1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$4x^5 + x^4 - 3x^2 + 4x^4 + 6x^3 + -x^6 + 4x^3 - 4x^2 = -x^6 + 4x^5 + 5x^4 + 10x^3 - 7x^2$$

[2] $-3x^6 + x^5 - 4x^2 + (-2x^6 - x^5) + (-x^4 + 2x^3) = -5x^6 - x^4 + 2x^3 - 4x^2$
[3] $7x^6 + x^5 + 2x^6 + 2x^4 + 4x + 2x^6 - x^3 = 11x^6 + x^5 + 2x^4 - x^3 + 4x$
[4] $3x^6 - 3x^5 - 4x^3 + -2x^6 + 4x^5 - 4x^2 + 4x^6 - 4x^5 + 4x^4 = 5x^6 - 3x^5 + 4x^4 - 4x^3 - 4x^2$
[5] $2x^5 - 4x^3 + x^2 + -8x^6 - x^5 + -x^5 - 4x = -8x^6 - 4x^3 + x^2 - 4x$
[6] $2x^5 - 2x^4 + 3x + -4x^3 - x^2 + 4x + -x^6 + 4x^5 + x^3 = -x^6 + 6x^5 - 2x^4 - 3x^3 - x^2 + 7x$
[7] $3x^6 - 4x^5 - 2x + 2x^2 - 4x + -2x^5 - 3x^2 + x = 3x^6 - 6x^5 - x^2 - 5x$
[8] $4x^6 - x^5 + 4x^2 + 3x^6 - x^2 + 4x + 3x^5 - 3x^4 + 4x = 7x^6 + 2x^5 - 3x^4 + 3x^2 + 8x$
[9] $x^5 + 3x^2 + 5x^6 - 2x^5 + -4x^4 - 3x^2 = 5x^6 - x^5 - 4x^4$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} &[1] \quad 0+0+0=0 \\ &[2] \quad x^2y+xy^2+3\,x^2y^2+4\,x^2y^2-x^2y=7\,x^2y^2+xy^2 \\ &[3] \quad 8\,xy^2+4\,xy+-28\,xy^2+(-2\,xy^2+4\,xy)=-22\,xy^2+8\,xy \\ &[4] \quad 24\,x^2y^2+9\,x^2y+3\,x^2y-12\,xy^2+-30\,xy^2=24\,x^2y^2+12\,x^2y-42\,xy^2 \\ &[5] \quad 64\,x^2y^2+16\,x^2y+48\,xy+-12\,x^2y^2+48\,xy+(-64\,x^2y^2+12\,x^2y-8\,xy)=-12\,x^2y^2+28\,x^2y+88\,xy \\ &[6] \quad 5\,x^2y^2-50\,xy^2+-5\,xy^2-65\,xy+(-175\,x^2y+100\,xy^2)=5\,x^2y^2-175\,x^2y+45\,xy^2-65\,xy \\ &[7] \quad 12\,x^2y^2+6\,x^2y-144\,xy+-18\,xy^2+30\,xy+(-54\,x^2y-108\,xy)=12\,x^2y^2-48\,x^2y-18\,xy^2-222\,xy \\ &[8] \quad 98\,x^2y^2-21\,xy^2-14\,xy+28\,x^2y^2-245\,xy+-98\,x^2y^2+14\,xy^2-147\,xy=28\,x^2y^2-7\,xy^2-406\,xy \\ &[9] \quad 40\,x^2y^2-128\,xy+56\,x^2y^2-16\,x^2y+-16\,x^2y^2-32\,xy^2=80\,x^2y^2-16\,x^2y-32\,xy^2-128\,xy \\ &[10] \quad -405\,x^2y^2-243\,xy^2+(-567\,x^2y^2-18\,x^2y)+(-324\,x^2y-243\,xy^2+324\,xy)=-972\,x^2y^2-342\,x^2y-486\,xy^2+324\,xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

[1]
$$0 - (0) + (0) = 0$$

[2] $-8xy + 3xy^2 - 4xy - (8x^2y^2 - 4xy) = -8x^2y^2 + 3xy^2 - 8xy$
[3] $-12x^2y^2 + 16x^2y^2 - 12x^2y + 4xy^2 - (-8x^2y^2 - 4x^2y + 4xy) = 12x^2y^2 - 8x^2y + 4xy^2 - 4xy$
[4] $-6x^2y + 24xy - (-6x^2y - 24xy^2) + (12x^2y - 48xy^2) = 12x^2y - 24xy^2 + 24xy$
[5] $16x^2y^2 - 16x^2y + 48xy + -48x^2y + 96xy - (16x^2y^2 + 16x^2y - 4xy^2) = -80x^2y + 4xy^2 + 144xy$
[6] $75x^2y^2 + -75x^2y + 95xy - (-50x^2y + 70xy) = 75x^2y^2 - 25x^2y + 25xy$

$$\begin{aligned} &[7] \quad 18\,x^2y^2 - 144\,x^2y - 72\,xy^2 - (6\,x^2y^2 + 24\,xy^2 - 108\,xy) + (90\,x^2y^2 - 24\,xy) = \\ &102\,x^2y^2 - 144\,x^2y - 96\,xy^2 + 84\,xy \\ &[8] \quad -98\,x^2y^2 + 42\,xy^2 + -21\,x^2y + 49\,xy - (-196\,x^2y^2 + 98\,x^2y - 49\,xy^2) = \\ &98\,x^2y^2 - 119\,x^2y + 91\,xy^2 + 49\,xy \\ &[9] \quad 128\,xy^2 + 16\,xy + -192\,x^2y^2 - 64\,x^2y + 32\,xy - (8\,x^2y^2 + 192\,xy^2) = -200\,x^2y^2 - \\ &64\,x^2y - 64\,xy^2 + 48\,xy \\ &[10] \quad -162\,x^2y^2 - 162\,xy^2 + 81\,xy - (36\,x^2y - 27\,xy^2 - 81\,xy) + (-243\,x^2y^2 + 36\,x^2y - 27\,xy^2) = -405\,x^2y^2 - 162\,xy^2 + 162\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

[1]
$$(0) \cdot (0) = 0$$

[2] $(4b^3xy^3z^3) \cdot (b^3x^2y^2z^3) = 4b^6x^3y^5z^6$
[3] $(8b^3x^3y^2z^3) \cdot (-8b^3x^3yz) = -64b^6x^6y^3z^4$
[4] $(-18b^2x^2y^2z) \cdot (108b^3x^2y^3z^3) = -1944b^5x^4y^5z^4$
[5] $(16bx^3yz^2) \cdot (-16bx^3yz^2) = -256b^2x^6y^2z^4$
[6] $(-250b^3x^3y^2z) \cdot (25b^3x^3y^3z^3) = -6250b^6x^6y^5z^4$
[7] $(432bx^3y^3z^3) \cdot (18b^2x^2y^3z^2) = 7776b^3x^5y^6z^5$
[8] $(-28bx^2yz^2) \cdot (686b^3x^2y^3z^3) = -19208b^4x^4y^4z^5$
[9] $(24b^2xyz^2) \cdot (-2048b^3x^2y^2z^3) = -49152b^5x^3y^3z^5$
[10] $(2187bxy^2z^2) \cdot (2187b^2xyz^2) = 4782969b^3x^2y^3z^4$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2) \cdot (-7x) = -7x^3$$

[2] $(-2x^2) \cdot (x^2) = -2x^4$
[3] $(x^2) \cdot (-3x^2 - 2x) = -3x^4 - 2x^3$
[4] $(x) \cdot (4x^2 + 2x) = 4x^3 + 2x^2$
[5] $(2x) \cdot (4x^2 + 4x) = 8x^3 + 8x^2$
[6] $(-3x) \cdot (x^2 + 6x) = -3x^3 - 18x^2$
[7] $(3x) \cdot (-x^2 + 6x) = -3x^3 + 18x^2$
[8] $(x^2) \cdot (x^2 + 8x) = x^4 + 8x^3$
[9] $(2x) \cdot (-3x^2 - 3x) = -6x^3 - 6x^2$
[10] $(-4x) \cdot (-10x^2 - x) = 40x^3 + 4x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2 - 4x) \cdot (x^2 + 4x) = -2x^4 - 12x^3 - 16x^2$$

[2] $(-5x) \cdot (-3x^2 - x) = 15x^3 + 5x^2$
[3] $(6x^2) \cdot (-3x^2 + 2x) = -18x^4 + 12x^3$
[4] $(-4x^2 - x) \cdot (-x^2 + 8x) = 4x^4 - 31x^3 - 8x^2$
[5] $(-4x^2) \cdot (-2x^2 + 2x) = 8x^4 - 8x^3$
[6] $(-3x^2 + 2x) \cdot (x^2 - 3x) = -3x^4 + 11x^3 - 6x^2$
[7] $(0) \cdot (3x) = 0$
[8] $(4x^2) \cdot (-3x) = -12x^3$

[9]
$$(-2x^2 - 4x) \cdot (3x^2 - 8x) = -6x^4 + 4x^3 + 32x^2$$

[10]
$$(x^2 - 3x) \cdot (3x^2 - 3x) = 3x^4 - 12x^3 + 9x^2$$

[11]
$$(x) \cdot (-3x^2 - 6x) = -3x^3 - 6x^2$$

[12]
$$(-x^2 + 4x) \cdot (-3x^2 + 3x) = 3x^4 - 15x^3 + 12x^2$$

[13]
$$(-6x^2) \cdot (3x^2) = -18x^4$$

[14]
$$(-x^2 - 2x) \cdot (2x^2 - 3x) = -2x^4 - x^3 + 6x^2$$

[15]
$$(-x^2 - 2x) \cdot (2x^2 - 2x) = -2x^4 - 2x^3 + 4x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(3x) \cdot (5x^3 - 2x^2) = 15x^4 - 6x^3$$

[2]
$$(-4x^2 - 4x) \cdot (-2x^3 - 6x^2) = 8x^5 + 32x^4 + 24x^3$$

[3]
$$(7x^2) \cdot (-3x^3 + 3x) = -21x^5 + 21x^3$$

[4]
$$(5x^3 + x^2) \cdot (x^3 - 4x^2 - 3x) = 5x^6 - 19x^5 - 19x^4 - 3x^3$$

[5]
$$(3x^2 - 4x) \cdot (-5x^3 + 2x^2 + 2x) = -15x^5 + 26x^4 - 2x^3 - 8x^2$$

[6]
$$(-x^3 - x) \cdot (2x^3 + 5x) = -2x^6 - 7x^4 - 5x^2$$

[7]
$$(-x^3 - 8x^2) \cdot (-3x^2 + 3x) = 3x^5 + 21x^4 - 24x^3$$

[8]
$$(-2x^2 - 2x) \cdot (x^3 - 3x) = -2x^5 - 2x^4 + 6x^3 + 6x^2$$

[9]
$$(-x^3 + 2x) \cdot (x^3 - 4x) = -x^6 + 6x^4 - 8x^2$$

[10]
$$(x^3 - 2x^2 - 3x) \cdot (-2x^3 - 2x) = -2x^6 + 4x^5 + 4x^4 + 4x^3 + 6x^2$$

[11]
$$(-2x^3 + 3x^2) \cdot (-3x^3 + 4x^2 + 3x) = 6x^6 - 17x^5 + 6x^4 + 9x^3$$

[12]
$$(-4x^3 - 3x) \cdot (4x^3 + 2x^2 - x) = -16x^6 - 8x^5 - 8x^4 - 6x^3 + 3x^2$$

[13]
$$(-2x^3 - 2x^2 + 4x) \cdot (-2x^2 + 3x) = 4x^5 - 2x^4 - 14x^3 + 12x^2$$

[14]
$$(-x^3 - 4x^2) \cdot (4x^3 - x^2 + 4x) = -4x^6 - 15x^5 - 16x^3$$

[15]
$$(-3x^2 + 3x) \cdot (8x^3 - 4x) = -24x^5 + 24x^4 + 12x^3 - 12x^2$$

[16]
$$(4x^3 - 3x) \cdot (-7x^2) = -28x^5 + 21x^3$$

[17]
$$(-3x^3) \cdot (5x^3 - x^2 - x) = -15x^6 + 3x^5 + 3x^4$$

[18]
$$(0) \cdot (-2x^3 + 2x) = 0$$

[19]
$$(x^2 + 2x) \cdot (-3x^3) = -3x^5 - 6x^4$$

[20]
$$(3x^3 - 3x) \cdot (2x^3 - x^2 - 2x) = 6x^6 - 3x^5 - 12x^4 + 3x^3 + 6x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^2y^2 + 4xy) \cdot (-x^2y - 3xy^2 - 4xy) = 3x^4y^3 + 9x^3y^4 + 12x^3y^3 - 4x^3y^2 - 12x^2y^3 - 16x^2y^2$$

[2]
$$(2x^2y^2 + xy) \cdot (4x^2y^2 + xy^2 - 3xy) = 8x^4y^4 + 2x^3y^4 - 2x^3y^3 + x^2y^3 - 3x^2y^2$$

[3]
$$(-5x^2y^2) \cdot (-3x^2y^2 + 2xy^2 + xy) = 15x^4y^4 - 10x^3y^4 - 5x^3y^3$$

$$[4] \quad (-3\,x^2y^2-x^2y)\cdot(2\,x^2y^2-4\,x^2y-xy) = -6\,x^4y^4+10\,x^4y^3+4\,x^4y^2+3\,x^3y^3+x^3y^2+2\,x^3y^2+3\,x^3y^3+2\,x^3y^2+2\,x^3y^3$$

[5]
$$(-2x^2y^2 + 4xy) \cdot (2x^2y + 4xy^2 + 4xy) = -4x^4y^3 - 8x^3y^4 - 8x^3y^3 + 8x^3y^2 + 16x^2y^3 + 16x^2y^2$$

[6]
$$(6x^2y) \cdot (x^2y + 5xy) = 6x^4y^2 + 30x^3y^2$$

[7]
$$(-5xy) \cdot (-2x^2y) = 10x^3y^2$$