1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$2x^6 - 3x^5 - 3x^3 + -3x^4 - 3x^3 - 4x + (-4x^2) = 2x^6 - 3x^5 - 3x^4 - 6x^3 - 4x^2 - 4x$$

[2] $x^5 + 4x^4 - x^2 + -4x^3 - 5x + (-4x^4 - 2x^3) = x^5 - 6x^3 - x^2 - 5x$
[3] $3x^6 + 3x^5 + x^4 + -2x^4 + 2x^2 + x + -x^5 - 3x^2 - 2x = 3x^6 + 2x^5 - x^4 - x^2 - x$
[4] $2x^2 + x^4 - 2x + -4x^6 + 3x^2 + 4x = -4x^6 + x^4 + 5x^2 + 2x$
[5] $-3x^5 + x^3 + (-4x^5 - 3x^2 - 4x) + (-x^5 - 4x^4 - 4x^3) = -8x^5 - 4x^4 - 3x^3 - 3x^2 - 4x$
[6] $3x^6 - 2x^3 + 2x^2 + -2x^4 + 3x^2 - x + -2x^3 + x^2 = 3x^6 - 2x^4 - 4x^3 + 6x^2 - x$
[7] $-3x^4 - 2x^2 - x + (-4x^6 - 4x^5 + 3x) + (-4x^3) = -4x^6 - 4x^5 - 3x^4 - 4x^3 - 2x^2 + 2x$
[8] $x^6 - 4x + -x^6 - x^5 - 2x^4 + (-x^6 + 3x^4 + 2x^2) = -x^6 - x^5 + x^4 + 2x^2 - 4x$
[9] $3x^4 - 4x + -2x^6 - 4x^2 + -8x^4 + 2x^3 = -2x^6 - 5x^4 + 2x^3 - 4x^2 - 4x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 2x^2y+4xy^2+2xy+-4x^2y^2+x^2y-xy+4x^2y^2+4xy^2=3x^2y+8xy^2+xy \\ [3] \quad 2x^2y+20xy^2+-2x^2y^2-8xy^2-16xy+4xy=-2x^2y^2+2x^2y+12xy^2-12xy \\ [4] \quad 45x^2y-27xy+-27x^2y^2-27xy^2+(-12x^2y^2+21xy^2)=-39x^2y^2+45x^2y-6xy^2-27xy \\ [5] \quad 64x^2y-8xy^2-8xy+-44x^2y^2-12xy+-64x^2y-48xy=-44x^2y^2-8xy^2-68xy \\ [6] \quad -20x^2y^2-5x^2y+(-30x^2y^2+75x^2y)+(-5x^2y^2+85xy^2)=-55x^2y^2+70x^2y+85xy^2 \\ [7] \quad 36x^2y^2+144x^2y^2-30x^2y+-18xy^2+24xy=180x^2y^2-30x^2y-18xy^2+24xy \\ [8] \quad 28x^2y^2-98x^2y+147xy+-231xy^2+217xy^2-98xy=28x^2y^2-98x^2y-14xy^2+49xy \\ [9] \quad 96x^2y^2+8xy+-128x^2y^2+256xy^2-128xy+0=-32x^2y^2+256xy^2-120xy \\ [10] \quad 162x^2y^2-81x^2y-162xy+-243x^2y-162xy^2+324xy+-36x^2y^2+9xy=126x^2y^2-324x^2y-162xy^2+171xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y^2 - 2\,xy^2 + 3\,xy + 4\,x^2y^2 + 3\,xy^2 + xy - (6\,x^2y^2 - 2\,x^2y) = -4\,x^2y^2 + 2\,x^2y + xy^2 + 4\,xy \\ &[3] \quad 8\,x^2y - 24\,xy + -8\,x^2y^2 - 8\,x^2y + 4\,xy - (12\,x^2y^2 + 2\,x^2y) = -20\,x^2y^2 - 2\,x^2y - 20\,xy \\ &[4] \quad 6\,x^2y + 21\,xy - (30\,x^2y^2 + 9\,x^2y) + (-3\,x^2y + 9\,xy^2 - 36\,xy) = -30\,x^2y^2 - 6\,x^2y + 9\,xy^2 - 15\,xy \end{aligned}$$

$$\begin{aligned} & [5] \quad -16\,x^2y + 64\,xy^2 - 16\,xy + -16\,xy - (8\,x^2y^2 - 64\,x^2y + 4\,xy) = -8\,x^2y^2 + \\ & 48\,x^2y + 64\,xy^2 - 36\,xy \\ & [6] \quad 20\,x^2y - 50\,xy^2 - 75\,xy + 50\,x^2y^2 + 15\,x^2y - (-50\,x^2y + 50\,xy^2) = 50\,x^2y^2 + \\ & 85\,x^2y - 100\,xy^2 - 75\,xy \\ & [7] \quad -12\,x^2y^2 + 144\,xy^2 + 108\,xy - (108\,x^2y + 12\,xy^2 + 18\,xy) + (12\,x^2y^2 + 18\,x^2y + \\ & 144\,xy) = -90\,x^2y + 132\,xy^2 + 234\,xy \\ & [8] \quad -21\,x^2y + 168\,xy^2 + -196\,xy^2 - 70\,xy - (14\,x^2y^2 + 196\,x^2y + 28\,xy^2) = \\ & -14\,x^2y^2 - 217\,x^2y - 56\,xy^2 - 70\,xy \\ & [9] \quad 8\,x^2y - 64\,xy^2 - 128\,xy + 192\,x^2y^2 - 16\,x^2y + 16\,xy^2 - (-96\,xy^2 - 128\,xy) = \\ & 192\,x^2y^2 - 8\,x^2y + 48\,xy^2 \\ & [10] \quad -36\,x^2y^2 - 27\,x^2y - 324\,xy - (-81\,x^2y^2 - 405\,xy^2) + (-9\,x^2y^2 + 36\,x^2y + 243\,xy^2) = 36\,x^2y^2 + 9\,x^2y + 648\,xy^2 - 324\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} & [1] \quad (0) \cdot (0) = 0 \\ & [2] \quad (-3\,b^3x^3yz^3) \cdot (2\,bx^2y^2z) = -6\,b^4x^5y^3z^4 \\ & [3] \quad (8\,b^3xyz) \cdot (4\,b^2xyz^2) = 32\,b^5x^2y^2z^3 \\ & [4] \quad (-9\,b^3xy^3z) \cdot (-9\,b^2x^3y^2z^2) = 81\,b^5x^4y^5z^3 \\ & [5] \quad (-64\,b^3x^3yz^3) \cdot (64\,b^2x^2y^3z) = -4096\,b^5x^5y^4z^4 \\ & [6] \quad (-20\,b^2xy^3z^3) \cdot (100\,bx^2yz) = -2000\,b^3x^3y^4z^4 \\ & [7] \quad (-432\,b^2x^2yz^2) \cdot (108\,b^3xyz^2) = -46656\,b^5x^3y^2z^4 \\ & [8] \quad (-1372\,bx^3yz^2) \cdot (-343\,bx^2yz) = 470596\,b^2x^5y^2z^3 \\ & [9] \quad (-192\,bx^2yz^3) \cdot (128\,bxy^2z) = -24576\,b^2x^3y^3z^4 \\ & [10] \quad (243\,b^3x^2y^2z) \cdot (243\,b^3x^2yz^3) = 59049\,b^6x^4y^3z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x^2) \cdot (-x^2 - 2\,x) = x^4 + 2\,x^3 \\ &[2] \quad (-2\,x) \cdot (-4\,x^2) = 8\,x^3 \\ &[3] \quad (2\,x^2) \cdot (6\,x^2 - 5\,x) = 12\,x^4 - 10\,x^3 \\ &[4] \quad (x) \cdot (-x^2 - 8\,x) = -x^3 - 8\,x^2 \\ &[5] \quad (3\,x) \cdot (-4\,x^2 - 4\,x) = -12\,x^3 - 12\,x^2 \\ &[6] \quad (2\,x^2) \cdot (-5\,x^2 + 3\,x) = -10\,x^4 + 6\,x^3 \\ &[7] \quad (3\,x) \cdot (-7\,x^2 + x) = -21\,x^3 + 3\,x^2 \\ &[8] \quad (-4\,x) \cdot (-x^2 + x) = 4\,x^3 - 4\,x^2 \\ &[9] \quad (3\,x) \cdot (-9\,x) = -27\,x^2 \\ &[10] \quad (2\,x^2) \cdot (-3\,x^2 + 3\,x) = -6\,x^4 + 6\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^2 - 4x) \cdot (2x^2 - 6x) = 2x^4 - 14x^3 + 24x^2$$

[2] $(6x^2) \cdot (2x^2 - 5x) = 12x^4 - 30x^3$
[3] $(5x^2) \cdot (2x^2) = 10x^4$
[4] $(-2x^2) \cdot (7x^2 - 3x) = -14x^4 + 6x^3$

[5]
$$(-x^2+3x)\cdot(6x^2-4x) = -6x^4+22x^3-12x^2$$

[6]
$$(x^2 + 4x) \cdot (3x^2 + 2x) = 3x^4 + 14x^3 + 8x^2$$

[7]
$$(-x^2 + 3x) \cdot (-x^2 - 5x) = x^4 + 2x^3 - 15x^2$$

[8]
$$(2x^2 - 2x) \cdot (-4x) = -8x^3 + 8x^2$$

[9]
$$(-x^2 + 3x) \cdot (x^2 - 5x) = -x^4 + 8x^3 - 15x^2$$

[10]
$$(-7x) \cdot (x^2 - 4x) = -7x^3 + 28x^2$$

[11]
$$(x^2) \cdot (x^2 + 3x) = x^4 + 3x^3$$

[12]
$$(-2x^2) \cdot (-4x^2) = 8x^4$$

[13]
$$(-6x^2) \cdot (2x^2 + 2x) = -12x^4 - 12x^3$$

[14]
$$(5x) \cdot (3x^2 + x) = 15x^3 + 5x^2$$

[15]
$$(2x^2) \cdot (-4x^2 + 5x) = -8x^4 + 10x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x^3 + 2x) \cdot (x^2 + 2x) = 2x^5 + 4x^4 + 2x^3 + 4x^2$$

[2]
$$(5x^3) \cdot (-5x^2 - 2x) = -25x^5 - 10x^4$$

[3]
$$(-x^3+x)\cdot(3x^3+x^2+x) = -3x^6-x^5+2x^4+x^3+x^2$$

[4]
$$(-3x^3 - 4x^2 - x) \cdot (-3x^2 - 4x) = 9x^5 + 24x^4 + 19x^3 + 4x^2$$

[5]
$$(3x^2 + 2x) \cdot (-x^3 + x^2) = -3x^5 + x^4 + 2x^3$$

[6]
$$(-2x^2 + 2x) \cdot (-5x^3) = 10x^5 - 10x^4$$

[7]
$$(x^2 - 2x) \cdot (-4x^3 - 5x) = -4x^5 + 8x^4 - 5x^3 + 10x^2$$

[8]
$$(3x) \cdot (-3x^3 + 3x^2 + 2x) = -9x^4 + 9x^3 + 6x^2$$

[9]
$$(-4x^2 + 2x) \cdot (x^2 + 9x) = -4x^4 - 34x^3 + 18x^2$$

[10]
$$(-3x^3 + x^2) \cdot (-6x^2 - x) = 18x^5 - 3x^4 - x^3$$

[11]
$$(2x^3 + 3x) \cdot (-x^3 - 3x^2 - 4x) = -2x^6 - 6x^5 - 11x^4 - 9x^3 - 12x^2$$

[12]
$$(-x^3 - 2x^2) \cdot (-3x^3 + 3x^2 - 2x) = 3x^6 + 3x^5 - 4x^4 + 4x^3$$

[13]
$$(3x^3 - 3x) \cdot (-2x^3 + 4x^2) = -6x^6 + 12x^5 + 6x^4 - 12x^3$$

[14]
$$(-4x^2 + 4x) \cdot (x^3 + 3x) = -4x^5 + 4x^4 - 12x^3 + 12x^2$$

[15]
$$(-x^3 + 4x^2) \cdot (-x^3 + 4x) = x^6 - 4x^5 - 4x^4 + 16x^3$$

[16]
$$(x) \cdot (-4x^3 - 3x^2) = -4x^4 - 3x^3$$

[17]
$$(0) \cdot (2x^3 + 4x^2 + 3x) = 0$$

[18]
$$(-4x^2 + 3x) \cdot (-4x^3 + 4x^2) = 16x^5 - 28x^4 + 12x^3$$

[19]
$$(3x^2 + 2x) \cdot (x^2 + 5x) = 3x^4 + 17x^3 + 10x^2$$

[20]
$$(6x^2) \cdot (3x^2 - 2x) = 18x^4 - 12x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$[1] \quad (-3\,x^2y^2 + 2\,xy) \cdot (x^2y^2 + 3\,x^2y - 3\,xy^2) = -3\,x^4y^4 - 9\,x^4y^3 + 9\,x^3y^4 + 2\,x^3y^3 + 6\,x^3y^2 - 6\,x^2y^3$$

[2]
$$(-2x^2y + 4xy) \cdot (2xy^2) = -4x^3y^3 + 8x^2y^3$$

[3]
$$(2x^2y^2 - 4x^2y) \cdot (3x^2y^2 + 7x^2y) = 6x^4y^4 + 2x^4y^3 - 28x^4y^2$$

[4]
$$(-3x^2y^2 + 3xy^2) \cdot (4x^2y - xy^2 + xy) = -12x^4y^3 + 3x^3y^4 + 9x^3y^3 - 3x^2y^4 + 3x^2y^3$$

$$[5] \quad (-2\,x^2y^2-2\,x^2y)\cdot(x^2y^2+3\,xy) = -2\,x^4y^4-2\,x^4y^3-6\,x^3y^3-6\,x^3y^2$$

[6]
$$(3xy^2 - 4xy) \cdot (-4x^2y^2 - 5xy^2) = -12x^3y^4 + 16x^3y^3 - 15x^2y^4 + 20x^2y^3$$

[7]
$$(-2xy^2 + 3xy) \cdot (-3x^2y + 2xy) = 6x^3y^3 - 9x^3y^2 - 4x^2y^3 + 6x^2y^2$$