## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1] 
$$5x^3 + 2x^2 + -x^6 - 2x^4 + (-3x^6 - 2x^4 - 3x^3) = -4x^6 - 4x^4 + 2x^3 + 2x^2$$
  
[2]  $3x^6 - 3x^5 - 4x^3 + -2x^5 - 2x^3 + -5x^6 + 4x^5 = -2x^6 - x^5 - 6x^3$   
[3]  $-x^4 + (-3x^6 + x^4 - 2x) + (-3x^4 - 2x^3 + 2x) = -3x^6 - 3x^4 - 2x^3$   
[4]  $4x^6 + 2x^2 + 2x + -3x^5 - 4x^2 - 2x + -x^3 + 3x^2 - 3x = 4x^6 - 3x^5 - x^3 + x^2 - 3x$   
[5]  $2x^6 - 2x^2 - 2x + -2x^4 + 7x^2 + 3x^6 - 3x^3 - 2x^2 = 5x^6 - 2x^4 - 3x^3 + 3x^2 - 2x$   
[6]  $4x^5 - 2x^3 + x^2 + -x^4 - x^3 + 2x^2 + 3x^5 + 2x^4 = 7x^5 + x^4 - 3x^3 + 3x^2$   
[7]  $2x^5 - 4x^4 - 3x^2 + 4x^6 - 3x^5 - 4x^3 + -4x^4 + 2x^2 - x = 4x^6 - x^5 - 8x^4 - 4x^3 - x^2 - x$   
[8]  $x^5 + 4x^4 + 4x^3 + -6x^2 - 4x + -3x^6 + x^2 + x = -3x^6 + x^5 + 4x^4 + 4x^3 - 5x^2 - 3x$   
[9]  $-x^6 - x^4 - 4x^2 + (-4x^6 + x^3 - 3x) + (-x^6 + 4x^4 - 4x) = -6x^6 + 3x^4 + x^3 - 4x^2 - 7x$   
[10]  $0 + -x^6 + 2x^5 - x + -3x^4 - 4x^3 + x = -x^6 + 2x^5 - 3x^4 - 4x^3$ 

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0 + 0 + 0 = 0 \\ & [2] \quad 3 \, x^2 y^2 + 4 \, x^2 y + x y^2 + -2 \, x^2 y^2 + 2 \, x^2 y + 3 \, x y + (-x^2 y^2 - 3 \, x y^2) = 6 \, x^2 y - 2 \, x y^2 + 3 \, x y \\ & [3] \quad 8 \, x^2 y \, + \, 10 \, x y \, + \, -6 \, x^2 y^2 \, - \, 4 \, x^2 y \, + \, 4 \, x y^2 \, + \, (-4 \, x^2 y^2 \, - \, 4 \, x y^2 \, - \, 4 \, x y) \, = \\ & -10 \, x^2 y^2 \, + \, 4 \, x^2 y \, + \, 6 \, x y \\ & [4] \quad 18 \, x^2 y \, - \, 15 \, x y^2 \, + \, -18 \, x y^2 \, + \, (-3 \, x^2 y^2 \, + \, 27 \, x^2 y) \, = \, -3 \, x^2 y^2 \, + \, 45 \, x^2 y \, - \, 33 \, x y^2 \\ & [5] \quad -48 \, x y^2 \, - \, 16 \, x y \, + \, (-20 \, x^2 y) \, + \, (-8 \, x^2 y^2 \, - \, 48 \, x^2 y \, + \, 32 \, x y) \, = \, -8 \, x^2 y^2 \, - \, 68 \, x^2 y \, - \\ & 48 \, x y^2 \, + \, 16 \, x y \\ & [6] \quad 15 \, x y^2 \, - \, 75 \, x y \, + \, -50 \, x^2 y^2 \, + \, 70 \, x^2 y \, + \, (-25 \, x^2 y \, + \, 50 \, x y^2 \, + \, 25 \, x y) \, = \, -50 \, x^2 y^2 \, + \\ & 45 \, x^2 y \, + \, 65 \, x y^2 \, - \, 50 \, x y \\ & [7] \quad 54 \, x^2 y \, - \, 144 \, x y^2 \, + \, -6 \, x^2 y^2 \, - \, 72 \, x y^2 \, + \, 36 \, x y \, + \, -6 \, x^2 y^2 \, - \, 108 \, x^2 y \, + \, 72 \, x y \, = \\ & -12 \, x^2 y^2 \, - \, 54 \, x^2 y \, - \, 216 \, x y^2 \, + \, 108 \, x y \\ & [8] \quad -196 \, x^2 y \, + \, 42 \, x y^2 \, + \, (-14 \, x^2 y^2 \, + \, 42 \, x y) \, + \, (-7 \, x^2 y \, - \, 14 \, x y) \, = \, -14 \, x^2 y^2 \, - \\ & 203 \, x^2 y \, + \, 42 \, x y^2 \, + \, 28 \, x y \\ & [9] \quad 280 \, x^2 y^2 \, - \, 256 \, x y^2 \, + \, 128 \, x^2 y^2 \, - \, 32 \, x^2 y \, - \, 16 \, x y^2 \, + \, 64 \, x^2 y \, - \, 16 \, x y^2 \, + \, 16 \, x y \, = \\ & [10] \quad 162 \, x^2 y^2 \, - \, 81 \, x^2 y \, + \, 9 \, x y \, + \, - \, 315 \, x y \, + \, - \, 243 \, x^2 y^2 \, - \, 162 \, x y^2 \, + \, 9 \, x y \, = \, - \, 81 \, x^2 y^2 \, - \, \\ & 81 \, x^2 y \, - \, 162 \, x y^2 \, - \, 297 \, x y \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y + -x^2y + 7\,xy - (-2\,x^2y^2) = 2\,x^2y^2 - 3\,x^2y + 7\,xy \\ &[3] \quad 2\,x^2y + 12\,xy + 8\,x^2y + 4\,xy^2 - 4\,xy - (12\,x^2y - 8\,xy^2) = -2\,x^2y + 12\,xy^2 + 8\,xy \\ &[4] \quad -27\,x^2y^2 - 27\,xy - (-63\,x^2y - 36\,xy) + (-36\,x^2y^2 - 27\,x^2y + 3\,xy^2) = -63\,x^2y^2 + 36\,x^2y + 3\,xy^2 + 9\,xy \end{aligned}$$

$$[5] \quad 64\,x^2y^2 + 16\,x^2y + 12\,xy + -16\,x^2y - 48\,xy^2 + 4\,xy - (8\,x^2y + 16\,xy^2 - 4\,xy) = \\ 64\,x^2y^2 - 8\,x^2y - 64\,xy^2 + 20\,xy \\ [6] \quad 15\,xy^2 + 95\,xy + -50\,x^2y - 100\,xy^2 - 5\,xy - (75\,x^2y^2 - 85\,x^2y) = -75\,x^2y^2 + \\ 35\,x^2y - 85\,xy^2 + 90\,xy \\ [7] \quad 90\,x^2y^2 - (36\,x^2y^2 - 18\,xy) + (-12\,x^2y - 90\,xy) = 54\,x^2y^2 - 12\,x^2y - 72\,xy \\ [8] \quad -70\,x^2y - 98\,xy^2 + -28\,x^2y - 133\,xy^2 - (21\,xy^2 + 42\,xy) = -98\,x^2y - 252\,xy^2 - \\ 42\,xy \\ [9] \quad -24\,x^2y^2 + 192\,x^2y - 16\,xy + 24\,x^2y^2 + 128\,xy^2 - (-192\,x^2y^2 - 64\,xy) = \\ 192\,x^2y^2 + 192\,x^2y + 128\,xy^2 + 48\,xy \\ [10] \quad -18\,xy^2 - (324\,xy^2) + (243\,xy^2 - 405\,xy) = -99\,xy^2 - 405\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (4\,b^3x^2yz^3) \cdot (-3\,b^3x^2y^3z^3) = -12\,b^6x^4y^4z^6 \\ &[3] \quad (8\,b^3x^2y^3z) \cdot (4\,bx^2yz^2) = 32\,b^4x^4y^4z^3 \\ &[4] \quad (-6\,b^3xy^3z) \cdot (-3\,b^3x^3y^2z^3) = 18\,b^6x^4y^5z^4 \\ &[5] \quad (-12\,b^2x^3y^2z^2) \cdot (-16\,bx^3yz) = 192\,b^3x^6y^3z^3 \\ &[6] \quad (15\,bx^3y^3z^3) \cdot (20\,b^2x^2yz^2) = 300\,b^3x^5y^4z^5 \\ &[7] \quad (216\,bxy^2z) \cdot (-24\,b^2x^3yz^3) = -5184\,b^3x^4y^3z^4 \\ &[8] \quad (-1029\,b^3x^2y^3z^2) \cdot (-686\,b^2xyz^2) = 705894\,b^5x^3y^4z^4 \\ &[9] \quad (-2048\,b^3x^2y^2z^2) \cdot (-128\,b^3x^3yz^3) = 262144\,b^6x^5y^3z^5 \\ &[10] \quad (243\,b^2x^3yz) \cdot (-324\,b^2xy^2z^3) = -78732\,b^4x^4y^3z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (-x^2) \cdot (-2\,x^2 + 3\,x) = 2\,x^4 - 3\,x^3 \\ & [2] \quad (3\,x) \cdot (3\,x^2) = 9\,x^3 \\ & [3] \quad (-3\,x) \cdot (x^2 - 11\,x) = -3\,x^3 + 33\,x^2 \\ & [4] \quad (2\,x^2) \cdot (x^2 - 2\,x) = 2\,x^4 - 4\,x^3 \\ & [5] \quad (-3\,x^2) \cdot (5\,x^2) = -15\,x^4 \\ & [6] \quad (4\,x^2) \cdot (3\,x^2 + x) = 12\,x^4 + 4\,x^3 \\ & [7] \quad (-2\,x) \cdot (4\,x^2 - 3\,x) = -8\,x^3 + 6\,x^2 \\ & [8] \quad (-x) \cdot (-2\,x^2 + 5\,x) = 2\,x^3 - 5\,x^2 \\ & [9] \quad (x) \cdot (-4\,x^2 - 4\,x) = -4\,x^3 - 4\,x^2 \\ & [10] \quad (-2\,x^2) \cdot (5\,x^2 + x) = -10\,x^4 - 2\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-6x) \cdot (5x^2 - 4x) = -30x^3 + 24x^2$$
  
[2]  $(-2x^2 + 2x) \cdot (5x^2 + 3x) = -10x^4 + 4x^3 + 6x^2$   
[3]  $(3x^2) \cdot (-4x^2 - 2x) = -12x^4 - 6x^3$   
[4]  $(-2x) \cdot (-8x) = 16x^2$   
[5]  $(-x^2) \cdot (-2x^2 + 3x) = 2x^4 - 3x^3$   
[6]  $(5x^2) \cdot (2x^2 + 4x) = 10x^4 + 20x^3$ 

[7] 
$$(-2x^2 - 4x) \cdot (3x^2 - 3x) = -6x^4 - 6x^3 + 12x^2$$

[8] 
$$(8x) \cdot (-2x^2 + 3x) = -16x^3 + 24x^2$$

[9] 
$$(6x) \cdot (-x^2 - 7x) = -6x^3 - 42x^2$$

[10] 
$$(x^2 + 2x) \cdot (-3x) = -3x^3 - 6x^2$$

[11] 
$$(4x^2 - x) \cdot (-7x^2 + 2x) = -28x^4 + 15x^3 - 2x^2$$

[12] 
$$(-x^2 + 4x) \cdot (-12x^2) = 12x^4 - 48x^3$$

[13] 
$$(-6x) \cdot (2x^2 + 3x) = -12x^3 - 18x^2$$

[14] 
$$(-6x) \cdot (-4x^2 - 5x) = 24x^3 + 30x^2$$

[15] 
$$(-5x^2) \cdot (-5x^2) = 25x^4$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(0) \cdot (3x^3 - 3x^2) = 0$$

[2] 
$$(x^2 + 3x) \cdot (-3x^3 - x^2 - 3x) = -3x^5 - 10x^4 - 6x^3 - 9x^2$$

[3] 
$$(-4x^3 + 4x^2) \cdot (x^3 + 2x^2 + 2x) = -4x^6 - 4x^5 + 8x^3$$

[4] 
$$(7x^3 + 3x^2) \cdot (-2x^2) = -14x^5 - 6x^4$$

[5] 
$$(-x^3 + x^2) \cdot (-x^3 + x^2 + 4x) = x^6 - 2x^5 - 3x^4 + 4x^3$$

[6] 
$$(3x^3 + x) \cdot (-2x^2 + x) = -6x^5 + 3x^4 - 2x^3 + x^2$$

[7] 
$$(-x) \cdot (2x^3 - x) = -2x^4 + x^2$$

[8] 
$$(-6x) \cdot (x^3 - 3x^2 - 4x) = -6x^4 + 18x^3 + 24x^2$$

[9] 
$$(x^3) \cdot (4x^3 - 7x^2 + 4x) = 4x^6 - 7x^5 + 4x^4$$

[10] 
$$(4x^3 - x^2) \cdot (2x) = 8x^4 - 2x^3$$

[11] 
$$(-2x^2 - 2x) \cdot (-2x^3 + 2x^2 - x) = 4x^5 - 2x^3 + 2x^2$$

[12] 
$$(4x^2 - 2x) \cdot (-3x^3 - x^2 - 3x) = -12x^5 + 2x^4 - 10x^3 + 6x^2$$

[13] 
$$(-7x^3 + 3x^2) \cdot (8x^3) = -56x^6 + 24x^5$$

[14] 
$$(5x) \cdot (-x^2 + x) = -5x^3 + 5x^2$$

[15] 
$$(-4x^3 - 4x) \cdot (4x^2 - 4x) = -16x^5 + 16x^4 - 16x^3 + 16x^2$$

[16] 
$$(-4x^2 + 4x) \cdot (x^3 - 2x^2) = -4x^5 + 12x^4 - 8x^3$$

[17] 
$$(4x^2 + x) \cdot (-3x^3 - 2x^2 - 3x) = -12x^5 - 11x^4 - 14x^3 - 3x^2$$

[18] 
$$(2x^2) \cdot (-6x^3 - 2x) = -12x^5 - 4x^3$$

[19] 
$$(3x^3 + 3x^2 + 4x) \cdot (-2x^3 + 3x^2) = -6x^6 + 3x^5 + x^4 + 12x^3$$

[20] 
$$(-3x^3 + 2x^2) \cdot (-x^3 + 4x^2 + 7x) = 3x^6 - 14x^5 - 13x^4 + 14x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$[1] \quad (3\,x^2y^2-x^2y)\cdot(-x^2y+xy^2-2\,xy) = -3\,x^4y^3+3\,x^3y^4+x^4y^2-7\,x^3y^3+2\,x^3y^2$$

[2] 
$$(-3x^2y^2 + 4xy^2) \cdot (-4x^2y + 2xy) = 12x^4y^3 - 22x^3y^3 + 8x^2y^3$$

[3] 
$$(6xy) \cdot (x^2y^2 + 2xy^2 + 4xy) = 6x^3y^3 + 12x^2y^3 + 24x^2y^2$$

[4] 
$$(4x^2y^2 - 3xy^2) \cdot (-7x^2y^2 - 4xy^2) = -28x^4y^4 + 5x^3y^4 + 12x^2y^4$$

[5] 
$$(x^2y^2 + xy^2) \cdot (x^2y^2 - 2xy^2) = x^4y^4 - x^3y^4 - 2x^2y^4$$

[6] 
$$(3x^2y^2) \cdot (-3x^2y^2 - 7x^2y) = -9x^4y^4 - 21x^4y^3$$

[7] 
$$(4x^2y^2 + x^2y) \cdot (-3x^2y^2 - x^2y + 3xy) = -12x^4y^4 - 7x^4y^3 - x^4y^2 + 12x^3y^3 + 3x^3y^2$$