1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$3x^5 + x^2 - 4x + -3x^6 + 6x + (-2x^6 - x^2) = -5x^6 + 3x^5 + 2x$$

[2] $4x^4 + 3x^3 - 4x^2 + -3x^5 + 2x^3 + 3x + (-x^5 + x^2 + 4x) = -4x^5 + 4x^4 + 5x^3 - 3x^2 + 7x$
[3] $2x^5 - 3x^4 - 3x^3 + -5x^3 + x^2 + (-2x^6 + 2x^5 - 4x) = -2x^6 + 4x^5 - 3x^4 - 8x^3 + x^2 - 4x$
[4] $2x^5 - x^2 + x + -3x^6 - 2x^5 - 4x^3 + -x^6 - x^5 + 4x^4 = -4x^6 - x^5 + 4x^4 - 4x^3 - x^2 + x$
[5] $-4x^6 - x^4 - x + (-8x) + (-2x^5 - x^3) = -4x^6 - 2x^5 - x^4 - x^3 - 9x$
[6] $-3x^4 - x^3 + (-x^5 + x) + (-2x^6 - x^5 + 2x^4) = -2x^6 - 2x^5 - x^4 - x^3 + x$
[7] $x^4 - x^3 + 3x^2 + 4x^6 + 3x^5 - 4x^4 + 3x^5 - 2x^3 + 3x^2 = 4x^6 + 6x^5 - 3x^4 - 3x^3 + 6x^2$
[8] $x^3 - x^2 + -x^4 - x^3 + x^2 + 3x^6 - 4x^5 + 3x^4 = 3x^6 - 4x^5 + 2x^4$
[9] $3x^6 - 4x^3 - 3x + -3x^4 - 3x^2 + (-7x^5 - x^3) = 3x^6 - 7x^5 - 3x^4 - 5x^3 - 3x^2 - 3x$
[10] $x^5 + x^3 - 4x + -8x^3 - 2x + 3x^6 = 3x^6 + x^5 - 7x^3 - 6x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 3xy^2+-3x^2y^2+xy+x^2y^2-x^2y+3xy^2=-2x^2y^2-x^2y+6xy^2+xy \\ [3] \quad 24x^2y^2-4xy^2+4x^2y^2-8x^2y+16xy+-8x^2y-12xy^2-12xy=28x^2y^2-16x^2y-16xy^2+4xy \\ [4] \quad 9x^2y^2+27xy^2+9xy+-3x^2y^2-9x^2y+27xy^2=6x^2y^2-9x^2y+54xy^2+9xy \\ [5] \quad 32x^2y^2-48x^2y+48xy+8x^2y^2+48x^2y+4x^2y^2=44x^2y^2+48xy \\ [6] \quad 5x^2y^2-100x^2y+50xy+-20x^2y^2-10xy+-100x^2y+25xy^2-5xy=-15x^2y^2-200x^2y+25xy^2+35xy \\ [7] \quad 42x^2y-72xy^2+-114x^2y^2+6x^2y+-108xy^2+30xy=-114x^2y^2+48x^2y-180xy^2+30xy \\ [8] \quad 196x^2y+294xy^2+-7x^2y^2+42x^2y+-168xy^2-196xy=-7x^2y^2+238x^2y+126xy^2-196xy \\ [9] \quad 128x^2y^2-8x^2y-32xy+32x^2y^2+64xy^2+8xy+24xy^2+192xy=160x^2y^2-8x^2y+88xy^2+168xy \\ [10] \quad 81x^2y^2-324x^2y+27xy+-261xy+(-162x^2y+405xy^2)=81x^2y^2-486x^2y+405xy^2-234xy \\ \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y + 3\,xy^2 + x^2y - 4\,xy^2 - (-3\,x^2y^2 + 4\,x^2y + 3\,xy^2) = 3\,x^2y^2 - 5\,x^2y - 4\,xy^2 \\ &[3] \quad 8\,x^2y + 10\,x^2y^2 + 6\,xy - (2\,x^2y^2 - 16\,x^2y - 4\,xy) = 8\,x^2y^2 + 24\,x^2y + 10\,xy \\ &[4] \quad -12\,x^2y^2 + 36\,x^2y - (-3\,x^2y^2 - 54\,x^2y) + (9\,x^2y) = -9\,x^2y^2 + 99\,x^2y \\ &[5] \quad 32\,x^2y + 64\,xy^2 - 64\,xy + 36\,xy - (-60\,x^2y) = 92\,x^2y + 64\,xy^2 - 28\,xy \\ &[6] \quad -15\,x^2y^2 - 20\,x^2y - 10\,xy^2 + 50\,x^2y^2 - 35\,xy - (-35\,xy) = 35\,x^2y^2 - 20\,x^2y - 10\,xy^2 \end{aligned}$$

$$[7] -18 x^2 y^2 - 18 x^2 y + 6 xy - (-54 x^2 y^2 - 24 xy) + (-12 x^2 y - 66 xy) = 36 x^2 y^2 - 30 x^2 y - 36 xy$$

$$[8] -196 x^2 y - 7 xy^2 + 28 xy + -28 x^2 y^2 - 7 xy^2 - 49 xy - (-196 x^2 y + 98 xy^2 + 98 xy) = -28 x^2 y^2 - 112 xy^2 - 119 xy$$

$$[9] 184 xy + 232 xy^2 - (-8 x^2 y^2 + 8 x^2 y + 8 xy^2) = 8 x^2 y^2 - 8 x^2 y + 224 xy^2 + 184 xy$$

$$[10] -27 x^2 y^2 + 81 xy^2 + 27 xy - (567 x^2 y^2 - 243 xy^2) + (342 x^2 y^2 + 81 xy^2) = -252 x^2 y^2 + 405 xy^2 + 27 xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{array}{ll} [1] & (0) \cdot (0) = 0 \\ [2] & (-b^2xyz^3) \cdot (-2\,b^2x^2y^3z^3) = 2\,b^4x^3y^4z^6 \\ [3] & (32\,bxy^2z^3) \cdot (-8\,b^2x^2y^3z^2) = -256\,b^3x^3y^5z^5 \\ [4] & (-9\,bx^2yz) \cdot (9\,bx^2yz^2) = -81\,b^2x^4y^2z^3 \\ [5] & (-192\,bx^3y^3z) \cdot (-128\,bx^3y^3z^3) = 24576\,b^2x^6y^6z^4 \\ [6] & (-125\,b^2x^3y^2z^3) \cdot (50\,b^2x^3yz^3) = -6250\,b^4x^6y^3z^6 \\ [7] & (144\,b^2x^3yz) \cdot (432\,b^2x^2y^3z^2) = 62208\,b^4x^5y^4z^3 \\ [8] & (14\,b^2x^2y^2z^2) \cdot (-1029\,bx^3yz) = -14406\,b^3x^5y^3z^3 \\ [9] & (16\,bx^2y^2z^2) \cdot (512\,b^2x^3yz) = 8192\,b^3x^5y^3z^3 \\ [10] & (729\,bx^3y^2z^3) \cdot (-18\,b^3x^2yz) = -13122\,b^4x^5y^3z^4 \\ \end{array}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x^2)\cdot(-4\,x^2) = -16\,x^4 \\ &[2] \quad (-2\,x)\cdot(2\,x) = -4\,x^2 \\ &[3] \quad (-4\,x^2)\cdot(3\,x^2-3\,x) = -12\,x^4+12\,x^3 \\ &[4] \quad (-x)\cdot(-2\,x^2) = 2\,x^3 \\ &[5] \quad (-4\,x)\cdot(6\,x^2-4\,x) = -24\,x^3+16\,x^2 \\ &[6] \quad (3\,x^2)\cdot(-4\,x^2+x) = -12\,x^4+3\,x^3 \\ &[7] \quad (-4\,x^2)\cdot(4\,x) = -16\,x^3 \\ &[8] \quad (x)\cdot(-x^2-4\,x) = -x^3-4\,x^2 \\ &[9] \quad (-2\,x)\cdot(3\,x^2-3\,x) = -6\,x^3+6\,x^2 \\ &[10] \quad (x^2)\cdot(-x^2+4\,x) = -x^4+4\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(5x^2) \cdot (3x) = 15x^3$$

[2] $(6x^2) \cdot (-5x) = -30x^3$
[3] $(-3x^2) \cdot (-3x^2) = 9x^4$
[4] $(2x^2 - x) \cdot (-3x^2 + 3x) = -6x^4 + 9x^3 - 3x^2$
[5] $(3x) \cdot (4x^2 + 2x) = 12x^3 + 6x^2$
[6] $(-x) \cdot (-3x^2) = 3x^3$
[7] $(-4x^2 - 4x) \cdot (x^2 - 7x) = -4x^4 + 24x^3 + 28x^2$
[8] $(-4x^2 + 2x) \cdot (-4x^2 + 7x) = 16x^4 - 36x^3 + 14x^2$

[9]
$$(4x^2 + 2x) \cdot (4x^2 - x) = 16x^4 + 4x^3 - 2x^2$$

[10]
$$(3x^2) \cdot (-5x^2) = -15x^4$$

[11]
$$(4x^2 - 4x) \cdot (-3x^2 - 7x) = -12x^4 - 16x^3 + 28x^2$$

[12]
$$(-x^2 + 4x) \cdot (3x^2 + 5x) = -3x^4 + 7x^3 + 20x^2$$

[13]
$$(-5x) \cdot (8x^2 + 3x) = -40x^3 - 15x^2$$

[14]
$$(4x^2) \cdot (2x) = 8x^3$$

[15]
$$(4x^2 + 2x) \cdot (-6x^2) = -24x^4 - 12x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x^2 + 2x) \cdot (x^3 - 2x) = 2x^5 + 2x^4 - 4x^3 - 4x^2$$

[2]
$$(x^3) \cdot (x^2 - 2x) = x^5 - 2x^4$$

[3]
$$(-x^2 - 2x) \cdot (-4x^3 + 3x^2 + 2x) = 4x^5 + 5x^4 - 8x^3 - 4x^2$$

[4]
$$(4x^3) \cdot (-4x^2) = -16x^5$$

[5]
$$(-8x) \cdot (5x^3 + 2x) = -40x^4 - 16x^2$$

[6]
$$(4x^2 - 4x) \cdot (2x^3 + 3x) = 8x^5 - 8x^4 + 12x^3 - 12x^2$$

[7]
$$(7x^3 - 3x) \cdot (-4x^2 + 2x) = -28x^5 + 14x^4 + 12x^3 - 6x^2$$

[8]
$$(2x) \cdot (-2x^3 + 2x^2 + 5x) = -4x^4 + 4x^3 + 10x^2$$

[9]
$$(-3x^3) \cdot (x^3 - 2x) = -3x^6 + 6x^4$$

[10]
$$(-x^3 + 3x^2 - x) \cdot (4x^3 + 2x^2 - 2x) = -4x^6 + 10x^5 + 4x^4 - 8x^3 + 2x^2$$

[11]
$$(x^3 - 4x^2) \cdot (3x^3 - 2x^2) = 3x^6 - 14x^5 + 8x^4$$

[12]
$$(3x^3 + 4x^2) \cdot (2x^3) = 6x^6 + 8x^5$$

[13]
$$(-3x^3 - 7x) \cdot (-4x^3 + 2x^2 + x) = 12x^6 - 6x^5 + 25x^4 - 14x^3 - 7x^2$$

[14]
$$(x^2 + 2x) \cdot (-4x^3 - 2x) = -4x^5 - 8x^4 - 2x^3 - 4x^2$$

[15]
$$(-x^3 + x^2) \cdot (-6x^3 + 2x) = 6x^6 - 6x^5 - 2x^4 + 2x^3$$

[16]
$$(-x^3 - x^2) \cdot (3x^3 - 2x^2 + x) = -3x^6 - x^5 + x^4 - x^3$$

[17]
$$(-3x^3 + 3x^2) \cdot (2x^3 + x^2 + x) = -6x^6 + 3x^5 + 3x^3$$

[18]
$$(-3x^3 - 2x) \cdot (-3x^3 + 4x^2 - 2x) = 9x^6 - 12x^5 + 12x^4 - 8x^3 + 4x^2$$

[19]
$$(x^3) \cdot (x^3) = x^6$$

[20]
$$(3x^3 - 2x^2) \cdot (0) = 0$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2y^2 + xy) \cdot (4x^2y^2 - 4x^2y) = 4x^4y^4 - 4x^4y^3 + 4x^3y^3 - 4x^3y^2$$

[2]
$$(-xy^2 - 3xy) \cdot (-x^2y^2 + 3xy^2) = x^3y^4 + 3x^3y^3 - 3x^2y^4 - 9x^2y^3$$

[3]
$$(x^2y + 3xy^2) \cdot (-6x^2y - 3xy^2) = -6x^4y^2 - 21x^3y^3 - 9x^2y^4$$

[4]
$$(-6xy) \cdot (3x^2y^2 - 2x^2y - 3xy^2) = -18x^3y^3 + 12x^3y^2 + 18x^2y^3$$

[5]
$$(-3x^2y - xy^2) \cdot (x^2y^2 - 3x^2y) = -3x^4y^3 - x^3y^4 + 9x^4y^2 + 3x^3y^3$$

[6]
$$(-2x^2y - xy^2) \cdot (-2x^2y^2 + x^2y - 4xy^2) = 4x^4y^3 + 2x^3y^4 - 2x^4y^2 + 7x^3y^3 + 4x^2y^4$$

[7]
$$(-xy^2 - 2xy) \cdot (6x^2y^2 - 4x^2y) = -6x^3y^4 - 8x^3y^3 + 8x^3y^2$$