1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$5x^5 + 3x^4 + -x^6 - 4x^4 + x^2 + 7x = -x^6 + 5x^5 - x^4 + x^2 + 7x$$

[2] $3x^6 - 3x^3 + x^2 + -2x^5 + x^4 - 3x^3 + -3x^5 + 2x^4 - 4x^2 = 3x^6 - 5x^5 + 3x^4 - 6x^3 - 3x^2$
[3] $x^3 + 2x^2 + -2x^5 - 4x^2 + 4x + -3x^3 - 4x^2 - x = -2x^5 - 2x^3 - 6x^2 + 3x$
[4] $x^6 + 2x^3 + -4x^6 + 2x^3 + x^4 = -3x^6 + x^4 + 4x^3$
[5] $2x^5 - 2x^2 + -2x^3 + -x^6 - 4x^3 - x^2 = -x^6 + 2x^5 - 6x^3 - 3x^2$
[6] $-5x^3 + 3x + (-7x^2) + (-8x^5 - 2x^2) = -8x^5 - 5x^3 - 9x^2 + 3x$
[7] $4x^3 - 4x^2 - x + x^6 - 3x^4 + 2x^2 + -5x^6 + 2x^4 = -4x^6 - x^4 + 4x^3 - 2x^2 - x$
[8] $3x^4 - 3x^2 + 2x + -x^6 + 4x^5 - 2x^2 + -4x^3 + 3x^2 + 3x = -x^6 + 4x^5 + 3x^4 - 4x^3 - 2x^2 + 5x$
[9] $-2x^5 - 2x^4 - x^3 + (-x^6 - x^5 - 4x^2) + (-3x^5 - 5x^4) = -x^6 - 6x^5 - 7x^4 - x^3 - 4x^2$
[10] $3x^6 + 2x^2 + -x^6 - 5x^3 + 4x^5 - 4x^4 + x = 2x^6 + 4x^5 - 4x^4 - 5x^3 + 2x^2 + x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 3x^2y-2xy^2+-4xy+-6x^2y-4xy^2=-3x^2y-6xy^2-4xy \\ [3] \quad 2x^2y-8xy+-18x^2y^2-8xy+-20xy^2=-18x^2y^2+2x^2y-20xy^2-16xy \\ [4] \quad -12x^2y+12xy^2+(-6x^2y^2+12xy^2+12xy)+(-12xy^2+15xy)=-6x^2y^2-12x^2y+12xy^2+27xy \\ [5] \quad 64x^2y^2-12x^2y+-4x^2y^2+12x^2y+64x^2y^2+16xy^2-48xy=124x^2y^2+16xy^2-48xy \\ [6] \quad 20x^2y^2+100xy^2-5xy+25x^2y^2-75x^2y+50xy^2+-75xy=45x^2y^2-75x^2y+150xy^2-80xy \\ [7] \quad 60x^2y+6xy+72x^2y^2+36x^2y-144xy+-6x^2y^2-24x^2y-24xy^2=66x^2y^2+72x^2y-24xy^2-138xy \\ [8] \quad 147x^2y+-49x^2y^2+42xy+(-294x^2y^2-7xy)=-343x^2y^2+147x^2y+35xy \\ [9] \quad 16x^2y^2+32x^2y-64xy^2+64x^2y+56xy+208x^2y^2-192x^2y=224x^2y^2-96x^2y-64xy^2+56xy \\ [10] \quad 243x^2y^2+9x^2y+162xy+9x^2y^2+27x^2y-324xy+-9x^2y^2-9x^2y-243xy=243x^2y^2+27x^2y-405xy \\ [10] \quad 243x^2y^2+9x^2y+162xy+9x^2y^2+27x^2y-324xy+-9x^2y^2-9x^2y-243xy=243x^2y^2+27x^2y-405xy \\ [243x^2y^2+27x^2y-405xy]$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 2x^2y^2 + x^2y + -3x^2y^2 + x^2y + xy - (-2xy) = -x^2y^2 + 2x^2y + 3xy \\ &[3] \quad 8x^2y^2 - 6xy^2 - 6xy + -4x^2y^2 - 16x^2y + 16xy^2 - (16x^2y^2 + 6xy^2 - 16xy) = \\ &-12x^2y^2 - 16x^2y + 4xy^2 + 10xy \\ &[4] \quad -6x^2y^2 + 27x^2y + 27xy - (24x^2y + 9xy^2) + (-3x^2y^2 + 27x^2y - 12xy) = \\ &-9x^2y^2 + 30x^2y - 9xy^2 + 15xy \\ &[5] \quad -64x^2y^2 - 16xy^2 + -16x^2y^2 + 80xy^2 - (-40x^2y + 64xy^2) = -80x^2y^2 + 40x^2y \end{aligned}$$

$$[6] \quad 60\,x^2y^2 - 5\,xy^2 + -15\,x^2y^2 + 15\,x^2y - 50\,xy^2 - (5\,x^2y + 90\,xy) = 45\,x^2y^2 + 10\,x^2y - 55\,xy^2 - 90\,xy$$

$$[7] \quad -72\,x^2y - 18\,xy^2 - (-72\,x^2y + 120\,xy) + (-72\,x^2y^2 - 36\,xy) = -72\,x^2y^2 - 18\,xy^2 - 156\,xy$$

$$[8] \quad -7\,xy^2 + -147\,x^2y^2 - 147\,xy^2 - 196\,xy - (-147\,x^2y^2 - 245\,x^2y) = 245\,x^2y - 154\,xy^2 - 196\,xy$$

$$[9] \quad -128\,x^2y + 56\,xy^2 + 256\,xy - (-128\,x^2y^2 + 248\,xy) = 128\,x^2y^2 - 128\,x^2y + 56\,xy^2 + 8\,xy$$

$$[10] \quad 324\,x^2y^2 - 162\,x^2y + 27\,xy^2 - (-45\,x^2y^2 + 27\,xy^2) + (-90\,x^2y + 27\,xy) = 369\,x^2y^2 - 252\,x^2y + 27\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-4\,b^2x^2y^2z^3) \cdot (-3\,b^3x^2y^3z) = 12\,b^5x^4y^5z^4 \\ &[3] \quad (-12\,b^3xy^3z^2) \cdot (-16\,b^3x^3y^3z^2) = 192\,b^6x^4y^6z^4 \\ &[4] \quad (-54\,b^2x^3y^2z) \cdot (-108\,b^2xy^3z^2) = 5832\,b^4x^4y^5z^3 \\ &[5] \quad (128\,b^3xy^3z^3) \cdot (-48\,bx^3y^3z) = -6144\,b^4x^4y^6z^4 \\ &[6] \quad (10\,b^3x^2y^3z^3) \cdot (-50\,b^2xy^2z^3) = -500\,b^5x^3y^5z^6 \\ &[7] \quad (18\,bxy^3z^2) \cdot (-12\,b^2x^2y^3z) = -216\,b^3x^3y^6z^3 \\ &[8] \quad (-49\,bxyz^2) \cdot (686\,bx^3yz^3) = -33614\,b^2x^4y^2z^5 \\ &[9] \quad (128\,b^2xy^3z^3) \cdot (-1024\,bxy^3z) = -131072\,b^3x^2y^6z^4 \\ &[10] \quad (-729\,bx^3y^3z^2) \cdot (-2916\,bx^2y^2z) = 2125764\,b^2x^5y^5z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-3x^2) \cdot (5x^2 + 2x) = -15x^4 - 6x^3$$

[2] $(-3x^2) \cdot (0) = 0$
[3] $(-x) \cdot (-4x^2 - x) = 4x^3 + x^2$
[4] $(-3x^2) \cdot (2x^2 + x) = -6x^4 - 3x^3$
[5] $(-4x) \cdot (2x^2) = -8x^3$
[6] $(x) \cdot (2x^2 + 8x) = 2x^3 + 8x^2$
[7] $(-2x^2) \cdot (4x^2 - 7x) = -8x^4 + 14x^3$
[8] $(-2x) \cdot (2x^2) = -4x^3$
[9] $(-3x) \cdot (7x^2 - 3x) = -21x^3 + 9x^2$
[10] $(2x^2) \cdot (6x^2 + 2x) = 12x^4 + 4x^3$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x)\cdot(4\,x^2) = -8\,x^3 \\ &[2] \quad (8\,x^2)\cdot(-4\,x^2) = -32\,x^4 \\ &[3] \quad (-x^2-x)\cdot(-3\,x) = 3\,x^3 + 3\,x^2 \\ &[4] \quad (3\,x^2-4\,x)\cdot(-5\,x^2-x) = -15\,x^4 + 17\,x^3 + 4\,x^2 \\ &[5] \quad (-2\,x)\cdot(2\,x) = -4\,x^2 \\ &[6] \quad (-5\,x)\cdot(-3\,x^2-7\,x) = 15\,x^3 + 35\,x^2 \end{aligned}$$

[7]
$$(-2x^2 + x) \cdot (2x^2 - 4x) = -4x^4 + 10x^3 - 4x^2$$

[8]
$$(4x^2 - 4x) \cdot (-2x^2 + 4x) = -8x^4 + 24x^3 - 16x^2$$

[9]
$$(-2x^2) \cdot (0) = 0$$

[10]
$$(x^2 - x) \cdot (-5x^2 + x) = -5x^4 + 6x^3 - x^2$$

[11]
$$(-x^2) \cdot (-6x^2 - 2x) = 6x^4 + 2x^3$$

[12]
$$(x^2) \cdot (-x^2 + 2x) = -x^4 + 2x^3$$

[13]
$$(-x^2 + 3x) \cdot (-x^2 + x) = x^4 - 4x^3 + 3x^2$$

[14]
$$(-4x^2) \cdot (-2x^2 - 7x) = 8x^4 + 28x^3$$

[15]
$$(-x^2 + 4x) \cdot (-2x^2 - 2x) = 2x^4 - 6x^3 - 8x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(4x^2) \cdot (4x^3 + x^2 - 4x) = 16x^5 + 4x^4 - 16x^3$$

[2]
$$(4x^3) \cdot (-x^2 + 2x) = -4x^5 + 8x^4$$

[3]
$$(-5x^2) \cdot (-7x^2 + x) = 35x^4 - 5x^3$$

[4]
$$(-6x^2 + 3x) \cdot (4x^3 - x) = -24x^5 + 12x^4 + 6x^3 - 3x^2$$

[5]
$$(-2x^2 - 3x) \cdot (2x^3 - 4x^2) = -4x^5 + 2x^4 + 12x^3$$

[6]
$$(5x^2) \cdot (-4x^3 + x^2) = -20x^5 + 5x^4$$

[7]
$$(3x^2) \cdot (4x^3 - 3x^2 - x) = 12x^5 - 9x^4 - 3x^3$$

[8]
$$(4x^2) \cdot (7x^3 - 2x^2 + 4x) = 28x^5 - 8x^4 + 16x^3$$

[9]
$$(4x^3 + 3x^2) \cdot (2x^3 - 5x^2) = 8x^6 - 14x^5 - 15x^4$$

[10]
$$(2x^3 + x^2) \cdot (2x^3 - x) = 4x^6 + 2x^5 - 2x^4 - x^3$$

[11]
$$(-2x^3) \cdot (-2x^3 + 6x) = 4x^6 - 12x^4$$

[12]
$$(-4x) \cdot (-2x^3 - x^2) = 8x^4 + 4x^3$$

[13]
$$(2x^3 - x) \cdot (4x) = 8x^4 - 4x^2$$

[14]
$$(5x^2) \cdot (-7x^2 + x) = -35x^4 + 5x^3$$

[15]
$$(0) \cdot (9x^2 - 2x) = 0$$

[16]
$$(-4x^2) \cdot (-3x^2 + x) = 12x^4 - 4x^3$$

[17]
$$(x^3 + 4x^2) \cdot (-4x) = -4x^4 - 16x^3$$

[18]
$$(2x^3 + x^2) \cdot (2x^3 - 3x^2 - x) = 4x^6 - 4x^5 - 5x^4 - x^3$$

[19]
$$(-x^3 + x) \cdot (4x^3 - 3x^2) = -4x^6 + 3x^5 + 4x^4 - 3x^3$$

[20]
$$(-x^3 - 4x^2) \cdot (4x^3 + 5x^2) = -4x^6 - 21x^5 - 20x^4$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-4x^2y + 3xy) \cdot (-2x^2y^2 + 2xy^2 + 3xy) = 8x^4y^3 - 14x^3y^3 - 12x^3y^2 + 6x^2y^3 + 9x^2y^2$$

[2]
$$(3x^2y + 3xy) \cdot (-2xy^2 - 5xy) = -6x^3y^3 - 15x^3y^2 - 6x^2y^3 - 15x^2y^2$$

[3]
$$(-5xy) \cdot (-2x^2y^2 - 4x^2y + 3xy) = 10x^3y^3 + 20x^3y^2 - 15x^2y^2$$

[4]
$$(-4x^2y^2 + 2xy^2) \cdot (-3x^2y^2 - 4x^2y) = 12x^4y^4 + 16x^4y^3 - 6x^3y^4 - 8x^3y^3$$

[5]
$$(3x^2y^2 - xy^2) \cdot (x^2y^2 + 3x^2y + xy) = 3x^4y^4 + 9x^4y^3 - x^3y^4 - x^2y^3$$

[5]
$$(3x^2y^2 - xy^2) \cdot (x^2y^2 + 3x^2y + xy) = 3x^4y^4 + 9x^4y^3 - x^3y^4 - x^2y^3$$

[6] $(-3x^2y^2 - x^2y) \cdot (4x^2y^2 - 2xy^2 - xy) = -12x^4y^4 - 4x^4y^3 + 6x^3y^4 + 5x^3y^3 + x^3y^2$

[7]
$$(0) \cdot (x^2y^2 + xy^2 + xy) = 0$$