1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$3x^6 - 2x^4 - 3x^2 + -4x^4 + x^3 - 3x + 2x^3 + 2x^2 + x = 3x^6 - 6x^4 + 3x^3 - x^2 - 2x$$

[2] $4x^6 + 2x^5 + 3x^4 + -3x^3 + 4x^2 + x + -2x^3 - 3x^2 - 2x = 4x^6 + 2x^5 + 3x^4 - 5x^3 + x^2 - x$
[3] $2x^4 - x^3 - x^2 + x^5 + 4x^3 + 3x^6 + 3x^4 + 2x^2 = 3x^6 + x^5 + 5x^4 + 3x^3 + x^2$
[4] $4x^5 + 5x^4 + 2x^5 + x^3 - 3x^2 + -3x^2 = 6x^5 + 5x^4 + x^3 - 6x^2$
[5] $2x^5 - 4x^4 - 2x^3 + 3x^6 + 2x^2 - 4x + -3x^5 - 4x^3 + 4x^2 = 3x^6 - x^5 - 4x^4 - 6x^3 + 6x^2 - 4x$
[6] $4x^3 - 4x^2 + -2x^6 - 5x^3 + 3x^6 + 3x^2 = x^6 - x^3 - x^2$
[7] $3x^5 - 6x + x^6 - 4x^3 + -4x^5 - 2x^3 - 3x^2 = x^6 - x^5 - 6x^3 - 3x^2 - 6x$
[8] $x^6 - 2x^5 - x^4 + -3x^6 + 4x^5 + x + (-3x^6 - 3x^2 + 4x) = -5x^6 + 2x^5 - x^4 - 3x^2 + 5x$
[9] $2x^5 - 2x^3 - x^2 + 4x^6 + 3x^3 + 4x^2 + 2x^5 - x^4 + 4x^3 = 4x^6 + 4x^5 - x^4 + 5x^3 + 3x^2 - x^4 + 5x^3 + 3x^2 - x^4 + 3x^3 + 3x^2 - x^4 + 3x^3 + 3x^2 - x + -3x^5 + 4x^2 - x = 3x^6 - 3x^5 - x^3 + 7x^2 - 2x^3 + 7x^2 -$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0$$

$$[2] \quad 3x^2y^2+x^2y+-2xy+-2x^2y-xy=3x^2y^2-x^2y-3xy$$

$$[3] \quad 6x^2y^2-2x^2y-16xy+-8x^2y^2+16x^2y+4xy^2-10xy=-2x^2y^2+14x^2y+4xy^2-26xy$$

$$[4] \quad 18x^2y+6xy^2-6xy+-9x^2y^2-3x^2y+-3x^2y^2=-12x^2y^2+15x^2y+6xy^2-6xy$$

$$[5] \quad 28xy^2+4xy+-4x^2y^2-64xy^2+48xy+-16x^2y+4xy^2=-4x^2y^2-16x^2y-32xy^2+52xy$$

$$[6] \quad 85x^2y-5xy+-25x^2y^2+5xy+100x^2y^2-100xy^2+10xy=75x^2y^2+85x^2y-100xy^2+10xy$$

$$[7] \quad 6x^2y-216xy+-144x^2y^2+18x^2y+12xy+12x^2y^2-12x^2y=-132x^2y^2+12x^2y-204xy$$

$$[8] \quad 21x^2y^2-28xy+-343x^2y+147xy^2+-49x^2y^2-21x^2y-147xy=-28x^2y^2-364x^2y+147xy^2-175xy$$

$$[9] \quad 128x^2y-8xy^2+128xy+-64x^2y+32xy^2+256xy+-8x^2y^2-96xy^2=-8x^2y^2+64x^2y-72xy^2+384xy$$

$$[10] \quad 243x^2y^2-45xy+-36x^2y+27xy+9x^2y^2+9xy^2=252x^2y^2-36x^2y+9xy^2-18xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 8\,xy^2 + -2\,x^2y - xy^2 + 4\,xy - (3\,x^2y - xy) = -5\,x^2y + 7\,xy^2 + 5\,xy \\ &[3] \quad -12\,x^2y - 16\,xy^2 - 4\,xy + -2\,x^2y^2 + 4\,x^2y + 16\,xy^2 - (-4\,x^2y + 4\,xy^2 - 8\,xy) = \\ &-2\,x^2y^2 - 4\,x^2y - 4\,xy^2 + 4\,xy \\ &[4] \quad -9\,x^2y - 9\,xy^2 - (27\,x^2y^2 - 27\,x^2y + 6\,xy) + (-12\,x^2y + 18\,xy^2 - 27\,xy) = \\ &-27\,x^2y^2 + 6\,x^2y + 9\,xy^2 - 33\,xy \end{aligned}$$

$$[5] \quad -32 \, x^2 y^2 - 8 \, xy^2 + -48 \, x^2 y^2 + 64 \, x^2 y + 16 \, xy^2 - (-16 \, xy^2 + 32 \, xy) = \\ -80 \, x^2 y^2 + 64 \, x^2 y + 24 \, xy^2 - 32 \, xy$$

$$[6] \quad -50 \, x^2 y^2 + 25 \, xy^2 + 20 \, x^2 y - 75 \, xy^2 - (-15 \, x^2 y^2 + 100 \, x^2 y + 25 \, xy^2) = \\ -35 \, x^2 y^2 - 80 \, x^2 y - 75 \, xy^2$$

$$[7] \quad -24 \, x^2 y - 24 \, xy - (108 \, x^2 y^2 + 48 \, xy^2) + (252 \, x^2 y - 6 \, xy) = -108 \, x^2 y^2 + \\ 228 \, x^2 y - 48 \, xy^2 - 30 \, xy$$

$$[8] \quad -7 \, x^2 y^2 - 7 \, xy^2 - 196 \, xy + 196 \, x^2 y + 49 \, xy - (49 \, x^2 y^2 + 21 \, xy^2 + 98 \, xy) = \\ -56 \, x^2 y^2 + 196 \, x^2 y - 28 \, xy^2 - 245 \, xy$$

$$[9] \quad -184 \, xy^2 - 192 \, xy + 24 \, xy - (24 \, x^2 y^2 + 8 \, x^2 y) = -24 \, x^2 y^2 - 8 \, x^2 y - 184 \, xy^2 - \\ 168 \, xy$$

$$[10] \quad -324 \, x^2 y - 45 \, xy^2 - (-18 \, x^2 y + 243 \, xy^2 - 81 \, xy) + (-252 \, xy^2 + 243 \, xy) = \\ -306 \, x^2 y - 540 \, xy^2 + 324 \, xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (2\,b^3x^2y^3z) \cdot (4\,b^3x^3y^3z^3) = 8\,b^6x^5y^6z^4 \\ &[3] \quad (16\,bxy^3z) \cdot (-24\,bx^2y^3z) = -384\,b^2x^3y^6z^2 \\ &[4] \quad (-18\,b^3xy^3z^2) \cdot (6\,bxy^3z^2) = -108\,b^4x^2y^6z^4 \\ &[5] \quad (-16\,bxyz) \cdot (48\,b^3x^3y^2z^3) = -768\,b^4x^4y^3z^4 \\ &[6] \quad (-20\,bx^2y^2z^2) \cdot (-15\,b^3xy^3z^3) = 300\,b^4x^3y^5z^5 \\ &[7] \quad (-12\,b^3x^2y^2z) \cdot (-648\,b^3x^3y^2z) = 7776\,b^6x^5y^4z^2 \\ &[8] \quad (-1372\,b^2x^2yz^2) \cdot (-14\,b^2x^3yz^3) = 19208\,b^4x^5y^2z^5 \\ &[9] \quad (2048\,b^3x^3y^2z) \cdot (-24\,bx^3y^3z^3) = -49152\,b^4x^6y^5z^4 \\ &[10] \quad (27\,bx^3y^3z^2) \cdot (324\,b^2x^2yz) = 8748\,b^3x^5y^4z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x) \cdot (-x^2 - x) = 3x^3 + 3x^2$$

[2] $(2x) \cdot (4x^2 + x) = 8x^3 + 2x^2$
[3] $(x^2) \cdot (3x^2 + x) = 3x^4 + x^3$
[4] $(-x) \cdot (-x^2 + 4x) = x^3 - 4x^2$
[5] $(4x) \cdot (4x^2 + x) = 16x^3 + 4x^2$
[6] $(x^2) \cdot (x^2 + 5x) = x^4 + 5x^3$
[7] $(-2x) \cdot (x^2) = -2x^3$
[8] $(-3x^2) \cdot (5x^2 - 3x) = -15x^4 + 9x^3$
[9] $(2x) \cdot (2x) = 4x^2$
[10] $(-3x) \cdot (8x^2 + 4x) = -24x^3 - 12x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x) \cdot (4x^2 + 2x) = 8x^3 + 4x^2$$

[2] $(x^2 - 4x) \cdot (-x^2 + 3x) = -x^4 + 7x^3 - 12x^2$
[3] $(3x^2 + 3x) \cdot (-2x^2 + 4x) = -6x^4 + 6x^3 + 12x^2$
[4] $(5x^2) \cdot (-5x^2 - 4x) = -25x^4 - 20x^3$

[5]
$$(5x) \cdot (-x^2 - 2x) = -5x^3 - 10x^2$$

[6]
$$(x^2) \cdot (-x^2 - 6x) = -x^4 - 6x^3$$

[7]
$$(-x^2 - 2x) \cdot (-4x) = 4x^3 + 8x^2$$

[8]
$$(2x) \cdot (2x^2 + 4x) = 4x^3 + 8x^2$$

[9]
$$(-3x^2 + x) \cdot (-3x^2 - 2x) = 9x^4 + 3x^3 - 2x^2$$

[10]
$$(-3x^2 + x) \cdot (-8x) = 24x^3 - 8x^2$$

[11]
$$(7x) \cdot (5x^2 + 3x) = 35x^3 + 21x^2$$

[12]
$$(-3x^2 - 2x) \cdot (-3x^2 - 4x) = 9x^4 + 18x^3 + 8x^2$$

[13]
$$(2x) \cdot (3x^2 + 3x) = 6x^3 + 6x^2$$

[14]
$$(-3x) \cdot (-2x^2 - 5x) = 6x^3 + 15x^2$$

[15]
$$(-4x) \cdot (6x^2 - 2x) = -24x^3 + 8x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(5x) \cdot (x^3 + x^2 + 4x) = 5x^4 + 5x^3 + 20x^2$$

[2]
$$(4x^2) \cdot (12x^2) = 48x^4$$

[3]
$$(-3x^3 - 2x) \cdot (-4x^3 - x) = 12x^6 + 11x^4 + 2x^2$$

[4]
$$(x^3 + x^2) \cdot (3x^2 - x) = 3x^5 + 2x^4 - x^3$$

[5]
$$(4x^3 - x^2) \cdot (-3x^3 + 7x^2) = -12x^6 + 31x^5 - 7x^4$$

[6]
$$(3x^3 + 3x^2) \cdot (-x^3 + 2x^2) = -3x^6 + 3x^5 + 6x^4$$

[7]
$$(3x^2 + 7x) \cdot (3x^3 - 3x^2) = 9x^5 + 12x^4 - 21x^3$$

[8]
$$(2x^3 - x^2) \cdot (7x^2 + x) = 14x^5 - 5x^4 - x^3$$

[9]
$$(4x^3 + 3x) \cdot (-5x) = -20x^4 - 15x^2$$

[10]
$$(0) \cdot (3x^2 + 2x) = 0$$

[11]
$$(2x^3 + 2x) \cdot (4x^3) = 8x^6 + 8x^4$$

[12]
$$(-4x^2 + 2x) \cdot (2x^3 - 3x^2) = -8x^5 + 16x^4 - 6x^3$$

[13]
$$(-x^3 + 3x^2) \cdot (x^3 + 2x^2 + x) = -x^6 + x^5 + 5x^4 + 3x^3$$

[14]
$$(x^2) \cdot (x^3 - 2x^2) = x^5 - 2x^4$$

[15]
$$(4x^2) \cdot (-5x^3 + 4x) = -20x^5 + 16x^3$$

[16]
$$(-7x^2) \cdot (3x^3 + 2x^2 - x) = -21x^5 - 14x^4 + 7x^3$$

[17]
$$(-4x^3 - 2x^2) \cdot (5x^2 + x) = -20x^5 - 14x^4 - 2x^3$$

[18]
$$(-x^2 - 2x) \cdot (x^2 + 2x) = -x^4 - 4x^3 - 4x^2$$

[19]
$$(x^3 - 4x) \cdot (x^3 + 4x^2 + 4x) = x^6 + 4x^5 - 16x^3 - 16x^2$$

[20]
$$(4x^3 + 4x) \cdot (-x^3 + 5x^2) = -4x^6 + 20x^5 - 4x^4 + 20x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^2y - 2xy) \cdot (-x^2y^2 - xy^2 - 4xy) = x^4y^3 + 3x^3y^3 + 4x^3y^2 + 2x^2y^3 + 8x^2y^2$$

[2]
$$(3x^2y + 2xy^2) \cdot (2x^2y^2 - 4xy^2 - 4xy) = 6x^4y^3 + 4x^3y^4 - 12x^3y^3 - 8x^2y^4 - 12x^3y^2 - 8x^2y^3$$

[3]
$$(-4x^2y - 4xy) \cdot (-2x^2y^2 - 8xy) = 8x^4y^3 + 8x^3y^3 + 32x^3y^2 + 32x^2y^2$$

[4]
$$(-2xy^2+xy)\cdot(-2x^2y^2+x^2y+2xy) = 4x^3y^4-4x^3y^3+x^3y^2-4x^2y^3+2x^2y^2$$

[5]
$$(x^2y^2 + 2x^2y) \cdot (-2x^2y^2) = -2x^4y^4 - 4x^4y^3$$

$$\text{[6]} \quad (-xy^2+3\,xy)\cdot(-2\,x^2y+2\,xy) = 2\,x^3y^3-6\,x^3y^2-2\,x^2y^3+6\,x^2y^2$$

[7]
$$(3x^2y - 3xy) \cdot (-4x^2y) = -12x^4y^2 + 12x^3y^2$$