

1. A binary string is called *dense* if the number of 1's in the string is more than the number of 0's. For example 1, 101, 110101 are *dense*, but 10, 1001, 100001 are not *dense*.

Given a binary string of length  $n$ , design an  $O(n \log n)$  time algorithm to compute the number of *dense* sub-strings of the given string. For example, given 10101, the answer is 6.

2. Given a binary string of length  $n$ , design a linear time algorithm to compute the length of the largest *dense* sub-string of the given string.
3. Given a binary string of length  $n$ , design a linear time algorithm to compute the length of the largest sub-string which contains equal number of 0's and 1's.
4. Given a binary string  $S$  of length  $n$ , design a linear time algorithm to compute  $k$ , such that the number of 0's in  $S[0..k]$  is equal to number of 1's in  $S[k+1..n-1]$ .
5. Write a linear time iterative algorithm to reverse a linked list.
6. Write a linear time algorithm to decide if a linked list contains a cycle or not.
7. Given a linked list containing a cycle, write a linear time algorithm to delete the cycle.
8. Design a linear time algorithm to decide if a given sequence of numbers is a stack sequence.
9. You are given an array of integers, there is a sliding window of size at most  $k$  which is moving from left to right. You can only see at most  $k$  numbers in the window. Each time the sliding window moves right by one position. Design an linear time algorithm to compute the maximum in each window.
10. Given a array  $A$  of numbers , write a linear time algorithm to compute array  $B$ , such that  $B[i] = j, j$  is the smallest  $j > i$  such that  $A[j] < A[i]$ .  $B[i] = n$  if all the numbers to the right of  $A[i]$  are greater than or equal to  $A[i]$ .
11. Given a array  $A$  of numbers , write a linear time algorithm to compute array  $B$ , such that  $B[i] = j, j$  is the largest  $j < i$  such that  $A[j] > A[i]$ .  $B[i] = -1$  if all the numbers to the left of  $A[i]$  are less than or equal to  $A[i]$ .
12. Given a array  $A$  of numbers , write an  $O(n \log n)$  time algorithm to compute array  $B$ , such that  $B[i] = j, j$  is the smallest  $j$  such that  $A[j] < A[i]$ .  $B[i] = -1$  if all the numbers to the left of  $A[i]$  are greater than or equal to  $A[i]$ .

13. Given a array A of numbers , write an  $O(n \log n)$  linear time algorithm to compute array B, such that  $B[i] = j, j$  is the largest  $j$  such that  $A[j] > A[i]$ .  $B[i] = n$  if all the numbers to the right of  $A[i]$  are less than or equal to  $A[i]$ .
14. Given a sequence of n numbers, representing the stock prices of a stock on different days, design a linear time algorithm to compute the maximum profit that you can make by buying and selling a stock exactly once, you can sell a stock only after you buy it.
15. Given a sequence of n numbers, representing the stock prices of a stock on different days, design a linear time algorithm to compute the maximum profit that you can make by buying and selling a stock exactly once, you can sell a stock exactly  $k$  days after you bought it.
16. Given a sequence of n numbers, representing the stock prices of a stock on different days, design a linear time algorithm to compute the maximum profit that you can make by buying and selling a stock exactly once, you can sell a stock at least  $k$  days after you bought it.
17. Given a sequence of n numbers, representing the stock prices of a stock on different days, design a linear time algorithm to compute the maximum profit that you can make by buying and selling a stock exactly once, you can sell a stock at most  $k$  days after you bought it.
18. Given a sequence of n numbers design a linear time algorithm to compute the length of the maximum sum sub array.
19. Given a sequence of n numbers and an integer k, design a linear time algorithm to compute the length of the maximum sum sub array , whos length is exactly k.
20. Given a sequence of n numbers and an integer k, design a linear time algorithm to compute the length of the maximum sum sub array , whos length is at least k.
21. Given a sequence of n numbers and an integer k, design a linear time algorithm to compute the length of the maximum sum sub array , whos length is at most k.
22. Let  $F(0) = 0, F(1) = 1$  and  $F(n) = (F(n - 1) + F(n - 2)) \% m$ . If  $n < 10^{18}$  and  $m < 10^5$ , write an efficient algorithm to compute  $F(n)$ .
23. Let  $F(0) = 0, F(1) = 1$  and  $F(n) = (F(n - 1) + F(n - 2)) \% m$ . If  $n < 10^{10000}$  and  $m < 10^5$ , write an efficient algorithm to compute  $F(n)$ .
24. Let  $F(0) = 0, F(1) = 1, F(2) = 2$  and  $F(n) = (F(n - 1) + F(n - 2) + F(n - 3) + 1) \% m$ . If  $n < 10^{10000}$  and  $m < 10^5$ , write an efficient algorithm to compute  $F(n)$ .
25. Let  $F(0) = 0, F(1) = 1, F(2) = 2$  and  $F(n) = (2F(n - 1) - 3F(n - 3)) \% m$ . If  $n < 10^{10000}$  and  $m < 10^5$ , write an efficient algorithm to compute  $F(n)$ .