

TP de Especificación

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Algoritmos y Estructuras de Datos I

Grupo: 15

Integrante	LU	Correo electrónico
Mauricio David Toranzo	63/20	david-toranzo-@hotmail.com
Matias Federico Sarmiento	741/18	mfsarmiento@gmail.com
Victor Manuel Asmad Murga	760/19	victorasmad2@gmail.com
Marco Antonio Avila Tapia	412/20	marco6267@hotmail.com



Facultad de Ciencias Exactas y Naturales

Universidad de Buenos Aires

Ciudad Universitaria - (Pabellón I/Planta Baja) Intendente Güiraldes 2610 - C1428EGA Ciudad Autónoma de Buenos Aires - Rep. Argentina

$$\label{eq:fax: problem} \begin{split} \text{Tel/Fax: (++54 +11) } & 4576\text{-}3300 \\ \text{http://www.exactas.uba.ar} \end{split}$$

1. Ejercicios - Primera Parte

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pred esValido (t : Toroide) {
(\forall i: \mathbb{Z})((0 \le i < |t| \land |t| \ge 3) \longrightarrow_L (|t[i]| \ge 3 \land |t[0]| = |t[i]|))
    pred toroideMuerto (t : Toroide) {
(\forall i : \mathbb{Z})((\forall j : \mathbb{Z})((0 \le i < |t| \land_L 0 \le j < |t[i]|) \longrightarrow_L (t[i][j] = \text{false})))
    pred posicionesVivas (t : Toroide, vivas: seq\langle \mathbb{Z}x\mathbb{Z}\rangle) {
\neg toroideMuerto(t) \land |vivas| > 0 \land (\forall i : \mathbb{Z})((0 \le i < |vivas|) \land
((0 \le vivas[i]_0 < |t| \land_L 0 \le vivas[i]_1 < |t[0]|) \longrightarrow_L (t[vivas[i]_0][vivas[i]_1] = \text{true})))
    aux densidadPoblacion (t : Toroide) : \mathbb{Z} =
(\sum_{i=0}^{|t|-1}(\sum_{j=0}^{|t[i]|-1}if(t[i][j]=\text{true})\ then\ 1\ else\ 0\ fi))/(|t|*|t[0]|) ;
    aux cantVecinosVivos (t : Toroide, f : \mathbb{Z}, c : \mathbb{Z}) : \mathbb{Z} =
(\sum_{i=f-1}^{f+1}(\sum_{j=c-1}^{c+1}if(i\neq f \land j\neq c \land (t[i\ mod\ |t|][j\ mod\ |t[0]|]=\mathrm{true}))\ then\ 1\ else\ 0\ fi));
    pred evolucionDePosicion (t : Toroide, posicion : \mathbb{Z}x\mathbb{Z}) {
0 \leq posicion_0 < |t| \land 0 \leq posicion_1 < |t[0]| \land
if t[posicion_0][posicion_1] then 2 \leq cantVecinosVivos(t, posicion_0, posicion_1) \leq 3
else cantVecinosVivos(t, posicion_0, posicion_1) = 3 fi
    pred evolucionToroide (t1 : Toroide, t2 : Toroide) {
|t1| = |t2| \wedge |t1[0]| = |t2[0]| \wedge_L
(\forall i: \mathbb{Z})(0 \leq i < |t1| \land_L (\forall j: \mathbb{Z})(0 \leq j < |t1[0]| \longrightarrow_L (evolutionDePosition(t1, (i, j)) = t2[i][j])))
2.
         Ejercicios - Segunda Parte
proc evolucionMultiple (in t: Toroide, in k: \mathbb{Z}, out result: Toroide) {
          Pre \{esValido(t) \land k > 0\}
          Post \{coincideTamanio(t, result) \land esKesimaEvolucion(t, k, result)\}
```

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 \begin{array}{l} \text{proc evolucionMultiple (in t: } \textit{Toroide, in k: } \mathbb{Z}, \text{ out result: } \textit{Toroide)} \  \, \\ \text{Pre } \{esValido(t) \land k > 0\} \\ \text{Post } \{coincideTamanio(t, result) \land esKesimaEvolucion(t, k, result)\} \\ \\ \text{Proc esPeriodico (in t: } \textit{Toroide, inout p: } \mathbb{Z}, \text{ out result: Bool)} \  \, \\ \text{Pre } \{esValido(t) \land p > 0\} \\ \text{Post } \{result = \text{true} \leftrightarrow (\exists k : \mathbb{Z})(k > 0 \land_L \ (esKesimaEvolucion(t, k, t) \land p = k))\} \\ \\ \text{Proc primosLejanos (in t1: } \textit{Toroide, in t2: } \textit{Toroide, out primos: Bool)} \  \, \\ \text{Pre } \{coincideTamanio(t1, t2)\} \\ \text{Post } \{primos = \text{true} \leftrightarrow (\exists k : \mathbb{Z}) \\ (k > 0 \land_L \ ((esKesimaEvolucion(t1, k, t2)) \lor (esKesimaEvolucion(t2, k, t1))))\} \\ \\ \} \\ \end{array}
```

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proc seleccionNatural (in ts: seq\langle Toroide \rangle, out res: \mathbb{Z}) {
        Pre \{|ts| > 0 \land noHayToroidesInmortales(ts)\}
        Post \{0 \le res < |ts| \land_L toroideTardaMasEnMorir(ts, res)\}
}
proc fusionar (in t1: Toroide, in t2: Toroide, out res: Toroide) {
        Pre \{coincideTamanio(t1, t2)\}
        Post \{coincideTamanio(t1, res) \land contieneVivas(t1, t2, result)\}
proc vistaTrasladada (in t1: Toroide, in t2: Toroide, out res: Bool) {
        Pre \{coincideTamanio(t1, t2)\}
        Post \{res = true \leftrightarrow esTraslado(t1, t2)\}\
}
proc menorSuperficieViva (in t: Toroide, out res: \mathbb{Z}) {
        Pre \{esValido(t) \land \neg toroideMuerto(t)\}
        Post \{0 < res \leq superficie(t) \land_L esLaMenorSuperficie(t, res)\}
}
proc enCrecimiento (in t: Toroide, out res: Bool) {
        Pre \{esValido(t) \land \neg toroideMuerto(t)\}
        Post \{res = true \leftrightarrow (\exists tEvo, tMenor : Toroide)(
            coincideTamanio(t, tEvo) \land coincideTamanio(t, tMenor) \land
            esTraslado(t, tMenor) \land estaCreciendo(t, tMenor, tEvo))
}
```

3. Funciones y Predicados Auxiliares:

```
pred coincideTamanio (t:toroide, tAux:toroide) { esValido(t) \land esValido(tAux) \land |t| = |tAux| \land_L |t[0]| = |tAux[0]| \} pred esKesimaEvolucion (t:toroide, k:Z, result: toroide) { (\exists ts: seq < toroide >)  (|ts| = k+1 \land_L ts[0] = t \land ts[k] = result \land (\forall i: \mathbb{Z})  (0 \le i < |ts| - 1 \longrightarrow_L evolucionToroide(ts[i], ts[i+1]))) \} pred noHayToroidesInmortales (ts: seq\langle Toroide\rangle) { (\forall i: \mathbb{Z})(0 \le i < |ts| \longrightarrow_L esValido(ts[i]) \land (\exists k: \mathbb{Z})(k > 0 \land_L muerteEnTicks(ts[i], k))) \} pred toroideTardaMasEnMorir (ts: seq\langle Toroide\rangle, res: \mathbb{Z}) { (\exists k: \mathbb{Z})(k > 0 \land_L (\forall i: \mathbb{Z})(0 \le i < |ts| \land_L i \ne res \longrightarrow_L  (\exists w: \mathbb{Z})(w > 0 \land k > w \land muerteEnTicks(ts[res], k) \land muerteEnTicks(ts[i], w)))) \} pred muerteEnTicks (t:toroide, k:\mathbb{Z}) { (\exists tm: toroide)(coincideTamanio(t, tm) \land toroideMuerto(tm) \land esKesimaEvolucion(t, k, tm)) \}
```

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pred contieneVivas (t1:toroide, t2:toroide, result:toroide) {
(\forall i: \mathbb{Z})(0 \leq i < |t1| \land_L (\forall j: \mathbb{Z})(0 \leq j < |t1[i]| \longrightarrow_L (result[i][j] = \text{true} \leftrightarrow (t1[i][j] = \text{true} \land
t2[i][j] = true))))
    pred esTraslado (t1:toroide, t2:toroide) {
(\exists x, y : \mathbb{Z})(0 \le x < |t1| \land_L 0 \le y < |t1[0]| \land (\forall i, k : \mathbb{Z})(0 \le i, k < |t1| \land_L
(\forall j, l : \mathbb{Z})(0 \le j, l < |t1[0]| \longrightarrow_L t2[i][j] = t1[(k+x) \ mod \ |t|][(l+y) \ mod \ |t[0]|])))
    pred esLaMenorSuperficie (t:Toroide, res:Z) {
(\exists ts : seg\langle Toroide \rangle)(esListaDeTraslados(ts, t) \land 
(\exists \ tMenor : Toroide)(tMenor \in ts \land )
(\forall tItem \in ts)(tItem \neq tMenor \longrightarrow_L noHaySuperficieMasChica(res, tItem)))))
    pred noHaySuperficieMasChica (\sup \mathbb{Z}, t:Toroide) {
(\exists matriz : seq\langle seq\langle Bool\rangle))(esValidaYEstaContenida(matriz, t) \land sup \leq superficie(matriz)))
    pred esValidaYEstaContenida (mat:seq\langle seq\langle \mathsf{Bool}\rangle\rangle, t:Toroide) {
(0 \le |mat| \le |t| \land 0 \le |mat[0]| \le |t[0]|) \land_L mismaCantVivas(t, mat) \land
(\exists x, y : \mathbb{Z})(0 \le x < |t| \land_L 0 \le y < |t[0]| \land (\forall i : \mathbb{Z})(0 \le i < |mat| \land_L)
(\forall j: \mathbb{Z})(0 \leq j < |mat[i]| \longrightarrow_L mat[i][j] = t[(i+x)mod|t|][(j+y)mod|t[0]|])))\}
    pred esListaDeTraslados (ts:seg\langle toroide \rangle, t:toroide) {
(|ts| > 0 \land_L sinRepetidos(ts)) \land (\forall i : \mathbb{Z})(0 \le i < |ts| \longrightarrow_L
esValido(t) \land coincideTamanio(ts[i], t) \land esTraslado(t, ts[i]))}
    pred sinRepetidos (ts:seq\langle Toroide\rangle) {
(\forall i : \mathbb{Z})(0 \le i < |ts| \longrightarrow_L (\forall j : \mathbb{Z})((0 \le j < |ts| \land i \ne j) \longrightarrow_L ts[i] \ne ts[j]))
    aux cantVivas (\text{m}:seq\langle seq\langle \mathsf{Bool}\rangle\rangle): \mathbb{Z} = (\sum_{i=0}^{|m|-1} (\sum_{j=0}^{|m[0]|-1} \mathsf{if}\ m[i][j]\ \mathsf{then}\ 1\ \mathsf{else}\ 0\ \mathsf{fi}));
    aux superficie (m:seq\langle seq\langle \mathsf{Bool}\rangle\rangle): \mathbb{Z} = |m|*|m[0]|;
    pred mismaCantVivas (t:Toroide, m:seq\langle seq\langle Bool\rangle\rangle) {cantVivas(t) = cantVivas(m)}
    pred estaCreciendo (tMenor:Toroide, tEvo:Toroide) {
(\exists k : \mathbb{Z})(0 < k \leq superficie(tMenor) \land_L esLaMenorSuperficie(tMenor, k) \land
(evolucionToroide(tMenor, tEvo) \land \neg toroideMuerto(tEvo)) \land 
(\exists j : \mathbb{Z})(0 < j \leq superficie(tMenor) \land j > k \land_L esLaMenorSuperficie(tEvo, j)))
```

4. Decisiones tomadas

Usamos la primer fila en nuestras funciones y predicados púes los toroides son matrices (todas sus filas tienen el mismo largo y sus columnas el mismo alto), por lo tanto no cambia si usamos la primer o la i-esima fila.