1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] -x^5 - 4x^2 - x + (-2x^6 - 2x^4 - 3x^3) + (-x^5 - x^2) = -2x^6 - 2x^5 - 2x^4 - 3x^3 - 5x^2 - x$$

$$[2] 4x^6 + 4x^4 - x^2 + -x^6 + 4x^5 - 3x^3 + -x^5 + 4x^2 = 3x^6 + 3x^5 + 4x^4 - 3x^3 + 3x^2$$

$$[3] 3x^3 + 3x + -2x^6 + 4x^5 + 4x^4 + 6x^3 = -2x^6 + 4x^5 + 4x^4 + 9x^3 + 3x$$

$$[4] 4x^5 - x^3 + 2x + -x^4 + 3x + x^4 = 4x^5 - x^3 + 5x$$

$$[5] 4x^2 + 7x + 2x^6 - 2x^3 - 3x + 2x^6 + 3x^5 - 2x^3 = 4x^6 + 3x^5 - 4x^3 + 4x^2 + 4x$$

$$[6] x^4 - 8x^2 + -3x^4 - 3x^2 - 4x + -x^4 = -3x^4 - 11x^2 - 4x$$

$$[7] 3x^6 + 3x^5 + 3x^4 + -4x^6 + 2x^4 + 3x^2 + (-2x^5 + 3x^3 + 3x) = -x^6 + x^5 + 5x^4 + 3x^3 + 3x^2 + 3x$$

$$[8] 8x^6 - 4x^4 + -4x^3 + 3x + -2x^5 - x^3 + 2x^2 = 8x^6 - 2x^5 - 4x^4 - 5x^3 + 2x^2 + 3x$$

$$[9] 4x^6 + x^4 + x^2 + 4x^6 + x^4 + 2x^2 + 4x^4 + 3x^3 = 8x^6 + 6x^4 + 3x^3 + 3x^2$$

$$[10] 4x^6 - 3x^3 - x + -6x^5 + 4x + (-5x) = 4x^6 - 6x^5 - 3x^3 - 2x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 2x^2y^2+2x^2y+3xy^2+7x^2y-xy^2+2x^2y-4xy^2=2x^2y^2+11x^2y-2xy^2 \\ [3] \quad 8x^2y-4xy^2-12xy+-12x^2y^2-16x^2y-6xy^2+-16x^2y^2-8x^2y-2xy=-28x^2y^2-16x^2y-10xy^2-14xy \\ [4] \quad 3x^2y^2+39x^2y+27xy^2+21x^2y^2-3x^2y=24x^2y^2+36x^2y+27xy^2 \\ [5] \quad 16x^2y^2-32x^2y+32xy^2+8x^2y^2+4xy^2+-8x^2y-48xy=24x^2y^2-40x^2y+36xy^2-48xy \\ [6] \quad 15x^2y^2+50x^2y-10xy+-100x^2y^2+20x^2y-5xy^2+-65x^2y+25xy^2=-85x^2y^2+5x^2y+20xy^2-10xy \\ [7] \quad 144x^2y^2-24xy^2+-84x^2y+24xy^2+-60x^2y^2-144xy^2=84x^2y^2-84x^2y-144xy^2 \\ [8] \quad 28x^2y^2-14xy^2-196xy+-196xy^2+98xy+35x^2y^2-196x^2y=63x^2y^2-196x^2y-210xy^2-98xy \\ [9] \quad -16xy^2+(-24x^2y-64xy^2+256xy)+(-248x^2y^2-128xy)=-248x^2y^2-24x^2y-80xy^2+128xy \\ [10] \quad 27x^2y-9xy^2+36xy+-36x^2y^2+567xy+(-162x^2y^2-243x^2y+18xy^2)=-198x^2y^2-216x^2y+9xy^2+603xy \\ [10] \quad 27x^2y-9xy^2+603xy+18xy^2+18xy^$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad x^2y - 3\,xy + 8\,x^2y - xy - (-4\,x^2y^2 - 2\,xy^2 - 2\,xy) = 4\,x^2y^2 + 9\,x^2y + 2\,xy^2 - 2\,xy \\ &[3] \quad -6\,x^2y + 4\,xy^2 + -6\,x^2y^2 - 4\,xy^2 - (-24\,x^2y^2 + 2\,x^2y) = 18\,x^2y^2 - 8\,x^2y \\ &[4] \quad -36\,x^2y^2 - 3\,x^2y + 12\,xy^2 - (-18\,x^2y^2 + 6\,x^2y - 27\,xy^2) + (27\,x^2y - 3\,xy) = \\ &-18\,x^2y^2 + 18\,x^2y + 39\,xy^2 - 3\,xy \\ &[5] \quad -28\,xy^2 - 16\,xy + -16\,x^2y + 32\,xy - (-8\,x^2y^2 + 48\,xy^2) = 8\,x^2y^2 - 16\,x^2y - \\ &76\,xy^2 + 16\,xy \end{aligned}$$

$$[6] \quad -25\,x^2y^2 - 10\,x^2y - 20\,xy + 25\,x^2y^2 + 10\,xy - (5\,x^2y^2 + 25\,x^2y - 5\,xy^2) = \\ -5\,x^2y^2 - 35\,x^2y + 5\,xy^2 - 10\,xy \\ [7] \quad -144\,xy^2 + 78\,xy - (108\,x^2y^2) + (6\,x^2y) = -108\,x^2y^2 + 6\,x^2y - 144\,xy^2 + 78\,xy \\ [8] \quad 28\,xy^2 - 196\,xy + -49\,xy^2 - (98\,x^2y^2 + 21\,xy^2 - 28\,xy) = -98\,x^2y^2 - 42\,xy^2 - \\ 168\,xy \\ [9] \quad -128\,x^2y + 8\,xy + -160\,x^2y + 32\,xy - (8\,x^2y^2 + 256\,xy^2) = -8\,x^2y^2 - 288\,x^2y - \\ 256\,xy^2 + 40\,xy \\ [10] \quad 270\,x^2y^2 + 162\,xy - (324\,x^2y^2 - 351\,xy^2) + (-81\,x^2y^2 + 9\,xy^2 - 324\,xy) = \\ -135\,x^2y^2 + 360\,xy^2 - 162\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-bx^3y^2z^3) \cdot (b^2x^3y^3z) = -b^3x^6y^5z^4 \\ &[3] \quad (-8\,b^2xy^3z) \cdot (32\,b^2xy^3z^3) = -256\,b^4x^2y^6z^4 \\ &[4] \quad (-9\,bx^2y^2z) \cdot (-36\,b^2x^2y^3z) = 324\,b^3x^4y^5z^2 \\ &[5] \quad (32\,b^2x^2yz^3) \cdot (4\,b^2xyz^2) = 128\,b^4x^3y^2z^5 \\ &[6] \quad (-75\,b^3x^2y^3z^2) \cdot (15\,bx^2yz^3) = -1125\,b^4x^4y^4z^5 \\ &[7] \quad (-648\,bx^2y^2z^2) \cdot (-144\,b^2x^3y^3z^2) = 93312\,b^3x^5y^5z^4 \\ &[8] \quad (98\,b^2x^3yz^3) \cdot (-14\,b^2x^2y^2z^2) = -1372\,b^4x^5y^3z^5 \\ &[9] \quad (-24\,bxy^2z) \cdot (2048\,bxy^2z^3) = -49152\,b^2x^2y^4z^4 \\ &[10] \quad (81\,b^3xyz) \cdot (-162\,b^3x^2y^3z) = -13122\,b^6x^3y^4z^2 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x) \cdot (5x^2 - 5x) = -10x^3 + 10x^2$$

[2] $(3x^2) \cdot (5x^2 - 4x) = 15x^4 - 12x^3$
[3] $(-2x^2) \cdot (3x^2) = -6x^4$
[4] $(3x) \cdot (-x^2) = -3x^3$
[5] $(3x) \cdot (-4x^2 - 5x) = -12x^3 - 15x^2$
[6] $(-3x) \cdot (-3x^2 + 8x) = 9x^3 - 24x^2$
[7] $(-3x) \cdot (10x^2) = -30x^3$
[8] $(x^2) \cdot (-2x^2) = -2x^4$
[9] $(-3x^2) \cdot (4x^2 + x) = -12x^4 - 3x^3$
[10] $(-x^2) \cdot (2x^2 + 3x) = -2x^4 - 3x^3$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (x^2-3\,x)\cdot(-6\,x^2-x) = -6\,x^4+17\,x^3+3\,x^2 \\ & [2] \quad (7\,x)\cdot(-x^2+4\,x) = -7\,x^3+28\,x^2 \\ & [3] \quad (7\,x^2)\cdot(4\,x^2+4\,x) = 28\,x^4+28\,x^3 \\ & [4] \quad (2\,x)\cdot(x^2-3\,x) = 2\,x^3-6\,x^2 \\ & [5] \quad (0)\cdot(x^2-2\,x) = 0 \\ & [6] \quad (x^2)\cdot(5\,x^2) = 5\,x^4 \\ & [7] \quad (-2\,x^2-4\,x)\cdot(7\,x^2+x) = -14\,x^4-30\,x^3-4\,x^2 \end{aligned}$$

$$\begin{split} [8] \quad & (2\,x^2)\cdot(10\,x^2) = 20\,x^4 \\ [9] \quad & (2\,x^2-x)\cdot(-4\,x^2+5\,x) = -8\,x^4+14\,x^3-5\,x^2 \\ [10] \quad & (3\,x^2+4\,x)\cdot(5\,x^2+4\,x) = 15\,x^4+32\,x^3+16\,x^2 \\ [11] \quad & (-x^2+2\,x)\cdot(-2\,x^2-x) = 2\,x^4-3\,x^3-2\,x^2 \\ [12] \quad & (x^2+3\,x)\cdot(5\,x^2+2\,x) = 5\,x^4+17\,x^3+6\,x^2 \\ [13] \quad & (x^2-x)\cdot(2\,x^2-3\,x) = 2\,x^4-5\,x^3+3\,x^2 \\ [14] \quad & (-3\,x^2-3\,x)\cdot(2\,x^2-7\,x) = -6\,x^4+15\,x^3+21\,x^2 \end{split}$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[15] $(-5x) \cdot (x^2 - 3x) = -5x^3 + 15x^2$

$$\begin{array}{ll} [1] & (2\,x^3+x) \cdot (-x^3-x^2-2\,x) = -2\,x^6-2\,x^5-5\,x^4-x^3-2\,x^2 \\ [2] & (8\,x) \cdot (-3\,x^3+x) = -24\,x^4+8\,x^2 \\ [3] & (-3\,x) \cdot (3\,x^3-x^2+3\,x) = -9\,x^4+3\,x^3-9\,x^2 \\ [4] & (-2\,x^3-4\,x) \cdot (3\,x^3+3\,x^2) = -6\,x^6-6\,x^5-12\,x^4-12\,x^3 \\ [5] & (-4\,x^2-4\,x) \cdot (x^3-4\,x^2) = -4\,x^5+12\,x^4+16\,x^3 \\ [6] & (-4\,x^3-4\,x) \cdot (0) = 0 \\ [7] & (-4\,x^2+4\,x) \cdot (x^3+3\,x^2-x) = -4\,x^5-8\,x^4+16\,x^3-4\,x^2 \\ [8] & (4\,x^2-2\,x) \cdot (0) = 0 \\ [9] & (0) \cdot (-4\,x^3-4\,x^2+x) = 0 \\ [10] & (-2\,x^3-2\,x^2) \cdot (-3\,x^2+7\,x) = 6\,x^5-8\,x^4-14\,x^3 \\ [11] & (0) \cdot (8\,x^3+3\,x^2-3\,x) = 0 \\ [12] & (3\,x^3-3\,x) \cdot (-6\,x^3-3\,x^2+x) = -18\,x^6-9\,x^5+21\,x^4+9\,x^3-3\,x^2 \\ [13] & (2\,x^2+x) \cdot (2\,x^3-x^2) = 4\,x^5-x^3 \\ [14] & (-4\,x^3) \cdot (3\,x^2-2\,x) = -12\,x^5+8\,x^4 \\ [15] & (-4\,x) \cdot (-4\,x^3+4\,x^2) = 16\,x^4-16\,x^3 \\ [16] & (-2\,x^3-3\,x) \cdot (-x^3) = 2\,x^6+3\,x^4 \\ [17] & (-2\,x^3+4\,x^2) \cdot (x^3-3\,x^2-4\,x) = -2\,x^6+10\,x^5-4\,x^4-16\,x^3 \\ [18] & (6\,x^2) \cdot (7\,x^3+4\,x^2+3\,x) = 42\,x^5+24\,x^4+18\,x^3 \\ [19] & (-8\,x^3-3\,x^2) \cdot (-4\,x^3-2\,x^2-2\,x) = 32\,x^6+28\,x^5+22\,x^4+6\,x^3 \\ [20] & (-6\,x^2) \cdot (-6\,x^2-x) = 36\,x^4+6\,x^3 \\ [20] & (-6\,x^2) \cdot (-6\,x^2-x) = 36\,x^4+6\,x^3 \\ \end{array}$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (3\,x^2y^2 - 2\,xy) \cdot (-4\,x^2y - xy^2 + xy) = -12\,x^4y^3 - 3\,x^3y^4 + 3\,x^3y^3 + 8\,x^3y^2 + \\ & 2\,x^2y^3 - 2\,x^2y^2 \\ & [2] \quad (x^2y^2) \cdot (x^2y) = x^4y^3 \\ & [3] \quad (x^2y + 2\,xy^2) \cdot (2\,x^2y^2 - 4\,x^2y + 3\,xy) = 2\,x^4y^3 + 4\,x^3y^4 - 4\,x^4y^2 - 8\,x^3y^3 + \\ & 3\,x^3y^2 + 6\,x^2y^3 \\ & [4] \quad (-2\,x^2y - xy^2) \cdot (-xy^2) = 2\,x^3y^3 + x^2y^4 \\ & [5] \quad (-3\,x^2y + 4\,xy) \cdot (x^2y + 3\,xy^2 + 3\,xy) = -3\,x^4y^2 - 9\,x^3y^3 - 5\,x^3y^2 + 12\,x^2y^3 + \\ & 12\,x^2y^2 \\ & [6] \quad (-x^2y - 4\,xy) \cdot (-3\,x^2y^2 - 5\,xy) = 3\,x^4y^3 + 12\,x^3y^3 + 5\,x^3y^2 + 20\,x^2y^2 \\ & [7] \quad (4\,x^2y^2 - xy^2) \cdot (-x^2y^2 + 6\,x^2y) = -4\,x^4y^4 + 24\,x^4y^3 + x^3y^4 - 6\,x^3y^3 + 20\,x^3y^3 + 20\,x^3y$$