1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad x^4 - x^2 + -2 x^5 - 3 x^4 - 4 x^3 + -2 x^6 + 4 x^4 - 4 x = -2 x^6 - 2 x^5 + 2 x^4 - 4 x^3 - x^2 - 4 x$$

$$[2] \quad 2 x^4 - x^3 + 2 x + x^6 + 7 x^5 + -3 x^6 + 4 x^5 + x = -2 x^6 + 11 x^5 + 2 x^4 - x^3 + 3 x$$

$$[3] \quad 2 x^6 + x^3 + 3 x^5 - x^3 - 3 x + -3 x^6 - 3 x^5 - 2 x^3 = -x^6 - 2 x^3 - 3 x$$

$$[4] \quad 2 x^6 + 6 x^3 + -4 x^6 + 4 x^5 + 2 x^4 + x^6 + 3 x^2 = -x^6 + 4 x^5 + 2 x^4 + 6 x^3 + 3 x^2$$

$$[5] \quad 5 x^5 - 4 x^4 + -6 x^6 + x^4 + -4 x^6 - 2 x^5 + x^4 = -10 x^6 + 3 x^5 - 2 x^4$$

$$[6] \quad 4 x^5 + 3 x^3 + x^3 + 2 x^2 + 2 x + 2 x^6 + 3 x^5 = 2 x^6 + 7 x^5 + 4 x^3 + 2 x^2 + 2 x$$

$$[7] \quad 4 x^6 + 2 x^2 + 4 x^5 + 3 x + -3 x^6 - x^3 + 4 x = x^6 + 4 x^5 - x^3 + 2 x^2 + 7 x$$

$$[8] \quad x^5 - 3 x^3 - 4 x^2 + 2 x^2 + 6 x + 3 x^3 + 2 x^2 = x^5 + 6 x$$

$$[9] \quad x^4 - 8 x + -2 x^6 + -3 x^6 = -5 x^6 + x^4 - 8 x$$

$$[10] \quad x^6 - 2 x^3 - x + -2 x^6 + 3 x^4 + x^3 + 3 x^6 + 3 x^3 = 2 x^6 + 3 x^4 + 2 x^3 - x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0$$

$$[2] \quad 4x^2y+xy+-5xy^2-4xy+(-8x^2y+2xy^2)=-4x^2y-3xy^2-3xy$$

$$[3] \quad -6xy^2+(-8xy^2)+(-4xy^2+20xy)=-18xy^2+20xy$$

$$[4] \quad 30x^2y^2+-18x^2y^2+18x^2y+12xy+-3x^2y^2+6x^2y+12xy^2=9x^2y^2+24x^2y+12xy^2+12xy$$

$$[5] \quad 16x^2y+16xy^2-64xy+-60x^2y-16xy^2+16x^2y+16xy^2=-28x^2y+16xy^2-64xy$$

$$[6] \quad 15x^2y^2+50x^2y-10xy+-15x^2y^2-100xy+-5xy^2=50x^2y-5xy^2-110xy$$

$$[7] \quad 180x^2y^2-36xy+144x^2y^2+12xy^2+24xy+-24x^2y^2+84xy=300x^2y^2+12xy^2+72xy$$

$$[8] \quad 147x^2y^2-42x^2y+-98x^2y^2+28x^2y-196xy+49x^2y^2+217x^2y=98x^2y^2+203x^2y-196xy$$

$$[9] \quad -64xy^2+184xy+(-8x^2y^2+176xy^2)+(-32x^2y^2-32x^2y)=-40x^2y^2-32x^2y+112xy^2+184xy$$

$$[10] \quad 324x^2y-9xy^2-81xy+207xy+-288x^2y+81xy=36x^2y-9xy^2+207xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -x^2y^2 - 3\,xy + xy^2 - 3\,xy - (4\,x^2y^2 + xy^2) = -5\,x^2y^2 - 6\,xy \\ &[3] \quad -8\,x^2y + 2\,xy^2 + 6\,x^2y + 12\,xy^2 - 8\,xy - (12\,x^2y) = -14\,x^2y + 14\,xy^2 - 8\,xy \\ &[4] \quad -18\,x^2y - 15\,xy^2 - (-12\,x^2y^2 - 9\,x^2y - 9\,xy) + (-12\,x^2y - 12\,xy^2) = 12\,x^2y^2 - 21\,x^2y - 27\,xy^2 + 9\,xy \\ &[5] \quad -32\,x^2y^2 + 4\,xy^2 - 12\,xy + -64\,x^2y^2 - 4\,xy - (-16\,x^2y^2 - 4\,x^2y + 48\,xy) = -80\,x^2y^2 + 4\,x^2y + 4\,xy^2 - 64\,xy \\ &[6] \quad -5\,x^2y^2 + 10\,xy^2 + -10\,x^2y + 15\,xy^2 - (-80\,x^2y^2 - 5\,x^2y) = 75\,x^2y^2 - 5\,x^2y + 25\,xy^2 \end{aligned}$$

$$[7] \quad 102\,x^2y + 12\,xy - (-36\,x^2y^2 + 72\,x^2y + 18\,xy^2) + (6\,x^2y^2 + 144\,xy^2 + 6\,xy) = 42\,x^2y^2 + 30\,x^2y + 126\,xy^2 + 18\,xy$$

$$[8] \quad -7\,x^2y^2 + 28\,x^2y + 49\,xy^2 + -140\,x^2y - 196\,xy - (196\,x^2y^2 - 49\,x^2y) = -203\,x^2y^2 - 63\,x^2y + 49\,xy^2 - 196\,xy$$

$$[9] \quad -40\,x^2y^2 + 32\,xy^2 + 480\,xy - (-240\,x^2y) = -40\,x^2y^2 + 240\,x^2y + 32\,xy^2 + 480\,xy$$

$$[10] \quad -243\,x^2y + 324\,xy^2 + 9\,xy - (-162\,x^2y^2 + 18\,x^2y - 36\,xy) + (315\,x^2y^2 + 27\,xy^2) = 477\,x^2y^2 - 261\,x^2y + 351\,xy^2 + 45\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-bx^2yz) \cdot (3\,bx^3y^3z) = -3\,b^2x^5y^4z^2 \\ &[3] \quad (-24\,b^3x^2yz^2) \cdot (-2\,b^3xy^2z) = 48\,b^6x^3y^3z^3 \\ &[4] \quad (9\,bxy^3z) \cdot (9\,bx^3yz^2) = 81\,b^2x^4y^4z^3 \\ &[5] \quad (32\,bx^2yz^2) \cdot (32\,bx^2y^3z^3) = 1024\,b^2x^4y^4z^5 \\ &[6] \quad (50\,b^3x^3y^2z) \cdot (-100\,bx^2y^2z^2) = -5000\,b^4x^5y^4z^3 \\ &[7] \quad (432\,b^2xy^3z) \cdot (-864\,b^2x^2yz^2) = -373248\,b^4x^3y^4z^3 \\ &[8] \quad (-147\,b^3x^3y^3z) \cdot (98\,b^3xyz^3) = -14406\,b^6x^4y^4z^4 \\ &[9] \quad (512\,b^3x^3y^3z^2) \cdot (-8\,bxy^3z^2) = -4096\,b^4x^4y^6z^4 \\ &[10] \quad (2916\,b^2x^3yz) \cdot (-81\,b^3x^2y^2z^2) = -236196\,b^5x^5y^3z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x) \cdot (-3\,x^2 - 4\,x) = 3\,x^3 + 4\,x^2 \\ &[2] \quad (-2\,x) \cdot (3\,x) = -6\,x^2 \\ &[3] \quad (2\,x^2) \cdot (-x^2 - x) = -2\,x^4 - 2\,x^3 \\ &[4] \quad (4\,x^2) \cdot (7\,x^2 + 3\,x) = 28\,x^4 + 12\,x^3 \\ &[5] \quad (x^2) \cdot (6\,x^2 + 2\,x) = 6\,x^4 + 2\,x^3 \\ &[6] \quad (-2\,x) \cdot (2\,x^2 + x) = -4\,x^3 - 2\,x^2 \\ &[7] \quad (-2\,x) \cdot (-6\,x^2 - 2\,x) = 12\,x^3 + 4\,x^2 \\ &[8] \quad (4\,x^2) \cdot (-x^2 + 2\,x) = -4\,x^4 + 8\,x^3 \\ &[9] \quad (-4\,x^2) \cdot (7\,x^2 - x) = -28\,x^4 + 4\,x^3 \\ &[10] \quad (-x) \cdot (-x^2 - 3\,x) = x^3 + 3\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^2 - 4x) \cdot (-3x^2 + x) = 3x^4 + 11x^3 - 4x^2$$

[2] $(4x^2 - x) \cdot (4x^2 + x) = 16x^4 - x^2$
[3] $(-4x^2) \cdot (9x) = -36x^3$
[4] $(x^2 + 2x) \cdot (-2x^2 + 4x) = -2x^4 + 8x^2$
[5] $(3x^2 - 2x) \cdot (-2x^2 + 7x) = -6x^4 + 25x^3 - 14x^2$
[6] $(-2x^2 + 2x) \cdot (-6x^2 + 3x) = 12x^4 - 18x^3 + 6x^2$
[7] $(-5x) \cdot (-3x^2 - x) = 15x^3 + 5x^2$
[8] $(x^2 - 4x) \cdot (3x^2 + 2x) = 3x^4 - 10x^3 - 8x^2$

[9]
$$(2x^2 + 3x) \cdot (3x) = 6x^3 + 9x^2$$

[10]
$$(-2x^2) \cdot (2x^2 - 5x) = -4x^4 + 10x^3$$

[11]
$$(0) \cdot (-7x^2 + 4x) = 0$$

[12]
$$(-3x^2-2x)\cdot(4x^2-x)=-12x^4-5x^3+2x^2$$

[13]
$$(x) \cdot (-4x^2 + 3x) = -4x^3 + 3x^2$$

[14]
$$(x^2 - 3x) \cdot (6x^2 - 4x) = 6x^4 - 22x^3 + 12x^2$$

[15]
$$(5x^2) \cdot (x^2 + 3x) = 5x^4 + 15x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x^3 - 3x^2) \cdot (-3x^3) = -6x^6 + 9x^5$$

[2]
$$(-x^2 - 4x) \cdot (-5x^3 - 3x) = 5x^5 + 20x^4 + 3x^3 + 12x^2$$

[3]
$$(-3x^2) \cdot (-8x^2 + 4x) = 24x^4 - 12x^3$$

[4]
$$(2x^3 - 3x^2 + 2x) \cdot (-x^3 - 4x) = -2x^6 + 3x^5 - 10x^4 + 12x^3 - 8x^2$$

[5]
$$(-4x^3 - 4x) \cdot (10x^3 + 2x) = -40x^6 - 48x^4 - 8x^2$$

[6]
$$(4x^3 - 4x) \cdot (-2x^3 - x) = -8x^6 + 4x^4 + 4x^2$$

[7]
$$(-2x^3 + 7x^2) \cdot (0) = 0$$

[8]
$$(4x^3 - 2x) \cdot (3x^3 + 2x^2) = 12x^6 + 8x^5 - 6x^4 - 4x^3$$

[9]
$$(-2x^3 - 3x^2) \cdot (8x^3 - 2x^2 - x) = -16x^6 - 20x^5 + 8x^4 + 3x^3$$

[10]
$$(-2x^2 - 3x) \cdot (6x^3 - x) = -12x^5 - 18x^4 + 2x^3 + 3x^2$$

[11]
$$(-3x^2 - 3x) \cdot (-3x^3 - 4x^2 - 6x) = 9x^5 + 21x^4 + 30x^3 + 18x^2$$

[12]
$$(2x^2) \cdot (-2x^3 - 3x^2) = -4x^5 - 6x^4$$

[13]
$$(-2x^3 + 2x^2 - x) \cdot (-4x^3 - 3x^2) = 8x^6 - 2x^5 - 2x^4 + 3x^3$$

[14]
$$(0) \cdot (-3x^3 + 3x^2) = 0$$

[15]
$$(3x^3) \cdot (6x^2 + 4x) = 18x^5 + 12x^4$$

[16]
$$(2x^3 - 2x^2 - x) \cdot (-3x^3 - 2x^2) = -6x^6 + 2x^5 + 7x^4 + 2x^3$$

[17]
$$(x^3 + 3x^2) \cdot (-x^3 + 7x^2) = -x^6 + 4x^5 + 21x^4$$

[18]
$$(-x^3 + x) \cdot (-7x^3 + 2x^2) = 7x^6 - 2x^5 - 7x^4 + 2x^3$$

[19]
$$(-2x^3 - 3x) \cdot (4x^3 + 4x^2 - 4x) = -8x^6 - 8x^5 - 4x^4 - 12x^3 + 12x^2$$

[20]
$$(3x^2) \cdot (10x^2 + 4x) = 30x^4 + 12x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2y + xy^2) \cdot (-3x^2y^2 + 2xy^2 - 4xy) = 6x^4y^3 - 3x^3y^4 - 4x^3y^3 + 2x^2y^4 + 8x^3y^2 - 4x^2y^3$$

[2]
$$(-xy^2 - 2xy) \cdot (-x^2y^2 + 2x^2y + 2xy) = x^3y^4 - 4x^3y^2 - 2x^2y^3 - 4x^2y^2$$

[3]
$$(4xy^2 + 2xy) \cdot (-8xy) = -32x^2y^3 - 16x^2y^2$$

[4]
$$(-4x^2y^2 - 4xy^2) \cdot (-4x^2y^2 + 4x^2y + 4xy) = 16x^4y^4 - 16x^4y^3 + 16x^3y^4 - 32x^3y^3 - 16x^2y^3$$

[5]
$$(-3x^2y) \cdot (-4x^2y^2 + xy) = 12x^4y^3 - 3x^3y^2$$

[6]
$$(2x^2y^2 + 2x^2y) \cdot (-5x^2y - 4xy) = -10x^4y^3 - 10x^4y^2 - 8x^3y^3 - 8x^3y^2$$

[7]
$$(-2x^2y^2 + 4xy) \cdot (x^2y^2 + 2x^2y) = -2x^4y^4 - 4x^4y^3 + 4x^3y^3 + 8x^3y^2$$