1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$-x^4 - 2x^2 + (-2x^2) + (-3x^6 - x^3 + x) = -3x^6 - x^4 - x^3 - 4x^2 + x$$

[2] $3x^5 - 3x + -7x^6 + 4x + -x^5 - x^4 = -7x^6 + 2x^5 - x^4 + x$
[3] $2x^5 - 4x^4 + 2x^2 + -3x^6 + x^4 + (-4x^6 - 2x^5 - x^3) = -7x^6 - 3x^4 - x^3 + 2x^2$
[4] $x^6 + 2x^5 - 3x^2 + 4x^3 - 5x + -x^6 - x^2 + 3x = 2x^5 + 4x^3 - 4x^2 - 2x$
[5] $4x^2 + -x^4 + 2x^2 - 2x + 3x^5 + 2x^3 = 3x^5 - x^4 + 2x^3 + 6x^2 - 2x$
[6] $4x^5 + x^4 + x^2 + -x^6 - 2x + (-3x^6 + 4x^2 - 3x) = -4x^6 + 4x^5 + x^4 + 5x^2 - 5x$
[7] $x^5 + 4x^4 + 4x + -4x^5 + x^4 + 4x^5 + 2x^3 - 4x = x^5 + 5x^4 + 2x^3$
[8] $-6x^4 - 3x^2 + (-3x^6 + x^3) + (-3x^4 - 3x^2) = -3x^6 - 9x^4 + x^3 - 6x^2$
[9] $4x^6 - 4x^3 + x + -2x^6 + 4x^4 - 3x^2 + (-3x^5 - 4x^4) = 2x^6 - 3x^5 - 4x^3 - 3x^2 + x$
[10] $3x^6 + 3x^5 - 4x^3 + -3x^3 + x + (-x^4 - 2x^3 - 4x) = 3x^6 + 3x^5 - x^4 - 9x^3 - 3x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0 + 0 + 0 = 0 \\ & [2] \quad -7 \, x^2 y + xy + (-8 \, x^2 y^2 + x^2 y) + (-4 \, x^2 y) = -8 \, x^2 y^2 - 10 \, x^2 y + xy \\ & [3] \quad 2 \, x^2 y^2 + 4 \, xy^2 - 16 \, xy + -10 \, x^2 y - 2 \, xy^2 + -6 \, x^2 y^2 - 2 \, x^2 y + 8 \, xy = -4 \, x^2 y^2 - 12 \, x^2 y + 2 \, xy^2 - 8 \, xy \\ & [4] \quad 9 \, x^2 y^2 - 36 \, xy + -72 \, x^2 y - 18 \, xy + 9 \, x^2 y + 9 \, xy^2 + 27 \, xy = 9 \, x^2 y^2 - 63 \, x^2 y + 9 \, xy^2 - 27 \, xy \\ & [5] \quad 48 \, x^2 y^2 - 48 \, x^2 y - 16 \, xy^2 + -4 \, xy^2 + 24 \, xy + 4 \, x^2 y^2 - 76 \, x^2 y = 52 \, x^2 y^2 - 124 \, x^2 y - 20 \, xy^2 + 24 \, xy \\ & [6] \quad -20 \, x^2 y^2 + 5 \, x^2 y - 100 \, xy + (-5 \, x^2 y^2 + 15 \, xy^2 + 50 \, xy) + (-25 \, x^2 y^2 - 75 \, xy^2 + 50 \, xy) = -50 \, x^2 y^2 + 5 \, x^2 y - 60 \, xy^2 \\ & [7] \quad -6 \, x^2 y - 18 \, xy^2 + 6 \, xy + (-72 \, x^2 y^2 - 84 \, xy) + (-144 \, x^2 y^2 + 12 \, xy^2) = -216 \, x^2 y^2 - 6 \, x^2 y - 6 \, xy^2 - 78 \, xy \\ & [8] \quad 28 \, x^2 y + 21 \, xy^2 - 147 \, xy + -14 \, x^2 y + 294 \, xy + (-147 \, x^2 y^2 - 21 \, x^2 y - 147 \, xy) = -147 \, x^2 y^2 - 7 \, x^2 y + 21 \, xy^2 \\ & [9] \quad 16 \, x^2 y - 8 \, xy^2 - 192 \, xy + 72 \, x^2 y^2 + 128 \, xy^2 + 64 \, x^2 y - 128 \, xy^2 - 128 \, xy = 72 \, x^2 y^2 + 80 \, x^2 y - 8 \, xy^2 - 320 \, xy \\ & [10] \quad 162 \, x^2 y^2 - 36 \, x^2 y - 36 \, xy + -171 \, x^2 y + 27 \, x^2 y - 333 \, xy = 162 \, x^2 y^2 - 180 \, x^2 y - 369 \, xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 4\,x^2y^2 - 2\,xy^2 - xy + x^2y^2 + 2\,x^2y + 2\,xy - (3\,x^2y) = 5\,x^2y^2 - x^2y - 2\,xy^2 + xy \\ &[3] \quad -4\,x^2y \, + \,12\,xy^2 \, + \,2\,xy \, + \, -8\,x^2y \, - \,4\,xy^2 \, - \,2\,xy \, - \,(12\,x^2y^2 \, - \,12\,xy^2) \, = \\ &-12\,x^2y^2 - 12\,x^2y + 20\,xy^2 \\ &[4] \quad 9\,x^2y^2 \, - \,27\,xy^2 \, - \,36\,xy \, - \,(-9\,x^2y^2 \, + \,9\,xy^2) \, + \,(9\,x^2y \, - \,27\,xy^2 \, + \,6\,xy) \, = \\ &18\,x^2y^2 \, + \,9\,x^2y \, - \,63\,xy^2 \, - \,30\,xy \\ &[5] \quad -48\,x^2y \, - \,16\,xy^2 \, + \,32\,xy \, + \,56\,x^2y^2 \, - \,(-16\,x^2y \, - \,32\,xy^2 \, + \,64\,xy) \, = \,56\,x^2y^2 \, - \\ &32\,x^2y \, + \,16\,xy^2 \, - \,32\,xy \end{aligned}$$

$$[6] \quad -20\,x^2y^2 + 75\,x^2y - 100\,xy^2 + -200\,x^2y^2 + 100\,x^2y - (30\,xy^2 + 20\,xy) = \\ -220\,x^2y^2 + 175\,x^2y - 130\,xy^2 - 20\,xy \\ [7] \quad 36\,x^2y + 36\,xy^2 - (-150\,x^2y^2 + 144\,xy) + (-72\,x^2y^2 + 144\,x^2y + 6\,xy^2) = \\ 78\,x^2y^2 + 180\,x^2y + 42\,xy^2 - 144\,xy \\ [8] \quad -28\,x^2y + 49\,xy^2 + 49\,xy + -49\,x^2y^2 - 224\,xy^2 - (21\,x^2y + 28\,xy) = -49\,x^2y^2 - 49\,x^2y - 175\,xy^2 + 21\,xy \\ [9] \quad -24\,xy^2 + 24\,xy + -8\,x^2y^2 - 64\,x^2y + 128\,xy^2 - (-24\,xy^2 + 24\,xy) = \\ -8\,x^2y^2 - 64\,x^2y + 128\,xy^2 - 472\,xy \\ [10] \quad 18\,x^2y^2 + 81\,x^2y + 36\,xy - (27\,x^2y + 252\,xy^2) + (-36\,x^2y^2 + 324\,xy^2 + 162\,xy) = \\ -18\,x^2y^2 + 54\,x^2y + 72\,xy^2 + 198\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{array}{lll} [1] & (0) \cdot (0) = 0 \\ [2] & (2\,b^2x^2y^2z^2) \cdot (-2\,bx^3yz) = -4\,b^3x^5y^3z^3 \\ [3] & (-12\,b^2xy^3z^3) \cdot (-4\,b^2x^2y^3z^2) = 48\,b^4x^3y^6z^5 \\ [4] & (-6\,b^3xyz) \cdot (-12\,bx^2y^3z^3) = 72\,b^4x^3y^4z^4 \\ [5] & (128\,b^2xy^2z) \cdot (8\,bxy^2z^2) = 1024\,b^3x^2y^4z^3 \\ [6] & (-100\,bx^3y^2z) \cdot (-500\,b^3xy^3z^2) = 50000\,b^4x^4y^5z^3 \\ [7] & (864\,b^3x^3y^2z^2) \cdot (72\,b^3x^2y^2z) = 62208\,b^6x^5y^4z^3 \\ [8] & (14\,bxy^2z^2) \cdot (98\,b^2x^3yz) = 1372\,b^3x^4y^3z^3 \\ [9] & (-128\,b^3x^3yz^2) \cdot (-16\,bx^2y^2z) = 2048\,b^4x^5y^3z^3 \\ [10] & (243\,b^3x^2yz^2) \cdot (-81\,bx^2y^3z^3) = -19683\,b^4x^4y^4z^5 \end{array}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x^2) \cdot (3\,x^2 + 4\,x) = -6\,x^4 - 8\,x^3 \\ &[2] \quad (-4\,x) \cdot (-2\,x^2 - x) = 8\,x^3 + 4\,x^2 \\ &[3] \quad (-4\,x) \cdot (-x^2) = 4\,x^3 \\ &[4] \quad (2\,x) \cdot (-5\,x^2 + 4\,x) = -10\,x^3 + 8\,x^2 \\ &[5] \quad (4\,x^2) \cdot (-2\,x^2 + 4\,x) = -8\,x^4 + 16\,x^3 \\ &[6] \quad (-3\,x^2) \cdot (-4\,x^2 - 2\,x) = 12\,x^4 + 6\,x^3 \\ &[7] \quad (2\,x^2) \cdot (-3\,x^2 + 3\,x) = -6\,x^4 + 6\,x^3 \\ &[8] \quad (x) \cdot (-3\,x^2 - 4\,x) = -3\,x^3 - 4\,x^2 \\ &[9] \quad (-3\,x^2) \cdot (x^2 + 5\,x) = -3\,x^4 - 15\,x^3 \\ &[10] \quad (-x) \cdot (x^2 + 3\,x) = -x^3 - 3\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(5x^2) \cdot (2x^2) = 10x^4$$

[2] $(-x^2 - 3x) \cdot (-3x) = 3x^3 + 9x^2$
[3] $(0) \cdot (2x^2 - 4x) = 0$
[4] $(6x^2) \cdot (-x^2 - 6x) = -6x^4 - 36x^3$
[5] $(-2x^2 - x) \cdot (4x) = -8x^3 - 4x^2$
[6] $(-5x^2) \cdot (-2x^2 + 4x) = 10x^4 - 20x^3$

[7]
$$(-x^2 - 4x) \cdot (2x) = -2x^3 - 8x^2$$

[8]
$$(6x^2) \cdot (x^2) = 6x^4$$

[9]
$$(-2x^2 - 4x) \cdot (-x^2 + 4x) = 2x^4 - 4x^3 - 16x^2$$

[10]
$$(-x) \cdot (-x^2) = x^3$$

[11]
$$(-5x) \cdot (-2x) = 10x^2$$

[12]
$$(-x^2 + x) \cdot (3x^2 + 6x) = -3x^4 - 3x^3 + 6x^2$$

[13]
$$(3x^2 + 4x) \cdot (-x^2 + 6x) = -3x^4 + 14x^3 + 24x^2$$

[14]
$$(2x^2) \cdot (x^2 + 7x) = 2x^4 + 14x^3$$

[15]
$$(x^2) \cdot (4x^2 + 5x) = 4x^4 + 5x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x) \cdot (-x^3 + 5x) = -x^4 + 5x^2$$

[2]
$$(4x^2 + 3x) \cdot (7x^3 - x^2 + 2x) = 28x^5 + 17x^4 + 5x^3 + 6x^2$$

[3]
$$(2x^3 - 2x) \cdot (-2x^3 + x^2 + 2x) = -4x^6 + 2x^5 + 8x^4 - 2x^3 - 4x^2$$

[4]
$$(-3x^3 + 4x^2) \cdot (x^3 - x) = -3x^6 + 4x^5 + 3x^4 - 4x^3$$

[5]
$$(-2x^3) \cdot (-x^3 - 4x^2) = 2x^6 + 8x^5$$

[6]
$$(-2x^3 + 4x) \cdot (-3x^3 - x^2) = 6x^6 + 2x^5 - 12x^4 - 4x^3$$

[7]
$$(3x^3 + 2x^2 + 3x) \cdot (-3x^3 + 3x^2 + 4x) = -9x^6 + 3x^5 + 9x^4 + 17x^3 + 12x^2$$

[8]
$$(-2x^3 + x^2) \cdot (6x^3 - 3x^2) = -12x^6 + 12x^5 - 3x^4$$

[9]
$$(-3x^2) \cdot (5x^3 - 4x) = -15x^5 + 12x^3$$

[10]
$$(-2x^3 - 2x^2 + 3x) \cdot (-5x^2 + 2x) = 10x^5 + 6x^4 - 19x^3 + 6x^2$$

[11]
$$(4x^3 - 3x^2) \cdot (-2x^3) = -8x^6 + 6x^5$$

[12]
$$(-4x^3 + 4x^2) \cdot (x^3 + x^2) = -4x^6 + 4x^4$$

[13]
$$(3x^3 - x^2) \cdot (-x^3 + x^2 + 2x) = -3x^6 + 4x^5 + 5x^4 - 2x^3$$

[14]
$$(4x^2 + 3x) \cdot (-2x^3 - 5x) = -8x^5 - 6x^4 - 20x^3 - 15x^2$$

[15]
$$(2x^3 - 2x) \cdot (-4x^3 + x^2) = -8x^6 + 2x^5 + 8x^4 - 2x^3$$

[16]
$$(-4x) \cdot (3x^3 + 3x) = -12x^4 - 12x^2$$

[17]
$$(2x^2 + 4x) \cdot (3x^3 - x^2 + x) = 6x^5 + 10x^4 - 2x^3 + 4x^2$$

[18]
$$(-x^2 + 2x) \cdot (5x^2) = -5x^4 + 10x^3$$

[19]
$$(2x^3 + 2x) \cdot (-3x^3 - 2x^2 + 2x) = -6x^6 - 4x^5 - 2x^4 - 4x^3 + 4x^2$$

[20]
$$(-x) \cdot (-3x^3 - 4x) = 3x^4 + 4x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-4xy^2 + 3xy) \cdot (4x^2y^2 + x^2y) = -16x^3y^4 + 8x^3y^3 + 3x^3y^2$$

[2]
$$(4x^2y^2 - 3xy^2) \cdot (-3x^2y^2 - 3x^2y + xy^2) = -12x^4y^4 - 12x^4y^3 + 13x^3y^4 + 9x^3y^3 - 3x^2y^4$$

[3]
$$(xy^2 - xy) \cdot (4x^2y - xy^2 + 4xy) = 4x^3y^3 - x^2y^4 - 4x^3y^2 + 5x^2y^3 - 4x^2y^2$$

[4]
$$(2xy^2 - 3xy) \cdot (-3x^2y^2 - 2xy^2 - 3xy) = -6x^3y^4 + 9x^3y^3 - 4x^2y^4 + 9x^2y^2$$

[5]
$$(-4xy^2 + 4xy) \cdot (-x^2y^2 + x^2y - 4xy^2) = 4x^3y^4 - 8x^3y^3 + 16x^2y^4 + 4x^3y^2 - 16x^2y^3$$

[6]
$$(-4x^2y^2 + 2xy) \cdot (-3x^2y + 2xy) = 12x^4y^3 - 8x^3y^3 - 6x^3y^2 + 4x^2y^2$$

[7]
$$(-3x^2y - 3xy) \cdot (-5x^2y^2 - xy^2) = 15x^4y^3 + 18x^3y^3 + 3x^2y^3$$