1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 2x^6 - 3x^5 - 3x + -x^6 + x^2 + 3x + (-4x^6 - 3x^5 - 3x^4) = -3x^6 - 6x^5 - 3x^4 + x^2$$

$$[2] \quad 3x^6 + 2x^3 + x^2 + -4x^5 + x^3 + -3x^5 - 2x = 3x^6 - 7x^5 + 3x^3 + x^2 - 2x$$

$$[3] \quad x^6 - 3x^2 - 2x + -x^5 + x + x^6 + 8x^5 = 2x^6 + 7x^5 - 3x^2 - x$$

$$[4] \quad -4x^4 - 7x^2 + (-3x^4 + 3x^2 - 3x) + (-x^4 + 2x^2) = -8x^4 - 2x^2 - 3x$$

$$[5] \quad 4x^5 - 3x^3 + 4x + -7x^2 + 3x + 3x^6 - 4x^5 - 3x^2 = 3x^6 - 3x^3 - 10x^2 + 7x$$

$$[6] \quad x^6 + 2x^5 + 4x^2 + 3x^5 + 2x^4 + x + -4x^5 - 4x^4 - 2x^3 = x^6 + x^5 - 2x^4 - 2x^3 + 4x^2 + x$$

$$[7] \quad -3x^6 - 2x^4 - 2x^3 + (-4x^6 - 4x^5 - 2x^2) + (-2x^6 + 3x^5 + 4x^3) = -9x^6 - x^5 - 2x^4 + 2x^3 - 2x^2$$

$$[8] \quad -6x^2 + 2x + (-3x^5 + x^3 - 2x) + (-4x^5 + 3x^2) = -7x^5 + x^3 - 3x^2$$

[9] $-3x + (-3x^6 - 4x^5 - x^4) + (-3x^6 + x^3 - x^2) = -6x^6 - 4x^5 - x^4 + x^3 - x^2 - 3x$ [10] $x^5 + 3x^3 - 4x^2 + -2x^6 + 2x^3 + 4x^2 + -3x^6 - 5x^2 = -5x^6 + x^5 + 5x^3 - 5x^2$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 4x^2y^2-2x^2y-4xy+4xy^2+4xy+3x^2y+4xy=4x^2y^2+x^2y+4xy^2+4xy^2\\ [3] \quad -8xy^2+(-4x^2y^2+4xy)+(-24x^2y-12xy)=-4x^2y^2-24x^2y-8xy^2-8xy \\ [4] \quad 18x^2y^2+3x^2y-12xy+-9x^2y^2-27xy^2-6xy+-9x^2y^2-12xy^2-9xy=3x^2y-39xy^2-27xy \\ [5] \quad -24x^2y+48xy^2+(-52x^2y^2-4xy)+(-32x^2y^2-8x^2y-16xy)=-84x^2y^2-32x^2y+48xy^2-20xy \\ [6] \quad 15x^2y^2+-100x^2y-20xy^2+100xy+-50x^2y+10xy^2+100xy=15x^2y^2-150x^2y-10xy^2+200xy \\ [7] \quad 36x^2y+36xy^2+-6x^2y^2+18x^2y-144xy+(-6x^2y^2-72x^2y-144xy)=-12x^2y^2-18x^2y+36xy^2-288xy \\ [8] \quad 70x^2y+21xy+-70x^2y+98xy+294xy^2+21xy=294xy^2+140xy \\ [9] \quad 24x^2y-24xy^2+64xy+64x^2y+160xy^2+-16x^2y-192xy^2=72x^2y-56xy^2+64xy \\ [10] \quad 162x^2y^2-279xy^2+126x^2y^2-81x^2y+63x^2y^2+9xy=351x^2y^2-81x^2y-279xy^2+9xy \\ [10] \quad 162x^2y^2-279xy^2+126x^2y^2-81x^2y+63x^2y^2+9xy=351x^2y^2-81x^2y-279xy^2+9xy \\ [279 xy^2+9xy]$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -3\,x^2y^2 + x^2y + 3\,xy^2 + -x^2y^2 - (-x^2y - xy^2 - xy) = -4\,x^2y^2 + 2\,x^2y + 4\,xy^2 + xy \\ &[3] \quad 4\,x^2y + 8\,xy^2 + -2\,x^2y^2 - (-8\,xy^2) = -2\,x^2y^2 + 4\,x^2y + 16\,xy^2 \\ &[4] \quad -12\,x^2y^2 - 36\,x^2y + 36\,xy - (-21\,x^2y + 6\,xy^2) + (-9\,x^2y^2 - 27\,xy^2 - 12\,xy) = \\ -21\,x^2y^2 - 15\,x^2y - 33\,xy^2 + 24\,xy \\ &[5] \quad -32\,x^2y - 12\,xy^2 - 48\,xy + 64\,x^2y^2 + 64\,xy^2 + 16\,xy - (-60\,x^2y^2 + 12\,x^2y) = \\ 124\,x^2y^2 - 44\,x^2y + 52\,xy^2 - 32\,xy \end{aligned}$$

$$\begin{aligned} & [6] \quad -25\,x^2y + 5\,xy^2 - 20\,xy + 15\,x^2y^2 - 5\,x^2y + 15\,xy^2 - (5\,x^2y^2 + 75\,x^2y - 20\,xy) = \\ & 10\,x^2y^2 - 105\,x^2y + 20\,xy^2 \\ & [7] \quad -114\,x^2y - 144\,xy - (-108\,x^2y^2 + 12\,x^2y + 72\,xy) + (24\,x^2y + 12\,xy^2) = \\ & 108\,x^2y^2 - 102\,x^2y + 12\,xy^2 - 216\,xy \\ & [8] \quad -196\,x^2y - 112\,xy^2 + -98\,x^2y^2 + 98\,xy - (-49\,x^2y^2 + 147\,x^2y) = -49\,x^2y^2 - \\ & 343\,x^2y - 112\,xy^2 + 98\,xy \\ & [9] \quad 24\,x^2y^2 - 216\,xy^2 + 32\,x^2y + 144\,xy^2 - (32\,x^2y^2) = -8\,x^2y^2 + 32\,x^2y - 72\,xy^2 \\ & [10] \quad 117\,xy^2 + 27\,xy - (-252\,x^2y - 27\,xy^2) + (162\,x^2y + 9\,xy) = 414\,x^2y + 144\,xy^2 + \\ & 36\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (3\,b^3x^3y^2z) \cdot (3\,b^2xy^2z) = 9\,b^5x^4y^4z^2 \\ &[3] \quad (4\,bx^3yz^2) \cdot (16\,b^3x^2y^2z^2) = 64\,b^4x^5y^3z^4 \\ &[4] \quad (-54\,b^3x^3y^2z^3) \cdot (9\,bx^3y^2z^3) = -486\,b^4x^6y^4z^6 \\ &[5] \quad (256\,bxy^2z^3) \cdot (-16\,bx^3y^3z^2) = -4096\,b^2x^4y^5z^5 \\ &[6] \quad (-500\,b^2x^3y^2z^3) \cdot (20\,b^2xyz) = -10000\,b^4x^4y^3z^4 \\ &[7] \quad (-144\,bx^3yz) \cdot (-18\,b^3x^2y^2z) = 2592\,b^4x^5y^3z^2 \\ &[8] \quad (-686\,b^2x^2y^2z^2) \cdot (14\,bxy^2z^2) = -9604\,b^3x^3y^4z^4 \\ &[9] \quad (-32\,b^3x^3yz^2) \cdot (512\,bxy^2z) = -16384\,b^4x^4y^3z^3 \\ &[10] \quad (-81\,bx^3y^3z^2) \cdot (-324\,b^3x^3y^2z) = 26244\,b^4x^6y^5z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x)\cdot(-7\,x^2) = 14\,x^3 \\ &[2] \quad (-3\,x)\cdot(2\,x^2+x) = -6\,x^3-3\,x^2 \\ &[3] \quad (3\,x)\cdot(3\,x^2+5\,x) = 9\,x^3+15\,x^2 \\ &[4] \quad (x)\cdot(-4\,x) = -4\,x^2 \\ &[5] \quad (-x)\cdot(2\,x^2-4\,x) = -2\,x^3+4\,x^2 \\ &[6] \quad (3\,x^2)\cdot(6\,x^2+x) = 18\,x^4+3\,x^3 \\ &[7] \quad (2\,x^2)\cdot(-x) = -2\,x^3 \\ &[8] \quad (-x^2)\cdot(-2\,x^2+6\,x) = 2\,x^4-6\,x^3 \\ &[9] \quad (3\,x)\cdot(-x^2+6\,x) = -3\,x^3+18\,x^2 \\ &[10] \quad (2\,x)\cdot(-2\,x^2-x) = -4\,x^3-2\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-4\,x^2-4\,x)\cdot(3\,x^2-5\,x) = -12\,x^4+8\,x^3+20\,x^2 \\ &[2] \quad (2\,x^2)\cdot(7\,x^2-3\,x) = 14\,x^4-6\,x^3 \\ &[3] \quad (3\,x^2+2\,x)\cdot(-x^2-4\,x) = -3\,x^4-14\,x^3-8\,x^2 \\ &[4] \quad (-3\,x^2)\cdot(-5\,x^2-4\,x) = 15\,x^4+12\,x^3 \\ &[5] \quad (4\,x^2+2\,x)\cdot(x^2-2\,x) = 4\,x^4-6\,x^3-4\,x^2 \\ &[6] \quad (x^2)\cdot(2\,x) = 2\,x^3 \\ &[7] \quad (-2\,x^2)\cdot(-2\,x^2+x) = 4\,x^4-2\,x^3 \end{aligned}$$

[8]
$$(0) \cdot (5x^2 - 4x) = 0$$

[9]
$$(-3x^2 + x) \cdot (-3x^2 - 2x) = 9x^4 + 3x^3 - 2x^2$$

[10]
$$(x^2 - x) \cdot (-4x^2 - x) = -4x^4 + 3x^3 + x^2$$

[11]
$$(-x^2 + 2x) \cdot (-3x^2 + 2x) = 3x^4 - 8x^3 + 4x^2$$

[12]
$$(3x^2 + 3x) \cdot (7x^2 + x) = 21x^4 + 24x^3 + 3x^2$$

[13]
$$(2x^2 - 2x) \cdot (-3x) = -6x^3 + 6x^2$$

[14]
$$(0) \cdot (0) = 0$$

[15]
$$(3x^2 + 4x) \cdot (3x^2 + x) = 9x^4 + 15x^3 + 4x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^3 - x^2) \cdot (x^3 + 2x^2 + 3x) = -x^6 - 3x^5 - 5x^4 - 3x^3$$

[2]
$$(-8x^2) \cdot (-2x^3 + x^2 - 2x) = 16x^5 - 8x^4 + 16x^3$$

[3]
$$(-3x^3) \cdot (-4x^3 - x) = 12x^6 + 3x^4$$

[4]
$$(2x^2 + 8x) \cdot (2x^3 + 4x) = 4x^5 + 16x^4 + 8x^3 + 32x^2$$

[5]
$$(-4x^3 - 2x) \cdot (-2x^3 + 4x^2 + 5x) = 8x^6 - 16x^5 - 16x^4 - 8x^3 - 10x^2$$

[6]
$$(-4x^3 + 4x^2) \cdot (0) = 0$$

[7]
$$(-2x^3 + x) \cdot (-3x^3 - 2x) = 6x^6 + x^4 - 2x^2$$

[8]
$$(x^2 + x) \cdot (2x^2 + x) = 2x^4 + 3x^3 + x^2$$

[9]
$$(-3x^3) \cdot (-3x^3 + 3x) = 9x^6 - 9x^4$$

[10]
$$(x^3) \cdot (-4x^3 + 4x) = -4x^6 + 4x^4$$

[11]
$$(0) \cdot (-3x^3 - 2x^2 + x) = 0$$

[12]
$$(2x^2 + 4x) \cdot (-6x^3 + x^2 + 3x) = -12x^5 - 22x^4 + 10x^3 + 12x^2$$

[13]
$$(-3x^3 - 5x^2) \cdot (-4x^3 + 4x^2) = 12x^6 + 8x^5 - 20x^4$$

[14]
$$(-3x^2 + x) \cdot (-4x^3 - x^2 - 5x) = 12x^5 - x^4 + 14x^3 - 5x^2$$

[15]
$$(4x^3 + 4x^2) \cdot (-3x^3 + 4x) = -12x^6 - 12x^5 + 16x^4 + 16x^3$$

[16]
$$(x^3 - 6x^2) \cdot (-4x^3 - 2x^2) = -4x^6 + 22x^5 + 12x^4$$

[17]
$$(x^3 - 3x) \cdot (2x^3 - 2x^2 - x) = 2x^6 - 2x^5 - 7x^4 + 6x^3 + 3x^2$$

[18]
$$(-x) \cdot (-2x^3 - 2x) = 2x^4 + 2x^2$$

[19]
$$(x^2 + x) \cdot (-x^2 + x) = -x^4 + x^2$$

[20]
$$(-3x^3) \cdot (-2x^3 - 2x^2 + x) = 6x^6 + 6x^5 - 3x^4$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^2y^2 - 4xy) \cdot (x^2y^2 - 2xy) = -3x^4y^4 + 2x^3y^3 + 8x^2y^2$$

[2]
$$(-4x^2y - 2xy) \cdot (x^2y - xy) = -4x^4y^2 + 2x^3y^2 + 2x^2y^2$$

[3]
$$(3xy^2 + 2xy) \cdot (6xy^2) = 18x^2y^4 + 12x^2y^3$$

[4]
$$(-4x^2y^2 - 3xy) \cdot (x^2y^2 + x^2y) = -4x^4y^4 - 4x^4y^3 - 3x^3y^3 - 3x^3y^2$$

[5]
$$(-x^2y - xy^2) \cdot (x^2y) = -x^4y^2 - x^3y^3$$

[6]
$$(4x^2y + 3xy^2) \cdot (4x^2y - 4xy^2) = 16x^4y^2 - 4x^3y^3 - 12x^2y^4$$

[7]
$$(-x^2y^2 - xy) \cdot (3xy^2 + 2xy) = -3x^3y^4 - 2x^3y^3 - 3x^2y^3 - 2x^2y^2$$