1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$2x^4 - 2x^3 - x^2 + -x^6 - x^5 - x^4 + (-x^6 + 4x^3 + 2x) = -2x^6 - x^5 + x^4 + 2x^3 - x^2 + 2x$$

[2] $2x^5 + 6x^3 + 3x^6 - 3x^4 + 3x^2 + 7x^6 - x^4 = 10x^6 + 2x^5 - 4x^4 + 6x^3 + 3x^2$
[3] $-3x^5 - 6x + (-2x^6 + x^4 - 3x^2) + (-x^5 + x) = -2x^6 - 4x^5 + x^4 - 3x^2 - 5x$
[4] $2x^6 - 3x^5 + x^3 + 3x^3 - 3x + -x^6 + 4x^2 = x^6 - 3x^5 + 4x^3 + 4x^2 - 3x$
[5] $x^6 + 4x^4 + x^3 + -2x^6 - 2x^5 + 4x^2 + -2x^3 + 2x^2 = -x^6 - 2x^5 + 4x^4 - x^3 + 6x^2$
[6] $x^6 + 2x^4 + 2x^6 - 2x^4 + 2x^3 + 2x^6 - 5x^2 = 5x^6 + 2x^3 - 5x^2$
[7] $3x^5 + 2x^4 - 4x^3 + -2x^3 + 6x + 4x^6 + x^4 = 4x^6 + 3x^5 + 3x^4 - 6x^3 + 6x$
[8] $7x^5 - 4x + 3x^5 + -2x^5 - 4x^4 + x^2 = 8x^5 - 4x^4 + x^2 - 4x$
[9] $3x^6 + 3x^4 + x^3 + -x^3 + (-x^3) = 3x^6 + 3x^4 - x^3$
[10] $-4x^3 - 2x^2 + x + (-4x^6 - 2x^5 + 2x^3) + (-4x^6 + x^3 - x^2) = -8x^6 - 2x^5 - x^3 - 3x^2 + x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} &[1] \quad 0+0+0=0 \\ &[2] \quad 4x^2y-xy^2+-x^2y^2-3\,x^2y+xy+5\,xy=-x^2y^2+x^2y-xy^2+6\,xy \\ &[3] \quad 4x^2y-8\,xy^2+4\,xy+-4\,x^2y+16\,xy^2+8\,xy+(-4\,x^2y-2\,xy)=-4\,x^2y+8\,xy^2+10\,xy \\ &[4] \quad 6x^2y^2+9\,xy^2+27\,xy+30\,xy^2+3\,x^2y^2+3\,xy^2-6\,xy=9\,x^2y^2+42\,xy^2+21\,xy \\ &[5] \quad 16\,x^2y-24\,xy+-32\,x^2y^2+64\,x^2y+48\,xy+128\,x^2y^2=96\,x^2y^2+80\,x^2y+24\,xy \\ &[6] \quad 75\,x^2y^2-25\,xy^2+75\,xy+-35\,x^2y^2+10\,x^2y+-20\,x^2y^2+65\,x^2y=20\,x^2y^2+75\,x^2y-25\,xy^2+75\,xy \\ &[7] \quad 24\,xy^2-54\,xy+24\,x^2y^2+288\,xy+72\,x^2y+48\,xy^2=24\,x^2y^2+72\,x^2y+72\,xy^2+234\,xy \\ &[8] \quad 175\,xy^2+7\,xy+-7\,x^2y^2+7\,xy+-119\,x^2y^2+147\,xy=-126\,x^2y^2+175\,xy^2+161\,xy \\ &[9] \quad 24\,x^2y^2+16\,x^2y+-32\,x^2y^2-160\,xy^2+128\,x^2y^2-128\,x^2y+16\,xy^2=120\,x^2y^2-112\,x^2y-144\,xy^2 \\ &[10] \quad 36\,x^2y-324\,xy^2+36\,xy+-18\,x^2y-27\,xy^2-9\,xy+-27\,x^2y^2+333\,xy^2=-27\,x^2y^2+18\,x^2y-18\,xy^2+27\,xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad x^2y^2 + 2\,x^2y - 4\,xy + -3\,x^2y^2 - x^2y - 3\,xy^2 - (-2\,x^2y^2) = x^2y - 3\,xy^2 - 4\,xy \\ &[3] \quad 4\,x^2y + 8\,xy^2 - 4\,xy + -8\,x^2y^2 + 10\,xy - (6\,x^2y - 14\,xy) = -8\,x^2y^2 - 2\,x^2y + 8\,xy^2 + 20\,xy \\ &[4] \quad -42\,x^2y + 36\,xy^2 - (9\,x^2y^2 + 9\,xy) + (-27\,x^2y^2 - 12\,xy^2 - 27\,xy) = -36\,x^2y^2 - 42\,x^2y + 24\,xy^2 - 36\,xy \\ &[5] \quad 8\,xy^2 + 64\,xy + 96\,x^2y - (-16\,x^2y - 32\,xy^2 + 12\,xy) = 112\,x^2y + 40\,xy^2 + 52\,xy \\ &[6] \quad 60\,xy^2 + 5\,x^2y^2 - 25\,xy^2 - (-25\,x^2y^2 + 50\,x^2y + 5\,xy^2) = 30\,x^2y^2 - 50\,x^2y + 30\,xy^2 \end{aligned}$$

$$[7] \quad 108 \, x^2 y^2 - 12 \, x^2 y - (-72 \, x^2 y^2 - 72 \, x^2 y - 36 \, xy^2) + (6 \, x^2 y + 12 \, xy^2 - 36 \, xy) = \\ 180 \, x^2 y^2 + 66 \, x^2 y + 48 \, xy^2 - 36 \, xy \\ [8] \quad -7 \, x^2 y^2 + 189 \, x^2 y + -28 \, x^2 y^2 + 98 \, xy^2 - (28 \, x^2 y - 98 \, xy^2 + 7 \, xy) = -35 \, x^2 y^2 + \\ 161 \, x^2 y + 196 \, xy^2 - 7 \, xy \\ [9] \quad 32 \, x^2 y^2 + 48 \, xy + -16 \, x^2 y - 24 \, xy^2 + 16 \, xy - (80 \, xy) = 32 \, x^2 y^2 - 16 \, x^2 y - \\ 24 \, xy^2 - 16 \, xy \\ [10] \quad -81 \, x^2 y^2 - 243 \, x^2 y - (135 \, x^2 y + 9 \, xy^2) + (81 \, x^2 y^2 - 27 \, x^2 y - 324 \, xy) = \\ -405 \, x^2 y - 9 \, xy^2 - 324 \, xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (b^3x^2y^2z^2) \cdot (2\,bx^3y^3z^2) = 2\,b^4x^5y^5z^4 \\ &[3] \quad (-24\,bx^2y^3z) \cdot (-6\,b^2x^3y^3z) = 144\,b^3x^5y^6z^2 \\ &[4] \quad (18\,bx^3y^3z) \cdot (-12\,bxy^3z^2) = -216\,b^2x^4y^6z^3 \\ &[5] \quad (-12\,b^3x^3y^2z^2) \cdot (-4\,bxy^3z) = 48\,b^4x^4y^5z^3 \\ &[6] \quad (50\,b^2xy^2z^2) \cdot (-20\,bx^3y^3z^3) = -1000\,b^3x^4y^5z^5 \\ &[7] \quad (216\,b^2xy^2z^2) \cdot (-18\,b^3xyz^3) = -3888\,b^5x^2y^3z^5 \\ &[8] \quad (1372\,b^2xyz) \cdot (-7\,b^2x^3yz^3) = -9604\,b^4x^4y^2z^4 \\ &[9] \quad (128\,b^3x^2y^2z^2) \cdot (-1024\,bx^3yz) = -131072\,b^4x^5y^3z^3 \\ &[10] \quad (729\,bx^2y^3z^3) \cdot (-2187\,bx^3y^3z) = -1594323\,b^2x^5y^6z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x^2) \cdot (-4\,x^2 - 3\,x) = 8\,x^4 + 6\,x^3 \\ &[2] \quad (4\,x^2) \cdot (x^2 - 8\,x) = 4\,x^4 - 32\,x^3 \\ &[3] \quad (-3\,x^2) \cdot (-5\,x^2 - 4\,x) = 15\,x^4 + 12\,x^3 \\ &[4] \quad (3\,x^2) \cdot (-2\,x^2 + 4\,x) = -6\,x^4 + 12\,x^3 \\ &[5] \quad (-4\,x^2) \cdot (-2\,x^2 - 3\,x) = 8\,x^4 + 12\,x^3 \\ &[6] \quad (-2\,x) \cdot (-5\,x^2 + 2\,x) = 10\,x^3 - 4\,x^2 \\ &[7] \quad (x) \cdot (4\,x^2 + 2\,x) = 4\,x^3 + 2\,x^2 \\ &[8] \quad (4\,x) \cdot (-x^2 - x) = -4\,x^3 - 4\,x^2 \\ &[9] \quad (-3\,x) \cdot (7\,x) = -21\,x^2 \\ &[10] \quad (4\,x) \cdot (-2\,x^2 - 2\,x) = -8\,x^3 - 8\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (2\,x^2-4\,x)\cdot(2\,x^2+7\,x) = 4\,x^4+6\,x^3-28\,x^2 \\ &[2] \quad (-3\,x^2-4\,x)\cdot(-3\,x^2+5\,x) = 9\,x^4-3\,x^3-20\,x^2 \\ &[3] \quad (x^2+3\,x)\cdot(-4\,x^2+x) = -4\,x^4-11\,x^3+3\,x^2 \\ &[4] \quad (-2\,x^2-3\,x)\cdot(-2\,x^2) = 4\,x^4+6\,x^3 \\ &[5] \quad (3\,x^2-4\,x)\cdot(2\,x^2+7\,x) = 6\,x^4+13\,x^3-28\,x^2 \\ &[6] \quad (-2\,x)\cdot(6\,x^2-4\,x) = -12\,x^3+8\,x^2 \\ &[7] \quad (-2\,x)\cdot(2\,x^2-2\,x) = -4\,x^3+4\,x^2 \\ &[8] \quad (x^2+x)\cdot(2\,x^2-x) = 2\,x^4+x^3-x^2 \end{aligned}$$

[9]
$$(x^2 - 4x) \cdot (4x^2 + 4x) = 4x^4 - 12x^3 - 16x^2$$

[10]
$$(-x^2 - 4x) \cdot (-6x^2 + 3x) = 6x^4 + 21x^3 - 12x^2$$

[11]
$$(4x^2) \cdot (2x^2) = 8x^4$$

[12]
$$(-3x^2 + 4x) \cdot (-3x^2) = 9x^4 - 12x^3$$

[13]
$$(-4x^2 - 3x) \cdot (-x^2 + 6x) = 4x^4 - 21x^3 - 18x^2$$

[14]
$$(-4x^2 + x) \cdot (4x^2 - x) = -16x^4 + 8x^3 - x^2$$

[15]
$$(2x) \cdot (2x) = 4x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^3 + 2x^2 + 4x) \cdot (-x^2 - 3x) = 2x^5 + 4x^4 - 10x^3 - 12x^2$$

[2]
$$(5x^2) \cdot (-2x^3 + 6x^2 - 2x) = -10x^5 + 30x^4 - 10x^3$$

[3]
$$(4x^3 - 2x^2) \cdot (-2x^3 - 2x^2 - 2x) = -8x^6 - 4x^5 - 4x^4 + 4x^3$$

[4]
$$(2x^3 - 5x) \cdot (-6x^3 - 3x^2) = -12x^6 - 6x^5 + 30x^4 + 15x^3$$

[5]
$$(x^2 + 2x) \cdot (-5x^3 + 2x^2 + 4x) = -5x^5 - 8x^4 + 8x^3 + 8x^2$$

[6]
$$(-2x^2 + 3x) \cdot (-4x^2 + 3x) = 8x^4 - 18x^3 + 9x^2$$

[7]
$$(-3x^3 - 2x^2) \cdot (-4x^2 + 2x) = 12x^5 + 2x^4 - 4x^3$$

[8]
$$(-3x^3 + 2x) \cdot (6x^3 + 3x^2) = -18x^6 - 9x^5 + 12x^4 + 6x^3$$

[9]
$$(-2x^2+4x)\cdot(-x^3+2x^2+3x)=2x^5-8x^4+2x^3+12x^2$$

[10]
$$(0) \cdot (7x^3 - 4x) = 0$$

[11]
$$(6x^2) \cdot (-x^3 + 6x^2 + 3x) = -6x^5 + 36x^4 + 18x^3$$

[12]
$$(-2x^2 - 2x) \cdot (-5x^3 - x) = 10x^5 + 10x^4 + 2x^3 + 2x^2$$

[13]
$$(-3x^3 + x^2 + 2x) \cdot (3x) = -9x^4 + 3x^3 + 6x^2$$

[14]
$$(2x^3) \cdot (-6x^3 - x^2 - 3x) = -12x^6 - 2x^5 - 6x^4$$

[15]
$$(-3x^3) \cdot (x^2 - 3x) = -3x^5 + 9x^4$$

[16]
$$(2x^3 - x^2 + 4x) \cdot (3x^3) = 6x^6 - 3x^5 + 12x^4$$

[17]
$$(2x^3 - 2x^2) \cdot (2x^3 + 2x) = 4x^6 - 4x^5 + 4x^4 - 4x^3$$

[18]
$$(-x^3 + 3x^2) \cdot (2x^2 - x) = -2x^5 + 7x^4 - 3x^3$$

[19]
$$(-9x) \cdot (-4x^2) = 36x^3$$

[20]
$$(-4x^3 - 4x^2) \cdot (-x^3 + x^2 - x) = 4x^6 + 4x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x^2y) \cdot (8xy) = 16x^3y^2$$

[2]
$$(2x^2y) \cdot (-3x^2y - 3xy) = -6x^4y^2 - 6x^3y^2$$

[3]
$$(-3x^2y^2 + 4x^2y) \cdot (-2xy^2 + xy) = 6x^3y^4 - 11x^3y^3 + 4x^3y^2$$

[4]
$$(-2xy^2) \cdot (6x^2y^2 + xy) = -12x^3y^4 - 2x^2y^3$$

[5]
$$(-4x^2y + xy^2) \cdot (-x^2y^2 + 4x^2y) = 4x^4y^3 - x^3y^4 - 16x^4y^2 + 4x^3y^3$$

[6]
$$(-x^2y^2) \cdot (7x^2y + 3xy^2) = -7x^4y^3 - 3x^3y^4$$

[7]
$$(-x^2y^2 - 4xy) \cdot (-5xy^2 + xy) = 5x^3y^4 - x^3y^3 + 20x^2y^3 - 4x^2y^2$$