## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad x^5 + 5 \, x^2 + 2 \, x^6 - x^4 + x + -x^5 - 4 \, x^3 = 2 \, x^6 - x^4 - 4 \, x^3 + 5 \, x^2 + x \\ [2] \quad x^3 + -x^5 + 2 \, x^4 - 4 \, x^2 + (-4 \, x^5 + 4 \, x^4 - x) = -5 \, x^5 + 6 \, x^4 + x^3 - 4 \, x^2 - x \\ [3] \quad 5 \, x^6 + 3 \, x^6 + 7 \, x^3 + -3 \, x^4 - x^3 + 4 \, x^2 = 8 \, x^6 - 3 \, x^4 + 6 \, x^3 + 4 \, x^2 \\ [4] \quad -x^5 + 3 \, x^2 + (-4 \, x^4 + x^2 - 3 \, x) + (-4 \, x^3 + 2 \, x^2 + 4 \, x) = -x^5 - 4 \, x^4 - 4 \, x^3 + 6 \, x^2 + x \\ [5] \quad 4 \, x^4 - 2 \, x + -3 \, x^6 - 3 \, x^4 + 2 \, x^2 + -2 \, x^6 - 2 \, x^4 = -5 \, x^6 - x^4 + 2 \, x^2 - 2 \, x \\ [6] \quad 3 \, x^5 - 2 \, x + x^6 + 2 \, x^4 + 3 \, x + -2 \, x^6 - 3 \, x^3 + 3 \, x^2 = -x^6 + 3 \, x^5 + 2 \, x^4 - 3 \, x^3 + 3 \, x^2 + x \\ [7] \quad -3 \, x^4 - 4 \, x^3 + 4 \, x^2 + (-4 \, x^6 - x^4) + (-2 \, x^4 - x^3) = -4 \, x^6 - 6 \, x^4 - 5 \, x^3 + 4 \, x^2 \\ [8] \quad -x^6 - 2 \, x^5 - 4 \, x^3 + (-3 \, x^5 + 4 \, x^4 - 3 \, x^2) + (-6 \, x^4 + 3 \, x) = -x^6 - 5 \, x^5 - 2 \, x^4 - 4 \, x^3 - 3 \, x^2 + 3 \, x \\ [9] \quad 4 \, x^6 - x^5 - 4 \, x^2 + -3 \, x^2 + (-x^4 - 4 \, x) = 4 \, x^6 - x^5 - x^4 - 7 \, x^2 - 4 \, x \\ [10] \quad -6 \, x^4 + 3 \, x^2 + (-2 \, x^5 + 2 \, x^3 - 2 \, x) + (-2 \, x^6 - 2 \, x^4 - 3 \, x^3) = -2 \, x^6 - 2 \, x^5 -$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} &[1] \quad 0 + 0 + 0 = 0 \\ &[2] \quad -2 \, x^2 y^2 + x^2 y - 4 \, xy + (-2 \, x^2 y^2 - 4 \, x^2 y + 2 \, xy^2) + (-2 \, x^2 y - 2 \, xy) = \\ &-4 \, x^2 y^2 - 5 \, x^2 y + 2 \, xy^2 - 6 \, xy \\ &[3] \quad 24 \, x^2 y^2 - 4 \, xy^2 + 12 \, x^2 y + 16 \, xy^2 + -4 \, xy^2 + 4 \, xy = 24 \, x^2 y^2 + 12 \, x^2 y + 8 \, xy^2 + 4 \, xy \\ &[4] \quad 3 \, x^2 y^2 + 9 \, xy^2 + -18 \, x^2 y^2 + 6 \, x^2 y + 3 \, xy + -9 \, x^2 y^2 - 36 \, xy^2 = -24 \, x^2 y^2 + 6 \, x^2 y - 27 \, xy^2 + 3 \, xy \\ &[5] \quad 16 \, x^2 y + 4 \, xy^2 - 64 \, xy + 4 \, xy^2 - 8 \, xy + -8 \, x^2 y^2 + 96 \, xy^2 = -8 \, x^2 y^2 + 16 \, x^2 y + 104 \, xy^2 - 72 \, xy \\ &[6] \quad 10 \, x^2 y^2 + 25 \, x^2 y + -60 \, x^2 y - 100 \, xy^2 + -80 \, x^2 y^2 + 5 \, xy^2 = -70 \, x^2 y^2 - 35 \, x^2 y - 95 \, xy^2 \\ &[7] \quad 24 \, x^2 y^2 - 30 \, xy + -6 \, x^2 y + 6 \, xy^2 + (-120 \, x^2 y + 144 \, xy^2) = 24 \, x^2 y^2 - 126 \, x^2 y + 150 \, xy^2 - 30 \, xy \\ &[8] \quad 49 \, x^2 y + 7 \, xy^2 + 196 \, xy + -147 \, x^2 y^2 + 98 \, x^2 y - 147 \, xy^2 + -203 \, xy = -147 \, x^2 y^2 + 147 \, x^2 y - 140 \, xy^2 - 7 \, xy \\ &[9] \quad -512 \, x^2 y^2 + 8 \, xy^2 + (-24 \, x^2 y - 192 \, xy^2 - 32 \, xy) + (-192 \, x^2 y^2 + 16 \, x^2 y - 24 \, xy) = -704 \, x^2 y^2 - 8 \, x^2 y - 184 \, xy^2 - 56 \, xy \\ &[10] \quad 9 \, x^2 y^2 + 324 \, xy^2 - 18 \, xy + -648 \, x^2 y^2 - 36 \, x^2 y + 45 \, x^2 y^2 - 324 \, x^2 y = -594 \, x^2 y^2 - 360 \, x^2 y + 324 \, xy^2 - 18 \, xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad 7 \, x^2 y^2 + x^2 y + 2 \, x^2 y + 4 \, x y^2 - 4 \, x y - (-2 \, x^2 y^2 - x^2 y + x y) = 9 \, x^2 y^2 + 4 \, x^2 y + 4 \, x y^2 - 5 \, x y \\ &[3] \quad 8 \, x^2 y^2 - 16 \, x^2 y - 16 \, x y + -2 \, x^2 y^2 + 8 \, x y - (-6 \, x^2 y^2 - 6 \, x y^2 - 4 \, x y) = 12 \, x^2 y^2 - 16 \, x^2 y + 6 \, x y^2 - 4 \, x y \\ &[4] \quad -9 \, x^2 y^2 + 18 \, x^2 y + 18 \, x y - (-6 \, x^2 y^2 - 6 \, x y) + (36 \, x y^2 + 12 \, x y) = -3 \, x^2 y^2 + 18 \, x^2 y + 36 \, x y^2 + 36 \, x y \end{aligned}$$

$$\begin{aligned} & [5] \quad -8\,x^2y - 64\,xy^2 - 12\,xy + 16\,x^2y^2 + 32\,xy^2 - (8\,x^2y + 28\,xy) = 16\,x^2y^2 - \\ & 16\,x^2y - 32\,xy^2 - 40\,xy \\ & [6] \quad -10\,x^2y^2 - 85\,x^2y + 30\,x^2y + 25\,xy^2 - (100\,x^2y^2 + 75\,x^2y - 15\,xy^2) = -110\,x^2y^2 - \\ & 130\,x^2y + 40\,xy^2 \\ & [7] \quad -36\,x^2y^2 - (-6\,x^2y^2 + 24\,x^2y + 72\,xy) + (-48\,x^2y^2 - 72\,xy) = -78\,x^2y^2 - \\ & 24\,x^2y - 144\,xy \\ & [8] \quad -140\,x^2y - 21\,xy + 147\,x^2y^2 - (14\,x^2y^2 - 98\,x^2y - 14\,xy^2) = 133\,x^2y^2 - 42\,x^2y + \\ & 14\,xy^2 - 21\,xy \\ & [9] \quad 96\,x^2y^2 - 192\,xy + 16\,xy^2 - (8\,x^2y^2 + 64\,x^2y - 256\,xy^2) = 88\,x^2y^2 - 64\,x^2y + \\ & 272\,xy^2 - 192\,xy \\ & [10] \quad 27\,x^2y^2 - 162\,x^2y - 36\,xy - (-9\,x^2y^2 - 72\,xy^2) + (162\,x^2y + 81\,xy^2 + 81\,xy) = \\ & 36\,x^2y^2 + 153\,xy^2 + 45\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-b^2x^2y^2z^3) \cdot (-2\,b^3x^3y^2z^2) = 2\,b^5x^5y^4z^5 \\ &[3] \quad (-6\,b^2xy^2z) \cdot (-12\,bx^2y^3z) = 72\,b^3x^3y^5z^2 \\ &[4] \quad (81\,b^3x^2y^3z^2) \cdot (12\,b^2xy^3z^2) = 972\,b^5x^3y^6z^4 \\ &[5] \quad (128\,b^2xy^3z^2) \cdot (128\,bx^3y^3z) = 16384\,b^3x^4y^6z^3 \\ &[6] \quad (375\,b^3xy^3z^3) \cdot (-25\,b^2x^2yz^3) = -9375\,b^5x^3y^4z^6 \\ &[7] \quad (-108\,b^3x^2y^3z) \cdot (648\,bx^3y^2z) = -69984\,b^4x^5y^5z^2 \\ &[8] \quad (-196\,bx^2yz) \cdot (98\,b^2xyz) = -19208\,b^3x^3y^2z^2 \\ &[9] \quad (-64\,bx^3y^3z^2) \cdot (-1536\,bx^2y^2z^2) = 98304\,b^2x^5y^5z^4 \\ &[10] \quad (27\,b^2x^2y^2z^2) \cdot (27\,b^3x^3y^2z) = 729\,b^5x^5y^4z^3 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x^2)\cdot(5\,x^2+x) = -10\,x^4-2\,x^3 \\ &[2] \quad (-x)\cdot(3\,x) = -3\,x^2 \\ &[3] \quad (-2\,x^2)\cdot(-5\,x^2+3\,x) = 10\,x^4-6\,x^3 \\ &[4] \quad (-x)\cdot(-2\,x^2-7\,x) = 2\,x^3+7\,x^2 \\ &[5] \quad (x)\cdot(-4\,x^2+7\,x) = -4\,x^3+7\,x^2 \\ &[6] \quad (3\,x^2)\cdot(x^2+4\,x) = 3\,x^4+12\,x^3 \\ &[7] \quad (4\,x^2)\cdot(-4\,x^2+9\,x) = -16\,x^4+36\,x^3 \\ &[8] \quad (3\,x^2)\cdot(4\,x^2+4\,x) = 12\,x^4+12\,x^3 \\ &[9] \quad (-4\,x^2)\cdot(-4\,x) = 16\,x^3 \\ &[10] \quad (-2\,x^2)\cdot(2\,x^2+x) = -4\,x^4-2\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(x^2 + 4x) \cdot (-2x^2) = -2x^4 - 8x^3$$
  
[2]  $(4x^2 + x) \cdot (0) = 0$   
[3]  $(-x) \cdot (-4x^2) = 4x^3$   
[4]  $(-3x^2 - 4x) \cdot (3x^2 - 2x) = -9x^4 - 6x^3 + 8x^2$ 

[5] 
$$(x^2 + 2x) \cdot (9x^2) = 9x^4 + 18x^3$$

[6] 
$$(3x) \cdot (-4x^2) = -12x^3$$

[7] 
$$(-x) \cdot (4x^2 - x) = -4x^3 + x^2$$

[8] 
$$(-4x^2) \cdot (4x) = -16x^3$$

[9] 
$$(-6x^2) \cdot (2x^2 - 3x) = -12x^4 + 18x^3$$

[10] 
$$(0) \cdot (-8x) = 0$$

[11] 
$$(4x^2 - 3x) \cdot (2x^2 - 5x) = 8x^4 - 26x^3 + 15x^2$$

[12] 
$$(-4x^2 + 2x) \cdot (-5x^2 + 3x) = 20x^4 - 22x^3 + 6x^2$$

[13] 
$$(5x^2) \cdot (-5x^2) = -25x^4$$

[14] 
$$(-4x^2 - x) \cdot (3x^2 - x) = -12x^4 + x^3 + x^2$$

[15] 
$$(2x^2 + 3x) \cdot (2x^2) = 4x^4 + 6x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(0) \cdot (-2x^3 - 3x^2) = 0$$

[2] 
$$(-5x) \cdot (-x^3 + 2x^2 - 5x) = 5x^4 - 10x^3 + 25x^2$$

[3] 
$$(-4x^2 - 2x) \cdot (3x^2 + 2x) = -12x^4 - 14x^3 - 4x^2$$

[4] 
$$(-5x^3 + 3x^2) \cdot (-2x^3 - 3x^2 - 3x) = 10x^6 + 9x^5 + 6x^4 - 9x^3$$

[5] 
$$(-2x^3 - 3x^2) \cdot (-4x^3 + 3x^2 - 4x) = 8x^6 + 6x^5 - x^4 + 12x^3$$

[6] 
$$(2x^3 + 4x) \cdot (-4x^3 - 3x) = -8x^6 - 22x^4 - 12x^2$$

[7] 
$$(-2x^3 - 4x^2) \cdot (3x^2 - 4x) = -6x^5 - 4x^4 + 16x^3$$

[8] 
$$(2x^2 - x) \cdot (x^2 - 5x) = 2x^4 - 11x^3 + 5x^2$$

[9] 
$$(-x^3 - 2x) \cdot (-4x^3 + 4x^2 - 3x) = 4x^6 - 4x^5 + 11x^4 - 8x^3 + 6x^2$$

[10] 
$$(x^3 - 2x^2 - x) \cdot (-2x^3 + 3x^2 + x) = -2x^6 + 7x^5 - 3x^4 - 5x^3 - x^2$$

[11] 
$$(-3x^2 + 3x) \cdot (-x^3 - x^2 - 2x) = 3x^5 + 3x^3 - 6x^2$$

[12] 
$$(-2x^2) \cdot (4x) = -8x^3$$

[13] 
$$(2x^3 + 5x) \cdot (x^3) = 2x^6 + 5x^4$$

[14] 
$$(0) \cdot (-4x^2 + x) = 0$$

[15] 
$$(-4x^2 + 4x) \cdot (2x^3 + 2x^2 + 4x) = -8x^5 - 8x^3 + 16x^2$$

[16] 
$$(3x^3 + 2x^2) \cdot (-5x^2 - 2x) = -15x^5 - 16x^4 - 4x^3$$

[17] 
$$(-4x^3 - 2x^2) \cdot (3x^3 - x^2 + 2x) = -12x^6 - 2x^5 - 6x^4 - 4x^3$$

[18] 
$$(2x^3 + x) \cdot (-x) = -2x^4 - x^2$$

[19] 
$$(-2x^3 - x^2 + 3x) \cdot (-2x) = 4x^4 + 2x^3 - 6x^2$$

[20] 
$$(2x^2 + 4x) \cdot (8x^3 + x^2 - 3x) = 16x^5 + 34x^4 - 2x^3 - 12x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-2x^2y - 4xy^2) \cdot (2x^2y + 2xy^2) = -4x^4y^2 - 12x^3y^3 - 8x^2y^4$$

[2] 
$$(2x^2y^2 - 2xy^2) \cdot (7x^2y - xy^2) = 14x^4y^3 - 2x^3y^4 - 14x^3y^3 + 2x^2y^4$$

[3] 
$$(4xy^2 - 4xy) \cdot (2x^2y^2 - 3x^2y - 4xy) = 8x^3y^4 - 20x^3y^3 + 12x^3y^2 - 16x^2y^3 + 16x^2y^2$$

[4] 
$$(-5xy) \cdot (-3x^2y^2 - x^2y) = 15x^3y^3 + 5x^3y^2$$

$$\begin{aligned} &[5] \quad (3\,x^2y^2 + 4\,x^2y) \cdot (-x^2y^2 + 3\,x^2y - 3\,xy^2) = -3\,x^4y^4 + 5\,x^4y^3 - 9\,x^3y^4 + 12\,x^4y^2 - \\ &12\,x^3y^3 \\ &[6] \quad (-4\,x^2y^2 + 3\,xy) \cdot (-3\,x^2y^2) = 12\,x^4y^4 - 9\,x^3y^3 \\ &[7] \quad (2\,x^2y^2 + 2\,xy^2) \cdot (-5\,x^2y) = -10\,x^4y^3 - 10\,x^3y^3 \end{aligned}$$