1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} &[1] \quad 4\,x^5 + x^4 + 2\,x + -4\,x^5 - 4\,x^4 - x^3 + (-3\,x^5 + 4\,x^2) = -3\,x^5 - 3\,x^4 - x^3 + 4\,x^2 + 2\,x \\ &[2] \quad x^3 - x^2 + 2\,x + -x^5 - 3\,x^3 + (-2\,x^5 + x) = -3\,x^5 - 2\,x^3 - x^2 + 3\,x \\ &[3] \quad -2\,x^3 + 2\,x^2 + (-2\,x^4 + x) + (-2\,x^6 - 5\,x^2) = -2\,x^6 - 2\,x^4 - 2\,x^3 - 3\,x^2 + x \\ &[4] \quad 2\,x^5 - x^2 - 3\,x + -5\,x^6 - 2\,x^4 + 3\,x^3 - 4\,x = -5\,x^6 + 2\,x^5 - 2\,x^4 + 3\,x^3 - x^2 - 7\,x \\ &[5] \quad 3\,x^3 - 2\,x^2 + 2\,x + -3\,x^6 + 2\,x^5 + 2\,x^3 + -4\,x^3 + 4\,x^2 - x = -3\,x^6 + 2\,x^5 + x^3 + 2\,x^2 + x \end{aligned}$$

[6]
$$3x^6 + x^3 + -4x^6 - 3x^5 - 4x + 3x^4 + 4x^3 + 4x^2 = -x^6 - 3x^5 + 3x^4 + 5x^3 + 4x^2 - 4x$$

[7]
$$2x^6 + 4x + 2x^6 + 3x^4 + -2x^6 + 3x^4 + 2x = 2x^6 + 6x^4 + 6x$$

[8]
$$x^5 - x^4 + 2x^2 + -2x^6 - 2x^5 - x^2 + -x^6 - 5x^3 = -3x^6 - x^5 - x^4 - 5x^3 + x^2$$

[9]
$$5x^4 + 3x + -x^5 + -x^5 - 3x^3 - 3x = -2x^5 + 5x^4 - 3x^3$$

[10]
$$4x^5 - x + -4x^2 + 5x + -4x^5 - 8x^2 = -12x^2 + 4x$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 3x^2y+2xy^2-3xy+-2x^2y^2-x^2y-4xy^2+-x^2y^2-2xy=-3x^2y^2+2x^2y-2xy^2-5xy \\ [3] \quad 4x^2y+4xy^2-8xy+-2x^2y+6xy^2+16xy+8x^2y-8xy^2-8xy=10x^2y+2xy^2 \\ [4] \quad 27x^2y^2-39x^2y+6x^2y^2-12xy^2+36xy+-6x^2y^2+36x^2y-18xy=27x^2y^2-3x^2y-12xy^2+18xy \\ [5] \quad 16x^2y^2-4x^2y+8xy+-16x^2y^2+16x^2y-16xy^2+-8x^2y+44xy=4x^2y-16xy^2+52xy \\ [6] \quad 15x^2y^2-50x^2y+-50x^2y^2-95x^2y+75x^2y^2-15x^2y+75xy^2=40x^2y^2-160x^2y+75xy^2 \\ [7] \quad 36x^2y^2+108xy+-144x^2y^2-108xy^2+144xy+-36x^2y^2+144x^2y-18xy^2=-144x^2y^2+144x^2y-126xy^2+252xy \\ [8] \quad 14x^2y^2+7x^2y+7xy^2+-196x^2y^2+7x^2y+196xy^2+49x^2y+105xy=-182x^2y^2+63x^2y+203xy^2+105xy \\ [9] \quad -32x^2y^2+128x^2y-128xy+(-64x^2y^2-128x^2y-32xy^2)+(-256x^2y^2-16xy)=-352x^2y^2-32xy^2-144xy \\ [10] \quad 27x^2y^2-324xy^2-324xy+27x^2y+81x^2y+243xy=27x^2y^2+108x^2y-128x^2y-1$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

 $324 xy^2 - 81 xy$

[1]
$$0 - (0) + (0) = 0$$

[2] $x^2y^2 - 4x^2y - xy + -5x^2y^2 + 2xy^2 - (-3x^2y^2 + xy^2) = -x^2y^2 - 4x^2y + xy^2 - xy$
[3] $8x^2y^2 + 28xy^2 + 4x^2y + 2xy - (-14x^2y + 16xy^2) = 8x^2y^2 + 18x^2y + 12xy^2 + 2xy$
[4] $-3xy - (-12xy^2 - 6xy) + (6xy^2 - 36xy) = 18xy^2 - 33xy$

$$\begin{aligned} & [5] \quad -64\,x^2y^2 - 60\,xy + -16\,x^2y^2 + 8\,x^2y + 4\,xy^2 - (16\,x^2y^2 - 16\,xy^2 + 48\,xy) = \\ & -96\,x^2y^2 + 8\,x^2y + 20\,xy^2 - 108\,xy \\ & [6] \quad -15\,x^2y^2 + 50\,x^2y - 50\,xy^2 + 50\,x^2y^2 + 75\,x^2y + 25\,xy - (30\,x^2y + 10\,xy) = \\ & 35\,x^2y^2 + 95\,x^2y - 50\,xy^2 + 15\,xy \\ & [7] \quad -108\,x^2y^2 - 18\,x^2y - 24\,xy - (24\,xy^2 - 72\,xy) + (12\,x^2y^2 - 24\,x^2y - 24\,xy) = \\ & -96\,x^2y^2 - 42\,x^2y - 24\,xy^2 + 24\,xy \\ & [8] \quad -147\,x^2y - 119\,xy + -49\,xy - (28\,x^2y^2 + 196\,x^2y - 14\,xy^2) = -28\,x^2y^2 - \\ & 343\,x^2y + 14\,xy^2 - 168\,xy \\ & [9] \quad -16\,x^2y^2 - 64\,x^2y + 24\,xy^2 + 256\,xy^2 + 168\,xy - (-24\,x^2y^2 - 16\,x^2y - 128\,xy) = \\ & 8\,x^2y^2 - 48\,x^2y + 280\,xy^2 + 296\,xy \\ & [10] \quad -405\,x^2y - 36\,xy^2 - (9\,x^2y^2 + 36\,xy) + (360\,x^2y^2 + 243\,xy^2) = 351\,x^2y^2 - \\ & 405\,x^2y + 207\,xy^2 - 36\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (4 \, b x^2 y z^2) \cdot (2 \, b^3 x^2 y^3 z^2) = 8 \, b^4 x^4 y^4 z^4 \\ &[3] \quad (-16 \, b^2 x^3 y^2 z) \cdot (-8 \, b^3 x y^3 z) = 128 \, b^5 x^4 y^5 z^2 \\ &[4] \quad (-18 \, b^2 x^3 y^2 z^2) \cdot (9 \, b^2 x^3 y^3 z^3) = -162 \, b^4 x^6 y^5 z^5 \\ &[5] \quad (-128 \, b x^3 y^2 z^2) \cdot (-12 \, b^3 x y^3 z^2) = 1536 \, b^4 x^4 y^5 z^4 \\ &[6] \quad (-125 \, b x^3 y z^3) \cdot (25 \, b^2 x y z^3) = -3125 \, b^3 x^4 y^2 z^6 \\ &[7] \quad (864 \, b x^3 y^3 z^3) \cdot (12 \, b^2 x y^2 z^2) = 10368 \, b^3 x^4 y^5 z^5 \\ &[8] \quad (-1372 \, b^2 x y^2 z^3) \cdot (-343 \, b x y^3 z^2) = 470596 \, b^3 x^2 y^5 z^5 \\ &[9] \quad (-1536 \, b^3 x y^3 z^2) \cdot (-512 \, b x^2 y^3 z^3) = 786432 \, b^4 x^3 y^6 z^5 \\ &[10] \quad (324 \, b^3 x^2 y^2 z^2) \cdot (-324 \, b^3 x^2 y^3 z^2) = -104976 \, b^6 x^4 y^5 z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(4x) \cdot (-5x^2 + 3x) = -20x^3 + 12x^2$$

[2] $(2x) \cdot (2x) = 4x^2$
[3] $(x^2) \cdot (-3x^2 - 4x) = -3x^4 - 4x^3$
[4] $(-2x^2) \cdot (-3x) = 6x^3$
[5] $(-4x) \cdot (x^2) = -4x^3$
[6] $(-4x) \cdot (-3x^2 + 3x) = 12x^3 - 12x^2$
[7] $(-2x^2) \cdot (5x^2 - 4x) = -10x^4 + 8x^3$
[8] $(-x) \cdot (-4x^2 + x) = 4x^3 - x^2$
[9] $(-4x) \cdot (-6x^2 - x) = 24x^3 + 4x^2$
[10] $(-2x^2) \cdot (x^2 - 3x) = -2x^4 + 6x^3$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(4x^2) \cdot (-x) = -4x^3$$

[2] $(8x) \cdot (x^2 + x) = 8x^3 + 8x^2$
[3] $(-4x^2) \cdot (2x^2 - 2x) = -8x^4 + 8x^3$
[4] $(-4x^2) \cdot (6x) = -24x^3$

[5]
$$(-4x^2 - 3x) \cdot (2x^2) = -8x^4 - 6x^3$$

[6] $(-x^2 - 3x) \cdot (-5x^2 - x) = 5x^4 + 16x^3 + 3x^2$
[7] $(-5x) \cdot (2x) = -10x^2$

[8]
$$(0) \cdot (2x^2 - 2x) = 0$$

[9]
$$(2x^2 + 2x) \cdot (-3x^2) = -6x^4 - 6x^3$$

[10]
$$(x^2) \cdot (2x^2) = 2x^4$$

[11]
$$(0) \cdot (-5x^2) = 0$$

[12]
$$(-4x^2 - 3x) \cdot (2x^2 + x) = -8x^4 - 10x^3 - 3x^2$$

[13]
$$(-5x) \cdot (4x^2 + 3x) = -20x^3 - 15x^2$$

[14]
$$(-2x^2 - 2x) \cdot (3x^2 - 6x) = -6x^4 + 6x^3 + 12x^2$$

[15]
$$(2x^2 + 3x) \cdot (-2x) = -4x^3 - 6x^2$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (-4\,x^3-x^2-2\,x)\cdot(-3\,x^3-5\,x) = 12\,x^6+3\,x^5+26\,x^4+5\,x^3+10\,x^2 \\ & [2] \quad (-4\,x^2+2\,x)\cdot(-2\,x^3-x^2+6\,x) = 8\,x^5-26\,x^3+12\,x^2 \\ & [3] \quad (-5\,x^2)\cdot(4\,x^3+4\,x^2+2\,x) = -20\,x^5-20\,x^4-10\,x^3 \\ & [4] \quad (-3\,x^3-6\,x)\cdot(4\,x^3+5\,x^2) = -12\,x^6-15\,x^5-24\,x^4-30\,x^3 \\ & [5] \quad (x^3+3\,x)\cdot(-x^3+4\,x^2+2\,x) = -x^6+4\,x^5-x^4+12\,x^3+6\,x^2 \\ & [6] \quad (-3\,x^3-2\,x)\cdot(3\,x^3+4\,x^2-x) = -9\,x^6-12\,x^5-3\,x^4-8\,x^3+2\,x^2 \\ & [7] \quad (2\,x^2)\cdot(-3\,x^3-2\,x) = -6\,x^5-4\,x^3 \\ & [8] \quad (-2\,x^3-4\,x)\cdot(4\,x^3-2\,x^2+4\,x) = -8\,x^6+4\,x^5-24\,x^4+8\,x^3-16\,x^2 \\ & [9] \quad (-3\,x^2+2\,x)\cdot(6\,x^2+2\,x) = -18\,x^4+6\,x^3+4\,x^2 \\ & [10] \quad (4\,x^2+2\,x)\cdot(x^3+x^2-x) = 4\,x^5+6\,x^4-2\,x^3-2\,x^2 \\ & [11] \quad (0)\cdot(-3\,x^3-x) = 0 \\ & [12] \quad (2\,x^3-3\,x^2)\cdot(-x^2-3\,x) = -2\,x^5-3\,x^4+9\,x^3 \\ & [13] \quad (2\,x^2)\cdot(5\,x) = 10\,x^3 \\ & [14] \quad (5\,x^3)\cdot(-7\,x^2+3\,x) = -35\,x^5+15\,x^4 \\ & [15] \quad (2\,x^3-2\,x)\cdot(-4\,x^3-7\,x^2+3\,x) = -8\,x^6-14\,x^5+14\,x^4+14\,x^3-6\,x^2 \\ & [16] \quad (-x^2+3\,x)\cdot(-3\,x^2+3\,x) = 3\,x^4-12\,x^3+9\,x^2 \\ & [17] \quad (2\,x^3-4\,x^2)\cdot(3\,x^3-7\,x^2-2\,x) = 6\,x^6-26\,x^5+24\,x^4+8\,x^3 \end{aligned}$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[20] $(-4x^3 - x^2) \cdot (-x) = 4x^4 + x^3$

[18] $(0) \cdot (-2x^2 - 2x) = 0$

$$\begin{aligned} & [1] \quad (-4\,x^2y - xy^2) \cdot (-x^2y + 2\,xy^2 - 2\,xy) = 4\,x^4y^2 - 7\,x^3y^3 - 2\,x^2y^4 + 8\,x^3y^2 + 2\,x^2y^3 \\ & [2] \quad (-3\,x^2y^2 + xy^2) \cdot (2\,xy^2 + 2\,xy) = -6\,x^3y^4 - 6\,x^3y^3 + 2\,x^2y^4 + 2\,x^2y^3 \\ & [3] \quad (-4\,x^2y^2 - 2\,xy) \cdot (-4\,x^2y - xy^2) = 16\,x^4y^3 + 4\,x^3y^4 + 8\,x^3y^2 + 2\,x^2y^3 \\ & [4] \quad (-x^2y - 4\,xy) \cdot (-x^2y^2 - 3\,x^2y - 4\,xy^2) = x^4y^3 + 3\,x^4y^2 + 8\,x^3y^3 + 12\,x^3y^2 + 16\,x^2y^3 \\ & [5] \quad (2\,x^2y^2) \cdot (4\,x^2y^2 - xy) = 8\,x^4y^4 - 2\,x^3y^3 \end{aligned}$$

[19] $(2x^3 - 2x^2 + 3x) \cdot (2x^3 + 4x^2) = 4x^6 + 4x^5 - 2x^4 + 12x^3$

[6]
$$(2x^2y + 2xy) \cdot (x^2y^2) = 2x^4y^3 + 2x^3y^3$$

[7]
$$(-2xy^2) \cdot (x^2y^2 - xy) = -2x^3y^4 + 2x^2y^3$$