## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad -2\,x^6 - 4\,x^4 + 2\,x^2 + (-x^6 - 4\,x^3 - 2\,x^2) + (-4\,x^5 - 2\,x^3 + 4\,x) = -3\,x^6 - 4\,x^5 - 4\,x^4 - 6\,x^3 + 4\,x$$

$$[2] \quad 4\,x^6 + 4\,x^4 - 2\,x^3 + -4\,x^6 - 7\,x^3 + 4\,x^6 + 4\,x^5 - 2\,x^3 = 4\,x^6 + 4\,x^5 + 4\,x^4 - 11\,x^3$$

$$[3] \quad -4\,x^5 + (-2\,x^5 - 2\,x^3) + (-2\,x^5 + x^3 - 2\,x) = -8\,x^5 - x^3 - 2\,x$$

$$[4] \quad 3\,x^5 - x^3 + -5\,x^2 - x + -7\,x^5 - 2\,x^2 = -4\,x^5 - x^3 - 7\,x^2 - x$$

$$[5] \quad 2\,x^2 + -2\,x^6 + 4\,x^5 - x^4 + (-3\,x^6 + 3\,x^2 + x) = -5\,x^6 + 4\,x^5 - x^4 + 5\,x^2 + x$$

$$[6] \quad -3\,x^6 - 2\,x^5 + 3\,x^2 + (-4\,x^4) + (-x^5 + 5\,x) = -3\,x^6 - 3\,x^5 - 4\,x^4 + 3\,x^2 + 5\,x$$

$$[7] \quad 2\,x^6 - x^4 + x^3 + 2\,x^5 - 2\,x^4 - 3\,x^2 + -3\,x^5 + 2\,x^4 - 4\,x = 2\,x^6 - x^5 - x^4 + x^3 - 3\,x^2 - 4\,x$$

$$[8] \quad x^2 + 2\,x + x^6 - x^5 - 2\,x^4 + -3\,x^4 - 4\,x^2 + 4\,x = x^6 - x^5 - 5\,x^4 - 3\,x^2 + 6\,x$$

$$[9] \quad x^5 + 2\,x^3 - x^2 + -8\,x^5 - 3\,x^3 - 3\,x + 3\,x^5 - x^2 + 4\,x = -10\,x^5 - x^3 - 2\,x^2 + 4\,x$$

$$[10] \quad 2\,x^6 - x^4 + -x^5 - 3\,x^3 - 3\,x + 3\,x^5 - 4\,x^4 - 3\,x^3 = 2\,x^6 + 2\,x^5 - 5\,x^4 - 6\,x^3 - 3\,x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 2x^2y^2-3x^2y+3xy^2+-x^2y^2+3x^2y+2xy+(-3x^2y-5xy^2)=x^2y^2-3x^2y-2xy^2+2xy \\ [3] \quad 10x^2y^2+2x^2y+-12x^2y^2+8x^2y+2xy+-4x^2y^2-8xy^2-4xy=-6x^2y^2+10x^2y-8xy^2-2xy \\ [4] \quad 27x^2y+3x^2y^2-18x^2y-27xy+-18xy^2-6xy=3x^2y^2+9x^2y-18xy^2-33xy \\ [5] \quad -4x^2y^2+12x^2y+(-4x^2y^2-4x^2y-16xy^2)+(-128x^2y^2+48xy^2)=-136x^2y^2+8x^2y+32xy^2 \\ [6] \quad 60x^2y^2-5x^2y+5x^2y-40xy+10x^2y+25xy^2+100xy=60x^2y^2+10x^2y+25xy^2+60xy \\ [7] \quad 12x^2y^2+36x^2y-36xy+108x^2y+18xy^2-144xy+-30x^2y-24xy^2=12x^2y^2+114x^2y-6xy^2-180xy \\ [8] \quad 308xy+-49x^2y+-28x^2y^2+28x^2y-196xy^2=-28x^2y^2-21x^2y-196xy^2+308xy \\ [9] \quad 40x^2y^2-8xy+-384x^2y+32xy^2+(-128x^2y^2+8xy^2)=-88x^2y^2-384x^2y+40xy^2-8xy \\ [10] \quad 261xy^2+-27xy^2+360xy+-9x^2y^2+9x^2y+18xy=-9x^2y^2+9x^2y+234xy^2+378xy \\ [10] \quad 261xy^2+2xy^2+360xy+-9x^2y^2+9x^2y+18xy=-9x^2y^2+9x^2y+234xy^2+18xy+2xy^2+378xy \\ [10] \quad 261xy^2+2$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -7\,x^2y^2 - 2\,xy^2 + -x^2y^2 + 2\,xy - (-x^2y^2 - x^2y) = -7\,x^2y^2 + x^2y - 2\,xy^2 + 2\,xy \\ &[3] \quad 4\,x^2y^2 + 12\,x^2y + 8\,xy + 8\,x^2y^2 + 12\,x^2y + 4\,xy - (4\,x^2y^2 - 6\,xy^2 - 4\,xy) = 8\,x^2y^2 + 24\,x^2y + 6\,xy^2 + 16\,xy \\ &[4] \quad -9\,x^2y - 12\,xy - (-33\,x^2y^2 - 27\,xy^2) + (-24\,x^2y^2 + 36\,xy) = 9\,x^2y^2 - 9\,x^2y + 27\,xy^2 + 24\,xy \end{aligned}$$

$$[5] \quad -12\,x^2y - 80\,xy + -16\,xy^2 + 4\,xy - (-48\,xy^2 + 16\,xy) = -12\,x^2y + 32\,xy^2 - 92\,xy$$

$$[6] \quad -25\,x^2y - 10\,xy^2 - 100\,xy + -50\,x^2y^2 + 20\,xy^2 - 5\,xy - (10\,xy^2 + 25\,xy) = -50\,x^2y^2 - 25\,x^2y - 130\,xy$$

$$[7] \quad -18\,x^2y^2 + 18\,xy - (-18\,x^2y^2 - 36\,x^2y - 108\,xy) + (72\,x^2y^2 + 18\,xy) = 72\,x^2y^2 + 36\,x^2y + 144\,xy$$

$$[8] \quad 49\,x^2y^2 + 28\,x^2y - 28\,xy + -196\,x^2y - (7\,x^2y^2 + 21\,x^2y + 28\,xy^2) = 42\,x^2y^2 - 189\,x^2y - 28\,xy^2 - 28\,xy$$

$$[9] \quad -192\,x^2y - 192\,xy^2 + -8\,x^2y^2 + 64\,x^2y + 8\,xy - (-152\,xy) = -8\,x^2y^2 - 128\,x^2y - 192\,xy^2 + 160\,xy$$

$$[10] \quad -567\,xy^2 - (-81\,x^2y - 324\,xy^2 - 243\,xy) + (324\,x^2y - 261\,xy) = 405\,x^2y - 243\,xy^2 - 18\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (4\,b^3x^2y^3z) \cdot (3\,bx^3y^3z) = 12\,b^4x^5y^6z^2 \\ &[3] \quad (32\,b^2x^3y^2z) \cdot (-8\,b^3x^3yz^2) = -256\,b^5x^6y^3z^3 \\ &[4] \quad (27\,b^3x^2yz^3) \cdot (108\,bx^3y^3z) = 2916\,b^4x^5y^4z^4 \\ &[5] \quad (16\,b^3xy^2z^3) \cdot (192\,bx^2y^3z^2) = 3072\,b^4x^3y^5z^5 \\ &[6] \quad (75\,bx^2y^2z) \cdot (-75\,b^2x^2y^3z^3) = -5625\,b^3x^4y^5z^4 \\ &[7] \quad (-12\,bx^3yz^3) \cdot (-864\,b^3x^3yz^2) = 10368\,b^4x^6y^2z^5 \\ &[8] \quad (-343\,b^3x^2y^3z^2) \cdot (-1372\,b^3xy^3z^3) = 470596\,b^6x^3y^6z^5 \\ &[9] \quad (-1536\,b^2x^3y^3z^3) \cdot (8\,b^3x^2yz^2) = -12288\,b^5x^5y^4z^5 \\ &[10] \quad (324\,b^2xyz) \cdot (-18\,bx^3y^2z^2) = -5832\,b^3x^4y^3z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-4x) \cdot (-2x) = 8x^2$$
  
[2]  $(-2x) \cdot (5x) = -10x^2$   
[3]  $(-2x^2) \cdot (-3x^2 - 3x) = 6x^4 + 6x^3$   
[4]  $(-4x) \cdot (7x^2 - 4x) = -28x^3 + 16x^2$   
[5]  $(2x) \cdot (-8x^2) = -16x^3$   
[6]  $(-2x) \cdot (-x) = 2x^2$   
[7]  $(-4x) \cdot (-6x) = 24x^2$   
[8]  $(4x) \cdot (-2x^2 + 2x) = -8x^3 + 8x^2$   
[9]  $(-2x^2) \cdot (-x^2 + 4x) = 2x^4 - 8x^3$   
[10]  $(x) \cdot (-4x^2 - 5x) = -4x^3 - 5x^2$ 

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(2x^2 + 2x) \cdot (6x^2 + 2x) = 12x^4 + 16x^3 + 4x^2$$
  
[2]  $(3x^2 - 2x) \cdot (4x^2 - 2x) = 12x^4 - 14x^3 + 4x^2$   
[3]  $(6x^2) \cdot (x) = 6x^3$   
[4]  $(2x) \cdot (-5x^2 + 3x) = -10x^3 + 6x^2$   
[5]  $(-3x) \cdot (-4x^2) = 12x^3$ 

[6] 
$$(4x^2 + x) \cdot (-x^2) = -4x^4 - x^3$$

[7] 
$$(-3x^2 - x) \cdot (x^2 + 2x) = -3x^4 - 7x^3 - 2x^2$$

[8] 
$$(4x^2 - 3x) \cdot (4x^2 + 2x) = 16x^4 - 4x^3 - 6x^2$$

[9] 
$$(-2x^2 + 2x) \cdot (2x^2 + 8x) = -4x^4 - 12x^3 + 16x^2$$

[10] 
$$(5x^2) \cdot (x^2) = 5x^4$$

[11] 
$$(-4x^2 - 3x) \cdot (-4x^2 - 6x) = 16x^4 + 36x^3 + 18x^2$$

[12] 
$$(x^2 - 4x) \cdot (x^2 - x) = x^4 - 5x^3 + 4x^2$$

[13] 
$$(5x^2) \cdot (-4x^2 - x) = -20x^4 - 5x^3$$

[14] 
$$(3x^2 + 2x) \cdot (-9x^2) = -27x^4 - 18x^3$$

[15] 
$$(0) \cdot (x^2 + 8x) = 0$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-x^3 - 4x^2 + 3x) \cdot (3x^3) = -3x^6 - 12x^5 + 9x^4$$

[2] 
$$(4x^3 + 3x) \cdot (5x^3 - 4x) = 20x^6 - x^4 - 12x^2$$

[3] 
$$(3x^3 + 2x) \cdot (6x^2 - 3x) = 18x^5 - 9x^4 + 12x^3 - 6x^2$$

[4] 
$$(2x^2 - 3x) \cdot (-x^3) = -2x^5 + 3x^4$$

[5] 
$$(-3x^3 + x) \cdot (-7x^2 - 4x) = 21x^5 + 12x^4 - 7x^3 - 4x^2$$

[6] 
$$(-6x) \cdot (x^3 + 3x) = -6x^4 - 18x^2$$

[7] 
$$(2x^2 - x) \cdot (4x^3) = 8x^5 - 4x^4$$

[8] 
$$(-4x^3 - 2x) \cdot (3x^3 + x^2 - 3x) = -12x^6 - 4x^5 + 6x^4 - 2x^3 + 6x^2$$

[9] 
$$(3x^3 + x) \cdot (x^3 + 6x^2 - 2x) = 3x^6 + 18x^5 - 5x^4 + 6x^3 - 2x^2$$

[10] 
$$(4x^3 + 4x^2) \cdot (3x^2) = 12x^5 + 12x^4$$

[11] 
$$(-x^3) \cdot (-3x^3 + 4x^2) = 3x^6 - 4x^5$$

[12] 
$$(-8x^3) \cdot (3x^3 - 4x^2) = -24x^6 + 32x^5$$

[13] 
$$(-2x^3 - 4x^2 - 3x) \cdot (-3x^3 - 3x^2) = 6x^6 + 18x^5 + 21x^4 + 9x^3$$

[14] 
$$(-3x^2 + 2x) \cdot (-6x^3 - 2x) = 18x^5 - 12x^4 + 6x^3 - 4x^2$$

[15] 
$$(-x^3 + 2x) \cdot (-3x^3 + x^2) = 3x^6 - x^5 - 6x^4 + 2x^3$$

[16] 
$$(-6x^2 + 4x) \cdot (x^2) = -6x^4 + 4x^3$$

[17] 
$$(-x^2 + x) \cdot (x^3) = -x^5 + x^4$$

[18] 
$$(2x^2 - 2x) \cdot (x^3 - 4x^2 + 2x) = 2x^5 - 10x^4 + 12x^3 - 4x^2$$

[19] 
$$(-5x^3 - 3x) \cdot (-4x^2 - 6x) = 20x^5 + 30x^4 + 12x^3 + 18x^2$$

[20] 
$$(-x^2) \cdot (5x^3 - 3x^2 + x) = -5x^5 + 3x^4 - x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(2x^2y^2 + 2xy) \cdot (-5xy) = -10x^3y^3 - 10x^2y^2$$

[2] 
$$(-4x^2y^2 + 2x^2y) \cdot (x^2y^2) = -4x^4y^4 + 2x^4y^3$$

[3] 
$$(-3x^2y^2 + x^2y) \cdot (-xy^2 - 2xy) = 3x^3y^4 + 5x^3y^3 - 2x^3y^2$$

[4] 
$$(-x^2y-2xy)\cdot(3x^2y^2-3x^2y-xy) = -3x^4y^3+3x^4y^2-6x^3y^3+7x^3y^2+2x^2y^2$$

[5] 
$$(x^2y - 3xy^2) \cdot (-3x^2y^2 + xy^2 - 2xy) = -3x^4y^3 + 9x^3y^4 + x^3y^3 - 3x^2y^4 - 2x^3y^2 + 6x^2y^3$$

[6] 
$$(-3x^2y^2 - 2xy^2) \cdot (-x^2y) = 3x^4y^3 + 2x^3y^3$$

[7] 
$$(2x^2y) \cdot (2x^2y - 3xy^2) = 4x^4y^2 - 6x^3y^3$$