1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad -7x^6 - 3x^5 + (-2x^6 - 3x^3 + x) + (-x^3 + 3x^2 + 3x) = -9x^6 - 3x^5 - 4x^3 + 3x^2 + 4x$$

$$[2] \quad 3x^4 + -3x^4 - 3x^2 + x + -x^6 - 3x^5 - 2x^4 = -x^6 - 3x^5 - 2x^4 - 3x^2 + x$$

$$[3] \quad 2x^6 + x^4 + x^3 + -x^6 + (-x^5 + 2x^4 - x)) = x^6 - x^5 + 3x^4 + x^3 - x$$

$$[4] \quad 2x^6 - 4x^4 - 2x + -3x^6 - 5x^5 + 4x^6 - 2x^3 - 3x = 3x^6 - 5x^5 - 4x^4 - 2x^3 - 5x$$

$$[5] \quad 3x^5 - x + -4x^6 + 2x^5 + x^3 + -4x^6 - 2x^2 + 2x = -8x^6 + 5x^5 + x^3 - 2x^2 + x$$

$$[6] \quad 3x^6 + x + -x^5 + 6x^4 + 4x^5 + x^3 + 2x = 3x^6 + 3x^5 + 6x^4 + x^3 + 3x$$

$$[7] \quad 3x^5 - 2x^2 - 4x + 4x^6 - x^5 - x^3 + 3x^4 + 3x^3 - 3x^2 = 4x^6 + 2x^5 + 3x^4 + 2x^3 - 5x^2 - 4x$$

$$[8] \quad 3x^6 - 5x^5 + x^6 + 2x^2 - 4x + -x^5 - x^4 - x^3 = 4x^6 - 6x^5 - x^4 - x^3 + 2x^2 - 4x$$

$$[9] \quad -x^6 - x + (-5x^6 - 3x^3) + (-x^3 - 2x) = -6x^6 - 4x^3 - 3x$$

$$[10] \quad 4x^6 + -x^4 - 3x^3 - 4x^2 + 4x^6 - x^4 - 3x^2 = 8x^6 - 2x^4 - 3x^3 - 7x^2$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0$$

$$[2] \quad x^2y-3\,xy+-x^2y^2+2\,xy^2+3\,xy+(-4\,x^2y-2\,xy) = -x^2y^2-3\,x^2y+2\,xy^2-2\,xy$$

$$[3] \quad 8\,x^2y^2-6\,x^2y+-20\,xy^2-8\,xy+(-12\,x^2y^2+8\,x^2y-16\,xy^2) = -4\,x^2y^2+2\,x^2y-36\,xy^2-8\,xy$$

$$[4] \quad 36\,x^2y-9\,xy+-15\,x^2y^2-9\,xy+3\,x^2y^2-12\,xy^2+9\,xy = -12\,x^2y^2+36\,x^2y-12\,xy^2-9\,xy$$

$$[5] \quad 32\,x^2y^2+80\,x^2y+32\,x^2y^2-60\,x^2y+-40\,x^2y+8\,xy=64\,x^2y^2-20\,x^2y+8\,xy$$

$$[6] \quad 100\,x^2y^2-10\,x^2y+50\,xy^2+-100\,xy^2+50\,xy^2+100\,xy^2+100\,xy = 40\,x^2y^2-10\,x^2y+150\,xy^2+100\,xy$$

$$[7] \quad 108\,xy^2+72\,xy+72\,x^2y^2-108\,xy^2-18\,xy+36\,x^2y^2-36\,x^2y+24\,xy = 108\,x^2y^2-36\,x^2y+78\,xy$$

$$[8] \quad 21\,x^2y^2+7\,xy^2+-21\,x^2y+14\,xy+49\,x^2y^2+7\,xy^2=70\,x^2y^2-21\,x^2y+14\,xy^2+14\,xy$$

$$[9] \quad 192\,x^2y^2+32\,xy^2+-16\,x^2y^2+160\,x^2y+128\,x^2y^2+192\,x^2y+32\,xy = 304\,x^2y^2+352\,x^2y+32\,xy^2+32\,xy$$

$$[10] \quad 27\,x^2y^2+288\,xy+-198\,x^2y^2+9\,xy+-54\,x^2y^2-27\,xy^2=-225\,x^2y^2-27\,xy^2+297\,xy$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -4\,x^2y^2 - 3\,x^2y - 2\,xy + 4\,x^2y^2 - xy^2 - (2\,x^2y^2 + x^2y - 4\,xy^2) = -2\,x^2y^2 - 4\,x^2y + 3\,xy^2 - 2\,xy \\ &[3] \quad -24\,x^2y + 2\,xy + -6\,x^2y^2 - 16\,x^2y + 4\,xy^2 - (-2\,x^2y^2 - 18\,xy) = -4\,x^2y^2 - 40\,x^2y + 4\,xy^2 + 20\,xy \\ &[4] \quad -27\,x^2y^2 + 21\,x^2y - (30\,xy^2 - 9\,xy) + (9\,x^2y^2 - 9\,x^2y - 6\,xy) = -18\,x^2y^2 + 12\,x^2y - 30\,xy^2 + 3\,xy \end{aligned}$$

$$[5] \quad 60\,x^2y - 32\,xy + 16\,x^2y^2 - 40\,xy^2 - (4\,x^2y^2 + 8\,x^2y - 8\,xy) = 12\,x^2y^2 + 52\,x^2y - 40\,xy^2 - 24\,xy \\ [6] \quad 95\,x^2y^2 + 20\,xy + -75\,x^2y^2 - 100\,x^2y - 5\,xy^2 - (-10\,x^2y - 25\,xy^2 + 15\,xy) = 20\,x^2y^2 - 90\,x^2y + 20\,xy^2 + 5\,xy \\ [7] \quad -6\,xy^2 + 96\,xy - (72\,xy^2 - 24\,xy) + (36\,x^2y^2 - 144\,xy^2 - 108\,xy) = 36\,x^2y^2 - 222\,xy^2 + 12\,xy \\ [8] \quad -91\,xy^2 + 28\,x^2y^2 - 28\,xy - (-98\,x^2y^2 + 84\,xy^2) = 126\,x^2y^2 - 175\,xy^2 - 28\,xy \\ [9] \quad -24\,x^2y^2 - 8\,x^2y - 256\,xy^2 + -128\,x^2y + 256\,xy^2 - 16\,xy - (-256\,x^2y^2 + 256\,x^2y - 8\,xy^2) = 232\,x^2y^2 - 392\,x^2y + 8\,xy^2 - 16\,xy \\ [10] \quad -81\,x^2y - 324\,xy - (297\,x^2y + 162\,xy) + (162\,x^2y^2 - 306\,xy) = 162\,x^2y^2 - 378\,x^2y - 792\,xy \\ \end{cases}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (4 \, b x^2 y z) \cdot (2 \, b^2 x^2 y^2 z) = 8 \, b^3 x^4 y^3 z^2 \\ &[3] \quad (-16 \, b^2 x^2 y^3 z^3) \cdot (16 \, b^3 x^3 y z) = -256 \, b^5 x^5 y^4 z^4 \\ &[4] \quad (-81 \, b^2 x^2 y^3 z) \cdot (-9 \, b x y z) = 729 \, b^3 x^3 y^4 z^2 \\ &[5] \quad (32 \, b^3 x^2 y^3 z) \cdot (256 \, b^2 x y^3 z^3) = 8192 \, b^5 x^3 y^6 z^4 \\ &[6] \quad (-100 \, b^2 x y^3 z) \cdot (-5 \, b^2 x y z^3) = 500 \, b^4 x^2 y^4 z^4 \\ &[7] \quad (-18 \, b^2 x^2 y^3 z^3) \cdot (-648 \, b^2 x y^2 z^2) = 11664 \, b^4 x^3 y^5 z^5 \\ &[8] \quad (98 \, b^3 x y^2 z^3) \cdot (49 \, b^2 x y z) = 4802 \, b^5 x^2 y^3 z^4 \\ &[9] \quad (-1536 \, b^3 x y^3 z^3) \cdot (128 \, b x^3 y^2 z^2) = -196608 \, b^4 x^4 y^5 z^5 \\ &[10] \quad (243 \, b^2 x^3 y^2 z^3) \cdot (-2916 \, b^3 x^2 y^3 z^2) = -708588 \, b^5 x^5 y^5 z^5 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(3x^2) \cdot (6x^2 + 3x) = 18x^4 + 9x^3$$

[2] $(4x) \cdot (x^2 - 2x) = 4x^3 - 8x^2$
[3] $(x) \cdot (-2x^2) = -2x^3$
[4] $(x) \cdot (6x^2 + 2x) = 6x^3 + 2x^2$
[5] $(x^2) \cdot (-x^2 - 3x) = -x^4 - 3x^3$
[6] $(-2x^2) \cdot (-5x^2 + 3x) = 10x^4 - 6x^3$
[7] $(-3x) \cdot (-2x^2 + 3x) = 6x^3 - 9x^2$
[8] $(-2x^2) \cdot (x) = -2x^3$
[9] $(-x^2) \cdot (x^2 + x) = -x^4 - x^3$
[10] $(2x) \cdot (3x^2 + 8x) = 6x^3 + 16x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (x^2-4\,x)\cdot(4\,x^2) = 4\,x^4-16\,x^3 \\ &[2] \quad (-4\,x^2-2\,x)\cdot(-x) = 4\,x^3+2\,x^2 \\ &[3] \quad (2\,x^2-2\,x)\cdot(-7\,x^2) = -14\,x^4+14\,x^3 \\ &[4] \quad (2\,x^2-4\,x)\cdot(-x) = -2\,x^3+4\,x^2 \\ &[5] \quad (-x^2+4\,x)\cdot(2\,x^2-2\,x) = -2\,x^4+10\,x^3-8\,x^2 \end{aligned}$$

[6]
$$(-x^2) \cdot (-4x^2) = 4x^4$$

[7]
$$(6x) \cdot (-5x) = -30x^2$$

[8]
$$(-2x^2+3x)\cdot(-4x^2-5x)=8x^4-2x^3-15x^2$$

[9]
$$(x^2 - 2x) \cdot (-2x) = -2x^3 + 4x^2$$

[10]
$$(4x^2 - 4x) \cdot (-5x^2 + 3x) = -20x^4 + 32x^3 - 12x^2$$

[11]
$$(3x^2 + 4x) \cdot (-x^2 - 4x) = -3x^4 - 16x^3 - 16x^2$$

[12]
$$(-6x) \cdot (-4x^2 - 6x) = 24x^3 + 36x^2$$

[13]
$$(7x^2) \cdot (4x^2 - 5x) = 28x^4 - 35x^3$$

[14]
$$(-2x^2 + x) \cdot (4x^2) = -8x^4 + 4x^3$$

[15]
$$(x) \cdot (-2x^2 + x) = -2x^3 + x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2 + 4x) \cdot (x^2 - 7x) = -2x^4 + 18x^3 - 28x^2$$

[2]
$$(x^2) \cdot (-2x^3 + 4x) = -2x^5 + 4x^3$$

[3]
$$(-3x^3 - 4x^2) \cdot (-6x^3 - 5x^2) = 18x^6 + 39x^5 + 20x^4$$

[4]
$$(4x^2 + 3x) \cdot (-x^2) = -4x^4 - 3x^3$$

[5]
$$(4x^3 - 4x^2) \cdot (x) = 4x^4 - 4x^3$$

[6]
$$(x^3 + x^2) \cdot (-6x^3 + 4x^2 - 4x) = -6x^6 - 2x^5 - 4x^3$$

[7]
$$(-x^3 - 2x^2 - 4x) \cdot (-2x^2 - 4x) = 2x^5 + 8x^4 + 16x^3 + 16x^2$$

[8]
$$(-2x^2 - x) \cdot (-x^2 + 3x) = 2x^4 - 5x^3 - 3x^2$$

[9]
$$(-6x^2) \cdot (-2x^3 + x^2) = 12x^5 - 6x^4$$

[10]
$$(-x^3 - 3x^2) \cdot (-4x^3 - x^2) = 4x^6 + 13x^5 + 3x^4$$

[11]
$$(4x^3 + x) \cdot (4x^3 + 4x^2 + 3x) = 16x^6 + 16x^5 + 16x^4 + 4x^3 + 3x^2$$

[12]
$$(-5x^2) \cdot (x^3 - 4x^2 - 3x) = -5x^5 + 20x^4 + 15x^3$$

[13]
$$(-3x^2 - 5x) \cdot (4x^2) = -12x^4 - 20x^3$$

[14]
$$(-3x^2 + x) \cdot (-6x) = 18x^3 - 6x^2$$

[15]
$$(2x^2) \cdot (2x^2 - 2x) = 4x^4 - 4x^3$$

[16]
$$(2x^3 + 4x^2 + 4x) \cdot (-2x^2 - 2x) = -4x^5 - 12x^4 - 16x^3 - 8x^2$$

[17]
$$(-2x^2 - 2x) \cdot (-x^3 - 2x^2) = 2x^5 + 6x^4 + 4x^3$$

[18]
$$(-4x^3 + x) \cdot (-3x^2 - x) = 12x^5 + 4x^4 - 3x^3 - x^2$$

[19]
$$(-3x) \cdot (3x^3 - 8x) = -9x^4 + 24x^2$$

[20]
$$(x^3) \cdot (-3x^3 + x^2 - 2x) = -3x^6 + x^5 - 2x^4$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(0) \cdot (x^2y - 2xy) = 0$$

[2]
$$(4x^2y^2 - 3x^2y) \cdot (x^2y - 4xy^2) = 4x^4y^3 - 16x^3y^4 - 3x^4y^2 + 12x^3y^3$$

[3]
$$(x^2y^2 - 2xy) \cdot (2x^2y^2 + 2x^2y + 3xy) = 2x^4y^4 + 2x^4y^3 - x^3y^3 - 4x^3y^2 - 6x^2y^2$$

[4]
$$(4xy^2 + 4xy) \cdot (2x^2y^2 + 4x^2y) = 8x^3y^4 + 24x^3y^3 + 16x^3y^2$$

[5]
$$(x^2y^2+2x^2y)\cdot(-2x^2y+4xy^2+xy) = -2x^4y^3+4x^3y^4-4x^4y^2+9x^3y^3+2x^3y^2$$

[6]
$$(-x^2y^2 + 3xy) \cdot (5x^2y^2 + xy) = -5x^4y^4 + 14x^3y^3 + 3x^2y^2$$

[7]
$$(-4x^2y^2 + 2xy^2) \cdot (x^2y^2 + 4xy^2 - 3xy) = -4x^4y^4 - 14x^3y^4 + 12x^3y^3 + 8x^2y^4 - 6x^2y^3$$