Some Significant Steganalysis

Algorithms

LSB Embedding and the Histogram Attack

Giving a relative message length q = m/n:

$$E\{\mathbf{T}_s[2i]\} = (1 - \frac{q}{2})\mathbf{T}_c[2i] + \frac{q}{2}\mathbf{T}_c[2i + 1]$$

$$E\{\mathbf{T}_s[2i + 1]\} = \frac{q}{2}\mathbf{T}_c[2i] + (1 - \frac{q}{2})\mathbf{T}_c[2i + 1].$$

- Ineffective for random work embedding.
- Improvements:
 - Sliding window.
 - ...

Sample Pairs Analysis

A very clever method!

- Use spatial correlation within images.
- More reliable and accurate.

Basic Idea

Giving a sequence of values s_1, s_2, \dots, s_n .

All adjacent pairs

$$\mathcal{P} = \{(u, v) = (s_i, s_{i+1}), 1 \leq i \leq n\}.$$

$$(s_1, s_2), (s_2, s_3), \cdots, (s_{n-1}, s_n).$$

• Partition of \mathcal{P} :

	v%2 = 0	v%2 = 1
u = v	$\mathcal Z$	${\cal Z}$
u < v	\mathcal{X}	\mathcal{Y}
u > v	\mathcal{Y}	\mathcal{X}

Partition of \mathcal{P}

Continue portioning \mathcal{Y} into \mathcal{W}, \mathcal{V} .

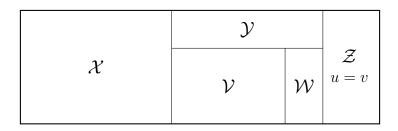
• \mathcal{W} : A small subset of \mathcal{Y} .

$$\{(u=2k, v=2k+1) \lor (u=2k+1, v=2k), k \in \mathbb{Z}\}.$$

 \circ $\mathcal{V} = \mathcal{P} - \mathcal{W}$.

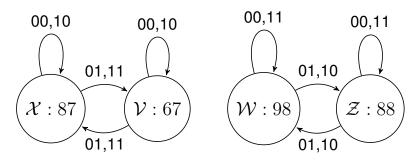
The bin of LSB: W + Z.

Partition of \mathcal{P}



A Finite State Machine

Notice that the **modification** pattern $\pi \in \{00, 01, 10, 11\}$ is not message binary sequence.



Transition Probability

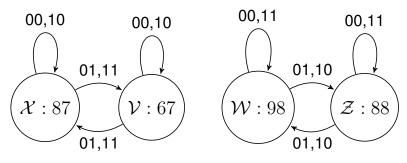
Giving relative message length q, expectation of modification (i.e. 1) is q/2:

$$\rho(00, \mathcal{P}) = \left(1 - \frac{q}{2}\right)^2$$

$$\rho(01, \mathcal{P}) = \rho(10, \mathcal{P}) = \frac{q}{2}\left(1 - \frac{q}{2}\right)$$

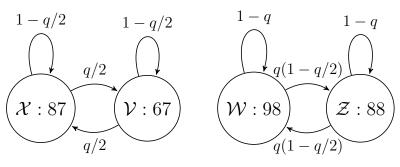
$$\rho(11, \mathcal{P}) = \left(\frac{q}{2}\right)^2.$$

Put Them Together



$$\begin{split} & \rho(00,\mathcal{P}) = \left(1 - \frac{q}{2}\right)^2 \\ & \rho(01,\mathcal{P}) = \frac{q}{2}\left(1 - \frac{q}{2}\right) \\ & \rho(10,\mathcal{P}) = \frac{q}{2}\left(1 - \frac{q}{2}\right) \\ & \rho(11,\mathcal{P}) = \left(\frac{q}{2}\right)^2 \end{split} \Rightarrow \begin{cases} 00,10: & \rho_{00} + \rho_{10} = 1 - q/2 \\ 01,11: & \rho_{01} + \rho_{11} = q/2 \\ 00,11: & \rho_{00} + \rho_{11} = 1 - q \\ 01,10: & \rho_{01} + \rho_{10} = q(1 - q/2) \end{cases}$$

Put Them Together



$$\rho(00, \mathcal{P}) = \left(1 - \frac{q}{2}\right)^{2}$$

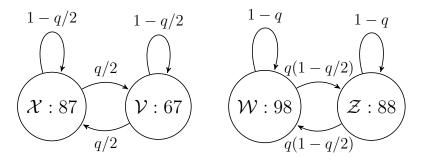
$$\rho(01, \mathcal{P}) = \frac{q}{2}\left(1 - \frac{q}{2}\right)$$

$$\rho(10, \mathcal{P}) = \frac{q}{2}\left(1 - \frac{q}{2}\right)$$

$$\rho(11, \mathcal{P}) = \left(\frac{q}{2}\right)^{2}$$

$$\Rightarrow \begin{cases}
00, 10: & \rho_{00} + \rho_{10} = 1 - q/2 \\
01, 11: & \rho_{01} + \rho_{11} = q/2 \\
00, 11: & \rho_{00} + \rho_{11} = 1 - q \\
01, 10: & \rho_{01} + \rho_{10} = q(1 - q/2)
\end{cases}$$

Put Them Together



Count in and out:

$$\begin{aligned} |\mathcal{X}'| &= |\mathcal{X}|(1 - q/2) + |\mathcal{V}|q/2 \\ |\mathcal{V}'| &= |\mathcal{V}|(1 - q/2) + |\mathcal{X}|q/2 \\ |\mathcal{W}'| &= |\mathcal{W}|(1 - q + q^2/2) + |\mathcal{Z}|q(1 - q/2). \end{aligned}$$

Some Math

To solve q, we have equalities

$$|\mathcal{X}'| = |\mathcal{X}|(1 - q/2) + |\mathcal{V}|q/2$$

$$|\mathcal{V}'| = |\mathcal{V}|(1 - q/2) + |\mathcal{X}|q/2$$

$$\Rightarrow$$

$$|\mathcal{X}'| - |\mathcal{V}'| = (|\mathcal{X}| - |\mathcal{V}|)(1 - p)$$

$$= |\mathcal{W}|(1 - p)$$

$$|\mathcal{W}'| = |\mathcal{W}|(1 - q + q^2/2) + |\mathcal{Z}|q(1 - q/2)$$

$$= |\mathcal{W}|(1 - q)^2 + (|\mathcal{W}| + |\mathcal{Z}|)|q(1 - q/2)$$

$$= |\mathcal{W}|(1 - q)^2 + \gamma q(1 - q/2)$$

$$= (|\mathcal{X}'| - |\mathcal{V}'|)(1 - q) + \gamma q(1 - q/2)$$

Continue

Because $|\mathcal{W}'| = |\mathcal{P}| - |\mathcal{X}'| - |\mathcal{V}'| - |\mathcal{Z}'|$:

$$\begin{split} |\mathcal{P}| - |\mathcal{X}'| - |\mathcal{V}'| - |\mathcal{Z}'| &= \\ (|\mathcal{X}'| - |\mathcal{V}'|)(1 - q) + \gamma q(1 - q/2) \\ \frac{\gamma}{2}q^2 + (|\mathcal{P}| - |\mathcal{X}'| - |\mathcal{V}'| - |\mathcal{Z}'|) &= \\ (|\mathcal{X}'| - |\mathcal{V}'|) - (|\mathcal{X}'| - |\mathcal{V}'|)q + \gamma q \\ \frac{\gamma}{2}q^2 + (|\mathcal{P}| - 2|\mathcal{X}'| - |\mathcal{Z}'|) &= \\ - (|\mathcal{X}'| - |\mathcal{V}'| - \gamma)q \\ \frac{\gamma}{2}q^2 + (|\mathcal{X}'| - |\mathcal{V}'| - \gamma)q + (|\mathcal{P}| - 2|\mathcal{X}'| - |\mathcal{Z}'|) &= 0. \end{split}$$

More Compacted Form

$$0 = \frac{\gamma}{2}q^{2} + (|\mathcal{X}'| - |\mathcal{V}'| - \gamma)q + (|\mathcal{P}| - 2|\mathcal{X}'| - |\mathcal{Z}'|)$$

$$= \frac{\gamma}{2}q^{2} + (|\mathcal{X}'| - |\mathcal{V}'| - |\mathcal{W}'| - |\mathcal{Z}'|)q$$

$$+ (|\mathcal{X}'| + |\mathcal{Y}'| + |\mathcal{Z}'| - 2|\mathcal{X}'| - |\mathcal{Z}'|)$$

$$= \frac{\gamma}{2}q^{2} + (2|\mathcal{X}'| - |\mathcal{P}|)q + (|\mathcal{Y}'| - |\mathcal{X}'|).$$

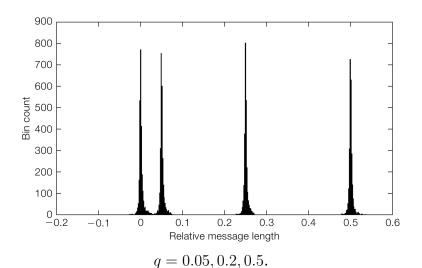
The Solution

• If
$$\gamma = 0$$
, $|\mathcal{X}| = |\mathcal{X}'| = |\mathcal{Y}| = |\mathcal{Y}'| = |\mathcal{P}|/2$.

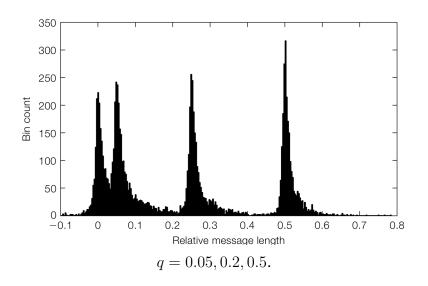
$$0q^2 + 0q + 0 = 0.$$

- If two complex conjugate roots:
 - Taking the real parts.
- If has a negative root:
 - p = 0.

JPEG



Raw Scan



Analysis

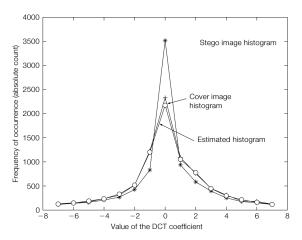
- Noisy has negative influence.
- Estimation for short message is not robust.
- Sample
 - Local is better
 - Thus neighboring pairs.

Extension

- One point: histogram
- Sample pairs.
- Sample more: 2×2 neighboring pixels.

Blind Steganalysis Using Calibration

Shift 4 pixels and re-compress.



In General

$$f_i = ||F_i(J_1) - F_i(J_2)||.$$

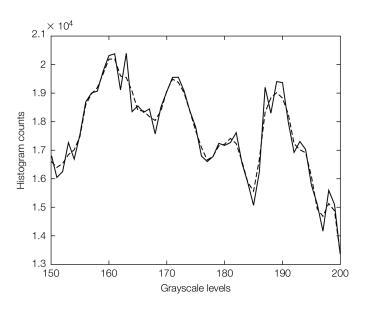
- J_1 : stego JPEG image.
- J₂: shift and re-compress stego JPEG image.
- Find efficient F_i or training.

In Spatial Domain

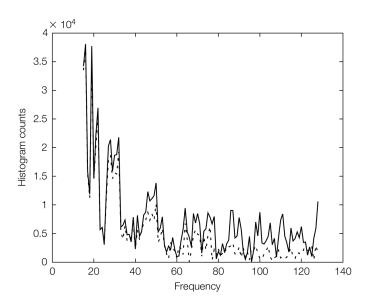
Just using different feature.

- Steganographic method: adding noise.
- Smooth the work a little bit and check the difference.

Illustration



Illustration



A Basic Method

Compute the noise residual from a smoother *F*:

$$\mathbf{r} = \mathbf{s} - F(\mathbf{s}).$$

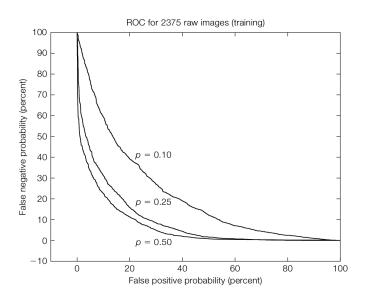
Then use $k = 1, 2, \cdots$ moments as the feature:

$$\mu_k = \sum (\mathbf{r} - \bar{\mathbf{r}})^k.$$

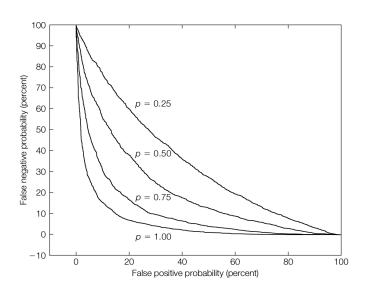
Classification via Fisher linear discriminant.

More details in the book.

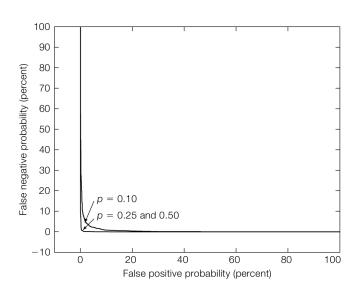
Raw Digital Camera



Raw Scans



JPEG



Analysis

- Noise!
 - It is better to pick noise image as the cover for steganography.