1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 4x^5 - x + -x^5 + 3x^3 + 4x + -3x^6 + 3x^3 + 4x^2 = -3x^6 + 3x^5 + 6x^3 + 4x^2 + 3x$$

$$[2] \quad 2x^4 - 4x^3 - 2x^2 + -3x^6 - 4x^5 + x + -2x^6 - 3x^2 - 3x = -5x^6 - 4x^5 + 2x^4 - 4x^3 - 5x^2 - 2x$$

$$[3] \quad 2x^4 - 3x^3 + -2x^3 + -3x^5 + x^4 + x = -3x^5 + 3x^4 - 5x^3 + x$$

$$[4] \quad 3x^6 + 2x^3 - 2x^2 + -x^6 + x^3 + 2x^3 - 3x = 2x^6 + 5x^3 - 2x^2 - 3x$$

$$[5] \quad 3x^6 - 3x^2 + 2x^3 - 2x^2 - x + -x^4 + 4x^2 + 4x = 3x^6 - x^4 + 2x^3 - x^2 + 3x$$

$$[6] \quad x^6 - 3x^5 + -x^6 + 5x^5 + -5x^6 + x^2 = -5x^6 + 2x^5 + x^2$$

$$[7] \quad 2x^3 - 3x^2 + 2x + 2x^6 + 3x^3 + 2x^6 - 2x^2 = 4x^6 + 5x^3 - 5x^2 + 2x$$

$$[8] \quad -x^3 - 5x^2 + (-4x^5 + 4x^4 - x) + (-2x^5 + 4x^3 - 4x^2) = -6x^5 + 4x^4 + 3x^3 - 9x^2 - x$$

$$[9] \quad 2x^4 - 4x^3 + 4x + -3x^6 + 4x^3 + 3x + (-x^4 - 4x^3 - x^2) = -3x^6 + x^4 - 4x^3 - x^2 + 7x$$

$$[10] \quad x^6 + 8x^5 + x^6 - 2x^5 + x^3 + -4x^5 - 4x^4 - 2x^2 = 2x^6 + 2x^5 - 4x^4 + x^3 - 2x^2$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0 + 0 + 0 = 0 \\ & [2] \quad 4 \, x^2 y^2 + x^2 y - x y^2 + 2 \, x^2 y + 4 \, x y + 3 \, x^2 y + 2 \, x y^2 = 4 \, x^2 y^2 + 6 \, x^2 y + x y^2 + 4 \, x y \\ & [3] \quad 2 \, x^2 y + -10 \, x^2 y^2 + (-8 \, x y^2 + 8 \, x y) = -10 \, x^2 y^2 + 2 \, x^2 y - 8 \, x y^2 + 8 \, x y \\ & [4] \quad 15 \, x^2 y^2 - 9 \, x^2 y + -36 \, x^2 y + 63 \, x y + 9 \, x^2 y^2 = 24 \, x^2 y^2 - 45 \, x^2 y + 63 \, x y \\ & [5] \quad 16 \, x^2 y^2 - 16 \, x^2 y - 48 \, x y + -16 \, x^2 y + -32 \, x^2 y + 4 \, x y = 16 \, x^2 y^2 - 64 \, x^2 y - 44 \, x y \\ & [6] \quad 25 \, x^2 y + 10 \, x y + -100 \, x y^2 - 20 \, x y + -25 \, x^2 y^2 - 75 \, x^2 y + 20 \, x y^2 = -25 \, x^2 y^2 - 50 \, x^2 y - 80 \, x y^2 - 10 \, x y \\ & [7] \quad 36 \, x^2 y + 12 \, x y^2 + 108 \, x y + -108 \, x^2 y^2 + 144 \, x y^2 - 144 \, x y + -24 \, x^2 y - 72 \, x y = -108 \, x^2 y^2 + 12 \, x^2 y + 156 \, x y^2 - 108 \, x y \\ & [8] \quad -343 \, x y^2 + 7 \, x y + (-21 \, x^2 y^2 - 77 \, x y^2) + (-14 \, x^2 y^2 + 196 \, x y^2 - 28 \, x y) = -35 \, x^2 y^2 - 224 \, x y^2 - 21 \, x y \\ & [9] \quad -32 \, x^2 y^2 + 64 \, x^2 y + 24 \, x y + (-168 \, x^2 y + 16 \, x y^2) + (-192 \, x^2 y^2 - 8 \, x y^2 + 64 \, x y) = -224 \, x^2 y^2 - 104 \, x^2 y + 8 \, x y^2 + 88 \, x y \\ & [10] \quad 18 \, x^2 y^2 - 36 \, x y^2 + 81 \, x y + 162 \, x^2 y^2 - 72 \, x y^2 + 162 \, x^2 y^2 = 342 \, x^2 y^2 - 108 \, x y^2 + 81 \, x y \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

[1]
$$0 - (0) + (0) = 0$$

[2] $-3x^2y^2 + 3xy^2 + 2x^2y^2 + xy^2 - (2x^2y) = -x^2y^2 - 2x^2y + 4xy^2$
[3] $2x^2y^2 + 4xy^2 + -6x^2y + 4xy^2 + 2xy - (8x^2y + 2xy^2) = 2x^2y^2 - 14x^2y + 6xy^2 + 2xy$
[4] $-3x^2y^2 - 6xy^2 - 27xy - (-12x^2y^2 + 36xy^2 + 36xy) + (6x^2y + 36xy^2 + 3xy) = 9x^2y^2 + 6x^2y - 6xy^2 - 60xy$
[5] $12x^2y^2 + 20xy^2 + 4x^2y^2 + 64xy^2 - (4x^2y^2 + 4xy) = 12x^2y^2 + 84xy^2 - 4xy$

$$[6] \quad -100 \, x^2 y - 10 \, xy^2 + 10 \, xy + -20 \, x^2 y - (100 \, x^2 y - 50 \, xy^2 - 20 \, xy) = -220 \, x^2 y + 40 \, xy^2 + 30 \, xy$$

$$[7] \quad -6 \, x^2 y - 144 \, xy^2 + 108 \, xy - (12 \, x^2 y + 108 \, xy^2) + (6 \, x^2 y^2 + 126 \, x^2 y) = 6 \, x^2 y^2 + 108 \, x^2 y - 252 \, xy^2 + 108 \, xy$$

$$[8] \quad 84 \, xy^2 + -7 \, x^2 y^2 + 196 \, xy^2 - 7 \, xy - (14 \, xy^2 + 147 \, xy) = -7 \, x^2 y^2 + 266 \, xy^2 - 154 \, xy$$

$$[9] \quad 0 + -128 \, xy^2 - 128 \, xy - (16 \, x^2 y^2 + 256 \, x^2 y + 32 \, xy) = -16 \, x^2 y^2 - 256 \, x^2 y - 128 \, xy^2 - 160 \, xy$$

$$[10] \quad 27 \, x^2 y - (324 \, x^2 y^2 - 27 \, x^2 y + 27 \, xy) + (18 \, xy) = -324 \, x^2 y^2 + 54 \, x^2 y - 9 \, xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (b^3x^3y^2z^2) \cdot (-3\,b^3x^2yz^3) = -3\,b^6x^5y^3z^5 \\ &[3] \quad (-32\,b^2x^3y^2z^2) \cdot (-8\,b^3x^3y^3z) = 256\,b^5x^6y^5z^3 \\ &[4] \quad (-3\,bx^3y^2z^2) \cdot (27\,b^2x^3yz^2) = -81\,b^3x^6y^3z^4 \\ &[5] \quad (64\,bx^3y^3z^2) \cdot (48\,bxyz^3) = 3072\,b^2x^4y^4z^5 \\ &[6] \quad (50\,bx^3y^2z^3) \cdot (25\,b^2x^3yz) = 1250\,b^3x^6y^3z^4 \\ &[7] \quad (144\,b^3x^3y^3z) \cdot (648\,bx^2yz) = 93312\,b^4x^5y^4z^2 \\ &[8] \quad (98\,b^3x^2y^3z) \cdot (-1372\,bxy^2z^2) = -134456\,b^4x^3y^5z^3 \\ &[9] \quad (-24\,bx^3yz^3) \cdot (-1536\,bxy^3z^3) = 36864\,b^2x^4y^4z^6 \\ &[10] \quad (-162\,bxyz) \cdot (-243\,b^3x^2yz^3) = 39366\,b^4x^3y^2z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-4x^2) \cdot (-5x^2 - 3x) = 20x^4 + 12x^3$$

[2] $(x) \cdot (-x^2 + 7x) = -x^3 + 7x^2$
[3] $(-4x) \cdot (x^2 + 11x) = -4x^3 - 44x^2$
[4] $(3x) \cdot (3x) = 9x^2$
[5] $(3x) \cdot (3x^2 + 2x) = 9x^3 + 6x^2$
[6] $(-x^2) \cdot (-x^2 + 5x) = x^4 - 5x^3$
[7] $(-x^2) \cdot (-4x^2) = 4x^4$
[8] $(-3x) \cdot (-2x^2 - x) = 6x^3 + 3x^2$
[9] $(-2x^2) \cdot (-4x^2 + 3x) = 8x^4 - 6x^3$
[10] $(3x) \cdot (-3x) = -9x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (2\,x)\cdot(3\,x^2+3\,x) = 6\,x^3+6\,x^2 \\ &[2] \quad (-2\,x^2-4\,x)\cdot(-3\,x) = 6\,x^3+12\,x^2 \\ &[3] \quad (-4\,x^2+2\,x)\cdot(6\,x) = -24\,x^3+12\,x^2 \\ &[4] \quad (-2\,x^2+x)\cdot(4\,x^2+3\,x) = -8\,x^4-2\,x^3+3\,x^2 \\ &[5] \quad (-3\,x^2+2\,x)\cdot(-2\,x^2-3\,x) = 6\,x^4+5\,x^3-6\,x^2 \\ &[6] \quad (-3\,x^2)\cdot(-3\,x^2+6\,x) = 9\,x^4-18\,x^3 \\ &[7] \quad (5\,x)\cdot(9\,x^2) = 45\,x^3 \end{aligned}$$

[8]
$$(x^2) \cdot (-x^2 - 3x) = -x^4 - 3x^3$$

[9] $(-2x^2 + 4x) \cdot (-5x^2 - 2x) = 10x^4 - 16x^3 - 8x^2$

[10]
$$(-2x^2 + 4x) \cdot (x^2) = -2x^4 + 4x^3$$

[11]
$$(6x) \cdot (-3x^2 - 2x) = -18x^3 - 12x^2$$

[12]
$$(-2x^2) \cdot (-4x^2 + 3x) = 8x^4 - 6x^3$$

[13]
$$(0) \cdot (-2x) = 0$$

[14]
$$(-3x^2 + 2x) \cdot (x) = -3x^3 + 2x^2$$

[15]
$$(-3x^2) \cdot (4x^2 + 4x) = -12x^4 - 12x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-7x^2) \cdot (2x^3 + 2x^2 - 4x) = -14x^5 - 14x^4 + 28x^3$$

[2]
$$(3x^2 - 2x) \cdot (-2x^3 + 2x^2 - 4x) = -6x^5 + 10x^4 - 16x^3 + 8x^2$$

[3]
$$(x^3 + x) \cdot (x^2 + x) = x^5 + x^4 + x^3 + x^2$$

[4]
$$(-2x^3 + 3x) \cdot (-4x^3) = 8x^6 - 12x^4$$

[5]
$$(-4x^2 + 3x) \cdot (10x^3 + 3x^2) = -40x^5 + 18x^4 + 9x^3$$

[6]
$$(-6x^3) \cdot (3x^3 - 2x^2 - x) = -18x^6 + 12x^5 + 6x^4$$

[7]
$$(-3x^3 + x^2 + 3x) \cdot (-2x^3 + 3x) = 6x^6 - 2x^5 - 15x^4 + 3x^3 + 9x^2$$

[8]
$$(-x^2 - x) \cdot (2x^3 + 3x) = -2x^5 - 2x^4 - 3x^3 - 3x^2$$

[9]
$$(-x) \cdot (2x^2 - 5x) = -2x^3 + 5x^2$$

[10]
$$(-2x^3 - 4x^2) \cdot (x^2 - 2x) = -2x^5 + 8x^3$$

[11]
$$(-x) \cdot (11x^3 - 4x^2) = -11x^4 + 4x^3$$

[12]
$$(x^2) \cdot (x) = x^3$$

[13]
$$(x^2 - 3x) \cdot (3x^3 - 4x^2) = 3x^5 - 13x^4 + 12x^3$$

[14]
$$(-3x^2 - 4x) \cdot (-7x^3 - 2x^2 + x) = 21x^5 + 34x^4 + 5x^3 - 4x^2$$

[15]
$$(7x^2) \cdot (-4x^3 - 2x^2 + 2x) = -28x^5 - 14x^4 + 14x^3$$

[16]
$$(-6x^3) \cdot (2x^3 + 2x^2) = -12x^6 - 12x^5$$

[17]
$$(-3x^3 + 3x) \cdot (2x^2 + 9x) = -6x^5 - 27x^4 + 6x^3 + 27x^2$$

[18]
$$(x^3) \cdot (-4x^2 + 2x) = -4x^5 + 2x^4$$

[19]
$$(3x^3 - 2x^2 - x) \cdot (x^3 + 3x^2 + 3x) = 3x^6 + 7x^5 + 2x^4 - 9x^3 - 3x^2$$

[20]
$$(-4x^3 - 3x^2) \cdot (-4x^3 + x^2) = 16x^6 + 8x^5 - 3x^4$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(4x^2y^2 + 3x^2y) \cdot (-2x^2y^2 - x^2y + 4xy^2) = -8x^4y^4 - 10x^4y^3 + 16x^3y^4 - 3x^4y^2 + 12x^3y^3$$

[3]
$$(4x^2y + 3xy^2) \cdot (-2x^2y^2 + 3x^2y) = -8x^4y^3 - 6x^3y^4 + 12x^4y^2 + 9x^3y^3$$

$$[3] \quad (4x^2y + 3xy^2) \cdot (-2x^2y^2 + 3x^2y) = -8x^2y^3 - 6x^3y^2 + 12x^2y^2 + 9x^3y^3$$

$$[4] \quad (-4x^2y + 4xy) \cdot (-4x^2y + 4xy^2 + 3xy) = 16x^4y^2 - 16x^3y^3 - 28x^3y^2 + 16x^2y^3 + 12x^2y^2$$

[5]
$$(-2xy^2) \cdot (x^2y^2 + 3x^2y - 2xy^2) = -2x^3y^4 - 6x^3y^3 + 4x^2y^4$$

[6]
$$(3x^2y - xy) \cdot (-5x^2y^2 + 4xy) = -15x^4y^3 + 5x^3y^3 + 12x^3y^2 - 4x^2y^2$$

[7]
$$(-2x^2y^2 - xy) \cdot (3x^2y^2 - 7x^2y) = -6x^4y^4 + 14x^4y^3 - 3x^3y^3 + 7x^3y^2$$