1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

$$[1] \quad 4x^5 - x^4 + 3x^4 + 3x + -2x^6 - 3x = -2x^6 + 4x^5 + 2x^4 \\ [2] \quad x^4 - 2x^3 - 4x^2 + -2x^3 + 3x^2 + 2x^4 + 4x^2 = 3x^4 - 4x^3 + 3x^2 \\ [3] \quad -x^5 - 4x^3 + 3x + (-x^6 - 2x^5 + x^2) + (-6x^4 - 2x) = -x^6 - 3x^5 - 6x^4 - 4x^3 + x^2 + x \\ [4] \quad 4x^6 - 4x^5 + -4x^4 + 2x^2 + x + x^4 + 5x^3 = 4x^6 - 4x^5 - 3x^4 + 5x^3 + 2x^2 + x \\ [5] \quad -2x^5 - 3x^2 - 3x + (-x^6 + 3x^3 + 2x^2) + (-7x^5 + 4x^2) = -x^6 - 9x^5 + 3x^3 + 3x^2 - 3x \\ [6] \quad 3x^3 + 5x^2 + -4x^5 - 3x^3 - 2x + 4x^5 - x^4 + 4x = -x^4 + 5x^2 + 2x \\ [7] \quad 9x^3 + -4x^6 + 2x^5 - 4x + (-2x^6 - 4x^4 + 4x^2) = -6x^6 + 2x^5 - 4x^4 + 9x^3 + 4x^2 - 4x \\ [8] \quad 2x^5 - x^4 + x^2 + -x^6 + 5x + 2x^6 = x^6 + 2x^5 - x^4 + x^2 + 5x \\ [9] \quad x^3 + 2x^2 + 4x^6 - x^5 + 2x^4 + -2x^5 - 2x^3 - 4x^2 = 4x^6 - 3x^5 + 2x^4 - x^3 - 2x^2 \\ [10] \quad 2x^3 + 3x^5 + 3x^3 + 2x^2 + -x^5 - x^3 + 3x^2 = 2x^5 + 4x^3 + 5x^2$$

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$[1] \quad 0+0+0=0 \\ [2] \quad 4xy^2-xy+2x^2y^2-4x^2y-3xy+-2x^2y^2+3x^2y=-x^2y+4xy^2-4xy \\ [3] \quad 12x^2y^2+4x^2y+12xy+-16x^2y^2-16xy^2+8xy+-16x^2y=-4x^2y^2-12x^2y-16xy^2+20xy \\ [4] \quad 36x^2y^2-12xy^2+-3x^2y+6xy^2-18xy+-12x^2y-9xy=36x^2y^2-15x^2y-6xy^2-27xy \\ [5] \quad 60x^2y^2-64x^2y+-92xy+(-32x^2y^2+48x^2y+64xy^2)=28x^2y^2-16x^2y+64xy^2-92xy \\ [6] \quad 120x^2y^2+15xy^2+-10x^2y^2-100xy+(-85x^2y^2-100xy^2)=25x^2y^2-85xy^2-100xy \\ [7] \quad 102xy^2+12xy+-144x^2y-54xy^2+-18x^2y^2+180xy=-18x^2y^2-144x^2y+48xy^2+192xy \\ [8] \quad 14x^2y^2-98x^2y+7xy+-7x^2y+14xy^2+196xy+-140xy^2=14x^2y^2-105x^2y-126xy^2+203xy \\ [9] \quad -64xy^2+272xy+(-120x^2y^2-32xy)+(-24x^2y-248xy)=-120x^2y^2-24x^2y-64xy^2-8xy \\ [10] \quad 27x^2y+18xy+-162x^2y^2-162x^2y+81x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-63xy \\ [10] \quad 27x^2y+18xy+-162x^2y^2-162x^2y^2-162x^2y+81x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-63xy \\ [10] \quad 27x^2y+18xy+2x^2+2x^2y^2-162x^2y^2-162x^2y+81x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-63xy \\ [10] \quad 27x^2y+18xy+2x^2+2x^2y^2-162x^2y^2-162x^2y+81x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-81xy=-162x^2y^2-54x^2y-243xy^2-81xy=-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-162x^2y^2-16$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

[1]
$$0 - (0) + (0) = 0$$

[2] $4x^2y^2 + 0 - (-7x^2y^2 + xy) = 11x^2y^2 - xy$
[3] $-2x^2y^2 + 10xy^2 + -12xy^2 - (14x^2y^2 + 4xy) = -16x^2y^2 - 2xy^2 - 4xy$
[4] $27x^2y^2 - 21x^2y - (-18x^2y + 3xy) + (3x^2y^2 - 6x^2y - 18xy^2) = 30x^2y^2 - 9x^2y - 18xy^2 - 3xy$

$$[5] \quad -32\,x^2y^2 - 64\,xy^2 - 16\,xy + 16\,x^2y^2 - 48\,xy^2 + 4\,xy - (32\,x^2y^2 - 48\,x^2y) = \\ -48\,x^2y^2 + 48\,x^2y - 112\,xy^2 - 12\,xy \\ [6] \quad 50\,x^2y^2 - 20\,x^2y - 5\,xy^2 + -10\,x^2y^2 + 15\,xy^2 - 50\,xy - (10\,x^2y^2 + 50\,x^2y - 25\,xy) = 30\,x^2y^2 - 70\,x^2y + 10\,xy^2 - 25\,xy \\ [7] \quad 114\,x^2y^2 + 36\,xy - (-168\,xy^2) + (-18\,x^2y + 24\,xy) = 114\,x^2y^2 - 18\,x^2y + 168\,xy^2 + 60\,xy \\ [8] \quad 7\,x^2y^2 + 21\,x^2y - 21\,xy + -28\,x^2y - 7\,xy^2 - (-28\,x^2y^2 + 49\,xy) = 35\,x^2y^2 - 7\,x^2y - 7\,xy^2 - 70\,xy \\ [9] \quad -32\,x^2y + -192\,x^2y + 224\,xy^2 - (192\,xy^2) = -224\,x^2y + 32\,xy^2 \\ [10] \quad -162\,x^2y^2 + 81\,x^2y + 324\,xy - (279\,x^2y^2 - 27\,x^2y) + (-99\,x^2y^2 + 324\,xy^2) = -540\,x^2y^2 + 108\,x^2y + 324\,xy^2 + 324\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (bxy^2z) \cdot (-3\,bxyz^3) = -3\,b^2x^2y^3z^4 \\ &[3] \quad (12\,b^3xyz^3) \cdot (12\,bxy^2z^3) = 144\,b^4x^2y^3z^6 \\ &[4] \quad (6\,b^3x^2yz^3) \cdot (-18\,bx^3y^3z) = -108\,b^4x^5y^4z^4 \\ &[5] \quad (-64\,b^3x^3yz^3) \cdot (-32\,bx^2yz^3) = 2048\,b^4x^5y^2z^6 \\ &[6] \quad (-375\,b^3x^2y^3z^3) \cdot (50\,b^2xy^3z^3) = -18750\,b^5x^3y^6z^6 \\ &[7] \quad (-72\,bxy^3z^2) \cdot (36\,b^3x^2y^2z^3) = -2592\,b^4x^3y^5z^5 \\ &[8] \quad (-49\,bxy^3z^3) \cdot (-1372\,b^2x^3y^3z^2) = 67228\,b^3x^4y^6z^5 \\ &[9] \quad (-8\,b^3x^2yz) \cdot (-2048\,b^3x^2y^3z) = 16384\,b^6x^4y^4z^2 \\ &[10] \quad (-2187\,b^2x^3y^2z^3) \cdot (9\,b^2x^2yz^3) = -19683\,b^4x^5y^3z^6 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x)\cdot(6\,x^2+4\,x) = -12\,x^3-8\,x^2 \\ &[2] \quad (-3\,x)\cdot(2\,x^2+3\,x) = -6\,x^3-9\,x^2 \\ &[3] \quad (-4\,x^2)\cdot(x^2) = -4\,x^4 \\ &[4] \quad (-2\,x)\cdot(x^2+x) = -2\,x^3-2\,x^2 \\ &[5] \quad (-4\,x)\cdot(0) = 0 \\ &[6] \quad (x)\cdot(x^2+3\,x) = x^3+3\,x^2 \\ &[7] \quad (-3\,x^2)\cdot(-7\,x^2-3\,x) = 21\,x^4+9\,x^3 \\ &[8] \quad (4\,x^2)\cdot(-3\,x) = -12\,x^3 \\ &[9] \quad (4\,x^2)\cdot(-3\,x^2) = -12\,x^4 \\ &[10] \quad (-x^2)\cdot(3\,x^2-2\,x) = -3\,x^4+2\,x^3 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (4\,x^2+x)\cdot(6\,x^2) = 24\,x^4+6\,x^3\\ &[2] \quad (-4\,x)\cdot(-2\,x^2+x) = 8\,x^3-4\,x^2\\ &[3] \quad (-7\,x)\cdot(3\,x^2+6\,x) = -21\,x^3-42\,x^2\\ &[4] \quad (-4\,x^2-x)\cdot(2\,x^2+2\,x) = -8\,x^4-10\,x^3-2\,x^2\\ &[5] \quad (2\,x^2-4\,x)\cdot(8\,x^2) = 16\,x^4-32\,x^3 \end{aligned}$$

[6]
$$(-3x^2 - 3x) \cdot (3x^2 - 4x) = -9x^4 + 3x^3 + 12x^2$$

[7]
$$(3x^2 + 3x) \cdot (x^2 + 7x) = 3x^4 + 24x^3 + 21x^2$$

[8]
$$(-6x) \cdot (6x^2 - x) = -36x^3 + 6x^2$$

[9]
$$(x^2 - 4x) \cdot (-6x^2 - 2x) = -6x^4 + 22x^3 + 8x^2$$

[10]
$$(6x) \cdot (-6x^2 + x) = -36x^3 + 6x^2$$

[11]
$$(-x^2 + 2x) \cdot (x^2 - 2x) = -x^4 + 4x^3 - 4x^2$$

[12]
$$(3x) \cdot (x^2) = 3x^3$$

[13]
$$(4x^2 + 2x) \cdot (x^2 + x) = 4x^4 + 6x^3 + 2x^2$$

[14]
$$(-6x^2) \cdot (-3x^2 - 7x) = 18x^4 + 42x^3$$

[15]
$$(2x^2 - 2x) \cdot (-5x^2) = -10x^4 + 10x^3$$

Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(x^3 - 3x^2) \cdot (-8x^3) = -8x^6 + 24x^5$$

[2]
$$(-3x^3 - 3x^2) \cdot (-x^3 - 4x^2 - x) = 3x^6 + 15x^5 + 15x^4 + 3x^3$$

[3]
$$(-x^2-2x)\cdot(-3x^3+2x^2-x)=3x^5+4x^4-3x^3+2x^2$$

[4]
$$(-4x^2 - 3x) \cdot (2x) = -8x^3 - 6x^2$$

[5]
$$(-6x^2) \cdot (-7x^3) = 42x^5$$

[6]
$$(-2x^2 + x) \cdot (3x^3 - 2x^2 + 3x) = -6x^5 + 7x^4 - 8x^3 + 3x^2$$

[7]
$$(-3x^3 + 3x^2 - 2x) \cdot (4x^3) = -12x^6 + 12x^5 - 8x^4$$

[8]
$$(-3x^3 + 4x^2) \cdot (2x^2 - 4x) = -6x^5 + 20x^4 - 16x^3$$

[9]
$$(x^2 + 4x) \cdot (-2x) = -2x^3 - 8x^2$$

[10]
$$(6x^2 - x) \cdot (6x^2) = 36x^4 - 6x^3$$

[11]
$$(2x^3 - 2x^2) \cdot (-x^3 - 4x^2 + 3x) = -2x^6 - 6x^5 + 14x^4 - 6x^3$$

[12]
$$(-2x^3 + 3x) \cdot (-x^3 - 3x^2) = 2x^6 + 6x^5 - 3x^4 - 9x^3$$

[13]
$$(-x^3 + x^2 - 2x) \cdot (4x^3 - 4x^2 + 2x) = -4x^6 + 8x^5 - 14x^4 + 10x^3 - 4x^2$$

[14]
$$(3x^2 - 2x) \cdot (-3x^3 + x) = -9x^5 + 6x^4 + 3x^3 - 2x^2$$

[15]
$$(x^3 - 3x^2) \cdot (2x^3 + 4x^2 + x) = 2x^6 - 2x^5 - 11x^4 - 3x^3$$

[16]
$$(4x) \cdot (2x^3 + x^2) = 8x^4 + 4x^3$$

[17]
$$(0) \cdot (3x^3 + 3x) = 0$$

[18]
$$(6x^2) \cdot (-x^2 - 6x) = -6x^4 - 36x^3$$

[19]
$$(4x^3 + 3x^2 + 3x) \cdot (2x^2) = 8x^5 + 6x^4 + 6x^3$$

[20]
$$(0) \cdot (-x^3 + 2x^2) = 0$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

[1]
$$(-2xy^2 + 4xy) \cdot (-xy^2 + xy) = 2x^2y^4 - 6x^2y^3 + 4x^2y^2$$

[2]
$$(4x^2y^2 + 4x^2y) \cdot (-2x^2y^2 - 2xy^2 - xy) = -8x^4y^4 - 8x^4y^3 - 8x^3y^4 - 12x^3y^3 - 4x^3y^2$$

[3]
$$(-3x^2y^2 + 3xy^2) \cdot (-7xy^2 - 4xy) = 21x^3y^4 + 12x^3y^3 - 21x^2y^4 - 12x^2y^3$$

[4]
$$(4x^2y^2 - x^2y) \cdot (2x^2y^2 + 2x^2y) = 8x^4y^4 + 6x^4y^3 - 2x^4y^2$$

[5]
$$(xy^2 - 4xy) \cdot (-3x^2y^2 + 2x^2y) = -3x^3y^4 + 14x^3y^3 - 8x^3y^2$$

[6]
$$(-2x^2y^2 - 2x^2y) \cdot (-2x^2y - 4xy^2) = 4x^4y^3 + 8x^3y^4 + 4x^4y^2 + 8x^3y^3$$

[7]
$$(2xy^2 - xy) \cdot (x^2y + 3xy^2 - xy) = 2x^3y^3 + 6x^2y^4 - x^3y^2 - 5x^2y^3 + x^2y^2$$