1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$x^5 - x^2 + -3x^6 + 2x^3 + x + -5x^2 + 2x = -3x^6 + x^5 + 2x^3 - 6x^2 + 3x$$

[2] $3x^6 - 3x^5 - 2x + -x^6 + 4x^2 + 2x + -x^6 - 2x^2 = x^6 - 3x^5 + 2x^2$
[3] $-2x^6 + 2x^3 + 2x + (-3x^6 + 6x^3) + (-x^6 + 3x^5 + 2x^3) = -6x^6 + 3x^5 + 10x^3 + 2x$
[4] $6x^3 - 2x^2 + -2x^2 + 2x + 6x^5 - 4x^3 = 6x^5 + 2x^3 - 4x^2 + 2x$
[5] $4x^4 - x + -8x^3 + 2x + x^6 - 4x^4 + 4x = x^6 - 8x^3 + 5x$
[6] $4x^5 + x^4 + 3x^2 + 3x^3 + 3x^5 + 2x^4 - 4x = 7x^5 + 3x^4 + 3x^3 + 3x^2 - 4x$
[7] $x^5 - 2x^3 - 3x^2 + -3x^3 - 4x^2 + x + -4x^3 - 2x^2 - 4x = x^5 - 9x^3 - 9x^2 - 3x$
[8] $4x^5 - 4x^3 + 4x^2 + 3x^6 - x^5 - 3x^2 + -x^6 + 2x^5 = 2x^6 + 5x^5 - 4x^3 + x^2$
[9] $-x^4 + x^2 + (-3x^5 + 3x^4 + 2x) + (-4x^4) = -3x^5 - 2x^4 + x^2 + 2x$
[10] $3x^6 - x^3 + 3x + -4x^2 + 3x^6 + 2x^4 = 6x^6 + 2x^4 - x^3 - 4x^2 + 3x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0+0+0=0 \\ & [2] \quad 2\,xy^2+4\,xy+-3\,x^2y^2-2\,x^2y+2\,xy+-3\,xy^2-xy=-3\,x^2y^2-2\,x^2y-xy^2+5\,xy \\ & [3] \quad 6\,xy^2-6\,xy+-8\,x^2y+8\,xy^2+-2\,x^2y^2+4\,x^2y+8\,xy=-2\,x^2y^2-4\,x^2y+14\,xy^2+2\,xy \\ & [4] \quad 15\,xy^2-12\,xy+-45\,x^2y-9\,xy+-18\,x^2y+9\,xy^2-18\,xy=-63\,x^2y+24\,xy^2-39\,xy \\ & [5] \quad 8\,x^2y^2+72\,xy+-16\,x^2y^2+48\,x^2y+12\,x^2y^2+4\,xy^2+48\,xy=4\,x^2y^2+48\,x^2y+4\,xy^2+120\,xy \\ & [6] \quad 75\,x^2y^2+15\,x^2y-75\,xy+-75\,x^2y^2+25\,x^2y+15\,xy+20\,x^2y^2+120\,x^2y=20\,x^2y^2+160\,x^2y-60\,xy \\ & [7] \quad 36\,x^2y^2+6\,xy^2+-72\,x^2y^2-108\,x^2y+6\,xy^2+72\,x^2y-36\,xy^2=-36\,x^2y^2-36\,x^2y-24\,xy^2 \\ & [8] \quad 49\,x^2y^2+98\,xy+7\,x^2y^2+196\,x^2y+196\,xy+147\,xy^2=56\,x^2y^2+196\,x^2y+147\,xy^2+294\,xy \\ & [9] \quad 256\,x^2y^2+256\,xy^2-64\,xy+-64\,x^2y-184\,xy+-24\,x^2y^2-32\,xy^2=232\,x^2y^2-64\,x^2y+224\,xy^2-248\,xy \\ & [10] \quad 243\,x^2y^2-81\,x^2y+27\,xy^2+81\,x^2y+18\,x^2y-81\,xy^2=243\,x^2y^2+18\,x^2y-54\,xy^2 \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad x^2y - 5\,xy^2 + 3\,x^2y - 2\,xy^2 - (3\,x^2y^2 + 5\,x^2y) = -3\,x^2y^2 - x^2y - 7\,xy^2 \\ &[3] \quad -4\,x^2y^2 + 8\,xy^2 + 8\,x^2y + 6\,xy^2 - 6\,xy - (26\,x^2y^2) = -30\,x^2y^2 + 8\,x^2y + 14\,xy^2 - 6\,xy \\ &[4] \quad 9\,x^2y^2 - 48\,xy - (-18\,x^2y - 6\,xy) + (-39\,x^2y^2 - 36\,xy^2) = -30\,x^2y^2 + 18\,x^2y - 36\,xy^2 - 42\,xy \\ &[5] \quad -48\,x^2y^2 - 16\,xy^2 + -12\,x^2y^2 + 16\,xy^2 + 12\,xy - (-32\,xy^2 - 32\,xy) = -60\,x^2y^2 + 32\,xy^2 + 44\,xy \end{aligned}$$

$$\begin{aligned} & [6] \quad 75\,x^2y^2 + 50\,xy^2 + 50\,xy + 100\,x^2y^2 + 75\,xy^2 - 75\,xy - (-15\,x^2y^2) = 190\,x^2y^2 + \\ & 125\,xy^2 - 25\,xy \\ & [7] \quad 84\,x^2y - (174\,x^2y^2) + (72\,x^2y^2 + 102\,xy^2) = -102\,x^2y^2 + 84\,x^2y + 102\,xy^2 \\ & [8] \quad -98\,xy^2 - 224\,xy + 196\,x^2y^2 - (-49\,x^2y + 21\,xy^2 + 196\,xy) = 196\,x^2y^2 + \\ & 49\,x^2y - 119\,xy^2 - 420\,xy \\ & [9] \quad -160\,x^2y^2 - 24\,xy + 144\,x^2y^2 + 192\,xy^2 - (-104\,x^2y^2 + 24\,xy) = 88\,x^2y^2 + \\ & 192\,xy^2 - 48\,xy \\ & [10] \quad 243\,x^2y^2 + 306\,xy - (216\,x^2y - 27\,xy) + (27\,x^2y^2 + 126\,x^2y) = 270\,x^2y^2 - \\ & 90\,x^2y + 333\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-2\,b^2xy^2z^3) \cdot (-b^3xy^2z^2) = 2\,b^5x^2y^4z^5 \\ &[3] \quad (24\,bxy^3z^2) \cdot (4\,bx^2y^2z) = 96\,b^2x^3y^5z^3 \\ &[4] \quad (108\,bx^3yz^3) \cdot (-9\,b^2xyz^2) = -972\,b^3x^4y^2z^5 \\ &[5] \quad (-16\,bxy^3z) \cdot (-16\,bxyz^2) = 256\,b^2x^2y^4z^3 \\ &[6] \quad (20\,bx^2y^2z) \cdot (25\,b^3xyz) = 500\,b^4x^3y^3z^2 \\ &[7] \quad (-864\,b^2xy^3z^3) \cdot (6\,b^3x^2y^2z^3) = -5184\,b^5x^3y^5z^6 \\ &[8] \quad (147\,b^2x^3y^2z^2) \cdot (-7\,b^3x^3y^2z) = -1029\,b^5x^6y^4z^3 \\ &[9] \quad (-192\,b^2x^3y^3z) \cdot (128\,b^2xy^3z^2) = -24576\,b^4x^4y^6z^3 \\ &[10] \quad (-2187\,b^2x^3yz^3) \cdot (2187\,bxyz^3) = -4782969\,b^3x^4y^2z^6 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x) \cdot (10x^2 + 3x) = -20x^3 - 6x^2$$

[2] $(x^2) \cdot (4x^2 - 2x) = 4x^4 - 2x^3$
[3] $(3x^2) \cdot (-x^2 - 3x) = -3x^4 - 9x^3$
[4] $(x) \cdot (3x^2 + 6x) = 3x^3 + 6x^2$
[5] $(2x) \cdot (-3x^2 - 4x) = -6x^3 - 8x^2$
[6] $(-2x) \cdot (-3x^2 - 3x) = 6x^3 + 6x^2$
[7] $(-2x^2) \cdot (-x^2 + 8x) = 2x^4 - 16x^3$
[8] $(-4x) \cdot (-2x^2) = 8x^3$
[9] $(-4x^2) \cdot (3x^2 - x) = -12x^4 + 4x^3$
[10] $(x^2) \cdot (5x^2 + 5x) = 5x^4 + 5x^3$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2 + 2x) \cdot (2x^2 + 2x) = -4x^4 + 4x^2$$

[2] $(-4x^2 - 3x) \cdot (-2x^2 - x) = 8x^4 + 10x^3 + 3x^2$
[3] $(0) \cdot (-4x^2 - 5x) = 0$
[4] $(-x^2 - 2x) \cdot (4x^2 - 2x) = -4x^4 - 6x^3 + 4x^2$
[5] $(0) \cdot (4x^2 - 4x) = 0$
[6] $(-5x^2) \cdot (-5x^2) = 25x^4$
[7] $(-4x^2 + 3x) \cdot (-3x^2 - 2x) = 12x^4 - x^3 - 6x^2$

[8]
$$(-8x) \cdot (-5x^2 + x) = 40x^3 - 8x^2$$

[9]
$$(4x^2) \cdot (-4x^2) = -16x^4$$

[10]
$$(2x^2) \cdot (-x^2 + 3x) = -2x^4 + 6x^3$$

[11]
$$(2x^2) \cdot (-x^2 - x) = -2x^4 - 2x^3$$

[12]
$$(2x) \cdot (2x^2 - x) = 4x^3 - 2x^2$$

[13]
$$(5x^2) \cdot (-2x^2 - 3x) = -10x^4 - 15x^3$$

[14]
$$(-3x^2 - 3x) \cdot (3x^2 - 3x) = -9x^4 + 9x^2$$

[15]
$$(-x^2 + 2x) \cdot (4x^2) = -4x^4 + 8x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^3 + 3x^2 - 3x) \cdot (-2x^2 + 5x) = 4x^5 - 16x^4 + 21x^3 - 15x^2$$

[2]
$$(-3x^3 + x^2) \cdot (6x^3 + x) = -18x^6 + 6x^5 - 3x^4 + x^3$$

[3]
$$(4x^3 - 2x) \cdot (2x^3 - 3x) = 8x^6 - 16x^4 + 6x^2$$

[4]
$$(x^3 + 4x^2 - x) \cdot (x) = x^4 + 4x^3 - x^2$$

[5]
$$(-x^2) \cdot (2x^3 - 8x^2) = -2x^5 + 8x^4$$

[6]
$$(6x) \cdot (-3x^2 + 4x) = -18x^3 + 24x^2$$

[7]
$$(x^3 + x^2 - x) \cdot (-x^3 - 6x^2) = -x^6 - 7x^5 - 5x^4 + 6x^3$$

[8]
$$(x^3 - 3x) \cdot (-x^3 + x) = -x^6 + 4x^4 - 3x^2$$

[9]
$$(-x^3 - 3x^2) \cdot (4x^3 - 3x^2 - x) = -4x^6 - 9x^5 + 10x^4 + 3x^3$$

[10]
$$(2x^2) \cdot (-3x^3 - 6x^2) = -6x^5 - 12x^4$$

[11]
$$(-3x^2 + 3x) \cdot (-x^3 - 4x^2 - 2x) = 3x^5 + 9x^4 - 6x^3 - 6x^2$$

[12]
$$(0) \cdot (-7x^3 + 2x^2 + x) = 0$$

[13]
$$(-4x^3 - 5x^2) \cdot (5x^3 + 2x^2) = -20x^6 - 33x^5 - 10x^4$$

[14]
$$(x^2 - 2x) \cdot (x^3 - 2x^2 + 7x) = x^5 - 4x^4 + 11x^3 - 14x^2$$

[15]
$$(5x^3) \cdot (2x^3 + x^2 + 2x) = 10x^6 + 5x^5 + 10x^4$$

[16]
$$(-4x^3 + 8x^2) \cdot (-3x^3) = 12x^6 - 24x^5$$

[17]
$$(-4x^3 - 4x^2) \cdot (4x^3 - 2x^2 + x) = -16x^6 - 8x^5 + 4x^4 - 4x^3$$

[18]
$$(2x^3 + 2x^2) \cdot (3x^3 + 3x^2) = 6x^6 + 12x^5 + 6x^4$$

[19]
$$(-7x^3 - x^2) \cdot (2x^3 - 4x^2 + 3x) = -14x^6 + 26x^5 - 17x^4 - 3x^3$$

[20]
$$(-2x^2 + 4x) \cdot (3x^2 - 6x) = -6x^4 + 24x^3 - 24x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$[1] \quad (-4x^2y^2 - 3xy^2) \cdot (2x^2y^2 - 3x^2y) = -8x^4y^4 + 12x^4y^3 - 6x^3y^4 + 9x^3y^3$$

[2]
$$(-3x^2y^2 - 2xy) \cdot (-3x^2y^2 + 3xy^2) = 9x^4y^4 - 9x^3y^4 + 6x^3y^3 - 6x^2y^3$$

[3]
$$(-3x^2y - 2xy) \cdot (-3x^2y + 3xy^2) = 9x^2y - 9x^2y + 6x^2y - 6x^2y$$

[3] $(-3x^2y - 2xy^2) \cdot (4x^2y^2 + 4x^2y + 3xy^2) = -12x^4y^3 - 8x^3y^4 - 12x^4y^2 - 17x^3y^3 - 6x^2y^4$

[4]
$$(-3x^2y^2 + 4xy) \cdot (-8x^2y + 3xy^2) = 24x^4y^3 - 9x^3y^4 - 32x^3y^2 + 12x^2y^3$$

[5]
$$(2x^2y^2 - 3xy) \cdot (x^2y - 2xy^2) = 2x^4y^3 - 4x^3y^4 - 3x^3y^2 + 6x^2y^3$$

[6]
$$(3x^2y^2 - 4xy^2) \cdot (5x^2y) = 15x^4y^3 - 20x^3y^3$$

[7]
$$(7x^2y^2) \cdot (-4xy^2 + 5xy) = -28x^3y^4 + 35x^3y^3$$