1. Evaluación 1ºD - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 4x^4 + 5x^3 + -7x^5 - 3x + -x^6 + x^5 - 3x^4 = -x^6 - 6x^5 + x^4 + 5x^3 - 3x$$

$$[2] \quad 4x^6 + x^3 + -3x^6 - x^4 + 2x^3 + -3x^4 + 7x^3 = x^6 - 4x^4 + 10x^3$$

$$[3] \quad 4x^3 + 5x^2 + x^6 - 4x^2 - 3x + -x^2 = x^6 + 4x^3 - 3x$$

$$[4] \quad 6x^4 - x^3 + -4x^3 - x^2 - x + (-3x^6 - 2x^4 - 3x) = -3x^6 + 4x^4 - 5x^3 - x^2 - 4x$$

$$[5] \quad 4x^6 + 3x^3 - x^2 + -2x^6 + x^5 + 2x^4 + -2x^6 - 2x^2 - 4x = x^5 + 2x^4 + 3x^3 - 3x^2 - 4x$$

$$[6] \quad 3x^5 - 2x^3 - 4x^2 + 3x^6 - 2x^5 + 2x^2 + -3x^3 + 2x = 3x^6 + x^5 - 5x^3 - 2x^2 + 2x$$

$$[7] \quad 3x^3 - x^2 - 2x + -2x^6 - 2x^3 - 4x^2 + 4x^6 + x^4 = 2x^6 + x^4 + x^3 - 5x^2 - 2x$$

$$[8] \quad 4x^6 + x^4 + 3x^6 - x^2 + -2x^6 + 3x^5 + x = 5x^6 + 3x^5 + x^4 - x^2 + x$$

$$[9] \quad 3x^3 - 3x^2 - 2x + -2x^5 + 4x^4 - 3x^2 + -4x^6 + 3x^4 - 4x = -4x^6 - 2x^5 + 7x^4 + 3x^3 - 6x^2 - 6x$$

[10]
$$x^6 - 4x^2 + 4x + -4x^5 - 4x^4 - 3x^2 + x^4 - 3x = x^6 - 4x^5 - 3x^4 - 7x^2 + x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0$$

$$[2] \quad 7x^2y-2xy^2+3x^2y^2-4xy^2+xy+2x^2y^2+3xy^2-4xy=5x^2y^2+7x^2y-3xy^2-3xy$$

$$[3] \quad 4xy^2-14xy+-10xy^2+8xy+16xy^2=10xy^2-6xy$$

$$[4] \quad 15x^2y^2-3x^2y+15x^2y^2-12xy^2+27x^2y^2+6xy^2-12xy=57x^2y^2-3x^2y-6xy^2-12xy$$

$$[5] \quad -76x^2y^2+4xy+(-16x^2y^2-8x^2y+48xy)+(-56x^2y^2)=-148x^2y^2-8x^2y+52xy$$

$$[6] \quad 10x^2y^2+75x^2y-50xy+-100x^2y-50xy+90x^2y^2+5x^2y=100x^2y^2-20x^2y-100xy$$

$$[7] \quad 6x^2y^2-144x^2y-6xy+-6x^2y+42xy^2+90xy^2-144xy=6x^2y^2-150x^2y+132xy^2-150xy$$

$$[8] \quad 196x^2y^2-21x^2y+49xy^2+-105x^2y-21xy+-168x^2y+49xy^2=196x^2y^2-294x^2y+98xy^2-21xy$$

$$[9] \quad 8x^2y^2-128xy+24x^2y^2-272xy+64x^2y^2+8x^2y-8xy^2=96x^2y^2+8x^2y-8xy^2-400xy$$

$$[10] \quad -324x^2y+81xy+(-243xy)+(-333x^2y+243xy^2)=-657x^2y+243xy^2-162xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -2\,x^2y^2 + x^2y - 4\,xy^2 + x^2y^2 + 4\,x^2y - (x^2y^2 - 3\,xy^2 + xy) = -2\,x^2y^2 + 5\,x^2y - xy^2 - xy \end{aligned}$$

$$\begin{aligned} &[3] \quad 8\,x^2y - 10\,xy^2 + -16\,x^2y^2 + 16\,x^2y - 16\,xy^2 - (-6\,x^2y^2 + 2\,x^2y - 8\,xy) = -10\,x^2y^2 + 22\,x^2y - 26\,xy^2 + 8\,xy \end{aligned}$$

$$\begin{aligned} &[4] \quad -24\,x^2y - 6\,xy^2 - (-6\,x^2y - 15\,xy^2) + (3\,x^2y^2 + 9\,xy^2) = 3\,x^2y^2 - 18\,x^2y + 18\,xy^2 \end{aligned}$$

$$\begin{aligned} &[5] \quad 64\,x^2y + 12\,xy + -4\,x^2y + 16\,xy - (16\,x^2y^2 + 24\,xy) = -16\,x^2y^2 + 60\,x^2y + 4\,xy \end{aligned}$$

$$[6] \quad -10\,x^2y + 50\,xy^2 - 25\,xy + -50\,xy^2 - 50\,xy - (25\,x^2y - 25\,xy^2) = -35\,x^2y + 25\,xy^2 - 75\,xy$$

$$[7] \quad 120\,x^2y^2 + 18\,xy^2 - (-90\,x^2y - 24\,xy^2) + (-18\,x^2y^2 + 12\,xy) = 102\,x^2y^2 + 90\,x^2y + 42\,xy^2 + 12\,xy$$

$$[8] \quad 28\,x^2y - 168\,xy^2 + 14\,x^2y^2 + 105\,x^2y - (7\,x^2y^2 - 196\,x^2y + 147\,xy^2) = 7\,x^2y^2 + 329\,x^2y - 315\,xy^2$$

$$[9] \quad 16\,x^2y^2 - 128\,xy^2 + 64\,xy + 40\,x^2y^2 - 64\,xy^2 - (-8\,x^2y^2 - 128\,xy^2 + 64\,xy) = 64\,x^2y^2 - 64\,xy^2$$

$$[10] \quad 81\,x^2y^2 - 324\,x^2y - 36\,xy^2 - (18\,x^2y^2 + 243\,xy) + (-162\,x^2y^2 - 36\,xy^2 - 27\,xy) = -99\,x^2y^2 - 324\,x^2y - 72\,xy^2 - 270\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-bx^2y^3z^2) \cdot (3\,b^3x^2y^3z^2) = -3\,b^4x^4y^6z^4 \\ &[3] \quad (-24\,b^2x^3y^2z^3) \cdot (-4\,b^2x^3yz^3) = 96\,b^4x^6y^3z^6 \\ &[4] \quad (12\,b^2xy^3z^2) \cdot (27\,b^3x^3yz^2) = 324\,b^5x^4y^4z^4 \\ &[5] \quad (16\,bxyz^2) \cdot (128\,b^3x^3y^3z^3) = 2048\,b^4x^4y^4z^5 \\ &[6] \quad (-75\,b^3xy^3z) \cdot (10\,b^2x^3y^3z^2) = -750\,b^5x^4y^6z^3 \\ &[7] \quad (-108\,bxy^3z^2) \cdot (-12\,b^3x^3y^2z^3) = 1296\,b^4x^4y^5z^5 \\ &[8] \quad (1029\,b^2x^2y^3z) \cdot (-147\,bx^2y^2z) = -151263\,b^3x^4y^5z^2 \\ &[9] \quad (32\,b^3xy^2z^2) \cdot (-1024\,b^2x^3y^2z^2) = -32768\,b^5x^4y^4z^4 \\ &[10] \quad (-2187\,b^2xy^2z^3) \cdot (-1458\,b^3x^3yz^2) = 3188646\,b^5x^4y^3z^5 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x)\cdot(-3\,x^2+5\,x) = 6\,x^3-10\,x^2 \\ &[2] \quad (3\,x^2)\cdot(5\,x^2-x) = 15\,x^4-3\,x^3 \\ &[3] \quad (-4\,x)\cdot(-x^2+3\,x) = 4\,x^3-12\,x^2 \\ &[4] \quad (3\,x)\cdot(6\,x^2+4\,x) = 18\,x^3+12\,x^2 \\ &[5] \quad (4\,x^2)\cdot(-3\,x^2) = -12\,x^4 \\ &[6] \quad (-x^2)\cdot(-5\,x^2-x) = 5\,x^4+x^3 \\ &[7] \quad (-2\,x^2)\cdot(7\,x^2-3\,x) = -14\,x^4+6\,x^3 \\ &[8] \quad (x)\cdot(-2\,x^2+4\,x) = -2\,x^3+4\,x^2 \\ &[9] \quad (4\,x^2)\cdot(-8\,x) = -32\,x^3 \\ &[10] \quad (3\,x)\cdot(x^2+2\,x) = 3\,x^3+6\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(0) \cdot (4x^2) = 0$$

[2] $(-2x) \cdot (2x^2) = -4x^3$
[3] $(4x^2 + x) \cdot (-8x^2 + 4x) = -32x^4 + 8x^3 + 4x^2$
[4] $(7x^2) \cdot (2x^2) = 14x^4$
[5] $(4x^2 - 2x) \cdot (3x) = 12x^3 - 6x^2$
[6] $(-x^2 - 4x) \cdot (-5x) = 5x^3 + 20x^2$

[7]
$$(-2x^2 + 3x) \cdot (-2x^2 - 4x) = 4x^4 + 2x^3 - 12x^2$$

[8]
$$(2x^2) \cdot (2x^2 - x) = 4x^4 - 2x^3$$

[9]
$$(4x^2 - 2x) \cdot (5x^2 + 4x) = 20x^4 + 6x^3 - 8x^2$$

[10]
$$(5x) \cdot (-5x) = -25x^2$$

[11]
$$(-4x) \cdot (2x^2 - 4x) = -8x^3 + 16x^2$$

[12]
$$(0) \cdot (-x^2) = 0$$

[13]
$$(3x^2 + 4x) \cdot (-x^2 - 3x) = -3x^4 - 13x^3 - 12x^2$$

[14]
$$(2x^2 + x) \cdot (-5x^2 + x) = -10x^4 - 3x^3 + x^2$$

[15]
$$(2x^2) \cdot (0) = 0$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-x^3 + 6x) \cdot (-3x^2) = 3x^5 - 18x^3$$

[2]
$$(-3x^3 - 3x^2) \cdot (-x^3 - 4x^2 - 3x) = 3x^6 + 15x^5 + 21x^4 + 9x^3$$

[3]
$$(3x^2 + 4x) \cdot (4x) = 12x^3 + 16x^2$$

[4]
$$(4x^3 - 4x) \cdot (x^3 + x) = 4x^6 - 4x^2$$

[5]
$$(4x^3 - 2x) \cdot (3x^2 - 3x) = 12x^5 - 12x^4 - 6x^3 + 6x^2$$

[6]
$$(-x^2 + 2x) \cdot (-4x^3 + 3x^2) = 4x^5 - 11x^4 + 6x^3$$

[7]
$$(4x^3 + 5x) \cdot (-4x^2 - 2x) = -16x^5 - 8x^4 - 20x^3 - 10x^2$$

[8]
$$(4x^3 + 2x) \cdot (5x^2 - 3x) = 20x^5 - 12x^4 + 10x^3 - 6x^2$$

[9]
$$(4x^3 + 2x) \cdot (2x^3 - 2x) = 8x^6 - 4x^4 - 4x^2$$

[10]
$$(-2x^3 - x^2) \cdot (-7x^3 + 4x^2) = 14x^6 - x^5 - 4x^4$$

[11]
$$(2x^3 - 4x) \cdot (4x^3 + 2x^2) = 8x^6 + 4x^5 - 16x^4 - 8x^3$$

[12]
$$(-4x) \cdot (2x^3 + 5x^2) = -8x^4 - 20x^3$$

[13]
$$(-x) \cdot (-2x^3 + 3x^2 - 3x) = 2x^4 - 3x^3 + 3x^2$$

[14]
$$(-2x^3 - 2x) \cdot (-6x^3 - 8x^2) = 12x^6 + 16x^5 + 12x^4 + 16x^3$$

[15]
$$(-x^3) \cdot (2x^2) = -2x^5$$

[16]
$$(-2x^3 + 2x^2) \cdot (-2x^3 + x) = 4x^6 - 4x^5 - 2x^4 + 2x^3$$

[17]
$$(-4x^2 - 4x) \cdot (-2x^3 - 2x^2 + 4x) = 8x^5 + 16x^4 - 8x^3 - 16x^2$$

[18]
$$(-2x^3 - 4x) \cdot (2x^2 + 4x) = -4x^5 - 8x^4 - 8x^3 - 16x^2$$

[19]
$$(7x^3 + 4x) \cdot (2x) = 14x^4 + 8x^2$$

[20]
$$(2x^3 - 2x^2) \cdot (x^2 - x) = 2x^5 - 4x^4 + 2x^3$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-xy^2 + 3xy) \cdot (4xy^2 + 3xy) = -4x^2y^4 + 9x^2y^3 + 9x^2y^2$$

[2]
$$(2xy^2 - 2xy) \cdot (-2xy) = -4x^2y^3 + 4x^2y^2$$

[3]
$$(2xy) \cdot (3x^2y^2 - xy) = 6x^3y^3 - 2x^2y^2$$

[4]
$$(3x^2y - 2xy) \cdot (-5x^2y^2 - x^2y) = -15x^4y^3 - 3x^4y^2 + 10x^3y^3 + 2x^3y^2$$

[5]
$$(2x^2y^2 - xy) \cdot (3x^2y^2 + 3x^2y) = 6x^4y^4 + 6x^4y^3 - 3x^3y^3 - 3x^3y^2$$

[6]
$$(-4x^2y + 2xy^2) \cdot (-6x^2y) = 24x^4y^2 - 12x^3y^3$$

[7]
$$(-4x^2y^2 - 2xy) \cdot (-2x^2y^2 + xy^2) = 8x^4y^4 - 4x^3y^4 + 4x^3y^3 - 2x^2y^3$$