1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$3x^6 + 4x^3 - 4x^2 + -3x^5 + 3x^4 + 3x^4 - 2x = 3x^6 - 3x^5 + 6x^4 + 4x^3 - 4x^2 - 2x$$

[2] $3x^5 + x^4 - 4x^2 + -2x^5 - 2x + -2x^5 + x = -x^5 + x^4 - 4x^2 - x$
[3] $x^4 - 5x^3 + -3x^5 + 2x^2 + x^5 - 4x^4 - 4x = -2x^5 - 3x^4 - 5x^3 + 2x^2 - 4x$
[4] $-3x^6 + x^3 - 4x^2 + (-3x^4 - 4x^3 - 3x^2) + (-3x^4 - x^3 - 2x^2) = -3x^6 - x^4 - x^3 - x^4 - x^4 - x^4 - x^3 - x^4 - x^$

$$6x^{4} - 4x^{3} - 9x^{2}$$

$$[5] 4x^{6} + x^{5} + x^{2} + -x^{5} + 7x^{3} + (-x^{6} + 3x^{5}) = 3x^{6} + 3x^{5} + 7x^{3} + x^{2}$$

[6]
$$3x^5 + 4x^2 + -x^6 + x^3 + 4x^6 - 4x^5 + 3x^2 = 3x^6 - x^5 + x^3 + 7x^2$$

[7]
$$7x^6 + x^2 + -3x + -2x^4 = 7x^6 - 2x^4 + x^2 - 3x$$

[8]
$$2x^6 + 3x^3 - x + 2x^6 - 3x^5 + 2x + 2x^6 - 3x^4 = 6x^6 - 3x^5 - 3x^4 + 3x^3 + x$$

$$[9] \quad 2\,x^6 - 2\,x^4 + 3\,x^2 + -3\,x^6 - x^5 + 3\,x^2 + (-x^5 - x^4) = -x^6 - 2\,x^5 - 3\,x^4 + 6\,x^2$$

[10]
$$x^4 + 2x^3 - 2x + x^6 - 6x^4 = -x^6 - 5x^4 - 2x^3 - 2x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0$$

$$[2] \quad 3x^2y^2-x^2y+-3x^2y^2-4x^2y-4xy+(-4x^2y^2-5xy)=-4x^2y^2-5x^2y-9\,xy$$

$$[3] \quad 4x^2y-16\,xy^2+6\,xy+8\,x^2y^2+8\,x^2y-2\,xy^2+6\,x^2y^2+12\,xy^2-2\,xy=14\,x^2y^2+12\,x^2y-6\,xy^2+4\,xy$$

$$[4] \quad 6x^2y^2+12\,x^2y+18\,xy^2+3\,x^2y+36\,xy^2+9\,x^2y^2=15\,x^2y^2+15\,x^2y+54\,xy^2$$

$$[5] \quad 80\,x^2y-12\,xy^2+16\,x^2y+-64\,x^2y^2+8\,x^2y-48\,xy^2=-64\,x^2y^2+104\,x^2y-60\,xy^2$$

$$[6] \quad -5\,x^2y^2+15\,x^2y+(-80\,xy^2)+(-10\,x^2y-10\,xy^2+20\,xy)=-5\,x^2y^2+5\,x^2y-90\,xy^2+20\,xy$$

$$[7] \quad 84\,x^2y^2+108\,x^2y+-102\,x^2y^2+108\,xy+-36\,x^2y^2+84\,x^2y=-54\,x^2y^2+192\,x^2y+108\,xy$$

$$[8] \quad 98\,x^2y^2+49\,xy^2-14\,xy+-49\,x^2y-49\,xy^2+7\,xy+49\,x^2y^2-21\,x^2y+14\,xy^2=147\,x^2y^2-70\,x^2y+14\,xy^2-7\,xy$$

$$[9] \quad 8\,xy^2+-192\,x^2y^2-272\,xy+256\,xy^2+192\,xy=-192\,x^2y^2+264\,xy^2-80\,xy$$

$$[10] \quad 243\,x^2y^2-18\,x^2y+-81\,xy+(-162\,x^2y^2+27\,xy^2+162\,xy)=81\,x^2y^2-162\,xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

 $18x^2y + 27xy^2 + 81xy$

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y - 3\,xy^2 - 3\,xy + 3\,x^2y + 2\,xy - (-3\,x^2y^2 + x^2y + 2\,xy^2) = 3\,x^2y^2 - 5\,xy^2 - xy \\ &[3] \quad 10\,x^2y^2 + 8\,x^2y + 6\,x^2y + 4\,xy - (-2\,xy) = 10\,x^2y^2 + 14\,x^2y + 6\,xy \\ &[4] \quad 12\,x^2y + 3\,xy^2 + 6\,xy - (-27\,x^2y^2 + 18\,xy) + (27\,x^2y^2 + 36\,x^2y + 12\,xy) = 54\,x^2y^2 + 48\,x^2y + 3\,xy^2 \\ &[5] \quad 64\,x^2y - 32\,xy + -32\,x^2y^2 + 64\,xy^2 + 32\,xy - (64\,x^2y^2 - 24\,xy^2) = -96\,x^2y^2 + 64\,x^2y + 88\,xy^2 \end{aligned}$$

$$[6] \quad 5\,x^2y^2 + 25\,xy + 50\,x^2y^2 + 5\,xy^2 + 10\,xy - (10\,x^2y^2 - 5\,xy) = 45\,x^2y^2 + 5\,xy^2 + 40\,xy \\ [7] \quad -24\,xy^2 - 24\,xy - (6\,xy^2 - 12\,xy) + (90\,x^2y) = 90\,x^2y - 30\,xy^2 - 12\,xy \\ [8] \quad -98\,x^2y - 49\,xy + -21\,x^2y^2 + 14\,x^2y - 14\,xy - (-49\,x^2y + 196\,xy^2 - 28\,xy) = -21\,x^2y^2 - 35\,x^2y - 196\,xy^2 - 35\,xy \\ [9] \quad 8\,x^2y^2 + 232\,x^2y + -192\,x^2y^2 + 200\,xy^2 - (160\,x^2y - 24\,xy) = -184\,x^2y^2 + 72\,x^2y + 200\,xy^2 + 24\,xy \\ [10] \quad -243\,x^2y + 27\,xy^2 - (243\,x^2y^2 + 117\,x^2y) + (360\,x^2y + 36\,xy) = -243\,x^2y^2 + 27\,xy^2 + 36\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (4\,b^3x^2y^2z) \cdot (4\,b^2x^3yz) = 16\,b^5x^5y^3z^2 \\ &[3] \quad (4\,bx^2yz^2) \cdot (-6\,b^3x^2y^3z^2) = -24\,b^4x^4y^4z^4 \\ &[4] \quad (-27\,bxy^2z) \cdot (-36\,b^2xyz^3) = 972\,b^3x^2y^3z^4 \\ &[5] \quad (-64\,bx^3yz) \cdot (-16\,b^2x^3yz^2) = 1024\,b^3x^6y^2z^3 \\ &[6] \quad (-375\,b^2x^3y^2z) \cdot (25\,b^2xy^3z^2) = -9375\,b^4x^4y^5z^3 \\ &[7] \quad (36\,bx^3y^2z^2) \cdot (18\,bx^2y^2z) = 648\,b^2x^5y^4z^3 \\ &[8] \quad (21\,b^2x^2yz^3) \cdot (-7\,bx^2yz^2) = -147\,b^3x^4y^2z^5 \\ &[9] \quad (-8\,b^2xy^3z^2) \cdot (-16\,bx^3y^2z) = 128\,b^3x^4y^5z^3 \\ &[10] \quad (-243\,b^2x^2y^2z^3) \cdot (2916\,b^2xyz^3) = -708588\,b^4x^3y^3z^6 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x^2)\cdot(-3\,x) = -12\,x^3 \\ &[2] \quad (-3\,x^2)\cdot(x^2+3\,x) = -3\,x^4-9\,x^3 \\ &[3] \quad (2\,x)\cdot(-4\,x^2-4\,x) = -8\,x^3-8\,x^2 \\ &[4] \quad (-4\,x^2)\cdot(4\,x^2) = -16\,x^4 \\ &[5] \quad (3\,x)\cdot(4\,x^2-4\,x) = 12\,x^3-12\,x^2 \\ &[6] \quad (-3\,x^2)\cdot(-3\,x^2-7\,x) = 9\,x^4+21\,x^3 \\ &[7] \quad (-2\,x)\cdot(-x^2+3\,x) = 2\,x^3-6\,x^2 \\ &[8] \quad (4\,x^2)\cdot(14\,x^2) = 56\,x^4 \\ &[9] \quad (-4\,x^2)\cdot(-x^2) = 4\,x^4 \\ &[10] \quad (x)\cdot(2\,x^2+x) = 2\,x^3+x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(4x^2 + 3x) \cdot (2x^2 - 4x) = 8x^4 - 10x^3 - 12x^2$$

[2] $(6x) \cdot (-2x^2 - x) = -12x^3 - 6x^2$
[3] $(-3x^2 + 4x) \cdot (x^2 - x) = -3x^4 + 7x^3 - 4x^2$
[4] $(x^2 - 2x) \cdot (-4x^2 + 2x) = -4x^4 + 10x^3 - 4x^2$
[5] $(-4x^2) \cdot (x^2) = -4x^4$
[6] $(x^2 + 2x) \cdot (-7x) = -7x^3 - 14x^2$
[7] $(x^2 + x) \cdot (x^2) = x^4 + x^3$

[8]
$$(x^2 - 4x) \cdot (-3x^2 - x) = -3x^4 + 11x^3 + 4x^2$$

[9]
$$(5x) \cdot (-x^2 - x) = -5x^3 - 5x^2$$

[10]
$$(x) \cdot (x^2 - 4x) = x^3 - 4x^2$$

[11]
$$(3x^2 + 4x) \cdot (-7x) = -21x^3 - 28x^2$$

[12]
$$(-7x^2) \cdot (4x^2) = -28x^4$$

[13]
$$(2x^2 - 2x) \cdot (3x^2 - x) = 6x^4 - 8x^3 + 2x^2$$

[14]
$$(-2x^2 - 2x) \cdot (-4x^2 + x) = 8x^4 + 6x^3 - 2x^2$$

[15]
$$(x^2 - 4x) \cdot (-4x^2 - 2x) = -4x^4 + 14x^3 + 8x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(2x^3 - 8x^2) \cdot (3x^2) = 6x^5 - 24x^4$$

[2]
$$(-2x^3 + 4x^2) \cdot (-x^3 + x^2 - x) = 2x^6 - 6x^5 + 6x^4 - 4x^3$$

[3]
$$(2x^2) \cdot (2x^3 - 2x^2 - 3x) = 4x^5 - 4x^4 - 6x^3$$

[4]
$$(2x^3 + x^2) \cdot (4x^3 - 4x^2) = 8x^6 - 4x^5 - 4x^4$$

[5]
$$(6x^3) \cdot (2x^3 - 2x) = 12x^6 - 12x^4$$

[6]
$$(4x^3 + 4x^2) \cdot (-x^3 - x) = -4x^6 - 4x^5 - 4x^4 - 4x^3$$

[7]
$$(-2x^3 + x) \cdot (x^3 - x^2) = -2x^6 + 2x^5 + x^4 - x^3$$

[8]
$$(3x^2 - 4x) \cdot (-x^3 - 6x^2 - x) = -3x^5 - 14x^4 + 21x^3 + 4x^2$$

[9]
$$(-2x^2) \cdot (-2x^2 + x) = 4x^4 - 2x^3$$

[10]
$$(-5x^2) \cdot (-7x) = 35x^3$$

[11]
$$(-4x^3 + 3x) \cdot (4x^3 + 3x) = -16x^6 + 9x^2$$

[12]
$$(-3x^2 + 4x) \cdot (-2x^3 - 2x) = 6x^5 - 8x^4 + 6x^3 - 8x^2$$

[13]
$$(x^3 + 5x) \cdot (-x^2 - 2x) = -x^5 - 2x^4 - 5x^3 - 10x^2$$

[14]
$$(2x^3 - 4x^2) \cdot (-4x^3 + 3x^2 + 2x) = -8x^6 + 22x^5 - 8x^4 - 8x^3$$

[15]
$$(-x^2 - x) \cdot (-5x^3 + 4x^2 - 4x) = 5x^5 + x^4 + 4x^2$$

[16]
$$(6x^2 - 4x) \cdot (-x^3 - 4x^2 - x) = -6x^5 - 20x^4 + 10x^3 + 4x^2$$

[17]
$$(-x^3) \cdot (4x^3 + 2x^2) = -4x^6 - 2x^5$$

[18]
$$(5x^3) \cdot (-2x^3 + 4x) = -10x^6 + 20x^4$$

[19]
$$(-4x^2 + x) \cdot (x^3 + x^2) = -4x^5 - 3x^4 + x^3$$

[20]
$$(x^3 - x) \cdot (-x^3 + 2x^2) = -x^6 + 2x^5 + x^4 - 2x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^2y + xy) \cdot (4x^2y^2 + x^2y) = -4x^4y^3 - x^4y^2 + 4x^3y^3 + x^3y^2$$

[2]
$$(-2x^2y + 4xy) \cdot (-3x^2y^2 - 3x^2y + 2xy^2) = 6x^4y^3 + 6x^4y^2 - 16x^3y^3 - 12x^3y^2 + 8x^2y^3$$

[3]
$$(4x^2y^2 - 2x^2y) \cdot (-2x^2y^2 + 3xy^2) = -8x^4y^4 + 4x^4y^3 + 12x^3y^4 - 6x^3y^3$$

$$[4] \quad (-2\,x^2y + 4\,xy^2) \cdot (-4\,x^2y^2 - 2\,xy^2 - xy) = 8\,x^4y^3 - 16\,x^3y^4 + 4\,x^3y^3 - 8\,x^2y^4 + 2\,x^3y^2 - 4\,x^2y^3$$

[5]
$$(0) \cdot (-x^2y^2 + x^2y + 4xy) = 0$$

[6]
$$(-3x^2y^2 + 2xy^2) \cdot (-x^2y^2 - 4x^2y) = 3x^4y^4 + 12x^4y^3 - 2x^3y^4 - 8x^3y^3$$

[7]
$$(4x^2y^2) \cdot (4x^2y - 7xy^2) = 16x^4y^3 - 28x^3y^4$$