1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$2x^6 + 2x + -x^2 - 5x + -3x^4 - 4x^3 - 4x = 2x^6 - 3x^4 - 4x^3 - x^2 - 7x$$

[2] $-4x^6 - 2x^2 + 3x + (-3x^6 - 2x^3) + (-2x^6 + 3x^4 + 4x^2) = -9x^6 + 3x^4 - 2x^3 + 2x^2 + 3x$
[3] $2x^5 - 5x^3 + -2x^6 + 4x^5 - 2x^2 + 4x^5 - 3x^4 + 3x^2 = -2x^6 + 10x^5 - 3x^4 - 5x^3 + x^2$
[4] $6x^5 - 3x^3 + 4x^6 + 2x^3 + 3x + -4x^5 + 2x^3 - 3x = 4x^6 + 2x^5 + x^3$
[5] $2x^2 + 2x + -x^3 + 2x + (-4x^5 - 3x^4 + 4x^2) = -4x^5 - 3x^4 - x^3 + 6x^2 + 4x$
[6] $4x^6 - 4x^5 - x^4 + -6x^5 - x + -x^5 - x = 4x^6 - 11x^5 - x^4 - 2x$
[7] $-x^6 + 3x^2 - 3x + (-4x^4) + (-2x^4 + 2x^3 + 3x^2) = -x^6 - 6x^4 + 2x^3 + 6x^2 - 3x$
[8] $3x^5 - 4x^4 + x^2 + -4x^6 - 3x^4 - 3x^2 + 4x^6 + 2x^5 - 2x^4 = 5x^5 - 9x^4 - 2x^2$
[9] $4x^6 + x^3 - 2x^2 + x^4 + 4x^3 - 3x + -2x^3 + x^2 = 4x^6 + x^4 + 3x^3 - x^2 - 3x$
[10] $4x^6 + 4x^3 + 2x^2 + -4x^6 + 4x^4 - 3x^3 + -6x^5 + x^4 = -6x^5 + 5x^4 + x^3 + 2x^2$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad -5x^2y^2-2\,xy+(-4\,x^2y^2-2\,x^2y-4\,xy)+(-x^2y-4\,xy)=-9\,x^2y^2-3\,x^2y-10\,xy \\ [3] \quad 4\,xy^2-16\,xy+-12\,xy^2-4\,xy+-2\,x^2y-16\,xy=-2\,x^2y-8\,xy^2-36\,xy \\ [4] \quad 9\,x^2y^2-12\,x^2y-9\,xy^2+-27\,x^2y+3\,xy^2+(-36\,x^2y^2-18\,xy^2)=-27\,x^2y^2-39\,x^2y-24\,xy^2 \\ [5] \quad 12\,x^2y^2+48\,xy+-8\,x^2y^2+4\,x^2y+(-32\,x^2y^2-64\,x^2y-16\,xy)=-28\,x^2y^2-60\,x^2y+32\,xy \\ [6] \quad 175\,x^2y-20\,xy+-10\,x^2y-20\,xy^2+20\,x^2y^2-95\,xy^2=20\,x^2y^2+165\,x^2y-115\,xy^2-20\,xy \\ [7] \quad 60\,x^2y^2+6\,xy^2+-72\,x^2y+150\,xy+-144\,x^2y^2-108\,xy^2+72\,xy=-84\,x^2y^2-72\,x^2y-102\,xy^2+222\,xy \\ [8] \quad 7\,x^2y^2+-196\,x^2y+49\,xy^2+126\,xy^2-28\,xy=7\,x^2y^2-196\,x^2y+175\,xy^2-28\,xy \\ [9] \quad 8\,x^2y+192\,xy^2+-240\,x^2y^2+64\,x^2y+-24\,x^2y^2+152\,xy=-264\,x^2y^2+72\,x^2y+192\,xy^2+152\,xy \\ [10] \quad 36\,x^2y+405\,xy+117\,x^2y+-9\,x^2y+18\,xy^2-9\,xy=144\,x^2y+18\,xy^2+396\,xy \\ [10] \quad 36\,x^2y+102\,xy+117\,x^2y+-9\,x^2y+18\,xy^2-9\,xy=144\,x^2y+18\,xy^2+396\,xy \\ [10] \quad 36\,x^2y+102\,xy+122\,xy+122\,xy+122\,xy+122\,xy+122\,xy+122\,x$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad x^2y^2 - 2\,x^2y + 4\,xy^2 + x^2y^2 - x^2y + 4\,xy - (-3\,x^2y^2 + 5\,xy^2) = 5\,x^2y^2 - 3\,x^2y - xy^2 + 4\,xy \\ &[3] \quad 12\,x^2y^2 + 8\,xy + 4\,x^2y - 10\,xy^2 - (-12\,x^2y - 8\,xy^2) = 12\,x^2y^2 + 16\,x^2y - 2\,xy^2 + 8\,xy \\ &[4] \quad 12\,x^2y - 12\,xy^2 - (9\,x^2y^2 + 27\,x^2y + 12\,xy) + (-3\,x^2y^2 - 21\,xy^2) = -12\,x^2y^2 - 15\,x^2y - 33\,xy^2 - 12\,xy \end{aligned}$$

$$\begin{aligned} & [5] \quad 16\,x^2y + 12\,xy^2 + -36\,x^2y^2 + 16\,x^2y - (8\,x^2y^2 - 16\,x^2y - 64\,xy^2) = -44\,x^2y^2 + \\ & 48\,x^2y + 76\,xy^2 \\ & [6] \quad -15\,x^2y^2 + 5\,xy + 10\,x^2y^2 + 40\,xy - (50\,x^2y^2 + 50\,xy^2 - 100\,xy) = -55\,x^2y^2 - \\ & 50\,xy^2 + 145\,xy \\ & [7] \quad -48\,xy - (-6\,x^2y^2 - 6\,xy^2) + (114\,x^2y + 108\,xy^2) = 6\,x^2y^2 + 114\,x^2y + 114\,xy^2 - \\ & 48\,xy \\ & [8] \quad -147\,x^2y - 21\,xy^2 + -49\,x^2y + 49\,xy^2 - (-98\,x^2y^2 + 49\,xy) = 98\,x^2y^2 - \\ & 196\,x^2y + 28\,xy^2 - 49\,xy \\ & [9] \quad 192\,x^2y^2 - 136\,xy + 24\,x^2y^2 - 192\,x^2y + 24\,xy - (-24\,xy^2 + 64\,xy) = 216\,x^2y^2 - \\ & 192\,x^2y + 24\,xy^2 - 176\,xy \\ & [10] \quad 324\,x^2y^2 - 324\,x^2y + 36\,xy^2 - (243\,x^2y + 117\,xy^2) + (-63\,xy^2 + 324\,xy) = \\ & 324\,x^2y^2 - 567\,x^2y - 144\,xy^2 + 324\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-4\,b^3xy^3z) \cdot (-2\,bxy^2z^3) = 8\,b^4x^2y^5z^4 \\ &[3] \quad (24\,b^2xy^3z^2) \cdot (8\,bx^3y^2z^3) = 192\,b^3x^4y^5z^5 \\ &[4] \quad (-18\,b^3x^2yz) \cdot (-18\,bx^3y^2z) = 324\,b^4x^5y^3z^2 \\ &[5] \quad (8\,bx^2y^2z^3) \cdot (-256\,b^2x^2yz^2) = -2048\,b^3x^4y^3z^5 \\ &[6] \quad (375\,bx^3yz^3) \cdot (50\,b^3xy^3z) = 18750\,b^4x^4y^4z^4 \\ &[7] \quad (-6\,bx^2y^3z^3) \cdot (6\,bx^2y^2z^3) = -36\,b^2x^4y^5z^6 \\ &[8] \quad (-1029\,bxyz^2) \cdot (-1372\,b^3xy^2z) = 1411788\,b^4x^2y^3z^3 \\ &[9] \quad (24\,b^3x^2y^3z^3) \cdot (-256\,bxyz) = -6144\,b^4x^3y^4z^4 \\ &[10] \quad (-36\,b^3x^3y^2z) \cdot (1458\,bxy^2z^3) = -52488\,b^4x^4y^4z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x) \cdot (4x^2 + 3x) = -8x^3 - 6x^2$$

[2] $(3x^2) \cdot (5x) = 15x^3$
[3] $(4x^2) \cdot (8x^2 - x) = 32x^4 - 4x^3$
[4] $(-x^2) \cdot (x^2 - 4x) = -x^4 + 4x^3$
[5] $(-2x) \cdot (2x^2 + x) = -4x^3 - 2x^2$
[6] $(4x^2) \cdot (-2x^2 + 6x) = -8x^4 + 24x^3$
[7] $(-4x) \cdot (0) = 0$
[8] $(4x) \cdot (-4x^2) = -16x^3$
[9] $(3x) \cdot (-5x^2 + 5x) = -15x^3 + 15x^2$
[10] $(3x^2) \cdot (-10x^2) = -30x^4$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(7x^2) \cdot (4x^2 + 3x) = 28x^4 + 21x^3$$

[2] $(-2x^2 - x) \cdot (-7x^2) = 14x^4 + 7x^3$
[3] $(2x) \cdot (-3x^2 - 2x) = -6x^3 - 4x^2$
[4] $(3x^2) \cdot (-5x^2 + 2x) = -15x^4 + 6x^3$

[5]
$$(0) \cdot (x^2 + x) = 0$$

[6]
$$(-2x^2 - 3x) \cdot (3x^2 + 5x) = -6x^4 - 19x^3 - 15x^2$$

[7]
$$(3x^2 + 3x) \cdot (6x^2 + 2x) = 18x^4 + 24x^3 + 6x^2$$

[8]
$$(2x^2 - x) \cdot (x) = 2x^3 - x^2$$

[9]
$$(x^2 + 2x) \cdot (4x^2) = 4x^4 + 8x^3$$

[10]
$$(-7x) \cdot (-5x^2 + x) = 35x^3 - 7x^2$$

[11]
$$(7x^2) \cdot (-2x) = -14x^3$$

[12]
$$(x^2 + x) \cdot (-3x^2 - x) = -3x^4 - 4x^3 - x^2$$

[13]
$$(-3x^2 - 4x) \cdot (x^2) = -3x^4 - 4x^3$$

[14]
$$(2x^2) \cdot (2x^2 + 6x) = 4x^4 + 12x^3$$

[15]
$$(-3x^2 - x) \cdot (-x^2 - 5x) = 3x^4 + 16x^3 + 5x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^2 + 2x) \cdot (3x^3 + 5x) = -3x^5 + 6x^4 - 5x^3 + 10x^2$$

[2]
$$(-4x^3 - 3x) \cdot (x^3 - 3x^2 + x) = -4x^6 + 12x^5 - 7x^4 + 9x^3 - 3x^2$$

[3]
$$(x^2 - 3x) \cdot (-2x^3 + 8x) = -2x^5 + 6x^4 + 8x^3 - 24x^2$$

[4]
$$(-x^2 - 3x) \cdot (-4x^3 + x^2) = 4x^5 + 11x^4 - 3x^3$$

[5]
$$(-8x) \cdot (6x^3 + 2x^2) = -48x^4 - 16x^3$$

[6]
$$(-2x^2 - 3x) \cdot (4x^3 - 4x^2 - x) = -8x^5 - 4x^4 + 14x^3 + 3x^2$$

[7]
$$(4x^2) \cdot (-x) = -4x^3$$

[8]
$$(-2x^3 - 4x^2) \cdot (-x^2 + x) = 2x^5 + 2x^4 - 4x^3$$

[9]
$$(-3x^2 + x) \cdot (-2x^2 - 7x) = 6x^4 + 19x^3 - 7x^2$$

[10]
$$(3x^2 - x) \cdot (-x^3 + 2x^2 - 3x) = -3x^5 + 7x^4 - 11x^3 + 3x^2$$

[11]
$$(3x^2) \cdot (6x^3 - 3x^2 - 2x) = 18x^5 - 9x^4 - 6x^3$$

[12]
$$(4x^3 - 4x) \cdot (3x^2) = 12x^5 - 12x^3$$

[13]
$$(6x^2 - x) \cdot (2x^3 - 3x^2 - x) = 12x^5 - 20x^4 - 3x^3 + x^2$$

[14]
$$(-3x^3 - 2x) \cdot (-2x^3 - 4x^2 - 4x) = 6x^6 + 12x^5 + 16x^4 + 8x^3 + 8x^2$$

[15]
$$(-4x^3 + x^2) \cdot (-2x^3 - 2x^2 - 5x) = 8x^6 + 6x^5 + 18x^4 - 5x^3$$

[16]
$$(-8x^3 + 2x^2) \cdot (-6x^2 - 3x) = 48x^5 + 12x^4 - 6x^3$$

[17]
$$(-2x) \cdot (5x^3 - x^2 - 2x) = -10x^4 + 2x^3 + 4x^2$$

[18]
$$(x^3 - x) \cdot (-4x^3 - 2x) = -4x^6 + 2x^4 + 2x^2$$

[19]
$$(-x^3 - x^2 + 4x) \cdot (x^2) = -x^5 - x^4 + 4x^3$$

[20]
$$(x^3 - x^2) \cdot (-4x^2 + 5x) = -4x^5 + 9x^4 - 5x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2y - 3xy) \cdot (3x^2y - 2xy^2) = -6x^4y^2 + 4x^3y^3 - 9x^3y^2 + 6x^2y^3$$

[2]
$$(-2xy^2 - 3xy) \cdot (-2xy) = 4x^2y^3 + 6x^2y^2$$

[3]
$$(-x^2y^2 - 4x^2y) \cdot (-2xy^2 + xy) = 2x^3y^4 + 7x^3y^3 - 4x^3y^2$$

[3]
$$(-x^2y^2 - 4x^2y) \cdot (-2xy^2 + xy) = 2x^3y^4 + 7x^3y^3 - 4x^3y^2$$

[4] $(x^2y^2 - 3xy^2) \cdot (3x^2y - 4xy^2 - 4xy) = 3x^4y^3 - 4x^3y^4 - 13x^3y^3 + 12x^2y^4 + 12x^2y^3$

$$\begin{aligned} &[5] \quad (4\,x^2y - xy) \cdot (-4\,x^2y^2 + 3\,x^2y - 3\,xy) = -16\,x^4y^3 + 12\,x^4y^2 + 4\,x^3y^3 - 15\,x^3y^2 + \\ &3\,x^2y^2 \\ &[6] \quad (3\,x^2y^2 + 4\,x^2y) \cdot (-5\,x^2y^2 + 4\,x^2y) = -15\,x^4y^4 - 8\,x^4y^3 + 16\,x^4y^2 \\ &[7] \quad (-2\,x^2y^2 + 2\,x^2y) \cdot (-2\,xy^2 + 3\,xy) = 4\,x^3y^4 - 10\,x^3y^3 + 6\,x^3y^2 \end{aligned}$$