## 1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1] 
$$3x^6 + 6x^3 + -3x^4 + -3x^4 + x^2 = 3x^6 - 6x^4 + 6x^3 + x^2$$
  
[2]  $x^5 - 3x^2 + -x^4 - 3x^2 + 3x + 4x^4 - 2x^3 + 4x^2 = x^5 + 3x^4 - 2x^3 - 2x^2 + 3x$   
[3]  $4x^5 + 4x + -2x^5 - x^3 - 2x^2 + (-x^3 - 2x) = 2x^5 - 2x^3 - 2x^2 + 2x$   
[4]  $2x^5 + 2x^4 - 4x^2 + -4x^6 + x^5 + 4x + -x^6 - 2x^3 + 4x = -5x^6 + 3x^5 + 2x^4 - 2x^3 - 4x^2 + 8x$   
[5]  $4x^5 - 4x^3 + 4x + 2x^6 - 2x^4 + x^3 + x^6 + 3x^4 - x^2 = 3x^6 + 4x^5 + x^4 - 3x^3 - x^2 + 4x$   
[6]  $3x^4 + x + 4x^5 + 3x^4 - x + -3x^5 + x^4 - 4x^2 = x^5 + 7x^4 - 4x^2$   
[7]  $3x^6 - 3x^3 + 2x^6 - 6x^2 + -4x^5 - 3x = 5x^6 - 4x^5 - 3x^3 - 6x^2 - 3x$   
[8]  $x^6 - x^2 + x^6 - 3x^3 - 2x + -5x^4 - 3x = 2x^6 - 5x^4 - 3x^3 - x^2 - 5x$   
[9]  $3x^6 - x^5 + x^4 + -x^6 + 4x^4 - 2x^2 + (-x^3 - 7x) = 2x^6 - x^5 + 5x^4 - x^3 - 2x^2 - 7x$   
[10]  $x^5 + x^5 + x^4 - x^2 + -2x^6 + x^3 + 3x = -2x^6 + 2x^5 + x^4 + x^3 - x^2 + 3x$ 

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 4x^2y^2-7x^2y+-4x^2y^2-x^2y-4xy+4x^2y^2-4xy=4x^2y^2-8x^2y-8xy \\ [3] \quad 2xy^2+-8x^2y^2-12x^2y+12xy^2+24xy^2-4xy=-8x^2y^2-12x^2y+38xy^2-4xy \\ [4] \quad -18x^2y-27xy+(-9x^2y^2-18xy)+(-6x^2y^2+9xy)=-15x^2y^2-18x^2y-36xy \\ [5] \quad 8xy^2-4xy+16x^2y^2+60x^2y+-4x^2y-48xy^2-32xy=16x^2y^2+56x^2y-40xy^2-36xy \\ [6] \quad 5x^2y^2+100x^2y-20xy^2+-5x^2y^2+35xy^2+10x^2y+15xy^2-100xy=110x^2y+30xy^2-100xy \\ [7] \quad 12x^2y-90xy+-12x^2y+36xy^2+36xy+-24x^2y^2-6xy^2+108xy=-24x^2y^2+30xy^2+54xy \\ [8] \quad 98x^2y-14xy^2+7xy+196x^2y^2+147x^2y-196xy+-147x^2y^2-7xy^2-196xy=49x^2y^2+245x^2y-21xy^2-385xy \\ [9] \quad 264x^2y^2-32xy+-224xy^2-32xy+192x^2y+64xy^2-256xy=264x^2y^2+192x^2y-160xy^2-320xy \\ [10] \quad -162x^2y^2-81xy^2-162xy+(-45xy^2-9xy)+(-324x^2y^2+18xy^2-27xy)=-486x^2y^2-108xy^2-198xy \\ [10] \quad -162x^2y^2-81xy^2-198xy \\ [10] \quad -162x^2y^2-108xy^2-198xy \\ [10] \quad -162x^2y^2-18xy^2-18xy^2-198xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$[1] \quad 0 - (0) + (0) = 0$$

$$[2] \quad -6xy + 3x^2y^2 + 4x^2y + 4xy^2 - (x^2y + 2xy^2) = 3x^2y^2 + 3x^2y + 2xy^2 - 6xy$$

$$[3] \quad 16x^2y^2 + 4xy^2 + 8xy + 8x^2y^2 + 8x^2y + 2xy^2 - (-2x^2y^2 + 6xy) = 26x^2y^2 + 8x^2y + 6xy^2 + 2xy$$

$$[4] \quad -9x^2y^2 + 24x^2y - (-3x^2y + 3xy^2 - 3xy) + (18x^2y^2 + 6x^2y - 9xy^2) = 9x^2y^2 + 33x^2y - 12xy^2 + 3xy$$

$$[5] \quad 24 \, x^2 y^2 + 16 \, x^2 y + 48 \, x^2 y^2 - 16 \, x^2 y - 64 \, xy - (-8 \, x^2 y^2 - 16 \, x^2 y - 32 \, xy) = 80 \, x^2 y^2 + 16 \, x^2 y - 32 \, xy$$
 
$$[6] \quad -30 \, x^2 y + 50 \, xy^2 + 75 \, xy^2 + 40 \, xy - (-115 \, x^2 y) = 85 \, x^2 y + 125 \, xy^2 + 40 \, xy$$
 
$$[7] \quad 24 \, x^2 y - 24 \, xy - (6 \, x^2 y^2 + 108 \, xy^2 - 24 \, xy) + (-48 \, x^2 y^2) = -54 \, x^2 y^2 + 24 \, x^2 y - 108 \, xy^2$$
 
$$[8] \quad 147 \, x^2 y^2 - 28 \, xy^2 - 196 \, xy + 21 \, xy - (98 \, x^2 y^2 + 28 \, x^2 y - 98 \, xy) = 49 \, x^2 y^2 - 28 \, x^2 y - 28 \, xy^2 - 77 \, xy$$
 
$$[9] \quad 32 \, x^2 y^2 - 256 \, xy^2 + 256 \, xy + -256 \, x^2 y - 64 \, xy^2 - (184 \, x^2 y^2) = -152 \, x^2 y^2 - 256 \, x^2 y - 320 \, xy^2 + 256 \, xy$$
 
$$[10] \quad -81 \, x^2 y - 234 \, xy - (81 \, x^2 y^2 - 63 \, xy^2) + (162 \, x^2 y - 135 \, xy) = -81 \, x^2 y^2 + 81 \, x^2 y + 63 \, xy^2 - 369 \, xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (4\,b^3x^3yz^3) \cdot (2\,b^3x^3y^2z^3) = 8\,b^6x^6y^3z^6 \\ &[3] \quad (-4\,b^3x^3y^3z^3) \cdot (4\,b^3xyz) = -16\,b^6x^4y^4z^4 \\ &[4] \quad (3\,b^3x^3yz) \cdot (-9\,bxyz) = -27\,b^4x^4y^2z^2 \\ &[5] \quad (4\,b^3x^3yz^3) \cdot (192\,b^2xy^2z) = 768\,b^5x^4y^3z^4 \\ &[6] \quad (-125\,b^2x^2yz^3) \cdot (-500\,b^3x^3y^3z^3) = 62500\,b^5x^5y^4z^6 \\ &[7] \quad (36\,b^3x^2yz^2) \cdot (-72\,bxyz^2) = -2592\,b^4x^3y^2z^4 \\ &[8] \quad (28\,b^3xyz^2) \cdot (7\,b^2x^3yz^3) = 196\,b^5x^4y^2z^5 \\ &[9] \quad (1024\,bx^3yz^3) \cdot (-24\,b^3xyz^3) = -24576\,b^4x^4y^2z^6 \\ &[10] \quad (729\,b^3xy^2z^2) \cdot (18\,bx^3y^2z^3) = 13122\,b^4x^4y^4z^5 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(3x) \cdot (-7x) = -21x^2$$
  
[2]  $(-3x^2) \cdot (-4x^2 + 6x) = 12x^4 - 18x^3$   
[3]  $(3x) \cdot (-3x^2 - x) = -9x^3 - 3x^2$   
[4]  $(-x) \cdot (4x^2 + 2x) = -4x^3 - 2x^2$   
[5]  $(x) \cdot (-2x^2 - 2x) = -2x^3 - 2x^2$   
[6]  $(-x) \cdot (-4x^2 + x) = 4x^3 - x^2$   
[7]  $(4x^2) \cdot (-7x) = -28x^3$   
[8]  $(2x) \cdot (-7x) = -14x^2$   
[9]  $(x^2) \cdot (-4x^2 - 6x) = -4x^4 - 6x^3$   
[10]  $(4x) \cdot (2x^2 - 2x) = 8x^3 - 8x^2$ 

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-3\,x^2+x)\cdot (-2\,x^2-2\,x) = 6\,x^4+4\,x^3-2\,x^2 \\ &[2] \quad (x)\cdot (-x^2) = -x^3 \\ &[3] \quad (x^2+2\,x)\cdot (-3\,x^2) = -3\,x^4-6\,x^3 \\ &[4] \quad (-4\,x)\cdot (4\,x^2-8\,x) = -16\,x^3+32\,x^2 \\ &[5] \quad (x^2-x)\cdot (-9\,x) = -9\,x^3+9\,x^2 \end{aligned}$$

$$\begin{aligned} &[6] \quad (-3\,x^2-2\,x)\cdot(x^2) = -3\,x^4-2\,x^3\\ &[7] \quad (-x^2+x)\cdot(-x^2+6\,x) = x^4-7\,x^3+6\,x^2\\ &[8] \quad (-4\,x^2+3\,x)\cdot(-2\,x) = 8\,x^3-6\,x^2\\ &[9] \quad (-5\,x)\cdot(-2\,x^2) = 10\,x^3\\ &[10] \quad (3\,x^2)\cdot(x^2-x) = 3\,x^4-3\,x^3\\ &[11] \quad (-x^2+x)\cdot(-3\,x^2+3\,x) = 3\,x^4-6\,x^3+3\,x^2\\ &[12] \quad (-2\,x^2-3\,x)\cdot(2\,x^2+6\,x) = -4\,x^4-18\,x^3-18\,x^2\\ &[13] \quad (0)\cdot(3\,x) = 0 \end{aligned}$$

[14] 
$$(2x) \cdot (-2x^2 - 3x) = -4x^3 - 6x^2$$

[15] 
$$(2x^2 - 3x) \cdot (4x) = 8x^3 - 12x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (-4\,x^2-6\,x) \cdot (2\,x^3-x) = -8\,x^5-12\,x^4+4\,x^3+6\,x^2 \\ & [2] \quad (-3\,x^2-4\,x) \cdot (-x^3+3\,x^2+x) = 3\,x^5-5\,x^4-15\,x^3-4\,x^2 \\ & [3] \quad (4\,x^3-3\,x) \cdot (-3\,x^3-2\,x^2) = -12\,x^6-8\,x^5+9\,x^4+6\,x^3 \\ & [4] \quad (2\,x^3+x^2) \cdot (2\,x^3) = 4\,x^6+2\,x^5 \\ & [5] \quad (-x^2+2\,x) \cdot (x^3-2\,x^2+x) = -x^5+4\,x^4-5\,x^3+2\,x^2 \\ & [6] \quad (4\,x) \cdot (-x^3+x^2+4\,x) = -4\,x^4+4\,x^3+16\,x^2 \\ & [7] \quad (-2\,x^2+3\,x) \cdot (3\,x^3-7\,x) = -6\,x^5+9\,x^4+14\,x^3-21\,x^2 \\ & [8] \quad (7\,x^2) \cdot (6\,x^3+4\,x^2-3\,x) = 42\,x^5+28\,x^4-21\,x^3 \\ & [9] \quad (3\,x^2-4\,x) \cdot (-2\,x^2+8\,x) = -6\,x^4+32\,x^3-32\,x^2 \\ & [10] \quad (-3\,x) \cdot (5\,x^3-4\,x) = -15\,x^4+12\,x^2 \\ & [11] \quad (-4\,x^2+x) \cdot (-3\,x^3-2\,x^2-x) = 12\,x^5+5\,x^4+2\,x^3-x^2 \\ & [12] \quad (x^2+x) \cdot (6\,x^3+2\,x^2-4\,x) = 6\,x^5+8\,x^4-2\,x^3-4\,x^2 \\ & [13] \quad (-4\,x^3+5\,x) \cdot (6\,x^3-x^2) = -24\,x^6+4\,x^5+30\,x^4-5\,x^3 \\ & [14] \quad (-3\,x^3-3\,x^2) \cdot (-4\,x^3-3\,x^2) = 12\,x^6+21\,x^5+9\,x^4 \\ & [15] \quad (-4\,x^3+3\,x) \cdot (x^3+6\,x^2+x) = -4\,x^6-24\,x^5-x^4+18\,x^3+3\,x^2 \\ & [16] \quad (-6\,x^3) \cdot (-3\,x^2) = 18\,x^5 \\ & [17] \quad (2\,x^3+x^2) \cdot (3\,x^3+11\,x) = 6\,x^6+3\,x^5+22\,x^4+11\,x^3 \\ & [18] \quad (-x^2+3\,x) \cdot (-2\,x^2+4\,x) = 2\,x^4-10\,x^3+12\,x^2 \\ & [19] \quad (-3\,x^3-2^2) \cdot (x^3) = -3\,x^6-x^5 \\ & [20] \quad (3\,x^3-2\,x) \cdot (4\,x^3+4\,x^2-x) = 12\,x^6+12\,x^5-11\,x^4-8\,x^3+2\,x^2 \end{aligned}$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$[1] \quad (4xy) \cdot (4xy) = 16x^2y^2$$

$$[2] \quad (6xy) \cdot (-3x^2y - 2xy) = -18x^3y^2 - 12x^2y^2$$

$$[3] \quad (x^2y^2 - 2xy) \cdot (-6x^2y^2 - 4xy) = -6x^4y^4 + 8x^3y^3 + 8x^2y^2$$

$$[4] \quad (4x^2y + 2xy) \cdot (-2x^2y + 2xy^2 + 4xy) = -8x^4y^2 + 8x^3y^3 + 12x^3y^2 + 4x^2y^3 + 8x^2y^2$$

$$[5] \quad (x^2y^2 - x^2y) \cdot (2x^2y^2 - 4xy) = 2x^4y^4 - 2x^4y^3 - 4x^3y^3 + 4x^3y^2$$

$$[6] \quad (2xy^2 - 4xy) \cdot (-x^2y^2 - 3xy^2 - 2xy) = -2x^3y^4 + 4x^3y^3 - 6x^2y^4 + 8x^2y^3 + 8x^2y^2$$

$$[7] \quad (4x^2y + 2xy) \cdot (2xy^2 - 4xy) = 8x^3y^3 - 16x^3y^2 + 4x^2y^3 - 8x^2y^2$$