1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad -2\,x^5 + 4\,x^3 - 2\,x^2 + (-2\,x^6 - 3\,x^4 + 3\,x^2) + (-4\,x^6 + x^5 + 4\,x^3) = -6\,x^6 - x^5 - 3\,x^4 + 8\,x^3 + x^2 \\ & [2] \quad x^6 - x^4 + -4\,x^6 - x^3 + (-2\,x^4 + 2\,x^3 - 4\,x) = -3\,x^6 - 3\,x^4 + x^3 - 4\,x \\ & [3] \quad 4\,x^4 + 2\,x^2 - x + -x^6 - 3\,x^4 + 2\,x + 5\,x^4 + x = -x^6 + 6\,x^4 + 2\,x^2 + 2\,x \\ & [4] \quad 6\,x^4 + 2\,x^2 + -2\,x^4 - x^2 + x^5 + x^4 = x^5 + 5\,x^4 + x^2 \\ & [5] \quad 3\,x^6 - 4\,x^4 - 4\,x + -3\,x^5 - 3\,x^3 - 4\,x^2 + -x^5 + 4\,x^2 = 3\,x^6 - 4\,x^5 - 4\,x^4 - 3\,x^3 - 4\,x \\ & [6] \quad -4\,x^5 - x^2 + 3\,x + (-x^5 - 3\,x^2) + (-4\,x^6 + 2\,x^5 + 3\,x^3) = -4\,x^6 - 3\,x^5 + 3\,x^3 - 4\,x^2 + 3\,x \end{aligned}$$

$$[7] \quad x^4 + 3\,x^2 + -2\,x^6 - 2\,x^4 + x + -2\,x^3 + 2\,x^2 = -2\,x^6 - x^4 - 2\,x^3 + 5\,x^2 + x \\ & [8] \quad 3\,x^6 + x^3 + x^2 + -3\,x^5 + -4\,x^6 - 3\,x^2 + x = -x^6 - 3\,x^5 + x^3 - 2\,x^2 + x \\ & [9] \quad 2\,x^4 + 4\,x^2 - 3\,x + -2\,x^4 + 3\,x^3 + 3\,x^6 - 2\,x^4 - x^2 = 3\,x^6 - 2\,x^4 + 3\,x^3 + 3\,x^2 - 3\,x \\ & [10] \quad 4\,x^6 + 3\,x^2 - x + 3\,x^6 + x^5 + 3\,x + -3\,x^6 - 2\,x^5 - x = 4\,x^6 - x^5 + 3\,x^2 + x \end{aligned}$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad -7x^2y^2+2xy+(-4xy^2)+(-4x^2y-4xy^2-4xy)=-7x^2y^2-4x^2y-8xy^2-2xy \\ [3] \quad 12x^2y^2+-6x^2y+8xy^2+-4x^2y-8xy^2=12x^2y^2-10x^2y \\ [4] \quad 12x^2y-45xy+-27x^2y^2+24xy+36x^2y^2-3xy^2+6xy=9x^2y^2+12x^2y-3xy^2-15xy \\ [5] \quad 16x^2y^2-32xy^2+16xy+12x^2y+4xy^2-12xy+32x^2y^2-52x^2y=48x^2y^2-40x^2y-28xy^2+4xy \\ [6] \quad 5xy^2-125xy+75x^2y^2+25xy^2-25xy+75x^2y-20xy^2+25xy=75x^2y^2+75x^2y+10xy^2-125xy \\ [7] \quad 12x^2y^2-6xy^2-12xy+24x^2y^2-36x^2y-24xy^2+-36x^2y+180xy^2=36x^2y^2-72x^2y+150xy^2-12xy \\ [8] \quad 14x^2y^2-98xy^2+196xy+-49x^2y+140xy+231xy^2=14x^2y^2-49x^2y+133xy^2+336xy \\ [9] \quad 24x^2y-192xy^2+16xy+-8x^2y^2-8xy^2+416xy^2=-8x^2y^2+24x^2y+216xy^2+16xy \\ [10] \quad -81x^2y+18xy^2-243xy+(-9x^2y+243xy)+(-324x^2y^2-81x^2y+9xy^2)=-324x^2y^2-171x^2y+27xy^2 \\ [10] \quad -81x^2y+18xy^2-243xy+(-9x^2y+243xy)+(-324x^2y^2-81x^2y+9xy^2)=-324x^2y^2-171x^2y+27xy^2 \\ [2] \quad -824x^2y^2-171x^2y+27xy^2 \\ [2] \quad -824x^2y^2-18x^2y^2-1$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 7 \, x^2 y^2 - 4 \, xy + - x^2 y^2 + 4 \, xy^2 + 2 \, xy - (4 \, x^2 y^2 + 3 \, xy) = 2 \, x^2 y^2 + 4 \, xy^2 - 5 \, xy \\ &[3] \quad -4 \, x^2 y^2 + 10 \, x^2 y + -16 \, x^2 y^2 - 12 \, x^2 y - 16 \, xy^2 - (6 \, x^2 y^2 - 4 \, xy^2) = -26 \, x^2 y^2 - 2 \, x^2 y - 12 \, xy^2 \\ &[4] \quad -54 \, x^2 y^2 + 12 \, xy - (-36 \, xy^2 - 36 \, xy) + (12 \, x^2 y^2 - 54 \, x^2 y) = -42 \, x^2 y^2 - 54 \, x^2 y + 36 \, xy^2 + 48 \, xy \end{aligned}$$

$$[5] \quad -16\,x^2y^2 - 48\,xy^2 - 32\,xy + 16\,x^2y^2 - 64\,x^2y + 16\,xy^2 - (-60\,x^2y + 32\,xy) = \\ -4\,x^2y - 32\,xy^2 - 64\,xy \\ [6] \quad -15\,x^2y^2 + 25\,x^2y + 50\,xy^2 + -15\,x^2y^2 + 20\,x^2y + 10\,xy^2 - (15\,x^2y^2 - 20\,xy^2 + 20\,xy) = \\ -45\,x^2y^2 + 45\,x^2y + 80\,xy^2 - 20\,xy \\ [7] \quad 6\,xy^2 + 12\,xy - (108\,x^2y - 36\,xy) + (-144\,x^2y) = \\ -252\,x^2y + 6\,xy^2 + 48\,xy \\ [8] \quad 49\,x^2y - 28\,xy^2 + 28\,xy^2 + 175\,xy - (-294\,xy^2 - 7\,xy) = \\ 49\,x^2y + 294\,xy^2 + 182\,xy \\ [9] \quad -8\,x^2y^2 + 24\,x^2y + 192\,xy + 16\,x^2y^2 - 24\,x^2y - (128\,x^2y^2 + 256\,x^2y) = \\ -120\,x^2y^2 - 256\,x^2y + 192\,xy \\ [10] \quad 324\,x^2y^2 - 18\,x^2y + 162\,xy^2 - (-243\,x^2y^2 - 54\,xy) + (162\,x^2y^2 + 324\,xy^2 - 324\,xy) = \\ 729\,x^2y^2 - 18\,x^2y + 486\,xy^2 - 270\,xy \\ \end{cases}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

[1]
$$(0) \cdot (0) = 0$$

[2] $(-3b^3x^3y^2z^3) \cdot (-4b^2x^2y^2z) = 12b^5x^5y^4z^4$
[3] $(8b^3xy^2z) \cdot (-24b^3x^2y^3z^2) = -192b^6x^3y^5z^3$
[4] $(3b^2x^3y^2z^2) \cdot (108bx^2y^2z) = 324b^3x^5y^4z^3$
[5] $(-32bxyz^3) \cdot (-192bxy^3z^2) = 6144b^2x^2y^4z^5$
[6] $(10b^3xy^3z^2) \cdot (10b^3xy^2z^3) = 100b^6x^2y^5z^5$
[7] $(108b^3xy^2z^3) \cdot (432b^2xyz^2) = 46656b^5x^2y^3z^5$
[8] $(-7b^3xy^3z) \cdot (-98b^3x^2yz) = 686b^6x^3y^4z^2$
[9] $(-16b^3x^3y^3z^2) \cdot (-128bx^2y^2z) = 2048b^4x^5y^5z^3$
[10] $(-36b^2x^3y^3z) \cdot (162b^3x^2yz^2) = -5832b^5x^5y^4z^3$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(3x) \cdot (x^2 - 2x) = 3x^3 - 6x^2$$

[2] $(3x) \cdot (-5x^2) = -15x^3$
[3] $(-x^2) \cdot (-x^2 + 2x) = x^4 - 2x^3$
[4] $(2x^2) \cdot (-5x^2 - 7x) = -10x^4 - 14x^3$
[5] $(-2x) \cdot (-6x) = 12x^2$
[6] $(-4x) \cdot (5x^2 - 7x) = -20x^3 + 28x^2$
[7] $(4x) \cdot (8x^2 + x) = 32x^3 + 4x^2$
[8] $(-x^2) \cdot (-x) = x^3$
[9] $(x) \cdot (-4x^2 - 3x) = -4x^3 - 3x^2$
[10] $(3x) \cdot (-x^2 + 2x) = -3x^3 + 6x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (6\,x)\cdot(-3\,x) = -18\,x^2 \\ &[2] \quad (-x^2+4\,x)\cdot(-x) = x^3-4\,x^2 \\ &[3] \quad (-2\,x)\cdot(-x^2-2\,x) = 2\,x^3+4\,x^2 \\ &[4] \quad (-4\,x^2+x)\cdot(6\,x^2+4\,x) = -24\,x^4-10\,x^3+4\,x^2 \\ &[5] \quad (5\,x)\cdot(4\,x) = 20\,x^2 \\ &[6] \quad (2\,x^2-x)\cdot(-x) = -2\,x^3+x^2 \end{aligned}$$

[7]
$$(3x^2) \cdot (2x^2 - 3x) = 6x^4 - 9x^3$$

[8] $(2x^2 - 4x) \cdot (4x^2 - 4x) = 8x^4 - 24x^3 + 16x^2$

[9]
$$(3x^2 + 3x) \cdot (2x^2 - 7x) = 6x^4 - 15x^3 - 21x^2$$

[10]
$$(-4x^2 + x) \cdot (3x^2 - 2x) = -12x^4 + 11x^3 - 2x^2$$

[10]
$$(-4x^2 + x) \cdot (3x^2 - 2x) = -12x^4 + 11x^3 - 2x^3$$

[11]
$$(-6x^2) \cdot (4x^2) = -24x^4$$

[12]
$$(-2x^2 + x) \cdot (-4x^2 - 2x) = 8x^4 - 2x^2$$

[13]
$$(-x^2 + 2x) \cdot (8x^2 - x) = -8x^4 + 17x^3 - 2x^2$$

[14]
$$(0) \cdot (x) = 0$$

[15]
$$(3x^2 - x) \cdot (-5x^2 + 4x) = -15x^4 + 17x^3 - 4x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^2 + 4x) \cdot (2x^3 + 4x^2) = -2x^5 + 4x^4 + 16x^3$$

[2]
$$(-2x^3) \cdot (-x^3 - x^2 + 2x) = 2x^6 + 2x^5 - 4x^4$$

[3]
$$(2x^2 - 3x) \cdot (-4x^3 + x^2) = -8x^5 + 14x^4 - 3x^3$$

[4]
$$(-3x^3 - 7x^2) \cdot (-x^2 + 2x) = 3x^5 + x^4 - 14x^3$$

[5]
$$(2x^3 - 3x^2) \cdot (-4x^3 - x^2 + 3x) = -8x^6 + 10x^5 + 9x^4 - 9x^3$$

[6]
$$(-x^2-4x)\cdot(-5x^3+x^2-4x)=5x^5+19x^4+16x^2$$

[7]
$$(0) \cdot (-2x^3) = 0$$

[8]
$$(2x^2 + 3x) \cdot (-x^3 + 5x) = -2x^5 - 3x^4 + 10x^3 + 15x^2$$

[9]
$$(-3x^2 + 4x) \cdot (-2x^3 + 2x^2 + 4x) = 6x^5 - 14x^4 - 4x^3 + 16x^2$$

[10]
$$(x^3 + 2x^2) \cdot (5x^2 - 4x) = 5x^5 + 6x^4 - 8x^3$$

[11]
$$(3x^3 - 4x) \cdot (-5x^3 - 4x^2 + x) = -15x^6 - 12x^5 + 23x^4 + 16x^3 - 4x^2$$

[12]
$$(x^3 + 4x) \cdot (5x^3 + 2x^2 - 4x) = 5x^6 + 2x^5 + 16x^4 + 8x^3 - 16x^2$$

[13]
$$(x^2 - 3x) \cdot (x^3 + 6x) = x^5 - 3x^4 + 6x^3 - 18x^2$$

[14]
$$(0) \cdot (-5x^3 - 5x) = 0$$

[15]
$$(-x^3 + 2x^2) \cdot (x^3 + 4x^2 - 4x) = -x^6 - 2x^5 + 12x^4 - 8x^3$$

[16]
$$(4x^3 - x^2 + x) \cdot (2x^3 - x^2) = 8x^6 - 6x^5 + 3x^4 - x^3$$

[17]
$$(-x^3 - 4x^2) \cdot (6x^3 - 3x) = -6x^6 - 24x^5 + 3x^4 + 12x^3$$

[18]
$$(-8x) \cdot (-x^3 + 3x^2 + 4x) = 8x^4 - 24x^3 - 32x^2$$

[19]
$$(-2x^3 + x^2) \cdot (-4x^3 + x) = 8x^6 - 4x^5 - 2x^4 + x^3$$

[20]
$$(4x^3 - 4x) \cdot (2x^3 + 4x^2 + 2x) = 8x^6 + 16x^5 - 16x^3 - 8x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^2y + 4xy^2) \cdot (x^2y^2 + 2x^2y) = -x^4y^3 + 4x^3y^4 - 2x^4y^2 + 8x^3y^3$$

[2]
$$(-2x^2y) \cdot (-4x^2y^2 + 4x^2y - xy) = 8x^4y^3 - 8x^4y^2 + 2x^3y^2$$

[3]
$$(-2x^2y^2 + xy^2) \cdot (4x^2y^2 - 2x^2y) = -8x^4y^4 + 4x^4y^3 + 4x^3y^4 - 2x^3y^3$$

[4]
$$(-3x^2y) \cdot (6x^2y^2 + x^2y) = -18x^4y^3 - 3x^4y^2$$

[5]
$$(3x^2y + 3xy) \cdot (x^2y + 2xy^2 - xy) = 3x^4y^2 + 6x^3y^3 + 6x^2y^3 - 3x^2y^2$$

[6]
$$(-xy) \cdot (x^2y^2 + 3x^2y + 3xy) = -x^3y^3 - 3x^3y^2 - 3x^2y^2$$

[7]
$$(-x^2y^2 - 3x^2y) \cdot (4x^2y - xy) = -4x^4y^3 - 12x^4y^2 + x^3y^3 + 3x^3y^2$$