## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 3x^6 - 2x^3 + -4x^6 + 3x^5 - x + -x^6 - 4x^5 - 3x^3 = -2x^6 - x^5 - 5x^3 - x$$

$$[2] \quad x^5 + 4x^2 - 2x + -2x^6 - 2x^3 + -3x^6 - 3x^5 + 3x^2 = -5x^6 - 2x^5 - 2x^3 + 7x^2 - 2x$$

$$[3] \quad x^6 - 2x^4 + 2x^3 + 4x^4 + 2x^3 - 2x + 2x^6 + 2x^4 + 3x^2 = 3x^6 + 4x^4 + 4x^3 + 3x^2 - 2x$$

$$[4] \quad 2x^4 - 4x^3 + 3x^2 + 4x^6 + 4x^5 - 3x^4 + -x^6 + 3x^4 - 3x^2 = 3x^6 + 4x^5 + 2x^4 - 4x^3$$

$$[5] \quad 5x^2 + -4x^5 + -3x^5 + 4x^2 = -7x^5 + 9x^2$$

$$[6] \quad 2x^6 - 3x^4 + 2x^3 + 4x^4 + 4x^2 + x + -5x^5 - x = 2x^6 - 5x^5 + x^4 + 2x^3 + 4x^2$$

$$[7] \quad x^6 + 2x^3 + 3x^2 + -x^6 - x^5 - 3x^3 + -4x^6 - 4x^5 + 2x^4 = -4x^6 - 5x^5 + 2x^4 - x^3 + 3x^2$$

$$[8] \quad 3x^6 - 2x^5 + 2x^3 + -3x^6 - x^3 + 2x^2 + (-2x^4 + 3x^2 + 2x) = -2x^5 - 2x^4 + x^3 + 5x^2 + 2x$$

$$[9] \quad 2x^4 + 3x^3 + x^5 - x^2 + 2x + x^6 = x^6 + x^5 + 2x^4 + 3x^3 - x^2 + 2x$$

$$[9] \quad 2x^4 + 3x^5 + -x^6 - x^4 - x^2 + 2x^6 - 4x^2 = 2x^6 + 3x^5 - x^4 - 5x^2$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 2xy^2+4xy+2x^2y+xy^2+xy+x^2y=3x^2y+3xy^2+5xy \\ [3] \quad 6x^2y+6xy^2-4xy+-6x^2y^2-8x^2y-2xy+4x^2y+12xy=-6x^2y^2+2x^2y+6xy^2+6xy \\ [4] \quad 36x^2y^2+3x^2y-6xy^2+-3xy^2-3xy+30xy=36x^2y^2+3x^2y-9xy^2+27xy \\ [5] \quad 72x^2y+16xy+-8x^2y^2+16x^2y+-48x^2y+16xy^2-16xy=-8x^2y^2+40x^2y+16xy^2 \\ [6] \quad 15x^2y^2-20xy+-50x^2y^2+5x^2y+10xy+-25x^2y^2=-60x^2y^2+5x^2y-10xy \\ [7] \quad 36x^2y+24xy^2-12xy+-108x^2y^2-144x^2y+-6x^2y^2+36x^2y+72xy^2=-114x^2y^2-72x^2y+96xy^2-12xy \\ [8] \quad -98x^2y+(-28x^2y^2+14xy^2)+(-175x^2y+196xy)=-28x^2y^2-273x^2y+14xy^2+196xy \\ [9] \quad -128x^2y^2-32xy^2+32xy+(-192x^2y^2-128x^2y)+(-128x^2y^2-232xy^2)=-448x^2y^2-128x^2y-264xy^2+32xy \\ [10] \quad 27x^2y^2-9xy^2+36xy+-324x^2y^2-324x^2y-243xy+(-162x^2y+18xy^2)=-297x^2y^2-486x^2y+9xy^2-207xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -4\,x^2y^2 - 2\,xy + -3\,x^2y^2 - 2\,xy^2 + 3\,xy - (6\,x^2y^2 - 2\,xy^2) = -13\,x^2y^2 + xy \\ &[3] \quad 6\,x^2y^2 + 4\,x^2y + 2\,xy^2 + -2\,x^2y^2 + 2\,x^2y - 8\,xy - (-4\,x^2y + 4\,xy^2 - 4\,xy) = \\ &4\,x^2y^2 + 10\,x^2y - 2\,xy^2 - 4\,xy \\ &[4] \quad 9\,x^2y^2 + 6\,xy^2 - (18\,x^2y + 6\,xy) + (-15\,x^2y^2 + 18\,xy^2) = -6\,x^2y^2 - 18\,x^2y + \\ &24\,xy^2 - 6\,xy \\ &[5] \quad 4\,x^2y^2 - 12\,x^2y - 4\,xy + -64\,x^2y - 16\,xy^2 - (-80\,xy^2) = 4\,x^2y^2 - 76\,x^2y + \\ &64\,xy^2 - 4\,xy \end{aligned}$$

$$\begin{aligned} & [6] \quad 10\,x^2y^2 - 75\,xy^2 + 5\,x^2y^2 + 60\,xy^2 - (50\,x^2y^2 - 30\,xy) = -35\,x^2y^2 - 15\,xy^2 + 30\,xy \\ & [7] \quad -144\,x^2y^2 - 48\,x^2y - (72\,x^2y^2 - 36\,x^2y - 72\,xy^2) + (-48\,x^2y - 108\,xy) = \\ & -216\,x^2y^2 - 60\,x^2y + 72\,xy^2 - 108\,xy \\ & [8] \quad 98\,x^2y^2 + 21\,x^2y - 147\,xy^2 + 56\,x^2y^2 + 7\,xy - (49\,xy^2 + 119\,xy) = 154\,x^2y^2 + \\ & 21\,x^2y - 196\,xy^2 - 112\,xy \\ & [9] \quad 8\,x^2y^2 + 192\,x^2y - 256\,xy^2 + -40\,xy^2 - 192\,xy - (64\,xy^2 - 200\,xy) = 8\,x^2y^2 + \\ & 192\,x^2y - 360\,xy^2 + 8\,xy \\ & [10] \quad -243\,x^2y + 243\,xy^2 - 18\,xy - (-81\,x^2y + 9\,xy^2 - 81\,xy) + (162\,x^2y - 36\,xy^2 + 81\,xy) = 198\,xy^2 + 144\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

[1] 
$$(0) \cdot (0) = 0$$
  
[2]  $(-bx^2yz^3) \cdot (3b^2x^2y^2z^3) = -3b^3x^4y^3z^6$   
[3]  $(-24bx^3yz^3) \cdot (6bxy^3z^2) = -144b^2x^4y^4z^5$   
[4]  $(-9bxy^3z^3) \cdot (-108bxyz^3) = 972b^2x^2y^4z^6$   
[5]  $(-16b^2x^3y^3z) \cdot (8bx^3y^2z) = -128b^3x^6y^5z^2$   
[6]  $(-250b^2x^3yz^3) \cdot (15b^3xy^2z^2) = -3750b^5x^4y^3z^5$   
[7]  $(-36b^3xy^3z) \cdot (-432bx^3y^3z) = 15552b^4x^4y^6z^2$   
[8]  $(1372bx^3y^2z^3) \cdot (-98bx^3y^2z^3) = -134456b^2x^6y^4z^6$   
[9]  $(8bx^2y^3z^2) \cdot (16b^2x^2yz^2) = 128b^3x^4y^4z^4$   
[10]  $(243b^2x^2yz^2) \cdot (162bx^2y^3z^2) = 39366b^3x^4y^4z^4$ 

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-2x^2) \cdot (-x^2 + 5x) = 2x^4 - 10x^3$$
  
[2]  $(-2x^2) \cdot (-5x^2) = 10x^4$   
[3]  $(2x) \cdot (4x^2 + 5x) = 8x^3 + 10x^2$   
[4]  $(3x^2) \cdot (0) = 0$   
[5]  $(x^2) \cdot (4x^2 + 2x) = 4x^4 + 2x^3$   
[6]  $(4x) \cdot (-3x^2 - 2x) = -12x^3 - 8x^2$   
[7]  $(-2x) \cdot (-2x^2 + 2x) = 4x^3 - 4x^2$   
[8]  $(-4x) \cdot (2x^2) = -8x^3$   
[9]  $(4x) \cdot (x^2 - 6x) = 4x^3 - 24x^2$   
[10]  $(-2x^2) \cdot (-6x^2 + 3x) = 12x^4 - 6x^3$ 

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-6x) \cdot (-2x^2 - x) = 12x^3 + 6x^2$$
  
[2]  $(2x^2 - 2x) \cdot (7x^2 + x) = 14x^4 - 12x^3 - 2x^2$   
[3]  $(2x^2 - 3x) \cdot (-3x^2) = -6x^4 + 9x^3$   
[4]  $(-2x) \cdot (4x^2 - 4x) = -8x^3 + 8x^2$   
[5]  $(x^2 + 4x) \cdot (-4x^2) = -4x^4 - 16x^3$   
[6]  $(-8x) \cdot (-2x^2 + x) = 16x^3 - 8x^2$   
[7]  $(x^2 + x) \cdot (-x^2 - 2x) = -x^4 - 3x^3 - 2x^2$ 

[8] 
$$(-x^2) \cdot (6x^2 + 2x) = -6x^4 - 2x^3$$
  
[9]  $(-x^2 - 4x) \cdot (2x^2 + 2x) = -2x^4 - 10x^3 - 8x^2$ 

[10] 
$$(4x^2 + x) \cdot (5x^2) = 20x^4 + 5x^3$$

[11] 
$$(4x^2 - 4x) \cdot (-2x^2 + x) = -8x^4 + 12x^3 - 4x^2$$

[12] 
$$(-x^2 + x) \cdot (-5x^2 + x) = 5x^4 - 6x^3 + x^2$$

[13] 
$$(6x) \cdot (-7x^2 - 4x) = -42x^3 - 24x^2$$

[14] 
$$(4x^2) \cdot (2x^2 + 4x) = 8x^4 + 16x^3$$

[15] 
$$(-2x^2 - 2x) \cdot (2x^2) = -4x^4 - 4x^3$$

## Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-4x^3 + x^2 + x) \cdot (2x^3 + 2x^2 + 2x) = -8x^6 - 6x^5 - 4x^4 + 4x^3 + 2x^2$$

[2] 
$$(-2x^3 + x^2) \cdot (x^3 - 7x^2) = -2x^6 + 15x^5 - 7x^4$$

[3] 
$$(-3x^3 - 4x) \cdot (3x^3 + x^2 + 5x) = -9x^6 - 3x^5 - 27x^4 - 4x^3 - 20x^2$$

[4] 
$$(x^3 + x) \cdot (5x^3 + 4x^2) = 5x^6 + 4x^5 + 5x^4 + 4x^3$$

[5] 
$$(-x^2 - 3x) \cdot (3x^2) = -3x^4 - 9x^3$$

[6] 
$$(x^3 - x^2) \cdot (-2x^3 - 6x^2 + x) = -2x^6 - 4x^5 + 7x^4 - x^3$$

[7] 
$$(2x^3 - x^2 + 4x) \cdot (-4x^3 - x^2 + x) = -8x^6 + 2x^5 - 13x^4 - 5x^3 + 4x^2$$

[8] 
$$(2x^2 - x) \cdot (-x^3) = -2x^5 + x^4$$

[9] 
$$(-5x) \cdot (-4x^3 + 3x^2 - 4x) = 20x^4 - 15x^3 + 20x^2$$

[10] 
$$(x^3) \cdot (4x^3 - 2x^2 + x) = 4x^6 - 2x^5 + x^4$$

[11] 
$$(4x^2 + x) \cdot (-x^3 + 3x^2) = -4x^5 + 11x^4 + 3x^3$$

[12] 
$$(-x^3 + 2x) \cdot (-2x^3 - 5x) = 2x^6 + x^4 - 10x^2$$

[13] 
$$(4x^3 - 3x^2 - 3x) \cdot (3x) = 12x^4 - 9x^3 - 9x^2$$

[14] 
$$(x^3 - 2x^2) \cdot (-6x^3 + 2x^2) = -6x^6 + 14x^5 - 4x^4$$

[15] 
$$(-3x^2 - 3x) \cdot (3x^3 + x) = -9x^5 - 9x^4 - 3x^3 - 3x^2$$

[16] 
$$(-x^3 - 2x^2 + 3x) \cdot (x^3 + 2x) = -x^6 - 2x^5 + x^4 - 4x^3 + 6x^2$$

[17] 
$$(7x^2) \cdot (8x^3) = 56x^5$$

[18] 
$$(4x) \cdot (x^3 + x^2 - 3x) = 4x^4 + 4x^3 - 12x^2$$

[19] 
$$(4x^3 + 2x^2 + 2x) \cdot (-4x^3 - 2x) = -16x^6 - 8x^5 - 16x^4 - 4x^3 - 4x^2$$

[20] 
$$(-4x^3 + x^2) \cdot (-x^2 - x) = 4x^5 + 3x^4 - x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$[1] \quad (4\,x^2y^2-4\,xy)\cdot(-3\,x^2y^2+xy) = -12\,x^4y^4+16\,x^3y^3-4\,x^2y^2$$

[2] 
$$(x^2y + 2xy) \cdot (3x^2y^2 - 7x^2y) = 3x^4y^3 - 7x^4y^2 + 6x^3y^3 - 14x^3y^2$$

[3] 
$$(3x^2y^2 - 2xy^2) \cdot (-4x^2y^2 + 3xy) = -12x^4y^4 + 8x^3y^4 + 9x^3y^3 - 6x^2y^3$$

[4] 
$$(2xy^2) \cdot (-4x^2y^2 + x^2y - 4xy) = -8x^3y^4 + 2x^3y^3 - 8x^2y^3$$

[5] 
$$(-4x^2y^2 + 3x^2y) \cdot (-2xy^2 + 3xy) = 8x^3y^4 - 18x^3y^3 + 9x^3y^2$$

[6] 
$$(-3x^2y^2+4xy)\cdot(4x^2y^2-xy^2-4xy)=-12x^4y^4+3x^3y^4+28x^3y^3-4x^2y^3-16x^2y^2$$

[7] 
$$(-2x^2y^2 - 4xy^2) \cdot (3x^2y^2 + 5x^2y) = -6x^4y^4 - 10x^4y^3 - 12x^3y^4 - 20x^3y^3$$