1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1]
$$x^3 + 3x + -x^4 + x^3 + 4x + (-2x^4 + 2x) = -3x^4 + 2x^3 + 9x$$

[2] $4x^6 + x^3 + 3x^2 + -3x^5 + x^3 + 3x + x^6 + 2x^3 + 4x^2 = 5x^6 - 3x^5 + 4x^3 + 7x^2 + 3x$
[3] $4x^6 + 4x^4 - 2x + -3x^6 + 2x^3 + 2x + (-4x^6 + x^4 + x^3) = -3x^6 + 5x^4 + 3x^3$
[4] $4x^6 + 2x^3 - 4x^2 + -x^5 - 3x^4 - 3x^2 + x^5 + 2x^2 - 2x = 4x^6 - 3x^4 + 2x^3 - 5x^2 - 2x$
[5] $2x^6 - x^3 - 3x + -3x^6 + x^4 + (-4x^6 + 3x^4 + x^3) = -5x^6 + 4x^4 - 3x$
[6] $x^6 - 3x^3 - x + x^6 - 3x + 4x^6 - 2x^5 + x = 6x^6 - 2x^5 - 3x^3 - 3x$
[7] $x^5 + 5x^3 + -2x^5 - 2x + (-6x) = -x^5 + 5x^3 - 8x$
[8] $x^2 + 7x + 2x^5 + 2x^2 + 3x + 2x^5 + 2x^4 - 2x = 4x^5 + 2x^4 + 3x^2 + 8x$
[9] $2x^5 - 2x + -3x^4 + 2x^3 + 4x + 2x^4 - 3x^3 + 3x^2 = 2x^5 - x^4 - x^3 + 3x^2 + 2x$
[10] $4x^3 - x^2 + -3x^5 - x^4 + 3x^2 + (-x^4 + 2x^3 - x) = -3x^5 - 2x^4 + 6x^3 + 2x^2 - x$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 2xy^2+-2x^2y+-x^2y^2-3xy^2=-x^2y^2-2x^2y-xy^2 \\ [3] \quad 6x^2y^2+6x^2y+-4x^2y+-8x^2y^2-8x^2y+8xy=-2x^2y^2-6x^2y+8xy \\ [4] \quad 18xy+-15x^2y+6xy^2+6x^2y+6xy=-9x^2y+6xy^2+24xy \\ [5] \quad 4x^2y+8xy^2+-16x^2y^2-12xy+64x^2y+64xy^2=-16x^2y^2+68x^2y+72xy^2-12xy \\ [6] \quad 50x^2y^2+70xy^2+-25x^2y-15xy^2-15xy+20x^2y^2-100xy^2-75xy=70x^2y^2-25x^2y-45xy^2-90xy \\ [7] \quad -72x^2y^2-18x^2y+72xy+(-66x^2y+36xy)+(-24xy^2+288xy)=-72x^2y^2-84x^2y-24xy^2+396xy \\ [8] \quad 49xy^2+21xy+-21x^2y^2+7xy^2+(-35x^2y+98xy)=-21x^2y^2-35x^2y+56xy^2+119xy \\ [9] \quad -32x^2y-128xy^2+(-24x^2y^2-104xy)+(-128x^2y+104xy^2)=-24x^2y^2-160x^2y-24xy^2-104xy \\ [10] \quad 324x^2y-288xy^2+-36x^2y^2+36x^2y+162xy+(-405x^2y^2-36xy^2)=-441x^2y^2+360x^2y-324xy^2+162xy \\ [10] \quad 324x^2y-288xy^2+360x^2y-324xy^2+162xy \\ \end{array}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -3\,x^2y^2 - 3\,xy^2 + 3\,xy + xy^2 + 6\,xy - (5\,x^2y - 2\,xy) = -3\,x^2y^2 - 5\,x^2y - 2\,xy^2 + 11\,xy \\ &[3] \quad 2\,x^2y^2 + 6\,xy^2 + 16\,xy + -2\,x^2y^2 + 6\,x^2y + 6\,xy^2 - (-12\,x^2y^2 + 14\,x^2y) = \\ &12\,x^2y^2 - 8\,x^2y + 12\,xy^2 + 16\,xy \\ &[4] \quad 72\,x^2y - (-18\,x^2y - 48\,xy^2) + (3\,xy^2 + 6\,xy) = 90\,x^2y + 51\,xy^2 + 6\,xy \\ &[5] \quad -16\,x^2y + 16\,xy + -16\,x^2y^2 - 64\,x^2y + 32\,xy^2 - (-48\,x^2y^2) = 32\,x^2y^2 - 80\,x^2y + \\ &32\,xy^2 + 16\,xy \\ &[6] \quad -100\,x^2y + 15\,xy^2 + 50\,xy + 50\,x^2y^2 - 50\,x^2y + 15\,xy - (50\,x^2y^2 - 25\,x^2y - 50\,xy^2) = -125\,x^2y + 65\,xy^2 + 65\,xy \end{aligned}$$

$$\begin{aligned} &[7] \quad 108\,x^2y - 6\,xy^2 + 6\,xy - (-36\,x^2y - 24\,xy^2 + 36\,xy) + (-72\,x^2y + 36\,xy^2 + 12\,xy) = \\ &72\,x^2y + 54\,xy^2 - 18\,xy \\ &[8] \quad 217\,xy^2 + 196\,x^2y^2 + 105\,x^2y - (196\,x^2y - 14\,xy^2) = 196\,x^2y^2 - 91\,x^2y + 231\,xy^2 \\ &[9] \quad -16\,xy^2 + 192\,xy + 64\,x^2y^2 + 16\,xy^2 + 192\,xy - (256\,x^2y^2 + 32\,x^2y - 192\,xy^2) = \\ &-192\,x^2y^2 - 32\,x^2y + 192\,xy^2 + 384\,xy \\ &[10] \quad 81\,x^2y^2 + 162\,x^2y - 9\,xy^2 - (153\,x^2y^2 + 9\,xy) + (-36\,x^2y^2 + 81\,xy^2 - 36\,xy) = \\ &-108\,x^2y^2 + 162\,x^2y + 72\,xy^2 - 45\,xy \end{aligned}$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{array}{ll} [1] & (0) \cdot (0) = 0 \\ [2] & (-4\,b^2x^3y^3z^3) \cdot (4\,b^3xyz^3) = -16\,b^5x^4y^4z^6 \\ [3] & (-16\,b^2x^2y^3z^2) \cdot (-16\,b^3x^3y^2z^2) = 256\,b^5x^5y^5z^4 \\ [4] & (-12\,bx^2y^2z^3) \cdot (36\,b^2xy^2z^3) = -432\,b^3x^3y^4z^6 \\ [5] & (4\,bxy^3z^3) \cdot (-64\,bx^3yz^3) = -256\,b^2x^4y^4z^6 \\ [6] & (-100\,b^2x^3yz^2) \cdot (125\,bx^3yz) = -12500\,b^3x^6y^2z^3 \\ [7] & (-864\,bx^2y^3z^3) \cdot (-144\,b^2xy^3z) = 124416\,b^3x^3y^6z^4 \\ [8] & (7\,b^3x^3y^2z^2) \cdot (-7\,b^3x^2y^2z) = -49\,b^6x^5y^4z^3 \\ [9] & (-8\,b^3x^2y^2z^2) \cdot (16\,b^2x^3y^2z^2) = -128\,b^5x^5y^4z^4 \\ [10] & (18\,b^2x^2y^2z) \cdot (729\,bxyz^3) = 13122\,b^3x^3y^3z^4 \\ \end{array}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^2) \cdot (9x^2) = -18x^4$$

[2] $(-2x) \cdot (-6x^2 - 2x) = 12x^3 + 4x^2$
[3] $(4x) \cdot (-3x^2 + x) = -12x^3 + 4x^2$
[4] $(3x) \cdot (-2x^2 + 3x) = -6x^3 + 9x^2$
[5] $(-x) \cdot (6x^2 - 6x) = -6x^3 + 6x^2$
[6] $(4x) \cdot (-4x^2 + 8x) = -16x^3 + 32x^2$
[7] $(4x) \cdot (5x) = 20x^2$
[8] $(x) \cdot (-x^2 + 3x) = -x^3 + 3x^2$
[9] $(4x) \cdot (3x^2 + 2x) = 12x^3 + 8x^2$
[10] $(4x) \cdot (-4x^2 + x) = -16x^3 + 4x^2$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x^2-2\,x)\cdot(-6\,x^2+2\,x) = -24\,x^4+20\,x^3-4\,x^2 \\ &[2] \quad (-x^2+3\,x)\cdot(6\,x^2+x) = -6\,x^4+17\,x^3+3\,x^2 \\ &[3] \quad (2\,x^2)\cdot(3\,x) = 6\,x^3 \\ &[4] \quad (-4\,x^2-2\,x)\cdot(3\,x^2+3\,x) = -12\,x^4-18\,x^3-6\,x^2 \\ &[5] \quad (3\,x^2)\cdot(-4\,x^2+3\,x) = -12\,x^4+9\,x^3 \\ &[6] \quad (6\,x^2)\cdot(-3\,x^2+x) = -18\,x^4+6\,x^3 \\ &[7] \quad (x)\cdot(2\,x^2+6\,x) = 2\,x^3+6\,x^2 \\ &[8] \quad (2\,x^2+3\,x)\cdot(-x^2-3\,x) = -2\,x^4-9\,x^3-9\,x^2 \end{aligned}$$

[9]
$$(6x) \cdot (9x^2) = 54x^3$$

[10]
$$(x^2 - 2x) \cdot (9x^2) = 9x^4 - 18x^3$$

[11]
$$(0) \cdot (2x^2 + 6x) = 0$$

[12]
$$(4x^2 + 2x) \cdot (2x^2 - x) = 8x^4 - 2x^2$$

[13]
$$(3x^2 + 4x) \cdot (-x^2 + 4x) = -3x^4 + 8x^3 + 16x^2$$

[14]
$$(2x^2 - x) \cdot (-2x^2 - 2x) = -4x^4 - 2x^3 + 2x^2$$

[15]
$$(-5x^2) \cdot (4x^2 + 3x) = -20x^4 - 15x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2x^3+6x)\cdot(6x^3-x^2)=-12x^6+2x^5+36x^4-6x^3$$

[2]
$$(4x^3 - 2x) \cdot (4x^3 - 2x^2) = 16x^6 - 8x^5 - 8x^4 + 4x^3$$

[3]
$$(2x) \cdot (-9x^2 + 4x) = -18x^3 + 8x^2$$

[4]
$$(3x^2 + 4x) \cdot (2x^2 + 4x) = 6x^4 + 20x^3 + 16x^2$$

[5]
$$(4x^3 + 2x^2) \cdot (4x^3 + 6x^2 - x) = 16x^6 + 32x^5 + 8x^4 - 2x^3$$

[6]
$$(-x^3 + 3x^2) \cdot (x^3 + 2x^2) = -x^6 + x^5 + 6x^4$$

[7]
$$(-5x^2) \cdot (-2x^2 - 2x) = 10x^4 + 10x^3$$

[8]
$$(-7x^2) \cdot (7x^3 + 2x^2) = -49x^5 - 14x^4$$

[9]
$$(2x^2 - 3x) \cdot (-2x^3 - 4x^2 + x) = -4x^5 - 2x^4 + 14x^3 - 3x^2$$

[10]
$$(-2x^3 + 6x^2) \cdot (-2x^2 - 2x) = 4x^5 - 8x^4 - 12x^3$$

[11]
$$(2x^3 - 3x^2) \cdot (-x^3 + 3x^2 + x) = -2x^6 + 9x^5 - 7x^4 - 3x^3$$

[12]
$$(x^3 + 2x^2) \cdot (-3x^3 - x^2) = -3x^6 - 7x^5 - 2x^4$$

[13]
$$(-5x^3 - 4x) \cdot (-2x^3) = 10x^6 + 8x^4$$

[14]
$$(-4x^2 - x) \cdot (2x) = -8x^3 - 2x^2$$

[15]
$$(7x) \cdot (-x^2 + 2x) = -7x^3 + 14x^2$$

[16]
$$(-4x^3 - 2x) \cdot (2x^3 - 4x^2 - x) = -8x^6 + 16x^5 + 8x^3 + 2x^2$$

[17]
$$(-6x^3) \cdot (-7x^2) = 42x^5$$

[18]
$$(2x^2 + 2x) \cdot (-3x^3 + 3x^2 + 2x) = -6x^5 + 10x^3 + 4x^2$$

[19]
$$(5x^3 - 3x^2) \cdot (-x^3 + x^2 - 4x) = -5x^6 + 8x^5 - 23x^4 + 12x^3$$

[20]
$$(2x^3 - 4x) \cdot (x^3 + 2x^2 + 3x) = 2x^6 + 4x^5 + 2x^4 - 8x^3 - 12x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-4x^2y^2 + 2xy) \cdot (-4x^2y - 3xy^2 + 2xy) = 16x^4y^3 + 12x^3y^4 - 8x^3y^3 - 8x^3y^2 - 6x^2y^3 + 4x^2y^2$$

$$8x^{3}y^{2} - 6x^{2}y^{3} + 4x^{2}y^{2}$$
[2]
$$(3x^{2}y - 2xy^{2}) \cdot (-2x^{2}y^{2} - x^{2}y + 3xy) = -6x^{4}y^{3} + 4x^{3}y^{4} - 3x^{4}y^{2} + 2x^{3}y^{3} + 9x^{3}y^{2} - 6x^{2}y^{3}$$

[3]
$$(-7xy) \cdot (3x^2y^2 - 5xy) = -21x^3y^3 + 35x^2y^2$$

[4]
$$(-3xy) \cdot (2x^2y^2 - 4xy^2 + 3xy) = -6x^3y^3 + 12x^2y^3 - 9x^2y^2$$

[5]
$$(-4x^2y^2 - 3xy) \cdot (-3x^2y + 2xy^2) = 12x^4y^3 - 8x^3y^4 + 9x^3y^2 - 6x^2y^3$$

[6]
$$(3x^2y - 2xy) \cdot (-6x^2y^2 + x^2y) = -18x^4y^3 + 3x^4y^2 + 12x^3y^3 - 2x^3y^2$$

[7]
$$(-2x^2y - xy) \cdot (3x^2y^2 - xy) = -6x^4y^3 - 3x^3y^3 + 2x^3y^2 + x^2y^2$$