## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 3\,x^4 + 4\,x^3 + -2\,x^4 + 3\,x^3 + 4\,x + 2\,x^5 + 3\,x = 2\,x^5 + x^4 + 7\,x^3 + 7\,x \\ [2] \quad 3\,x^5 + 2\,x^4 + 2\,x^3 + -4\,x^4 + 5\,x^2 + -5\,x^6 + 4\,x^4 = -5\,x^6 + 3\,x^5 + 2\,x^4 + 2\,x^3 + 5\,x^2 \\ [3] \quad 2\,x^4 + 2\,x^3 + 3\,x + -2\,x^5 + x^4 - 4\,x + 2\,x^5 - 2\,x^4 - 2\,x^2 = x^4 + 2\,x^3 - 2\,x^2 - x \\ [4] \quad 2\,x^6 + 4\,x^5 + 2\,x^4 - x^2 - 2\,x + -4\,x^6 - 4\,x^4 + 4\,x^3 = -2\,x^6 + 4\,x^5 - 2\,x^4 + 4\,x^3 - x^2 - 2\,x \\ [5] \quad 3\,x^6 - 2\,x^3 + -3\,x^5 - 2\,x^3 + 2\,x + 3\,x^3 + x^2 = 3\,x^6 - 3\,x^5 - x^3 + x^2 + 2\,x \\ [6] \quad x^6 + 5\,x^4 + -x^5 - 4\,x^3 - x^2 + 6\,x^5 + 4\,x^2 = x^6 + 5\,x^5 + 5\,x^4 - 4\,x^3 + 3\,x^2 \\ [7] \quad -2\,x^5 - 6\,x^4 + (-3\,x^5 + 2\,x^3 - x) + (-x^4) = -5\,x^5 - 7\,x^4 + 2\,x^3 - x \\ [8] \quad 2\,x^5 - 2\,x^4 + x^2 + 2\,x^6 + 5\,x^4 + -2\,x^5 + x^4 - 4\,x = 2\,x^6 + 4\,x^4 + x^2 - 4\,x \\ [9] \quad 4\,x^5 - 4\,x^4 - 3\,x + -4\,x^6 - x^3 + -x^4 + 4\,x^2 + x = -4\,x^6 + 4\,x^5 - 5\,x^4 - x^3 + 4\,x^2 - 2\,x \\ [10] \quad 6\,x^5 + x^3 + -2\,x^5 + x^4 - 4\,x^3 + 4\,x^5 - 4\,x^4 - 3\,x^3 = 8\,x^5 - 3\,x^4 - 6\,x^3 \\ \end{cases}$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0 + 0 + 0 = 0 \\ & [2] \quad x^2y^2 + x^2y + 4\,x^2y^2 - 4\,x^2y + 2\,xy^2 + -4\,x^2y - 4\,xy^2 - 2\,xy = 5\,x^2y^2 - 7\,x^2y - 2\,xy^2 - 2\,xy \\ & [3] \quad 4\,x^2y^2 + 16\,x^2y \, + \, -16\,x^2y \, - \,4\,xy^2 \, - \,4\,xy \, + \, (-16\,x^2y^2 \, + \,2\,xy^2 \, - \,8\,xy) \, = \\ & -12\,x^2y^2 - 2\,xy^2 - 12\,xy \\ & [4] \quad 6\,x^2y^2 - 3\,x^2y - 12\,xy^2 + \, -30\,x^2y^2 - 18\,x^2y \, + \, -36\,x^2y \, + \, 6\,xy^2 \, = \, -24\,x^2y^2 \, - \\ & 57\,x^2y - 6\,xy^2 \\ & [5] \quad 28\,xy + - 8\,x^2y^2 - 4\,x^2y + 16\,xy^2 \, + \, 12\,x^2y^2 + 12\,xy \, = \, 4\,x^2y^2 - 4\,x^2y + 16\,xy^2 \, + \\ & 40\,xy \\ & [6] \quad 55\,x^2y \, + \, 5\,xy^2 \, + \, -75\,xy^2 \, + \, -30\,xy^2 \, + \, 75\,xy \, = \, 55\,x^2y \, - \, 100\,xy^2 \, + \, 75\,xy \\ & [7] \quad 84\,x^2y^2 - 12\,x^2y \, + \, -36\,xy \, + \, (-36\,x^2y^2 \, + \, 108\,xy) \, = \, 48\,x^2y^2 - 12\,x^2y \, + \, 72\,xy \\ & [8] \quad 21\,x^2y^2 \, + \, 21\,x^2y \, - \, 7\,xy^2 \, + \, -14\,x^2y^2 \, - \, 14\,xy^2 \, + \, 21\,xy \, + \, -14\,x^2y \, - \, 224\,xy^2 \, = \\ & 7\,x^2y^2 \, + \, 7\,x^2y \, - \, 245\,xy^2 \, + \, 21\,xy \\ & [9] \quad 192\,x^2y \, + \, 24\,x^2y \, + \, 8\,xy^2 \, + \, 256\,xy \, + \, -64\,x^2y^2 \, - \, 32\,x^2y \, = \, -64\,x^2y^2 \, + \, 184\,x^2y \, + \\ & 8\,xy^2 \, + \, 256\,xy \\ & [10] \quad 252\,x^2y \, + \, 27\,xy \, + \, -\, 315\,x^2y \, + \, -\, 36\,x^2y \, - \, 162\,xy^2 \, = \, -99\,x^2y \, - \, 162\,xy^2 \, + \, 27\,xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 2x^2y^2 + 2x^2y + 3xy^2 + 8x^2y^2 - 2x^2y - (4xy^2 + 4xy) = 10x^2y^2 - xy^2 - 4xy \\ &[3] \quad 16x^2y^2 + 2xy^2 + 2xy + 4x^2y^2 - 8xy^2 + 8xy - (4x^2y - 14xy) = 20x^2y^2 - 4x^2y - 6xy^2 + 24xy \\ &[4] \quad 36x^2y^2 + 6xy^2 - 9xy - (-6x^2y^2 - 6x^2y + 27xy) + (3x^2y^2 + 9x^2y - 9xy^2) = 45x^2y^2 + 15x^2y - 3xy^2 - 36xy \\ &[5] \quad 24x^2y^2 - 16x^2y + 32x^2y^2 - 16xy^2 - 4xy - (-48x^2y^2 - 16x^2y) = 104x^2y^2 - 16xy^2 - 4xy \end{aligned}$$

$$\begin{aligned} & [6] \quad 75\,x^2y^2 + 25\,x^2y - 100\,xy^2 + 15\,xy^2 + 5\,xy - (-50\,x^2y^2 - 100\,x^2y - 15\,xy) = \\ & 125\,x^2y^2 + 125\,x^2y - 85\,xy^2 + 20\,xy \\ & [7] \quad -12\,x^2y^2 + 6\,x^2y + 36\,xy - (288\,x^2y^2 + 72\,x^2y) + (24\,x^2y + 12\,xy^2) = -300\,x^2y^2 - \\ & 42\,x^2y + 12\,xy^2 + 36\,xy \\ & [8] \quad 21\,x^2y^2 + 147\,xy^2 - 21\,xy + -28\,x^2y^2 - 49\,xy^2 + 21\,xy - (49\,x^2y^2 - 98\,x^2y - 7\,xy) = -56\,x^2y^2 + 98\,x^2y + 98\,xy^2 + 7\,xy \\ & [9] \quad 32\,x^2y + 16\,xy^2 - 24\,xy + -64\,x^2y^2 + 192\,x^2y - 128\,xy^2 - (-8\,x^2y + 192\,xy) = \\ & -64\,x^2y^2 + 232\,x^2y - 112\,xy^2 - 216\,xy \\ & [10] \quad -153\,x^2y + 9\,xy - (324\,x^2y^2 - 36\,xy^2 - 243\,xy) + (81\,x^2y^2 + 54\,xy^2) = \\ & -243\,x^2y^2 - 153\,x^2y + 90\,xy^2 + 252\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (2 \, bxyz) \cdot (-b^2 x^3 yz^2) = -2 \, b^3 x^4 y^2 z^3 \\ &[3] \quad (-16 \, b^3 x^3 y^2 z^2) \cdot (16 \, b^2 x^2 y^2 z^2) = -256 \, b^5 x^5 y^4 z^4 \\ &[4] \quad (-3 \, b^3 x^2 y^2 z^2) \cdot (27 \, bxyz^3) = -81 \, b^4 x^3 y^3 z^5 \\ &[5] \quad (192 \, bxy^3 z^2) \cdot (-256 \, b^3 xy^3 z^3) = -49152 \, b^4 x^2 y^6 z^5 \\ &[6] \quad (25 \, b^2 xy^2 z^2) \cdot (-250 \, bx^3 y^2 z^2) = -6250 \, b^3 x^4 y^4 z^4 \\ &[7] \quad (-144 \, bx^3 y^2 z^2) \cdot (-648 \, b^3 x^2 yz^3) = 93312 \, b^4 x^5 y^3 z^5 \\ &[8] \quad (-686 \, b^3 x^3 y^3 z^3) \cdot (7 \, b^3 x^2 yz) = -4802 \, b^6 x^5 y^4 z^4 \\ &[9] \quad (-64 \, bxyz) \cdot (256 \, bxyz^2) = -16384 \, b^2 x^2 y^2 z^3 \\ &[10] \quad (243 \, b^2 x^3 y^2 z^3) \cdot (1458 \, b^3 x^2 y^2 z) = 354294 \, b^5 x^5 y^4 z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(2x) \cdot (-3x) = -6x^2$$
  
[2]  $(3x) \cdot (-4x^2 - x) = -12x^3 - 3x^2$   
[3]  $(-3x) \cdot (3x^2 + 3x) = -9x^3 - 9x^2$   
[4]  $(-3x^2) \cdot (-6x^2 - 5x) = 18x^4 + 15x^3$   
[5]  $(4x) \cdot (-2x^2 + 2x) = -8x^3 + 8x^2$   
[6]  $(-x^2) \cdot (x^2 - x) = -x^4 + x^3$   
[7]  $(-2x^2) \cdot (-x^2 + 3x) = 2x^4 - 6x^3$   
[8]  $(3x^2) \cdot (3x^2) = 9x^4$   
[9]  $(-4x) \cdot (-x^2) = 4x^3$   
[10]  $(x^2) \cdot (8x^2 - 3x) = 8x^4 - 3x^3$ 

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(2x) \cdot (2x^2 + x) = 4x^3 + 2x^2$$
  
[2]  $(3x^2 + 2x) \cdot (4x^2 + 5x) = 12x^4 + 23x^3 + 10x^2$   
[3]  $(3x^2 + 3x) \cdot (-3x) = -9x^3 - 9x^2$   
[4]  $(4x) \cdot (-2x^2 + x) = -8x^3 + 4x^2$   
[5]  $(-2x^2 + 4x) \cdot (-7x) = 14x^3 - 28x^2$   
[6]  $(-6x^2) \cdot (-x^2) = 6x^4$ 

[7] 
$$(4x^2 - 2x) \cdot (x^2 + 5x) = 4x^4 + 18x^3 - 10x^2$$

[8] 
$$(3x^2 - 3x) \cdot (7x) = 21x^3 - 21x^2$$

[9] 
$$(-8x^2) \cdot (6x^2) = -48x^4$$

[10] 
$$(-x^2) \cdot (3x^2 + 5x) = -3x^4 - 5x^3$$

[11] 
$$(2x^2) \cdot (-2x) = -4x^3$$

[12] 
$$(-x^2 + 4x) \cdot (-3x^2 - 3x) = 3x^4 - 9x^3 - 12x^2$$

[13] 
$$(x) \cdot (2x) = 2x^2$$

[14] 
$$(-5x) \cdot (-x^2 + 3x) = 5x^3 - 15x^2$$

[15] 
$$(-4x^2 - 2x) \cdot (-4x^2 + 6x) = 16x^4 - 16x^3 - 12x^2$$

## Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(3x^3 + x^2) \cdot (-x^3 + 3x^2) = -3x^6 + 8x^5 + 3x^4$$

[2] 
$$(2x^3 - 2x^2) \cdot (2x^2 - 2x) = 4x^5 - 8x^4 + 4x^3$$

[3] 
$$(-x^3 + 4x) \cdot (3x^3 - 2x^2 - 4x) = -3x^6 + 2x^5 + 16x^4 - 8x^3 - 16x^2$$

[4] 
$$(-2x) \cdot (2x^3 - x^2 + 2x) = -4x^4 + 2x^3 - 4x^2$$

[5] 
$$(3x^3 + 4x^2) \cdot (-x^3 - 9x) = -3x^6 - 4x^5 - 27x^4 - 36x^3$$

[6] 
$$(3x^2 + 2x) \cdot (-6x^3 - x) = -18x^5 - 12x^4 - 3x^3 - 2x^2$$

[7] 
$$(5x^2 + 3x) \cdot (3x^3 - 2x^2 - 4x) = 15x^5 - x^4 - 26x^3 - 12x^2$$

[8] 
$$(x^2 + 4x) \cdot (-2x^3 + 3x) = -2x^5 - 8x^4 + 3x^3 + 12x^2$$

[9] 
$$(0) \cdot (3x^3 - 2x^2 + 2x) = 0$$

[10] 
$$(-x) \cdot (-2x^3 + 3x^2 + 3x) = 2x^4 - 3x^3 - 3x^2$$

[11] 
$$(-x^2) \cdot (-4x^3 + x^2 - 5x) = 4x^5 - x^4 + 5x^3$$

[12] 
$$(2x^3) \cdot (2x^2 + 4x) = 4x^5 + 8x^4$$

[13] 
$$(-6x^2 + 2x) \cdot (-3x^2 - 7x) = 18x^4 + 36x^3 - 14x^2$$

[14] 
$$(3x^2 + x) \cdot (-3x^3 + x^2) = -9x^5 + x^3$$

[15] 
$$(2x^2 - 3x) \cdot (6x^2 + 6x) = 12x^4 - 6x^3 - 18x^2$$

[16] 
$$(3x^3 - 3x) \cdot (-2x^3 + 3x) = -6x^6 + 15x^4 - 9x^2$$

[17] 
$$(2x^3) \cdot (-3x^3 + 5x^2) = -6x^6 + 10x^5$$

[18] 
$$(-x^3 + x^2) \cdot (x^3 - 3x) = -x^6 + x^5 + 3x^4 - 3x^3$$

[19] 
$$(7x^3 + 3x^2) \cdot (3x^3 + 4x) = 21x^6 + 9x^5 + 28x^4 + 12x^3$$

[20] 
$$(-5x) \cdot (2x) = -10x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(3x^2y - 4xy) \cdot (-x^2y^2 - x^2y) = -3x^4y^3 - 3x^4y^2 + 4x^3y^3 + 4x^3y^2$$

[2] 
$$(3xy) \cdot (x^2y^2 - 4x^2y - 2xy^2) = 3x^3y^3 - 12x^3y^2 - 6x^2y^3$$

[3] 
$$(-2x^2y + xy^2) \cdot (3x^2y^2 + 3x^2y + 3xy) = -6x^4y^3 + 3x^3y^4 - 6x^4y^2 + 3x^3y^3 - 6x^3y^2 + 3x^2y^3$$

[4] 
$$(-2xy^2 - xy) \cdot (-4xy^2 + 5xy) = 8x^2y^4 - 6x^2y^3 - 5x^2y^2$$

[5] 
$$(3x^2y-2xy^2)\cdot(2x^2y-3xy^2+3xy) = 6x^4y^2-13x^3y^3+6x^2y^4+9x^3y^2-6x^2y^3$$

[6] 
$$(-x^2y - 4xy^2) \cdot (-4xy) = 4x^3y^2 + 16x^2y^3$$

[7] 
$$(2xy^2) \cdot (3x^2y + 2xy) = 6x^3y^3 + 4x^2y^3$$