

- Which one of the following is a proposition? d
- How are you?
  - What time is it?
  - $4 + x = 5$
  - India is in Europe.
- What is the negation of the statement “Salman sent more than 100 text messages every day”? c
- Salman sent more than 200 text messages every day.
  - Salman sent less than 100 text messages but not every day.
  - Salman did not send more than 100 text messages every day.
  - Salman did not send any text message every day.
- b
- Select the appropriate option after evaluating following four biconditionals are true or false. c
- $2 + 2 = 4$  if and only if  $1 + 1 = 2$ .
  - $1 + 1 = 2$  if and only if  $2 + 3 = 4$ .
  - $1 + 1 = 3$  if and only if fishes can fly.
  - $0 > 1$  if and only if  $2 > 1$ .
- Only 1 and 3 are True
  - Only option 3 and 4 are True
  - Option 1 is True
  - All options are false
- What will be Truth values of the statement  $p \leftrightarrow \neg p$  for the Truth values T, F of p? d
- T, F
  - F, T
  - T, T
  - F, F
- What will be Truth values of the statement  $(p \wedge q) \rightarrow (p \vee q)$  for the Truth values T, T, F, F of p and T, F, T, F of q? C
- T, F, T, F
  - F, T, F, T
  - T, T, T, T
  - F, F, F, F
- If  $p$ : “You can use the wireless network in the airport,”  $q$ : “You pay the daily fee,” and  $r$ : “You are a subscriber to the service”. Which is the right expression for the statement “To use the wireless network in the airport you must pay the daily fee unless you are a subscriber to the service”. B
- $q \wedge r \rightarrow p$
  - $q \vee r \rightarrow p$
  - $p \wedge (q \vee r)$

d)  $p \wedge (q \wedge r)$

What is the negation of the statement “Sam is rich and happy”?

C

- a) Sam is poor and unhappy.
- b) Either Sam is poor or happy
- c) Either Sam is poor or unhappy
- d) Sam is not rich and happy.

Let  $Q(x, y)$  denote the statement “y is the capital of x.” What are these truth values?

C

i)  $Q(\text{Punjab, Chandigarh})$ , ii)  $Q(\text{India, New Delhi})$  iii)  $Q(\text{Rajasthan, Shimla})$ , iv)  $Q(\text{Nepal, Kathmandu})$

- a) T,F,T,F
- b) T,T,F,F
- c) T,T,F,T
- d) T,T,T,T

$(\neg q \wedge (p \rightarrow q)) \rightarrow \neg p$  is a

b

- a) Contingency
- b) Tautology
- c) Contradiction
- d) None of these

$(p \rightarrow q) \wedge (p \rightarrow r)$  is logically equivalent to

B

- a)  $p \rightarrow (q \vee r)$
- b)  $p \rightarrow (q \wedge r)$
- c)  $p \wedge (q \rightarrow r)$
- d)  $p \wedge \neg(q \rightarrow r)$

$\neg p \leftrightarrow q$  is logically equivalent to

A

- a)  $p \leftrightarrow \neg q$
- b)  $p \leftrightarrow q$
- c)  $p \wedge \neg q$
- d)  $p \vee \neg q$

$\neg p \leftrightarrow q$  is logically equivalent to

B

- a)  $p \leftrightarrow \neg q$
- b)  $p \leftrightarrow q$
- c)  $p \wedge \neg q$
- d)  $p \vee \neg q$

$(p \rightarrow q) \wedge (q \rightarrow r) \rightarrow (p \rightarrow r)$  is a

- a) Contingency
- b) Contradiction
- c) Tautology
- d) All the above are true

If x and y are integers of opposite parity (one odd another even) the  $5x+5y$  is

A

- a) Always Odd
- b) Always Even
- c) Odd for some values and even for other values
- d) Can not be decided

$\neg(\forall x \in A)p(x)$  is logically equivalent to

A

- a)  $(\exists x \in A)\neg p(x)$
- b)  $(\exists x \in \neg A)p(x)$
- c)  $(\forall x \in \neg A)p(x)$
- d)  $(\forall x \in A)\neg p(x)$

Contrapositive of the statement “If you are honest, then you are respected.”

B

- a) If You are honest then he is not respected.
- b) If You are not respected than you are not honest.
- c) If you are not honest then you are not respected.
- d) If you are respected then you are honest.

Contrapositive of the statement “If Sahir is a poet, then he is poor”

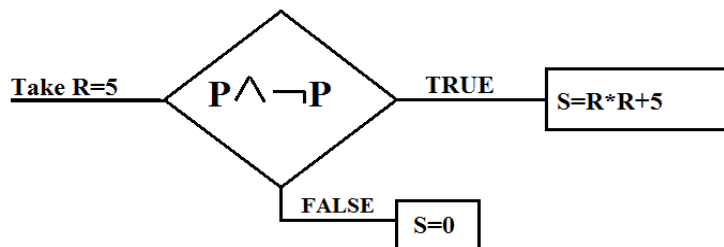
A

- e) If Sahir is rich then he is not poet
- f) If Sahir is not a poet then he is not poor
- g) If Sahir is not poor then he is a poet
- h) If Sahir is not a poet then he is not poor

Let P: Dogs can fly

c

And consider the following flow chart of a computer program



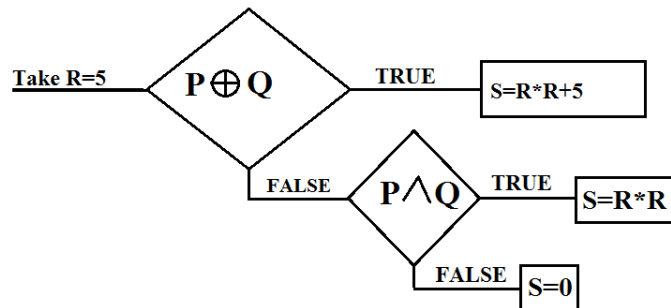
Then the value of S is

- a) 30
- b) 20
- c) 0
- d) 10

a

Let P:  $5+10=15$ , Q:  $5*10=50$

And consider the following flow chart of a computer program



Then the value of S is

- a) 30
- b) 25
- c) 0
- d) 10

What is the correct translation of the following statement into mathematical logic? C  
 “Some COVID 19 vaccines have completed the last trial are ready for production”  
 where:  $x$ : COVID-19 vaccine,  $t(x)$ :  $x$  has completed the last trial,  $p(x)$ :  $x$  is ready for production.

- a)  $\exists x (t(x) \vee p(x))$
- b)  $\exists x (t(x) \rightarrow p(x))$
- c)  $\exists x (t(x) \wedge p(x))$
- d)  $\exists x (p(x) \rightarrow t(x))$

Consider the following statements over the set of integers c

$P$ :  $k$  is even     $Q$ :  $3k+1$  is odd

Then which of the following is/are true

- a) Only converse for the proposition  $P \rightarrow Q$  is true
- b) Only inverse for the proposition  $P \rightarrow Q$  is true
- c) Both converse and inverse for the proposition  $P \rightarrow Q$  is true
- d) Neither converse nor inverse for the proposition  $P \rightarrow Q$  is true

Which of the following statements is the contrapositive of the statement, “You win the game if you know the rules but are not over confident?” a

- a) If you lose the game then you don’t know the rules or you are overconfident.
- b) A sufficient condition that you win the game is that you know the rules or you are not overconfident.
- c) If you don’t know the rules or are overconfident you lose the game.
- d) If you know the rules and are overconfident then you win the game.

In proving  $\pi$  as irrational, we begin with assumption  $\sqrt{7}$  is rational in which type of proof? B

- a) Direct proof
- b) Proof by Contradiction
- c) Vacuous proof
- d) Mathematical Induction

Which of the following can only be used in disproving the statements? C

- a) Direct proof
- b) Contrapositive proofs
- c) Counter Example
- d) Mathematical Induction

Let P: We should be honest., Q: We should be dedicated., R: We should be overconfident. Then 'We should be honest or dedicated but not overconfident.' is best represented by? D

- a)  $\neg P \vee \neg Q \vee R$
- b)  $P \wedge \neg Q \wedge R$
- c)  $P \vee Q \wedge R$
- d)  $P \vee Q \wedge \neg R$

What is the contrapositive of the conditional statement "I come to class whenever there is going to be a test"? B

- a) "If I come to class, then there will be a test."
- b) "If I do not come to class, then there will not be a test."
- c) "If there is not going to be a test, then I don't come to class."
- d) "If there is going to be a test, then I don't come to class."

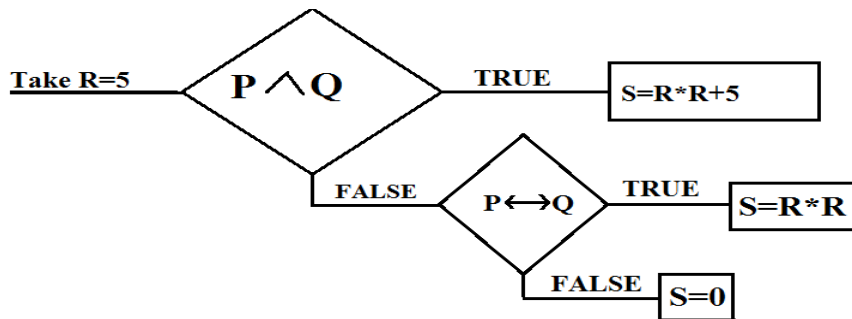
Let  $a$  and  $b$  are the legs of a right triangle with hypotenuse  $c$   
A sufficient condition that a triangle  $T$  be a right angled triangle is that  $a^2 + b^2 = c^2$ . An equivalent statement is B

- (a) If  $T$  is a right angled triangle then  $a^2 + b^2 = c^2$ .
- (b) If  $a^2 + b^2 = c^2$  then  $T$  is a right triangle.
- (c)  $a^2 + b^2 \neq c^2$  Then  $T$  is not a right triangle.
- (d)  $T$  is a right triangle only if  $a^2 + b^2 = c^2$

Let P:  $R^2 - 5 = 10$ . C

$$Q: R^2 - 5 = 20$$

And consider the following flow chart of a computer program



Then the value of S is

- (A) 30
- (B) 25
- (C) 0
- (D) 10

Which one of the following is the most appropriate logical formula to represent the statement? “Students who know Mathematical , coding skills are placed”.

The following notations are used:

$M(x)$ :  $x$  is knowing the Mathematical skills

$C(x)$ :  $x$  is knowing the Coding skills

$P(x)$ :  $x$  is placed

(A)  $\forall x(P(x) \rightarrow (M(x) \wedge C(x)))$

(B)  $\forall x((M(x) \wedge C(x)) \rightarrow P(x))$

(C)  $\exists x((M(x) \wedge C(x)) \rightarrow P(x))$

(D)  $\forall x((M(x) \vee C(x)) \rightarrow P(x))$

P and Q are two propositions. Which of the following logical expressions are equivalent?

I.  $P \vee \sim Q$

II.  $\sim(\sim P \wedge Q)$

III.  $(P \wedge Q) \vee (P \wedge \sim Q) \vee (\sim P \wedge \sim Q)$

IV.  $(P \wedge Q) \vee (P \wedge \sim Q) \vee (\sim P \wedge Q)$

(A) Only I and II

(B) Only I, II and III

(C) Only I, II and IV

(D) All of I, II, III and IV