1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 2x^2 + x + 4x^6 - 2x^5 - 2x^4 + x^6 + 4x^4 + x^3 = 5x^6 - 2x^5 + 2x^4 + x^3 + 2x^2 + x \\ [2] \quad 4x^6 - 4x^5 + x^3 + -3x^6 + x^4 - 3x + 2x^6 - 4x^2 + 4x = 3x^6 - 4x^5 + x^4 + x^3 - 4x^2 + x \\ [3] \quad 3x^4 - 3x^3 - x^2 + -4x^6 - 4x^5 + x^6 + 4x^5 + 3x^3 = -3x^6 + 3x^4 - x^2 \\ [4] \quad 2x^6 - 3x^4 + 4x + -4x^6 - x^3 + 3x^6 - 3x^5 + 2x = x^6 - 3x^5 - 3x^4 - x^3 + 6x \\ [5] \quad -x^4 + 3x + (-x^6 + x^4 + 2x) + (-x^6 + 3x^4) = -2x^6 + 3x^4 + 5x \\ [6] \quad 4x^6 + 3x^5 + 4x^3 + x^3 + 7x + -4x^6 + 3x^5 + 2x^2 = 6x^5 + 5x^3 + 2x^2 + 7x \\ [7] \quad 3x^5 - x^3 + -x^4 - 5x + -2x^6 + 3x^4 - 2x = -2x^6 + 3x^5 + 2x^4 - x^3 - 7x \\ [8] \quad 2x^6 - 2x^2 + 4x^6 - 3x^4 + 3x + -4x^5 - 3x^4 = 6x^6 - 4x^5 - 6x^4 - 2x^2 + 3x \\ [9] \quad 4x^6 - 4x^3 + 2x + -x^4 + 4x^2 + 4x + 2x^6 + 2x^2 - x = 6x^6 - x^4 - 4x^3 + 6x^2 + 5x \\ [10] \quad 3x^6 - 4x^4 + 3x^2 + 3x^6 + 2x^4 + x + -3x^3 + x^2 = 6x^6 - 2x^4 - 3x^3 + 4x^2 + x \\ [10] \quad 3x^6 - 4x^4 + 3x^2 + 3x^6 + 2x^4 + x + -3x^3 + x^2 = 6x^6 - 2x^4 - 3x^3 + 4x^2 + x \\ [10] \quad 3x^6 - 4x^4 + 3x^2 + 3x^6 + 2x^4 + x + -3x^3 + x^2 = 6x^6 - 2x^4 - 3x^3 + 4x^2 + x \\ [10] \quad 3x^6 - 4x^4 + 3x^2 + 3x^6 + 2x^4 + x + -3x^3 + x^2 = 6x^6 - 2x^4 - 3x^3 + 4x^2 + x \\ [10] \quad 3x^6 - 3x^4 + 3x^4 + 3x^2 + 3x^6 + 2x^4 + x + -3x^3 + x^2 + 2x^2 - x \\ [10] \quad 3x^6 - 3x^4 + 3x^4 + 3x^2 + 3x^6 + 2x^4 + x + -3x^3 + x^2 + 2x^2 - x \\ [10] \quad 3x^6 - 3x^4 + 3x^4 + 3x^4 + 3x^4 + x^4 + x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0 + 0 + 0 = 0 \\ & [2] \quad 2x^2y + 6xy^2 + -2x^2y^2 - 3x^2y + xy^2 + 2x^2y^2 + x^2y + 3xy^2 = 10xy^2 \\ & [3] \quad -8x^2y^2 + 8x^2y - 16xy^2 + (-4xy^2 - 2xy) + (-6x^2y^2 - 12xy^2 - 2xy) = -14x^2y^2 + 8x^2y - 32xy^2 - 4xy \\ & [4] \quad 27x^2y^2 - 18x^2y + -27x^2y - 9xy^2 + 36x^2y^2 + 39xy = 63x^2y^2 - 45x^2y - 9xy^2 + 39xy \\ & [5] \quad 64x^2y^2 - 4xy^2 + -16x^2y^2 - 72x^2y + (-32xy^2 - 4xy) = 48x^2y^2 - 72x^2y - 36xy^2 - 4xy \\ & [6] \quad 50x^2y^2 - 5x^2y + 20xy^2 + 100x^2y^2 + 20x^2y^2 + 15xy^2 + 75xy = 170x^2y^2 - 5x^2y + 35xy^2 + 75xy \\ & [7] \quad 36xy + -72x^2y + 216xy + -12x^2y - 108xy^2 + 36xy = -84x^2y - 108xy^2 + 288xy \\ & [8] \quad 147x^2y + 147xy^2 - 21xy + 14x^2y + 35xy^2 + -7xy^2 + 21xy = 161x^2y + 175xy^2 \\ & [9] \quad 256x^2y^2 + 256xy + -24x^2y^2 + 128x^2y - 32xy + 192x^2y^2 - 32x^2y + 128xy^2 = 424x^2y^2 + 96x^2y + 128xy^2 + 224xy \\ & [10] \quad 234x^2y^2 - 36xy^2 + 224xy \\ & [10] \quad 234x^2y^2 - 36xy^2 + -324x^2y^2 - 72x^2y + -243x^2y^2 + 225xy = -333x^2y^2 - 72x^2y - 36xy^2 + 225xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 3\,x^2y - 3\,xy^2 + 4\,xy + -2\,x^2y + 2\,xy^2 - (-2\,x^2y^2) = 2\,x^2y^2 + x^2y - xy^2 + 4\,xy \\ &[3] \quad -8\,x^2y + 8\,xy^2 - 8\,xy + 14\,x^2y + 8\,xy^2 - (-8\,x^2y^2 - 14\,xy) = 8\,x^2y^2 + 6\,x^2y + 16\,xy^2 + 6\,xy \\ &[4] \quad -36\,x^2y^2 + 12\,x^2y + 9\,xy - (39\,x^2y + 36\,xy) + (-3\,x^2y^2 - 18\,xy^2 - 36\,xy) = -39\,x^2y^2 - 27\,x^2y - 18\,xy^2 - 63\,xy \\ &[5] \quad -16\,x^2y^2 + 28\,x^2y + -32\,x^2y^2 + 8\,xy^2 - (16\,x^2y + 28\,xy^2) = -48\,x^2y^2 + 12\,x^2y - 20\,xy^2 \end{aligned}$$

$$\begin{aligned} & [6] \quad -15\,x^2y + 15\,xy^2 - 75\,xy + 15\,x^2y^2 - 5\,xy^2 - 15\,xy - (-30\,x^2y + 10\,xy) = \\ & 15\,x^2y^2 + 15\,x^2y + 10\,xy^2 - 100\,xy \\ & [7] \quad -72\,x^2y^2 + 42\,xy^2 - (-24\,x^2y) + (-108\,x^2y^2 - 96\,x^2y) = -180\,x^2y^2 - 72\,x^2y + \\ & 42\,xy^2 \\ & [8] \quad 147\,x^2y^2 - 21\,xy^2 - 196\,xy + -14\,x^2y^2 + 147\,xy^2 + 14\,xy - (140\,x^2y^2 + 21\,xy^2) = \\ & -7\,x^2y^2 + 105\,xy^2 - 182\,xy \\ & [9] \quad 224\,x^2y^2 + 16\,xy + -192\,x^2y^2 - 120\,x^2y - (-128\,x^2y - 128\,xy^2 - 32\,xy) = \\ & 32\,x^2y^2 + 8\,x^2y + 128\,xy^2 + 48\,xy \\ & [10] \quad -324\,x^2y^2 - 9\,xy^2 - 27\,xy - (27\,x^2y^2) + (-162\,x^2y + 243\,xy^2 - 81\,xy) = \\ & -351\,x^2y^2 - 162\,x^2y + 234\,xy^2 - 108\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (bx^2y^2z^3) \cdot (4\,b^3x^2y^3z) = 4\,b^4x^4y^5z^4 \\ &[3] \quad (16\,b^3x^3y^3z^2) \cdot (-2\,b^3x^2y^3z) = -32\,b^6x^5y^6z^3 \\ &[4] \quad (27\,bx^3y^3z^2) \cdot (9\,bx^3yz^2) = 243\,b^2x^6y^4z^4 \\ &[5] \quad (32\,bx^2y^3z^3) \cdot (-192\,bxy^3z) = -6144\,b^2x^3y^6z^4 \\ &[6] \quad (-5\,bxy^3z^2) \cdot (-125\,b^2x^3y^3z) = 625\,b^3x^4y^6z^3 \\ &[7] \quad (-144\,b^2xyz^3) \cdot (-12\,bx^3yz^2) = 1728\,b^3x^4y^2z^5 \\ &[8] \quad (-686\,bx^2yz^2) \cdot (98\,b^3xyz^2) = -67228\,b^4x^3y^2z^4 \\ &[9] \quad (-192\,b^2x^3yz^3) \cdot (-24\,b^3xy^3z^3) = 4608\,b^5x^4y^4z^6 \\ &[10] \quad (27\,b^3x^3y^2z) \cdot (729\,bx^3y^2z^2) = 19683\,b^4x^6y^4z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x) \cdot (x^2 + 3\,x) = -x^3 - 3\,x^2 \\ &[2] \quad (-x^2) \cdot (-3\,x^2 + 4\,x) = 3\,x^4 - 4\,x^3 \\ &[3] \quad (-4\,x^2) \cdot (-3\,x^2 - 4\,x) = 12\,x^4 + 16\,x^3 \\ &[4] \quad (-3\,x) \cdot (x^2 + 2\,x) = -3\,x^3 - 6\,x^2 \\ &[5] \quad (-2\,x) \cdot (-3\,x^2 - 5\,x) = 6\,x^3 + 10\,x^2 \\ &[6] \quad (3\,x^2) \cdot (4\,x^2 - 3\,x) = 12\,x^4 - 9\,x^3 \\ &[7] \quad (-3\,x) \cdot (3\,x^2 - 3\,x) = -9\,x^3 + 9\,x^2 \\ &[8] \quad (-4\,x^2) \cdot (4\,x^2) = -16\,x^4 \\ &[9] \quad (-4\,x) \cdot (x^2 + 6\,x) = -4\,x^3 - 24\,x^2 \\ &[10] \quad (-3\,x) \cdot (-4\,x^2 - 4\,x) = 12\,x^3 + 12\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x)\cdot(3\,x) = 12\,x^2 \\ &[2] \quad (-5\,x^2)\cdot(4\,x^2+5\,x) = -20\,x^4-25\,x^3 \\ &[3] \quad (-x)\cdot(2\,x^2-5\,x) = -2\,x^3+5\,x^2 \\ &[4] \quad (0)\cdot(-4\,x) = 0 \\ &[5] \quad (2\,x^2+4\,x)\cdot(-4\,x^2) = -8\,x^4-16\,x^3 \\ &[6] \quad (4\,x^2+x)\cdot(-x^2-4\,x) = -4\,x^4-17\,x^3-4\,x^2 \end{aligned}$$

$$[7] \quad (-3x^2) \cdot (-3x) = 9x^3$$

$$[8] \quad (4x^2 - x) \cdot (2x^2 + 4x) = 8x^4 + 14x^3 - 4x^2$$

$$[9] \quad (x^2 + x) \cdot (2x^2 + x) = 2x^4 + 3x^3 + x^2$$

$$[10] \quad (3x^2 + 3x) \cdot (-x^2 - 3x) = -3x^4 - 12x^3 - 9x^2$$

$$[11] \quad (-3x^2 + 2x) \cdot (x^2 + 5x) = -3x^4 - 13x^3 + 10x^2$$

$$[12] \quad (-4x^2 - 4x) \cdot (3x^2 + 4x) = -12x^4 - 28x^3 - 16x^2$$

$$[13] \quad (-3x^2 + x) \cdot (2x^2 - 3x) = -6x^4 + 11x^3 - 3x^2$$

$$[14] \quad (4x^2 + 4x) \cdot (2x^2 - x) = 8x^4 + 4x^3 - 4x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[15] $(6x^2) \cdot (4x^2) = 24x^4$

[1]
$$(x^3) \cdot (-x^3 + 2x) = -x^6 + 2x^4$$

[2] $(x^2 - x) \cdot (-4x^3 + x) = -4x^5 + 4x^4 + x^3 - x^2$
[3] $(x^2 - x) \cdot (-6x^3 + 4x) = -6x^5 + 6x^4 + 4x^3 - 4x^2$
[4] $(-2x^3 - x^2) \cdot (-x^2 + 2x) = 2x^5 - 3x^4 - 2x^3$
[5] $(4x^3 + 4x^2) \cdot (-5x^3 + 4x^2) = -20x^6 - 4x^5 + 16x^4$
[6] $(-2x^2) \cdot (2x^3 + 4x^2 + 4x) = -4x^5 - 8x^4 - 8x^3$
[7] $(-4x^2 + 6x) \cdot (-2x^3 - x^2) = 8x^5 - 8x^4 - 6x^3$
[8] $(3x^2 - x) \cdot (-3x^2 - 4x) = -9x^4 - 9x^3 + 4x^2$
[9] $(x^3 - 3x) \cdot (-3x^3 + 3x^2 + 3x) = -3x^6 + 3x^5 + 12x^4 - 9x^3 - 9x^2$
[10] $(-2x^3 - 3x^2) \cdot (2x^2 - 5x) = -4x^5 + 4x^4 + 15x^3$
[11] $(-x^2 - 3x) \cdot (3x^3 + 3x^2 - 8x) = -3x^5 - 12x^4 - x^3 + 24x^2$
[12] $(2x^3 - 4x^2) \cdot (-5x^3 - 2x) = -10x^6 + 20x^5 - 4x^4 + 8x^3$
[13] $(-3x) \cdot (4x^3 + 8x) = -12x^4 - 24x^2$
[14] $(-2x^3 + 4x^2) \cdot (-x^3 + 4x^2) = 2x^6 - 12x^5 + 16x^4$
[15] $(-4x^2 + 2x) \cdot (-2x^3 + 3x^2) = 8x^5 - 16x^4 + 6x^3$
[16] $(-6x^2 - 3x) \cdot (-4x^3 + x^2) = 24x^5 + 6x^4 - 3x^3$
[17] $(8x^2) \cdot (x^3 - 5x^2 + 3x) = 8x^5 - 40x^4 + 24x^3$
[18] $(-2x^3 + 4x) \cdot (4x^3 - 2x^2 + 4x) = -8x^6 + 4x^5 + 8x^4 - 8x^3 + 16x^2$
[19] $(3x^2 - 2x) \cdot (-x) = -3x^3 + 2x^2$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (2\,x^2y^2-3\,x^2y)\cdot(2\,x^2y) = 4\,x^4y^3-6\,x^4y^2 \\ &[2] \quad (-2\,x^2y-4\,xy^2)\cdot(2\,x^2y^2+xy) = -4\,x^4y^3-8\,x^3y^4-2\,x^3y^2-4\,x^2y^3 \\ &[3] \quad (-4\,x^2y^2+2\,x^2y)\cdot(xy) = -4\,x^3y^3+2\,x^3y^2 \\ &[4] \quad (4\,xy^2-2\,xy)\cdot(-3\,x^2y+2\,xy) = -12\,x^3y^3+6\,x^3y^2+8\,x^2y^3-4\,x^2y^2 \\ &[5] \quad (-3\,xy^2)\cdot(xy^2+6\,xy) = -3\,x^2y^4-18\,x^2y^3 \\ &[6] \quad (-3\,x^2y-3\,xy)\cdot(4\,x^2y^2-4\,x^2y+xy) = -12\,x^4y^3+12\,x^4y^2-12\,x^3y^3+9\,x^3y^2-3\,x^2y^2 \\ &[7] \quad (2\,xy^2)\cdot(2\,x^2y^2-x^2y+xy) = 4\,x^3y^4-2\,x^3y^3+2\,x^2y^3 \end{aligned}$$