Relatório Lista1

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Implementação:

Estratégias:

Foi implementado 2 classes, Search que possui os algoritmos e mantém alguns atributos de interesse como listas, State, que seriam os nodos, possuindo atributos como custo, valor da heurística, e o estado que é representado como um vetor de int, além de outros valores adicionados por conveniência. State possui uma função que seria succ para gerar uma lista dos sucessores e Search possui todos algoritmos, onde idfs e idastar não compartilham a função recursiva, sendo a que retorna uma tupla a do idastar, além de um arquivo de util com a heurística e um parse.

A estratégia era implementar um estado que funcionasse de forma dinâmica e aceitasse qualquer tamanho de entrada. Inicialmente uma string, mas acabou sendo trocada para um vetor de int, o intuito era evitar o problema da representação de valores na string, o que poderia ter sido evitado mudando valores como 10 para A, mesmo assim ficou mais fácil mexer no vetor. As funções de busca então controlariam as listas e chamariam a função de sucessor e todas outras questões relacionadas com a busca como tempo. Eventualmente tivemos que fazer uma busca especializada para o problema com 15 tiles, mas o algoritmo normal também aceitaria, embora pudesse demorar ou até estourar a memória normalmente.

Desafios:

Um deles foi para calcular a média das heurísticas e o número de nodos expandidos, pois era difícil saber onde contar eles, também alguns detalhes do pseudo-código, na hora de passar, que fazia com que o algoritmo abrisse um número diferente de nodos

Os testes foram realizados em um sistema com processador ryzen 5 5600g 12 cores, 16gb ram e com o sistema operacional Ubuntu 22.04.3 LTS

8_puzzle_instances médias:

	avg_expande d_nodes	avg_soluti on_cost	avg_time	avg_avg_h_cost	avg_initial_h_c ost
astar	895.0	22.16	0.0057218430999999995	10.027754223930009	13.88
bfs	81459.54	22.16	0.6109954079	0.0	13.88
gbfs	392.42	140.52	0.0024713955999999997	6.89304647844	13.88
idastar	2373.03	22.16	0.007692446400000002	10.432846666690002	13.88
idfs	2578290.56	22.16	6.848442800199998	0.0	13.88

8 puzzle instances:

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	astar	bts	gors	idastar	lats
			•		1

562718340	835,22,0.005777300,	70436,22,0.455	579,156,0.004101040	2631,22,0.008578180	809224,22,2.1487
	9.082437276,12	174830,0,12	,7.008771930,12	,9.777978339,12	78080,0,12
532871406	1024,23,0.00659114	98412,23,0.576	437,187,0.002699700	3276,23,0.010294330	1659716,23,4.415
	0,10.066706021,15	042600,0,15	,6.869509044,15	,10.598317176,15	463520,0,15
107524386	72,17,0.000663250,9 .150793651,13	11718,17,0.073 638940,0,13	430,189,0.002650400 ,6.610747051,13		56332,17,0.15413 5730,0,13
364280571	953,25,0.005644950,	134664,25,0.92	466,207,0.002893960	2720,25,0.008614460	3832745,25,10.31
	11.678321678,17	3698860,0,17	,6.945454545,17	,11.781368398,17	7531870,0,17
061742385	91,16,0.000815640,6	5209,16,0.0292	16,16,0.000086570,5.	165,16,0.000556050,	20305,16,0.05351
	.725609756,10	98980,0,10	500000000,10	7.137809187,10	1270,0,10
038214765	652,22,0.003866600, 9.371818182,12	59830,22,0.414 840030,0,12	407,152,0.002486300 ,6.590846047,12	· '	572929,22,1.5848 68650,0,12
082156734	350,22,0.002176010, 10.439522998,14	71614,22,0.608 393130,0,14	422,168,0.002536880 ,6.612600536,14		840836,22,2.2790 56490,0,14
502648173	612,21,0.003695880, 9.811357074,11	42704,21,0.299 410340,0,11	96,27,0.000645020,8. 054216867,11		336804,21,0.9139 23860,0,11
308412675	232,17,0.001518660, 7.862500000,7	10486,17,0.060 601750,0,7	576,87,0.003376570, 6.730019493,7		48030,17,0.13171 2030,0,7
726315804	177,21,0.001052790,	55230,21,0.399	634,119,0.003867100	611,21,0.001922630,	523656,21,1.4185
	10.827118644,13	892120,0,13	,7.052537845,13	11.501489573,13	72760,0,13
247036815	511,23,0.003060970,	86288,23,0.609	90,57,0.000690500,6.	724,23,0.002317180,	1183127,23,3.159
	9.976553341,15	794280,0,15	809815951,15	11.724137931,15	671300,0,15
216043758	1037,23,0.00646830	87902,23,0.624	560,141,0.003280600	1659,23,0.005247610	1229083,23,3.302
	0,10.386350492,11	138630,0,11	,6.932391524,11	,10.909418982,11	320960,0,11
128037564	197,19,0.001434710,	24271,19,0.160	83,47,0.000603440,5.	372,19,0.001220810,	144153,19,0.3895
	8.389380531,13	408360,0,13	891156463,13	9.075079872,13	22580,0,13
148276035	697,22,0.004167770,	67445,22,0.529	502,146,0.002989440	1420,22,0.004562110	726908,22,1.9543
	9.280956447,14	322740,0,14	,6.734304933,14	,9.659368421,14	46610,0,14
502168734	239,19,0.001629180,	21294,19,0.143	66,39,0.000500450,6.	465,19,0.001534700,	119854,19,0.3258
	7.905707196,13	268930,0,13	134453782,13	8.212311558,13	56350,0,13
621504387	1622,22,0.01029312	67976,22,0.470	501,146,0.002950870	2130,22,0.006812850	746437,22,1.9882
	0,9.725906926,10	452870,0,10	,6.698768197,10	,9.635014006,10	49770,0,10
180452673	315,20,0.002303650, 8.873394495,10	30932,20,0.203 033390,0,10	81,44,0.000572880,6. 510638298,10		201422,20,0.5372 68260,0,10
764813502	30,21,0.000246260,1	51926,21,0.360	46,37,0.000281630,7.	71,21,0.000228230,1	463439,21,1.2300
	0.326923077,19	934520,0,19	869047619,19	2.972972973,19	15880,0,19
187504236	373,22,0.002140140, 10.561797753,18	74010,22,0.524 219310,0,18	386,160,0.002257060 ,6.806404658,18		880730,22,2.3545 65660,0,18
280417563	550,22,0.003322270, 10.553030303,16	57200,22,0.421 173980,0,16	429,190,0.002783250 ,6.808201058,16		529433,22,1.4105 69060,0,16
781362450	34,16,0.000331220,8	6175,16,0.0459	540,132,0.003296920	27,16,0.000100490,9.	25389,16,0.06776
	.229508197,14	98990,0,14	,6.774428274,14	636363636,14	2250,0,14
147362085	118,16,0.000795700,	4890,16,0.0271	453,166,0.002753890	76,16,0.000255480,8.	18803,16,0.05017
	8.475490196,10	73470,0,10	,6.643750000,10	563492063,10	7680,0,10
523471806	1449,25,0.00867077	128087,25,0.87	464,181,0.002823530	2805,25,0.008969720	3233556,25,8.646
	0,10.864540182,15	0836120,0,15	,6.876073620,15	,11.128685173,15	742500,0,15
513264780	873,22,0.006001430, 10.083901774,14	59140,22,0.423 869070,0,14	651,198,0.003910080 ,7.221929825,14		559966,22,1.4959 63990,0,14
102586473	808,23,0.005498970,	86044,23,0.641	406,189,0.002578760	1666,23,0.005545760	1161412,23,3.105
	9.784356725,13	694360,0,13	,6.628453039,13	,10.285560345,13	314230,0,13
476052381	1167,25,0.00745957 0,10.505646817,15	124428,25,0.90 0360320,0,15	423,187,0.002621040 ,6.837365591,15		3012022,25,8.017 030700,0,15

582176304	308,21,0.002169490, 9.424761905,15	55828,21,0.423 331850,0,15	453,203,0.002796680 ,6.817164179,15		533665,21,1.4745 69220,0,15
302614578	41,13,0.000327210,6	1904,13,0.0121	17,15,0.000213400,5.	100,13,0.000528990,	6472,13,0.01777
	.080000000,7	24080,0,7	382352941,7	6.928176796,7	4540,0,7
201753864	533,23,0.003169080,	89286,23,0.666	405,165,0.002404430	1609,23,0.005583930	1258485,23,3.382
	11.037078652,13	764860,0,13	,6.697771588,13	,11.262020127,13	661850,0,13
810537246	346,24,0.002278700,	96167,24,0.692	542,140,0.003329080	225,24,0.000712450,	1506581,24,4.017
	11.500000000,16	919520,0,16	,6.953271028,16	14.002777778,16	059370,0,16
026547138	929,24,0.007748320,	108997,24,0.79	135,38,0.000884470,	1820,24,0.005790730	2082556,24,5.668
	10.288535032,14	4758980,0,14	8.691304348,14	,11.523000000,14	021220,0,14
450172386	117,16,0.000937070, 8.699507389,12	6800,16,0.0420 01550,0,12	67,34,0.000399250,7. 914529915,12		28816,16,0.07838 4000,0,12
063582174	26,18,0.000192670,9 .020833333,16	12237,18,0.069 360470,0,16	452,194,0.002697190 ,6.759051186,16		57963,18,0.15563 8070,0,16
148075263	666,23,0.003985530,	91221,23,0.745	432,195,0.002664930	1500,23,0.004798960	1339032,23,3.614
	10.135992747,13	688390,0,13	,6.809210526,13	,10.929971989,13	152940,0,13
150843276	1734,26,0.01093063 0,10.785144047,14	146642,26,1.02 1040220,0,14	521,162,0.003279990 ,6.914502165,14		5227219,26,14.05 8819870,0,14
236810547	1824,27,0.01209903	166169,27,1.35	111,79,0.000969830,	5873,27,0.018461940	10582097,27,28.5
	0,12.141566265,17	5843940,0,17	7.827411168,17	,12.113548924,17	31232510,0,17
160738452	231,22,0.001378900, 11.418181818,14	61999,22,0.544 719690,0,14	590,98,0.003698980, 6.833491912,14		618550,22,1.6711 47330,0,14
843165072	1807,26,0.01153206 0,10.707727873,14	149038,26,0.91 5776710,0,14	549,148,0.003416840 ,6.898773006,14		5647709,26,15.25 2149800,0,14
382751064	655,22,0.003952760,	66394,22,0.592	447,184,0.002826540	2349,22,0.007558360	707091,22,1.9112
	9.455454545,12	687000,0,12	,6.728192162,12	,9.770907248,12	18910,0,12
723648105	2298,25,0.01489761 0,10.224357310,13	134964,25,0.94 3810610,0,13	460,211,0.003212060 ,6.956790123,13		3906491,25,10.55 6317570,0,13
312408576	76,14,0.000455960,7	3528,14,0.0222	394,140,0.003776930	125,14,0.000444540,	13166,14,0.03654
	.451851852,8	30950,0,8	,6.472103004,8	7.921658986,8	5660,0,8
853126407	786,25,0.004583850, 11.269619270,19	141058,25,0.97 9598520,0,19	65,45,0.000616760,7. 798319328,19		4826279,25,13.28 8337330,0,19
208613475	609,21,0.003789450,	51334,21,0.392	510,155,0.003059780	1193,21,0.003860090	445186,21,1.2007
	9.228035538,11	573120,0,11	,6.728982301,11	,9.671307807,11	42440,0,11
367128450	2231,26,0.01440118	147235,26,1.06	525,222,0.003259850	9239,26,0.029695030	5301125,26,14.30
	0,10.650430571,16	4540900,0,16	,6.770652174,16	,10.244678786,16	0915820,0,16
036128475	1757,24,0.01128289	96629,24,0.863	533,130,0.003296520	2256,24,0.007266010	1521264,24,4.078
	0,9.851374279,14	571510,0,14	,6.888771186,14	,10.434656085,14	214050,0,14
486507132	299,24,0.001759520,	117820,24,0.84	416,184,0.002603810	626,24,0.002069510,	2550556,24,6.914
	11.503006012,20	9787600,0,20	,6.963464141,20	13.157213930,20	213290,0,20
720186345	41,18,0.000317700,9 .959459459,14	12721,18,0.078 495500,0,14	19,18,0.000236750,7. 472222222,14		60744,18,0.16409 6830,0,14
407132586	543,23,0.003264660,	82402,23,0.581	428,181,0.002505530	1145,23,0.003705690	1071876,23,2.878
	10.689502762,15	253320,0,15	,6.787598945,15	,11.042925278,15	040880,0,15
143058762	438,21,0.002788170,	55950,21,0.452	552,149,0.003399920	1201,21,0.003989430	542261,21,1.4801
	10.062078273,11	341890,0,11	,6.852342159,11	,10.725062035,11	30210,0,11
136584027	2864,28,0.01887933	170358,28,1.12	461,198,0.002905590	5557,28,0.019452000	13426501,28,35.8
	0,12.255917160,16	8757970,0,16	,7.300370828,16	,12.401424658,16	79532620,0,16
316408752	221,20,0.001396040,	41346,20,0.480	496,174,0.003017400	730,20,0.002453830,	323493,20,0.8562
	9.784974093,12	499010,0,12	,7.079128440,12	9.972016461,12	46220,0,12
805143726	2849,27,0.01935542 0,11.071413435,15	163708,27,1.15 6549400,0,15	88,49,0.000635600,7. 538961039,15		9617303,27,25.19 0685790,0,15

102873465	179,19,0.001080030,	25948,19,0.334	601,101,0.003537970	661,19,0.002268880,	160297,19,0.4297
	8.827922078,11	687990,0,11	,6.789915966,11	8.786607143,11	15310,0,11
581473260	1075,26,0.00653643 0,11.579865017,16	146431,26,0.95 2611110,0,16	452,206,0.002853680 ,7.279040404,16		5150682,26,13.51 8834390,0,16
641203785	177,18,0.001052190, 8.581168831,12	16644,18,0.103 383470,0,12	560,132,0.003418650 ,6.863911290,12		86884,18,0.22813 8670,0,12
617483520	752,24,0.004599580,	113398,24,0.86	43,36,0.000392040,7.	2440,24,0.007980160	2296791,24,6.159
	10.091699605,16	8470550,0,16	33333333333,16	,10.669041769,16	953290,0,16
015387642	182,18,0.001286130, 8.186495177,8	12763,18,0.076 409170,0,8	480,180,0.002815810 ,6.946745562,8		60654,18,0.16473 8040,0,8
782643015	1355,24,0.00823544	102477,24,0.72	459,216,0.002861700	2316,24,0.007501250	1715624,24,4.527
	0,10.085322723,12	5984110,0,12	,7.028290283,12	,10.876103896,12	848620,0,12
608743521	205,23,0.001573360,	91593,23,0.770	80,55,0.000559360,7.	272,23,0.000929650,	1336827,23,3.613
	11.060344828,17	493380,0,17	758865248,17	13.210161663,17	670200,0,17
540762831	712,24,0.004259840,	116022,24,0.91	68,46,0.000399260,6.	3401,24,0.010893850	2536222,24,6.941
	10.585833333,16	9741690,0,16	628099174,16	,10.829941603,16	123540,0,16
561870243	1421,27,0.00864712	170975,27,1.33	525,219,0.003096040	9544,27,0.030116120	15171649,27,41.4
	0,12.022785899,19	0976820,0,19	,6.796517954,19	,11.501880778,19	82851260,0,19
167420358	2186,25,0.01397457	132375,25,1.02	401,153,0.002485190	8845,25,0.028631020	3587527,25,9.884
	0,9.916120219,13	9090510,0,13	,6.597475456,13	,9.669585129,13	791510,0,13
536472108	168,21,0.000997280,	43631,21,0.327	632,195,0.003892350	360,21,0.001302760,	344582,21,0.9311
	10.681818182,15	475080,0,15	,7.222924188,15	10.371859296,15	52750,0,15
087426135	39,22,0.000265100,1	61343,22,0.492	416,188,0.002596900	103,22,0.000421290,	599226,22,1.6279
	2.014705882,18	614170,0,18	,6.955223881,18	13.398773006,18	30880,0,18
720543861	4038,28,0.02760509	173107,28,1.30	496,210,0.003014690	11359,28,0.03609531	15073854,28,40.3
	0,11.154131986,14	6448940,0,14	,7.478857143,14	0,11.551142690,14	45842700,0,14
530671824	90,20,0.001606030,9 .616883117,16	37323,20,0.451 298220,0,16	20,20,0.000104700,7. 916666667,16		277227,20,0.7952 87000,0,16
572836401	2905,27,0.01799595	166627,27,1.05	659,129,0.004024300	8302,27,0.025836850	10843669,27,29.3
	0,10.862562189,17	2045230,0,17	,7.118803419,17	,11.225801760,17	20440890,0,17
378146502	2301,27,0.01422164	165544,27,1.17	474,197,0.002957380	6762,27,0.021395970	10295974,27,26.8
	0,11.877160817,15	2782640,0,15	,6.955847255,15	,11.858743390,15	02639120,0,15
745863201	698,25,0.004168870, 10.871050384,19	136365,25,0.97 3619150,0,19	62,41,0.000472190,7. 633928571,19		4095213,25,10.57 0038040,0,19
041825376	2190,24,0.01372380	101428,24,0.68	423,170,0.002469160	3944,24,0.012690740	1665813,24,4.266
	0,9.485266288,10	1980580,0,10	,6.562248996,10	,9.623691794,10	372930,0,10
517236840	936,24,0.005631120,	99337,24,0.746	514,158,0.003189820	899,24,0.002915800,	1583030,24,4.062
	11.838396897,16	288420,0,16	,6.832969432,16	11.516891892,16	575990,0,16
634821570	238,22,0.001666450,	69657,22,0.504	394,166,0.002449820	868,22,0.002810000,	792904,22,2.0539
	9.926289926,16	233200,0,16	,6.625000000,16	10.504485852,16	86070,0,16
201576483	3038,27,0.01878675	169153,27,1.31	420,181,0.002604020	14476,27,0.04804666	12496979,27,32.4
	0,10.956961523,15	4632180,0,15	,6.912634409,15	0,10.902895657,15	71673910,0,15
780631254	1632,26,0.00979708 0,10.818418121,18	146614,26,1.22 8414500,0,18	410,178,0.002555820 ,6.706206897,18	, ,	5225955,26,13.44 9717040,0,18
624370518	4306,25,0.02908228 0,10.300276625,11	136769,25,1.06 2949900,0,11	386,175,0.002415160 ,6.514577259,11		4088312,25,10.60 2118040,0,11
754836021	739,26,0.004392980,	144168,26,1.12	448,176,0.002741270	1631,26,0.005250410	4873453,26,12.62
	11.903624382,20	7060060,0,20	,6.877525253,20	,11.602259887,20	3636830,0,20
384571062	382,20,0.002451130, 9.364353312,14	32178,20,0.272 353180,0,14	389,164,0.002412160 ,6.535455861,14		214527,20,0.5534 64010,0,14
562871034	2084,26,0.01296096 0,10.702232531,16	149505,26,1.14 0443320,0,16	466,194,0.002898160 ,6.904126214,16		5735592,26,15.08 4778740,0,16

324658071	99,16,0.000615160,7	6810,16,0.0561	453,194,0.002804990	166,16,0.000657040,	28881,16,0.07698
	.528409091,10	18690,0,10	,6.616149068,10	8.810344828,10	1450,0,10
751684203	2764,27,0.01712391	165286,27,1.31	442,193,0.002722640	7986,27,0.025369870	10128430,27,27.2
	0,11.431719023,17	6535180,0,17	,6.836550837,17	,11.354103574,17	87612160,0,17
352081467	428,19,0.002620540,	20088,19,0.145	590,129,0.003601800	490,19,0.001688280,	110829,19,0.2949
	8.660714286,11	427590,0,11	,6.828820116,11	8.291414752,11	36500,0,11
806713524	715,25,0.004313330,	134133,25,1.10	454,197,0.002866400	324,25,0.001107890,	3745531,25,9.920
	13.085197935,21	0047900,0,21	,7.008695652,21	14.170634921,21	619530,0,21
258410637	68,15,0.000584200,7	3471,15,0.0234	57,39,0.000454360,5.	56,15,0.000276520,8.	12608,15,0.03291
	.352459016,11	52250,0,11	575471698,11	010869565,11	6010,0,11
702186345	34,17,0.000216300,9	9452,17,0.0643	18,17,0.000117330,7.	83,17,0.000361580,9.	42323,17,0.11094
	.274193548,13	93800,0,13	257142857,13	753623188,13	2330,0,13
215380674	121,15,0.000710240,	4001,15,0.0253	387,149,0.002308160	186,15,0.000691700,	15054,15,0.03955
	7.377990431,7	97220,0,7	,6.435860058,7	7.257861635,7	0820,0,7
386470152	993,25,0.006053830,	134421,25,1.05	572,175,0.003517240	2713,25,0.008738190	3814064,25,9.906
	10.744873341,17	5082960,0,17	,7.080357143,17	,11.475497874,17	578320,0,17
107243685	163,17,0.001231620,	10951,17,0.082	417,179,0.002601710	206,17,0.000781180,	51080,17,0.13558
	8.925531915,11	476220,0,11	,6.644897959,11	9.260623229,11	3420,0,11
367580412	2389,27,0.01587235	165164,27,1.37	596,175,0.003634860	5691,27,0.018109770	10083429,27,26.0
	0,11.712006079,17	3487220,0,17	,7.102927290,17	,11.795929241,17	45233820,0,17
620314875	369,20,0.002229810,	32194,20,0.459	382,168,0.002450530	1408,20,0.004719310	216000,20,0.5626
	8.338118022,8	752770,0,8	,6.388807069,8	,8.118487395,8	78790,0,8
715403268	356,20,0.002192340,	37083,20,0.256	522,150,0.003204640	573,20,0.001970820,	269408,20,0.6937
	8.593023256,12	524420,0,12	,6.742734123,12	9.433021807,12	04210,0,12
807461523	1461,27,0.00878628	163614,27,1.11	580,151,0.003566830	2764,27,0.008923140	9608157,27,24.74
	0,11.142619543,21	0630960,0,21	,7.113592233,21	,11.330114135,21	6378860,0,21
820576134	854,26,0.005506190,	145000,26,1.12	458,208,0.002888350	2791,26,0.008965810	4963354,26,12.81
	11.481377372,18	0967660,0,18	,6.909987670,18	,10.976107732,18	7018660,0,18
385701642	730,22,0.004640560,	68791,22,0.540	485,176,0.004132490	2006,22,0.006589930	761900,22,1.9581
	9.600164204,12	515360,0,12	,6.989449004,12	,9.715939448,12	85200,0,12
354176028	257,22,0.001751410,	69185,22,0.555	580,152,0.004851950	1238,22,0.004070480	779904,22,2.0426
	11.321759259,14	601920,0,14	,6.989278752,14	,10.963160446,14	50570,0,14
028541736	414,22,0.002588580,	66051,22,0.612	409,152,0.002607010	1016,22,0.003383380	713444,22,1.8879
	9.852482270,12	514700,0,12	,6.717241379,12	,10.976387249,12	45160,0,12
437061582	181,19,0.001186940, 9.896440129,17	25603,19,0.196 415400,0,17	403,161,0.002480880 ,6.648951049,17		156601,19,0.4171 20350,0,17
213465078	336,20,0.002085740,	30499,20,0.217	636,186,0.003839350	722,20,0.002475270,	197513,20,0.5152
	9.108996540,8	981200,0,8	,7.133752244,8	9.396411093,8	09420,0,8
105462738	707,21,0.004381670,	45472,21,0.361	48,29,0.000444630,5.	2213,21,0.007279130	365116,21,0.9449
	8.577593361,9	885520,0,9	715909091,9	,8.091270894,9	69710,0,9
723154860	1467,24,0.00905749	106698,24,0.82	613,104,0.003641470	2265,24,0.007180450	1905883,24,4.972
	0,11.038823049,14	6176650,0,14	,6.960514233,14	,11.277570591,14	171920,0,14
572640831	1319,25,0.00833914	130566,25,0.96	450,203,0.002838350	3613,25,0.011390690	3411288,25,8.812
	0,10.782807499,13	2969150,0,13	,6.843750000,13	,10.676061008,13	192660,0,13
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15_puzzle_instances(91 resolvidos e 9 não resolvidos):

	astar_15_puzzle
14 13 15 7 11 12 9 5 6 0 2 1 4 8 10 3	14028344,57,15.146497526,27.186899998,41

13 5 4 10 9 12 8 14 2 3 7 1 0 15 11 6	4415279,55,4.212458407,23.394823321,43
14 7 8 2 13 11 10 4 9 12 5 0 3 6 1 15	30003145,59,27.729149380,27.751703100,41
5 12 10 7 15 11 14 0 8 2 1 13 3 4 9 6	5253685,56,7.082921185,26.620789126,42
4 7 14 13 10 3 9 12 11 5 6 15 1 2 8 0	2021382,56,1.106967476,28.153197960,42
14 7 1 9 12 3 6 15 8 11 2 5 10 0 4 13	969356,52,0.510923089,27.416487786,36
2 11 15 5 13 4 6 7 12 8 10 1 9 3 14 0	7170013,52,4.369050519,23.383736205,30
12 11 15 3 8 0 4 2 6 13 9 5 14 1 10 7	2618503,50,1.898846547,24.424522613,32
3 14 9 11 5 4 8 2 13 12 6 7 10 1 15 0	313211,46,0.271005333,21.503714064,32
13 11 8 9 0 15 7 10 4 3 6 14 5 12 2 1	17805045,59,10.999859932,27.734989500,43
5 9 13 14 6 3 7 12 10 8 4 0 15 2 11 1	3525006,57,2.861210064,28.750543947,43
14 1 9 6 4 8 12 5 7 2 3 0 10 11 13 15	32334,45,0.082738111,26.236207746,35
3 6 5 2 10 0 15 14 1 4 13 12 9 8 11 7	831333,46,0.425397191,19.507478939,36
7 6 8 1 11 5 14 10 3 4 9 13 15 2 0 12	26088053,59,18.126284706,28.499027968,41
13 11 4 12 1 8 9 15 6 5 14 2 7 3 10 0	25792756,62,19.096799405,31.454643237,44
1 3 2 5 10 9 15 6 8 14 13 11 12 4 7 0	909219,42,2.299503355,18.651622057,24
15 14 0 4 11 1 6 13 7 5 8 9 3 2 10 12	7,7,7,7
6 0 14 12 1 15 9 10 11 4 7 2 8 3 5 13	1267588,55,4.152380246,27.259432873,43
7 11 8 3 14 0 6 15 1 4 13 9 5 12 2 10	154092,46,0.101688486,22.987149518,36
6 12 11 3 13 7 9 15 2 14 8 10 4 1 5 0	1995813,52,1.065798910,24.572979382,36
12 8 14 6 11 4 7 0 5 1 10 15 3 13 9 2	5668025,54,3.289645526,26.403395498,34
14 3 9 1 15 8 4 5 11 7 10 13 0 2 12 6	13338796,59,8.631032407,28.247415200,41
10 9 3 11 0 13 2 14 5 6 4 7 8 15 1 12	1398857,49,1.278959286,24.277053264,33
7 3 14 13 4 1 10 8 5 12 9 11 2 15 6 0	4691710,54,2.873773970,26.312233807,34
11 4 2 7 1 0 10 15 6 9 14 8 3 13 5 12	6227205,52,3.595406180,24.700271656,32
5 7 3 12 15 13 14 8 0 10 9 6 1 4 2 11	20161235,58,13.434805798,27.585266352,40
14 1 8 15 2 6 0 3 9 12 10 13 4 7 5 11	11278428,53,8.250586784,25.459157070,33
13 14 6 12 4 5 1 0 9 3 10 2 15 11 8 7	909442,52,0.848970507,27.872709694,36
9 8 0 2 15 1 4 14 3 10 7 5 11 13 6 12	3917549,54,2.285731804,26.119066251,38
12 15 2 6 1 14 4 8 5 3 7 0 10 13 9 11	215990,47,0.180093671,24.840168697,35

12 8 15 13 1 0 5 4 6 3 2 11 9 7 14 10	192534,50,0.085533491,28.164809614,38
14 10 9 4 13 6 5 8 2 12 7 0 1 3 11 15	17025056,59,11.217413925,29.273735534,43
14 3 5 15 11 6 13 9 0 10 2 12 4 1 7 8	18535767,60,12.723717676,30.110062220,42
6 11 7 8 13 2 5 4 1 10 3 9 14 0 12 15	2063117,52,2.208614419,25.982463471,36
1 6 12 14 3 2 15 8 4 5 13 9 0 7 11 10	4626661,55,2.591590644,26.974809435,39
12 6 0 4 7 3 15 1 13 9 8 11 2 14 5 10	2309697,52,1.387135228,25.791490696,36
8 1 7 12 11 0 10 5 9 15 6 13 14 2 3 4	20889986,58,14.034871953,27.636038186,40
7 15 8 2 13 6 3 12 11 0 4 10 9 5 1 14	827864,53,1.688304507,28.710055144,41
9 0 4 10 1 14 15 3 12 6 5 7 11 13 8 2	1118025,49,0.682406457,24.280758227,35
11 5 1 14 4 12 10 0 2 7 13 3 9 15 6 8	6540243,54,4.349934985,26.380556654,36
8 13 10 9 11 3 15 6 0 1 2 14 12 5 4 7	5727374,54,3.523838702,26.121908881,36
4 5 7 2 9 14 12 13 0 3 6 11 8 1 15 10	48447,42,0.159907016,23.300038513,30
11 15 14 13 1 9 10 4 3 6 2 12 7 5 8 0	7332466,64,4.056159279,33.052825986,48
12 9 0 6 8 3 5 14 2 4 11 7 10 1 15 13	2731989,50,1.672824395,24.607500763,32
3 14 9 7 12 15 0 4 1 8 5 6 11 10 2 13	539196,51,0.328794047,27.316122324,39
8 4 6 1 14 12 2 15 13 10 9 5 3 7 0 11	1430455,49,0.769865485,22.917919500,35
6 10 1 14 15 8 3 5 13 0 2 7 4 9 11 12	179689,47,0.110743018,25.475309125,35
8 11 4 6 7 3 10 9 2 12 15 13 0 1 5 14	119535,49,0.060144115,25.168520808,39
10 0 2 4 5 1 6 12 11 13 9 7 15 3 14 8	7,7,7,7
12 5 13 11 2 10 0 9 7 8 4 3 14 6 15 1	4399444,53,5.389449751,25.099391556,39
10 2 8 4 15 0 1 14 11 13 3 6 9 7 5 12	3031922,56,1.686261128,28.074824893,44
10 8 0 12 3 7 6 2 1 14 4 11 15 13 9 5	11641228,56,7.340103410,26.803444668,38
14 9 12 13 15 4 8 10 0 2 1 7 3 11 5 6	38607523,64,28.351341589,30.428446052,50
12 11 0 8 10 2 13 15 5 4 7 3 6 9 14 1	7221615,56,7.765572559,27.820720322,40
13 8 14 3 9 1 0 7 15 5 4 10 12 2 6 11	152123,41,0.275460112,20.696139214,29
3 15 2 5 11 6 4 7 12 9 1 0 13 14 10 8	7,7,7,7
5 11 6 9 4 13 12 0 8 2 15 10 1 7 3 14	484048,50,3.800729508,26.117384742,36
5 0 15 8 4 6 1 14 10 11 3 9 7 12 2 13	506538,51,0.271726784,25.545293672,37
15 14 6 7 10 1 0 11 12 8 4 9 2 5 13 3	7,7,7,7
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	1
11 14 13 1 2 3 12 4 15 7 9 5 10 6 8 0	
6 13 3 2 11 9 5 10 1 7 12 14 8 4 0 15	508957,45,3.253268022,21.727099095,31
4 6 12 0 14 2 9 13 11 8 3 15 7 10 1 5	1828847,57,0.961352043,29.084569116,43
8 10 9 11 14 1 7 15 13 4 0 12 6 2 5 3	21862510,56,15.098298591,25.547554173,40
5 2 14 0 7 8 6 3 11 12 13 15 4 10 9 1	5622335,51,4.584968315,23.618298023,31
7 8 3 2 10 12 4 6 11 13 5 15 0 1 9 14	920623,47,0.549316450,22.622818579,31
11 6 14 12 3 5 1 15 8 0 10 13 9 7 4 2	77777
7 1 2 4 8 3 6 11 10 15 0 5 14 12 13 9	8430894,50,8.357040985,23.921400655,28
7 3 1 13 12 10 5 2 8 0 6 11 14 15 4 9	5471060,51,3.334964449,25.117996142,31
6 0 5 15 1 14 4 9 2 13 8 10 11 12 7 3	4579005,53,2.675190400,25.342839888,37
15 1 3 12 4 0 6 5 2 8 14 9 13 10 7 11	8179227,52,4.873294957,24.664403262,30
5 7 0 11 12 1 9 10 15 6 2 3 8 4 13 14	557862,44,0.524471864,20.630121935,30
12 15 11 10 4 5 14 0 13 7 1 2 9 8 3 6	34437004,56,25.392588122,25.394338195,38
6 14 10 5 15 8 7 1 3 4 2 0 12 9 11 13	188717,49,2.925514988,23.873066342,37
14 13 4 11 15 8 6 9 0 7 3 1 2 10 12 5	1373939,56,0.738810601,28.771617648,46
14 4 0 10 6 5 1 3 9 2 13 15 12 7 8 11	3440513,48,1.961967094,22.060243222,30
15 10 8 3 0 6 9 5 1 14 13 11 7 2 12 4	7622602,57,4.316702757,27.729741041,41
0 13 2 4 12 14 6 9 15 1 10 3 11 5 8 7	2184110,54,1.377100851,27.597979875,34
3 14 13 6 4 15 8 9 5 12 10 0 2 7 1 11	619299,53,0.330551684,27.380696856,41
0 1 9 7 11 13 5 3 14 12 4 2 8 6 10 15	68633,42,0.076729003,21.781102812,28
11 0 15 8 13 12 3 5 10 1 4 6 14 9 7 2	3951356,57,2.147463188,26.913582603,43
13 0 9 12 11 6 3 5 15 8 1 10 4 14 2 7	744209,53,0.440950536,28.051742599,39
14 10 2 1 13 9 8 11 7 3 6 12 15 5 4 0	-,-,-,-
12 3 9 1 4 5 10 2 6 11 15 0 14 7 13 8	1900358,49,4.393936120,24.127774626,31
15 8 10 7 0 12 14 1 5 9 6 3 13 11 4 2	10972804,55,6.753401542,26.658956691,37
4 7 13 10 1 2 9 6 12 8 14 5 3 0 11 15	158355,44,0.445412593,20.888586322,32
6 0 5 10 11 12 9 2 1 7 4 3 14 8 13 15	195222,45,0.099640091,22.290462753,35
9 5 11 10 13 0 2 1 8 6 14 12 4 7 3 15	4681483,52,2.643273409,25.962040067,34
15 2 12 11 14 13 9 5 1 3 8 7 0 10 6 4	7,7,7,7

11 1 7 4 10 13 3 8 9 14 0 15 6 5 2 12	3559259,54,5.501645738,26.461863489,38
5 4 7 1 11 12 14 15 10 13 8 6 2 0 9 3	820923,50,0.503062764,26.079187488,36
9 7 5 2 14 15 12 10 11 3 6 1 8 13 0 4	18150875,57,11.801331091,26.873360856,41
3 2 7 9 0 15 12 4 6 11 5 14 8 13 10 1	-,-,-,-
13 9 14 6 12 8 1 2 3 4 0 7 5 10 11 15	438960,46,3.373360219,20.965216714,34
5 7 11 8 0 14 9 13 10 12 3 15 6 1 4 2	276325,53,0.137981605,27.766560116,45
4 3 6 13 7 15 9 0 10 5 8 11 2 12 1 14	751475,50,0.399737948,25.063399547,34
1 7 15 14 2 6 4 9 12 11 13 3 0 8 5 10	1263033,49,0.688816825,22.922221345,35
9 14 5 7 8 15 1 2 10 4 13 6 12 0 11 3	191601,44,0.112213676,21.267765068,32
0 11 3 12 5 2 1 9 8 10 14 15 7 4 13 6	9499694,54,5.761415314,25.127288869,34
7 15 4 0 10 9 2 5 12 11 13 6 1 3 14 8	5342754,57,3.241079379,28.762484231,39
11 4 0 8 6 10 5 13 12 7 14 3 1 2 9 15	4484857,54,2.713224245,25.170227912,38

Problemas com a saída (-,-,-,-) não foram resolvidos, que foram 9.