## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 6x^6 - 3x^3 + 4x + -2x^4 - 2x = 6x^6 - 2x^4 - 3x^3 + 2x$$

$$[2] \quad 5x^4 + 4x^3 + 2x^4 - 3x^3 - 2x + 3x^6 + 2x^4 - 2x^2 = 3x^6 + 9x^4 + x^3 - 2x^2 - 2x$$

$$[3] \quad 2x^5 - x^3 + 2x + -x^4 - 2x + x^4 - 2x^3 - 2x^2 = 2x^5 - 3x^3 - 2x^2$$

$$[4] \quad 4x^5 + 2x^4 - 3x^2 + -3x^6 - 2x^5 + 4x^4 + -2x^6 + 3x = -5x^6 + 2x^5 + 6x^4 - 3x^2 + 3x$$

$$[5] \quad 3x^6 + 4x^5 - 3x^2 + -4x^5 + 2x^4 = 3x^6 + 2x^4 - 3x^2$$

$$[6] \quad -x^6 - x^4 + 3x^2 + (-4x^5 - x^3 + 2x) + (-4x^5 + 3x^3 - x) = -x^6 - 8x^5 - x^4 + 2x^3 + 3x^2 + x$$

$$[7] \quad x^4 - 5x^3 + -x^2 + 2x^4 + 3x^3 - 4x^2 = 3x^4 - 2x^3 - 5x^2$$

$$[8] \quad 4x^6 + -4x^6 - 3x^5 - 2x^2 + 2x^3 + 2x^2 - 2x = -3x^5 + 2x^3 - 2x$$

$$[9] \quad x^3 + 4x + x^6 + 2x^3 - x^2 + 4x^4 - 5x^3 = x^6 + 4x^4 - 2x^3 - x^2 + 4x$$

[10]  $4x^5 - x^4 + 2x^2 + -x^6 - 4x^5 - 3x^3 + -4x^6 + x^5 - 2x^2 = -5x^6 + x^5 - x^4 - 3x^3$ 

Ejercicio 2: Realiza las siguientes sumas de polinomios:

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 4\,x^2y^2 + 3\,xy + 2\,x^2y^2 - (3\,xy) = 6\,x^2y^2 \\ &[3] \quad -10\,x^2y^2 + 2\,xy + 4\,x^2y^2 - 16\,x^2y - (-6\,x^2y^2 - 8\,x^2y + 4\,xy) = -8\,x^2y - 2\,xy \\ &[4] \quad 18\,x^2y^2 + 36\,xy^2 - (-27\,x^2y - 27\,xy^2 - 27\,xy) + (36\,x^2y^2 - 3\,xy^2 + 6\,xy) = 54\,x^2y^2 + 27\,x^2y + 60\,xy^2 + 33\,xy \end{aligned}$$

$$[5] \quad 16\,xy^2 - 16\,xy + 8\,xy^2 - (-48\,xy) = 24\,xy^2 + 32\,xy$$

$$[6] \quad 100\,xy^2 - 50\,xy + 5\,x^2y^2 + 50\,x^2y - 5\,xy - (75\,x^2y^2 + 100\,xy^2 - 20\,xy) = -70\,x^2y^2 + 50\,x^2y - 35\,xy$$

$$[7] \quad 144\,x^2y^2 + 48\,xy - (-48\,x^2y + 18\,xy) + (-144\,x^2y^2 - 24\,x^2y - 12\,xy) = 24\,x^2y + 18\,xy$$

$$[8] \quad -154\,x^2y^2 + 21\,x^2y + -21\,x^2y^2 - 7\,xy - (49\,x^2y + 84\,xy) = -175\,x^2y^2 - 28\,x^2y - 91\,xy$$

$$[9] \quad 32\,x^2y - 184\,xy + 160\,x^2y^2 - (8\,x^2y^2 - 16\,x^2y - 256\,xy) = 152\,x^2y^2 + 48\,x^2y + 72\,xy$$

$$[10] \quad -162\,x^2y^2 - 27\,xy^2 - 18\,xy - (27\,x^2y^2 + 45\,xy^2) + (-162\,x^2y^2 + 18\,x^2y - 243\,xy^2) = -351\,x^2y^2 + 18\,x^2y - 315\,xy^2 - 18\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-bx^2y^2z) \cdot (bxyz) = -b^2x^3y^3z^2 \\ &[3] \quad (4\,b^3xy^3z) \cdot (4\,b^2x^2yz^3) = 16\,b^5x^3y^4z^4 \\ &[4] \quad (27\,b^3xy^3z^2) \cdot (-27\,bx^2yz) = -729\,b^4x^3y^4z^3 \\ &[5] \quad (192\,bx^3yz) \cdot (192\,b^2x^2y^3z^3) = 36864\,b^3x^5y^4z^4 \\ &[6] \quad (-500\,bx^3y^2z^3) \cdot (100\,bx^3yz^3) = -50000\,b^2x^6y^3z^6 \\ &[7] \quad (648\,b^3x^3yz^2) \cdot (-648\,b^2x^3y^2z^3) = -419904\,b^5x^6y^3z^5 \\ &[8] \quad (343\,b^2x^2y^3z^2) \cdot (-1029\,bxy^2z^2) = -352947\,b^3x^3y^5z^4 \\ &[9] \quad (1024\,b^2xy^3z^3) \cdot (192\,bx^2y^3z) = 196608\,b^3x^3y^6z^4 \\ &[10] \quad (-81\,bxy^3z^2) \cdot (-2187\,b^3x^3y^3z^3) = 177147\,b^4x^4y^6z^5 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-3\,x)\cdot(4\,x^2-2\,x) = -12\,x^3+6\,x^2 \\ &[2] \quad (-2\,x)\cdot(x^2+4\,x) = -2\,x^3-8\,x^2 \\ &[3] \quad (-x^2)\cdot(-3\,x^2+2\,x) = 3\,x^4-2\,x^3 \\ &[4] \quad (4\,x^2)\cdot(3\,x) = 12\,x^3 \\ &[5] \quad (-3\,x^2)\cdot(-6\,x) = 18\,x^3 \\ &[6] \quad (x)\cdot(5\,x^2+x) = 5\,x^3+x^2 \\ &[7] \quad (-3\,x^2)\cdot(-3\,x^2+x) = 9\,x^4-3\,x^3 \\ &[8] \quad (-x)\cdot(-3\,x^2-4\,x) = 3\,x^3+4\,x^2 \\ &[9] \quad (-x^2)\cdot(2\,x^2-5\,x) = -2\,x^4+5\,x^3 \\ &[10] \quad (-x^2)\cdot(3\,x^2+2\,x) = -3\,x^4-2\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{split} &[1] \quad (-6\,x)\cdot(4\,x^2+2\,x) = -24\,x^3-12\,x^2 \\ &[2] \quad (6\,x^2)\cdot(-4\,x^2-x) = -24\,x^4-6\,x^3 \\ &[3] \quad (-3\,x^2-2\,x)\cdot(-5\,x^2-2\,x) = 15\,x^4+16\,x^3+4\,x^2 \\ &[4] \quad (2\,x^2+3\,x)\cdot(6\,x^2+2\,x) = 12\,x^4+22\,x^3+6\,x^2 \\ &[5] \quad (2\,x^2)\cdot(-x^2) = -2\,x^4 \end{split}$$

[6] 
$$(0) \cdot (4x^2 + 5x) = 0$$
  
[7]  $(-2x^2) \cdot (x^2 + 7x) = -2x^4 - 14x^3$   
[8]  $(-6x^2) \cdot (-x^2 + 5x) = 6x^4 - 30x^3$   
[9]  $(3x^2 + 4x) \cdot (-2x^2 + 2x) = -6x^4 - 2x^3 + 8x^2$   
[10]  $(-2x^2 + 3x) \cdot (3x) = -6x^3 + 9x^2$   
[11]  $(-x^2 - 4x) \cdot (-3x^2 + x) = 3x^4 + 11x^3 - 4x^2$   
[12]  $(-3x^2 - 2x) \cdot (-5x^2 - 3x) = 15x^4 + 19x^3 + 6x^2$   
[13]  $(4x^2 + 3x) \cdot (2x) = 8x^3 + 6x^2$ 

[14]  $(-4x^2) \cdot (-4x) = 16x^3$ 

[15]  $(0) \cdot (2x^2 + 6x) = 0$ 

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (-x^3-2\,x^2+4\,x)\cdot(2\,x^2) = -2\,x^5-4\,x^4+8\,x^3 \\ & [2] \quad (2\,x^3+3\,x^2)\cdot(-7\,x^2) = -14\,x^5-21\,x^4 \\ & [3] \quad (3\,x^2-x)\cdot(-5\,x^2+6\,x) = -15\,x^4+23\,x^3-6\,x^2 \\ & [4] \quad (4\,x^2)\cdot(2\,x^3-5\,x^2) = 8\,x^5-20\,x^4 \\ & [5] \quad (3\,x^2-x)\cdot(-x^3+x^2+2\,x) = -3\,x^5+4\,x^4+5\,x^3-2\,x^2 \\ & [6] \quad (x^3+4\,x)\cdot(-10\,x^2+x) = -10\,x^5+x^4-40\,x^3+4\,x^2 \\ & [7] \quad (4\,x^3)\cdot(x^3-3\,x^2) = 4\,x^6-12\,x^5 \\ & [8] \quad (4\,x^3-2\,x)\cdot(-6\,x^2+5\,x) = -24\,x^5+20\,x^4+12\,x^3-10\,x^2 \\ & [9] \quad (4\,x^2+3\,x)\cdot(-4\,x) = -16\,x^3-12\,x^2 \\ & [10] \quad (x^3-3\,x^2+x)\cdot(4\,x^3+x^2) = 4\,x^6-11\,x^5+x^4+x^3 \\ & [11] \quad (2\,x^2+4\,x)\cdot(x^3-2\,x^2) = 2\,x^5-8\,x^3 \\ & [12] \quad (x^3-x)\cdot(3\,x^3-2\,x^2+4\,x) = 3\,x^6-2\,x^5+x^4+2\,x^3-4\,x^2 \\ & [13] \quad (2\,x^2+6\,x)\cdot(2\,x^3-2\,x) = 4\,x^5+12\,x^4-4\,x^3-12\,x^2 \\ & [14] \quad (2\,x^2+4\,x)\cdot(2\,x^3+x) = 4\,x^5+8\,x^4+2\,x^3+4\,x^2 \\ & [15] \quad (x^3-4\,x^2)\cdot(-x^3+3\,x^2) = -x^6+7\,x^5-12\,x^4 \\ & [16] \quad (5\,x^2-2\,x)\cdot(4\,x^3-3\,x^2) = 20\,x^5-23\,x^4+6\,x^3 \\ & [17] \quad (-4\,x^3+x)\cdot(-3\,x^3-3\,x^2-4\,x) = 12\,x^6+12\,x^5+13\,x^4-3\,x^3-4\,x^2 \\ & [18] \quad (3\,x^3-3\,x)\cdot(x^2) = 3\,x^5-3\,x^3 \\ & [19] \quad (-3\,x^3)\cdot(-4\,x^3+4\,x^2) = 12\,x^6-12\,x^5 \\ & [20] \quad (2\,x^2-4\,x)\cdot(3\,x^3-6\,x) = 6\,x^5-12\,x^4-12\,x^3+24\,x^2 \end{aligned}$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x^2y^2 - 4\,x^2y) \cdot (4\,x^2y^2 - xy^2 - xy) = -4\,x^4y^4 - 16\,x^4y^3 + x^3y^4 + 5\,x^3y^3 + 4\,x^3y^2 \\ &[2] \quad (-2\,x^2y - xy^2) \cdot (-2\,x^2y - 3\,xy^2 - 2\,xy) = 4\,x^4y^2 + 8\,x^3y^3 + 3\,x^2y^4 + 4\,x^3y^2 + 2\,x^2y^3 \\ &[3] \quad (4\,x^2y + 4\,xy) \cdot (2\,xy^2 + 4\,xy) = 8\,x^3y^3 + 16\,x^3y^2 + 8\,x^2y^3 + 16\,x^2y^2 \\ &[4] \quad (3\,xy^2) \cdot (-3\,x^2y - 4\,xy^2 + 4\,xy) = -9\,x^3y^3 - 12\,x^2y^4 + 12\,x^2y^3 \\ &[5] \quad (-2\,x^2y^2 + 2\,xy) \cdot (-x^2y + 4\,xy) = 2\,x^4y^3 - 8\,x^3y^3 - 2\,x^3y^2 + 8\,x^2y^2 \\ &[6] \quad (-7\,xy) \cdot (2\,x^2y^2 + 4\,x^2y + 4\,xy^2) = -14\,x^3y^3 - 28\,x^3y^2 - 28\,x^2y^3 \\ &[7] \quad (4\,xy^2 + 2\,xy) \cdot (-3\,x^2y + 7\,xy) = -12\,x^3y^3 - 6\,x^3y^2 + 28\,x^2y^3 + 14\,x^2y^2 \end{aligned}$$