

# **Digital Watermarking and Steganography**

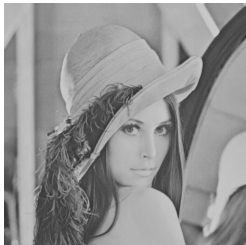
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## **Chapter 9. Robust Watermarking**

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2015

# Valumetric Scaling



$c * 0.8$

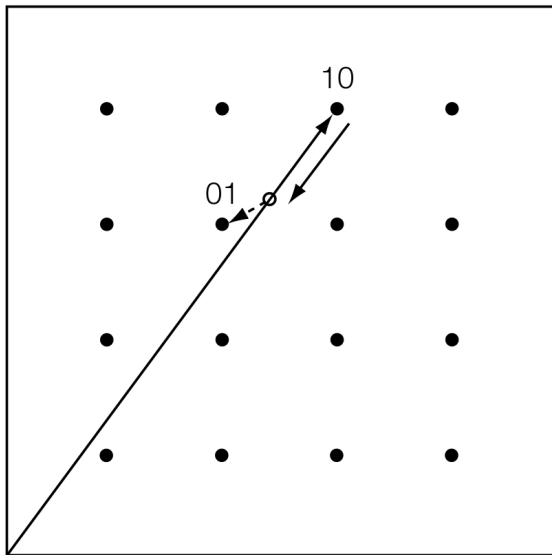


$c * 1.0$

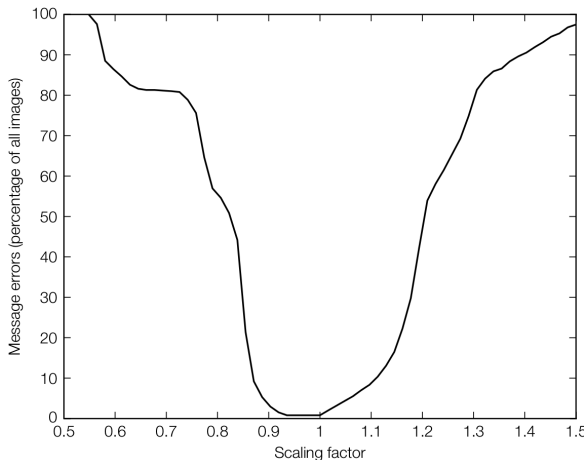


$c * 1.2$

# QIM is not Robust



# Error Illustration



*Valumetric scaling on the E\_LATTICE/D\_LATTICE system.*

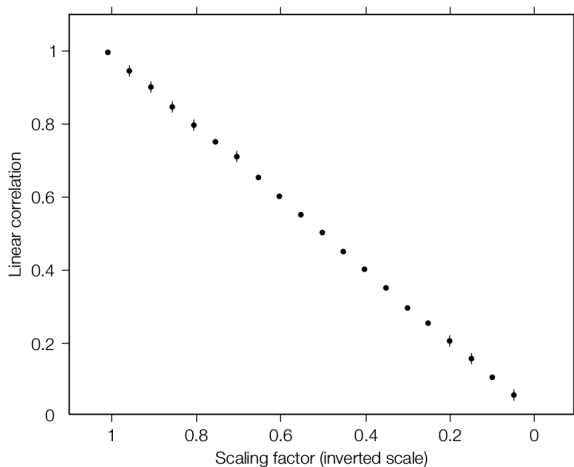
# Reason

$$\begin{aligned}z_{lc}(s) &= (s\mathbf{c}_w) \cdot \mathbf{w}_r \\&= s(\mathbf{c}_w) \cdot \mathbf{w}_r \\&= s \cdot z_{lc}.\end{aligned}$$

Possible solution?

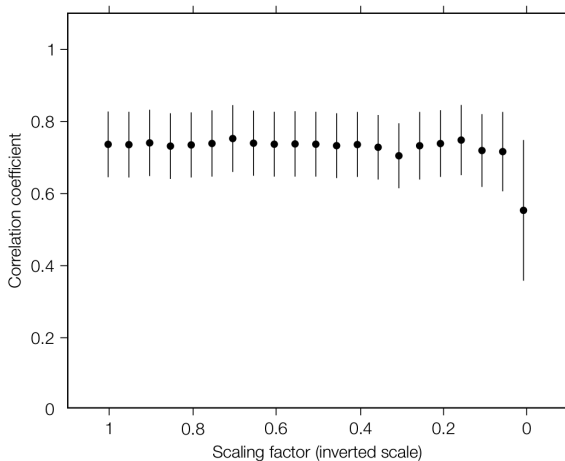
$$\begin{aligned}z_{nc}(s) &= \frac{s\mathbf{c}_w}{\|s\mathbf{c}_w\|} \cdot \mathbf{w}_r \\&= \frac{\mathbf{c}_w}{\|\mathbf{c}_w\|} \cdot \mathbf{w}_r \\&= \cos(\theta(\mathbf{c}_w, \mathbf{w}_r)).\end{aligned}$$

# Linear Correlation



*E\_FIXED\_LC/D\_LC.*

# Correlation Coefficients

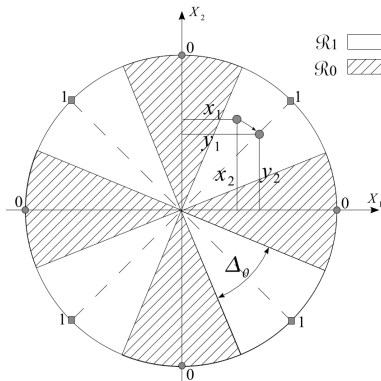


*E\_BLK\_FIXED\_R/D\_BLK\_CC.*

# $z_{nc}$ with Dirty Paper

Angle QIM (Ourique et al. ICASSP 2005.):

- Snap work to the closest “grid angle”.





## 2-Dimensional Case

- Choosing two bases  $\mathbf{X}_1, \mathbf{X}_2$ .
- Get coordinates  $x_1, x_2$ .
- Evaluate the length and angle:

$$r = \sqrt{x_1^2 + x_2^2}, \quad \theta = \arctan(x_2/x_1).$$

- Angle QIM:

$$\theta^Q = Q_{m,\Delta}(\theta) = \left\lfloor \frac{\theta + m\Delta}{2\Delta} \right\rfloor 2\Delta + m\Delta.$$

- Restore:

$$x'_1 = r \cos(\theta^Q), \quad x'_2 = r \sin(\theta^Q).$$

# $L$ -Dimensional Case

- $L$  bases:  $\mathbf{X}_i, i = 1, \dots, L$ .
- $L$  coordinates:  $\mathbf{x}_i, i = 1, \dots, L$ .
- $L - 1$  angles:  $\mathbf{x}_i, i = 1, \dots, L - 1$ .

$$\theta_1 = \arctan(x_2/x_1)$$

$$\theta_i = \arctan \frac{x_{i+1}}{\sqrt{\sum_{k=1}^i x_k^2}}, i = 2, \dots, L - 1.$$

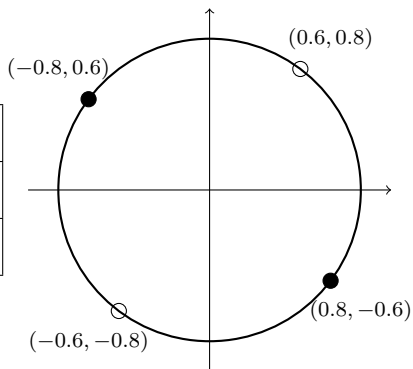
- Restore:

$$x'_1 = r \prod_{k=1}^{L-1} \cos \theta_k^Q$$

$$x'_i = r \sin \theta_{i-1}^Q \prod_{k=i}^{L-1} \cos \theta_k^Q, i = 2, \dots, L.$$

# Question: AQIM

	$(\sqrt{5}, 2)$	$(\sqrt{7}, -3)$
0		
1		



*Circle is for 0, dot is for 1.*