3 - 24x^2$$

[18]
$$(-4x^3 + 4x^2) \cdot (5x^3 - 5x^2) = -20x^6 + 40x^5 - 20x^4$$

[19]
$$(2x^3) \cdot (-2x^3 - 2x) = -4x^6 - 4x^4$$

[20]
$$(-4x^3 + 2x) \cdot (-x^3 - 6x^2) = 4x^6 + 24x^5 - 2x^4 - 12x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^2y^2 - 4xy^2) \cdot (-2x^2y^2 - xy^2 - 3xy) = 6x^4y^4 + 11x^3y^4 + 9x^3y^3 + 4x^2y^4 + 12x^2y^3$$

[2] $(x^2y^2 + 2xy^2) \cdot (x^2y^2 - 3x^2y) = x^4y^4 - 3x^4y^3 + 2x^3y^4 - 6x^3y^3$
[3] $(2x^2y^2 + 4x^2y) \cdot (x^2y - 4xy) = 2x^4y^3 + 4x^4y^2 - 8x^3y^3 - 16x^3y^2$

$$[4] \quad (-3\,x^2y^2 + 2\,xy^2) \cdot (-3\,x^2y^2 + x^2y - xy^2) = 9\,x^4y^4 - 3\,x^4y^3 - 3\,x^3y^4 + 2\,x^3y^3 - 2\,x^2y^4$$

[5]
$$(x^2y + 2xy) \cdot (-x^2y + 3xy) = -x^4y^2 + x^3y^2 + 6x^2y^2$$

[6]
$$(-x^2y^2 - 3xy) \cdot (3xy^2) = -3x^3y^4 - 9x^2y^3$$

[6]
$$(-x^2y^2 - 3xy) \cdot (3xy^2) = -3x^3y^2 - 9x^2y^3$$

[7] $(-4x^2y^2 - 4xy) \cdot (3x^2y + 4xy^2 + xy) = -12x^4y^3 - 16x^3y^4 - 4x^3y^3 - 12x^3y^2 - 16x^2y^3 - 4x^2y^2$