Evaluación 1ºD - Funciones 1.

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$3x^4 + 3x^2 + x + -4x^2 + -2x^5 = -2x^5 + 3x^4 - x^2 + x$$

[2] $2x^5 + 4x^3 + x + 4x^5 + -2x^6 = -2x^6 + 6x^5 + 4x^3 + x$
[3] $4x^5 + -2x^5 - 3x + -3x^6 + 2x^3 + 3x = -3x^6 + 2x^5 + 2x^3$
[4] $8x^2 + x + -3x + (-2x^4 - x^3 + 4x) = -2x^4 - x^3 + 8x^2 + 2x$
[5] $3x^3 + 4x^6 + 4x^3 - x + x^6 - 4x^5 = 5x^6 - 4x^5 + 7x^3 - x$
[6] $2x^5 + x + 4x^2 - 4x + -3x^5 - 3x^2 - 2x = -x^5 + x^2 - 5x$
[7] $4x^6 - 5x + -3x^3 + x^2 + x + -4x^5 + 3x^4 + 4x^2 = 4x^6 - 4x^5 + 3x^4 - 3x^3 + 5x^2 - 4x$
[8] $-4x^5 + x^2 + (-3x^3 - x^2 + 3x) + (-3x^6) = -3x^6 - 4x^5 - 3x^3 + 3x$
[9] $4x^5 + 2x^4 + 3x + -3x^4 + 6x^2 + -4x^5 + 7x^2 = -x^4 + 13x^2 + 3x$

[10]
$$x^6 + 3x^5 + x^3 + -2x^4 - 4x^3 + 4x + -x^6 + x^5 - x^4 = 4x^5 - 3x^4 - 3x^3 + 4x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad x^2y^2 + 3\,xy + -3\,x^2y^2 - 4\,x^2y - 2\,xy^2 - (3\,x^2y^2 + xy^2) = -5\,x^2y^2 - 4\,x^2y - \\ &3\,xy^2 + 3\,xy \end{aligned} \\ &[3] \quad 2\,x^2y + 18\,x^2y - 4\,xy - (8\,x^2y^2 + 8\,x^2y - 8\,xy^2) = -8\,x^2y^2 + 12\,x^2y + 8\,xy^2 - 4\,xy \\ &[4] \quad -3\,x^2y - (12\,x^2y^2) + (18\,x^2y^2) = 6\,x^2y^2 - 3\,x^2y \\ &[5] \quad 64\,x^2y + -8\,x^2y - (-32\,x^2y - 12\,xy^2) = 88\,x^2y + 12\,xy^2 \\ &[6] \quad -25\,x^2y^2 - 5\,x^2y - 5\,xy^2 + 5\,x^2y - (100\,x^2y - 40\,xy) = -25\,x^2y^2 - 100\,x^2y - 5\,xy^2 + 40\,xy \end{aligned}$$

$$[7] -90 xy - (-36 xy^2 - 78 xy) + (-6 x^2y^2 - 24 x^2y + 6 xy) = -6 x^2y^2 - 24 x^2y + 36 xy^2 - 6 xy$$

$$[8] -21 xy^2 - 70 xy + 21 x^2y^2 - 28 x^2y + 7 xy - (-14 x^2y^2 + 70 xy) = 35 x^2y^2 - 28 x^2y - 21 xy^2 - 133 xy$$

$$[9] -280 x^2y^2 + 16 xy + -24 x^2y + 256 xy^2 - (-16 x^2y + 32 xy^2) = 280 x^2y^2 - 8 x^2y + 224 xy^2 + 16 xy$$

$$[10] -36 x^2y^2 - 81 x^2y + 36 xy^2 - (-243 x^2y^2 + 45 x^2y) + (81 x^2y^2 - 324 x^2y + 27 xy^2) = 288 x^2y^2 - 450 x^2y + 63 xy^2$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

[1]
$$(0) \cdot (0) = 0$$

[2] $(4b^2xyz) \cdot (b^2xy^2z^3) = 4b^4x^2y^3z^4$
[3] $(24b^2xy^3z^2) \cdot (8bx^2yz) = 192b^3x^3y^4z^3$
[4] $(-18b^2x^2y^2z) \cdot (36b^2x^3y^2z^2) = -648b^4x^5y^4z^3$
[5] $(64bx^3y^2z) \cdot (256b^3x^2y^2z) = 16384b^4x^5y^4z^2$
[6] $(50bx^2y^3z) \cdot (-20b^3x^3y^3z) = -1000b^4x^5y^6z^2$
[7] $(-864b^3x^2y^3z^3) \cdot (-432b^2x^2yz^3) = 373248b^5x^4y^4z^6$
[8] $(-7b^2x^3y^3z^3) \cdot (-21b^2xyz^2) = 147b^4x^4y^4z^5$
[9] $(-512bx^2yz^3) \cdot (-32b^3x^3y^3z) = 16384b^4x^5y^4z^4$
[10] $(1458b^3x^2y^3z) \cdot (2187bx^2y^3z^3) = 3188646b^4x^4y^6z^4$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (2\,x)\cdot(-7\,x^2-3\,x) = -14\,x^3-6\,x^2 \\ &[2] \quad (2\,x)\cdot(-3\,x^2-2\,x) = -6\,x^3-4\,x^2 \\ &[3] \quad (-2\,x^2)\cdot(-x^2-6\,x) = 2\,x^4+12\,x^3 \\ &[4] \quad (2\,x)\cdot(5\,x^2) = 10\,x^3 \\ &[5] \quad (-3\,x)\cdot(-2\,x^2+x) = 6\,x^3-3\,x^2 \\ &[6] \quad (2\,x)\cdot(-3\,x^2+5\,x) = -6\,x^3+10\,x^2 \\ &[7] \quad (-3\,x)\cdot(x^2-3\,x) = -3\,x^3+9\,x^2 \\ &[8] \quad (2\,x)\cdot(4\,x^2+3\,x) = 8\,x^3+6\,x^2 \\ &[9] \quad (2\,x)\cdot(4\,x^2+2\,x) = 8\,x^3+4\,x^2 \\ &[10] \quad (-3\,x)\cdot(2\,x^2-4\,x) = -6\,x^3+12\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-x^2+x)\cdot(x^2-x) = -x^4+2\,x^3-x^2 \\ &[2] \quad (-x^2+4\,x)\cdot(4\,x) = -4\,x^3+16\,x^2 \\ &[3] \quad (-4\,x)\cdot(-x^2-2\,x) = 4\,x^3+8\,x^2 \\ &[4] \quad (-2\,x^2)\cdot(9\,x^2) = -18\,x^4 \\ &[5] \quad (3\,x^2)\cdot(-5\,x^2+4\,x) = -15\,x^4+12\,x^3 \\ &[6] \quad (4\,x)\cdot(5\,x^2-3\,x) = 20\,x^3-12\,x^2 \\ &[7] \quad (-2\,x^2-2\,x)\cdot(x^2-x) = -2\,x^4+2\,x^2 \\ &[8] \quad (2\,x^2+4\,x)\cdot(-7\,x^2-3\,x) = -14\,x^4-34\,x^3-12\,x^2 \end{aligned}$$

[9]
$$(x^2) \cdot (2x^2 + 6x) = 2x^4 + 6x^3$$

[10]
$$(4x^2 - 3x) \cdot (-2x^2 - 6x) = -8x^4 - 18x^3 + 18x^2$$

[11]
$$(4x^2) \cdot (3x^2 + 3x) = 12x^4 + 12x^3$$

[12]
$$(6x^2) \cdot (2x^2) = 12x^4$$

[13]
$$(-x^2 - 4x) \cdot (x^2 + 3x) = -x^4 - 7x^3 - 12x^2$$

[14]
$$(-2x^2 - x) \cdot (-2x^2 - 6x) = 4x^4 + 14x^3 + 6x^2$$

[15]
$$(-4x^2) \cdot (5x^2 - 3x) = -20x^4 + 12x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(4x^3 - 2x^2 + x) \cdot (-5x^2 + 2x) = -20x^5 + 18x^4 - 9x^3 + 2x^2$$

[2]
$$(-3x^3 + 4x) \cdot (-3x^2 + x) = 9x^5 - 3x^4 - 12x^3 + 4x^2$$

[3]
$$(-3x^3 + 4x^2) \cdot (2x^3 - 8x^2 - 4x) = -6x^6 + 32x^5 - 20x^4 - 16x^3$$

[4]
$$(x^3 - 2x) \cdot (-x) = -x^4 + 2x^2$$

[5]
$$(x^2 + 2x) \cdot (-2x^3 + 2x^2 + x) = -2x^5 - 2x^4 + 5x^3 + 2x^2$$

[6]
$$(-x^2 + x) \cdot (4x^3 + 4x^2 + 7x) = -4x^5 - 3x^3 + 7x^2$$

[7]
$$(x^2 - x) \cdot (-3x^3 + 6x^2) = -3x^5 + 9x^4 - 6x^3$$

[8]
$$(-x^3 + x^2) \cdot (-3x^3 - 3x^2 + 4x) = 3x^6 - 7x^4 + 4x^3$$

[9]
$$(-7x) \cdot (-3x^2 - 2x) = 21x^3 + 14x^2$$

[10]
$$(-4x) \cdot (x^3 - 3x^2) = -4x^4 + 12x^3$$

[11]
$$(4x^2 - x) \cdot (-x^2 - 6x) = -4x^4 - 23x^3 + 6x^2$$

[12]
$$(-3x^3 - x) \cdot (x^2 + x) = -3x^5 - 3x^4 - x^3 - x^2$$

[13]
$$(x^2 - 2x) \cdot (-2x^3 + 5x) = -2x^5 + 4x^4 + 5x^3 - 10x^2$$

[14]
$$(0) \cdot (-5x^3 + 4x^2) = 0$$

[15]
$$(5x^3) \cdot (-x^3 + 3x) = -5x^6 + 15x^4$$

[16]
$$(3x) \cdot (0) = 0$$

[17]
$$(-4x^2 - 4x) \cdot (-5x) = 20x^3 + 20x^2$$

[18]
$$(4x^3 + 3x^2) \cdot (-3x^2 + 4x) = -12x^5 + 7x^4 + 12x^3$$

[19]
$$(2x^3) \cdot (-3x^2) = -6x^5$$

[20]
$$(-2x^3 - 4x) \cdot (-6x^3 - 4x^2 + x) = 12x^6 + 8x^5 + 22x^4 + 16x^3 - 4x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2y^2 + 3xy) \cdot (-3x^2y^2 - 3xy^2 - xy) = 6x^4y^4 + 6x^3y^4 - 7x^3y^3 - 9x^2y^3 - 3x^2y^2$$

[2]
$$(2x^2y^2 - 3xy^2) \cdot (-2x^2y) = -4x^4y^3 + 6x^3y^3$$

[3]
$$(-3x^2y^2 - xy^2) \cdot (3x^2y - 3xy^2) = -9x^4y^3 + 9x^3y^4 - 3x^3y^3 + 3x^2y^4$$

[4]
$$(-3x^2y + xy) \cdot (3x^2y^2 - 3x^2y) = -9x^4y^3 + 9x^4y^2 + 3x^3y^3 - 3x^3y^2$$

[5]
$$(-2x^2y^2 - 3xy^2) \cdot (-2x^2y - 3xy^2) = 4x^4y^3 + 6x^3y^4 + 6x^3y^3 + 9x^2y^4$$

[6]
$$(3x^2y + xy^2) \cdot (-x^2y^2 + 7xy) = -3x^4y^3 - x^3y^4 + 21x^3y^2 + 7x^2y^3$$

[7]
$$(-x^2y^2 + 4x^2y) \cdot (-x^2y^2 + x^2y + xy^2) = x^4y^4 - 5x^4y^3 - x^3y^4 + 4x^4y^2 + 4x^3y^3$$