1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 2x^3 + 3x^2 - 3x + -4x^4 + 2x^3 - 4x^2 + (-x^5 - x^3 - x) = -x^5 - 4x^4 + 3x^3 - x^2 - 4x$$

$$[2] \quad 3x^6 - 4x^4 + 2x^2 + -3x^3 + -x^5 + 2x^4 - x^3 = 3x^6 - x^5 - 2x^4 - 4x^3 + 2x^2$$

$$[3] \quad -4x^4 - 2x^2 + (-2x^6) + (-2x^6 + 5x^5) = -4x^6 + 5x^5 - 4x^4 - 2x^2$$

$$[4] \quad -x^3 + 2x + (-3x^6 + 2x^4 + x^2) + (-x^6 + 2x^5) = -4x^6 + 2x^5 + 2x^4 - x^3 + x^2 + 2x$$

$$[5] \quad 3x^6 - 2x^5 + x^4 + -4x^4 - 3x^2 + 2x + -x^6 + 2x^4 + 4x^3 = 2x^6 - 2x^5 - x^4 + 4x^3 - 3x^2 + 2x$$

$$[6] \quad -4x^5 - 4x^4 + x^3 + (-3x^5) + (-2x^4 - 2x^2 + 3x) = -7x^5 - 6x^4 + x^3 - 2x^2 + 3x$$

$$[7] \quad 3x^5 - 3x^2 + -x^6 + 2x^3 - 4x + 2x^6 + 2x^5 + 2x^3 = x^6 + 5x^5 + 4x^3 - 3x^2 - 4x$$

$$[8] \quad 4x^4 - 3x^2 + 4x^6 + 4x^5 + 3x^3 + 2x^5 - 3x^3 - x^2 = 4x^6 + 6x^5 + 4x^4 - 4x^2$$

$$[9] \quad x^6 - 4x^5 + 7x^4 + x + 5x^2 + 4x = x^6 - 4x^5 + 7x^4 + 5x^2 + 5x$$

$$[10] \quad x^4 - 4x^2 - 3x + -4x^5 - 3x^4 - 4x^2 + 2x^3 - x^2 = -4x^5 - 2x^4 + 2x^3 - 9x^2 - 3x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 3xy+-5x^2y^2-4xy+(-2x^2y^2-x^2y-3xy)=-7x^2y^2-x^2y-4xy \\ [3] \quad 28x^2y^2+16xy^2+-6x^2y^2-8xy^2-6xy+(-2x^2y-2xy)=22x^2y^2-2x^2y+8xy^2-8xy \\ [4] \quad 27x^2y^2+12x^2y-12xy^2+12x^2y+3xy^2+12xy+-3x^2y^2+12xy^2=24x^2y^2+24x^2y+3xy^2+12xy \\ [5] \quad 32x^2y^2+12xy^2-32xy+-12x^2y^2+48x^2y-16xy+64x^2y^2=84x^2y^2+48x^2y+12xy^2-48xy \\ [6] \quad 75x^2y^2+-5x^2y^2-50x^2y-15xy+-75x^2y^2-100x^2y-75xy=-5x^2y^2-150x^2y-90xy \\ [7] \quad 12x^2y+72xy^2-72xy+-24x^2y^2+30xy+18x^2y^2+108x^2y-6xy=-6x^2y^2+120x^2y+72xy^2-48xy \\ [8] \quad 49x^2y^2-14xy^2+14xy+-98x^2y-245xy^2+21x^2y^2+98x^2y+49xy^2=70x^2y^2-210xy^2+14xy \\ [9] \quad 24x^2y^2+256xy+8x^2y^2+24xy^2+16xy+192x^2y^2-224x^2y=224x^2y^2-224x^2y+272xy \\ [10] \quad 324xy^2+-9x^2y+81xy^2+27xy+-18x^2y^2+27x^2y+9xy=-18x^2y^2+18x^2y+405xy^2+36xy \\ [10] \quad 324xy^2+9x^2+36xy \\ [10] \quad 324xy^2+36xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -6\,x^2y^2 + xy + -x^2y - 3\,xy^2 + 2\,xy - (3\,x^2y^2 + 2\,xy^2 + 3\,xy) = -9\,x^2y^2 - x^2y - 5\,xy^2 \\ &[3] \quad 12\,x^2y^2 + 4\,xy^2 + 12\,x^2y - (8\,x^2y - 12\,xy) = 12\,x^2y^2 + 4\,x^2y + 4\,xy^2 + 12\,xy \\ &[4] \quad 9\,x^2y^2 + 3\,x^2y + 3\,xy^2 - (27\,x^2y^2 + 27\,x^2y - 9\,xy) + (36\,x^2y^2 + 6\,x^2y - 3\,xy^2) = 18\,x^2y^2 - 18\,x^2y + 9\,xy \\ &[5] \quad 4\,x^2y^2 + -96\,xy^2 - 16\,xy - (-44\,xy^2 - 8\,xy) = 4\,x^2y^2 - 52\,xy^2 - 8\,xy \end{aligned}$$

 $180 x^2 y + 162 x y^2 + 18 x y$

$$[6] \quad 15\,x^2y + -5\,x^2y^2 - 25\,x^2y - 15\,xy^2 - (250\,x^2y) = -5\,x^2y^2 - 260\,x^2y - 15\,xy^2 \\ [7] \quad -108\,x^2y^2 + 108\,xy^2 - 12\,xy - (-48\,x^2y^2 + 144\,xy^2) + (-12\,x^2y^2 - 6\,x^2y - 144\,xy) = -72\,x^2y^2 - 6\,x^2y - 36\,xy^2 - 156\,xy \\ [8] \quad 126\,x^2y + 98\,x^2y^2 + 98\,xy^2 - 7\,xy - (14\,x^2y^2 - 98\,xy^2) = 84\,x^2y^2 + 126\,x^2y + 196\,xy^2 - 7\,xy \\ [9] \quad 24\,x^2y + 32\,xy^2 - 256\,xy + -232\,x^2y^2 - (-56\,x^2y^2 + 16\,x^2y) = -176\,x^2y^2 + 8\,x^2y + 32\,xy^2 - 256\,xy \\ [10] \quad 243\,x^2y^2 - 36\,x^2y + 18\,xy - (144\,x^2y - 162\,xy^2) + (-360\,x^2y^2) = -117\,x^2y^2 - 126\,x^2y^2 + 126\,x^2y^$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-2\,b^3x^2y^3z) \cdot (2\,bxy^3z^2) = -4\,b^4x^3y^6z^3 \\ &[3] \quad (8\,b^3x^2y^3z) \cdot (-12\,b^2x^2yz^3) = -96\,b^5x^4y^4z^4 \\ &[4] \quad (-18\,bx^2yz^2) \cdot (-6\,b^2x^2y^3z^2) = 108\,b^3x^4y^4z^4 \\ &[5] \quad (-32\,b^2x^3y^3z) \cdot (8\,b^3xyz^3) = -256\,b^5x^4y^4z^4 \\ &[6] \quad (-375\,b^3x^2yz^2) \cdot (-20\,b^2x^3yz) = 7500\,b^5x^5y^2z^3 \\ &[7] \quad (432\,b^3x^3y^2z) \cdot (108\,b^2xy^3z) = 46656\,b^5x^4y^5z^2 \\ &[8] \quad (-147\,b^3x^3yz^3) \cdot (-147\,b^3x^2y^2z^3) = 21609\,b^6x^5y^3z^6 \\ &[9] \quad (1536\,bx^3yz) \cdot (256\,b^2x^2y^3z^2) = 393216\,b^3x^5y^4z^3 \\ &[10] \quad (18\,b^2x^3yz^3) \cdot (36\,b^2x^2yz^3) = 648\,b^4x^5y^2z^6 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (-3\,x^2) \cdot (-3\,x^2 + 6\,x) = 9\,x^4 - 18\,x^3 \\ & [2] \quad (3\,x^2) \cdot (-2\,x^2 - 2\,x) = -6\,x^4 - 6\,x^3 \\ & [3] \quad (2\,x) \cdot (3\,x) = 6\,x^2 \\ & [4] \quad (4\,x) \cdot (x^2 + 4\,x) = 4\,x^3 + 16\,x^2 \\ & [5] \quad (2\,x) \cdot (-x^2 + 4\,x) = -2\,x^3 + 8\,x^2 \\ & [6] \quad (3\,x^2) \cdot (x) = 3\,x^3 \\ & [7] \quad (3\,x) \cdot (-x^2 - x) = -3\,x^3 - 3\,x^2 \\ & [8] \quad (3\,x^2) \cdot (7\,x^2 + 3\,x) = 21\,x^4 + 9\,x^3 \\ & [9] \quad (2\,x) \cdot (7\,x^2 - 2\,x) = 14\,x^3 - 4\,x^2 \\ & [10] \quad (3\,x) \cdot (-4\,x^2 - 3\,x) = -12\,x^3 - 9\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x^2+3\,x)\cdot(7\,x^2-4\,x) = -14\,x^4+29\,x^3-12\,x^2 \\ &[2] \quad (2\,x^2)\cdot(-2\,x^2+4\,x) = -4\,x^4+8\,x^3 \\ &[3] \quad (-2\,x^2)\cdot(7\,x^2) = -14\,x^4 \\ &[4] \quad (-3\,x^2-x)\cdot(x^2+4\,x) = -3\,x^4-13\,x^3-4\,x^2 \\ &[5] \quad (-2\,x^2+3\,x)\cdot(-2\,x^2) = 4\,x^4-6\,x^3 \\ &[6] \quad (2\,x^2+4\,x)\cdot(-2\,x^2-4\,x) = -4\,x^4-16\,x^3-16\,x^2 \\ &[7] \quad (x^2+x)\cdot(-2\,x) = -2\,x^3-2\,x^2 \end{aligned}$$

[8]
$$(-x^2 - 3x) \cdot (-3x^2 + 2x) = 3x^4 + 7x^3 - 6x^2$$

[9]
$$(3x^2 + 3x) \cdot (2x^2 - 2x) = 6x^4 - 6x^2$$

[10]
$$(-x) \cdot (x^2 - 5x) = -x^3 + 5x^2$$

[11]
$$(4x) \cdot (x^2 + 3x) = 4x^3 + 12x^2$$

[12]
$$(2x) \cdot (5x^2 + x) = 10x^3 + 2x^2$$

[13]
$$(-8x) \cdot (x^2 - 2x) = -8x^3 + 16x^2$$

[14]
$$(-3x^2 - 2x) \cdot (5x) = -15x^3 - 10x^2$$

[15]
$$(-4x^2 + 3x) \cdot (-6x^2 - 2x) = 24x^4 - 10x^3 - 6x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(4x^3 - 3x^2 + 3x) \cdot (x^3 - 2x) = 4x^6 - 3x^5 - 5x^4 + 6x^3 - 6x^2$$

[2]
$$(x^3 + x) \cdot (2x^3 - 4x^2 - x) = 2x^6 - 4x^5 + x^4 - 4x^3 - x^2$$

[3]
$$(2x^3 - 3x^2) \cdot (-7x^3 + x^2) = -14x^6 + 23x^5 - 3x^4$$

[4]
$$(-2x^3 + 3x^2 - 3x) \cdot (2x^2 + 8x) = -4x^5 - 10x^4 + 18x^3 - 24x^2$$

[5]
$$(7x) \cdot (-4x^3 - x^2 - 4x) = -28x^4 - 7x^3 - 28x^2$$

[6]
$$(-2x^2 - 4x) \cdot (-2x^3 + 3x^2) = 4x^5 + 2x^4 - 12x^3$$

[7]
$$(-9x^2) \cdot (-2x^3) = 18x^5$$

[8]
$$(-3x^3) \cdot (10x^3 - 2x^2) = -30x^6 + 6x^5$$

[9]
$$(7x) \cdot (4x^2) = 28x^3$$

[10]
$$(2x^3 - 3x) \cdot (-7x^3 + 3x^2) = -14x^6 + 6x^5 + 21x^4 - 9x^3$$

[11]
$$(-2x^3 - 2x) \cdot (-2x^3 - 2x^2) = 4x^6 + 4x^5 + 4x^4 + 4x^3$$

[12]
$$(-3x^3 + 2x^2) \cdot (-4x^3 + 8x) = 12x^6 - 8x^5 - 24x^4 + 16x^3$$

[13]
$$(-4x^2 + 2x) \cdot (-4x^2 - 2x) = 16x^4 - 4x^2$$

[14]
$$(-x^3 - 3x^2) \cdot (-x^2 - 2x) = x^5 + 5x^4 + 6x^3$$

[15]
$$(3x^3 - 4x) \cdot (x^3 + 6x) = 3x^6 + 14x^4 - 24x^2$$

[16]
$$(-8x^2 + 3x) \cdot (2x^3 - 3x^2) = -16x^5 + 30x^4 - 9x^3$$

[17]
$$(3x^3 + 3x) \cdot (-x^3 - 4x^2 - 4x) = -3x^6 - 12x^5 - 15x^4 - 12x^3 - 12x^2$$

[18]
$$(5x^3) \cdot (-7x^2 + 8x) = -35x^5 + 40x^4$$

[19]
$$(-6x^3 + 2x) \cdot (-x) = 6x^4 - 2x^2$$

[20]
$$(-2x^2 - x) \cdot (4x^3 - x^2 - 3x) = -8x^5 - 2x^4 + 7x^3 + 3x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^2y^2 - 4xy) \cdot (x^2y + xy^2) = -3x^4y^3 - 3x^3y^4 - 4x^3y^2 - 4x^2y^3$$

[2]
$$(0) \cdot (6x^2y^2 - 2x^2y) = 0$$

[3]
$$(x^2y^2 - 2xy^2) \cdot (-3xy^2) = -3x^3y^4 + 6x^2y^4$$

[4]
$$(-4x^2y - xy) \cdot (3xy^2 + 4xy) = -12x^3y^3 - 16x^3y^2 - 3x^2y^3 - 4x^2y^2$$

[5]
$$(-3xy^2 - xy) \cdot (-2x^2y - 4xy) = 6x^3y^3 + 2x^3y^2 + 12x^2y^3 + 4x^2y^2$$

$$[6] \quad (-2\,x^2y^2-x^2y)\cdot(x^2y^2+2\,x^2y+xy) = -2\,x^4y^4-5\,x^4y^3-2\,x^4y^2-2\,x^3y^3-x^3y^2-x^3y^2-x^2$$

[7]
$$(2x^2y - 2xy^2) \cdot (2x^2y^2 - 4x^2y) = 4x^4y^3 - 4x^3y^4 - 8x^4y^2 + 8x^3y^3$$