## 1. Evaluación 1°D - Funciones

Ejercicio 1: Realiza las siguientes sumas de polinomios:

[1] 
$$x^6 + 5x^3 + -2x^6 - x^4 - 4x + x^4 - 7x^3 = -x^6 - 2x^3 - 4x$$
  
[2]  $-3x^3 + (-2x^6 - 2x^2 - x) + (-x^5 - 4x) = -2x^6 - x^5 - 3x^3 - 2x^2 - 5x$   
[3]  $3x^6 - 2x^4 + 4x^3 + -3x^5 - 4x^3 + 3x + 3x^5 - 4x^4 - 3x = 3x^6 - 6x^4$   
[4]  $2x^6 - 4x^4 - 2x + 2x^5 + 3x^4 - x^2 + 2x^4 + 2x^3 = 2x^6 + 2x^5 + x^4 + 2x^3 - x^2 - 2x$   
[5]  $2x^6 - x^5 - 4x^4 + -3x^5 - 3x^4 + x^3 + -x^4 = 2x^6 - 4x^5 - 8x^4 + x^3$   
[6]  $2x^3 + 4x + -4x^6 - x^5 - 3x^4 + 3x^5 - 2x^4 - 2x^2 = -4x^6 + 2x^5 - 5x^4 + 2x^3 - 2x^2 + 4x$   
[7]  $2x^6 + 2x^2 + 3x + -x^5 - 4x^4 - 4x^3 + 4x^6 - 2x^3 = 6x^6 - x^5 - 4x^4 - 6x^3 + 2x^2 + 3x$   
[8]  $4x^6 + 2x^2 - x + 4x^3 - x + -4x^5 - 4x^3 - x^2 = 4x^6 - 4x^5 + x^2 - 2x$   
[9]  $4x^5 + 3x^4 - x^3 + -4x^6 + 2x^4 - 3x + 8x^4 + 2x^3 = -4x^6 + 4x^5 + 13x^4 + x^3 - 3x$ 

[10]  $2x^4 + 2x^3 - x^2 + x^6 + x^3 + -2x^6 - x^5 + 3x^2 = -x^6 - x^5 + 2x^4 + 3x^3 + 2x^2$ 

Ejercicio 2: Realiza las siguientes sumas de polinomios:

$$\begin{aligned} & [1] \quad 0+0+0=0 \\ & [2] \quad 5x^2y-2\,xy+-3\,x^2y-2\,xy+(-x^2y-3\,xy)=x^2y-7\,xy \\ & [3] \quad 16\,x^2y^2+8\,x^2y+16\,xy+-6\,x^2y^2+8\,x^2y-4\,xy+-12\,x^2y^2-16\,xy^2=\\ & -2\,x^2y^2+16\,x^2y-16\,xy^2+12\,xy \\ & [4] \quad 24\,x^2y-9\,xy^2+-12\,x^2y+9\,xy^2+9\,xy+-3\,x^2y+30\,xy=9\,x^2y+39\,xy \\ & [5] \quad 8\,x^2y+48\,xy^2+32\,xy+-4\,x^2y-64\,xy^2-4\,xy+36\,x^2y=40\,x^2y-16\,xy^2+28\,xy \\ & [6] \quad 15\,x^2y-5\,xy^2-20\,xy+-50\,xy^2-10\,xy+(-10\,x^2y+15\,xy^2+5\,xy)=\\ 5\,x^2y-40\,xy^2-25\,xy \\ & [7] \quad -36\,x^2y^2-72\,x^2y-24\,xy^2+(-36\,x^2y-144\,xy^2+144\,xy)+(-138\,xy)=\\ -36\,x^2y^2-108\,x^2y-168\,xy^2+6\,xy \\ & [8] \quad 147\,x^2y-189\,xy^2+-196\,x^2y^2+196\,x^2y-196\,xy+-98\,x^2y^2=-294\,x^2y^2+\\ 343\,x^2y-189\,xy^2-196\,xy \\ & [9] \quad 96\,x^2y-64\,xy^2+-16\,x^2y^2-64\,xy^2-16\,xy+(-24\,x^2y+128\,xy^2-64\,xy)=\\ -16\,x^2y^2+72\,x^2y-80\,xy \\ & [10] \quad 81\,x^2y^2+81\,x^2y+81\,xy+342\,x^2y+27\,xy^2+279\,x^2y^2+243\,xy=360\,x^2y^2+\\ 423\,x^2y+27\,xy^2+324\,xy \end{aligned}$$

Ejerciio 3 Realiza las siguientes sumas y restas de polinomios:

$$\begin{aligned} &[1] \quad 0 - (0) + (0) = 0 \\ &[2] \quad -4\,xy^2 + -3\,x^2y^2 - 3\,xy - (3\,x^2y^2 - 3\,x^2y + 3\,xy^2) = -6\,x^2y^2 + 3\,x^2y - 7\,xy^2 - 3\,xy \\ &[3] \quad 20\,x^2y + 12\,x^2y^2 + 14\,xy - (24\,x^2y^2 - 8\,x^2y) = -12\,x^2y^2 + 28\,x^2y + 14\,xy \\ &[4] \quad 6\,x^2y^2 - 21\,xy^2 - (-3\,x^2y^2 + 9\,x^2y + 3\,xy) + (6\,x^2y - 36\,xy) = 9\,x^2y^2 - 3\,x^2y - 21\,xy^2 - 39\,xy \\ &[5] \quad -20\,x^2y + -16\,x^2y - 16\,xy^2 + 48\,xy - (8\,x^2y^2 + 16\,x^2y + 64\,xy^2) = -8\,x^2y^2 - 52\,x^2y - 80\,xy^2 + 48\,xy \end{aligned}$$

$$[6] \quad -20\,x^2y^2 - 80\,x^2y + 110\,x^2y^2 - 75\,xy - (-5\,x^2y^2 - 5\,xy) = 95\,x^2y^2 - 80\,x^2y - 70\,xy$$
 
$$[7] \quad 18\,x^2y - (-108\,x^2y^2 + 24\,x^2y + 72\,xy) + (192\,xy) = 108\,x^2y^2 - 6\,x^2y + 120\,xy$$
 
$$[8] \quad -14\,x^2y^2 - 147\,x^2y - 49\,xy + -84\,x^2y + 49\,xy - (-91\,xy^2 - 49\,xy) = -14\,x^2y^2 - 231\,x^2y + 91\,xy^2 + 49\,xy$$
 
$$[9] \quad -64\,x^2y + 24\,xy^2 + 192\,xy + -184\,xy^2 - (8\,x^2y^2 + 24\,x^2y - 256\,xy^2) = -8\,x^2y^2 - 88\,x^2y + 96\,xy^2 + 192\,xy$$
 
$$[10] \quad 9\,x^2y^2 + 45\,x^2y - (288\,x^2y^2 + 81\,xy) + (216\,xy^2) = -279\,x^2y^2 + 45\,x^2y + 216\,xy^2 - 81\,xy$$

Ejercicio 3: Realiza las siguientes multiplicaciones de monomios:

$$\begin{aligned} &[1] \quad (0) \cdot (0) = 0 \\ &[2] \quad (-2\,b^3x^3y^3z^3) \cdot (-2\,b^3x^2yz^3) = 4\,b^6x^5y^4z^6 \\ &[3] \quad (-4\,b^2x^2yz^3) \cdot (2\,bxy^3z^3) = -8\,b^3x^3y^4z^6 \\ &[4] \quad (18\,b^2x^2yz) \cdot (-6\,bx^2y^2z) = -108\,b^3x^4y^3z^2 \\ &[5] \quad (-64\,bx^2y^2z^2) \cdot (64\,b^2xy^2z^3) = -4096\,b^3x^3y^4z^5 \\ &[6] \quad (15\,b^2x^3y^2z) \cdot (-250\,b^2x^3y^3z^3) = -3750\,b^4x^6y^5z^4 \\ &[7] \quad (144\,bx^3y^2z) \cdot (-72\,bxy^3z^2) = -10368\,b^2x^4y^5z^3 \\ &[8] \quad (-14\,b^2x^3yz^2) \cdot (-14\,bxy^2z^2) = 196\,b^3x^4y^3z^4 \\ &[9] \quad (-1536\,bx^2yz^3) \cdot (-1536\,b^2x^3y^3z) = 2359296\,b^3x^5y^4z^4 \\ &[10] \quad (18\,bxy^2z^3) \cdot (-1458\,b^2xyz) = -26244\,b^3x^2y^3z^4 \end{aligned}$$

Ejercicio 4: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} & [1] \quad (x^2) \cdot (-2\,x^2 - x) = -2\,x^4 - x^3 \\ & [2] \quad (-2\,x) \cdot (x^2 - 7\,x) = -2\,x^3 + 14\,x^2 \\ & [3] \quad (4\,x^2) \cdot (-6\,x) = -24\,x^3 \\ & [4] \quad (-x^2) \cdot (-2\,x^2 + 3\,x) = 2\,x^4 - 3\,x^3 \\ & [5] \quad (2\,x) \cdot (6\,x^2 - x) = 12\,x^3 - 2\,x^2 \\ & [6] \quad (x) \cdot (3\,x^2 + 3\,x) = 3\,x^3 + 3\,x^2 \\ & [7] \quad (x^2) \cdot (-4\,x^2 + x) = -4\,x^4 + x^3 \\ & [8] \quad (-4\,x) \cdot (-x^2 - 5\,x) = 4\,x^3 + 20\,x^2 \\ & [9] \quad (-4\,x^2) \cdot (4\,x^2) = -16\,x^4 \\ & [10] \quad (-2\,x) \cdot (-2\,x^2 + 6\,x) = 4\,x^3 - 12\,x^2 \end{aligned}$$

Ejercicio 5: Realiza las siguientes multiplicaciones de polinomios:

$$\begin{aligned} &[1] \quad (-2\,x^2) \cdot (-2\,x^2 - 2\,x) = 4\,x^4 + 4\,x^3 \\ &[2] \quad (-3\,x^2) \cdot (6\,x^2 + 3\,x) = -18\,x^4 - 9\,x^3 \\ &[3] \quad (5\,x^2) \cdot (-3\,x^2 + 6\,x) = -15\,x^4 + 30\,x^3 \\ &[4] \quad (x^2 + 3\,x) \cdot (8\,x^2 + 3\,x) = 8\,x^4 + 27\,x^3 + 9\,x^2 \\ &[5] \quad (x^2) \cdot (-2\,x^2) = -2\,x^4 \\ &[6] \quad (-2\,x) \cdot (8\,x^2) = -16\,x^3 \\ &[7] \quad (-x^2 - x) \cdot (x^2 + x) = -x^4 - 2\,x^3 - x^2 \end{aligned}$$

[8] 
$$(0) \cdot (-7x^2 + 3x) = 0$$

[9] 
$$(-3x^2 + x) \cdot (3x^2 - x) = -9x^4 + 6x^3 - x^2$$

[10] 
$$(-2x^2 + 2x) \cdot (6x^2) = -12x^4 + 12x^3$$

[11] 
$$(x^2 + 2x) \cdot (2x^2 - 4x) = 2x^4 - 8x^2$$

[12] 
$$(-8x) \cdot (5x^2 + 3x) = -40x^3 - 24x^2$$

[13] 
$$(3x^2 - x) \cdot (3x^2 + x) = 9x^4 - x^2$$

[14] 
$$(x^2 - x) \cdot (4x^2 + 3x) = 4x^4 - x^3 - 3x^2$$

[15] 
$$(7x) \cdot (-4x^2 + x) = -28x^3 + 7x^2$$

## Ejercicio 6: Realiza las siguientes multiplicaciones de polinomios:

[1] 
$$(-x^3 - 3x) \cdot (-4x^2 - x) = 4x^5 + x^4 + 12x^3 + 3x^2$$

[2] 
$$(4x^3 - 4x) \cdot (-3x^3 + 9x) = -12x^6 + 48x^4 - 36x^2$$

[3] 
$$(x^2) \cdot (-3x^2 - 5x) = -3x^4 - 5x^3$$

[4] 
$$(x^3 + x) \cdot (-x^2) = -x^5 - x^3$$

[5] 
$$(2x^2 - 2x) \cdot (-2x^3 - 5x^2) = -4x^5 - 6x^4 + 10x^3$$

[6] 
$$(-5x^3) \cdot (3x^3 - 2x^2 - 5x) = -15x^6 + 10x^5 + 25x^4$$

[7] 
$$(4x^2) \cdot (-6x^3 + 2x^2) = -24x^5 + 8x^4$$

[8] 
$$(-x^3+x)\cdot(x^3)=-x^6+x^4$$

[9] 
$$(3x) \cdot (2x^3) = 6x^4$$

[10] 
$$(-5x^3 + 4x^2) \cdot (-2x^3 + 4x^2) = 10x^6 - 28x^5 + 16x^4$$

[11] 
$$(2x^3 + 3x) \cdot (-x^3 + 8x^2 - 4x) = -2x^6 + 16x^5 - 11x^4 + 24x^3 - 12x^2$$

[12] 
$$(x^3 - 3x) \cdot (-4x^3 - 3x^2 + 2x) = -4x^6 - 3x^5 + 14x^4 + 9x^3 - 6x^2$$

[13] 
$$(-4x^3 - x^2) \cdot (-3x^2) = 12x^5 + 3x^4$$

[14] 
$$(-2x^3 - 2x^2) \cdot (-5x^2) = 10x^5 + 10x^4$$

[15] 
$$(-2x^3 + 2x^2) \cdot (2x^3 + 9x^2) = -4x^6 - 14x^5 + 18x^4$$

[16] 
$$(-2x^3 - 2x^2 - 3x) \cdot (x^3 - x^2 + x) = -2x^6 - 3x^4 + x^3 - 3x^2$$

[17] 
$$(-4x^3 - x) \cdot (5x^2) = -20x^5 - 5x^3$$

[18] 
$$(-x^2 + 4x) \cdot (-x^2 - 2x) = x^4 - 2x^3 - 8x^2$$

[19] 
$$(2x) \cdot (3x^2) = 6x^3$$

[20] 
$$(-x^2 + 3x) \cdot (3x^2 - 8x) = -3x^4 + 17x^3 - 24x^2$$

Ejercicio 7: Realiza las siguientes multiplicaciones de polinomios:

$$[1] \quad (-x^2y^2 - 2xy) \cdot (x^2y^2 - 3x^2y - 3xy) = -x^4y^4 + 3x^4y^3 + x^3y^3 + 6x^3y^2 + 6x^2y^2 + 6x^2y^$$

[2] 
$$(4x^2y^2 - 2xy) \cdot (5x^2y^2 - 2x^2y) = 20x^4y^4 - 8x^4y^3 - 10x^3y^3 + 4x^3y^2$$

[3] 
$$(-x^2y^2+xy^2)\cdot(2x^2y^2-x^2y-4xy^2) = -2x^4y^4+x^4y^3+6x^3y^4-x^3y^3-4x^2y^4$$

[4] 
$$(x^2y^2 - 2xy) \cdot (2x^2y^2 - 4x^2y + 2xy^2) = 2x^4y^4 - 4x^4y^3 + 2x^3y^4 - 4x^3y^3 + 8x^3y^2 - 4x^2y^3$$

[5] 
$$(-4x^2y^2 - x^2y) \cdot (4x^2y^2) = -16x^4y^4 - 4x^4y^3$$

[6] 
$$(x^2y^2) \cdot (-3x^2y - xy^2 + 4xy) = -3x^4y^3 - x^3y^4 + 4x^3y^3$$

[7] 
$$(0) \cdot (-5x^2y + 2xy) = 0$$